

Primordial Non-Gaussianity

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We now have a Standard Model of Cosmology!

- Bad news for theorists:

We now know the basic global properties of the Universe. The model correctly predicts (almost) all observed phenomena.

- Good news for theorists:

We don't understand most of the constituents of the Universe.

We don't know how it began

How to make a Universe: the observer's recipe



How to make a Universe: the theorist's view



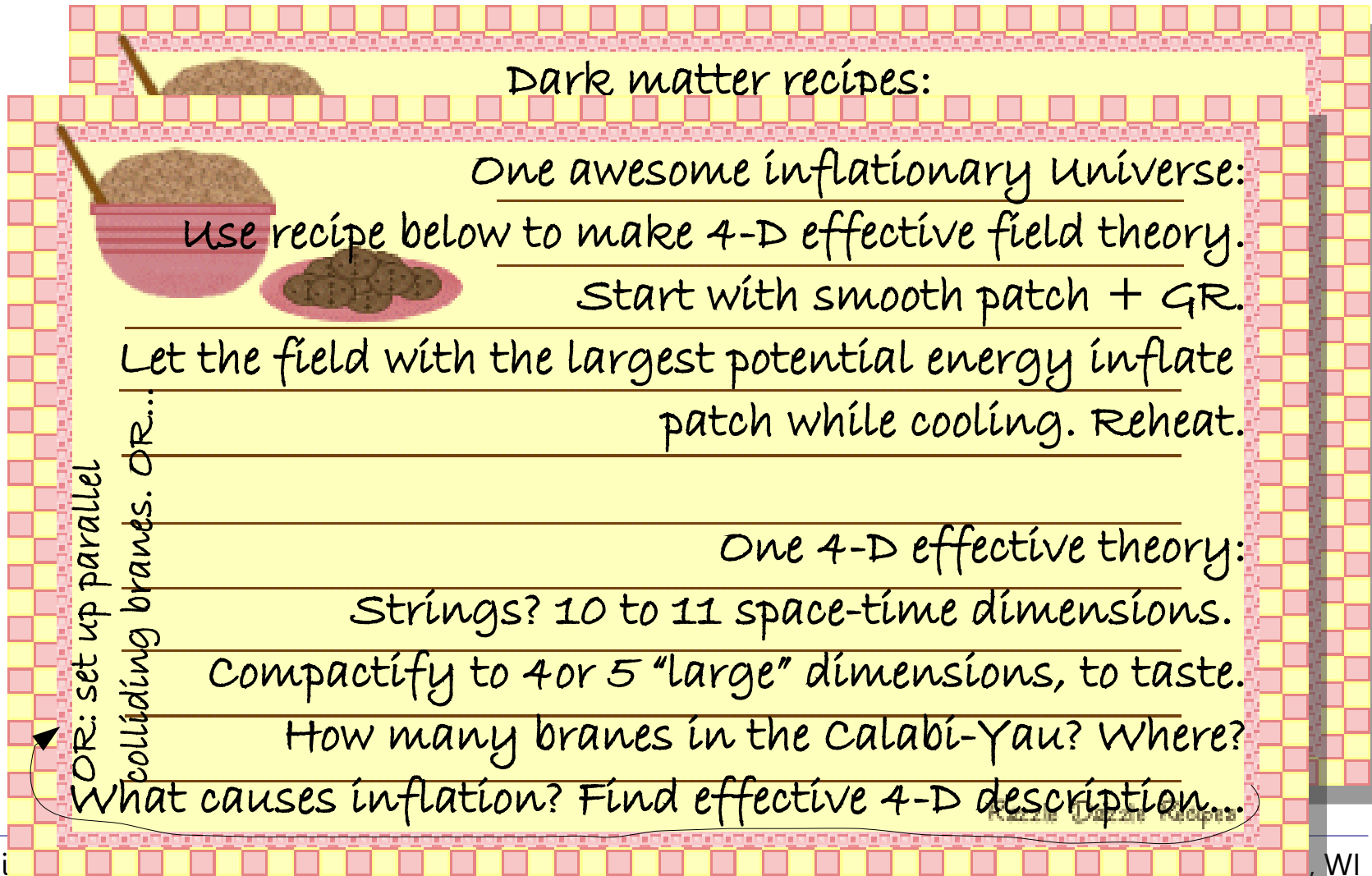
One awesome inflationary universe:
use recipe below to make 4-D effective field theory.
Start with smooth patch + GR.
Let the field with the largest potential energy inflate patch while cooling. Reheat.

One 4-D effective theory:
Strings? 10 to 11 space-time dimensions.
Compactify to 4 or 5 "large" dimensions, to taste.
How many branes in the Calabi-Yau? Where?
What causes inflation? Find effective 4-D description...

OR: set up parallel colliding branes. OR...

Benjami, WI

How to make a Universe: the theorist's view



Dark matter recipes:

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How to make a Universe: the theorist's view



Dark energy recipes:



Dark matter recipes:



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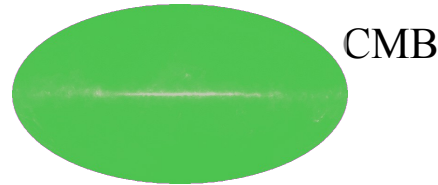
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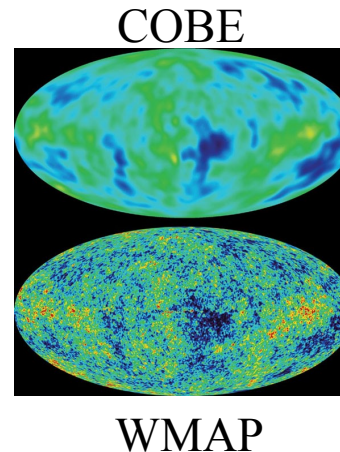
The Physics of the Beginning

- Why Homogeneity and Isotropy?



- Why Flatness?

- Whence
seed perturbations?



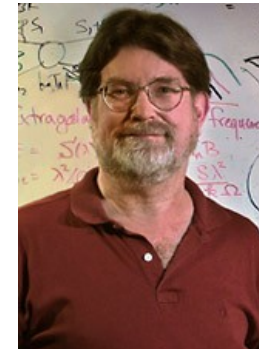
1978 Nobel Prize
in Physics



Robert Wilson and Arno Penzias



2006 Nobel Prize
in Physics

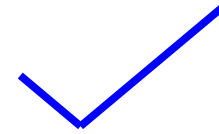


George Smoot John C. Mather

COSMO08 – Madison, WI

Predictions of Standard Inflation

(i) Flat, homogeneous and isotropic

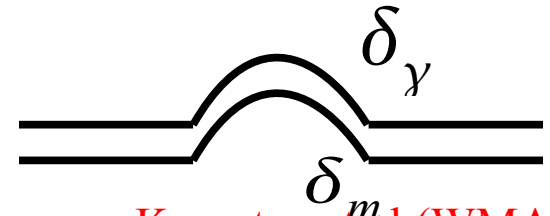
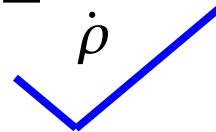


Komatsu et al (WMAP5)
+ e.g. HST: **~2%**

(ii) Seed perturbations:
canonical models predict

- Nearly adiabatic:

$$\frac{\delta \rho_i}{\dot{\rho}_i} = \frac{\delta \rho}{\dot{\rho}}$$



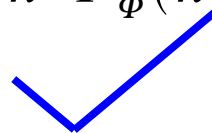
Komatsu et al (WMAP5):
~10%

- Close to Gaussian

$$\langle \Phi(\vec{k}) \Phi(\vec{k}') \rangle = P_\Phi(k) \delta^3(\vec{k} - \vec{k}')$$

- Nearly Scale Invariant

$$k^3 P_\Phi(k) = A k^{n_s - 1}$$



Komatsu et al (WMAP5):
a few percent.

CMB tests of inflation: Current Status

Test

Std. Inflation Ekpyrosis Obs

• Is observable universe flat?	• Yes.	• Built in.	• Yes, to ~2%
• Do the fluctuations have the predicted correlations (nearly scale independent)?	• Yes.	• Yes.	• Yes, to few %
• Are fluctuation adiabatic?	• Yes.	• ?	• Yes, to ~10%
• primordial gravitational waves	• Maybe	• No	• ?
• Are fluctuations nearly Gaussian?	• Yes: predicted to be true at 0.001%!	• Much higher deviations from Gaussianity	• Hints of deviation from Gaussianity from WMAP data!

Yadav & Wandelt 2007

Komatsu et al. (WMAP5) 2008

Primordial perturbations and Gaussianity

- Slow-roll- $\rightarrow$ shallow potential- $\rightarrow$ nearly free field; has Gaussian quantum perturbations (field modes in S.H.O. potential). Theorem for single field.
- If multi-field, can have isocurvature perturbations that convert into non-Gaussian curvature perturbations outside horizon.
- Non-standard kinetic term: can inflate in spite of steep potential - $\rightarrow$ non-Gaussianity
- Standard choice of vacuum – can get flattened triangle contributions if not Bunch-Davies.

Non-Gaussianity – a new frontier

- In addition to the information to be gained from 2-point correlations, non-Gaussianity opens a new window on the Physics of the Beginning.
- What is the program?
 - Reliable theoretical prediction of non-Gaussianity from models of the early Universe
 - Characterization of non-Gaussian confusion effects
 - Development of efficient and practical statistical methods to draw inferences about non-Gaussianity from the data.

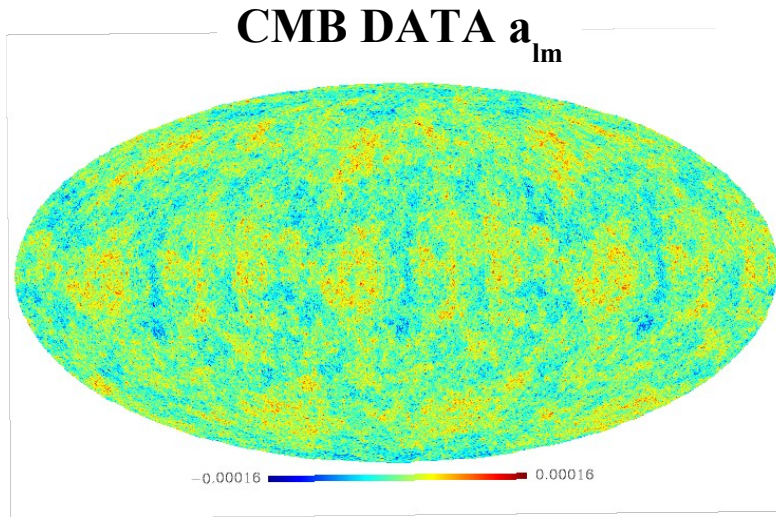
Our push at the frontier

- How to search for primordial non-Gaussianity
- How to search for f_{NL}
- What we find
- How to interpret our result
- Future prospects

How to search for (weak) primordial non-Gaussianity in 3 easy steps

- Reconstruct curvature perturbation from data
- Test for non-Gaussian features
- Compute error bars using Gaussian Monte Carlo realizations of the data

Reconstructed Primordial Perturbations

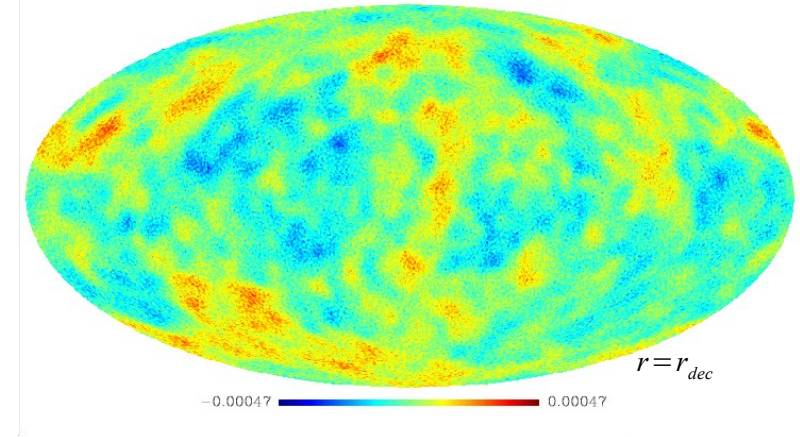


$$\Phi_{lm} = O_l a_{lm}$$

SW limit

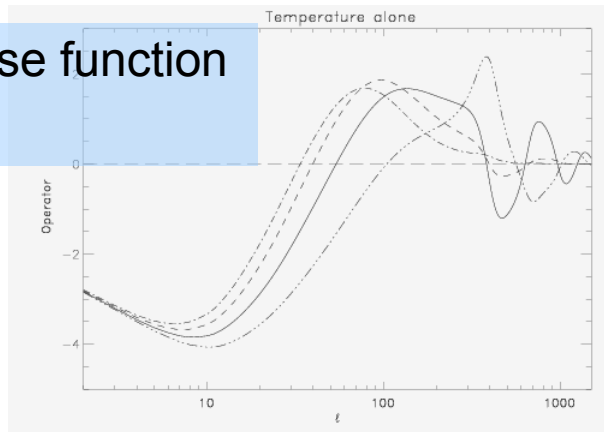
$$\frac{\delta \phi}{\phi} = -3 \frac{\delta T}{T}$$

Reconstructed Primordial perturbations with T alone

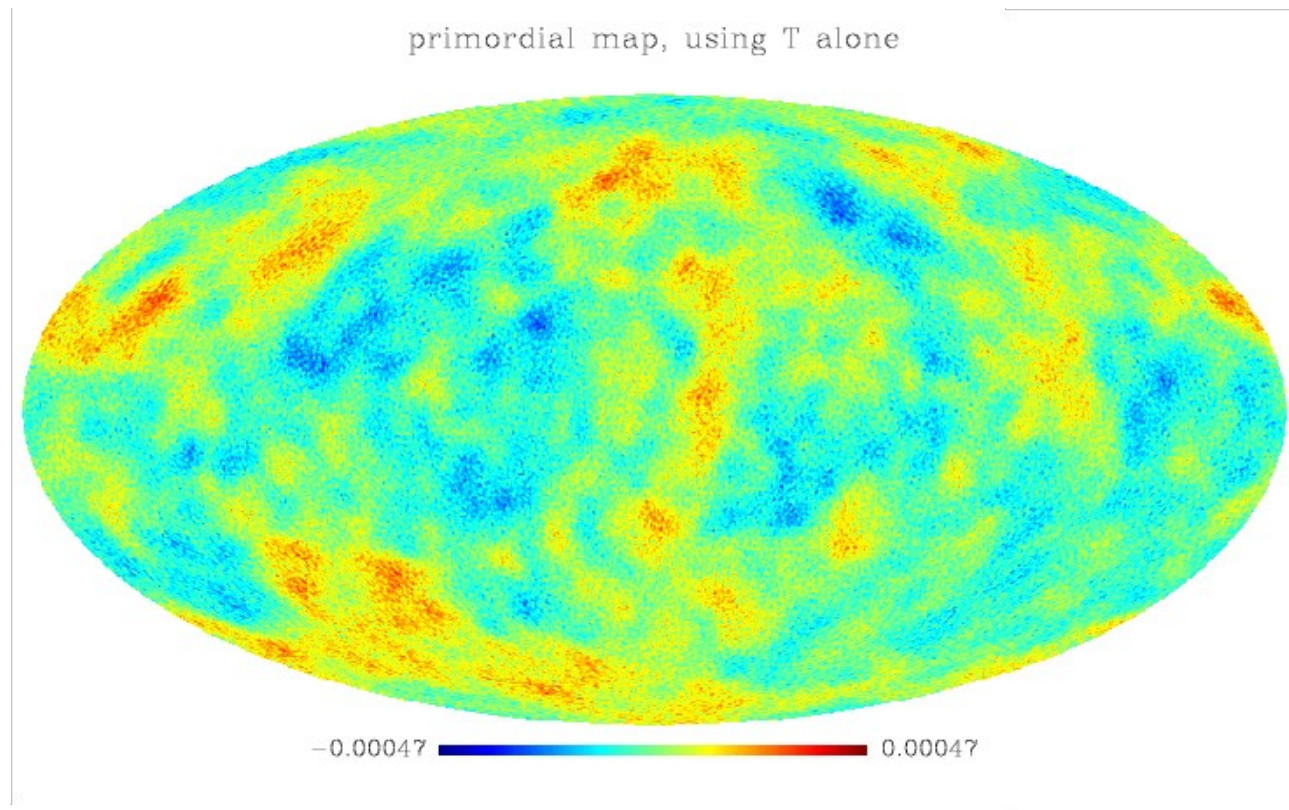


Response function

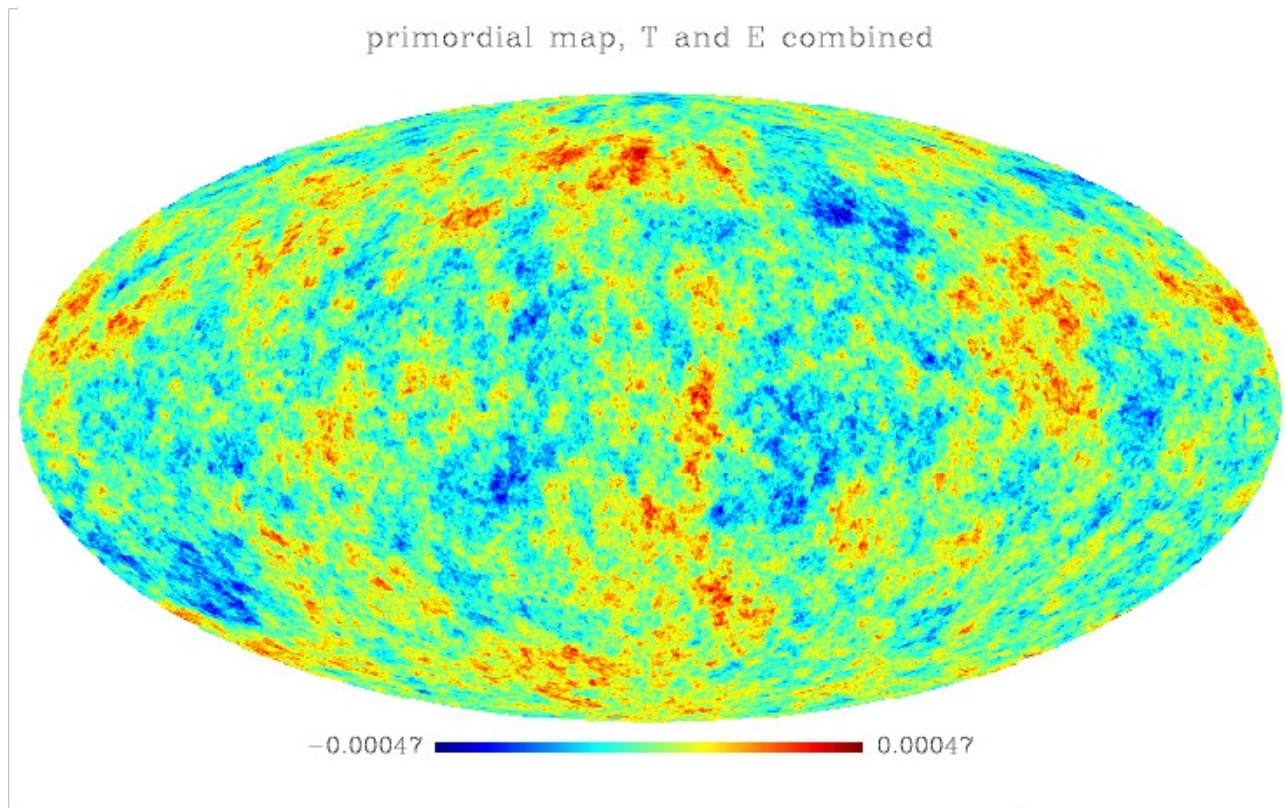
$$O_l = \beta / C_l$$



$$\beta_\ell^i(r) = \frac{2b_\ell^i}{\pi} \int k^2 dk P_\phi(k) g_\ell^i(k) j_\ell(kr).$$



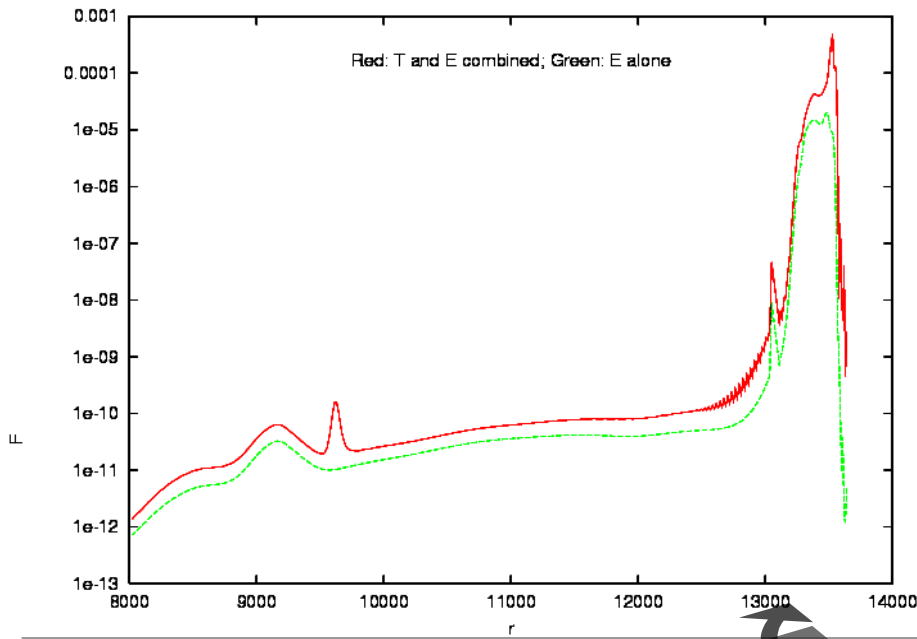
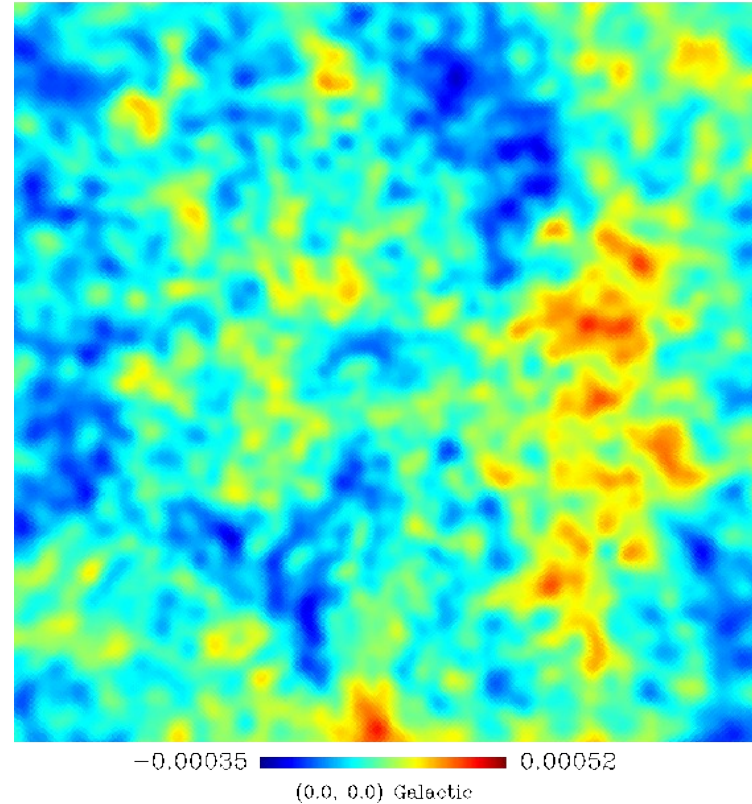
Yadav, and Wandelt, PRD (2005)



Yadav, and Wandelt, PRD (2005)

Reconstructed perturbations at different radii

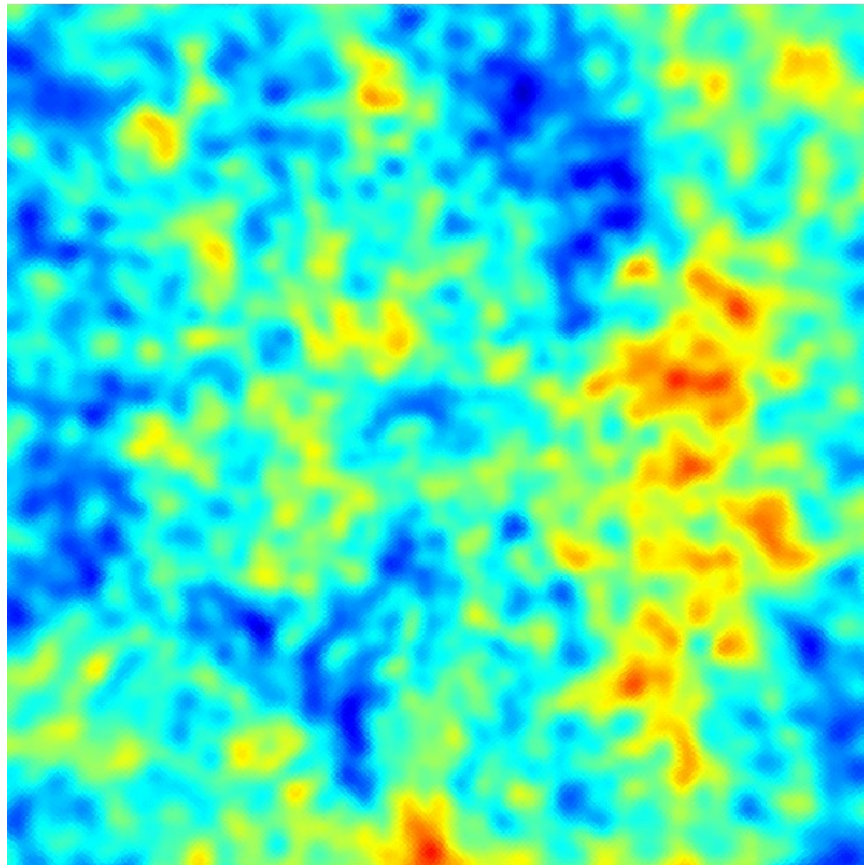
Curvature fluctuations



Yadav, and Wandelt, PRD (2005)

Tomographic reconstruction of inflationary scalar curvature

Curvature fluctuations



-0.00035 0.00052
(0.0, 0.0) Galactic

We construct filters that invert linear radiative transport.

Generates a single scalar that contains all the information from T&E.

Anyone intending to test primordial non-Gaussianity (and anisotropy!) in T and/or E data should do so using curvature perturbations obtained with our filters.

Yadav and Wandelt 2006

f_{NL} – a specific parameterization of non-Gaussianity

$$\Phi(x) = \Phi_G(x) + f_{NL} \Phi_G^2(x)$$

Salopek & Bond 1990
Komatsu & Spergel 2001

Characterizes the amplitude of non-Gaussianity

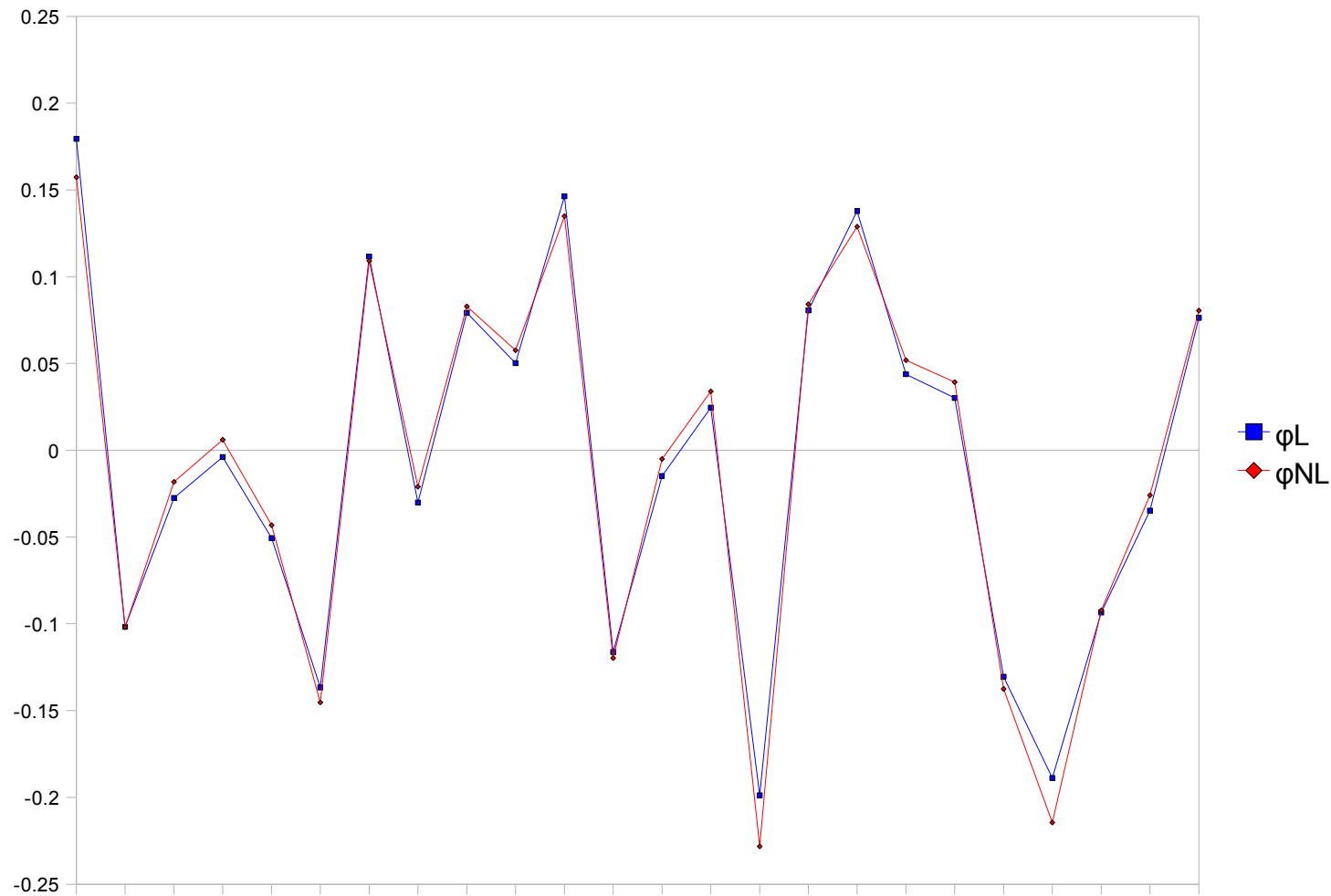
- This non-Gaussianity creates a bispectrum signature (as well as higher order moments)
 $\langle \Phi(k_1) \Phi(k_2) \Phi(k_3) \rangle = 2(2\pi)^3 f_{NL} \delta(k_1 + k_2 + k_3) P(k_1) P(k_2),$

where $(2\pi)^3 \delta(k_1 + k_2) P(k_1) = \langle \Phi(k_1) \Phi(k_2) \rangle$

- This translates into a bispectrum signature in the CMB through

$$a_{lm} = 4\pi(-i)^l \int \frac{d^3\mathbf{k}}{(2\pi)^3} \Phi(\mathbf{k}) g_{Tl}(k) Y_{lm}^*(\hat{\mathbf{k}})$$

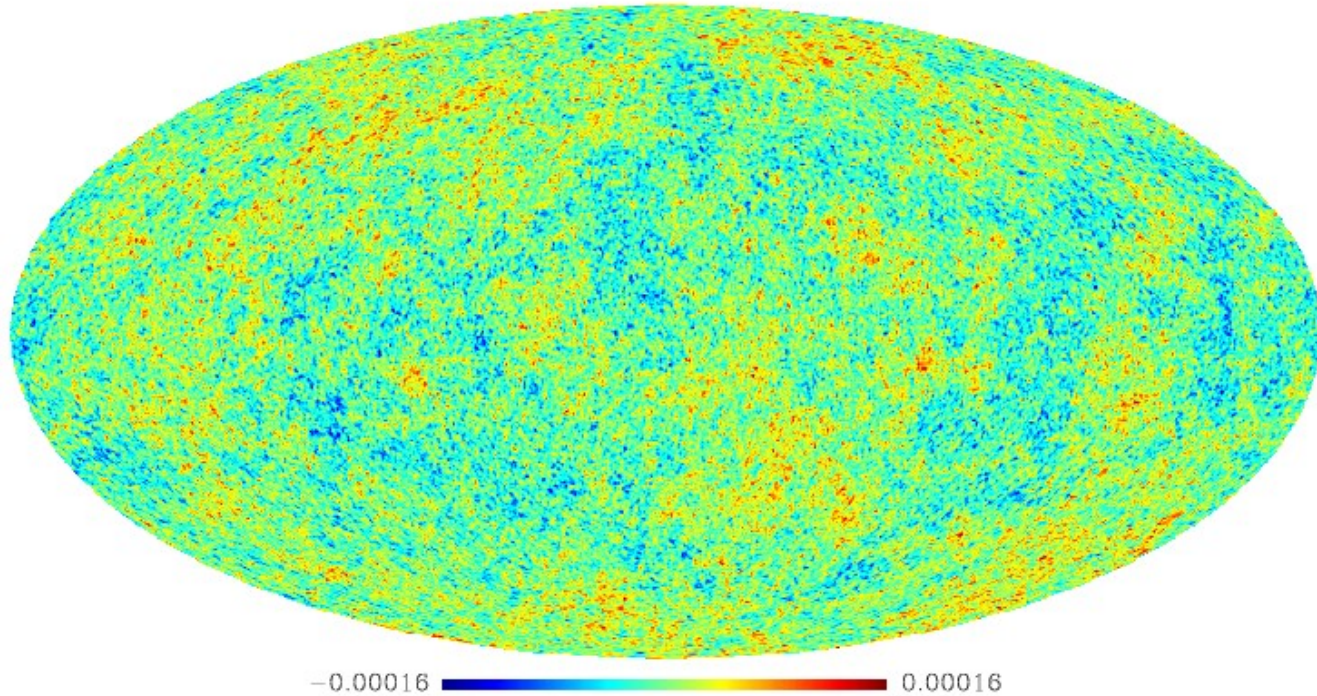
Statistics of local non-Gaussianity in the CMB



- Local non-Gaussianity smoothes hot spots and creates more structure in cold spots.

$$f_{NL} = 0$$

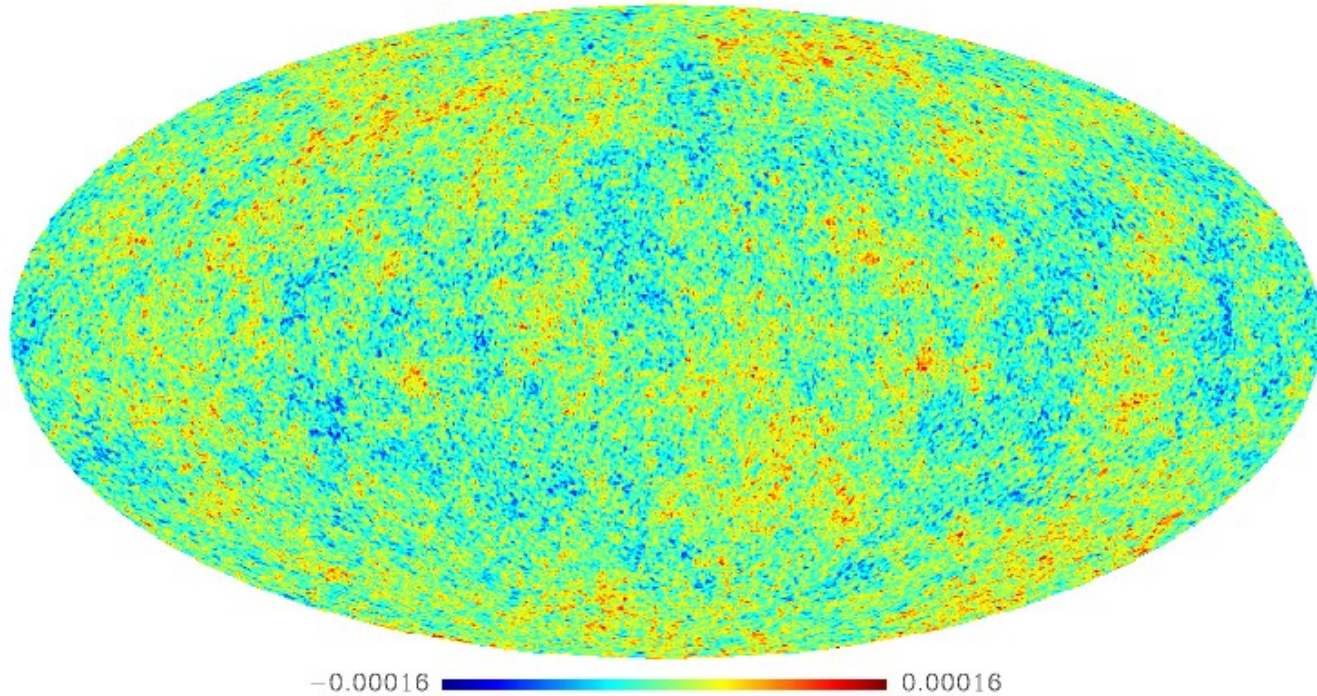
Temperature ($f_{NL} = 0$)



Liguori, Yadav, Hansen, Komatsu, Matarrese, Wandelt 2007

$$f_{NL} = 10^1$$

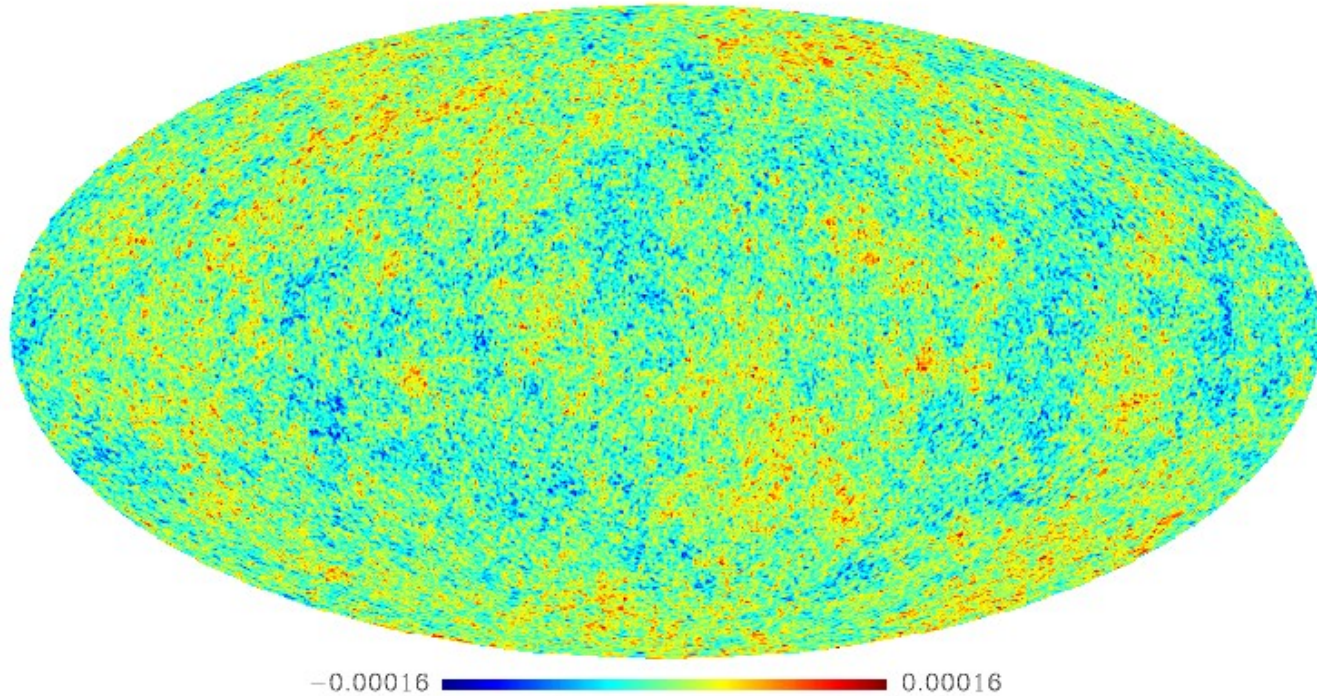
Temperature ($f_{NL} = 10$)



Liguori, Yadav, Hansen, Komatsu, Matarrese, Wandelt 2007

$$f_{NL} = 10^2$$

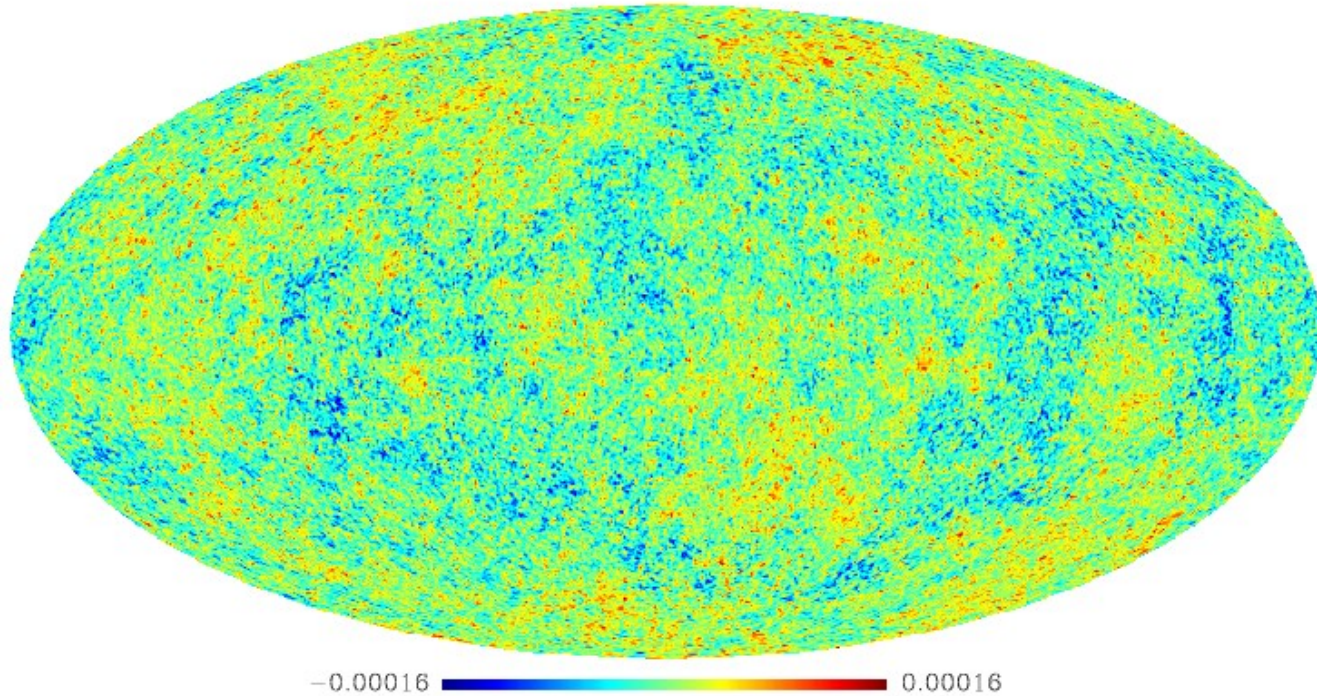
Temperature ($f_{NL} = 10^2$)



Liguori, Yadav, Hansen, Komatsu, Matarrese, Wandelt 2007

$$f_{NL} = 10^3$$

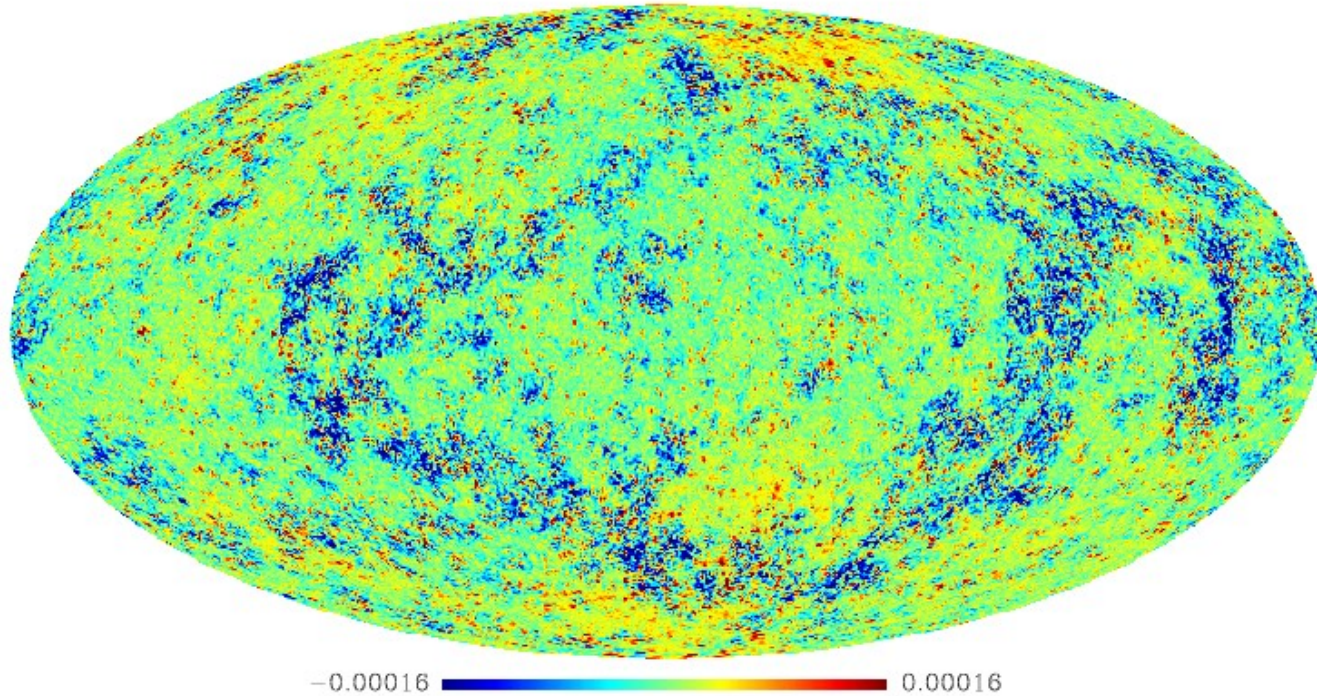
Temperature ($f_{NL} = 10^3$)



Liguori, Yadav, Hansen, Komatsu, Matarrese, Wandelt 2007

$$f_{NL} = 10^4$$

Temperature ($f_{NL} = 10^4$)



Liguori, Yadav, Hansen, Komatsu, Matarrese, Wandelt 2007

Why use the bispectrum?

$$B_{\text{non-Gaussian}} = 0 + f_{\text{NL}} b^2$$

$$T_{\text{non-Gaussian}} = T_{\text{Gaussian}} + f_{\text{NL}}^2 \delta T$$

For weak non-Gaussianity any even moment has a much larger contribution from Gaussian perturbations. This makes measuring the non-Gaussian component difficult.

Babich (2005): bispectrum contains nearly all the information about f_{NL} . Kogo&Komatsu: Trispectrum contains complementary information

Unfortunately evaluating all $B_{l_1 l_2 l_3}$ is too expensive.

Fast, bispectrum based estimator of local f_{NL}

Cubic Statistic:

$$\hat{S}_{\text{prim}} = \frac{1}{f_{\text{sky}}} \int r^2 dr \int d^2 \hat{n} B(\hat{n}, r) B(\hat{n}, r) A(\hat{n}, r)$$

Komatsu, Spergel and Wandelt 2005

$$B(\hat{n}, r) \equiv \sum_{ip} \sum_{lm} (C^{-1})^{ip} a_{\ell m}^i \beta_{\ell}^p(r) Y_{\ell m}(\hat{n})$$

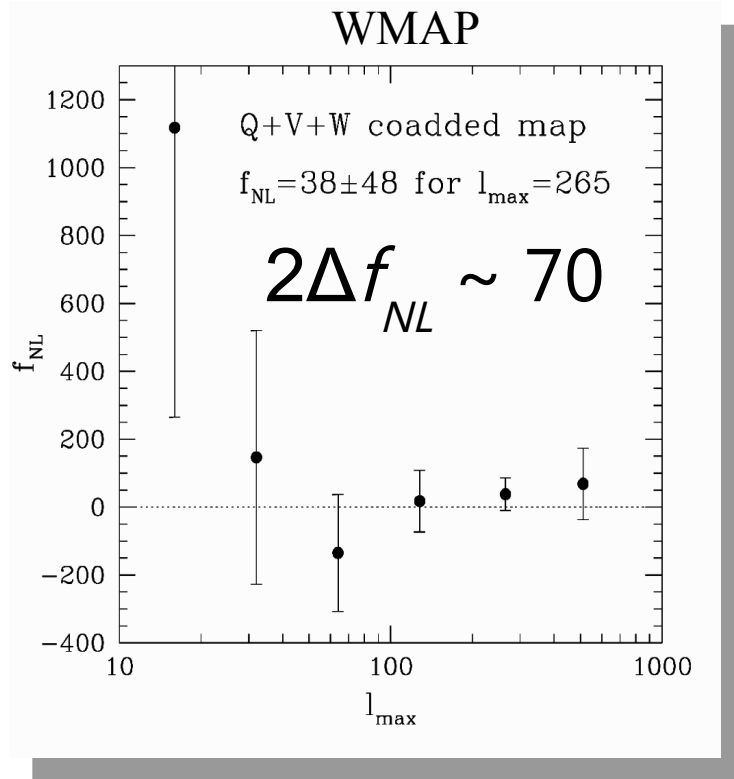
B(r) is a map of reconstructed primordial perturbations

$$A(\hat{n}, r) \equiv \sum_{ip} \sum_{lm} (C^{-1})^{ip} a_{\ell m}^i \alpha_{\ell}^p(r) Y_{\ell m}(\hat{n})$$

A(r) picks out relevant configurations of the bispectrum

Above statistics combine all configurations of bispectrum such that it most sensitive to “local” primordial non-Gaussianity i.e f_{NL}

Status before December 2007



We are far from $\Delta f_{NL} \sim 1$ but can already start putting constraints on some models like DBI inflation, ghost inflation etc.

$$-58 < f_{NL} < 137 \text{ (95\%)}$$

WMAP 1yr

$$-54 < f_{NL} < 114 \text{ (95\%)}$$

WMAP 3yr

$$-36 < f_{NL} < 100 \text{ (95\%)}$$

**Creminelli et. al. 2006
using WMAP3 data**

Non-Gaussianity from Inflation

$f_{NL} \sim 0.05$ canonical inflation (single field, couple of derivatives) (Maldacena 2003, Acquaviva et al 2003)

$f_{NL} \sim 0.1--100$ higher order derivatives

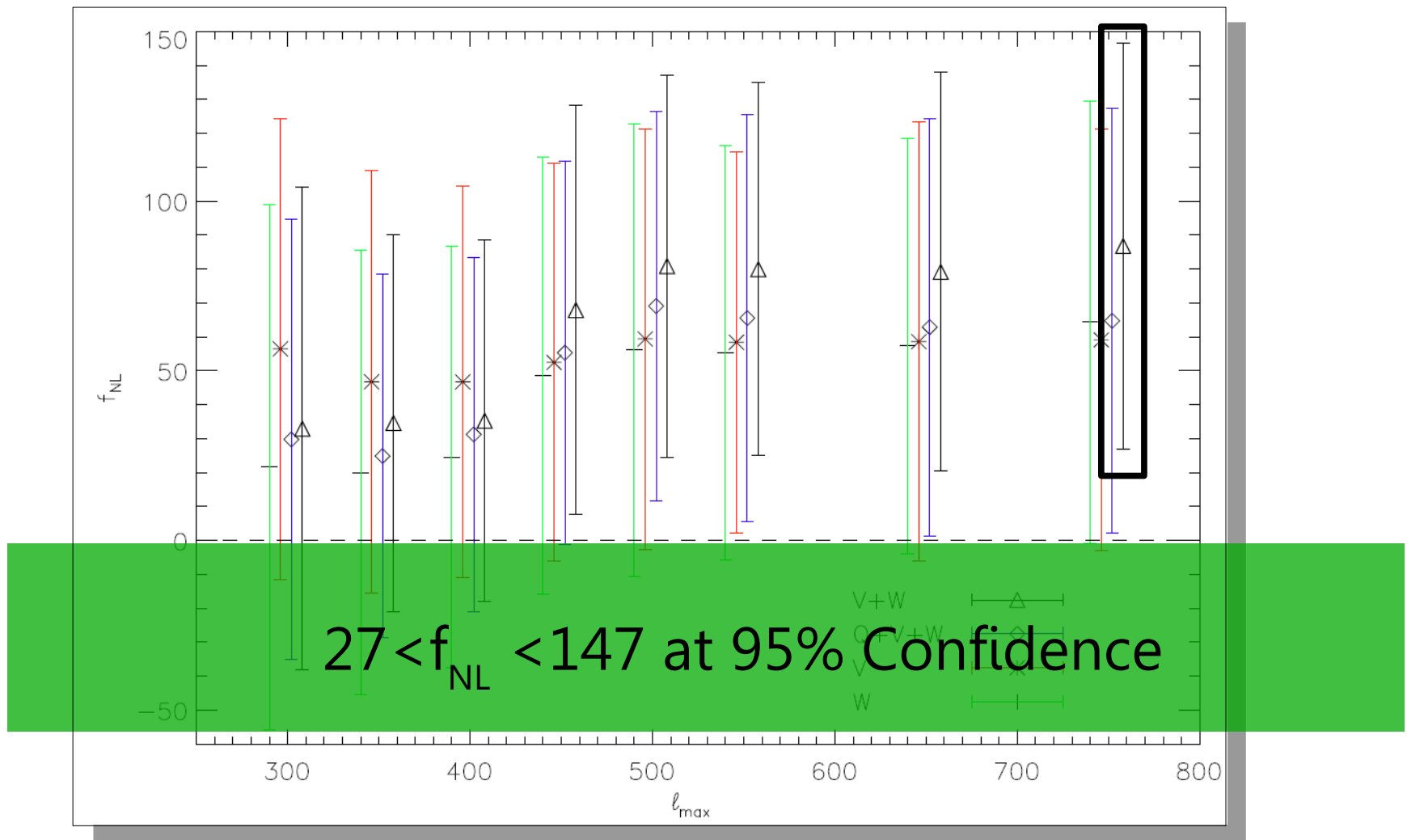
DBI inflation (Alishahiha, Silverstein and Tong 2004)

UV cutoff (Creminelli and Cosmol, 2003)

$f_{NL} > 10$ curvaton models (Lyth, Ungarelli and Wands, 2003)

$f_{NL} \sim 100$ ghost inflation (Arkani-Hamed et al., Cosmol, 2004)

Our result:



Questions you might ask (and we did)

Might this result be due to...

- Known instrument systematic? **NO**
- Known Foregrounds? **NO**
- Secondary anisotropies? ($f_{\text{NL}} \sim 5$)
- Just rediscovery of other non-Gaussian signals? **NO**
- Noise fluctuation? **Could be, $P \sim 0.01$.**

Detailed analysis shows that standard inflation ($f_{\text{NL}} \sim 0$) is disfavored by the data.

Noise fluctuation?

- Possible. Noise couples to any bispectrum form.
- It's a 2.5-2.8 sigma result. $P \leq 0.01$

2.5 sigma when after conservative increase of error bar to model uncertainty in residual systematics

[The most aggressive interpretation of the WMAP3 data would be a 3.3 sigma effect (correcting for negative foreground bias and using best fit WMAP parameters and $l_{\text{max}}=750$)]

Summary of Yadav & Wandelt 2008

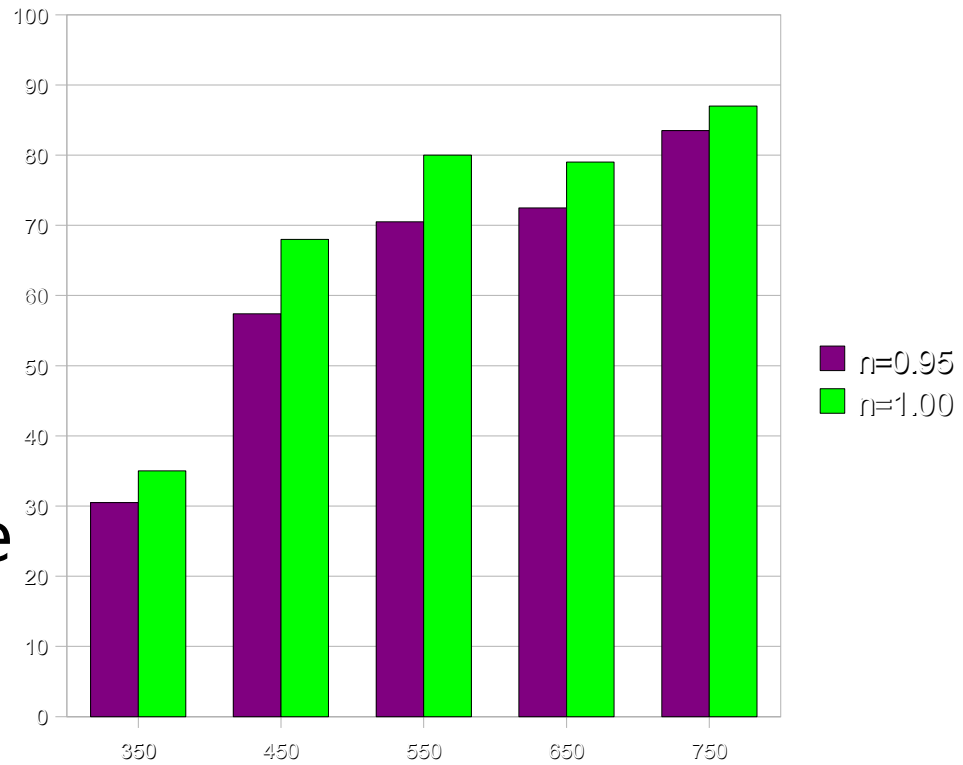
- $\Delta f_{NL} \sim 30$ for all of WMAP 3 using YKWLHM07 and WMAP best fit parameters (statistical)
- First bispectrum-based analysis of the full WMAP3 data
- First significant departure of f_{NL} from 0 at $>99\%$ C.L.
- Estimators tested against Gaussian and non-Gaussian simulations with and without inhomogeneous noise
- If any bias, it is likely to be negative.
- 2.5-2.8 sigma, depending on choices and assumptions

WMAP 5-year analysis

- Komatsu et al. 2008
- Differences to our analysis:
 - mask shape that enhances the statistical error compared to the 3-yr mask;
 - stop at $l_{\text{max}}=500$
 - Different background cosmology
 - subtract generous estimate of point source bias.
- Quoted result: $f_{\text{NL}}^{\text{local}} = 51 \pm 60$ (95%)
- Significance: 1.7 sigma
- 2.3 sigma for most similar case to our analysis

Sensitivity to assumed cosmology

- The filters depend weakly on assumed cosmology. We used $n=1$.
- Choosing $n=0.95$ reduces the error bars by 10%, and reduces the central values between 5% and 15%.
- At $l_{\max}=750$, significance *increases* to just over 3 sigma; at lower $l_{\max}$ significance *decreases a little*.



WMAP 5 year constraint on f^{equil}

$$-151 < f_{\text{NL}}^{\text{equil}} < 253; \quad \Delta f_{\text{NL}}^{\text{equil}} = 201$$

- Of interest for DBI inflation, ghost condensation

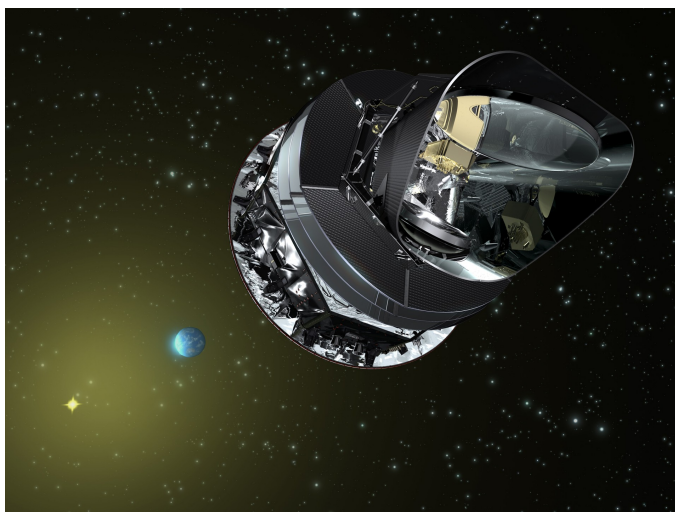
(for reference: Planck should get $\Delta f_{\text{NL}}^{\text{equil}} \sim 35$)

The future

- Planck is a major joint ESA/NASA mission to **L2**.
- Principal scientific goal:
 - to make definitive all-sky maps of CMB temperature anisotropy down to 5' resolution.
- Two instruments:
 - Low Frequency Instrument (PI: Reno Mandolesi)
 - High Frequency Instrument (PI: Jean-Loup Puget)
- Temperature measurement at 9 frequencies
 - 30, 44, 70, 100, 143, 217, 353, 545, 857 GHz
- Polarization measurement at 7 frequencies
 - 30, 44, 70, 100, 143, 217, 353 GHz
- **Detailed Planck Science Case in the “Blue Book.” Google it.**



- Planck will launch in months, not years!
 - Current launch date January – February 2009.
- Dual launch with Herschel on an Ariane 5 rocket
- Then cruise to L2



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COSMO08 – Madison, WI



Schedule

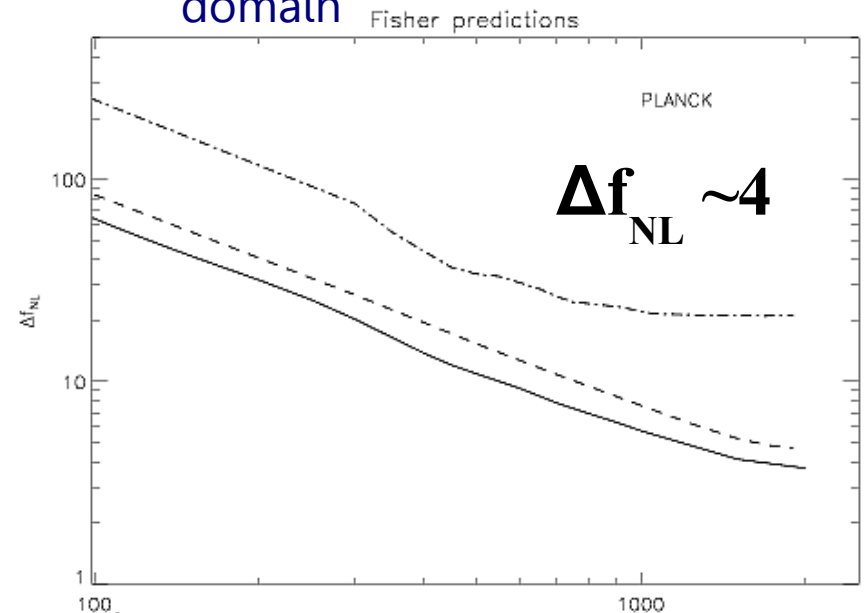
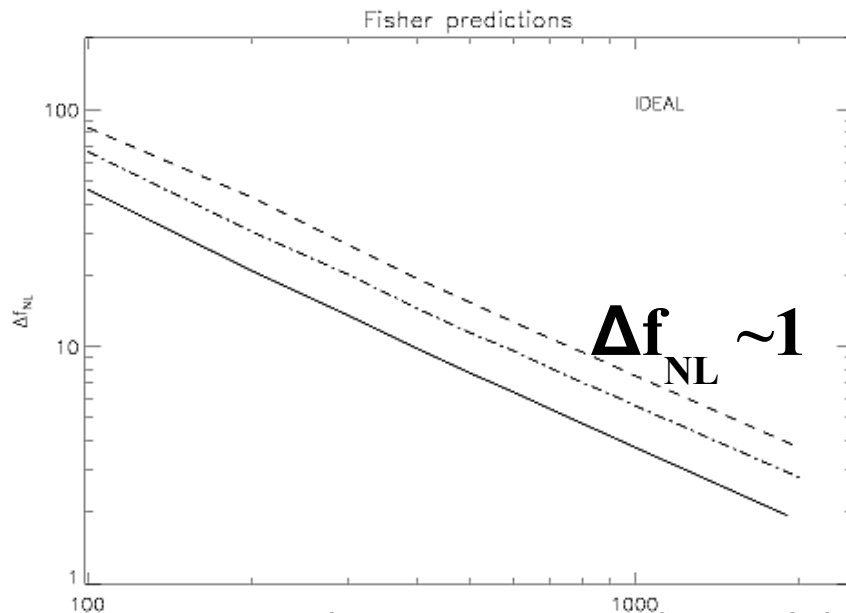


- Launch
 - ~February 2009?
- Cruise and checkout
 - ~3 months
- Two sky surveys
 - +12 months = L + 15
- Release of Early Release Compact Source Catalog
 - Based on first sky survey
 - L + 19 (= September 2010?)
- Two more sky surveys (assuming mission extension approved by ESA)
 - + 12 months = L + 27 (= May 2011?)
- Public release of 1-year data, first set of papers
 - L + 3 months + 3 years (= May 2012?)
- Public release of 2-year data, etc, TBD.



Planck's promise for Non-Gaussianity

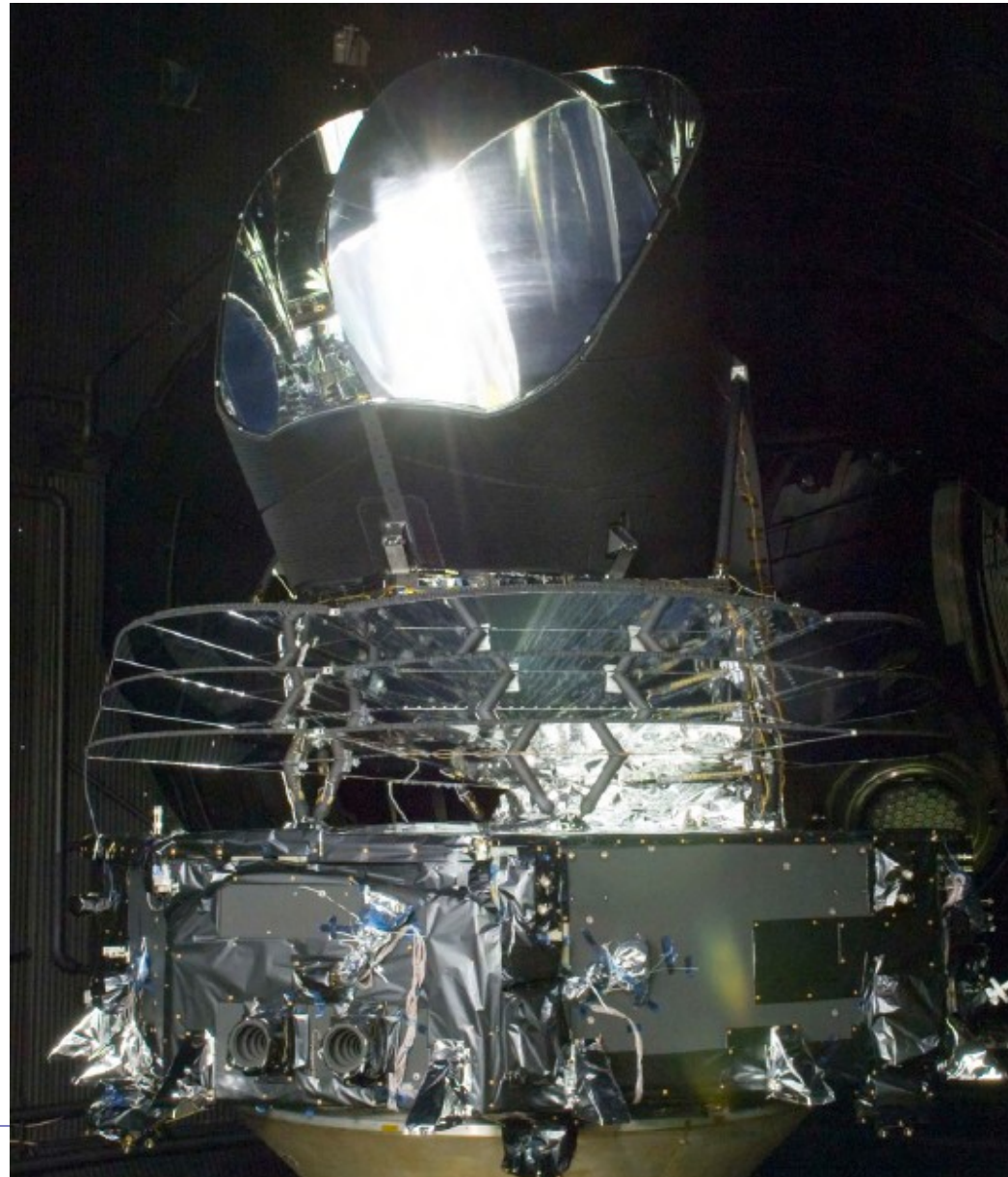
- Many modes
 - large sky coverage
 - high resolution
- Frequency coverage
 - foreground removal
- Polarization
 - complementary to T
 - adds a great deal of information
- Multiple sky coverages
 - control of systematics in time-domain



Yadav, Komatsu and Wandelt, astro-ph/0701921, ApJ (2007)

The hope of doing NG with Planck

- One of the main outcomes of Yadav and Wandelt 2008:
 - Search for primordial NG using bispectrum templates is *much more robust* than was previously realized.
- Temperature and Polarization are *complementary* and can give *independent and combined* constraints.
- The radiation transfer functions give the bispectrum of primordial non-Gaussianity a *very different signature* from late time secondary effects, foregrounds, or non-Gaussian systematics.
- Expect that this robustness will make studying non-Gaussianity with Planck *possible* but not *easy*.



Non-Gaussianity and Planck

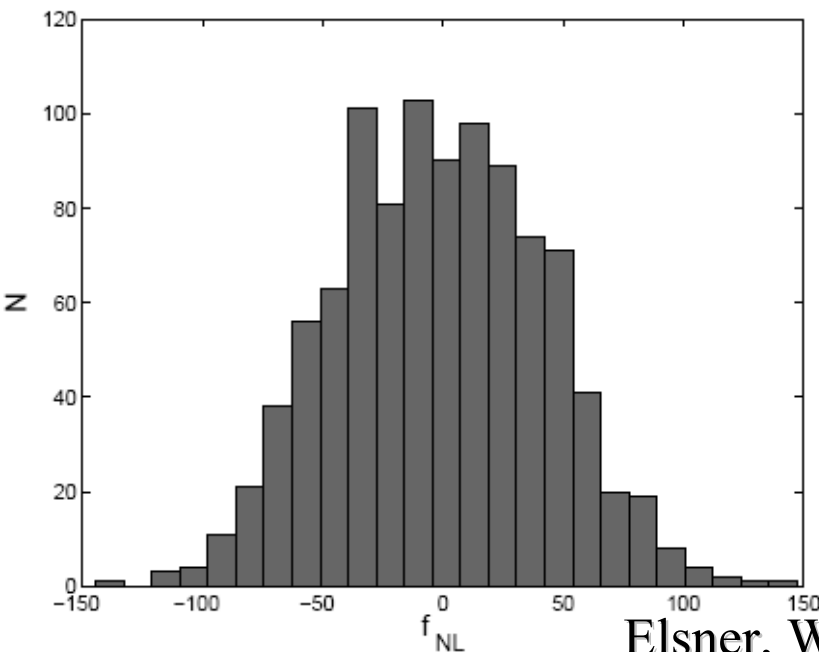
- Non-Gaussianity with Planck will be a new window on the early Universe, complementary to the wealth of information in the two-point function.
- Different early Universe models have distinct predictions for the type and amount of non-Gaussianity expected.
- Ekpyrotic/Cyclic models generically predict non-Gaussianity at detectable levels for Planck (Leners&Steinhardt 2008)
- The search for non-Gaussianity is complementary to the search for primordial gravitational waves
 - Primordial B-modes are the “smoking gun” of inflation
 - Finding primordial non-Gaussianity would rule out all single-field models of slow-roll inflation
- Planck will improve WMAP non-Gaussianity error bars by nearly an order of magnitude

The challenge(s) of constraining NG with Planck

- Higher signal-to-noise requires understanding systematics at a much better level than WMAP
- Secondary anisotropies at Planck signal/noise
 - ISW-lensing bispectrum
 - SZ-lensing bispectrum
 - point sources
 - all triplets of second order effects...
- Foregrounds
 - Diffuse Galactic foregrounds
 - Unresolved Galactic and extra-Galactic point sources
- Instrument systematics
- Optimality of estimators
 - Fast estimators are better for smooth masks (have demonstrated near-optimality)
 - Planck's observing strategy

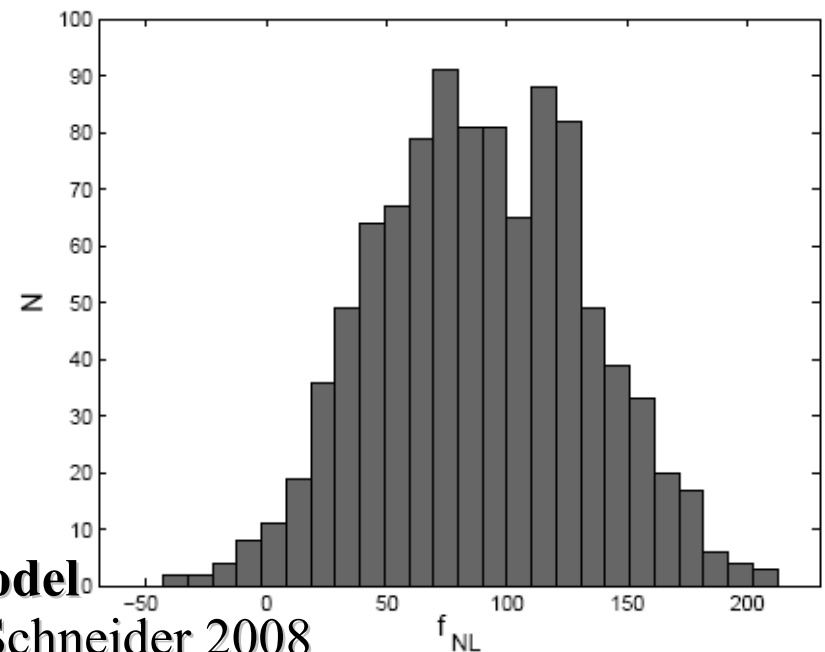
Next generation f_{NL} statistics: Fully Bayesian non-Gaussianity analysis

- Instead of going via the bispectrum, build full statistical model of the data, including non-Gaussianity, and a detailed model of the observations and systematics
- Returns the full $P(f_{\text{NL}}|\text{data})$



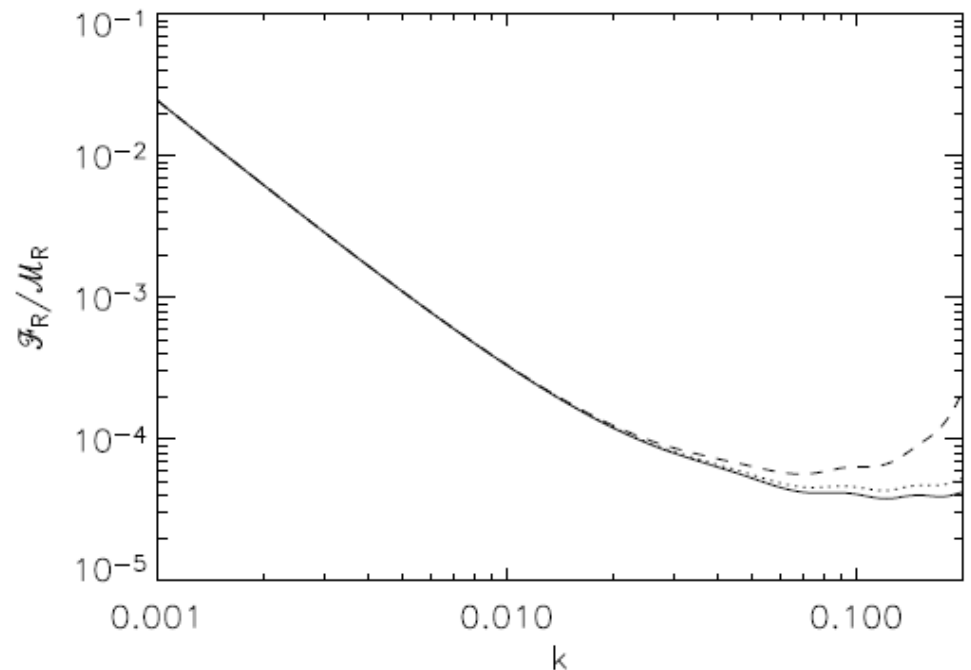
Toy model

Elsner, Wandelt, Schneider 2008



f_{NL} from large scale structure

- Halo mass function: Verde, Matarrese, Jimenez (2000); LoVerde, Miller, Shandera & Verde (2007)
- Halo correlations: Dalal et al. (2007) and Verde & Matarrese (2008) find a universal, scale dependent bias on *large* scales.
- Afshordi (2008):
 $f_{NL} = 240 \pm 120$ from CMB/LSS X-correlations
Ho et al 2008
- Sloszar et al 2008:
 $-29(-85) < f_{NL} < +70(+90)$
at 95% (99.7%)
- Ultimately, $\Delta f_{NL} \sim 5$?



NG status summary

- Yadav&Wandelt (2008) and Komatsu et al (2008) see 2.5-2.8 sigma and 1.7-2.3 sigma hints of local NG in the WMAP 3-year and 5-year data, respectively.
- Tightest LSS constraints consistent with CMB constraints (Sloszar et al 2008)
- Further analysis of the WMAP 5 year data continues

Conclusions

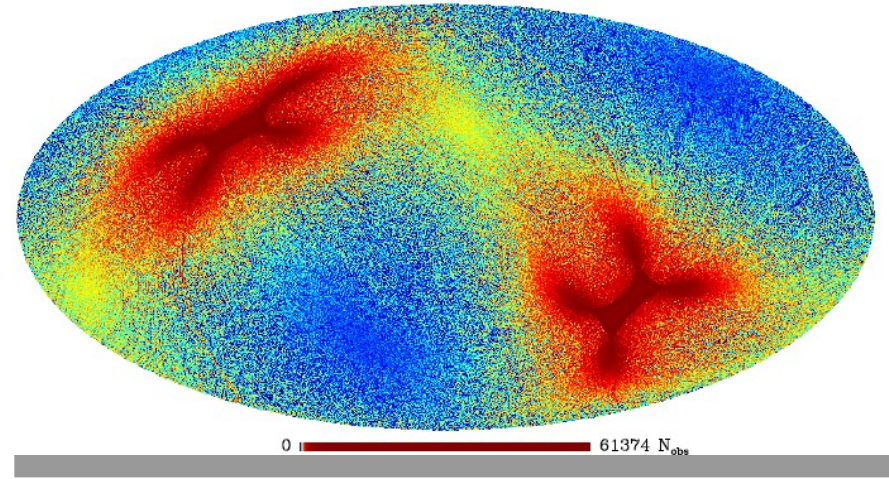
- Non-Gaussianity is a powerful probe of the physics of the beginning
- In combination with power spectrum very powerful test of inflation and its alternatives
- Currently the *highest precision* test of inflation
 - Non-Gaussianity is a $\sim 0.1\%$ test
 - flatness in second place $\sim 1.5\%$
- A way to distinguish between classes of models that give similar predictions for the two-point correlations
- Already starting to rule out significant portions of parameter space, for inflation as well as cyclic/ekpyrotic/new ekpyrotic models.
- WMAP 8 and Planck are on the way.
- A new, exciting and fast-moving frontier

f_{NL} phenomenology from the bispectrum

- Komatsu & Spergel 2001 – CMB bispectrum from f_{NL}
- Komatsu, Wandelt, Spergel, Banday, Gorski 2001 – f_{NL} from COBE
- Komatsu Spergel & Wandelt 2003 – fast f_{NL} estimator
- Komatsu et al (WMAP team) 2003 – WMAP1 analysis using KSW
- Babich and Zaldarriaga 2004 – temperature + polarization
- Creminelli, Nicolis, Senatore, Tegmark, Zaldarriaga 2006 – introduce linear term to improve KSW estimator
- Spergel et al (WMAP team) 2006 – WMAP3 analysis using KSW
- Creminelli, Senatore, Tegmark, Zaldarriaga 2006 – apply cubic + linear term to WMAP3 data
- Yadav & Wandelt 2005 – tomography of the curvature perturbations
- Yadav Komatsu & Wandelt 2007 – KSW generalized to T+P
- Liguori, Yadav, Hansen, Komatsu, Matarrese, Wandelt 2007 – calibrate YKW estimator against non-Gaussian simulations
- Yadav, Komatsu, Wandelt, Liguori, Hansen, Matarrese 2007 – Creminelli et al. corrected and generalized to T+P
- Yadav & Wandelt 2007 – application of YKWLHM07 to WMAP3
- Komatsu et al 2008 – application of YKWLHM07 to WMAP5

Anisotropic sky coverage

- The KSW and YKWLHM estimators are optimal only for uniform sky coverage and noise distribution. Anisotropic noise distribution couples different l and produces excess variance.



- For non-uniform noise the addition of a linear term reduces the variance of the estimator $\hat{S}_{prim}^{linear} = \frac{-3}{f_{sky}} \int r^2 dr \int d^2 \hat{n} \{B(\hat{n}, r) S_{AB}(\hat{n}, r) + S_{BB}(\hat{n}, r) A(\hat{n}, r)\}$ (Creminelli et al. 2005)

- We (Yadav, Komatsu, Wandelt, et al. arxiv:0711.4933) generalized this estimator to include polarization; and discovered and corrected an error in the linear term.

$$A(\hat{n}, r) \equiv \sum_{ip} \sum_{lm} (C^{-1})^{ip} a_{\ell m}^i \alpha_{\ell}^p(r) Y_{\ell m}(\hat{n}).$$

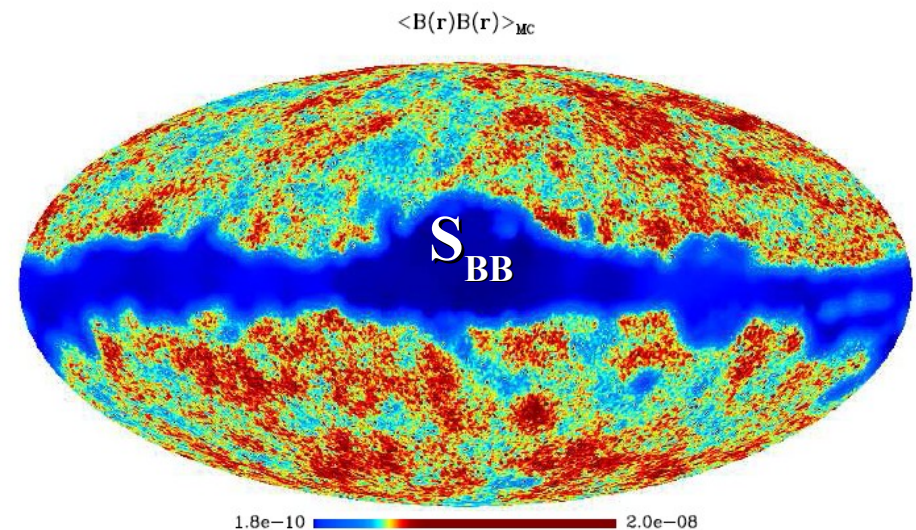
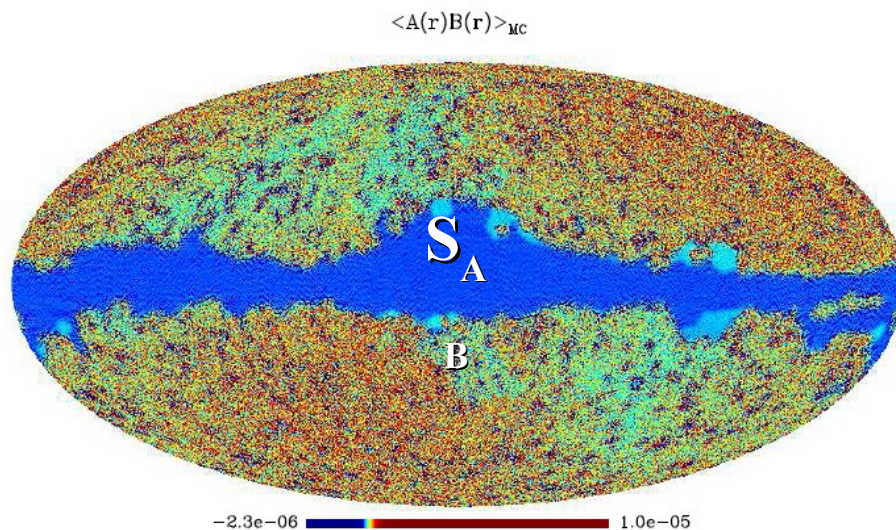
$$B(\hat{n}, r) \equiv \sum_{ip} \sum_{lm} (C^{-1})^{ip} a_{\ell m}^i \beta_{\ell}^p(r) Y_{\ell m}(\hat{n}).$$

Anisotropic noise

- Linear weight maps make linear term maximally anticorrelated with the cubic term to reduce its variance due to anisotropic noise

$$S_{AB}(\hat{n}, r) \equiv \sum_{ipqr} \sum_{\ell_1 m_1 \ell_2 m_2} \beta_{\ell_1}^i(r) (C^{-1})^{ip}_{\ell_1} Y_{\ell_1 m_1}(\hat{n}) \alpha_{\ell_2}^j(r) (C^{-1})^{jq}_{\ell_2} Y_{\ell_2 m_2}(\hat{n}) \langle a_{\ell_1 m_1}^p a_{\ell_2 m_2}^q \rangle$$

$$S_{BB}(\hat{n}, r) \equiv \sum_{ipqr} \sum_{\ell_1 m_1 \ell_2 m_2} \beta_{\ell_1}^i(r) (C^{-1})^{ip}_{\ell_1} Y_{\ell_1 m_1}(\hat{n}) \beta_{\ell_2}^j(r) (C^{-1})^{jq}_{\ell_2} Y_{\ell_2 m_2}(\hat{n}) \langle a_{\ell_1 m_1}^p a_{\ell_2 m_2}^q \rangle$$



Instrument systematics?

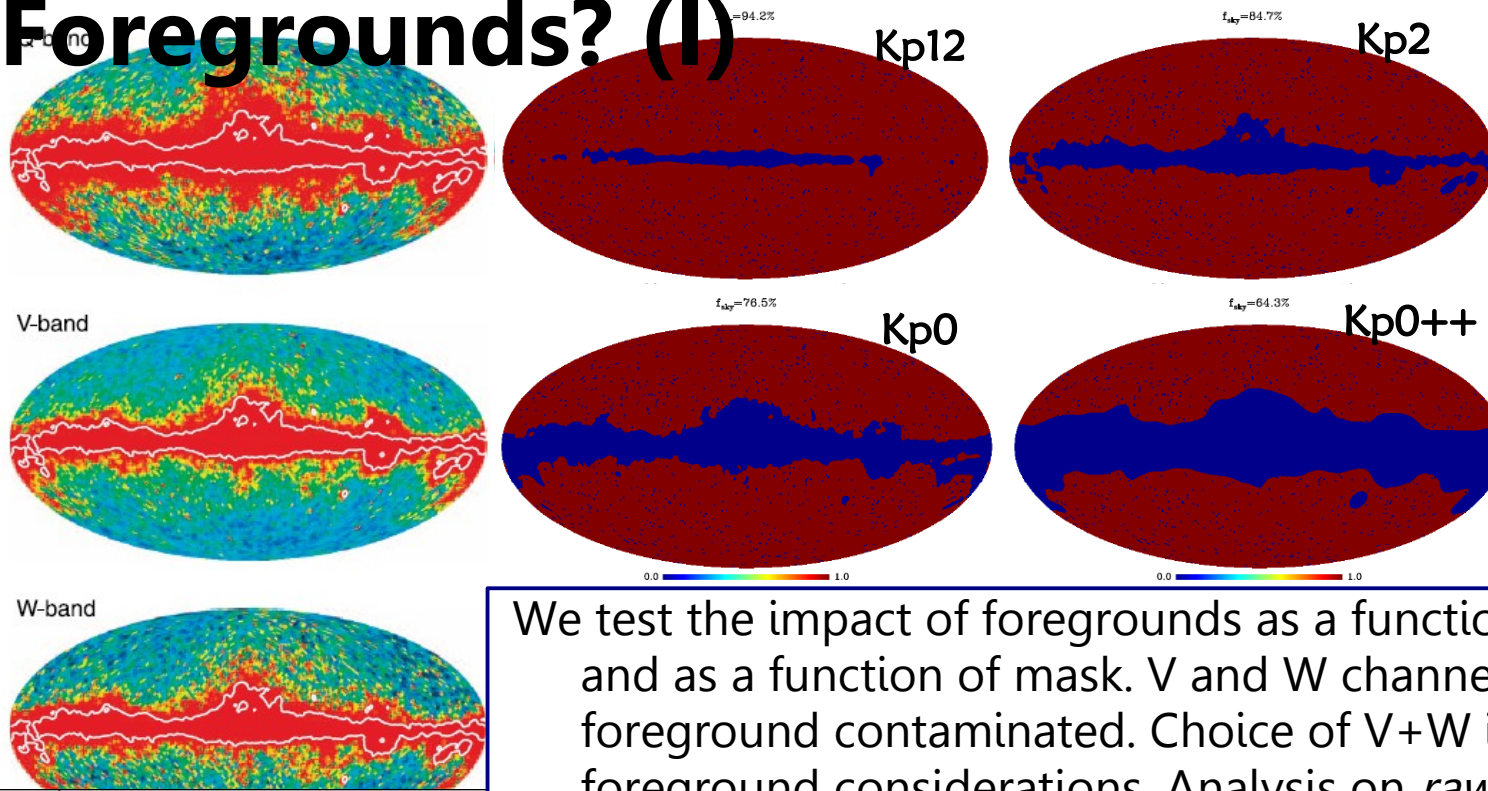
I) Beam asymmetries

- If the CMB is Gaussian, no asymmetry of the main beam can produce non-vanishing bispectrum.
- If there are large side-lobes that spread foreground around the sky they will produce large scale features – unlikely to affect the high l regime. Further, we do not see evidence for frequency dependence.

Instrument systematics? II: WMAP Noise

- Noise correlations (striping)
 - As long as noise is Gaussian, **no** noise correlations will produce a bispectrum.
- Non-Gaussian noise?
Analyzed differences of WMAP yearly maps
 - year1-year2 $f_{\text{NL}}=1.1$ (+/- ~60 at 95% C.L.)
 - year2-year3 $f_{\text{NL}}=1.8$
 - year1-year3 $f_{\text{NL}}=-3.4$
- So to explain our results an instrumental systematic has to be 1) non-Gaussian, 2) the same in individual years and 3) mimic the specific bispectrum signature of f_{NL} .

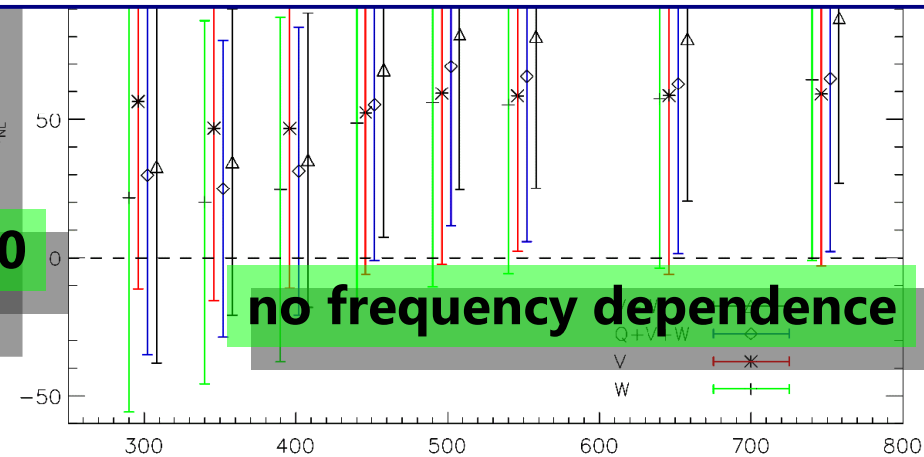
Foregrounds? (I)



We test the impact of foregrounds as a function of frequency and as a function of mask. V and W channels are the least foreground contaminated. Choice of V+W is driven by foreground considerations. Analysis on *raw* maps to avoid FG oversubtraction.

$\ell_{\max}$	$f_{\text{sky}} = 94.2\%$ Kp12	$f_{\text{sky}} = 84.7\%$ Kp2	$f_{\text{sky}} = 76.5\%$ Kp0	$f_{\text{sky}} = 64.3\%$ Kp0++
350	-3145.22	-26.68	34.62	19.24
450	-1425.06	-15.63	67.94	64.69
550	-1509.92	-13.09	79.99	83.53
650	-1559.91	-22.43	86.81	86.52
750	-1575.11	-22.81		

stable beyond kp0



no frequency dependence

Foregrounds? (II)

- WMAP raw maps vs WMAP cleaned maps
 - Foreground subtracted maps do not show negative f_{NL} behavior
 - Same level of f_{NL} , uniformly higher for FG subtracted maps
 - We quote the result from raw maps to be conservative and because the cleaned maps could contain *oversubtracted* foregrounds giving a positive bias.

Foregrounds (III)

- Simulations of Gaussian CMB + Foregrounds + WMAP Noise
 - negative for smaller masks
 - goes to zero by the time you reach Kp0 mask
 - is consistent with zero for masks greater than kp0

$\ell_{\max}$	VW				Q	QVW			
	Kp12	Kp2	Kp0	Kp0+	Kp0	Kp12	Kp2	Kp0	Kp0+
350	-1290	-27	35	19	1	-2384	-75	25	8
450	-1425	-16	68	65	-6	-2792	-80	55	65
550	-1510	-13	80	84	-11	-3136	-94	66	80
650	-1560	-22	79	81	-14	-3307	-94	63	77
750	-1575	-23	87	87	-20	-3368	-108	65	78
750*	$-1105 \pm_{19}^{19}$	$-42 \pm_5^5$	$-6 \pm_4^4$	$-0.3 \pm_4^4$				$-13 \pm_5^5$	$1 \pm_6^6$

Secondary Anisotropies?

- Point sources, including SZ
 - Orthogonal overlap with primordial bispectrum. Bias of $|f_{\text{NL}}| < 1$. SZ and point sources have opposite signs. **X**
- Serra and Cooray (arxiv:0801.3276)
 - dominant secondary confusion level to WMAP bispectrum arises from
 - ISW-lensing bispectrum (positive bias)
 - SZ-lensing bispectrum (negative bias)
 - **If $f_{\text{NL}} = 20$** effective bias around 10%. **Negligible** for $f_{\text{NL}} > 20$, because effects add in quadrature. **X**

Re-discovery of another non-Gaussian signal?

- Larson/Wandelt (hot and cold spots not hot or cold enough):
 - at smaller angular scales
 - symmetric-> no odd correlation. Probably noise model. **X**
- The Cold Spot (Vielva et al. 2004) is localized in the map and covers a particular range in scale. **X**
Preliminary result: **$f_{NL}=94 \pm 60$ (95% C.L.)**
- Large Scale anomaly? Can check by removing large scale signal. Preliminary result: **X**
Removing $l < 21$, $f_{NL}=135 \pm 96$ (95% C.L.)

WMAP 5 year continued...

- A ***very preliminary*** result by K. Smith et al., obtained at the Perimeter Workshop in March:

$$f_{\text{NL}}^{\text{local}} = 21 \pm 44 \text{ (95\%)}$$

- Note that this uses the exact same data as the WMAP 5, so the difference is entirely due to different weighting in the estimator.
 - Smaller error bar due to optimal weighting
 - This remains to be checked and the differences remain to be understood – no news since then.