



# Introduction

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Besides being interesting in their own right, it is essential to know the parton density functions (PDFs) of the proton as precisely as possible in order to maximise the physics potential at both current and future colliders e.g. high-x gluon is dominating uncertainty in several LHC processes

HERA data are now very precise and cover a wide range in  $(x, Q^2)$

▶ **determination of proton PDFs now possible within one experiment**

Most recently, ZEUS have performed a NLO QCD analyses on their full set of HERA-I  $e^+$  and  $e^-$  structure function data and high precision jet data → the [ZEUS-JETS PDF](#)

With future measurements at HERA, hope to be able to do even better ...

**Presented here are the results of studies that give a first look at the potential impact of future HERA measurements on the proton PDFs:**

- 1. within current HERA-II running scenario**
  - increased luminosity
  - cross sections optimised for sensitivity to PDFs
- 2. other running scenarios: low energy ( $F_L$ ),  $eD$  (sea quark asymmetry)**

# Determination of proton PDFs at HERA

**Factorisation: observable = short range interaction  $\otimes$  PDFs**

Observables used in QCD fits to determine PDFs:

- Inclusive NC/CC DIS ep cross sections  $\rightarrow$

$$\frac{d^2\sigma(\mathbf{e}^\pm p)}{dx dQ^2} \sim Y_+ F_2 - y^2 F_L \square Y_- x F_3; Y_\pm = 1 \pm (1-y)^2$$

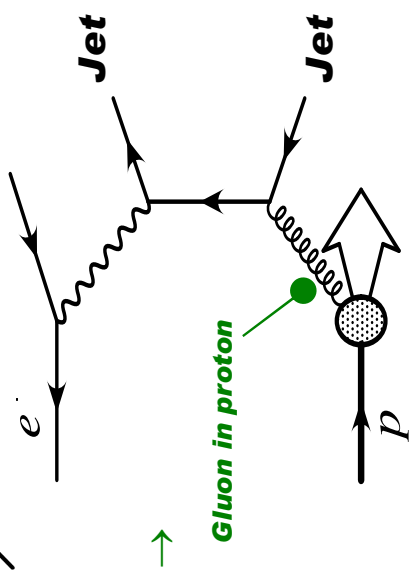
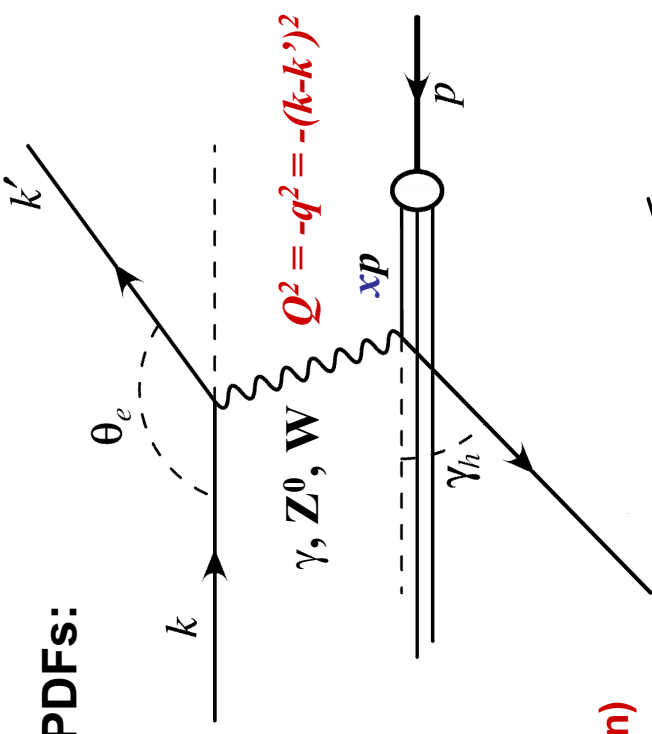
$F_2 \sim \sum x(q_i + \bar{q}_i)$  Dominates  
 $x F_3 \sim \sum x(q_i - \bar{q}_i)$  High  $Q^2$   
 $F_L \sim \alpha_s \cdot x g(x, Q^2)$  High  $y$  ( $\geq NLO$ )

$\times$  direct sensitivity to quarks

$\times$  only indirect sensitivity to gluon (scaling violation)

- Jet cross sections:

$\times$  directly sensitive to gluon through boson-gluon-fusion  $\rightarrow$



Now, after the HERA-I (94-00) phase of data-taking, the full set of inclusive NC/CC  $e^+e^-$  data, and high precision jet data are available for QCD analysis...

# ZEUS-JETS NLO QCD fit

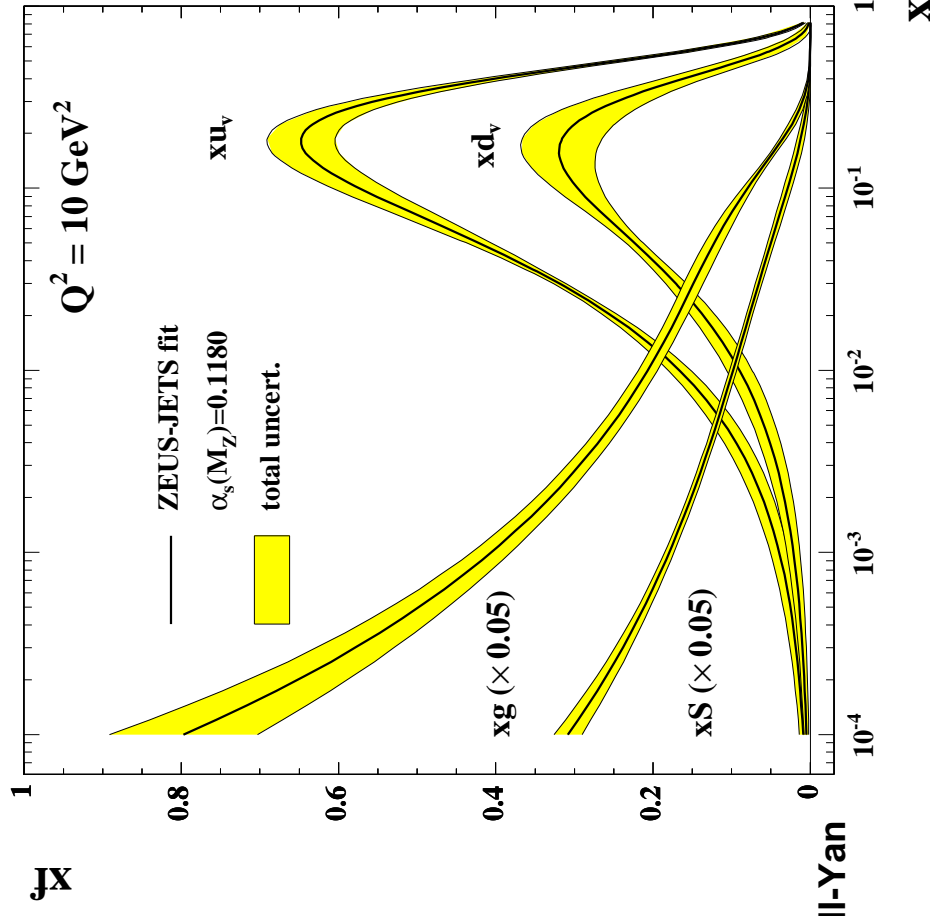
For more details on the ZEUS-JETS fit (hep-ph/05030274), and the data included, see cont. to this workshop, “Proton PDFs using Structure Functions and Jet Data from **Data!**”, Juan Terron.

all HERA-I ZEUS incl. NC/CC e <sup>+</sup> /e <sup>-</sup> (94-00)
ZEUS inclusive jets in DIS (96-97)
ZEUS dijets in photoproduction (96-97)

## Parameterisation:

PDF	Param. at $Q_0^2 = 7 \text{ GeV}^2$
u-val. ( $xu_v$ )	$A_{uv} x^{bu_v} (1-x)^{cu_v} (1+d_{uv}x)$
d-val. ( $xd_v$ )	$A_{dv} x^{bd_v} (1-x)^{cd_v} (1+d_{dv}x)$
total sea (xS)	$A_S x^{bs} (1-x)^{cs}$
gluon (xg)	$A_g x^{bg} (1-x)^{cg} (1+d_gx)$
dbar-ubar ( $x\Delta$ )	$A_\Delta x^{b\Delta} (1-x)^{c\Delta}$

- parameter constraints:
  - x momentum and quark number sum rules
  - x low-x behaviour of  $u_v$  and  $d_v$  set equal
  - x  $\Delta$  set consistent with Gottfried sum and Drell-Yan
- ▶▶ **11 free parameters in total**
- heavy quarks treated in variable flavour number scheme of Thorne and Roberts
- **uncertainties evaluated using Offset Method**

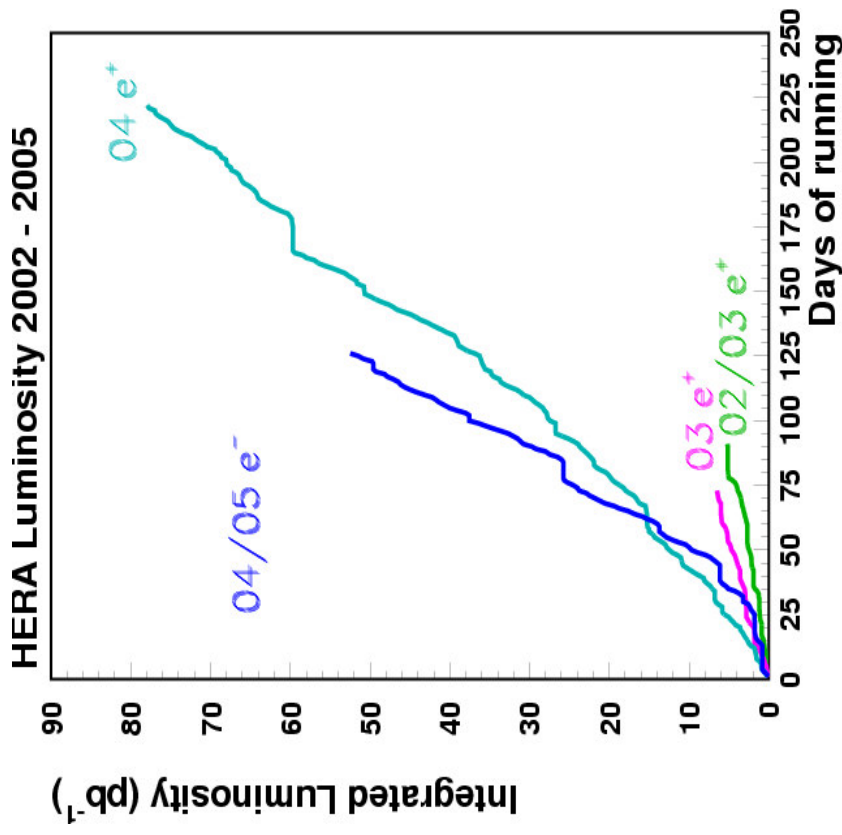


**PART I:**  
**Impact of future HERA measurements**  
**on the ZEUS PDF fit: within current**  
**HERA-II running scenario**

# Current HERA-II running scenario

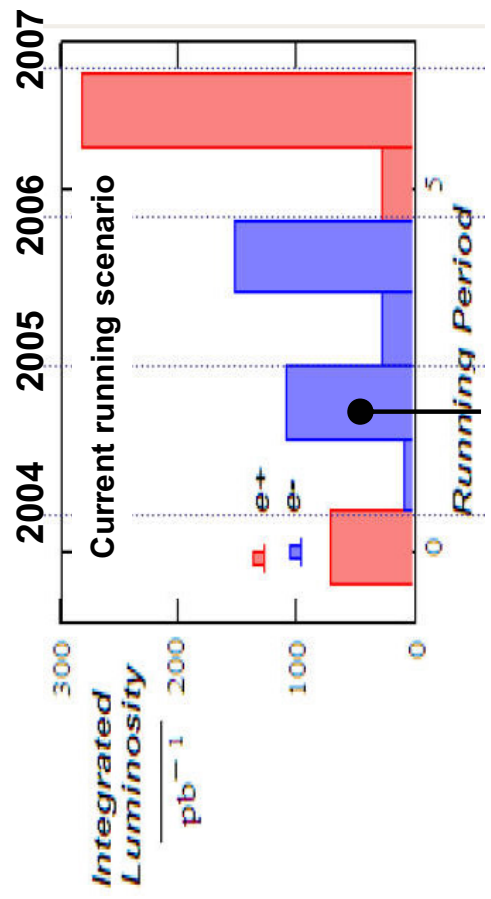
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- HERA-II is running efficiently...



**HERA delivered luminosity ( $pb^{-1}$ )**

	HERA-I (92-00)	HERA-II (02 → )
$e^+$	165	90
$e^-$	27	> 50



**We are here...**

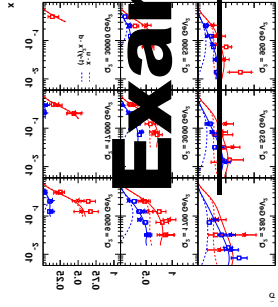
“ 700 $pb^{-1}$  integrated luminosity, equally divided between  $e^+/e^-$ , expected by the end of HERA-II running in mid-2007 ”

# What impact will future HERA measurements have on the PDFs?

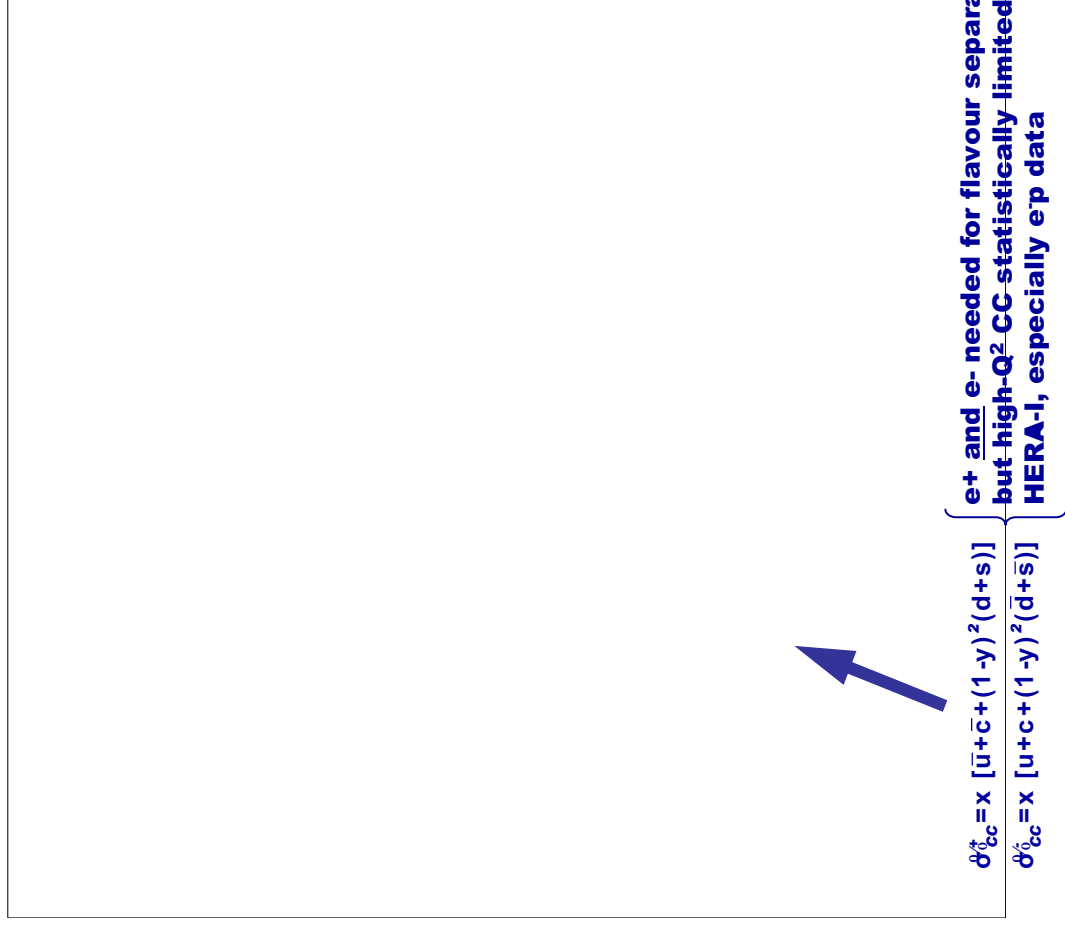
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Where does the information come from in a HERA-Only fit ?

<b>Valence</b>	<b>High <math>Q^2</math> inclusive NC/CC <math>e^\pm</math> cross sections</b>	HERA-I: statistics limited
<b>Sea</b>	Low-x from inclusive NC DIS High-x ? Flavour ? (assumptions needed)	
<b>Gluon</b>	Low-x from HERA $dF_2/d\ln Q^2$ Mid-to-high-x from HERA jet data High-x from momentum sum rule	HERA-I: statistics limited at high- $E_T$ and high- $Q^2$



# Example: high-Q<sup>2</sup> NC and CC data



**F<sub>2</sub> dominates NC cross section, HERA-I: δF<sub>2</sub>/F<sub>2</sub> ~ 30%**

- HERA-II will provide greatly increased luminosity



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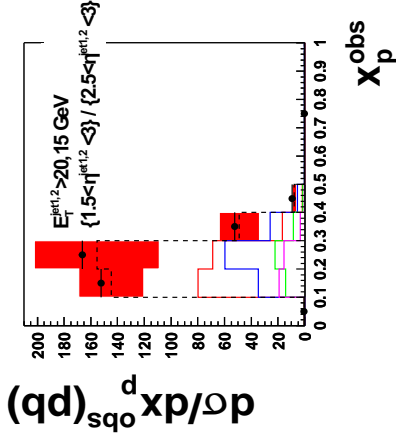
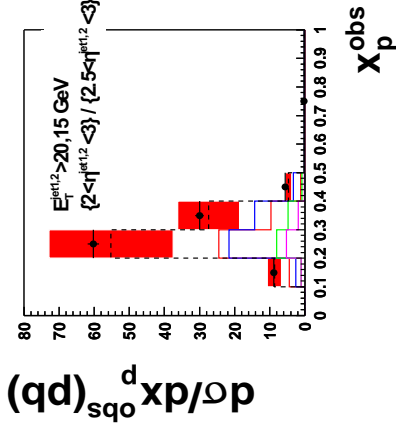
HERA-I: measurements in only certain kinematic regions  
 → potential to optimise cuts for sensitivity to gluon

# Optimised jet cross sections

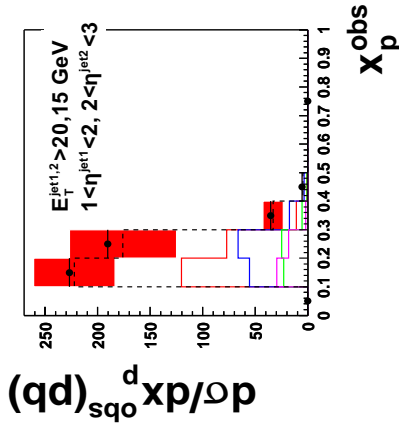
Christopher Targett-Adams (UCL)

- Measure jet cross sections in kinematic regions “optimised” for sensitivity to gluon
- ongoing ZEUS study: dijets in photoproduction ( $Q^2 < 1 \text{ GeV}^2$ )
- data simulated using NLO QCD (Frixione-Ridolfi) and CTEQ5M1 proton PDF (500 pb<sup>-1</sup>)

**resolved-photon enhanced:  $x_y^{OBS} < 0.75$**



**direct-photon enhanced:  $x_y^{OBS} > 0.75$**



- ZEUS Simulated Data (500 pb<sup>-1</sup>)
- NLO (ZEUS-S)
- Gluon PDF error (ZEUS-S)
- Gluon component (ZEUS-S)
- Up Valence component (ZEUS-S)
- Down Valence component (ZEUS-S)
- Sea component (ZEUS-S)

$E_T^{jet1,2} > 20, 15 \text{ GeV}$   
 $1 < \eta^{jet1} < 2, 2 < \eta^{jet2} < 3$

$E_T^{jet1,2} > 30, 25 \text{ GeV}$   
 $1 < \eta^{jet1}, \eta^{jet2} < 2$

$E_T^{jet1,2} > 35, 30 \text{ GeV}$   
 $-1 < \eta^{jet1}, \eta^{jet2} < 2.5$

# Impact of HERA-II in current running scenario:- case study

Data sample	L of HERA-I measurement (pb <sup>-1</sup> )	assumed L of HERA-II measurement (pb <sup>-1</sup> )	Central values taken from...	Systematic uncertainties taken from...
High-Q <sup>2</sup> NC e+	63	350	existing	existing data
High-Q <sup>2</sup> NC e-	16	350	existing data	existing data
High-Q <sup>2</sup> CC e+	61	350	existing data	existing data
High-Q <sup>2</sup> CC e-	16	350	existing data	existing data
Inclusive DIS jets	37	500	existing data	existing data
Dijets in $\gamma p$	37	500	existing data	existing data

## statistically limited data-sets

- scale statistical uncerts. on existing data assuming max. 700 pb<sup>-1</sup> (equally between e+/e-)
- systematic uncertainties taken from existing data

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Optimised dijets in $\gamma p$	-	500	NLO QCD	NOT INCLUDED

## statistically limited data-sets

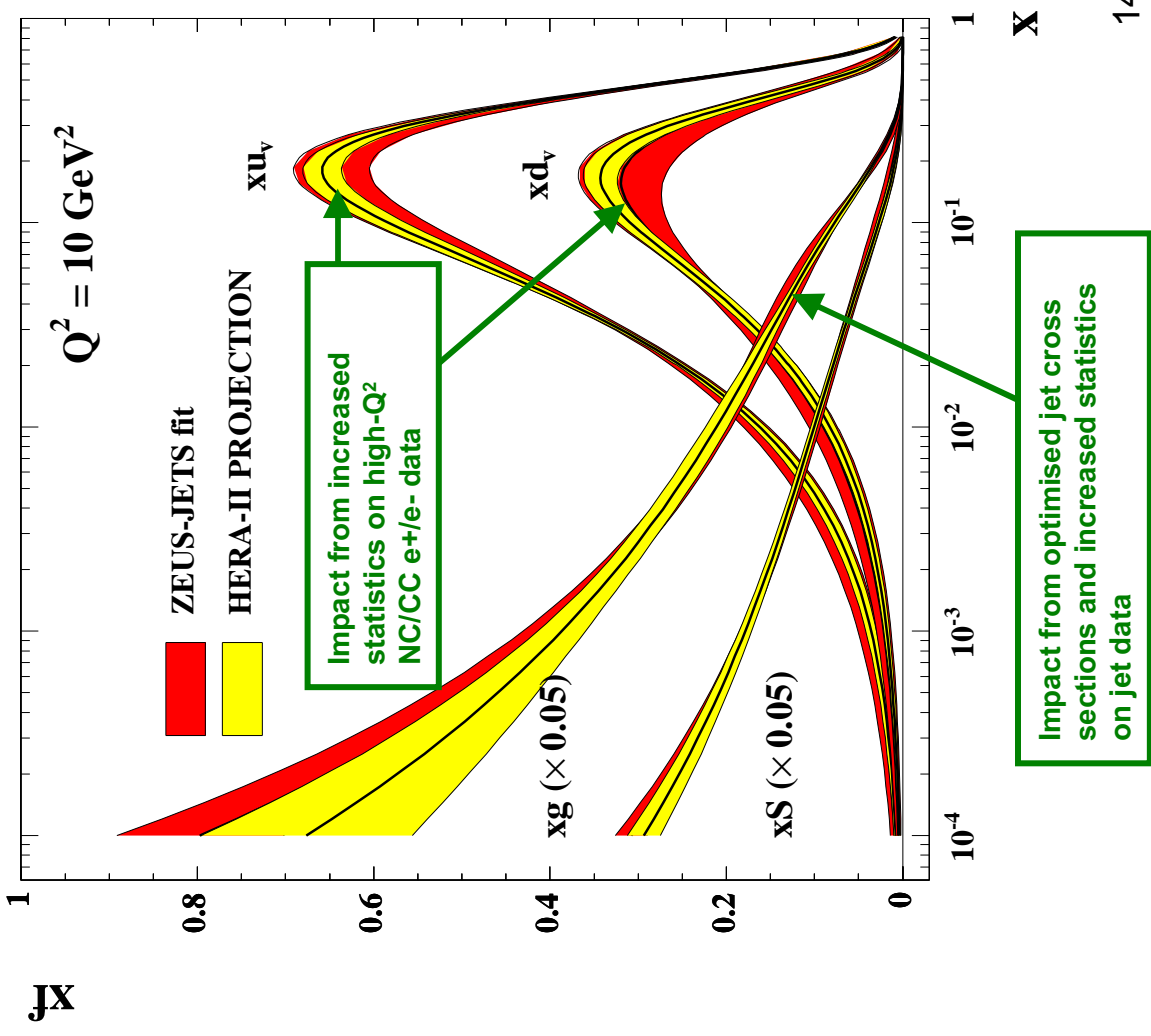
- scale statistical uncerts. on existing data assuming max. 700 pb<sup>-1</sup> (equally between e+/e-)
- systematic uncertainties taken from existing data

## optimised jet cross sections

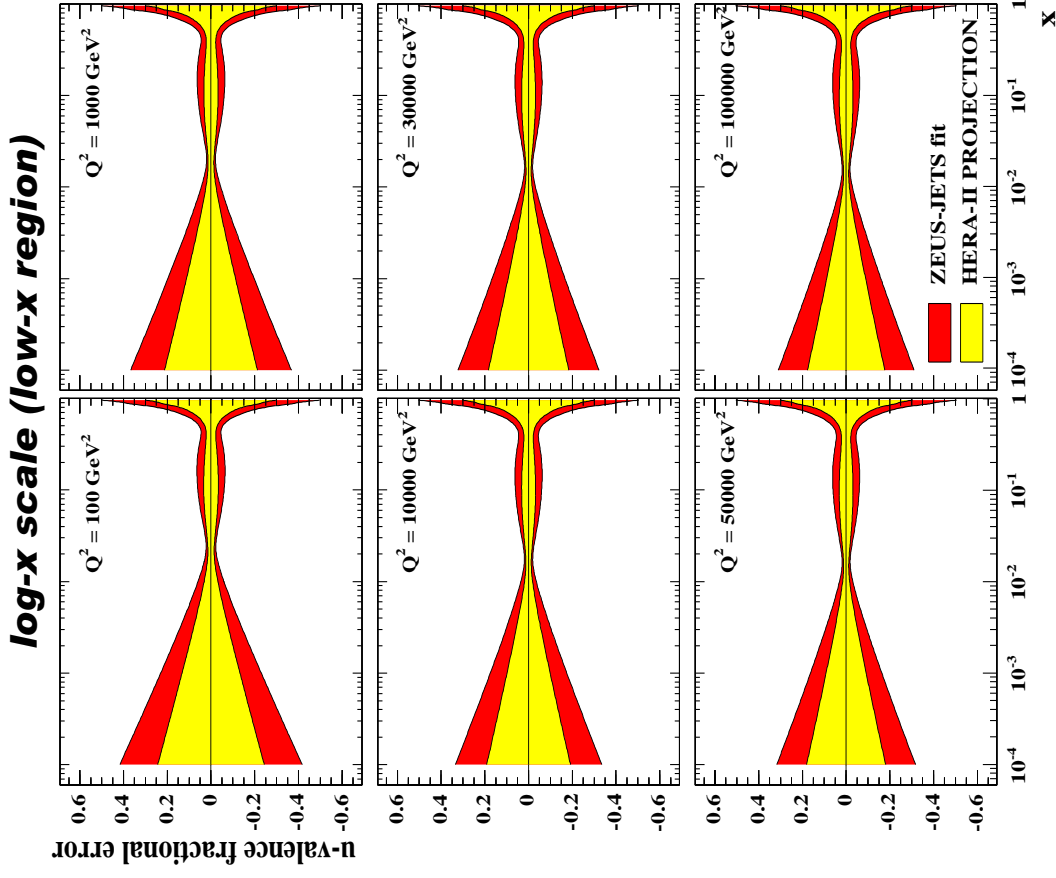
- include simulated data-points from NLO QCD, statistical uncertainties assume 500 pb<sup>-1</sup>
- no systematics included

# HERA-II projected fit

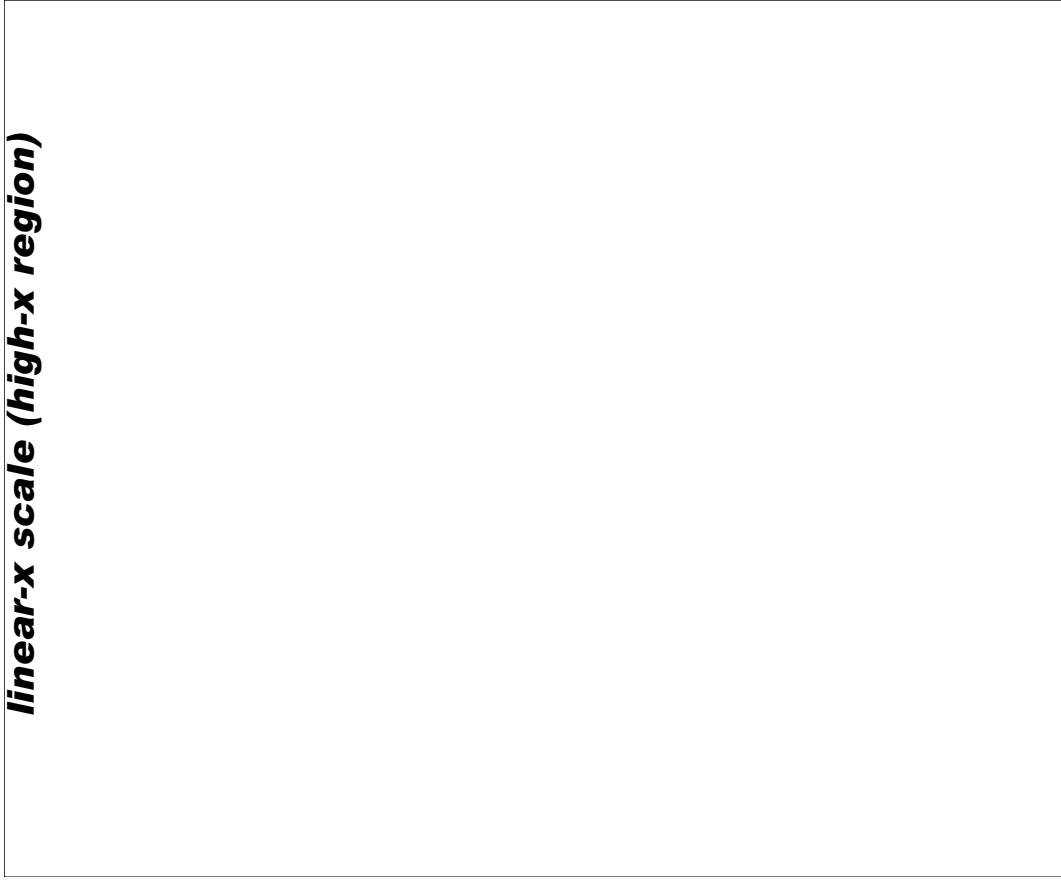
- Impact of the projected HERA-II measurements has been studied in context of the ZEUS-JETS fit



# u-valence uncertainties

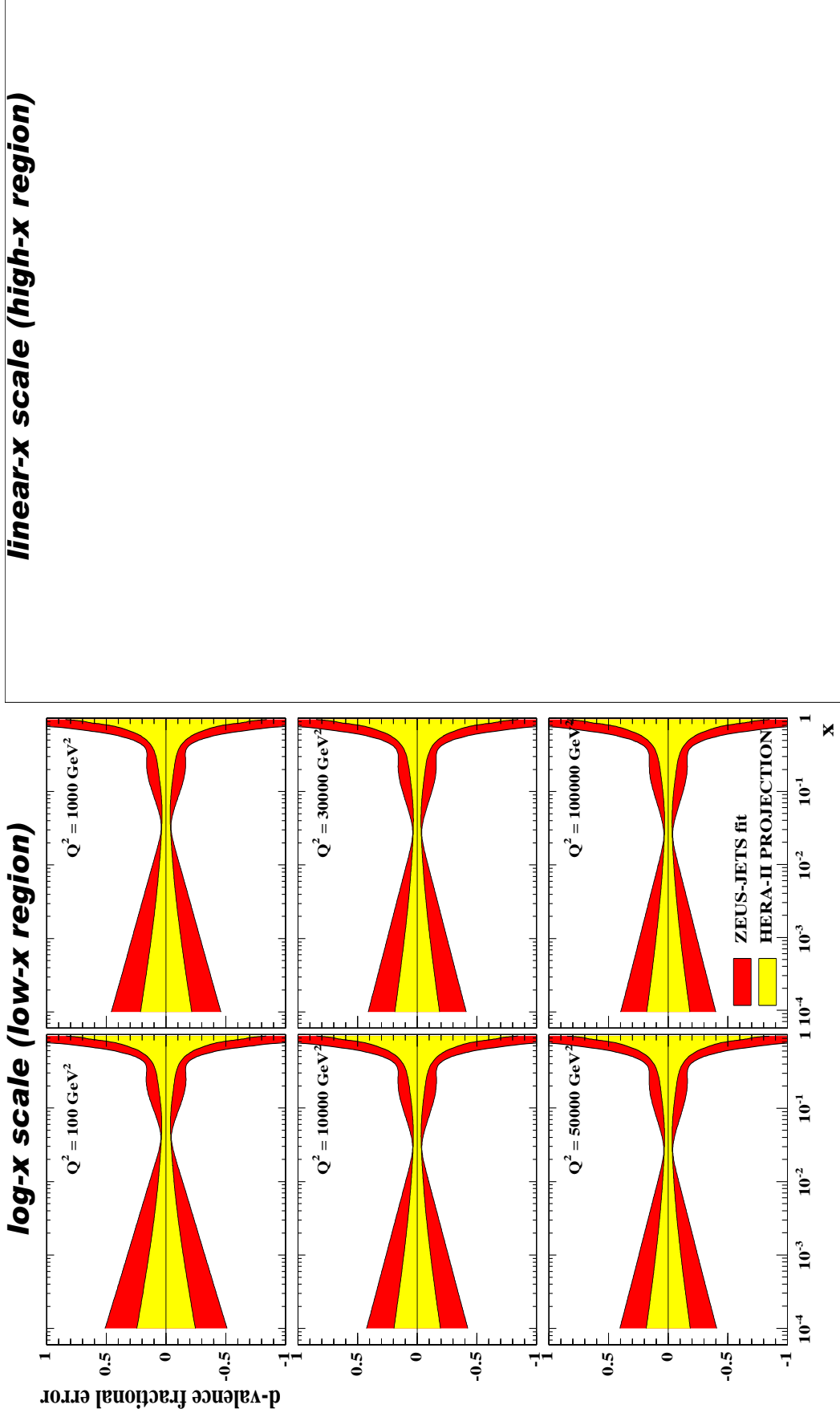


**linear-x scale (high-x region)**



- uncertainties on u-valence distribution significantly reduced over visible x range

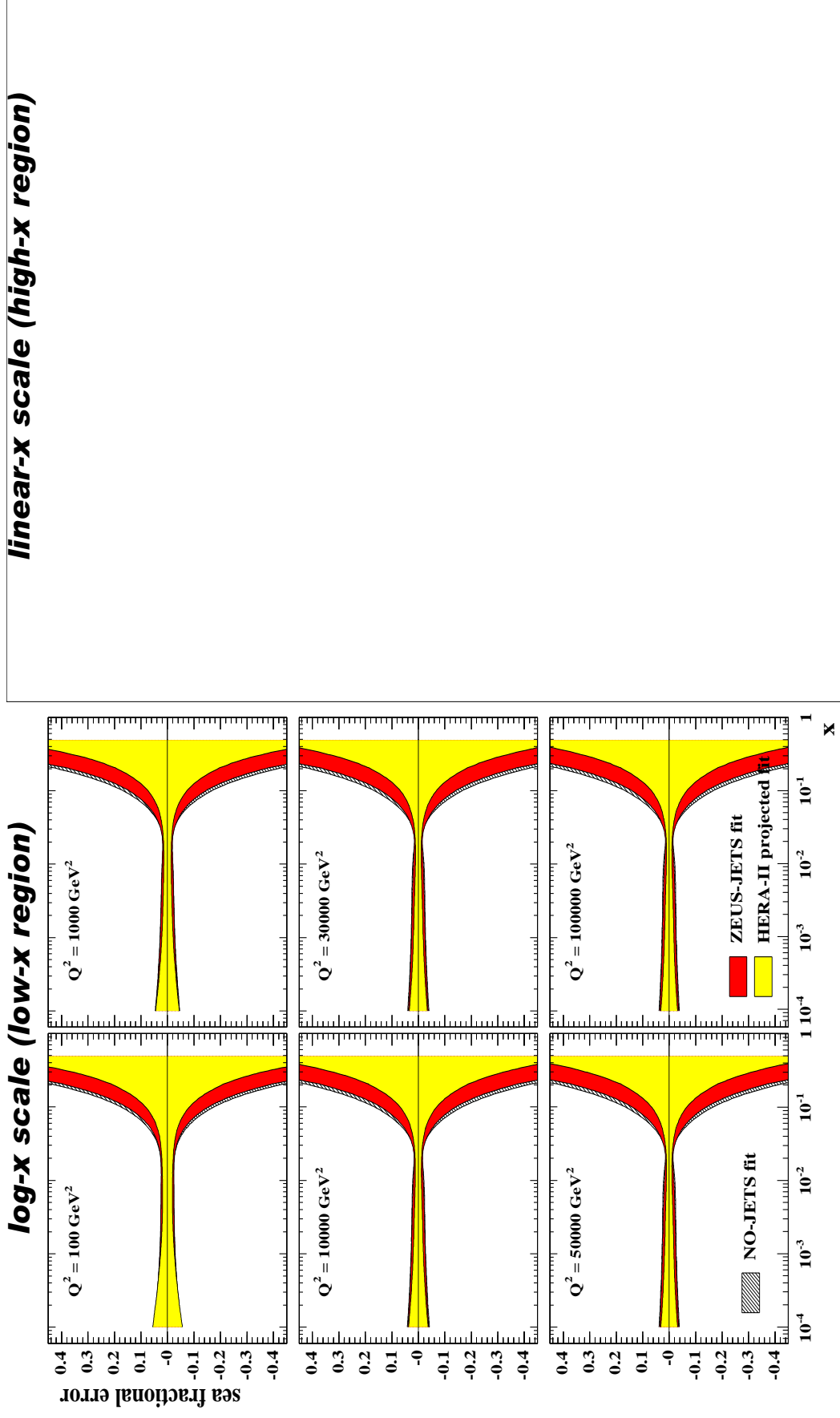
# d-valence uncertainties



- uncertainties on d-valence distribution significantly reduced over visible x range



# Sea-quark uncertainties

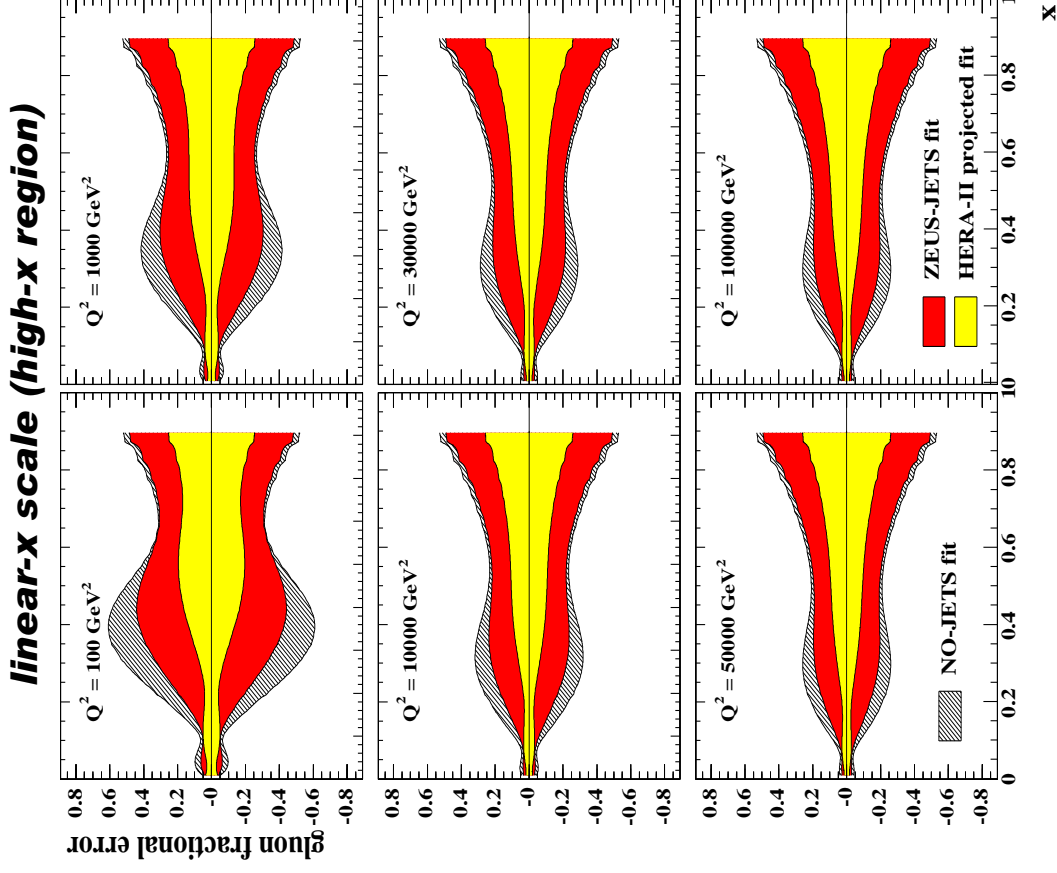


- **uncertainties on sea-quark distribution significantly reduced at high-x**

→ most significant improvement from increased statistics at HERA-II

# gluon uncertainties

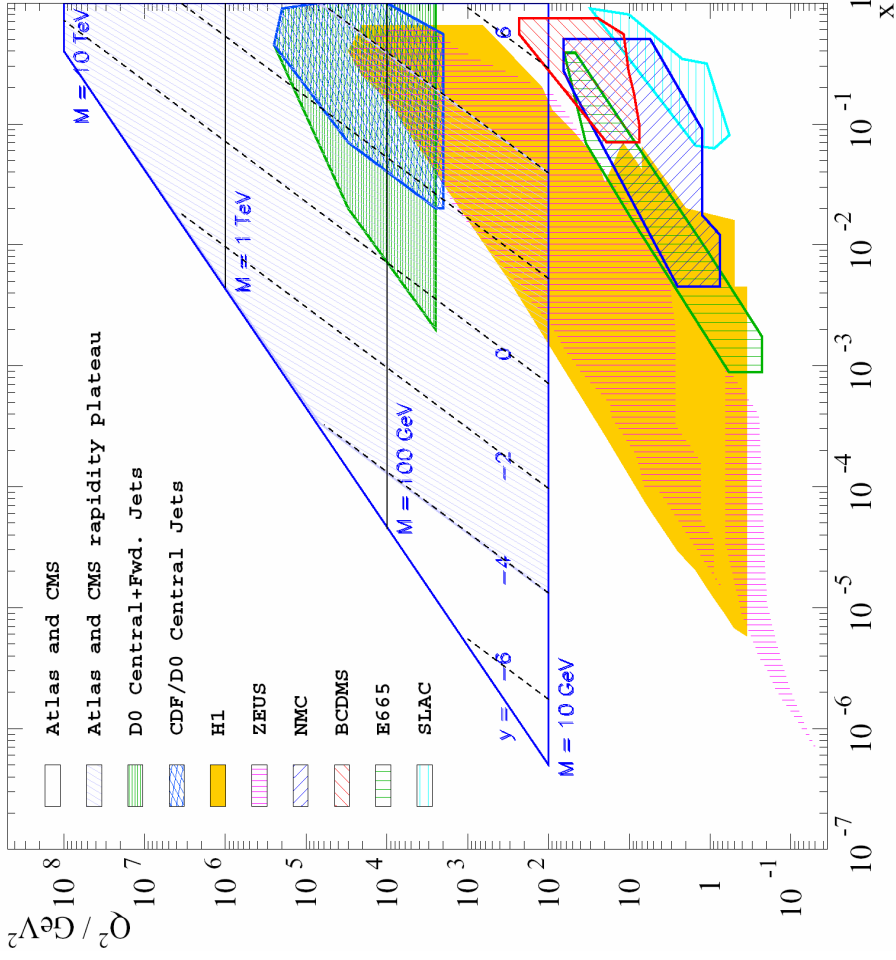
*log-x scale (low-x region)*



• uncertainties on mid-to-high-x gluon significantly reduced

→ most significant improvement comes from optimised cross section

# HERA Kinematic ( $x, Q^2$ ) Range



HERA data covers large region in ( $x, Q^2$ )  
 → also relevant  $x$ -region for LHC

High- $p_T$  jets, new particle searches etc  
 at LHC all depend strongly on high- $x$   
 partons → improvement to LHC cross  
 section uncertainties after HERA-II

Impact of HERA-II projected PDF on  
 LHC cross sections under study

## **PART II:**

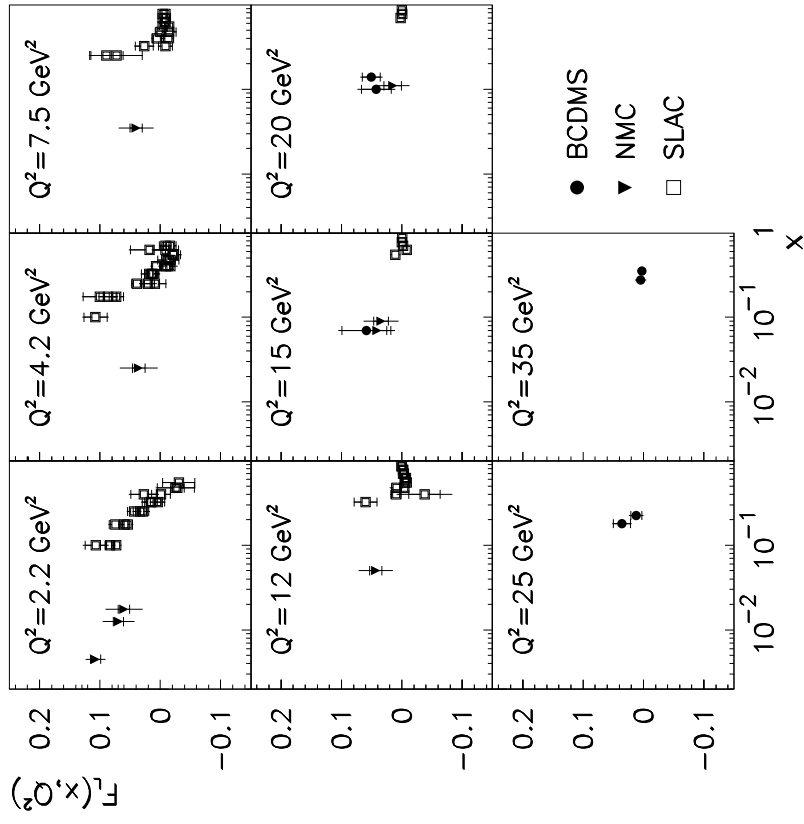
**Alternative HERA running scenarios:  
low energy running and a precision  
measurement of  $F_L$**

# Impact of a HERA measurement of $F_L$

$$\frac{d^2\sigma_{NC}(e^\pm p)}{dx dQ^2} \sim Y_+ F_2 - y^2 F_L \text{ where } F_L = \alpha_s g(x, Q^2)$$

$F_L$  contributes at  $O(\alpha_s)$  (and HO) and is directly sensitive to the gluon density in the proton

- measured at fixed target expts. ( $x > 10^{-3}$ )
- precision  $F_L$  measurement at HERA requires low- $E_p$  running  $\rightarrow$  vary  $y$  at fixed  $(x, Q^2)$

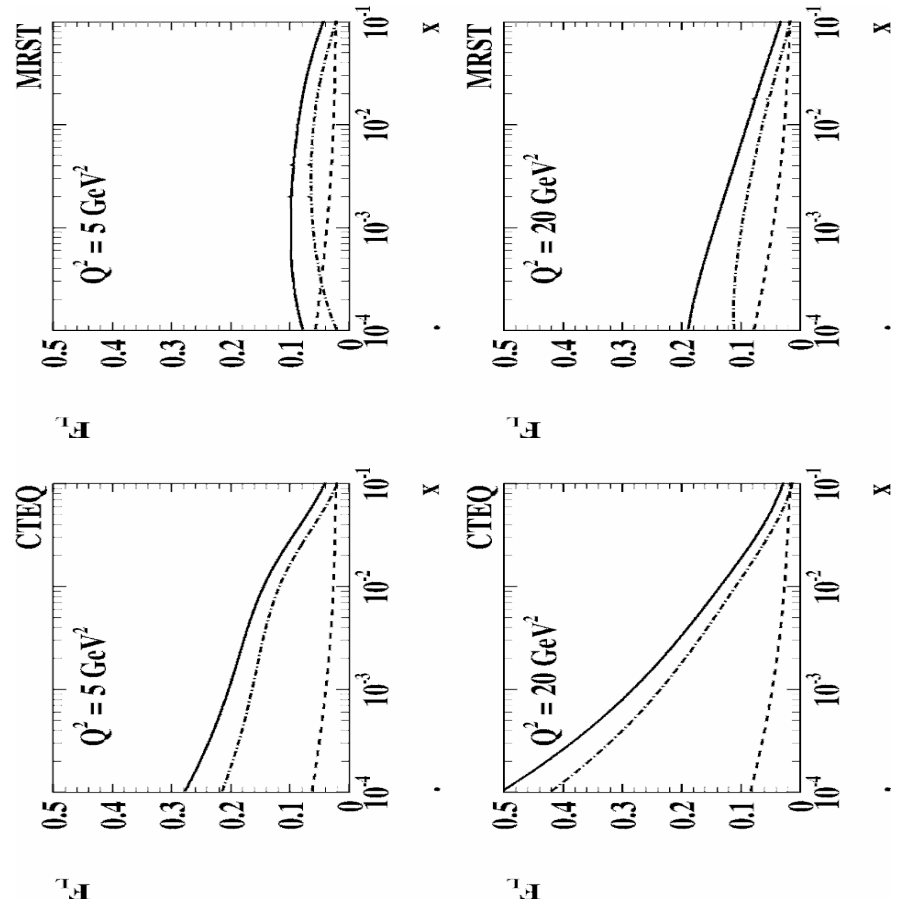


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- precision measurement of  $F_L$  at HERA-II:
  - x pin down gluon density at low-x
  - x reduce uncertainties on gluon PDF

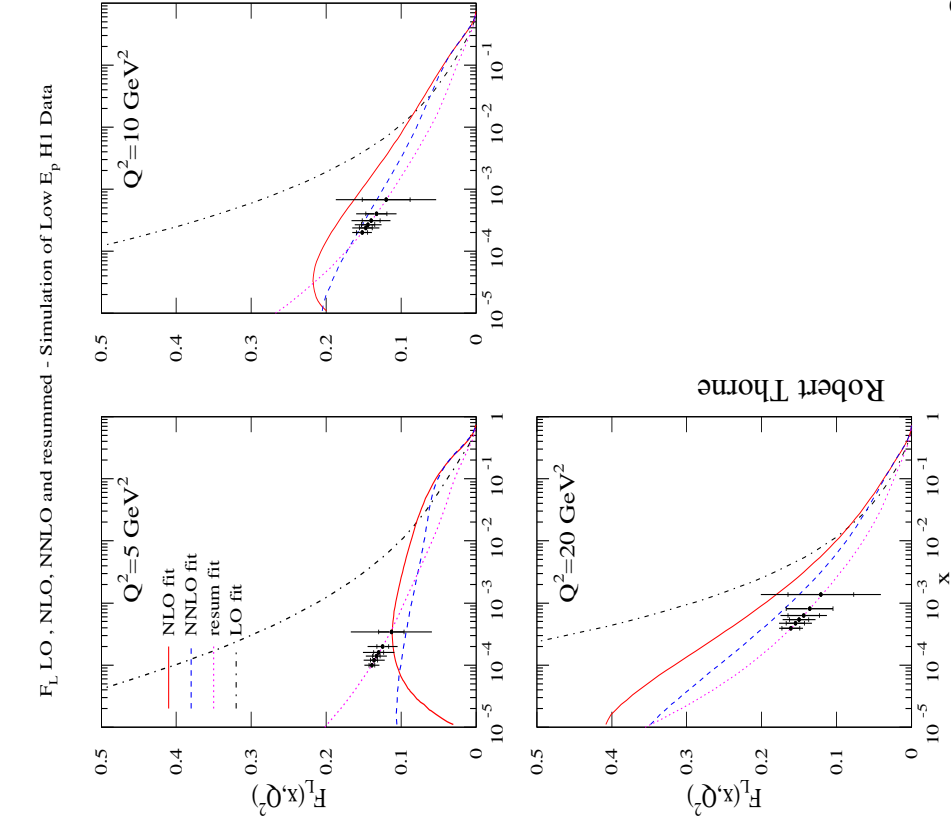


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  - × test the need for extensions to DGLAP at low-x

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# Impact of a HERA measurement of $F_L$

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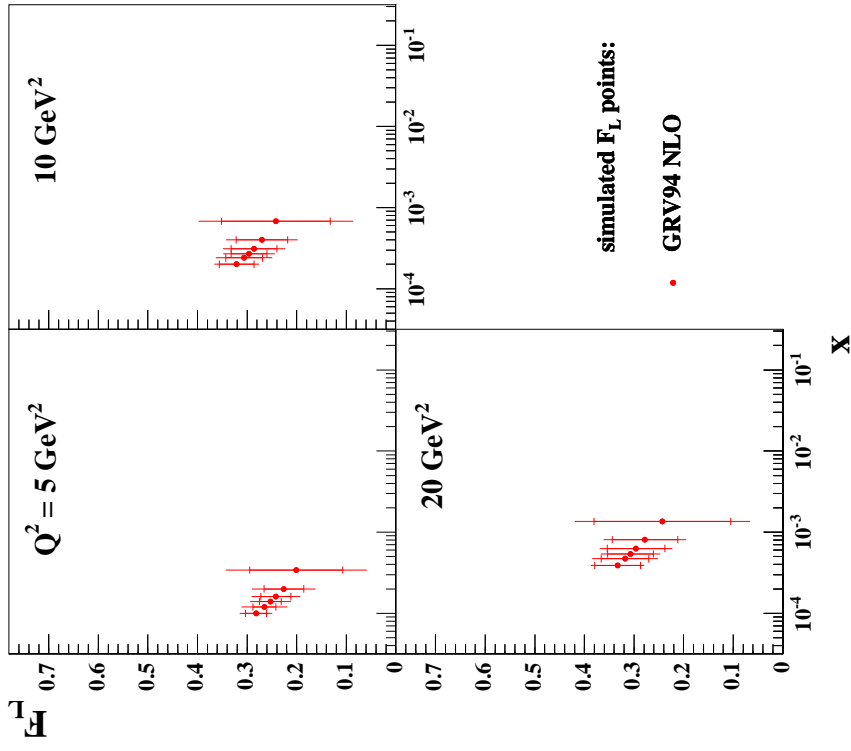
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## Simulation of HERA-II $F_L$ : Max Klein (DESY)

- $F_L$  simulated using GRV94 NLO PDF
- **statistical uncertainties correspond to:**

$E_p$ (GeV)	920	575	465	400
$L$ (pb <sup>-1</sup> )	10	5	3	2

- systematic uncertainties from current H1 analysis of 99-00 data (few %)



For further details, see “On the future measurement of  $F_L$  at low-x at HERA”, Max Klein, in proceedings NIS04



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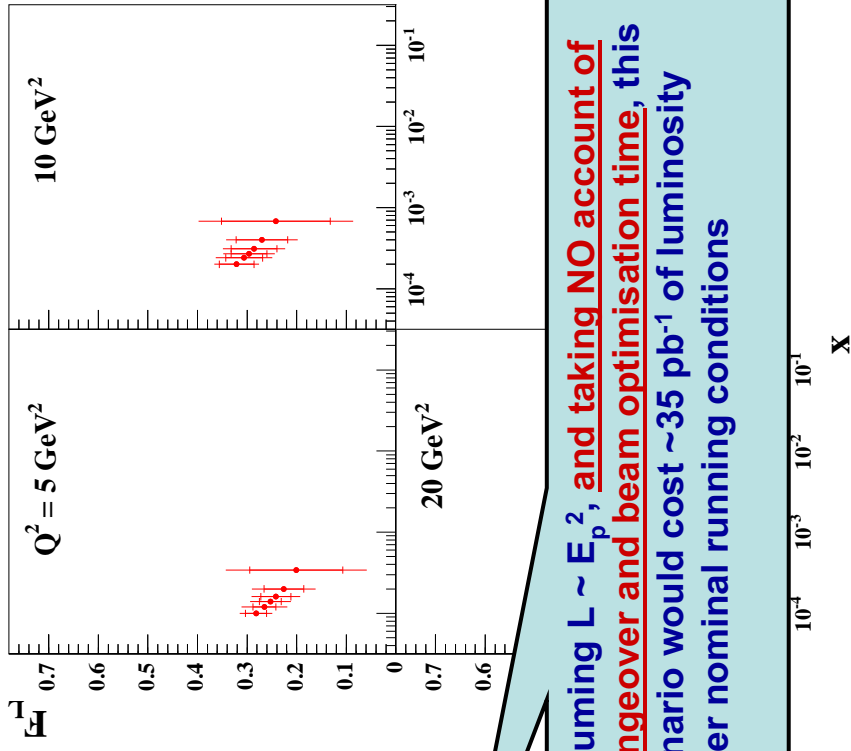
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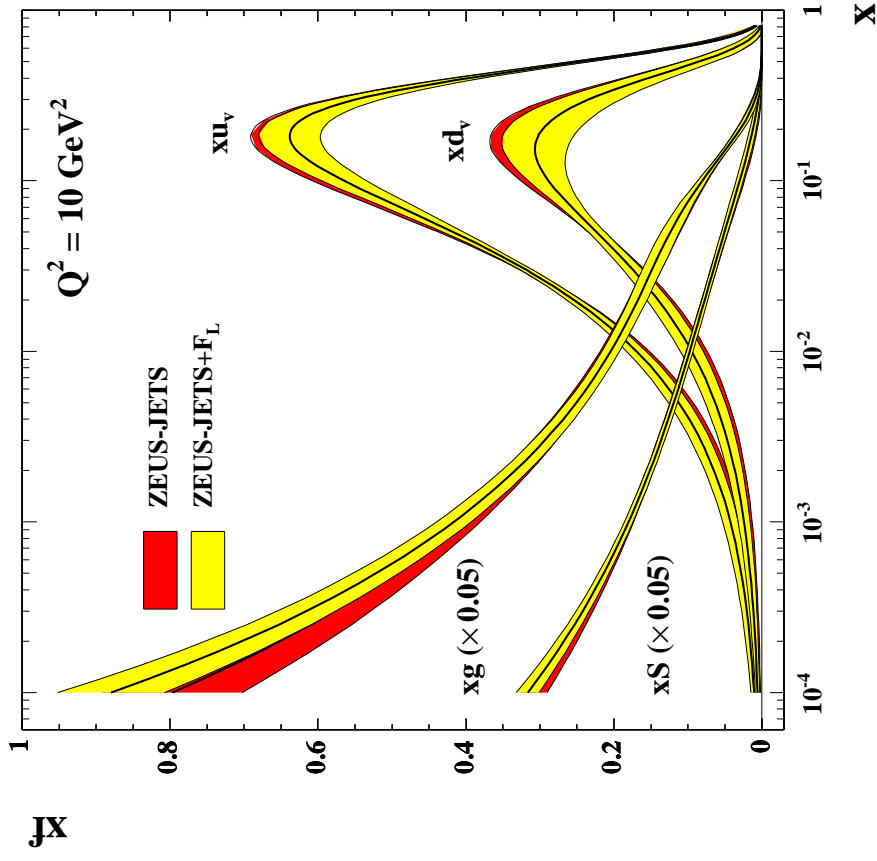
- systematic uncertainties from current H1 analysis of 99-00 data (few %)



Assuming  $L \sim E_p^2$ , and taking **NO account of changeover and beam optimisation time**, this scenario would cost  $\sim 35 \text{ pb}^{-1}$  of luminosity under nominal running conditions

For further details, see “On the future measurement of  $F_L$  at low-x at HERA”, Max Klein, in proceedings NIS04

# Impact on gluon distribution



- Fit including simulated  $F_L$  data compared to the ZEUS-JETS PDF  $\uparrow$
- Gluon uncertainties reduced at low- $x$  and low- $Q^2$  (not relevant for LHC)

# Sensitivity of the NLO QCD fit

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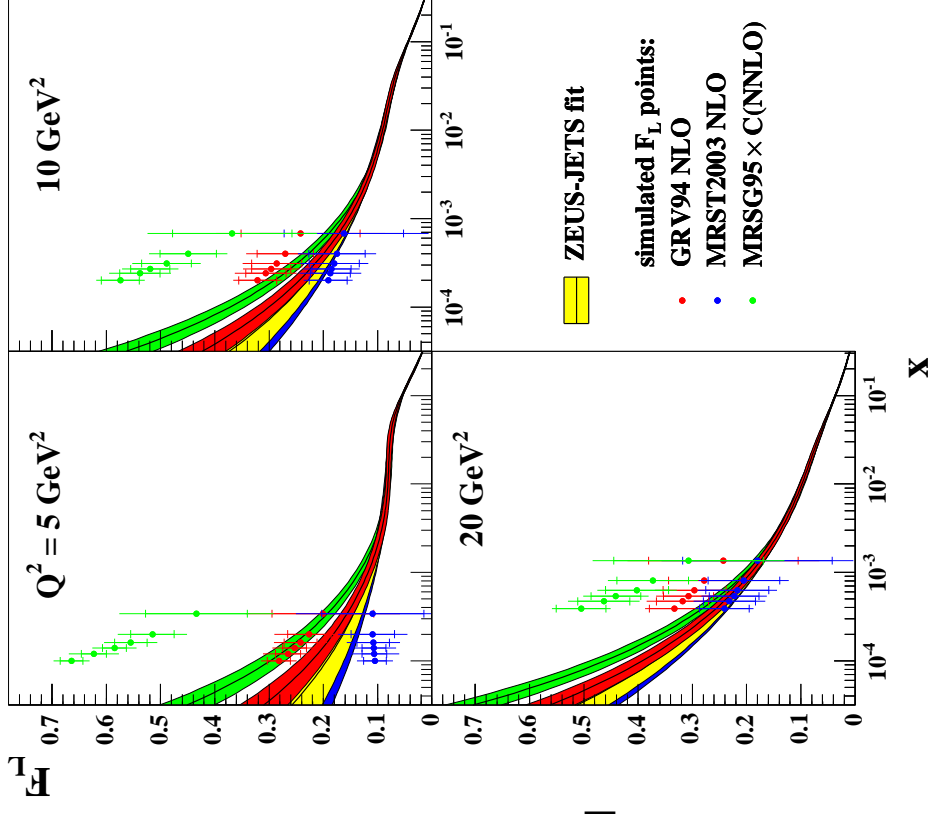
- $F_L$  predictions very sensitive to underlying theory  
 → choice of PDF, order of QCD calculation ...
- how sensitive is the NLO QCD fit to inclusion of “extreme” sets of simulated  $F_L$  data?

## Simulated $F_L$ data

extremes provided by Robert Thorne

(Cambridge) PDF	QCD theory
Max. $F_L$ MRSG95	NNLO*
Mid. $F_L$ GRV94	NLO
Min. $F_L$ MRST2003	NLO

- ZEUS fit relatively stable to inclusion of extreme  $F_L$  data-sets
- an  $F_L$  measurement of this precision should have power to discriminate between theoretical models



**Bonus Extra:**  
**Alternative HERA running scenarios:**  
**deuteron running and the sea quark**  
**asymmetry**

# sea quark asymmetry

## a study by Max Klein and Burkard Reiser

(in the context of the H1 fit)

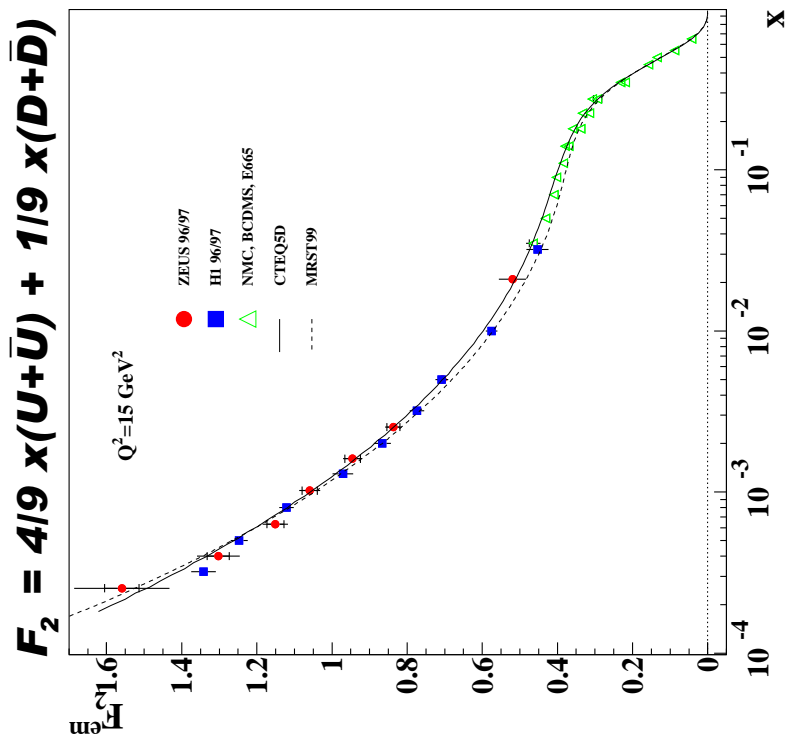
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What causes the rise of  $F_2$  at low- $x$ ?

$F_2$  of the proton measures  $4\bar{u}+\bar{d}$  but  $\bar{u}$  and  $\bar{d}$  are unknown at low  $x \rightarrow$  would be accessible via deuteron (eD) running at HERA-II

$\bar{u}=\bar{d}$  was a natural assumption for long time, until E866, HERMES found a difference at  $x \sim 0.1$

**are sea quarks and anti-quarks equal ?**  
**are up and down quarks equal at low  $x$  ?**



# The H1 NLO QCD fit

HERA-I H1 incl. NC/CC e <sup>+</sup> /e <sup>-</sup> (94-00): H1-Only
+ BCDMS (p,D data): H1+BCDMS

PDF	Param. at $Q_0^2 = 4 \text{ GeV}^2$
$xU = x(u+c)$	$A_U x^{b_U} (1-x)^{c_U} (1+d_U x + e_U x^3)$
$xU_{\text{bar}}$	$A_{U_{\text{bar}}} x^{b_{U_{\text{bar}}}} (1-x)^{c_{U_{\text{bar}}}}$
$xD = x(d+s)$	$A_D x^{b_D} (1-x)^{c_D} (1+d_D x)$
$xD_{\text{bar}}$	$A_{D_{\text{bar}}} x^{b_{D_{\text{bar}}}} (1-x)^{c_{D_{\text{bar}}}}$
$xg$	$A_g x^{b_g} (1-x)^{c_g} (1+d_g x)$

- No information on sea flavour composition
- only one measurement at low-x:

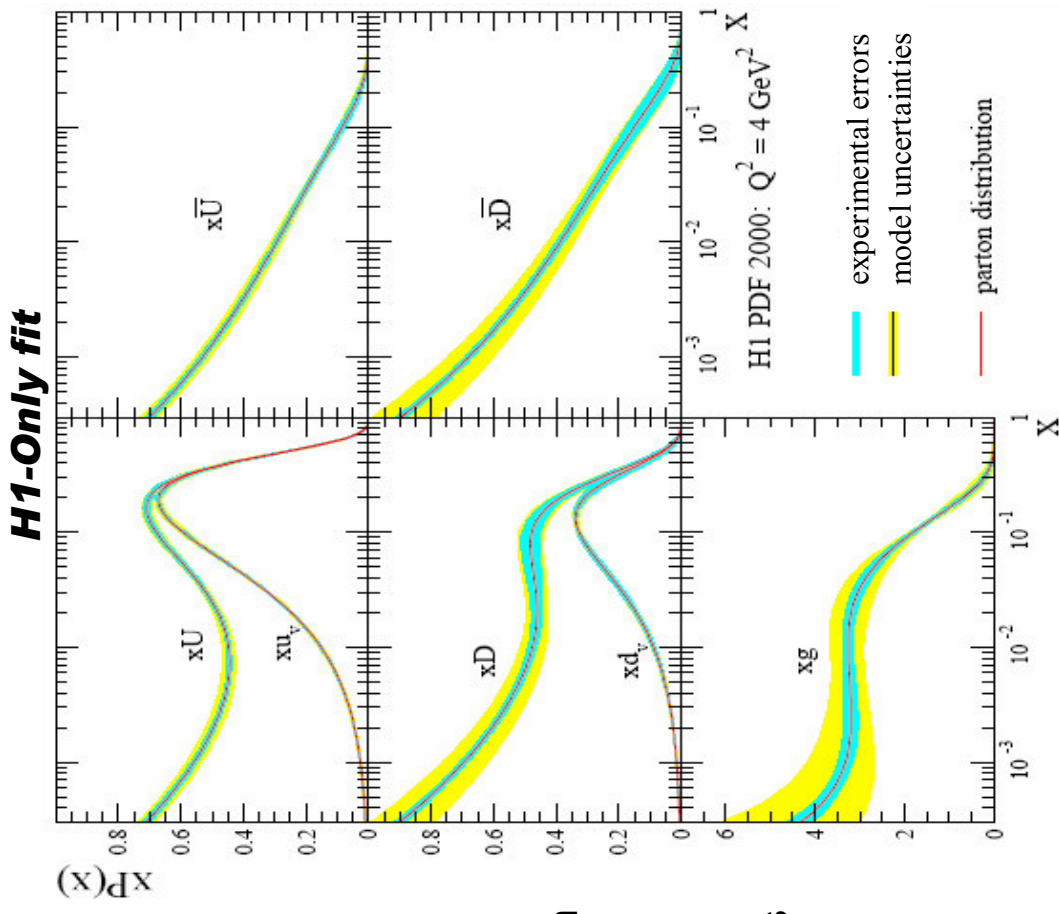
$$F_2 = 4/9 x(U+\bar{U}) + 1/9 x(D+\bar{D})$$

- Assume quark and anti-quark distributions are equal at low-x and u=d

$$- \mathbf{b}_U = \mathbf{b}_D = \mathbf{b}_{\bar{U}} = \mathbf{b}_{\bar{D}} \equiv \mathbf{b}_q$$

$$- \mathbf{A}_{\bar{U}} = \mathbf{A}_{\bar{D}} \cdot (\mathbf{1} - \mathbf{f}_s) / (\mathbf{1} - \mathbf{f}_c), \text{ which means}$$

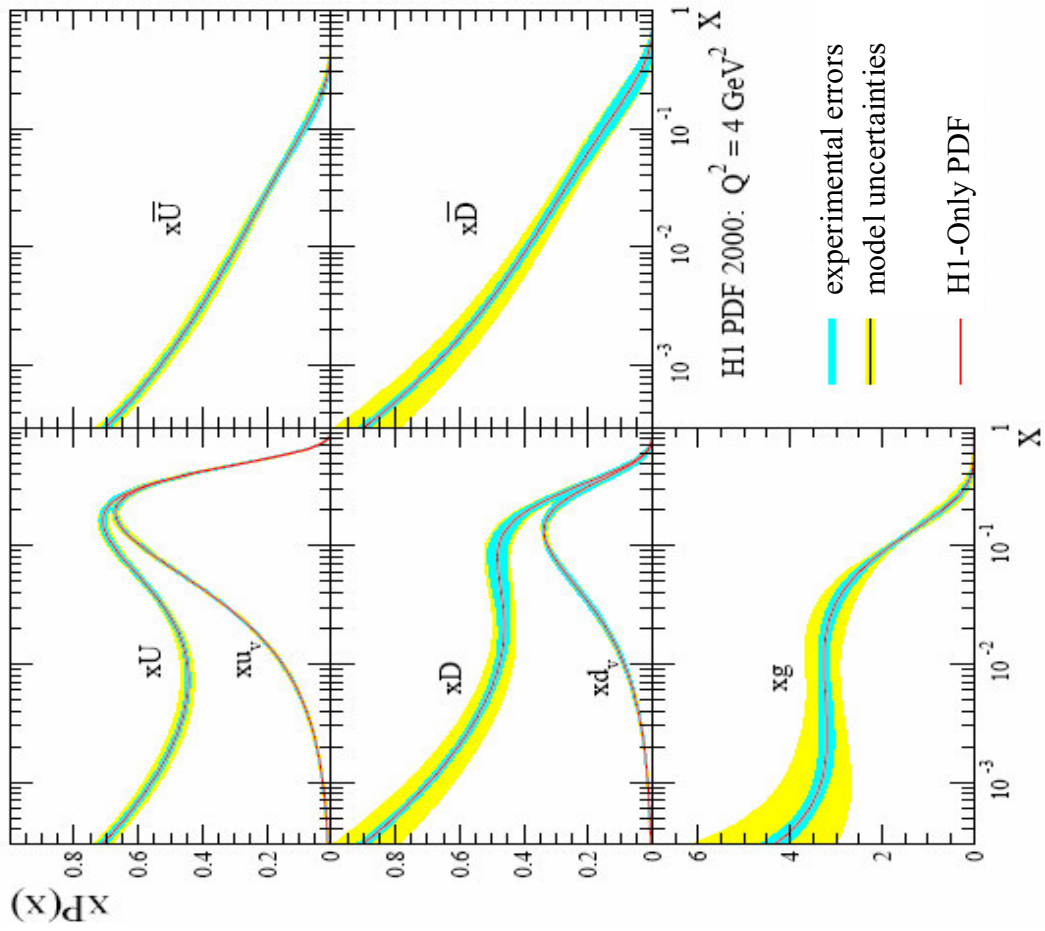
$$\text{that } \bar{d} / \bar{u} \rightarrow 1 \text{ as } x \rightarrow 0$$



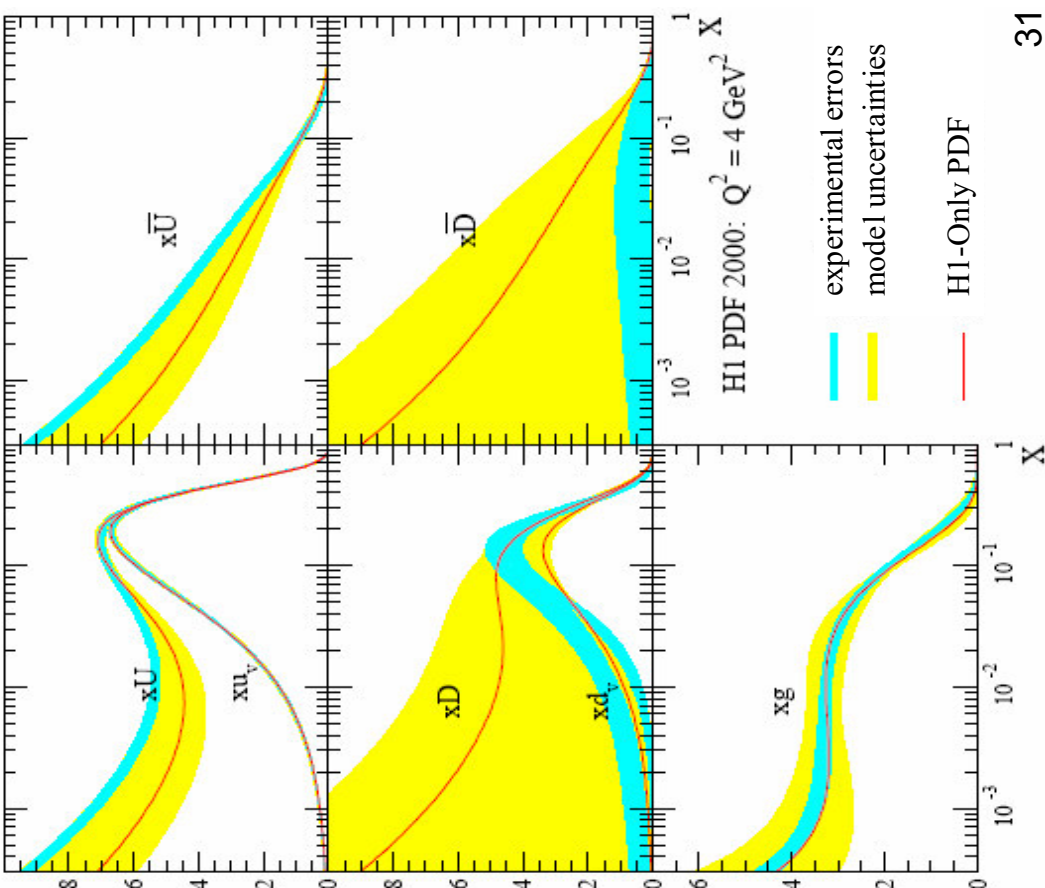
# Releasing the dbar-ubar constraint

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**H1-Only fit (default assumptions)**

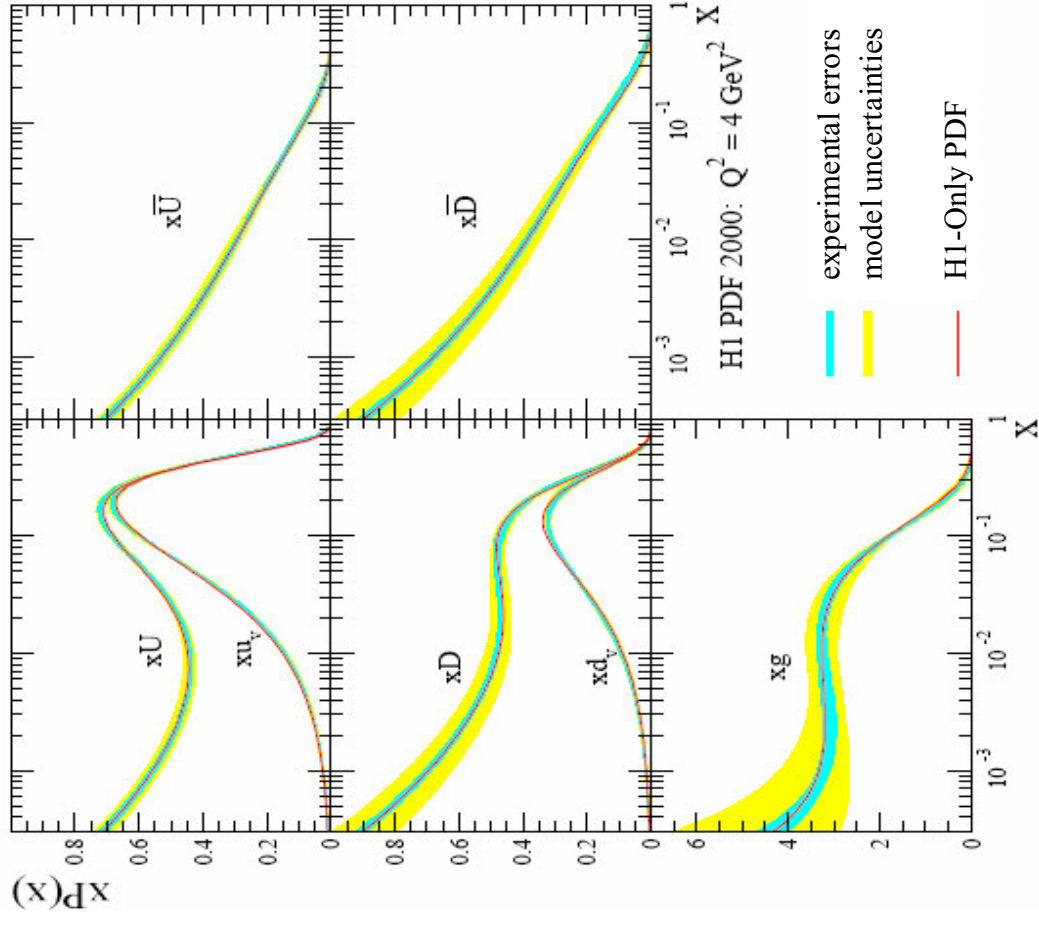


**H1-Only fit (no constraint on A, b)**

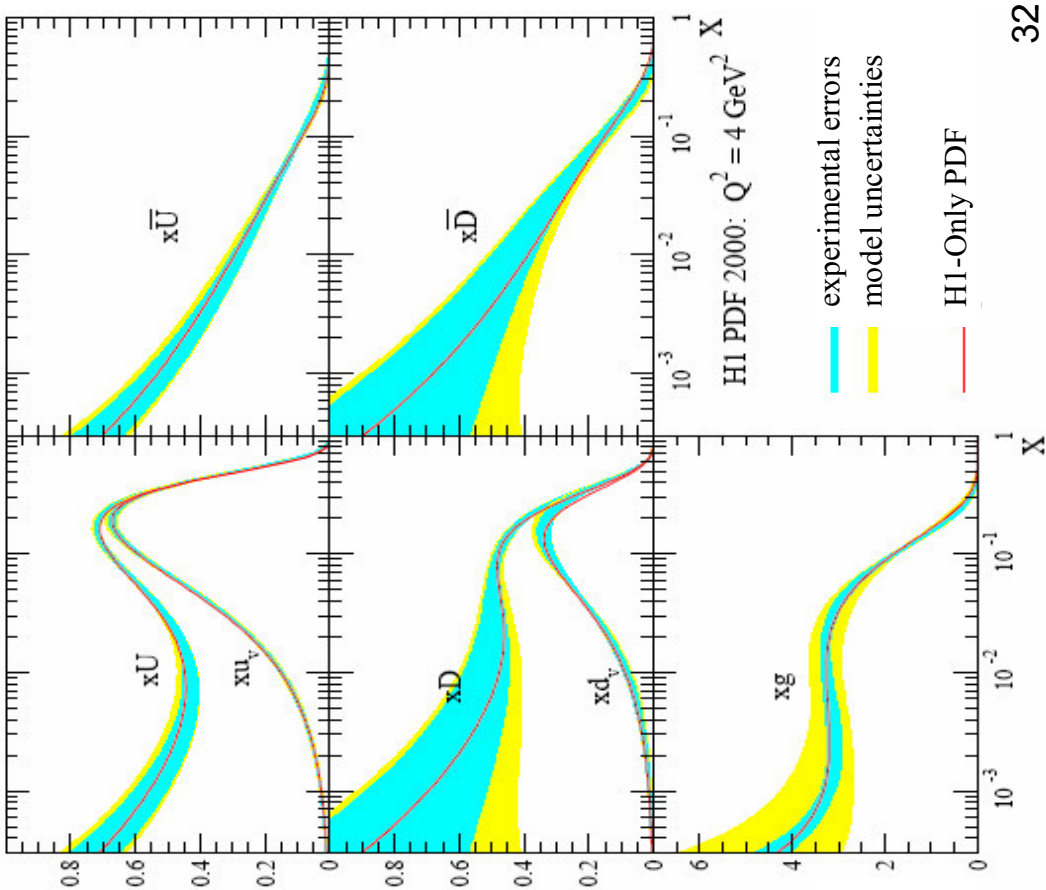


# Releasing the dbar-ubar constraint

**H1+BCDMS fit**

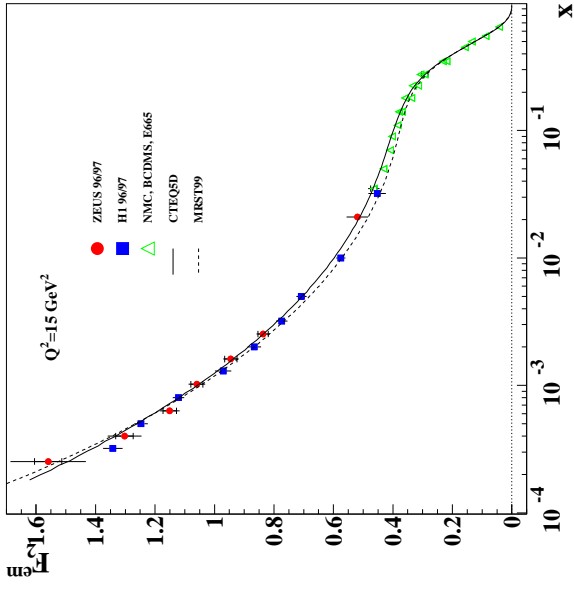


**H1 + BCDMS fit (no constraint on A, b)**



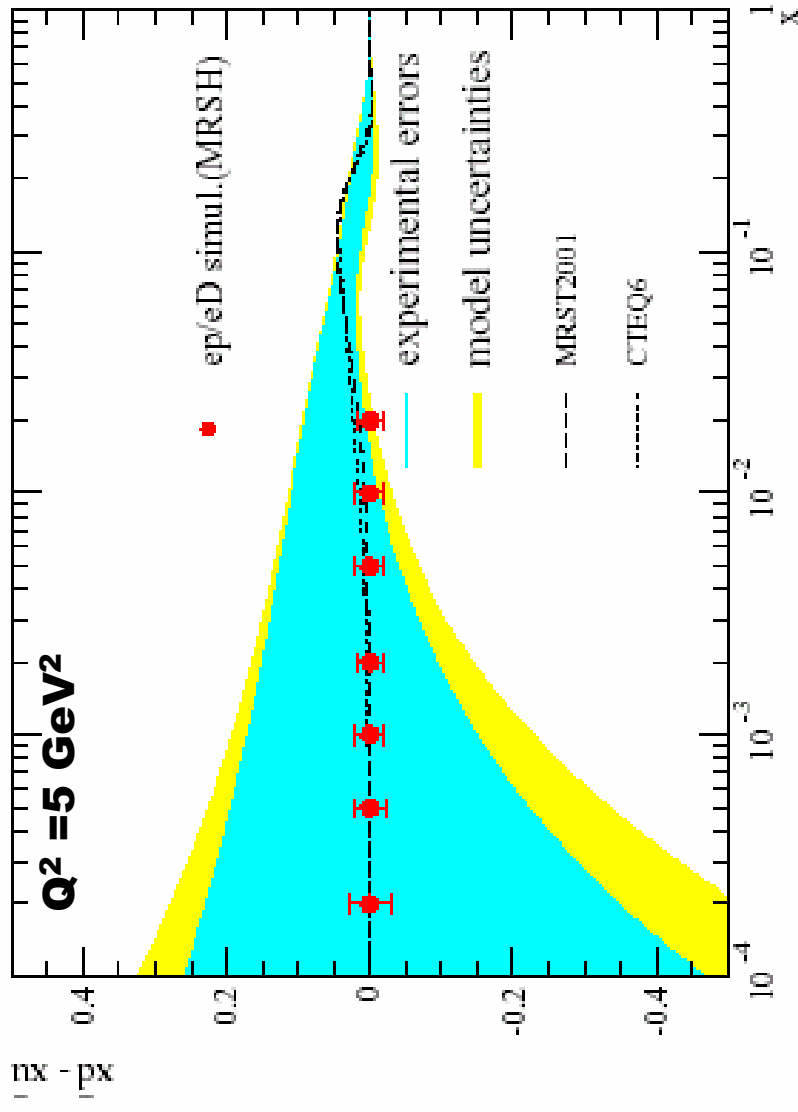


# Releasing the dbar-ubar constraint



The light sea quark asymmetry is expected and has been assumed to vanish at low  $x$ . However,  $F_2$  rises strongly towards low  $x$  which deserves to be studied.

## H1+BCDMS fit



$$\begin{aligned} & \frac{1}{2}(F_2^p + F_2^n) - F_2^p \\ &= x \left( \frac{1}{6} d_v - \frac{1}{6} u_v + \frac{1}{3} \bar{d} - \frac{1}{3} \bar{u} \right) \\ &\approx \frac{1}{3} x (\bar{d} - \bar{u}) \text{ at low } x \end{aligned}$$

simulated accuracy (20 pb<sup>-1</sup> eD, 40 pb<sup>-1</sup> ep)

# Summary

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Potential impact of future HERA data on proton PDFs has been investigated:

## 1. Impact on PDFs of current HERA-II running scenario:

- increased luminosity of HERA-II will provide
  - significantly improved precision on statistically limited data-sets
    - high- $Q^2$  NC/CC data → significant improvement to valence distributions
    - high- $Q^2$  and high- $E_T$  jet data → improvement to high-x sea and gluon
- measurements of jet cross sections optimised for sensitivity to gluon
  - significant improvement to high-x gluon

▶ **impact of projected HERA-II PDFs on LHC cross sections under study**

## 2. Low energy running scenario:

- precise measurement of  $F_L$  at low-x possible with low- $E_p$  running
- inclusion of simulated  $F_L$  data in NLO QCD fit indicates:
  - improvement in gluon uncertainties at low-x and low- $Q^2$
  - **ability of precision HERA  $F_L$  to discriminate between theoretical models**

# Summary (cont.)

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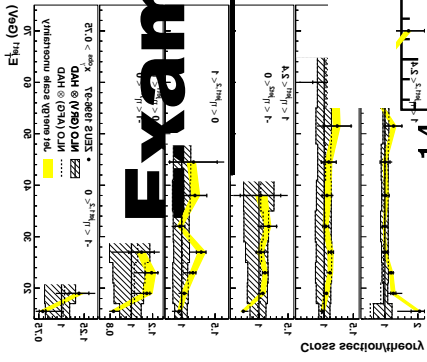
## 3. Deuteron running and the sea-quark asymmetry:

(Max Klein, Burkard Reiser):

- **So far HERA has not resolved the light sea quarks at low  $x$** 
  - × relaxing assumption that  $\bar{u}=\bar{d}$ ,  $u=\bar{u}$  and  $d=\bar{d}$  at low- $x$  leads to large uncertainties
  - × deuteron data from fixed target experiments (e.g. BCDMS) help but cannot solve the problem since the data lie at higher- $x$
- ▶ **would need deuteron running at HERA to resolve this issue**

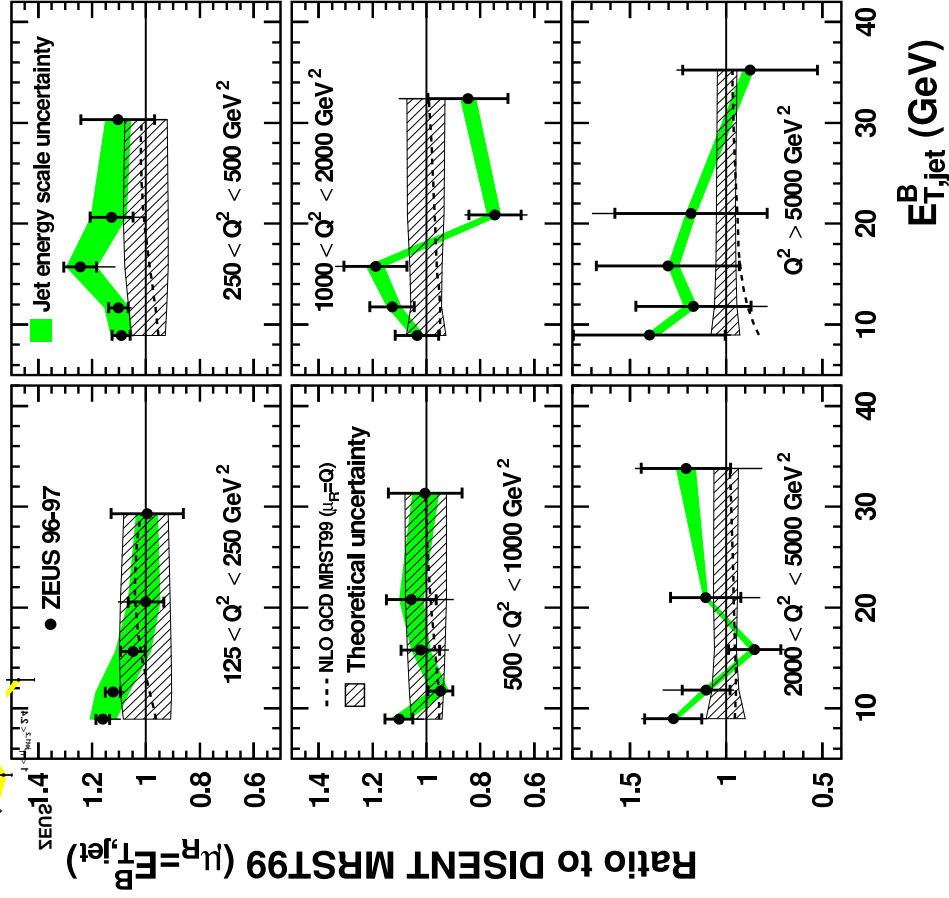
# Extras ...

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# Example: high- $Q^2$ /high- $E_T$ jet data

## ZEUS inclusive jets in DIS



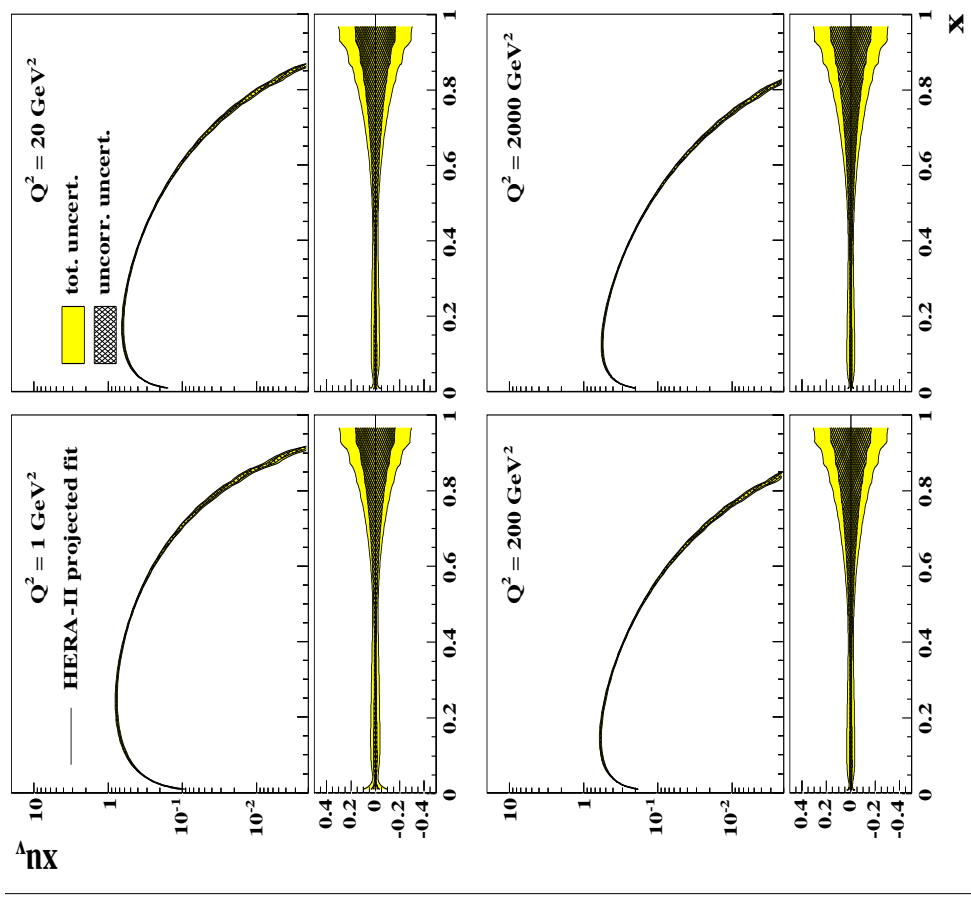
## ZEUS dijets in photoproduction

- HERA-II will provide greatly increased luminosity

# Comparison with global fit (u-val.)

**ZEUS-S global PDF**

**HERA-II Projected PDF**

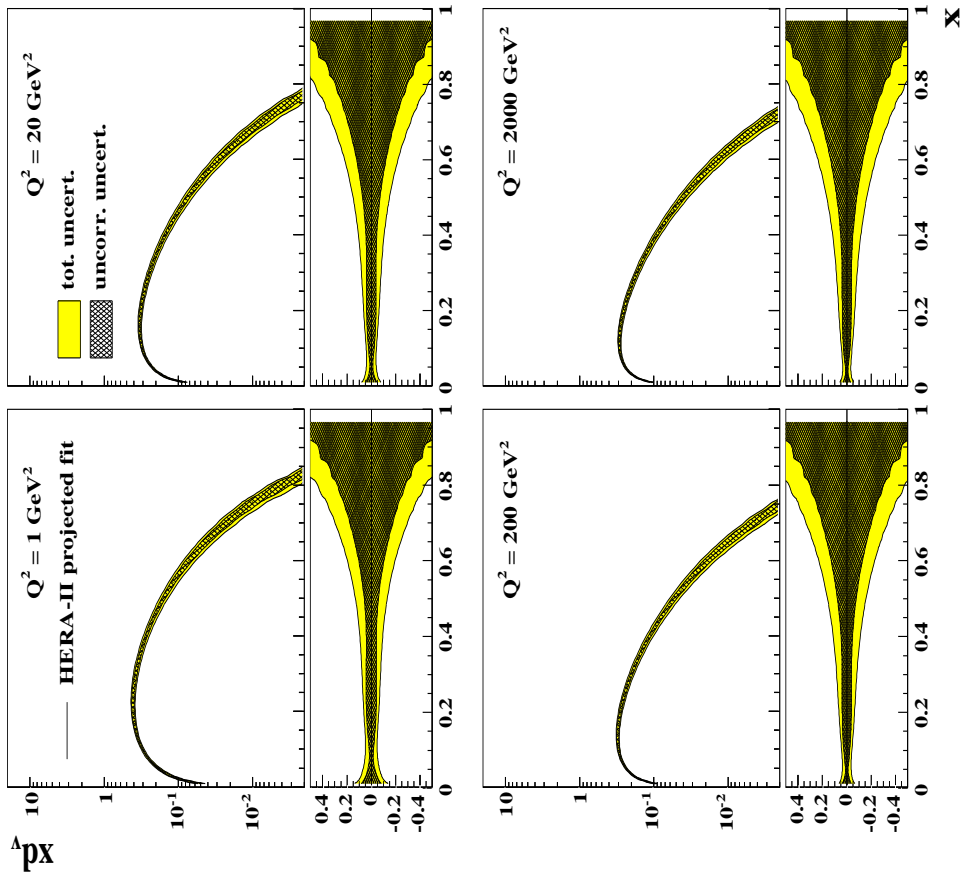


- Uncertainties with full HERA-II inclusive data-set comparable to global fits

# Comparison with global fit (d-val.)

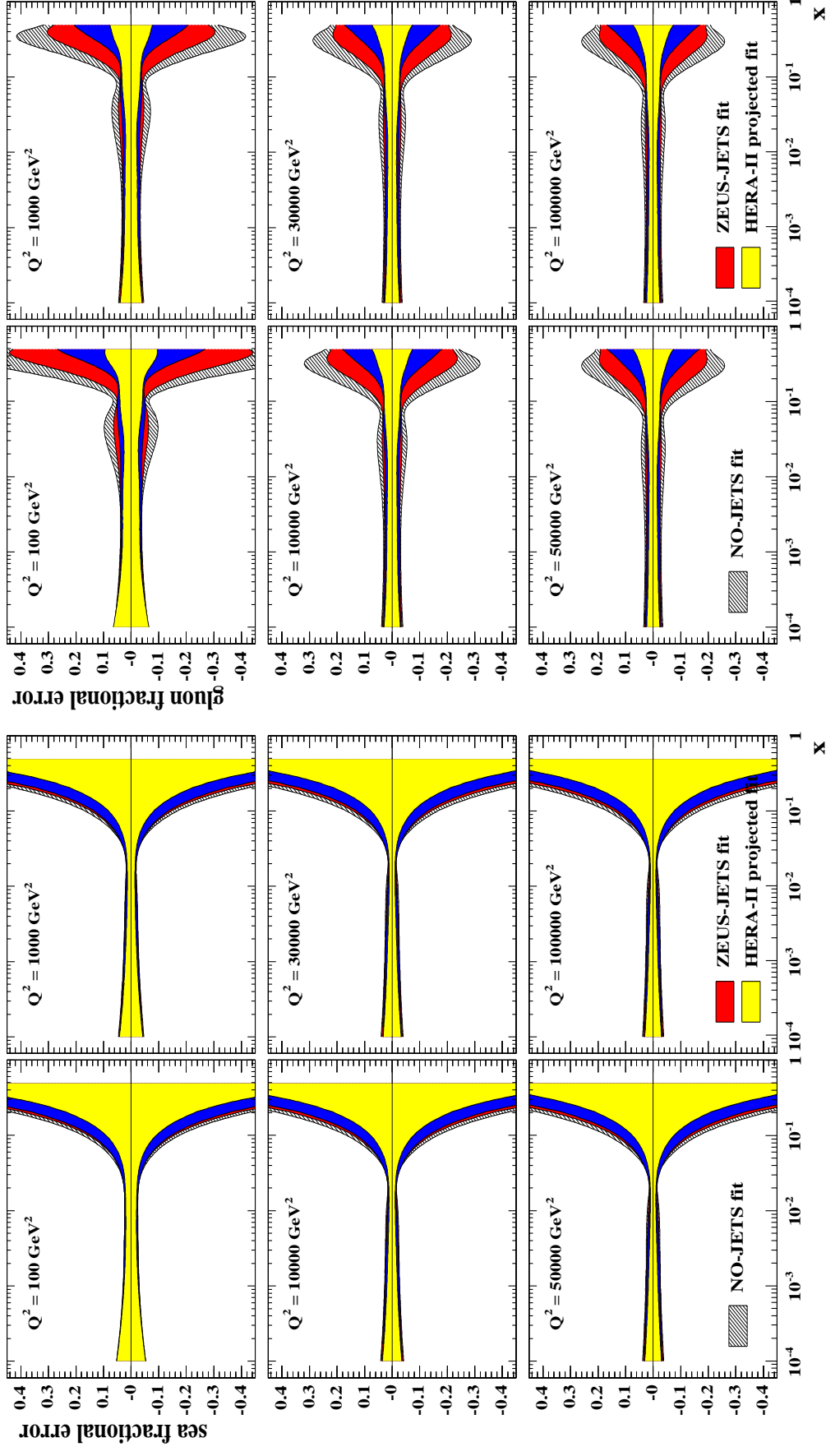
**ZEUS-S global PDF**

**HERA-II Projected PDF**



• Uncertainties comparable to or better than current global fit

# Impact on sea/gluon uncertainties



- blue band: ZEUS-JETS fit + 120  $\text{pb}^{-1}$  (HERA-I) optimised jet cross sections only

- already at HERA-I, optimised jet cross sections would have significant impact on high-x gluon