

CMB Features of Brane Inflation

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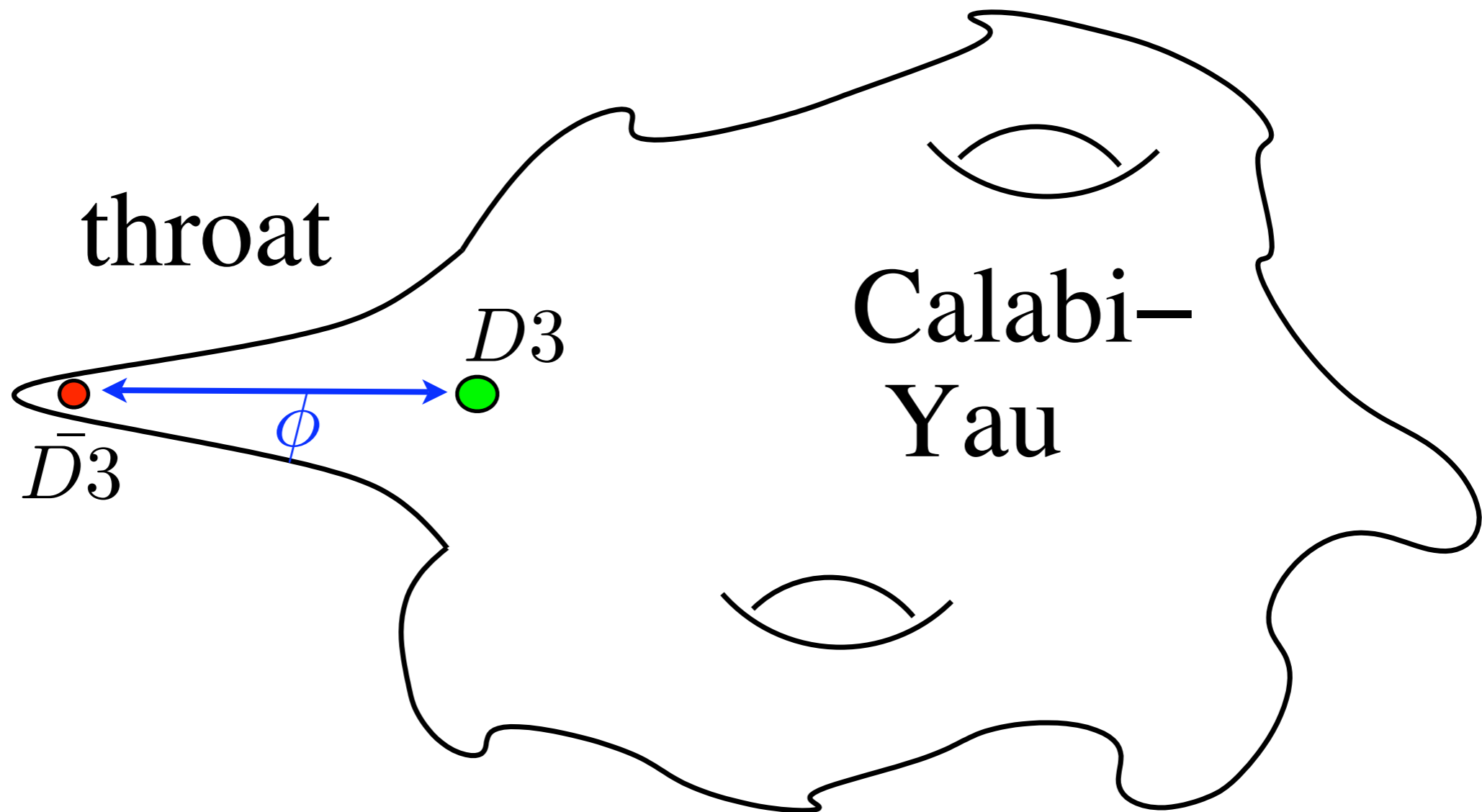
Cornell University

With R. Bean, X. Chen, G. Hailu, S. Shandera and S.H. Tye

hep-th/0702107, arXiv:0710.1812, arXiv:0802.0491

Cosmo 08

Brane Inflation (Dvali & Tye, KKLM, DBI)



Brane Inflation in Warped Throat

Consider D3 Branes moving in the $AdS_5 \times X_5$ background

$$ds^2 = h^2(r)(-dt^2 + a(t)^2 d\mathbf{x}^2) + h^{-2}(r)(dr^2 + r^2 ds_{X_5}^2),$$

in the UV region, $ds_{X_5}^2 = ds_{T^{1,1}}^2$

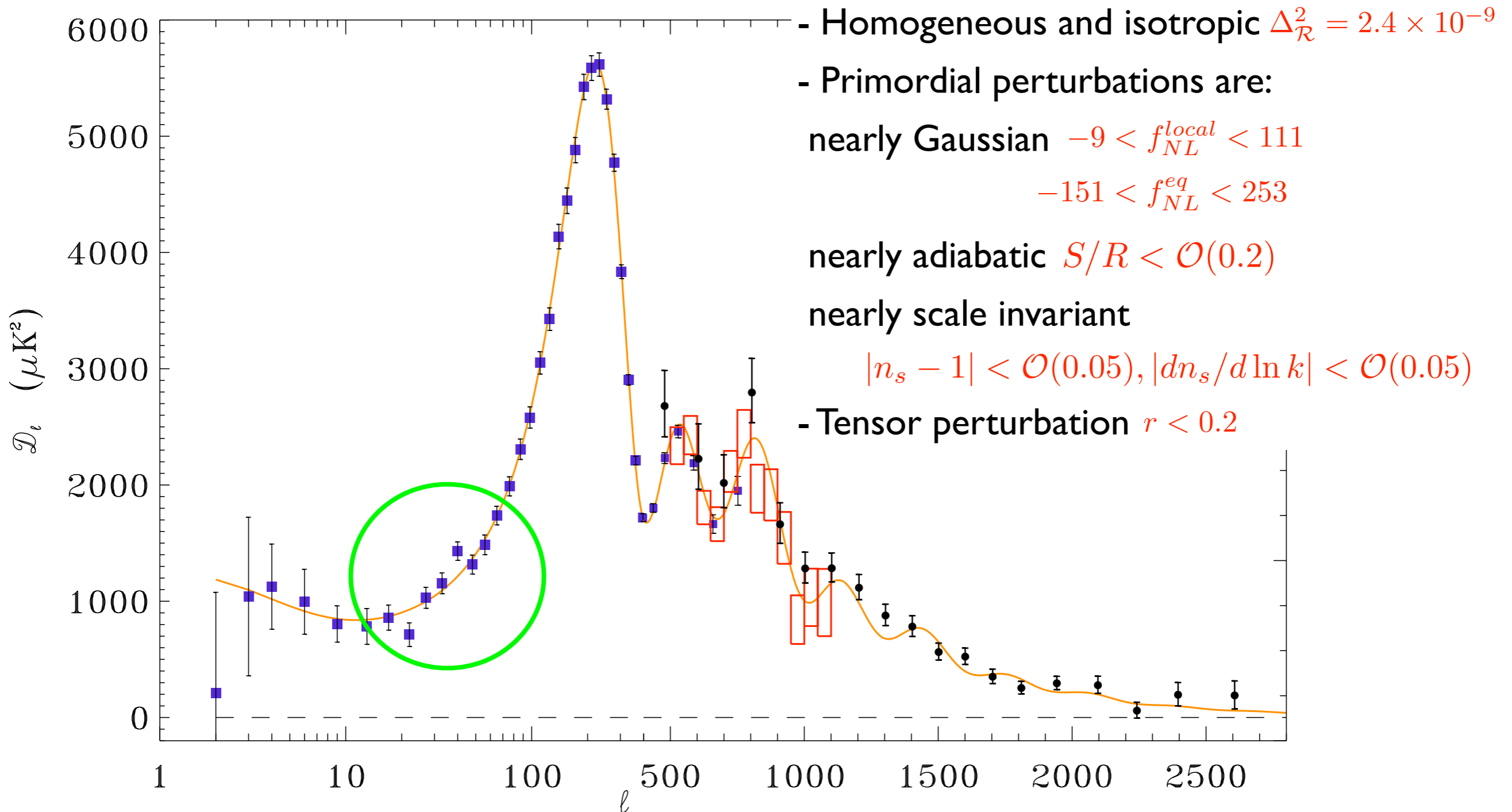
$$S = \int d^4x \sqrt{-g} \left[-e^{-\Phi} T(\phi) \sqrt{1 - \frac{\dot{\phi}^2}{T(\phi)}} + T(\phi) - V(\phi) \right]$$

$$T_3 \sim \frac{m_s^4}{g_s} = \frac{m_s^4}{\langle g_s \rangle} e^{-\Phi(r)}$$

$$T(\phi) = T_3 h^4(\phi)$$

$$\begin{aligned} V(\phi) &= V_{D\bar{D}}(\phi) + \text{corrections} \\ V_{D\bar{D}}(\phi) &= V_0 \left(1 - \frac{V_0}{4\pi^2 v} \frac{1}{\phi^4} \right) \\ V_0 &= 2T_3 h_A^4 \end{aligned}$$

Our Current Understanding of the Early Universe



Three Scenarios

- non-relativistic slow roll (KKLMMT)

$$-e^{-\Phi} T(\phi) \sqrt{1 - \frac{\dot{\phi}^2}{T(\phi)}} + T(\phi) - V(\phi)$$

If $e^{-\Phi} \neq 1$, geometric features in warp factor shows up in power spectrum and non-gaussianity.

$$= \frac{1}{2} e^{-\Phi} \dot{\phi}^2 - [T(\phi)(e^{-\Phi} - 1) + V(\phi)]$$

(Bean, Chen, Hailu, Tye, JX, arXiv:0802.0491)

- DBI (UV) : steep potential attracting the brane to the bottom. (Silverstein & Tong) $V(\phi) = m^2 \phi^2$

$$f_{NL}^{eq} \sim -\frac{M_{pl}^4}{\phi^4} \quad \frac{\phi}{M_{pl}} \lesssim \frac{1}{\sqrt{KM}}$$

(Baumann & McAllister, hep-th/0610285)
(Bean, Shandera, Tye, JX, hep-th/0702107)

- DBI (IR) : steep potential driving the brane out of the throat. (Chen) $V(\phi) = -m^2 \phi^2$

$$-0.046 \leq \frac{dn_s}{d \ln k} \leq -0.01$$

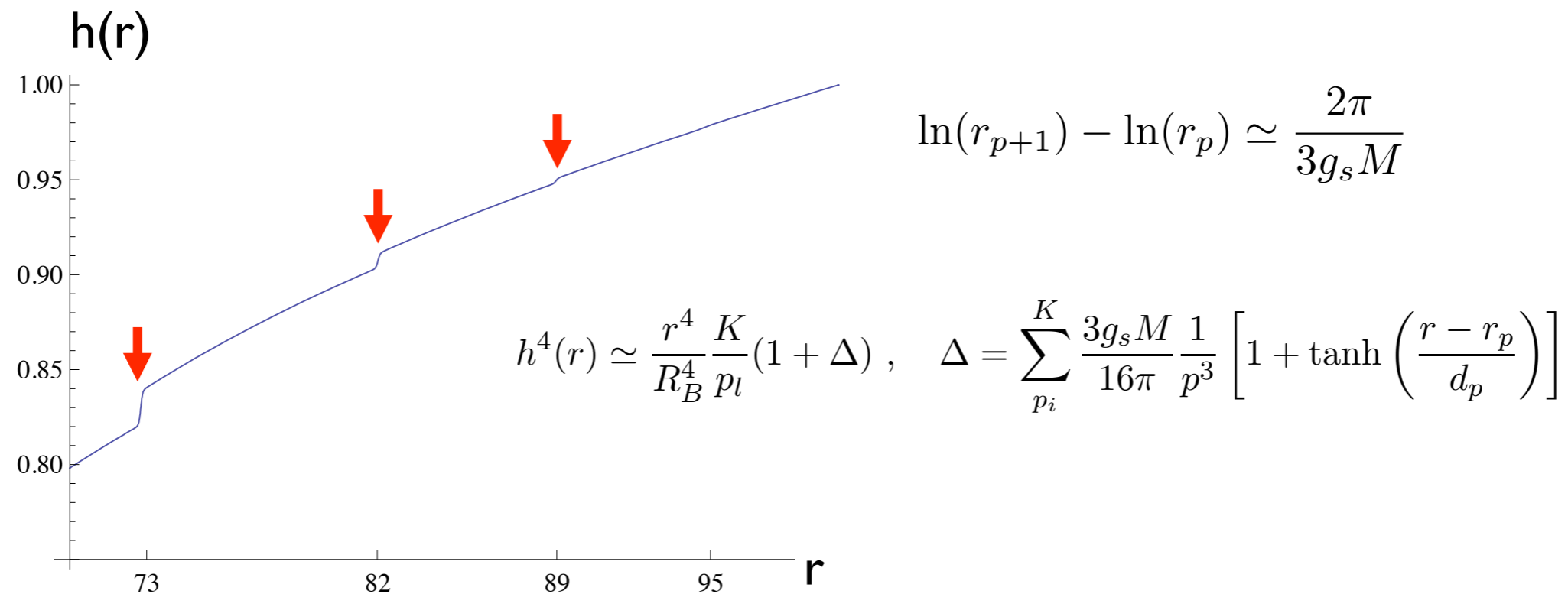
Due to a stringy suppression of power spectrum on large scales

$$-270 \leq f_{NL}^{eq} \leq -70$$

(Bean, Chen, Peries, JX, arXiv:0710.1812)

Sharp features in Brane Inflation

- Background geometry is not smooth and dilaton runs.
(Hailu & Tye)



- For slow roll, steps in the potential

$$V_{eff}(\phi) = T(\phi)(e^{-\Phi} - 1) + V(\phi) \quad \frac{\Delta V}{V} \equiv c$$

- For DBI, steps in the speed limit $T(\phi) \quad \frac{\Delta T}{T} \equiv b$

The Power Spectrum

- The power spectrum

$$v_k'' + \left(k^2 c_s^2 - \frac{z''}{z} \right) v_k = 0 \quad v_k \equiv z u_k, \quad z \equiv a \sqrt{2\epsilon} / c_s$$


$$P_{\mathcal{R}} \equiv \frac{k^3}{2\pi^2} |u_{\mathbf{k}}|^2 \sim \left(\frac{H^2}{2\pi \dot{\phi}} \right)^2$$

- z''/z encodes all the information from the inflationary background

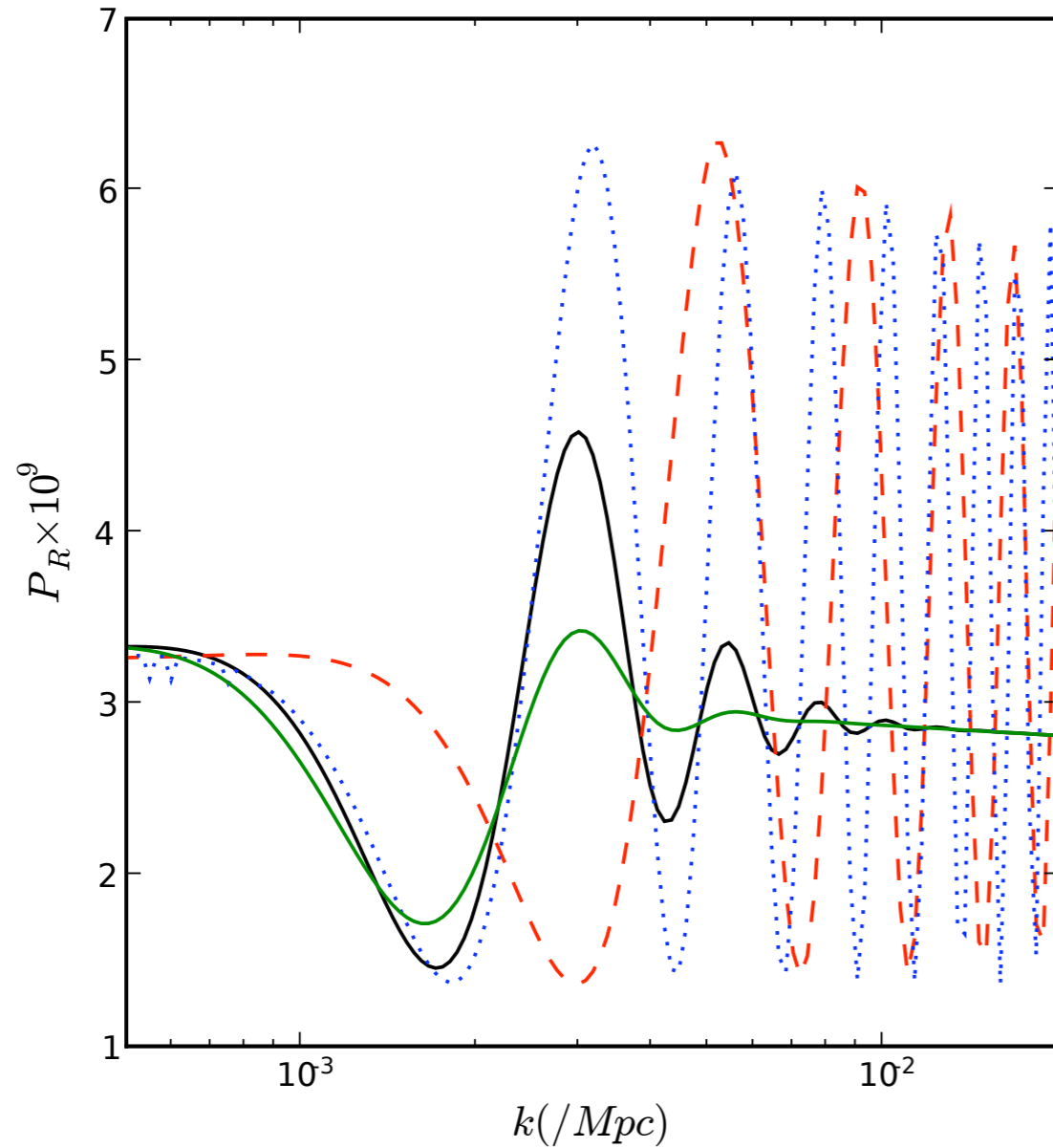
- Define three parameters $\epsilon \equiv -\frac{\dot{H}}{H^2}$, $\tilde{\eta} \equiv \frac{\dot{\epsilon}}{H\epsilon}$, $s \equiv \frac{\dot{c}_s}{Hc_s}$.

$$\frac{z''}{z} = 2a^2 H^2 \left(1 - \frac{\epsilon}{2} - \frac{3\tilde{\eta}}{4} - \frac{3s}{2} - \frac{\epsilon\tilde{\eta}}{4} + \frac{\epsilon s}{2} + \frac{\tilde{\eta}^2}{8} - \frac{\tilde{\eta}s}{2} + \frac{s^2}{2} + \frac{\dot{\tilde{\eta}}}{4H} - \frac{\dot{s}}{2H} \right)$$


 dominant in slow-roll


 dominant in DBI inflation

The Slow-Roll Power Spectrum



$$\frac{z''}{z} \sim 2a^2 H^2 \left(1 - \frac{c}{\epsilon} \frac{1}{\Delta N_e^2} \right) \quad \frac{\Delta V}{V} \equiv c$$

$$\frac{c}{\epsilon} \sim 1, \Delta N_e \ll 1$$

↑
observable

In KKLMMT,
 $\epsilon \sim 10^{-11}$ → $c \sim 10^{-11}$
observable !!

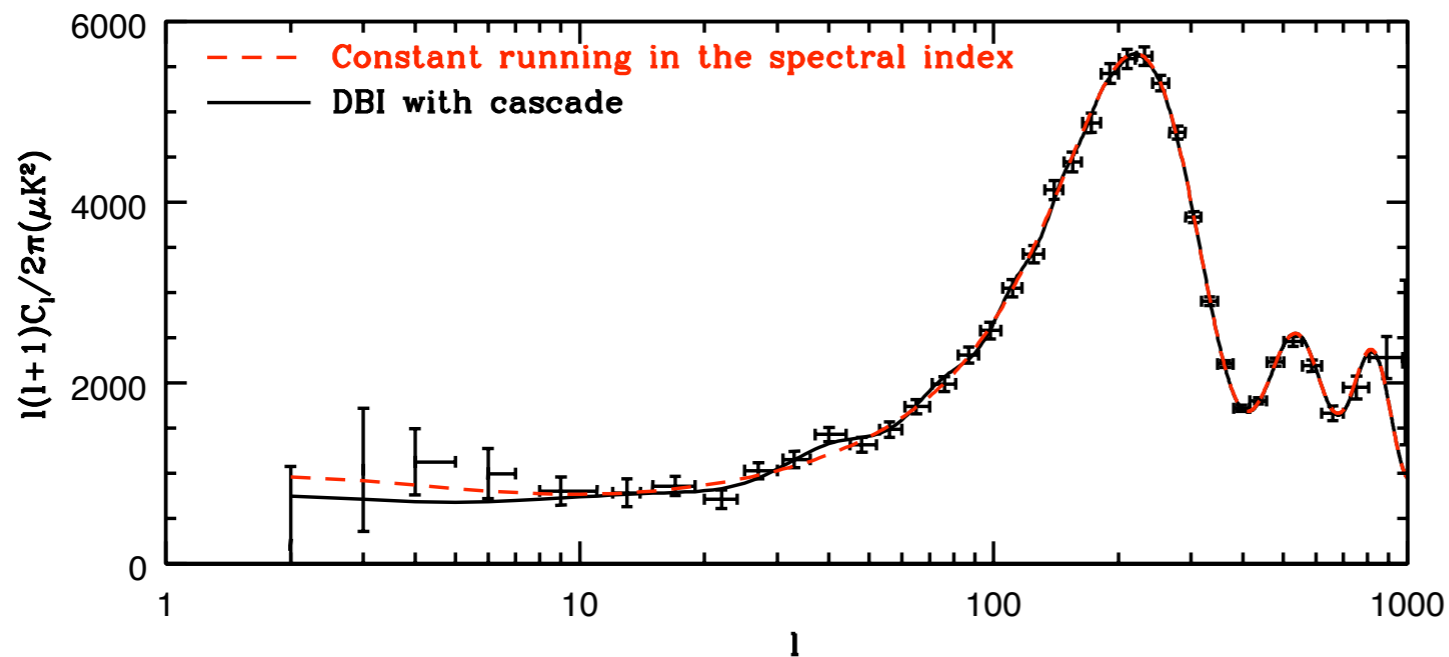
Best Fit:

$$c/\epsilon = 0.2$$

$$\sqrt{c}/d = \mathcal{O}(1)$$

(Adams, Ross, Sarkar 1997,
 Leach, Liddle, 2001
 Hunt, Sakar, 2004, 2007
 Adams, Creswell, Easter, 2001
 Peiris et al, 2003
 Covi et al, 2006, 2007)

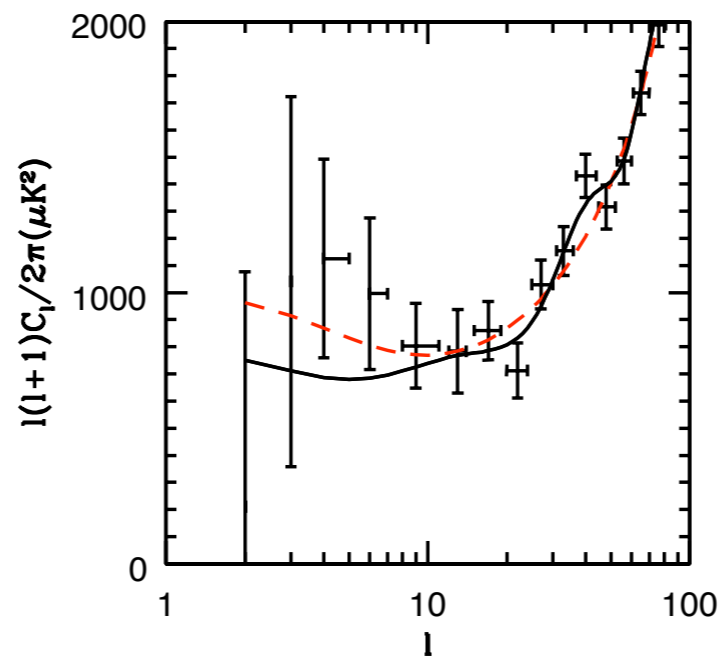
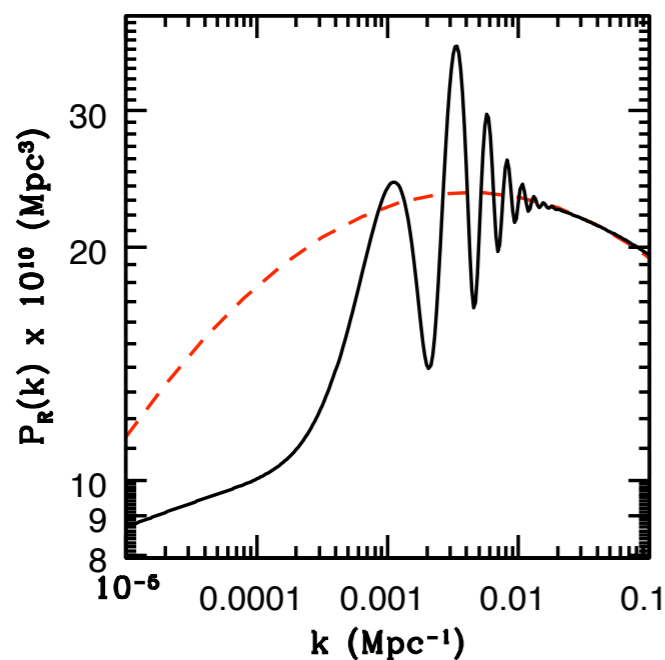
The DBI Power Spectrum



$$\frac{z''}{z} \sim 2a^2 H^2 \left(1 - \frac{b}{\Delta N_e^2} \right)$$

$$\frac{\Delta T}{T} \equiv b$$

$$\frac{b}{\Delta N_e} \lesssim \frac{1}{c_s^3}$$



need $b = -0.3$, too large for steps due to duality cascade

Estimations of Non-Gaussianity

- **Slow-roll:** $\prod u_i \int a^2 \epsilon \tilde{\eta}' u_1 u_2 u_3' \rightarrow \text{non_G} \sim \mathcal{O}(\Delta \tilde{\eta})$

$$\Delta \epsilon \approx \Delta V / H^2 \approx 5c \qquad \Delta \tilde{\eta} \approx \tilde{\eta} = \frac{\dot{\epsilon}}{H\epsilon} \approx \frac{7c^{3/2}}{d\epsilon},$$

$$\Delta t_{\text{accel}} \approx \Delta \phi / \dot{\phi} \approx d / \sqrt{cV},$$

$$c/\epsilon = 0.2 \quad \sqrt{c}/d = \mathcal{O}(1) \quad \rightarrow \text{non_G} \sim \mathcal{O}(1)$$

- **DBI:** $(a^3 \epsilon / c_s^4) \zeta \dot{\zeta}^2 \rightarrow \text{non_G} \sim \mathcal{O}(c_s^{-2})$

$$\frac{a^3 \epsilon}{2c_s^2} \frac{d}{dt} \left(\frac{\tilde{\eta}}{c_s^2} \right) \zeta^2 \dot{\zeta} \rightarrow \text{non_G} \sim \Delta \frac{\tilde{\eta}}{c_s^2} \sim \frac{\Delta s}{c_s} \sim \frac{1}{c_s} \frac{b}{\Delta N_e}$$

$$\frac{a\epsilon}{c_s^2} s \zeta (\partial \zeta)^2 \rightarrow \text{non_G} \sim \frac{s}{c_s^2} H \Delta t \sim \frac{\Delta c_s}{c_s^3} \sim \frac{b}{c_s^2}$$

$$\frac{b}{\Delta N_e} \lesssim \frac{1}{c_s^3}$$

Given $b = 0.01, \Delta N_e = 0.001, c_s = 0.1,$

$$\frac{1}{c_s} \frac{b}{\Delta N_e} \sim 100, \quad \frac{b}{c_s^2} \sim 1$$

Multiple Steps

- Duality cascade gives a series of steps,

$$\ln(r_{p+1}) - \ln(r_p) \simeq \frac{2\pi}{3g_s M}$$

- Feature on scale k in the power spectrum shows up on angular scale l on CMB

$$\frac{\pi}{l} \simeq \frac{k^{-1}}{H_0^{-1}}$$
$$-dN_e \simeq d \ln k \simeq d \ln l \simeq H dt \simeq \frac{H}{\dot{\phi}} d\phi \quad d \ln l \propto d\phi$$

- Take $l=2, l=20$ as two steps for example,

$$\ln(2) - \ln(20) = \ln(20) - \ln(l_3) \Rightarrow l_3 = 200, l_4 = 2000$$

Summary

- Brane inflation with D3 branes in KS throat is very rich in CMB phenomenology. (f_{NL} , $dn_s/d \ln k$, local features)
- Generically the dilaton runs, and features in the warp geometry translate into features in the slow-roll potential. The sensitivity to the steps is controlled by c/ϵ . Brane inflation is **highly sensitive** to small features in the inflaton potential because its small field nature.
- DBI scenario: sharp features in warp factor gives features in non-gaussianity on top of the smooth $f_{NL} \sim -c_s^{-2}$.
- Sharp features if shows up in CMB power spectrum, they appears on several correlated scales, and accompanied by non-G. If no signal in CMB power spectrum, non-G has a better chance to see it.

