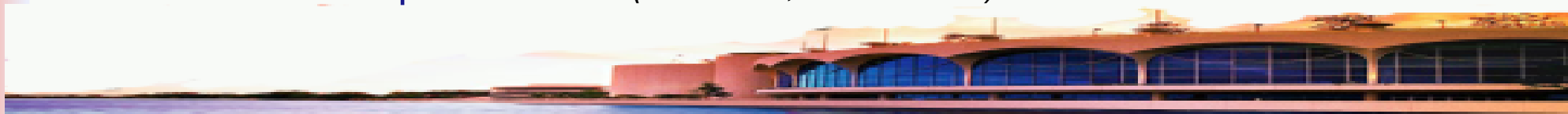


# Hadronic Final States Working group: theory talks

*Pavel Nadolsky (Argonne National Laboratory)*

- Perturbative QCD** (*Klasen, Kniehl, Sassot*)
- Monte-Carlo generators** (*Frixione*)
- Resummations** (*Andersen, Kidonakis, Kyrieleis, Olness*)
- Photon structure** (*Levy*)
- Unitarity at high energy & small  $x$**  (*Marquet, Weiss*)
- Pentaquarks** (*Szczepaniak*)
- Polarization phenomena** (*Dubnicka, Dubnickova*)



## Status of NNLO calculations

(M. Klasen)

- ☞ **Inclusive processes:**
  - NNLO calculation completed for  $F_{1,2,3} \rightarrow$  first NNLO fits
  - NNLO calculation completed for Higgs and DY production
- ☞ **Less inclusive processes:**
  - $e^+e^- \rightarrow 3$  jets: 1  $\rightarrow$  4 subtraction terms partially completed  
 $\rightarrow$  First (preliminary and partial) result for average thrust
  - $e^+e^- \rightarrow QQ$  : 1  $\rightarrow$  2 vector and axial-vector vertex @ 2-loop  
 $\rightarrow$  Subtraction terms still missing
  - $p p \rightarrow 2$  jets: 2  $\rightarrow$  2 quark helicity amplitudes completed  
 $\rightarrow$  Subtraction terms still missing
- ☞ **Multi-particle processes: Twistor methods**
  - Tree-level: Works for non-SUSY, non-MHV, also fermions
  - Loop-level: Works for N=4 SYM @ 1-loop, extension unclear

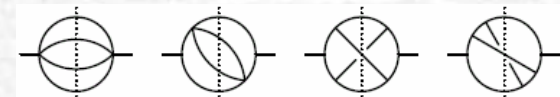
## Jets (2)

### Ingredients:

- $1 \rightarrow 3$  @ 2-loop: Inteference with  $1 \rightarrow 3$  @ 0-loop ✓
- $1 \rightarrow 4$  @ 1-loop: Single soft and/or collinear regions ✓
- $1 \rightarrow 5$  @ 0-loop: Double soft ... triple collinear regions ✓

### Methods:

- Optical theorem: 3-loop propagators
- Subtraction terms: Antenna functions



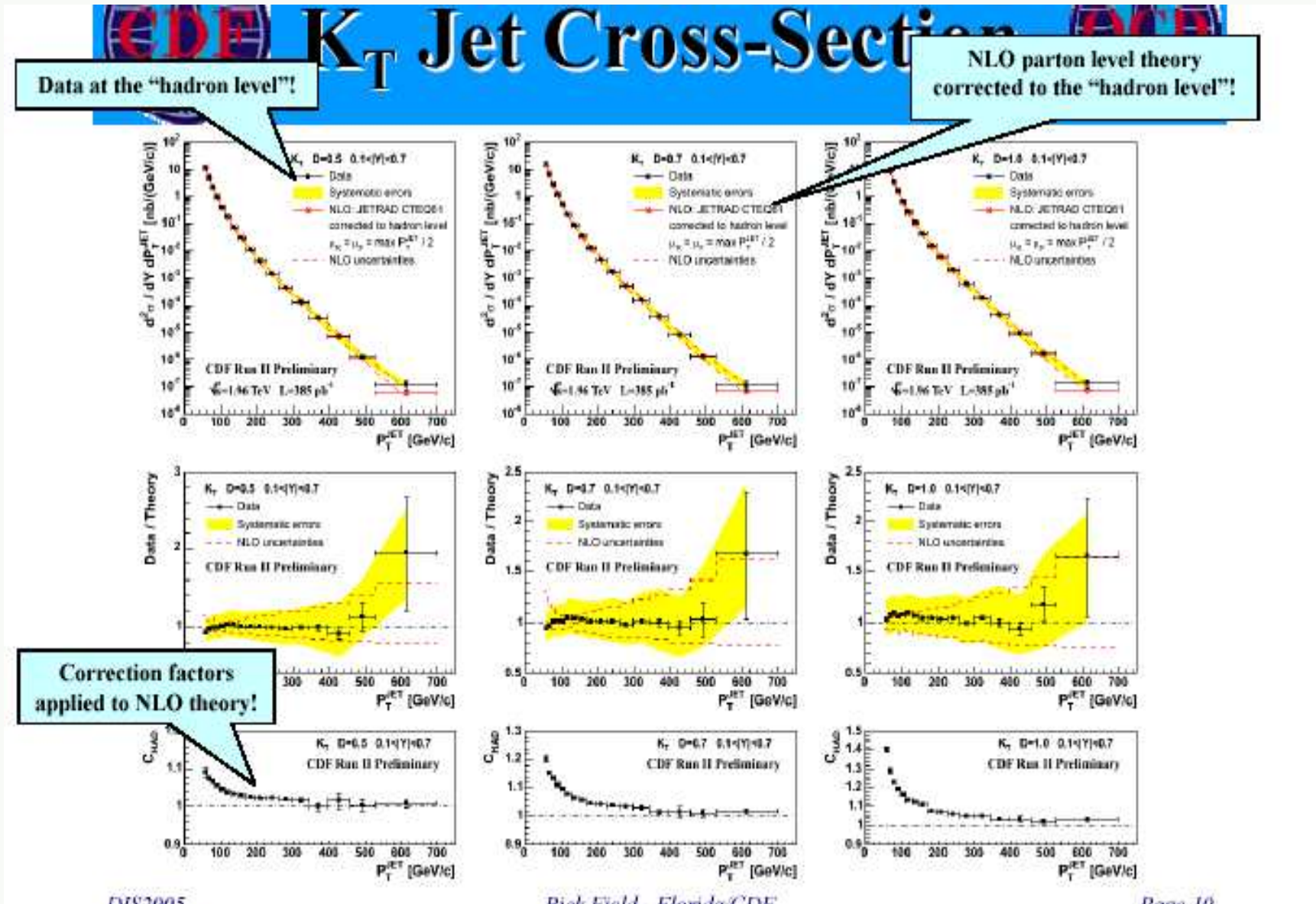
$$\begin{aligned}
 H(p) &= \int \frac{d^4k_0}{(2\pi)^4} \frac{d^4k_1}{(2\pi)^4} \frac{d^4k_2}{(2\pi)^4} \frac{d^4k_3}{(2\pi)^4} \\
 &= -ig_s^2 \lambda \left[ f^{abe} f^{cde} (g^{\mu\rho} g^{\nu\sigma} - g^{\mu\sigma} g^{\nu\rho}) \right. \\
 &\quad \left. + f^{ade} f^{bce} (g^{\mu\nu} g^{\rho\sigma} - g^{\rho\sigma} g^{\nu\mu}) + f^{ace} f^{dbe} (g^{\mu\sigma} g^{\nu\rho} - g^{\mu\nu} g^{\rho\sigma}) \right]
 \end{aligned}$$

### First (preliminary) numerical result:

- Average thrust:  $\langle 1 - T \rangle = \int (1 - T) \frac{1}{\sigma_0} \frac{d\sigma}{d\mathbf{T}} = C_F \left[ \left( \frac{\alpha_s}{2\pi} \right) A + \left( \frac{\alpha_s}{2\pi} \right)^2 B + \left( \frac{\alpha_s}{2\pi} \right)^3 C + \dots \right]$
- $A = 1.57, B = 32.3, C = (-20.4 \pm 4) C_F^2 + \dots$
- A. Gehrmann, T. Gehrmann, N. Glover, LL 2004



# Future NNLO cross sections for $p + p \rightarrow jets + X$ needed for the full NNLO PDF analysis

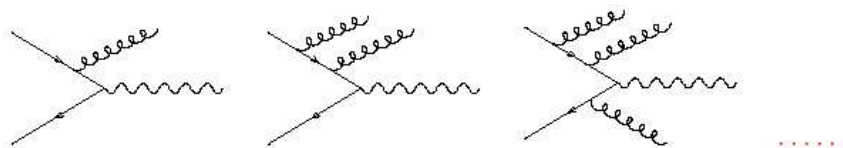


## Monte-Carlo event generators *(S. Frixione)*

- ❑ Adequate Monte-Carlo showering models are crucially important for many measurements (including jet cross sections)
- ❑ To what extent can we combine powerful features of perturbative calculations and Monte-Carlo methods in a single formalism?

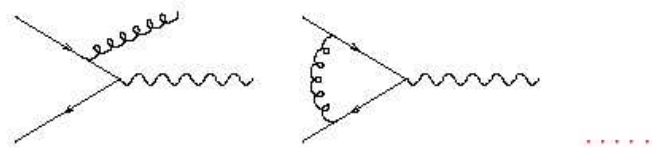
### ○ Matrix-element corrections (MEC)

Just compute (exactly) more **real emission** diagrams before starting the shower



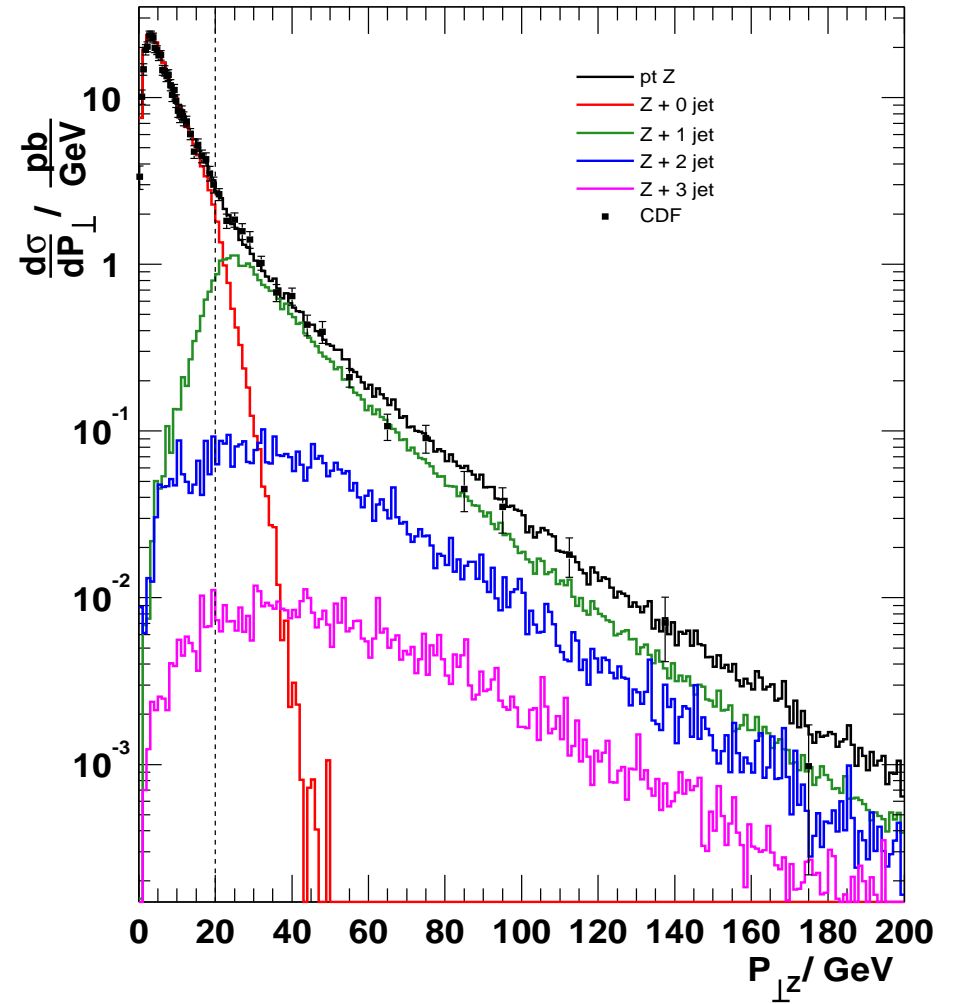
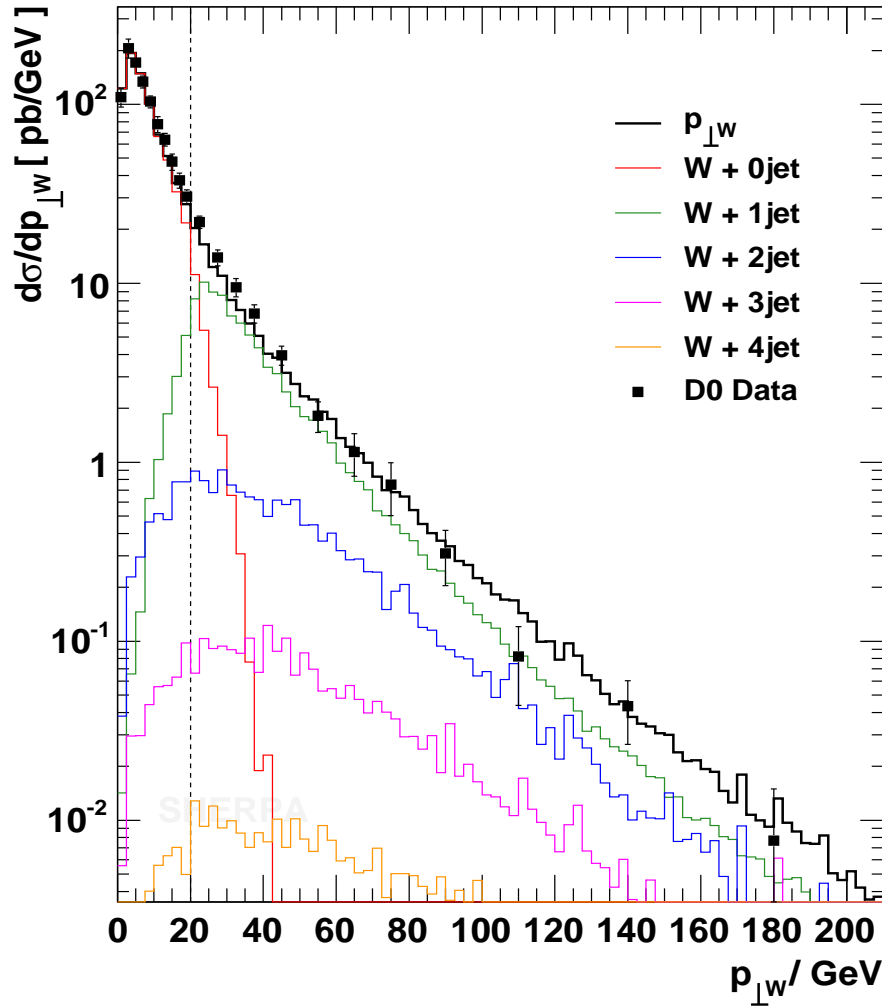
### ○ NLO with parton showering (NLOwPS)

Compute **all NLO** diagrams before starting the shower



▷ pros and cons of two methods

# Using MEC

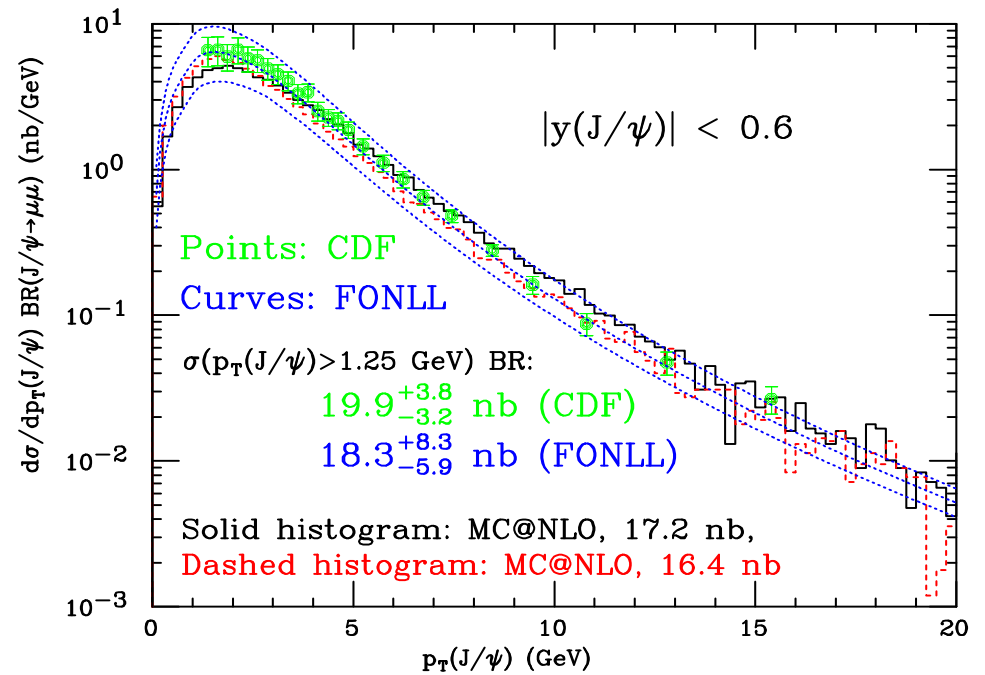
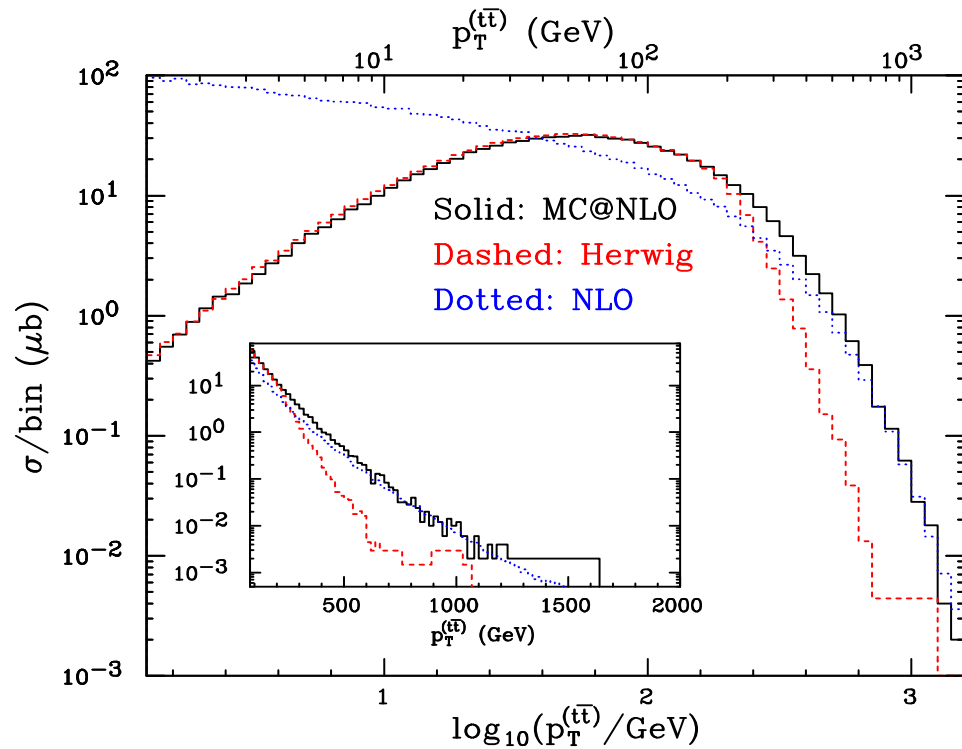


SHERPA (from hep-ph/0409122) – CKKW is built in

Different partonic subprocesses cooperate to give the physical result

■ How about the  $\delta_{sep}$  dependence?

# What to expect from an NLOwPS (here MC@NLO)



- MC@NLO rate = NLO rate  $\implies$  K-factors are included **consistently**
- MC@NLO- and MC-predicted **shapes** are identical where MC does a good job
- $\mathcal{S}+0$  jet and  $\mathcal{S}+1$  jet treated **exactly**,  $\mathcal{S}+n$  jets ( $n > 1$ ) better than in MC's
- No dependence on  $\delta_{sep} \implies$  tuning is the same as in ordinary MC's
- Some **negative-weight events**, to be subtracted (rather than added) from histograms

# NLOwPS versus MEC

## ■ Why is the definition of NLOwPS's much more difficult than MEC?

The problem is a serious one: **KLN cancellation** is achieved in standard MC's through **unitarity**, and embedded in Sudakovs. This is no longer possible: IR singularities **do appear in hard ME's**

IR singularities are avoided in MEC by cutting them off with  $\delta_{sep}$ . This must be so, since only loop diagrams can cut off the divergences of real matrix elements

NLOwPS's are better than MEC since:

- + There is no  $\delta_{sep}$  dependence (i.e., no merging systematics)
- + The computation of total rates is meaningful and reliable

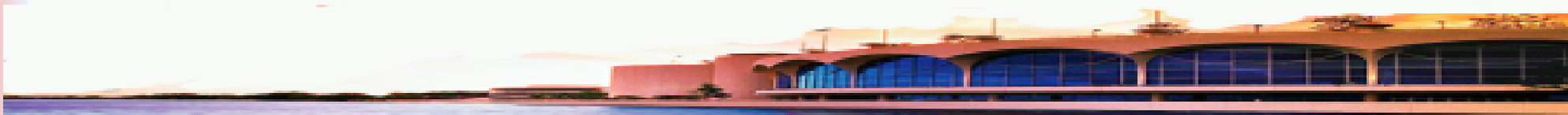
NLOwPS's are worse than MEC since:

- The number of hard legs is smaller
- There are negative weights (i.e., more running time required)



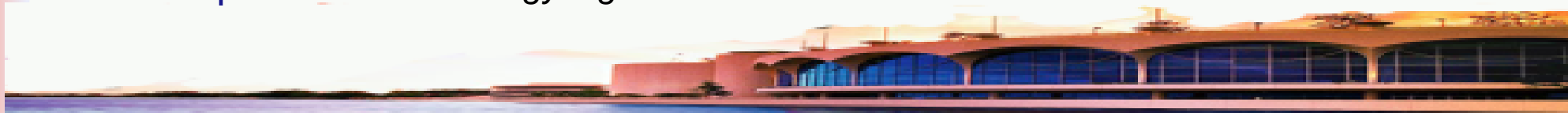
- ❑ **MEC** programs: AcerMC, ALPGEN, AMEGIC++, CompHEP, Grace, MadEvent
- ❑ **NLOwPS** programs: MC@NLO,  $\Phi$ -veto, grcNLO

... and a lot of ongoing theoretical activity



## Underlying event at hadron colliders

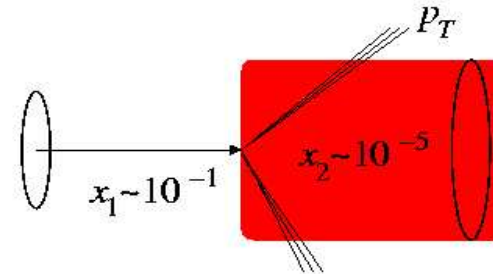
- ❑ under active investigation
- ❑ requires a serious study and Monte-Carlo tuning at the Tevatron  
(*R. Field*)
- ❑ Current models for LHC fall in the “plug and pray” category  
(*S. Frixione*)
  - unknown dependence on  $\sqrt{S}$
  - not well-understood at high luminosities and parton densities
  - will require substantial tuning in the first years of LHC
- ❑ *pp* data from RHIC ( $\sqrt{S} = 200$  GeV) can help constrain the energy dependence  $\Rightarrow$  *Jiangyong Jia's talk*



## Black-body limit in central $pp/pA$ collisions at LHC

L. Frankfurt (Tel Aviv), M. Strikman (Penn State), Ch. Weiss (JLab)  
DIS2005, April 27 – May 1, 2005

- Interaction of large- $x_1$  partons with small- $x_2$  gluons approaches “black-body” (unitarity) limit



- large  $p_{\perp} \gg \Lambda_{\text{QCD}}$
- modified forward hadron production
- affects  $pp$  events with new particle production (Higgs)

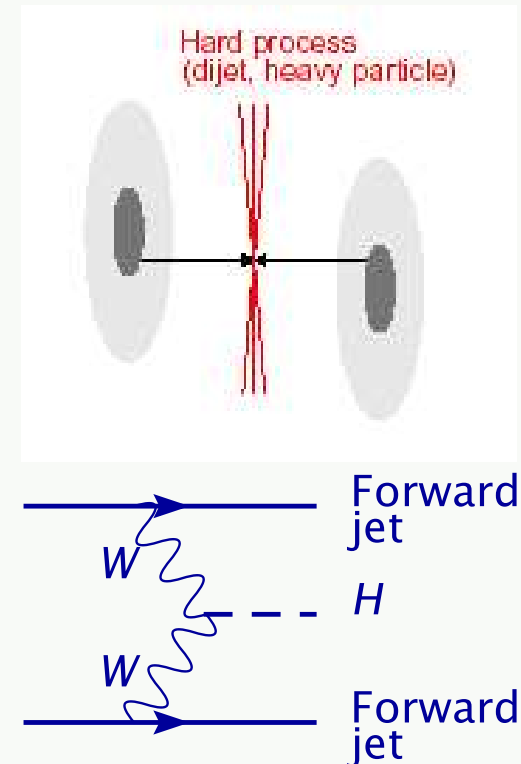
- Ingredients: HERA data on  $G(x, Q^2)$ , transverse size  
QCD factorization (DGLAP)  $\longleftrightarrow$  dipole picture

## Black-body limit at the LHC II

- ❑ may affect forward-rapidity hadronic activity in central  $pp/pA$  collisions
- ❑ e.g., in production of massive particles or jet systems at small rapidities (Higgs production in vector boson fusion)

### Signatures:

- ❑ lost coherence of parton radiation (“shattered” projectiles)
- ❑ leading-energy hadrons have suppressed multiplicity and large  $p_T$  w.r.t. to the jet
- ❑ increased soft particle multiplicities at central rapidities

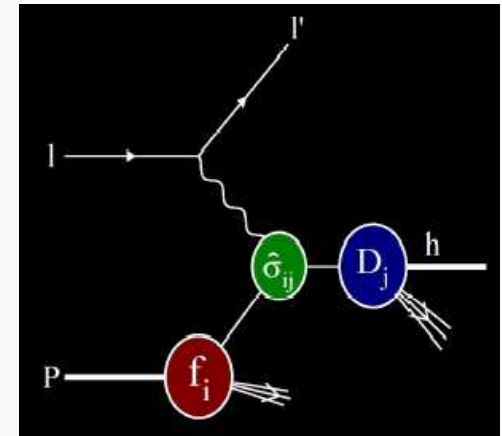


Not implemented yet in Monte-Carlo generators

## $\mathcal{O}(\alpha_s^2)$ corrections to semi-inclusive DIS at high $p_T$ (B. Kniehl, R. Sassot)

### □ Completed recently by several groups

- 0-loop real emission:  $\gamma q^{(-)} \rightarrow q^{(-)} gg$ ,  
 $\gamma g \rightarrow q\bar{q}g$ , etc.
- 1-loop virtual corrections:  $\gamma q^{(-)} \rightarrow q^{(-)} g$ ,  
 $\gamma g \rightarrow q\bar{q}$



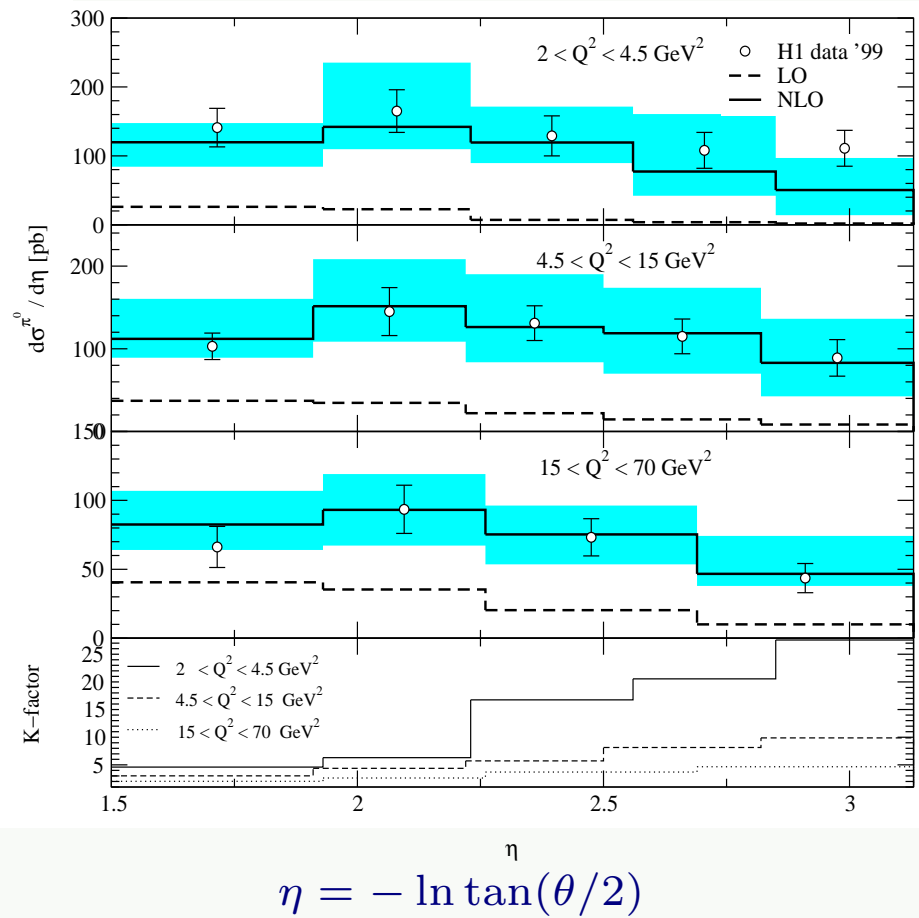
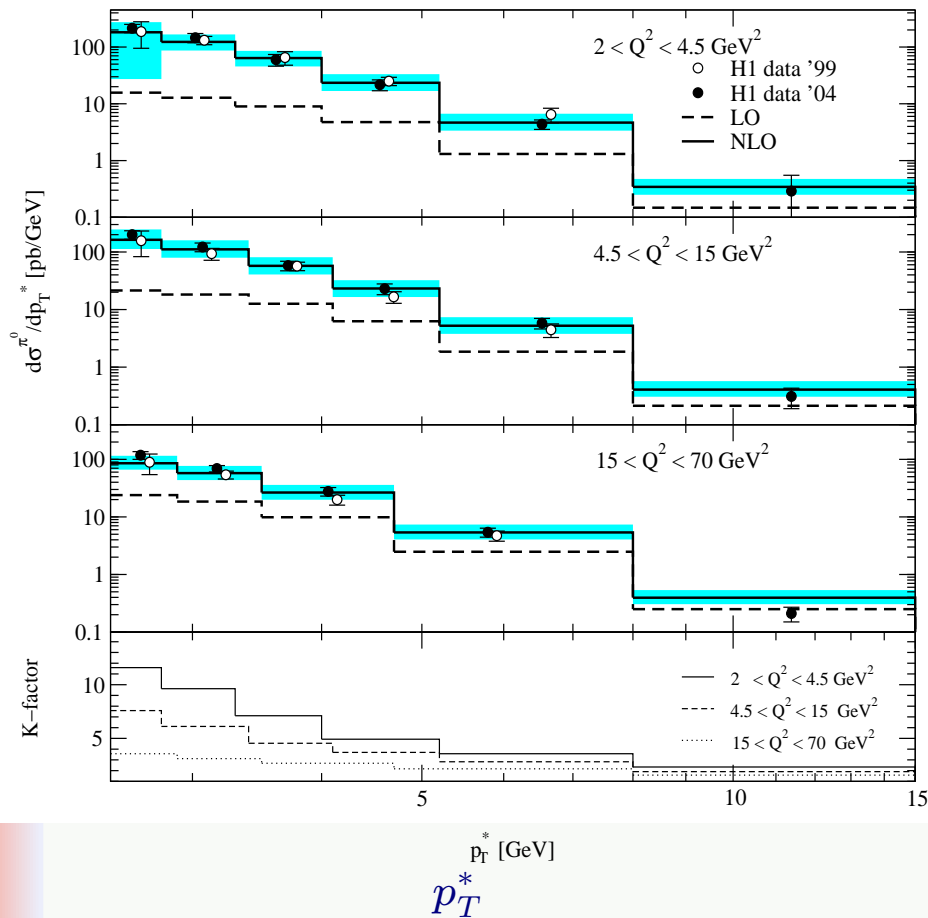
### □ Agrees with most of the HERA data within uncertainties; at the same time,

- $K = \sigma_{NLO}/\sigma_{LO}$  is in the range  $\sim 1 - 25$   
 $K$  increases at smaller  $Q$ ,  $x$ ,  $p_T^*$ , or large  $\eta$
- Scale uncertainty of  $\sim 100\%$
- Substantial dependence on fragmentation functions

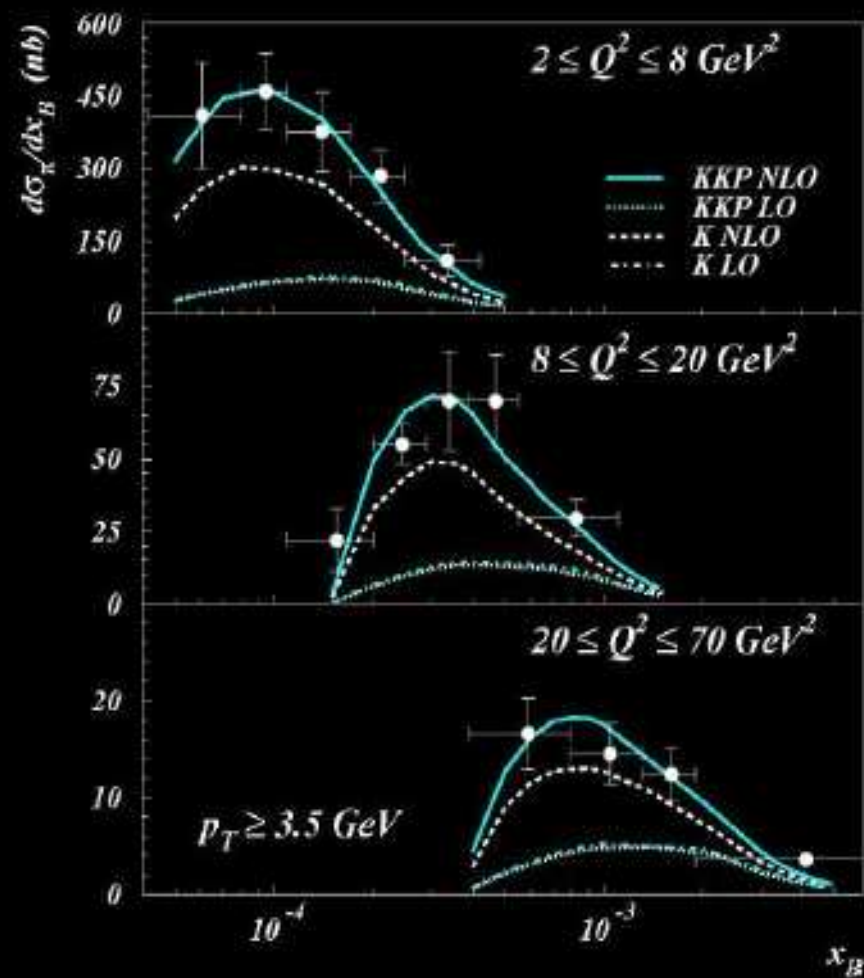
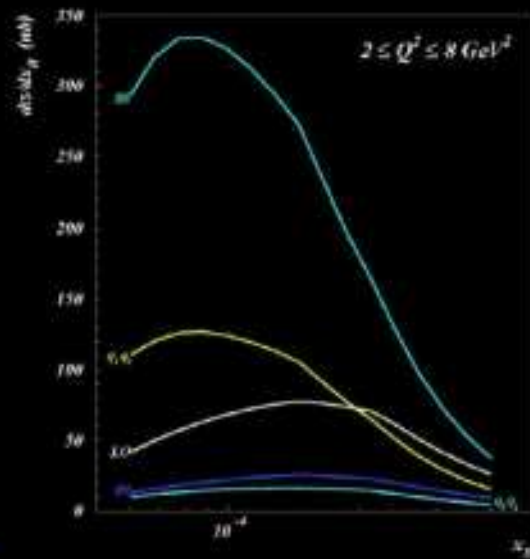


DIS 2005

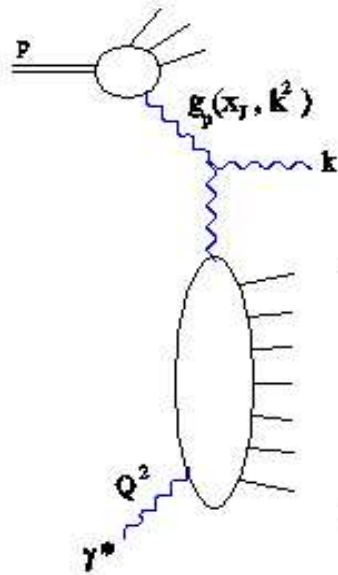
Hadronic Final States

(a)  $\pi^0$  mesons in the forward region (H1)

# Forward jet production at H1



# The forward-jet cross-section in LL BFKL with saturation (C. Marquet)



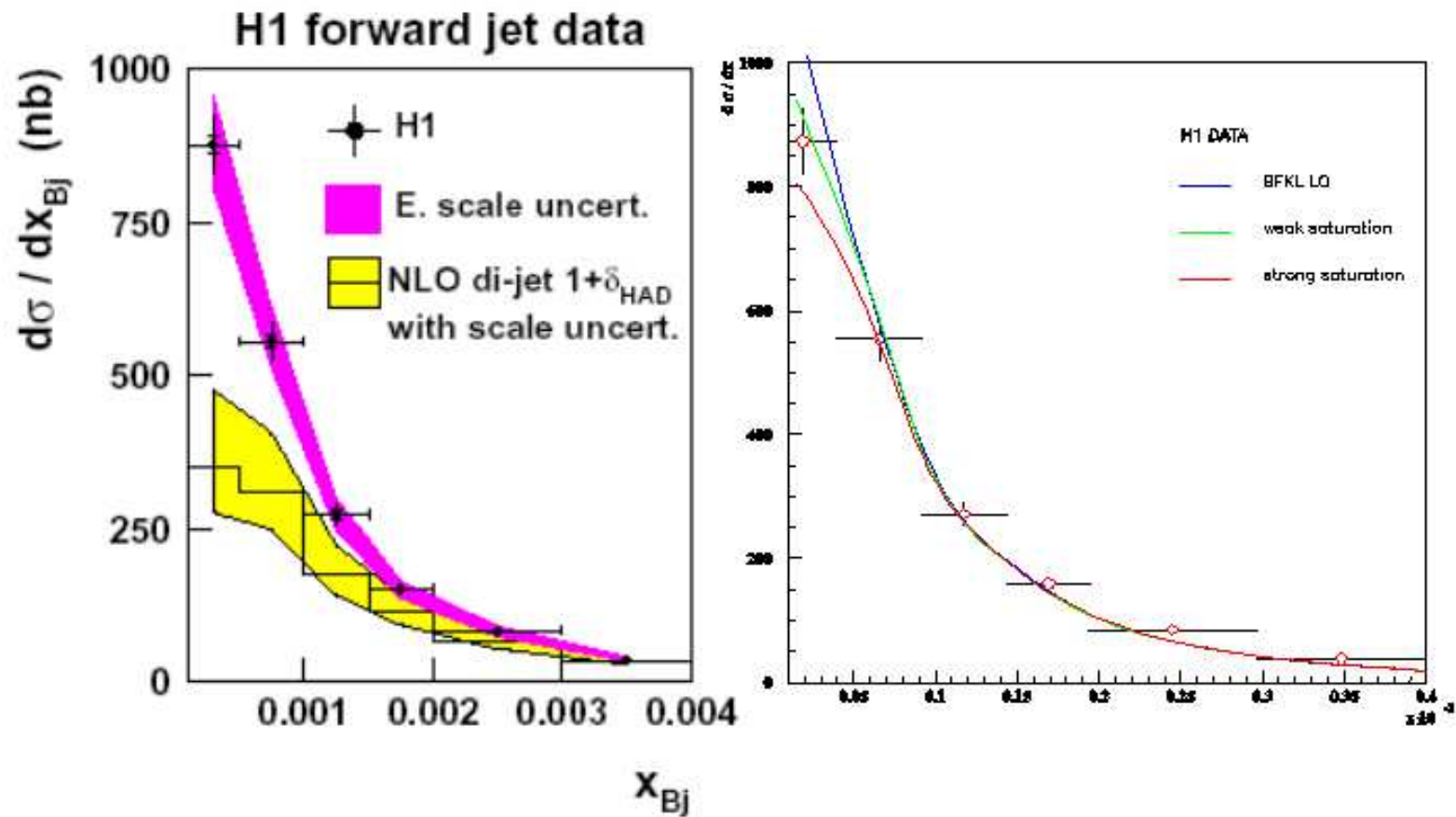
- $x, y, Q_2$ : usual kinematic variables of DIS
- $x_j, k$ : longitudinal and transverse momentum of the jet
- $\Delta\eta = \log(x_j/x)$ : rapidity interval

$$\frac{d\sigma}{dk dQ^2 dk_j dk^2} = \frac{\alpha g_p(x_j, k^2)}{2xk^2 Q^2} \left\{ \frac{y^2 d\sigma_T}{2 dk^2} + (1-y) \left( \frac{d\sigma_T}{dk^2} + \frac{d\sigma_L}{dk^2} \right) \right\}$$

with the hard cross-section given by

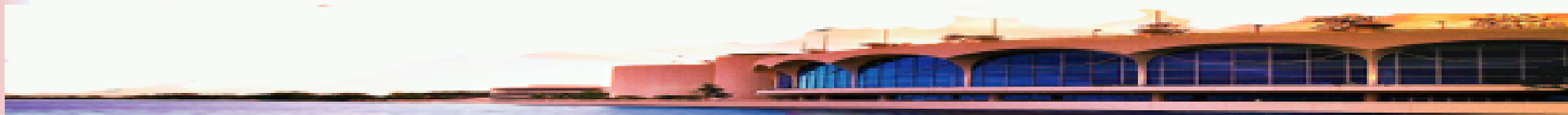
$$\frac{d\sigma_{T,L}}{dk^2} = \int d^2r_1 d^2r_2 \left| \Psi_{T,L}(r_1, Q^2) \right|^2 \frac{J_0(kr_2)}{2\pi r_2} \frac{\partial}{\partial r_2} r_2 \frac{\partial}{\partial r_2} \sigma_{(gg)d}(\Delta\eta, r_1, r_2)$$

# Predictions for H1 preliminary data



# Resummations

Methods for systematic calculation  
of perturbative cross sections  
depending on several momentum scales





# Computation of NNNLO-NLL logarithms in threshold resummation (N. Kidonakis)

## NNNLO master formula

$$\begin{aligned}
\sigma^{(3)} &= \sigma^B \frac{\alpha_s^3(\mu_R^2)}{\pi^3} \frac{1}{8} c_3^2 \mathcal{D}_5(s_4) \\
&+ \sigma^B \frac{\alpha_s^3(\mu_R^2)}{\pi^3} \left\{ \frac{5}{8} c_3^2 c_2 - \frac{5}{2} c_3 X_3 \right\} \mathcal{D}_4(s_4) + \frac{\alpha_s^{d_{as}+3}(\mu_R^2)}{\pi^3} \frac{5}{8} c_3^2 A^c \mathcal{D}_4(s_4) \\
&+ \sigma^B \frac{\alpha_s^3(\mu_R^2)}{\pi^3} \left\{ c_3 c_2^2 + \frac{c_2^2}{2} c_1 - \zeta_2 c_3^2 + (\beta_0 - 4c_2) X_3 + 2c_3 X_2 - \sum_j C_j \frac{\beta_0^2}{48} \right\} \mathcal{D}_3(s_4) \\
&+ \frac{\alpha_s^{d_{as}+3}(\mu_R^2)}{\pi^3} \left\{ \frac{1}{2} c_3^2 T_1^c + \left[ 2c_3 c_2 - \frac{\beta_0}{2} c_3 - 4X_3 \right] A^c + c_3 F^c \right\} \mathcal{D}_3(s_4) \\
&+ \sigma^B \frac{\alpha_s^3(\mu_R^2)}{\pi^3} \left\{ \frac{3}{2} c_3 c_2 c_1 + \frac{1}{2} c_2^2 - 3\zeta_2 c_3^2 c_2 + \frac{5}{2} \zeta_3 c_3^2 + \left( -3c_1 + \frac{27}{2} \zeta_2 c_3 \right) X_3 \right. \\
&\quad \left. + (3c_2 - \beta_0) X_2 - \frac{3}{2} c_3 X_1 - \sum_i C_i \frac{\beta_1}{8} + \sum_j \frac{\beta_0^2}{16} B_j^{(1)} + \sum_j \frac{3}{32} C_j \beta_1 \right. \\
&\quad \left. + \sum_j C_j \frac{\beta_0}{16} \left[ \beta_0 \ln \left( \frac{\mu_R^2}{M^2} \right) + 2K \right] \right\} \mathcal{D}_2(s_4) \\
&+ \frac{\alpha_s^{d_{as}+3}(\mu_R^2)}{\pi^3} \left\{ \left( \frac{3}{2} c_3 c_2 - 3X_3 \right) T_1^c + \frac{3}{2} \left[ c_2 + c_3 \ln \left( \frac{M^2}{s} \right) \right] F^c \right. \\
&\quad \left. + \left[ \frac{3}{2} c_2^2 + \frac{3}{2} c_3 c_1 - 3\zeta_2 c_3^2 + 3X_2 + \frac{\beta_0^2}{4} - \frac{3}{4} \beta_0 \left( c_2 - \frac{c_3}{2} \ln \left( \frac{\mu_R^2}{M^2} \right) \right) \right. \right. \\
&\quad \left. \left. - \frac{3\beta_0}{8} c_3 \ln \left( \frac{M^2}{s} \right) \right] A^c + \frac{3}{2} c_3 G^c + \frac{1}{2} K_3^c \right\} \mathcal{D}_2(s_4) + \dots
\end{aligned}$$

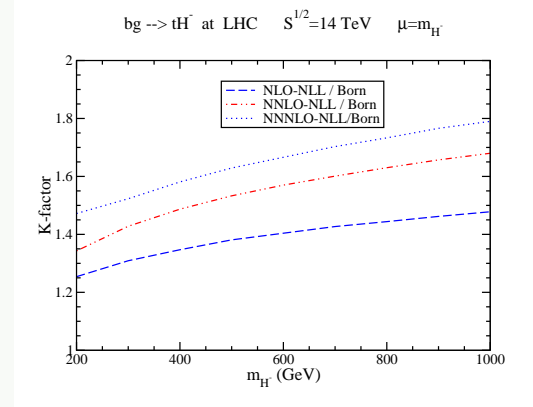
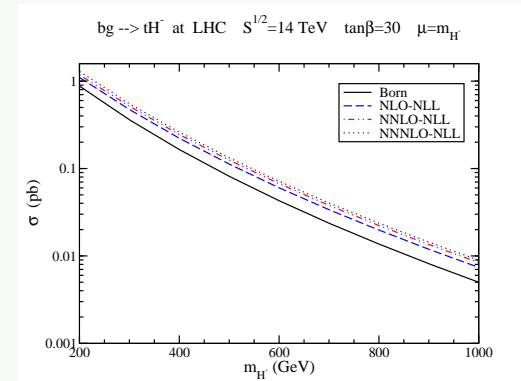
$$\text{Here } X_3 = (\beta_0/12)c_3 - \sum_j C_j \beta_0/24$$

$$X_2 = -(\beta_0/4)T_2 + (\beta_0/8)c_3 \ln(\mu_R^2/M^2) + c_3 K/4 - \sum_j (\beta_0/8) B_j^{(1)}$$

$$X_1 = c_2 c_1 - \zeta_2 c_3 c_2 + \zeta_3 c_3^2 + (\beta_0/4) \zeta_2 c_3 - \sum_j C_j (\beta_0/8) \zeta_2 - C_{D_0}^{(2)}$$

$$\begin{aligned}
K_3^c &= \text{tr} \left[ H^{(0)} \left( \Gamma_S^{(1)\dagger} \right)^3 S^{(0)} + H^{(0)} S^{(0)} \left( \Gamma_S^{(1)} \right)^3 \right. \\
&\quad \left. + 3 H^{(0)} \left( \Gamma_S^{(1)\dagger} \right)^2 S^{(0)} \Gamma_S^{(1)} + 3 H^{(0)} \Gamma_S^{(1)\dagger} S^{(0)} \left( \Gamma_S^{(1)} \right)^2 \right]
\end{aligned}$$

## NNNLO soft-gluon corrections for charged Higgs production

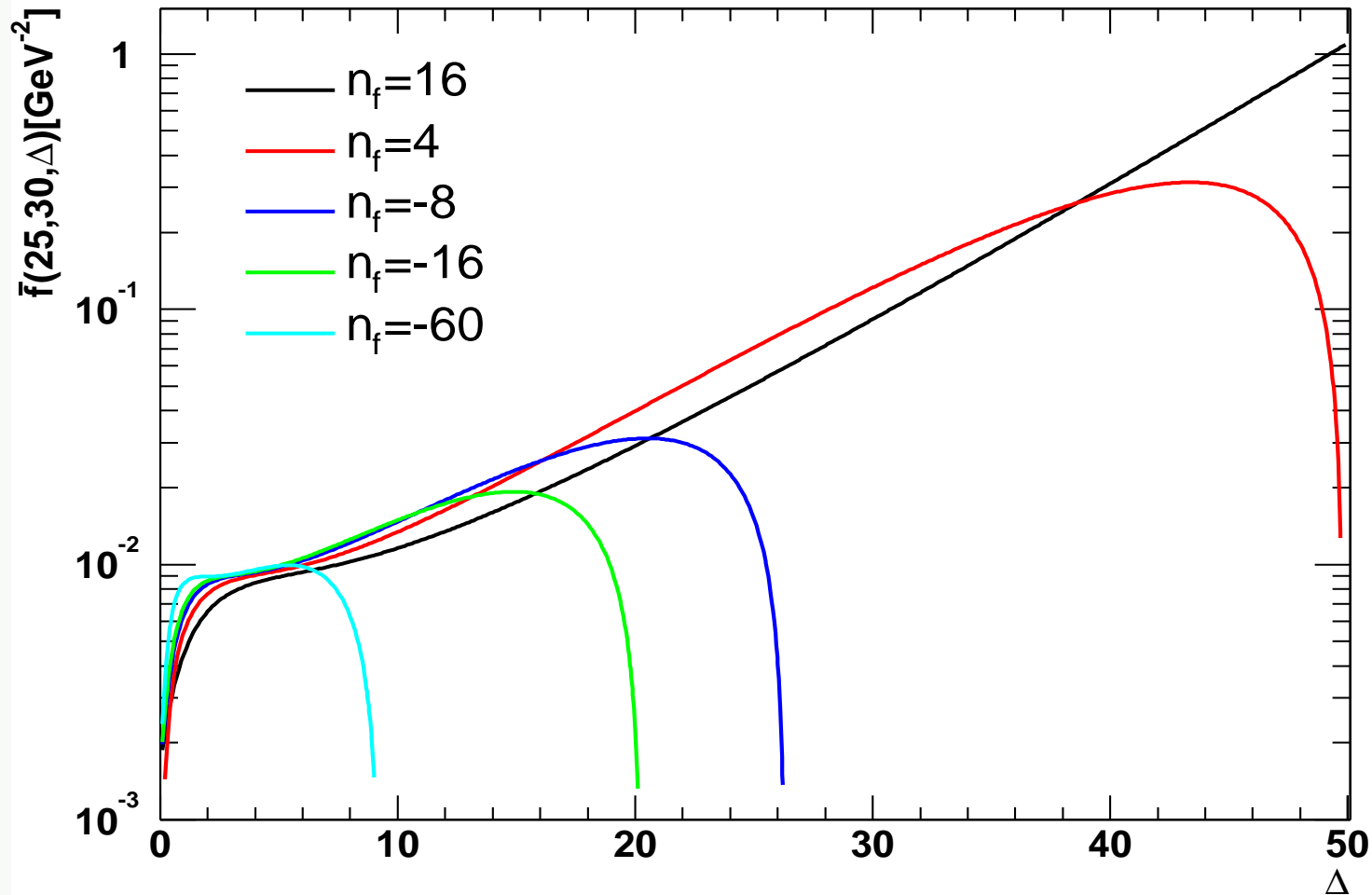


## Solving NLL BFKL by iteration (J. Andersen)

We propose an iterative approach to the BFKL equation at NLLA that solves the equation with *no approximations*

- Directly in the physical rapidity and transverse momentum space  
(avoids the use of the troublesome Mellin transform completely)
- The right language for use of impact factors (physics predictions!)
- Hopeful in extending the approach to final state studies like at LL
- Expresses the solution in terms of effective vertices and no-emission probabilities (physical insight into the BFKL solution at NLLA!)

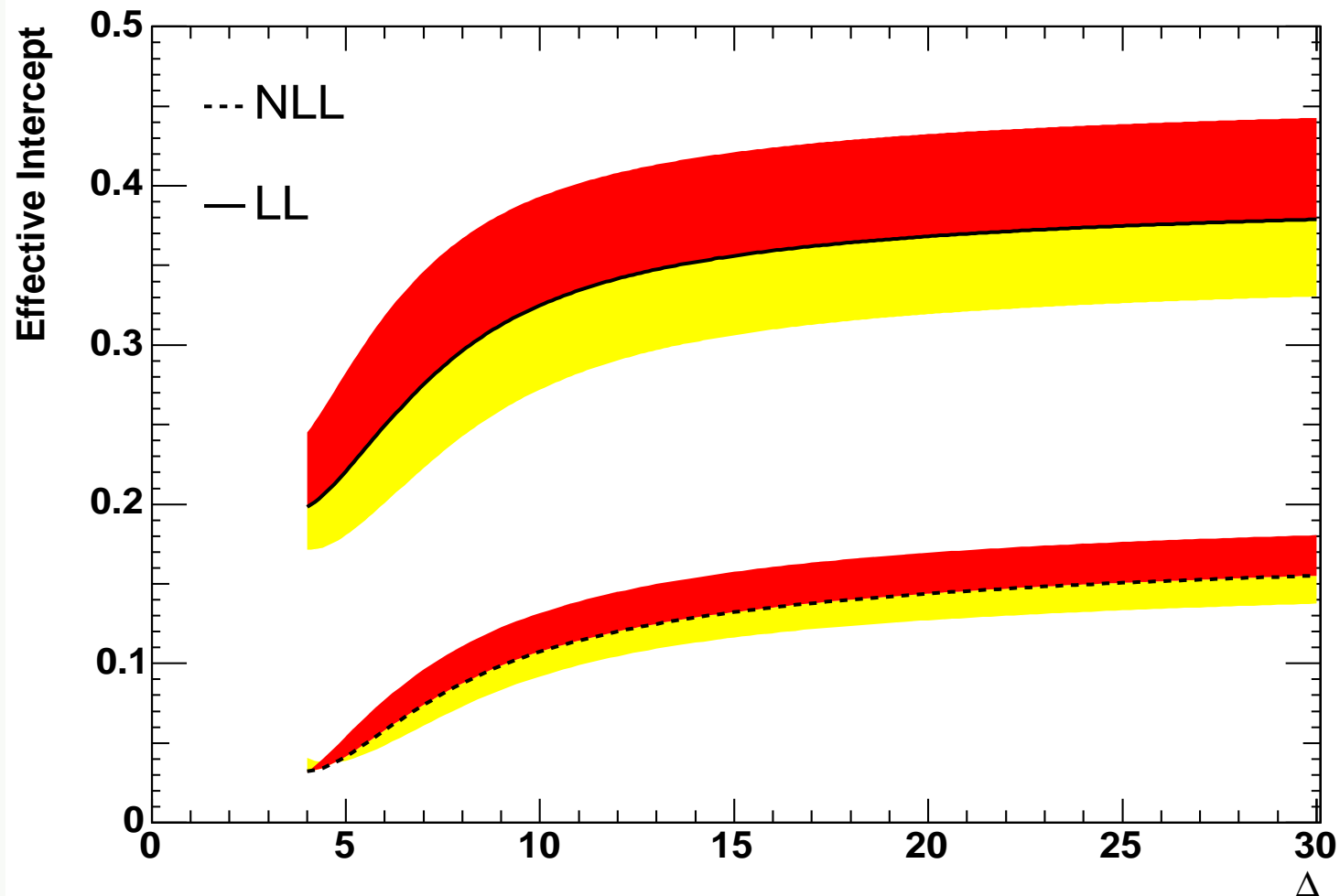
# Leading Log tools at NLL



!!this would be a major catastrophe!!

# BFKL Intercept

QCD,  $n_f = 4$ , one loop running

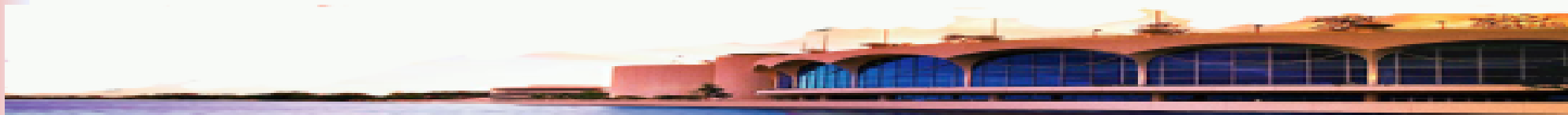


## Transverse momentum resummation at small $x$

*(F. Olness, in collaboration with S. Berge, P. N., and C.-P. Yuan)*

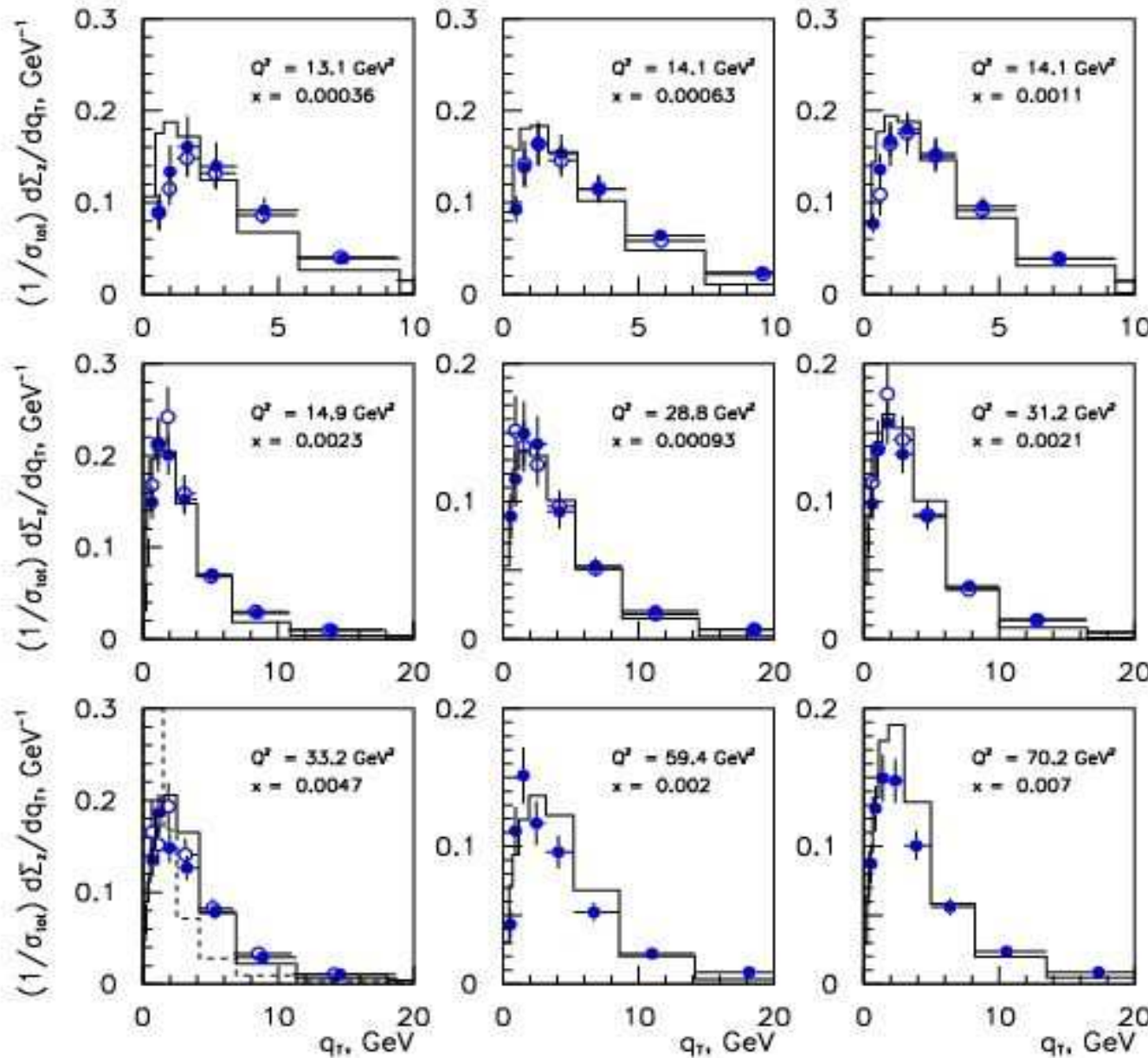
Universality of soft-gluon resummation at small  $q_T$  in the Drell-Yan process and current region of SIDIS

$\Rightarrow$  predictions for Drell-Yan  $q_T$  distributions at  $x < 10^{-2}$  based on HERA  $E_T$  data



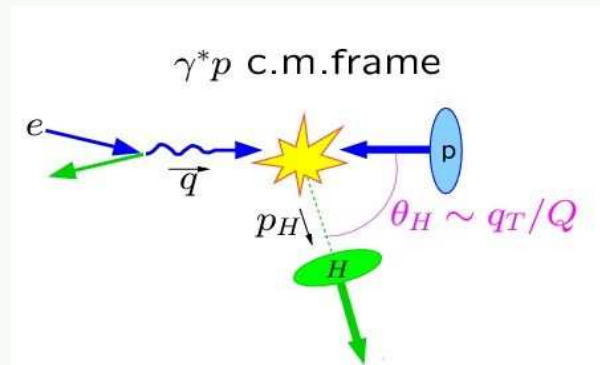


# Differential energy flow at small-x???



$$\frac{d\Sigma_z}{dx dQ^2 dq_T}$$

$$d\Sigma_z = \int z \frac{d\sigma}{dz}$$

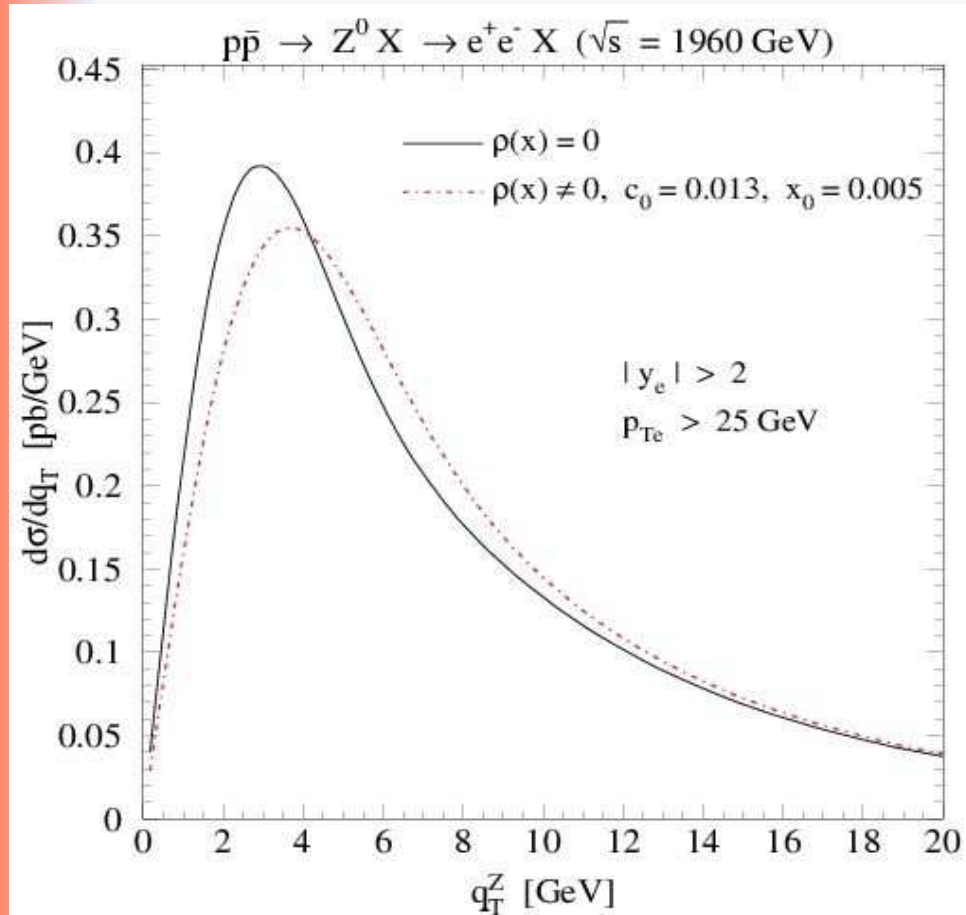


Extra  $q_T$  broadening  
for  $x < 10^{-2}$

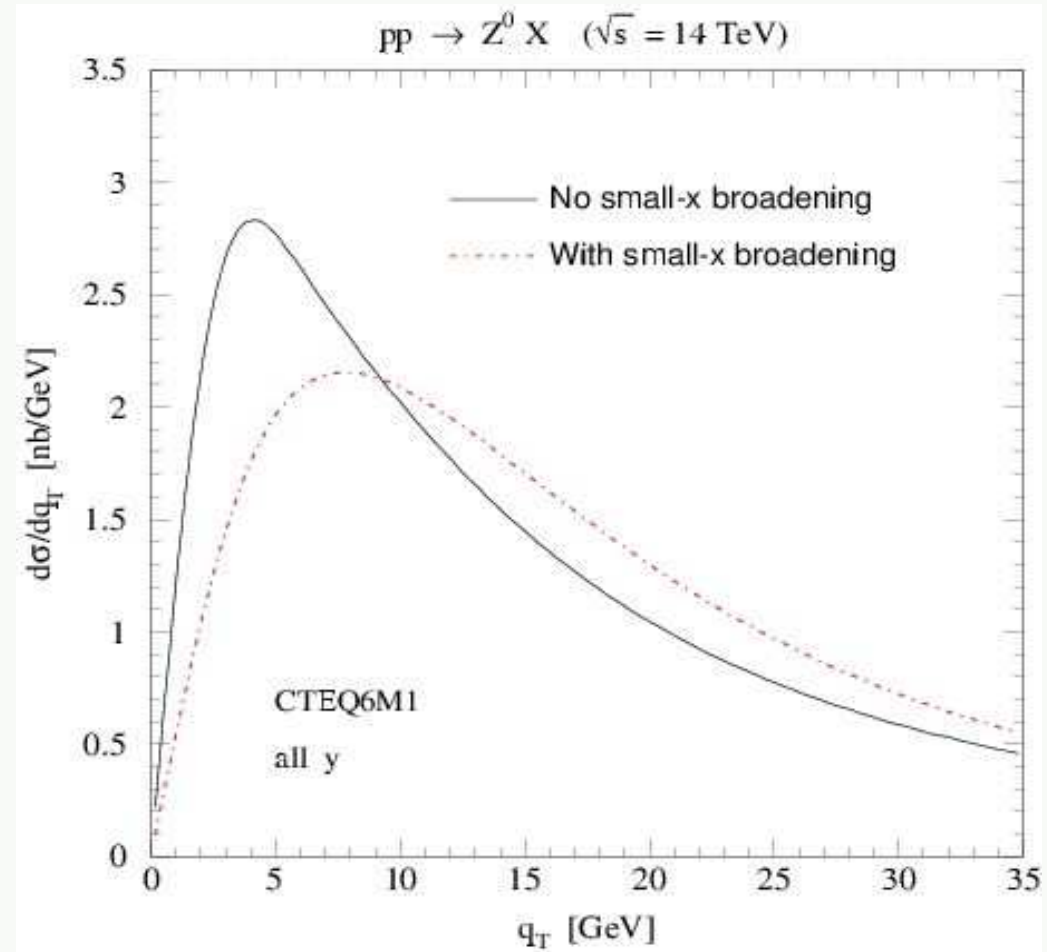
H1 Collaboration,  
PL B356, 118 (1995)  
EPJ C12.595 (2000)

# Z Production: Tevatron & LHC

## Tevatron



## LHC

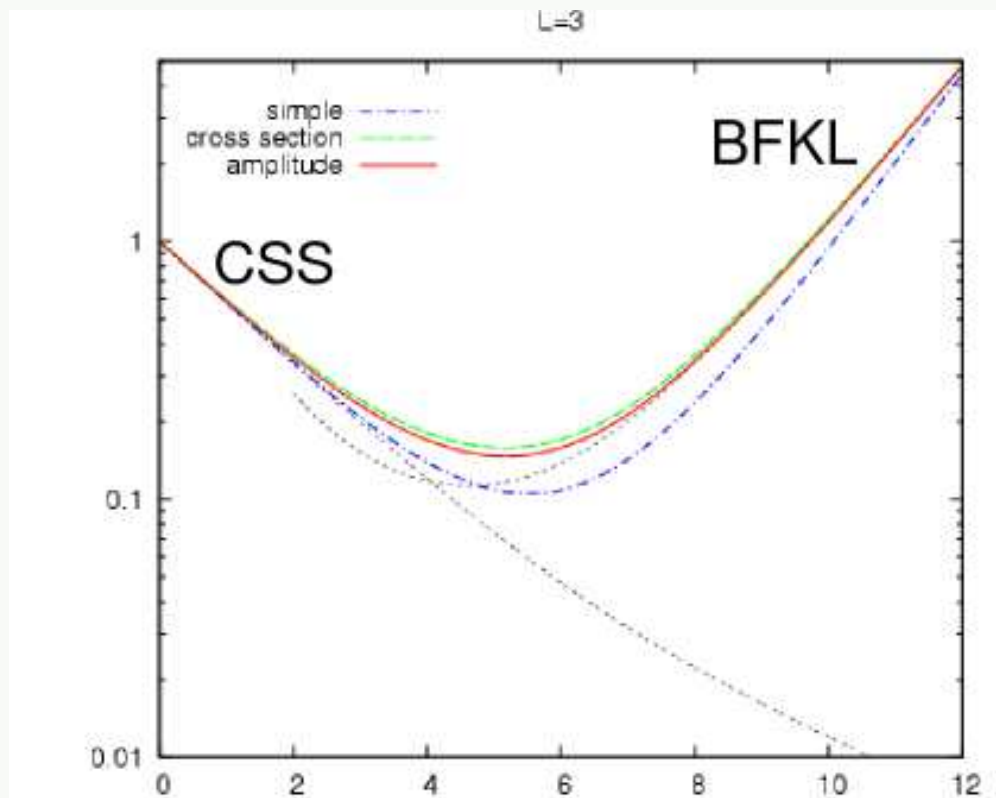


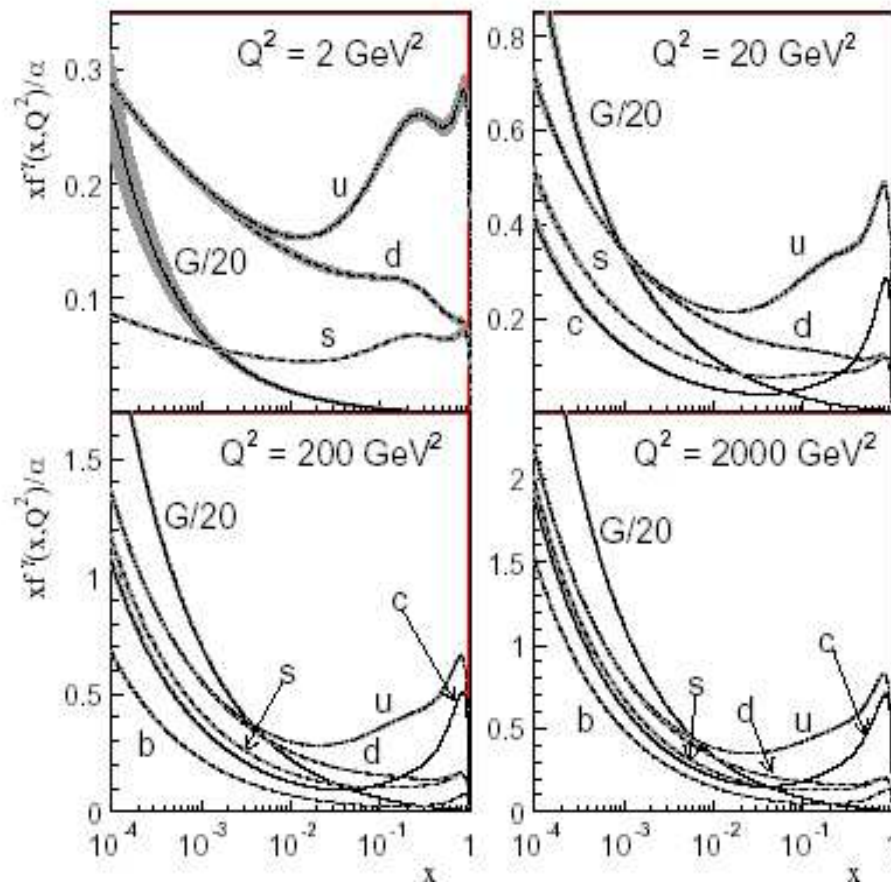
With cuts on  $y_e$  and  $p_{Te}$

No y cut necessary !!!



Merging CSS and BFKL resummations for  
interjet particle production at high energies (A. Kyrieleis)





## SAL PDFs

The bands mark the fit uncertainty.

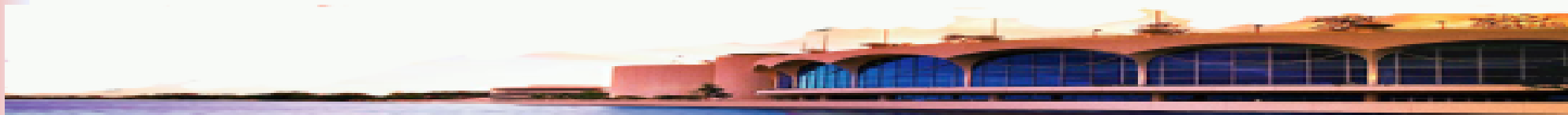
New parametrization of photon PDF's from ee and ep data (A. Levy)

## Pentaquarks:

critical examination of the (absence) of the evidence

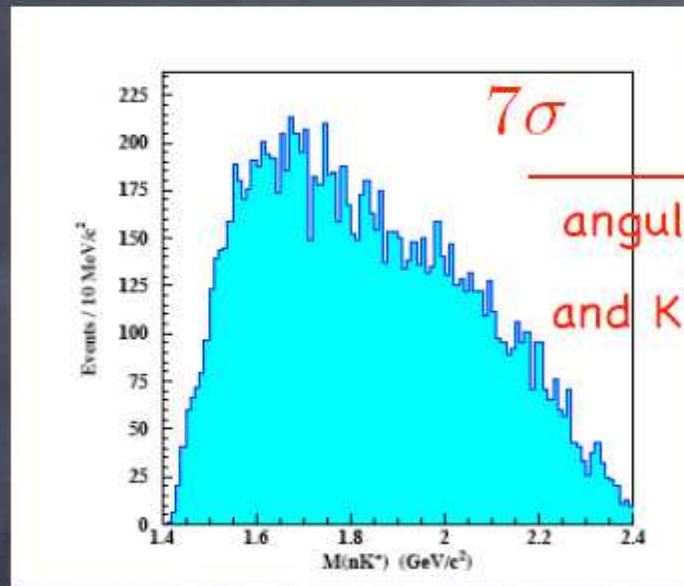
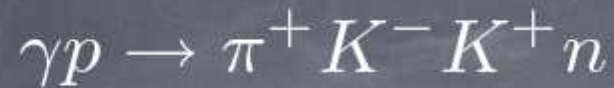
(A. Szczepaniak, based on hep-ex/0412077 with A. Dzierba and C. Mayer)

- ❑ Statistical significance of the discovery reports
  
- ❑ Conventional sources of spurious peaks
  - Kinematical reflections
  - Hidden particle exchanges
  - Kinematical cuts

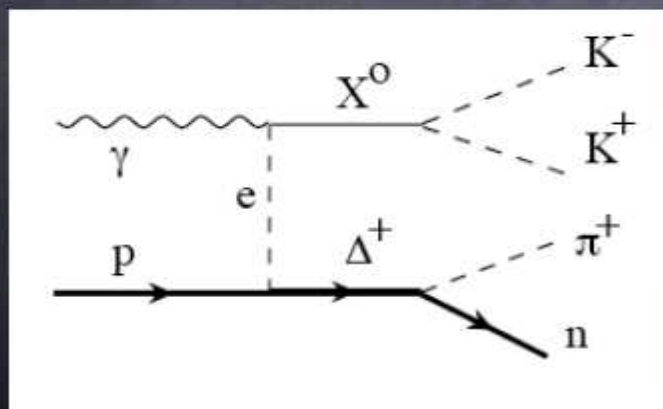
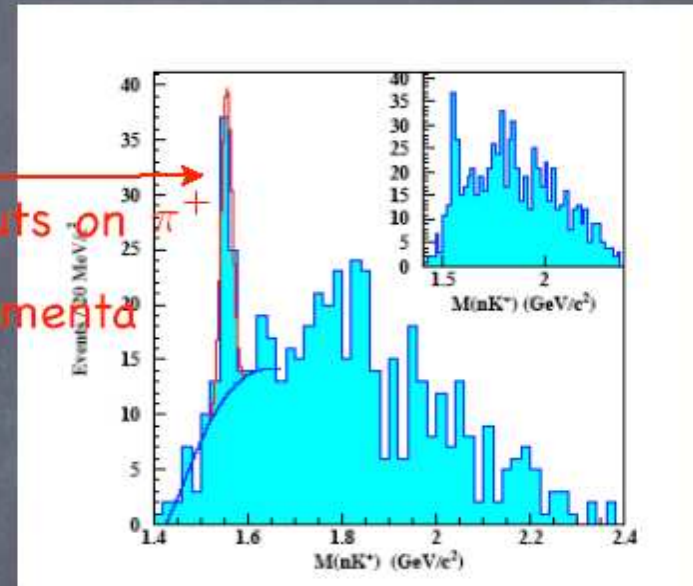




CLAS (proton)



angular cuts on  
and  $K^+$  momenta

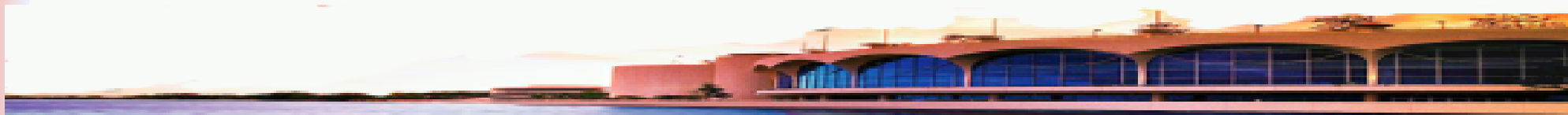


Can generate resonance-like structure in  $K^+K^-n$  spectrum and  $\pi^+$  momentum cut enhances kinematic reflections from decays of  $K^+K^-$  resonances

not an explanation of the actual pentaquark data!

Pentaquark sightings come from low statistics, low resolution, low-energy experiments with kinematically constrained final states after complicated cuts are imposed.

High resolution, high statistics, experiments with both low- and high- particle multiplicity do not report the pentaquarks.



DIS 2005 April 27-May 1, 2005 Madison, Wisconsin U.S.A.

## New possible insight into JLab proton polarization data puzzle by DIS

A. Z. Dubničková<sup>1</sup>,  
S. Dubnička<sup>2</sup>,

**Proton** is compound of **quarks**  $\Rightarrow$  **non-pointlike** - in EM interactions it **manifests EM structure** to be described (equally well neutron EM structure) by **two independent scalar functions (form factors FF's) of one variable**  $t = -Q^2$ , the squared four-momentum transferred by the exchanged virtual photon.

There is some **freedom in the choice of proton EM FF's**.

The most suitable in extracting of experimental information are **Sachs electric**  $G_{Ep}(t)$  and **magnetic**  $G_{Mp}(t)$  FF's, giving in the Breit frame the **charge and magnetization distributions** within the proton, respectively.

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## Conclusions

- ❑ Progress is made towards understanding of various aspects of hadroproduction
- ❑ Many questions remain, especially related to QCD physics at energies accessible at the LHC
- ❑ Systematic study of perturbative corrections, resummations, and non-perturbative models must go on in order to meet objectives of the LHC physics program

