How to Generate the Cosmological Power Asymmetry during Inflation



Adrienne Erickcek California Institute of Technology

In collaboration with Sean Carroll and Marc Kamionkowski

"A Hemispherical Power Asymmetry from Inflation" arXiv:0806.0377, submitted to PRL "Superhorizon Perturbations and the CMB" arXiv:0808.1570, submitted to PRD

Cosmo '08: August 25, 2008

A Hemispherical Power Asymmety



Simulated maps courtesy of H. K. Eriksen

Cosmo '08: August 25, 2008

A Hemispherical Power Asymmety





Asymmetric



A Hemispherical Power Asymmety





Asymmetric



A Power Asymmety?

Isotropic or Asymmetric?



WMAP First Year Low-Resolution Map

Image from Eriksen, et al. astro-ph/0307507

Cosmo '08: August 25, 2008

There is a hemispherical power asymmetry! There is more power on large scales south of the ecliptic.

Hansen, Banday, Gorski, 2004 Eriksen, Hansen, Banday, Gorski, Lilje 2004



Cosmo '08: August 25, 2008

There is a hemispherical power asymmetry! There is more power on large scales south of the ecliptic.

Hansen, Banday, Gorski, 2004 Eriksen, Hansen, Banday, Gorski, Lilje 2004



Cosmo '08: August 25, 2008

There is a hemispherical power asymmetry! There is more power on large scales south of the ecliptic.

- Power asymmetry is maximized when the "equatorial" plane is tilted with respect to the Galactic plane: "north" pole at $(\ell, b) = (237^\circ, -10^\circ)$.
 - Only 0.7% of simulated isotropic maps contain this much asymmetry.



CMB image from Eriksen, et al. astro-ph/0307507

Cosmo '08: August 25, 2008

Hansen, Banday, Gorski,

2004

Eriksen, Hansen, Banday,

Gorski, Lilje 2004





Cosmo '08: August 25, 2008



The amplitude of quantum fluctuations depends on the background value of the inflaton field.

$$P_{\Psi} = \frac{2}{9k^3} \left[\frac{H(\phi)^2}{\dot{\phi}} \right]^2 \bigg|_{k=1}^{2}$$

Power Spectrum of Potential Fluctuations

a H



The amplitude of quantum fluctuations depends on the background value of the inflaton field.

$$P_{\Psi} = \frac{2}{9k^3} \left[\frac{H(\phi)^2}{\dot{\phi}} \right]^2 \bigg|_{k=aH}$$

Power Spectrum of Potential Fluctuations

Create asymmetry by adding a large-amplitude superhorizon fluctuation: a "supermode."

A modulation amplitude $A \simeq 0.12 \Longrightarrow \frac{\Delta P_{\Psi}(k)}{P_{\Psi}(k)_{360^{\circ}}} \simeq \pm 0.20$

Generating this much asymmetry requires a **BIG** supermode.

- Perturbations with different wavelengths are very weakly coupled.
- The fluctuation power is not very sensitive to $\phi \iff n_s \simeq 1$.



A modulation amplitude $A \simeq 0.12 \Longrightarrow \frac{\Delta P_{\Psi}(k)}{P_{\Psi}(k)_{360^{\circ}}} \simeq \pm 0.20$

Generating this much asymmetry requires a **BIG** supermode.

- Perturbations with different wavelengths are very weakly coupled.
- The fluctuation power is not very sensitive to $\phi \iff n_s \simeq 1$.



 $\Delta \phi \Longrightarrow \Delta \Psi \Longrightarrow \Delta T$

Surely the resulting temperature dipole would be far too large?

The Dipole Sometimes Cancels...



In an Einstein - deSitter Universe, a superhorizon perturbation induces no CMB dipole. Grishchuk, Zel'dovich 1978 • The SW dipole is cancelled by the Doppler dipole.

- If there is radiation or a cosmological constant, then the Dopper dipole is reduced.
- The ISW dipole will partially cancel the SW dipole.

Will a superhorizon perturbation $\Delta \Psi$ induce a CMB dipole in our Universe?

The Dipole Cancels!



The Dipole Cancels!



Superhorizon perturbation: $\Psi(\vec{x}, t) = \Psi_{SM}(t) \sin[\vec{k} \cdot \vec{x} + \varpi]$ Temperature anisotropy:

$$\frac{\Delta T}{T}(\hat{n}) = \Psi_{\rm SM} \begin{bmatrix} (\vec{k} \cdot \vec{x}_{\rm d})\delta_1 \cos \varpi - (\vec{k} \cdot \vec{x}_{\rm d})^2 \delta_2 \frac{\sin \varpi}{2} - (\vec{k} \cdot \vec{x}_{\rm d})^3 \delta_3 \frac{\cos \varpi}{6} \end{bmatrix}$$

$$\begin{array}{c} Observed \ CMB \\ \hline Dipole \\ \hline \hline Dipole \\ \hline D$$

The supermode generates a CMB quadrupole and octupole. $\Delta \Psi \simeq (k x_d) \Psi_{\rm SM} |\cos \varpi|$





Superhorizon perturbation: $\Psi(\vec{x}, t) = \Psi_{SM}(t) \sin[\vec{k} \cdot \vec{x} + \varpi]$ Temperature anisotropy:

 $\frac{\Delta T}{T}(\hat{n}) = \Psi_{\rm SM} \begin{bmatrix} (\vec{k} \cdot \vec{x}_{\rm d})\delta_1 \cos \varpi - (\vec{k} \cdot \vec{x}_{\rm d})^2 \delta_2 \frac{\sin \varpi}{2} - (\vec{k} \cdot \vec{x}_{\rm d})^3 \delta_3 \frac{\cos \varpi}{6} \end{bmatrix}$ $\begin{array}{c} Observed \ CMB \\ \hline Dipole \\ \hline Temperature \\ \end{array}$

The supermode generates a CMB quadrupole and octupole. $\Delta \Psi \simeq (kx_d) \Psi_{SM} |\cos \varpi|$ Octupole Constraint:

> distance to last scattering surface $\Delta \Psi (kx_{\rm d})^2 \lesssim 32 \mathcal{O} \leftarrow |a_{30}|$ $\mathcal{O} \lesssim 3\sqrt{C_3} \simeq 2.7 \times 10^{-5}$

 $2x_d$

Superhorizon perturbation: $\Psi(\vec{x},t) = \Psi_{SM}(t) \sin[\vec{k} \cdot \vec{x} + \varpi]$ <u>Temperature anisotropy:</u>

 $\begin{array}{c} \frac{\Delta T}{T}(\hat{n}) = \Psi_{\rm SM} \begin{bmatrix} (\vec{k} \cdot \vec{x}_{\rm d}) \delta_{\rm T} \cos \varpi - (\vec{k} \cdot \vec{x}_{\rm d})^2 \delta_2 \frac{\sin \varpi}{2} & -(\vec{k} \cdot \vec{x}_{\rm d})^3 \delta_3 \frac{\cos \varpi}{6} \end{bmatrix} \\ \begin{array}{c} \text{Observed CMB} \\ \text{Dipole} \\ \text{Temperature} \end{bmatrix} \\ \begin{array}{c} \text{Observed CMB} \\ \text{Temperature} \end{bmatrix} \\ \begin{array}{c} \text{Observed CMB} \\ \text{Temperature} \end{bmatrix} \\ \begin{array}{c} \text{Octupole} \\ \text{Octupole} \end{bmatrix} \\ \end{array} \\ \begin{array}{c} \text{Octupole} \\ \text{Octupole} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \text{Octupole} \\ \end{array} \\ \end{array} \\ \begin{array}{c} \text{Octupole} \\ \end{array} \\ \begin{array}{c} \text{Octupole} \\ \end{array} \\ \end{array} \\ \end{array} \\ \end{array}$ \\ \begin{array}{c} \text{Octupole} \\ \end{array} \\ \end{array} \\ \end{array} \\ \end{array} \\ \begin{array}{c}

$$\begin{split} \Delta\Psi & |\Psi| < 1 \Longrightarrow \Delta\Psi \lesssim kx_{\rm d} \\ \Delta\Psi & [32\mathcal{O}]^{1/3} = 0.095 \\ 2x_{\rm d} & \text{Cosmo '08: August 25, 2008} \end{split}$$

 $\mathcal{O} \lesssim 3\sqrt{C_3} \simeq 2.7 \times 10^{-5}$

Superhorizon perturbation: $\Psi(\vec{x},t) = \Psi_{SM}(t) \sin[\vec{k} \cdot \vec{x} + \varpi]$ Temperature anisotropy:

 $\frac{\Delta T}{T}(\hat{n}) = \Psi_{\rm SM} \begin{bmatrix} (\vec{k} \cdot \vec{x}_{\rm d})\delta_1 \cos \varpi - (\vec{k} \cdot \vec{x}_{\rm d})^2 \delta_2 \frac{\sin \varpi}{2} - (\vec{k} \cdot \vec{x}_{\rm d})^3 \delta_3 \frac{\cos \varpi}{6} \end{bmatrix}$ Observed CMB
Dipole
Quadrupole Observed CMB Temperature The supermode generates a CMB quadrupole and octupole. $\Delta \Psi \simeq (k x_{\rm d}) \Psi_{\rm SM} |\cos \varpi|$ Octupole Constraint: distance to last $\Delta\Psi\lesssim[32{\cal O}]^{1/3}=0.095$ scattering surface **Recall:** $\frac{\Delta P_{\Psi}}{P_{\Psi}} \propto \Delta \phi \propto \Delta \Psi$ $rac{\Delta P_\Psi}{P_\Psi} \lesssim 0.01$ $2x_{d}$

Superhorizon perturbation: $\Psi(\vec{x},t) = \Psi_{SM}(t) \sin[\vec{k} \cdot \vec{x} + \varpi]$ Temperature anisotropy:



The problem with the inflaton model is two-fold:

The fluctuation power is only weakly dependent on the background value.
The inflaton dominates the energy density of the universe, so a "supermode" in the inflaton field generates a huge potential perturbation.

The solution: the primordial fluctuations could be generated by a subdominant scalar field, the curvaton.

The solution: the primordial fluctuations could be generated by a subdominant scalar field, the curvaton. The Curvaton Model of Inflation

Mollerach 1990; Linde, Mukhanov 1997; Lyth, Wands 2002; Moroi, Takahashi 2001

The inflaton still dominates the energy density and drives inflation.
 The curvaton (σ) is a light scalar field during inflation: m_σ ≪ H_{inf}(φ) potential: V(σ) = ¹/₂m²_σσ² quantum fluctuations: (δσ)_{rms} = <sup>H_{inf}/_{2π} ≪ σ
 After inflation, when m_σ ≃ H, the curvaton oscillates in its potential.
 Then the curvaton decays into radiation; its quantum fluctuations produce a spectrum of adiabatic perturbations.
</sup>

$$P_{\Psi,\sigma} \propto \left(rac{H_{
m Inf}}{ar{\sigma}}
ight)^2$$

The solution: the primordial fluctuations could be generated by a subdominant scalar field, the curvaton. The Curvaton Model of Inflation

Mollerach 1990; Linde, Mukhanov 1997; Lyth, Wands 2002; Moroi, Takahashi 2001

The inflaton still dominates the energy density and drives inflation.
 The curvaton (σ) is a light scalar field during inflation: m_σ ≪ H_{inf}(φ) potential: V(σ) = ¹/₂m²_σσ² quantum fluctuations: (δσ)_{rms} = <sup>H_{inf}/_{2π} ≪ σ
 After inflation, when m_σ ≃ H, the curvaton oscillates in its potential.
 Then the curvaton decays into radiation; its quantum fluctuations produce a spectrum of adiabatic perturbations. δσ
</sup>



Cosmo '08: August 25, 2008

The solution: the primordial fluctuations could be generated by a subdominant scalar field, the curvaton. The Curvaton Model of Inflation

Mollerach 1990; Linde, Mukhanov 1997; Lyth, Wands 2002; Moroi, Takahashi 2001

The inflaton still dominates the energy density and drives inflation.
 The curvaton (σ) is a light scalar field during inflation: m_σ ≪ H_{inf}(φ) potential: V(σ) = ¹/₂m²_σσ² quantum fluctuations: (δσ)_{rms} = <sup>H_{inf}/_{2π} ≪ σ̄
 After inflation, when m_σ ≃ H, the curvaton oscillates in its potential.
 Then the curvaton decays into radiation; its quantum fluctuations produce a spectrum of adiabatic perturbations. δσ̄
</sup>



Cosmo '08: August 25, 2008

Curvaton Supermodes in the CMB

 $\delta \bar{\sigma}$

Curvaton supermode: $\delta \bar{\sigma}(\vec{x}, t) = \bar{\sigma}_{SM}(t) \sin[\vec{k} \cdot \vec{x} + \varpi]$

The curvaton supermode generates a superhorizon potential fluctuation, but it is suppressed.

 $R =
ho_\sigma /
ho$ just prior to decay

$$\Psi = -\frac{\frac{4}{R}}{5} \left[2\left(\frac{\delta\bar{\sigma}}{\bar{\sigma}}\right) + \left(\frac{\delta\bar{\sigma}}{\bar{\sigma}}\right)^2 \right] - \frac{\delta\rho_{\sigma}}{\rho_{\sigma}}$$



The potential perturbation is not sinusoidal!

• The CMB quadrupole and octupole have complicated ϖ dependences.

lacksquare There is still a quadrupole if arpi=0.

Curvaton Supermodes in the CMB



$$\Psi = -\frac{\frac{R}{\delta \sigma}}{5} \left[2\left(\frac{\delta \bar{\sigma}}{\bar{\sigma}}\right) + \left(\frac{\delta \bar{\sigma}}{\bar{\sigma}}\right)^{2} \right] - \frac{\delta \rho_{\sigma}}{\rho_{\sigma}}$$

The potential perturbation is not sinusoidal!

- The CMB quadrupole and octupole have complicated ϖ dependences.
- lacksim There is still a quadrupole if arpi=0.















The Dealbreaker
The window for
$$\frac{\Delta P_{\Psi}}{P_{\Psi}} = 0.2$$

disappears if $f_{\rm NL,max} \lesssim 50$
 $f_{\rm NL} \leq 100$
 $f_{\rm NL} = 100$
 $f_{\rm N$

Summary: How to Generate the Power Asymmetry

There is a power asymmetry in the CMB.

present at the 99% confidence level
detected on large scales

Hansen, Banday, Gorski, 2004 Eriksen, Hansen, Banday, Gorski, Lilje 2004 Eriksen, Banday, Gorski, Hansen, Lilje 2007



A superhorizon perturbation during inflation

generates a power asymmetry.

- also generates large-scale CMB temperature perturbations
- no dipole; quadrupole and octupole set limits.

Erickcek, Carroll, Kamionkowski arXiv:0808.1570

- an inflaton perturbation is ruled out
- a curvaton perturbation is a viable source of the observed asymmetry Erickcek, Kamionkowski, Carroll arXiv:0806.0377



Summary: How to Generate the Power Asymmetry

There is a power asymmetry in the CMB.

present at the 99% confidence level
detected on large scales

Hansen, Banday, Gorski, 2004 Eriksen, Hansen, Banday, Gorski, Lilje 2004 Eriksen, Banday, Gorski, Hansen, Lilje 2007



Features of the Curvaton-Generated Power Asymmetry

- the superhorizon curvaton perturbation is not a quantum fluctuation
- the produced asymmetry is scale-invariant, but it may be possible to modify that
- ullet suppressed tensor-scalar ratio: $r \propto (1-\xi)$
- high non-Gaussianity: $f_{\rm NL}\gtrsim 50$



Cosmo '08: August 25, 2008