

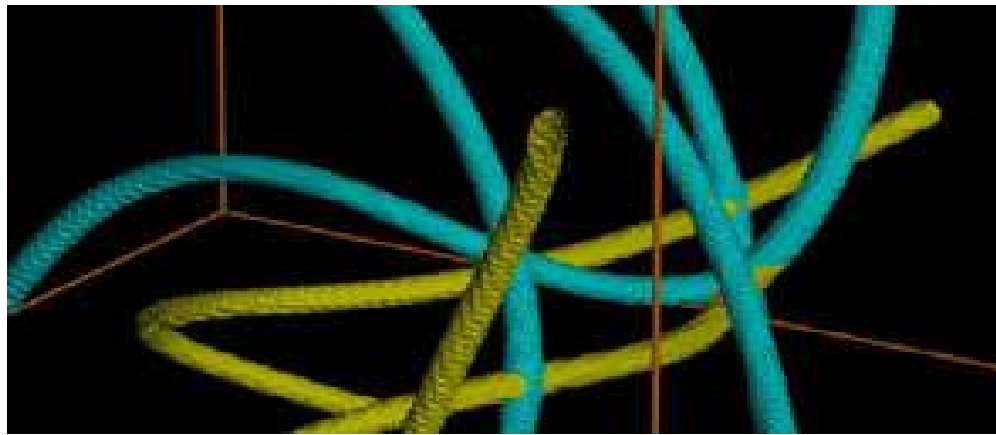
dynamics of cosmic superstring networks



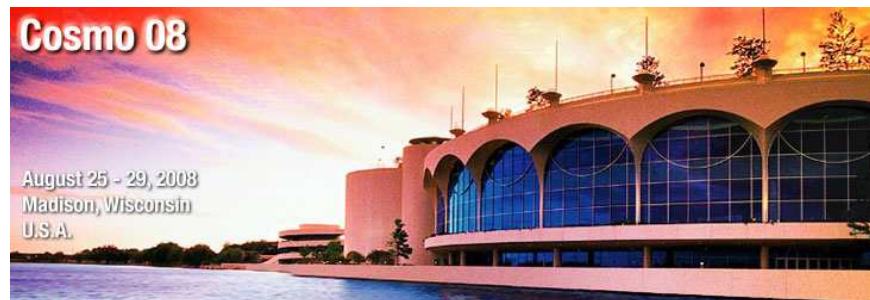
Rajantie, Sakellariadou, Stoica (JCAP 2007)

Sakellariadou, Stoica (JCAP 2008)

Davis, Nelson, Rajamanoharan, Sakellariadou (2008)

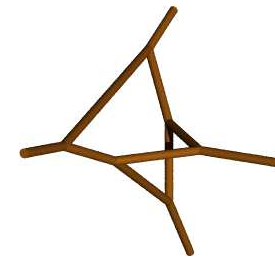
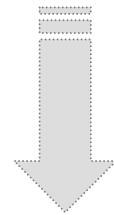


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Fundamental (F) strings and 1-dim Dirichlet branes (D-strings) are generically produced at the end of brane inflation

collisions of F-strings & D-strings produce FD bound states



superstring intercommutations form a trilinear vertex

does a cosmic superstring network reach scaling, or does it freeze
leading to predictions inconsistent with our observed universe?



evolution of cosmic superstring networks

aim: build a simple field theory model of bound states, in analogy with the Abelian Higgs model, and study its properties using lattice simulations

characteristics:

- bound states have different tension than single-charge strings
- set long-range interaction of each species of strings individually;
different components of the FD-string are expected to exhibit different types of long-range interactions



the model

- two different species of cosmic strings:
include two sets of fields of the Abelian Higgs model
- formation of bound states:
introduce a coupling of the scalar fields via a potential
- one non-BPS species of strings (such strings have long range interactions):
consider the second type of string to be the topological defect of a scalar field with a global $U(1)$ symmetry

Rajantie, Sakellariadou, Stoica (JCAP 2007)



if both species of strings are BPS:

$$S = \int d^3x dt \left[-\frac{1}{4}F^2 - \frac{1}{2}(D_\mu\phi)(D^\mu\phi)^* - \frac{\lambda_1}{4}(\phi\phi^* - \eta_1^2)^2 \right. \\ \left. - \frac{1}{4}H^2 - \frac{1}{2}(D_\mu\chi)(D^\mu\chi)^* - \frac{\lambda_2}{4}\phi\phi^*(\chi\chi^* - \eta_2^2)^2 \right]$$

$$D_\mu\phi = \partial_\mu\phi - ie_1A_\mu\phi$$

$$D_\mu\chi = \partial_\mu\chi - ie_2C_\mu\chi$$

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$$

$$H_{\mu\nu} = \partial_\mu C_\nu - \partial_\nu C_\mu$$

ϕ the Higgs field

χ the axion field

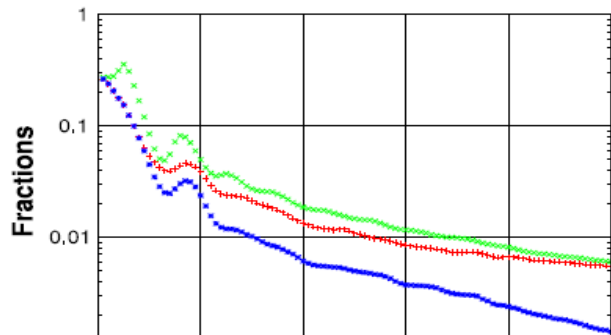
- in the case of a non-BPS species of string: set $e_2 = 0$



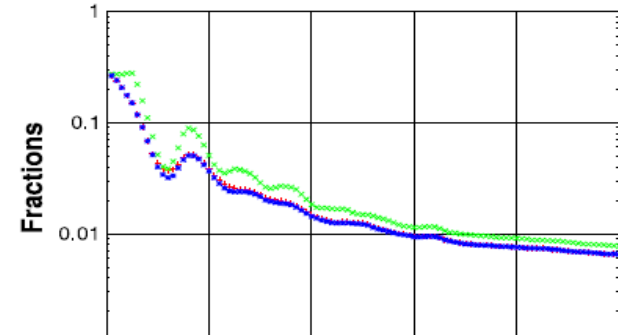
splitting of a bound state as a result of the long-range interactions between strings

the total physical volume of the simulation box occupied by **Higgs strings** the **axion strings**, and their **bound states**

local-global networks

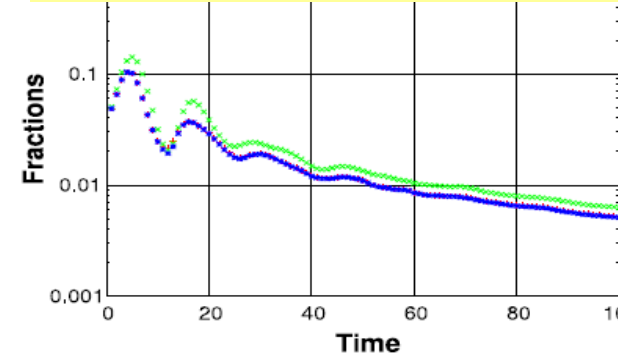
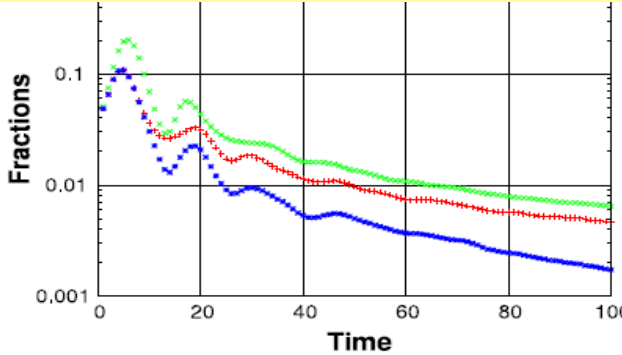


a significant fraction of the strings becomes unbound early



volume of bound states identical with that of axion strings

local-local networks



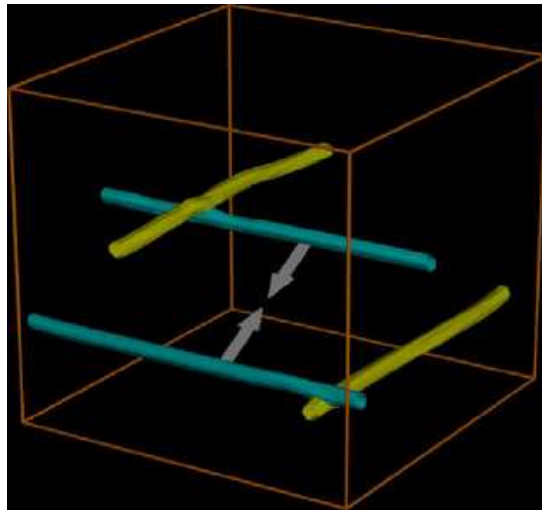
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only one pair of **local** and one pair of **global** strings

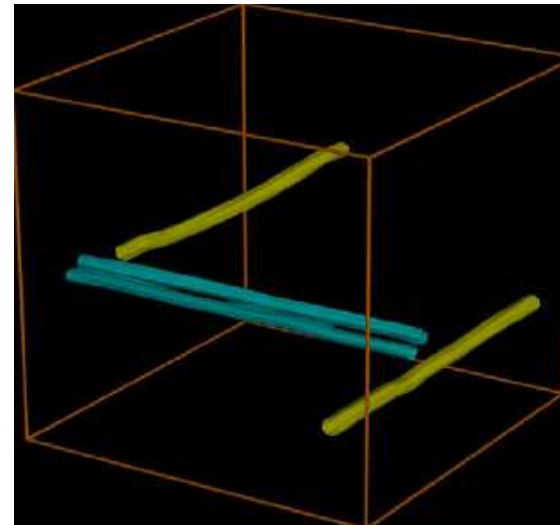
attractive interactions between global strings result in their motion towards the local ones

does the formation of bound states can stop the motion of the global strings?



global strings move towards local ones and cross them, forming bound states

bound states split as global strings continue to move towards each other finally they collide and annihilate



bound states do not survive the long-range interactions of global strings

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dynamics of cosmic superstring networks

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does the existence of bound states prevent a cosmic superstring network from reaching a scaling solution?

use a field theory model to study the effect of junctions in the evolution of a network composed by F, D and FD-strings

we have control over the initial population of bound states

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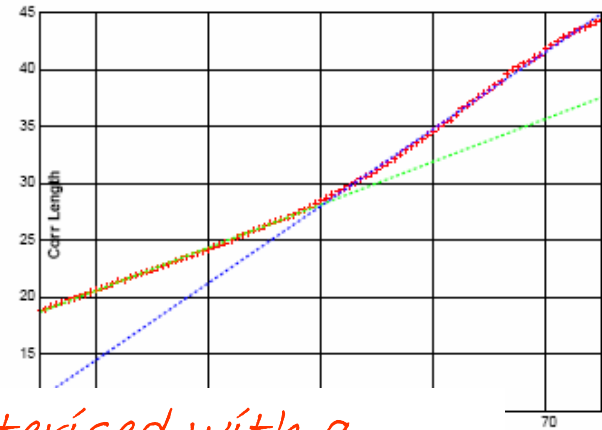
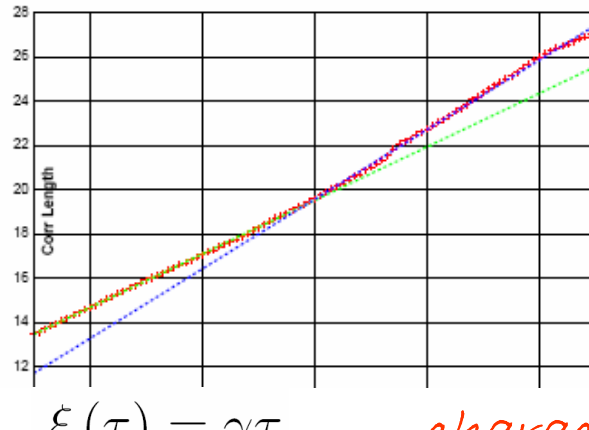
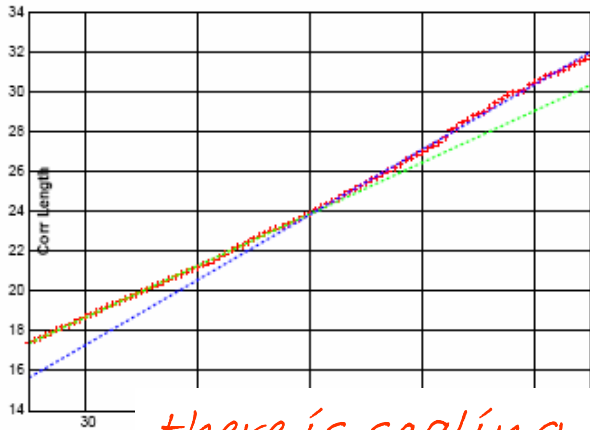
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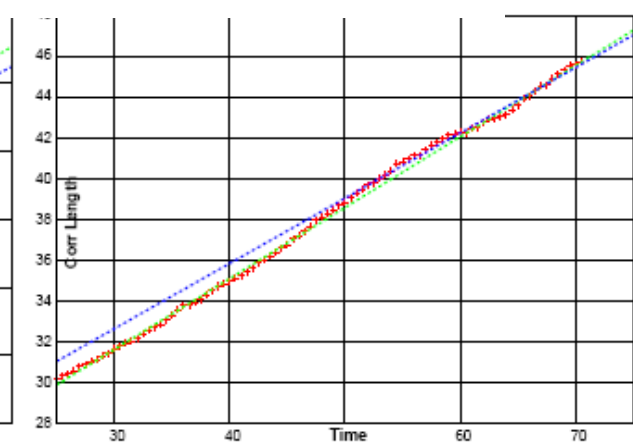
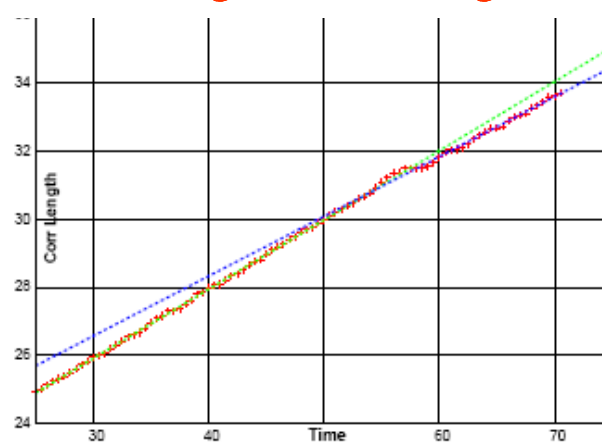
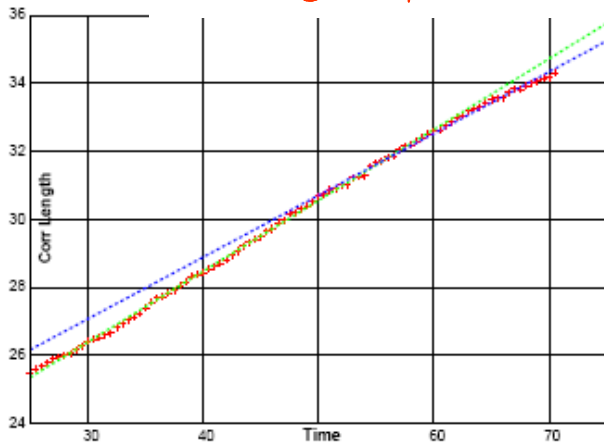


correlation length as function of time in a local-global network

$$\xi = \sqrt{V/L}$$



there is scaling $\xi(\tau) = \gamma\tau$, characterised with a change of correlation length during network evolution



correlation length as function of time in a local-local network

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- scaling of F,D,FD-strings is robust and independent of initial configurations
- the existence of bound states effects the evolution of the network
- there is a supplementary energy loss mechanism, in addition to chopping off loops

new mechanism: formation of bound states with increasing length
the overall network does not freeze because the string length of the unbound states decreases faster

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the three-string junction

BPS saturated formula

$$\tau_{(p,q)} = \sqrt{[p\tau_{(1,0)}]^2 + [q\tau_{(0,1)}]^2}$$

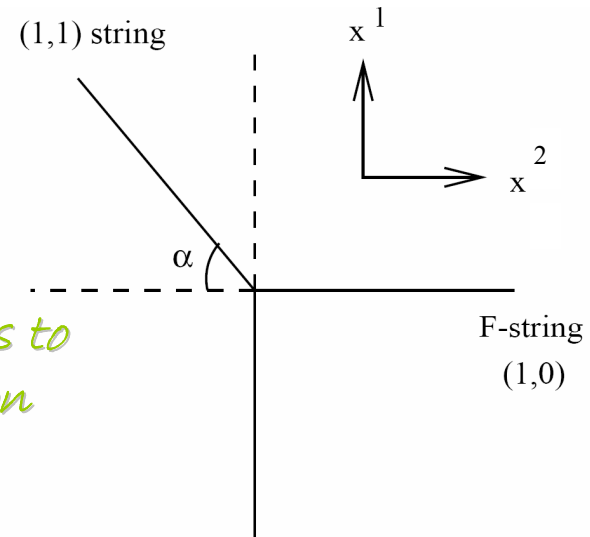
solution:

$$\tau_{(p,q)} \sin \alpha = q\tau_{(0,1)} \quad \tau_{(p,q)} \cos \alpha = p\tau_{(1,0)}$$

where $\tan \alpha = q/(pg_s)$

balance conditions for three strings

when an F-string ends on a D-string it causes to bend at an angle set by the string coupling; on the other side of the junction is a (1,1) string

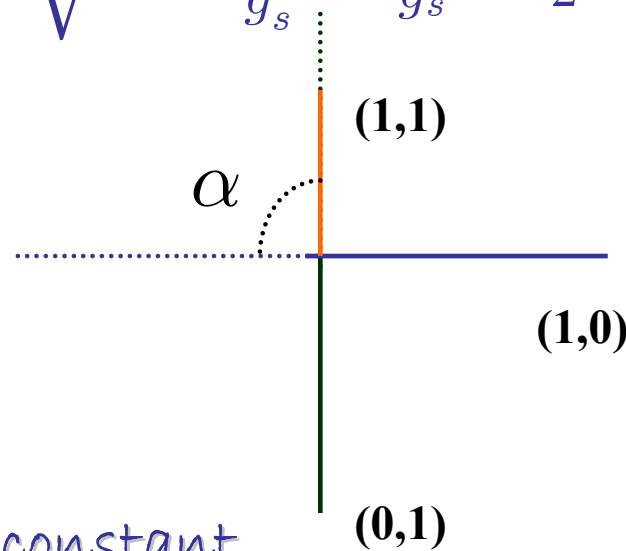
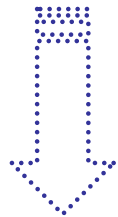


F-string: $\tau_1 = 1$

D-string: $\tau_2 = 1/g_s$

FD-bound state: $\tau_3 = \sqrt{1 + \frac{1}{g_s^2}} = \frac{1}{g_s} + \frac{g_s}{2} + \mathcal{O}(g_s^2)$

in the small g_s -limit:



the angle α goes to $\pi/2$ in the limit of zero string coupling

- length of F-string remains constant
- length of D-string decreases and length of FD-bound state increases



cosmic superstring detection

cosmic superstrings interact with SM particles via gravity

➔ detection involves the gravitational interactions of cosmic superstrings

- gravitational lensing
- micro-lensing
- CMB anisotropies
- gravity waves
- RR/dilaton emission

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cosmic strings in flat space-time

$$\mathbf{x}(\sigma, t)$$

constraint equations and string e.o.m.:

$$\begin{aligned}\dot{\mathbf{x}} \cdot \mathbf{x}' &= 0 \\ \dot{\mathbf{x}}^2 + \mathbf{x}'^2 &= 1 \\ \ddot{\mathbf{x}} - \mathbf{x}'' &= 0\end{aligned}$$

general solution to string e.o.m. in flat space-time:

$$\mathbf{x} = \frac{1}{2} \left[\mathbf{a}(\sigma - t) + \mathbf{b}(\sigma + t) \right]$$

continuous arbitrary functions which satisfy:

$$\mathbf{a}'^2 = \mathbf{b}'^2 = 1$$



cusps

property of loop solutions:

points along the string can reach the velocity of light

$$\dot{\mathbf{x}}^2(\sigma, t) = \frac{1}{4}[\mathbf{a}'(\sigma - t) - \mathbf{b}'(\sigma + t)]^2$$

$\mathbf{a}'(\sigma)$ and $-\mathbf{b}'(\sigma)$ describe closed curves on a unit sphere

the satisfy: $\int_0^L \mathbf{a}' d\sigma = \int_0^L \mathbf{b}' d\sigma = 0$

but otherwise are arbitrary

if the two curves intersect then: $\dot{\mathbf{x}}^2(\sigma, t) = 1$

smooth loops will in general have such luminal points: cusps



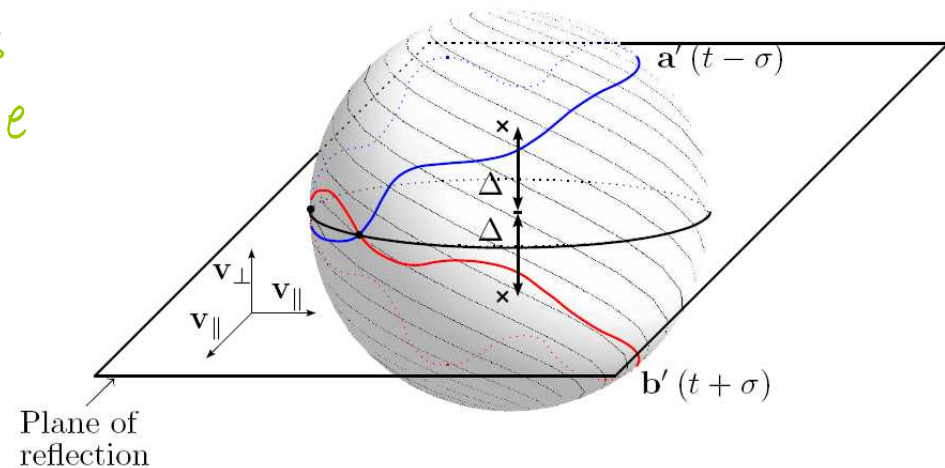
non-periodic strings ending on branes

a DBI string ending on two stationary and parallel D n -branes

from BC, a' and b' curves are related by inversion through a surface of identical dimension and orientation to the D-branes, that passes through the center of the unit sphere

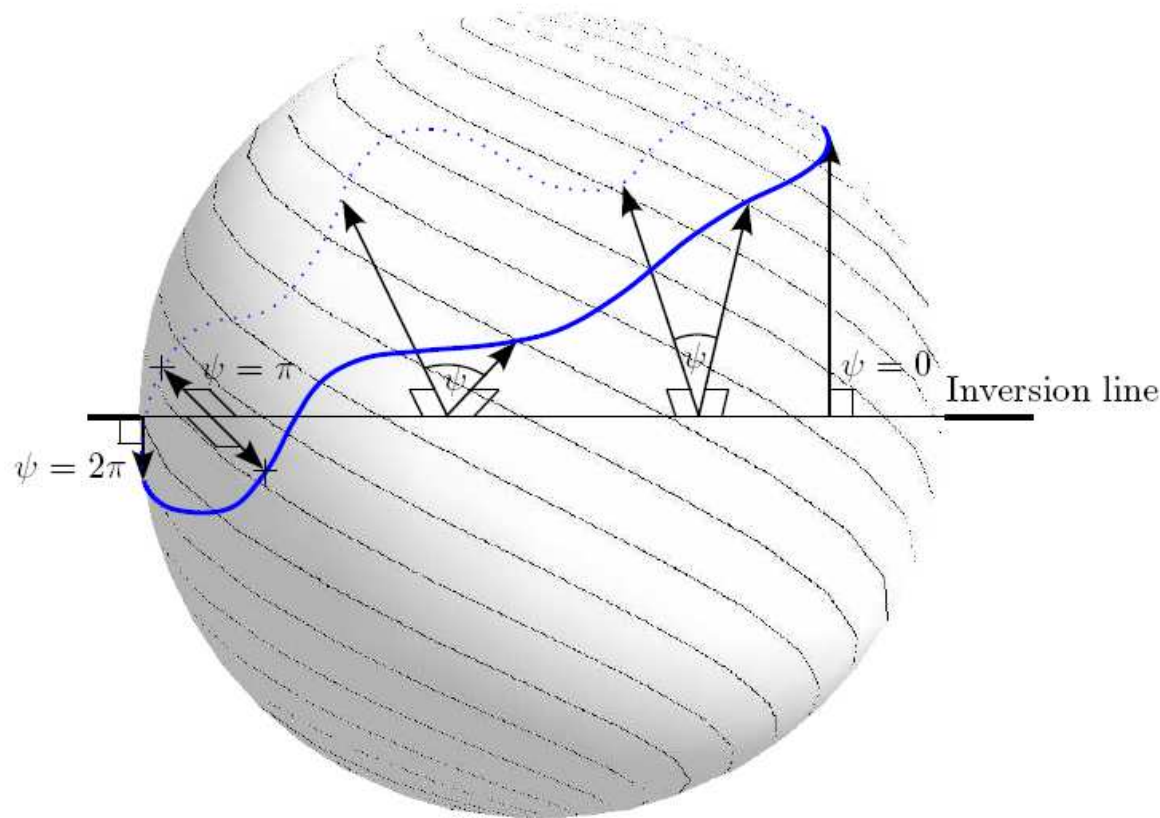
a' and b' trace out closed curves on a unit sphere separated by the inter-brane distance

cusps: if a' and b' intersect



D1-branes

a' and b' intersect whenever the line through which they are inverted is enclosed by the closed curves



when the angle between the 2 vectors perpendicular to the inversion line and ending on the curve is equal to π , the inverted curve will intersect the original one

Davis, Nelson, Rajamanoharan, Sakellariadou (2008)



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genericity of cusps on non-periodic strings ending on branes

- cusps are generic features of an F-string ending on two parallel D-strings
- an F-string stretched between 2 three-string junctions behaves as an F-string between 2 D1-branes (to order g_s)

 a pair of three-string junctions would have cusps

Davis, Nelson, Rajamanoharan, Sakellariadou (2008)



$g_s \rightarrow 0$ limit: the heavy D/FD string behaves as a single string unaffected by dynamics of light F-string

cusps are significant if the typical separation of the heavy strings must be small w.r.t. length of the F-string stretched between them

as heavy strings move apart, F-strings stretch increasing the distance and the importance of cusps gets reduced

under S-duality the role of F and D strings is reversed:

F-strings and bound FD-strings are the heavy ones

cusps exist on light D-strings ending on three-string junctions



➤ cosmic strings

- cusps can be formed on smooth closed string loops
- intercommutation leads to kinks, which may reduce cusp formation
- GW and SM fields can be emitted

➤ cosmic superstrings

- cusps exist in non-periodic strings ending on D-branes
- cusps in loops may be less important
- intercommutation leads to junctions
- GW and SM fields + dilaton/RR/moduli/gravitinos/stable SUSY particles can be emitted

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conclusions

towards the end of brane inflation cosmic superstrings are produced

their properties and subsequent cosmological evolution into a scaling network open up their possible detections in the near future, via cosmological, astrophysical and gravitational wave measurements

finding distinctive stringy signatures in observations will reveal the particular brane inflationary scenario and validate string theory and the brane world scenario

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