# Measurements of the Structure Functions $F_2(x,Q^2)$ and $F_L(x,Q^2)$ at low $Q^2$

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**Abstract.** Recent measurements of the proton structure function  $F_2$  and determination of the structure function  $F_L$  in  $e^+p$  deep inelastic scattering (DIS) by the H1 Collaboration are summarized. The  $F_2$  results presented here extend the previous measurements at HERA into the  $Q^2$  region below 1 GeV<sup>2</sup> by also using Initial State Radiation (ISR) events. The  $F_L$  structure function determined in the current analysis is more precise and accesses lower  $Q^2$  values as compared to previous determinations published by H1.

**Keywords:**  $F_2$  proton structure function, longitudinal proton structure function, DIS, HERA, H1, initial state radiation, low  $Q^2$ , low x **PACS:** 13.85.Lg

### **INTRODUCTION**

At low  $Q^2$  the DIS double-differential cross section can be expressed as:

$$\frac{d^2\sigma}{dx\,dQ^2} \cdot \frac{Q^4x}{2\pi\alpha^2 Y_+} = \sigma_r = F_2(x,Q^2) - \frac{y^2}{Y_+} \cdot F_L(x,Q^2),\tag{1}$$

where  $Q^2$  is the squared four-momentum transfer, x is the Bjorken scaling variable,  $Y_+ = 1 + (1 - y)^2$ . The inelasticity  $y = Q^2/sx$  is a fraction of the lepton's energy loss and s denotes the center of mass energy squared of the lepton-nucleon system. For y < 0.6 the contribution of  $F_L$  is supressed by the kinematic factor  $y^2/Y_+$ . Therefore the measurement of  $\sigma_r$  at low y determines  $F_2$  with a small correction for  $F_L$ . At high y the contribution of the longitudinal structure function becomes significant which allows to determine  $F_L$ .

## **MEASUREMENT OF THE CROSS SECTION**

The data used in the analysis are taken by the H1 detector during special running periods with open triggers for inclusive DIS events. In order to access low values of  $Q^2$  around 1 GeV<sup>2</sup> the interaction vertex for the 2000 data was shifted by approximately 70 cm along the proton beam direction. This data sample is also used for accessing larger values of x with ISR events. Data collected in 1999 with a nominal position of the interaction vertex are used for measurements in the high y region and 1997 data for accessing of low values of y using QED Compton events (QEDC). A new ISR analysis method is applied where the radiative photon is not required to be measured in the photon detector. Details concerning the ISR analysis can be found in [1].

The kinematic reconstruction was done with two methods. The sigma method [2] has been used for medium and low y and the electron method was prefered at highest y due to better y resolution in this region. The H1 and ZEUS inclusuve cross sections measurements at low  $Q^2$  are shown in Fig. 1 together with the fixed target data.



**FIGURE 1.** Measurements of the cross section - H1 shifted vertex ISR data 2000 (closed points) [1], data from ZEUS BPT97 (closed triangles) [3], NMC (stars) [4], H1 QEDC97 (open points) [5], H1 shifted vertex preliminary data 2000 (open boxes) [6] and H1 preliminary data 1999 (closed boxes) [7]. The data are compared to the Fractal fit  $F_2$  [8] and dipol model  $F_L$  [9] (solid curve), to the ALLM97 [10] parameterization (dotted curve) and also to the H1 QCD fit [11] (dashed curve)

The preliminary results of the ISR analysis and the QEDC results from H1 extend the measured kinematic range at low  $Q^2$  towards higher x values.

## STRUCTURE FUNCTION $F_2$ AT LOW $Q^2$

The proton structure function  $F_2$  obtained from the inclusive cross section measurements rises towards low x for all measured  $Q^2$  bins. The detailed analysis of the x dependence of  $F_2$  is described in [12]. It was found that the x dependence of  $F_2$  at fixed  $Q^2$  exhibits a power law behaviour  $F_2 = c \cdot x^{-\lambda(Q^2)}$ . The result of fitting this form to the shifted vertex data [1] and [6], compared to published H1 [13] and ZEUS [3] data, is presented in Fig. 2.



**FIGURE 2.** The slope  $\lambda(Q^2)$  from the fit  $F_2 = c \cdot x^{-\lambda(Q^2)}$  to the H1 and ZEUS data.

One can see that the shifted vertex results are in agreement with previously published data in the regions of overlap. Deviation of  $\lambda(Q^2)$  from logarithmic dependence  $a \cdot \ln[Q^2/\Lambda^2]$  was observed around  $Q^2=1$  GeV<sup>2</sup>.

## THE EXTRACTION OF FL

Fig. 1 shows the rise of the cross section with decreasing x for fixed  $Q^2$ . However, for the lowest x, a turnover of the cross section can be seen. Lowest x corresponds to highest y and the contribution of  $F_L(x,Q^2)$  to the cross section is not negligible at such values of y. An extraction of  $F_L$  was done with a "shape method" [14]. It assumes the power behaviour of  $F_2$  and the difference in the shape between the cross section and  $F_2$  to be mostly driven by kinematic factor  $y^2/Y_+$ . Using the cross section, parametrised as  $\sigma_r = F_2 - y^2/Y_+ \cdot F_L$ ,  $F_L$  for a given  $Q^2$  was extracted by fitting. The results of such an  $F_L$  extraction, together with previously published H1 results and different QCD fits, are presented in Fig. 3.

Good agreement of the data and  $F_L$  determined by H1 [14], Alekhin's [17] and H1's QCD [11] fits is observed. However, MRST [16] and ZEUS [15] fits tend to be lower.



**FIGURE 3.**  $F_L$  obtained from H1 data compared to H1 QCD fit (dashed curve) [11], ZEUS NLO fit (dotted curve) [15], MRST NLO fit (dash-dotted curve) [16], Alekhin's fit (solid curve) [17]

## SUMMARY

The inclusive cross section measurements presented here extend the kinematic region covered by HERA at low  $Q^2$ . The ISR and QEDC data allow access medium and high x values. The  $F_L$  values determined in this analysis are significantly above zero everywhere and already now can discriminate between different predictions.

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