

# Theoretical aspects of pentaquark searches

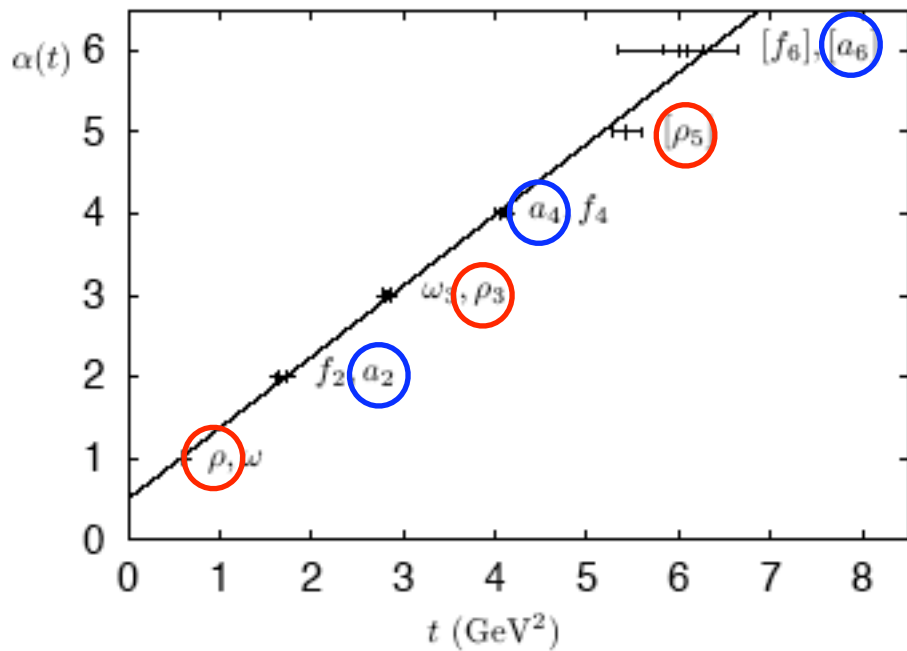
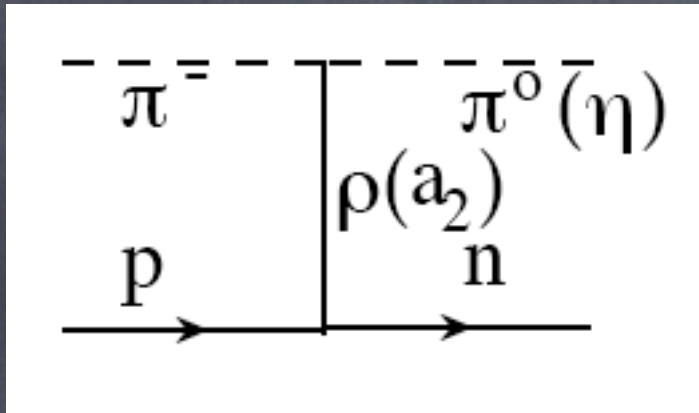
Adam Szczepaniak (Indiana U.)

Two examples from the past

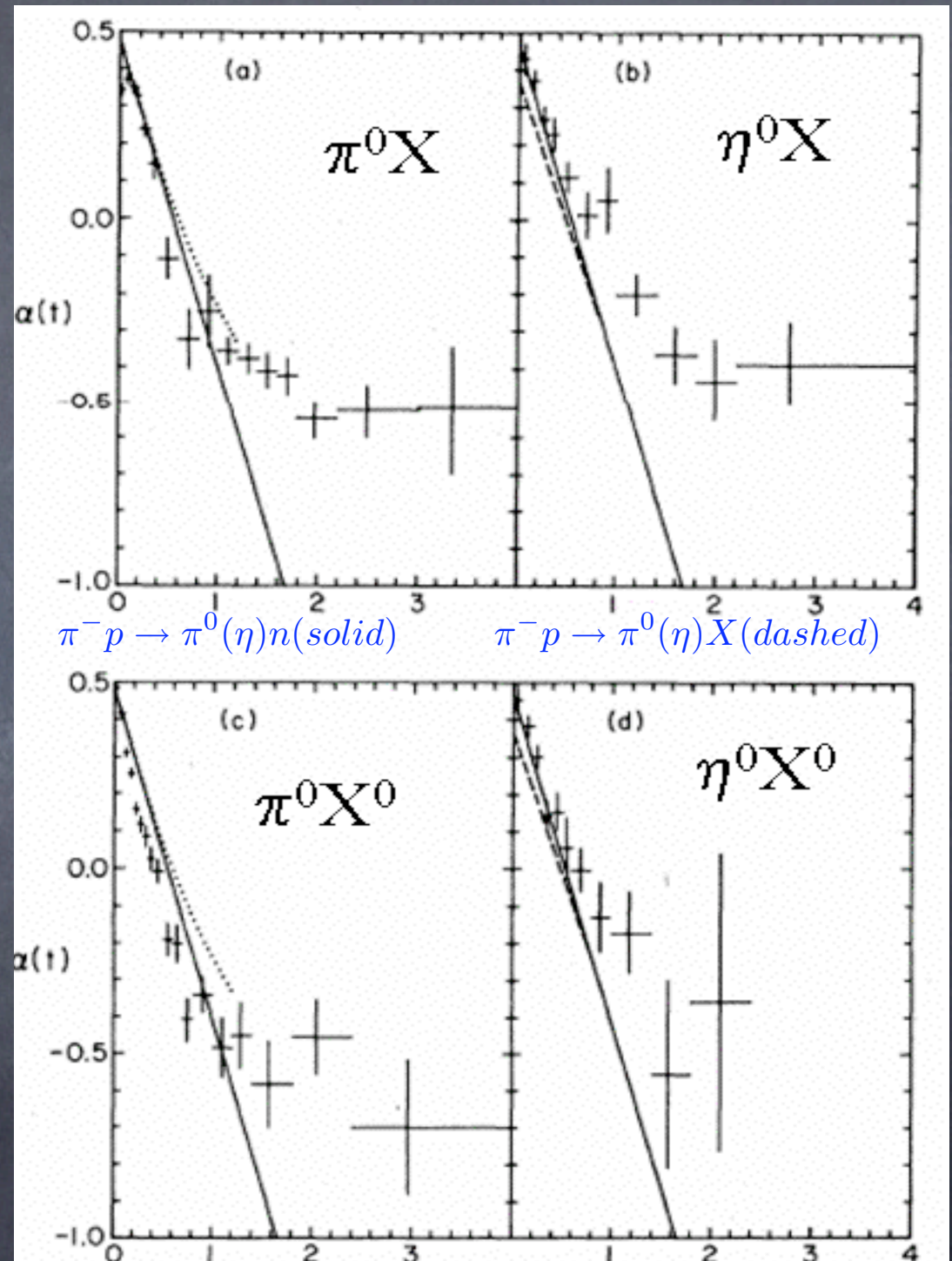
Pentaquark sightings and kinematic effects

Based in part on collaboration with Dzierba and Meyer

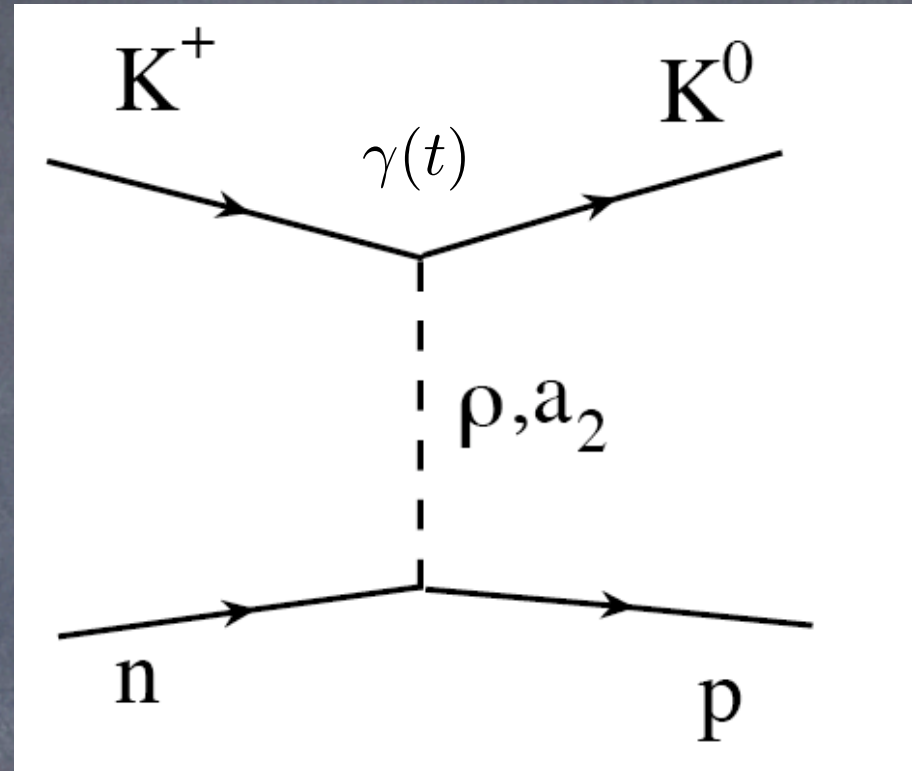
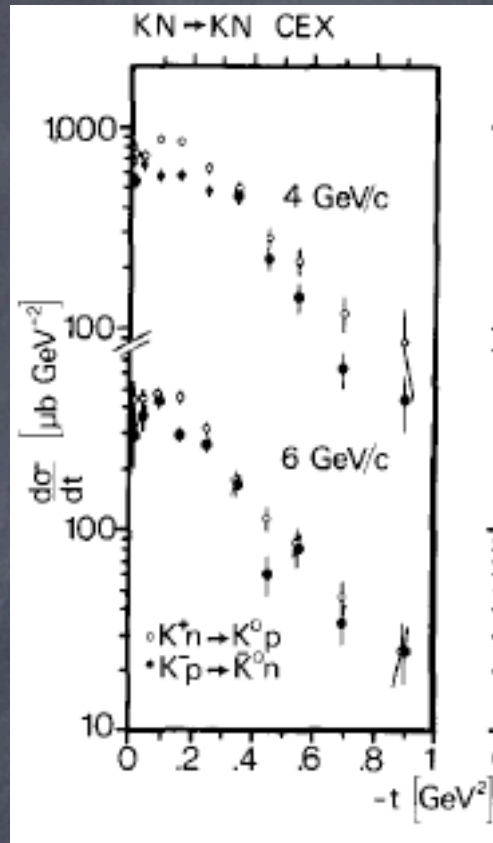
# Exchange degeneracy



$$\alpha_\rho(t) = \alpha_{a_2}(t) \sim 0.5 + t$$



Strong exchange degeneracy  $\gamma_\rho(t) = \gamma_{a_2}(t)$



$$A(K^+ n \rightarrow K^0 p) = \rho + a_2 = 2\gamma(s/s_0)^\alpha \quad \text{Real !}$$

$$A(K^- p \rightarrow \bar{K}^0 n) = \rho - a_2 = -2\gamma(s/s_0)^\alpha e^{-i\pi\alpha}$$

Amplitude at low (resonances) and high (reggions) energy is constrained by analyticity.

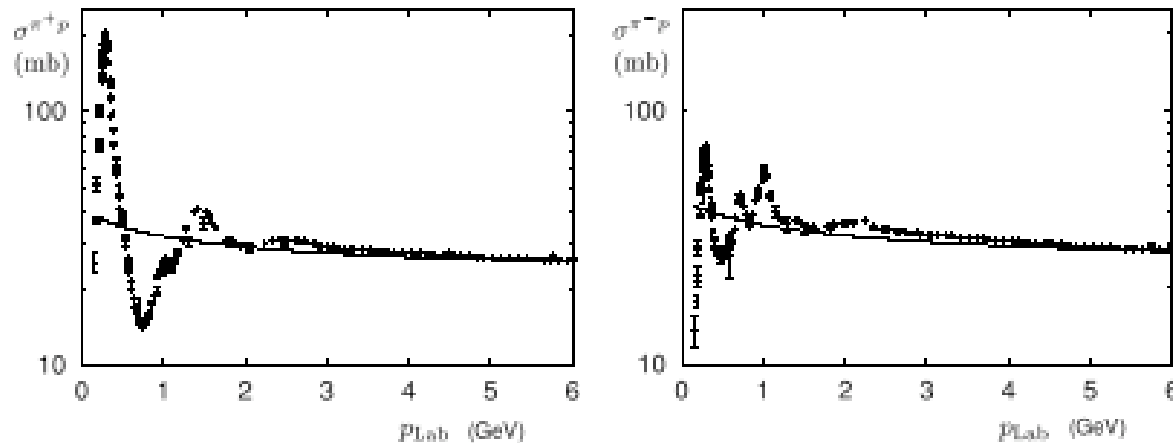
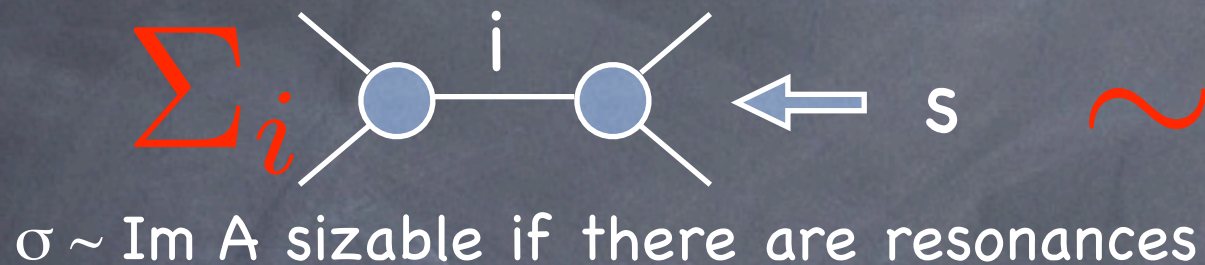


FIG. 6. Total  $\pi^+p$  (left plot) and  $\pi^-p$  (right plot) cross sections as a function of laboratory momentum,  $p_{\text{Lab}}$ , compared with Regge fits to high energy data. (Adapted from Ref. [18].)

Real CEX  $K^+n$   
amplitude



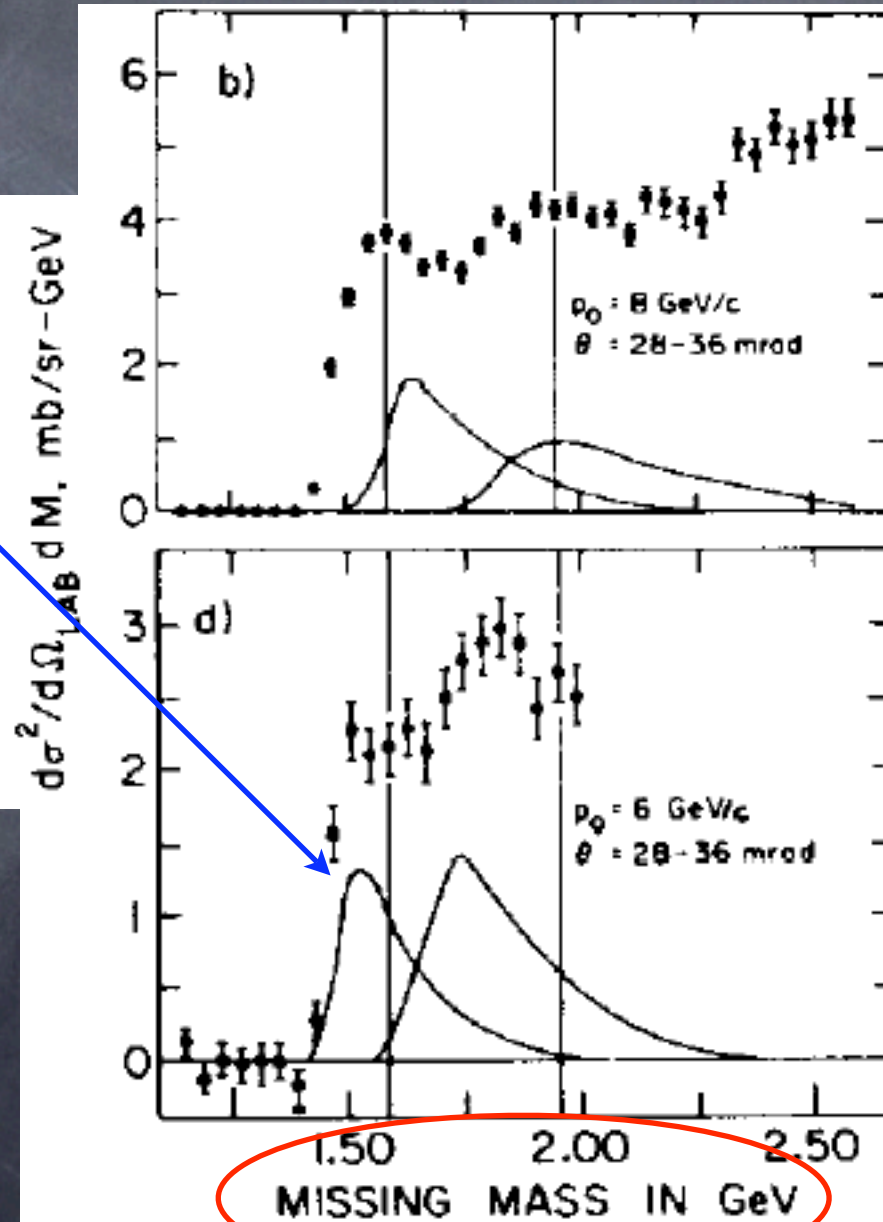
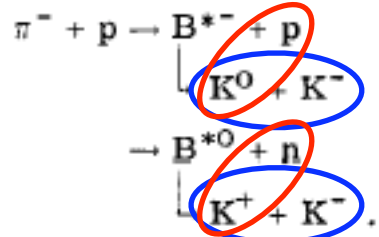
No resonances in  $K^+n$

SEARCH FOR THE  $Z^*$  IN  $\pi^- + p \rightarrow K^- + Z^*$  AT 6 AND 8 GeV/c†

E. W. ANDERSON, E. J. BLESER‡‡, H. R. BLIEDEN, G. B. COLLINS, D. GARELICK

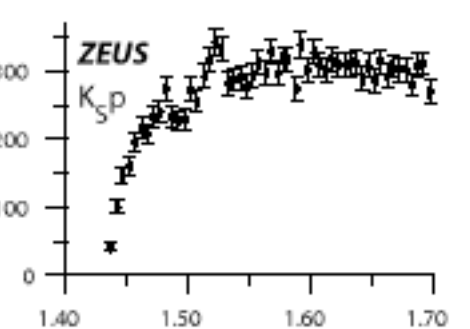
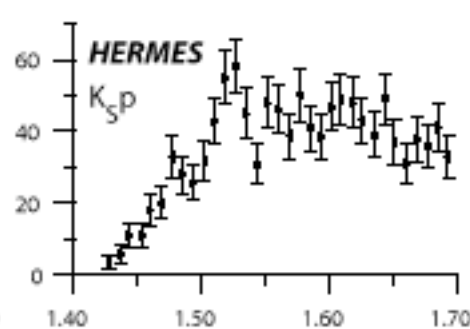
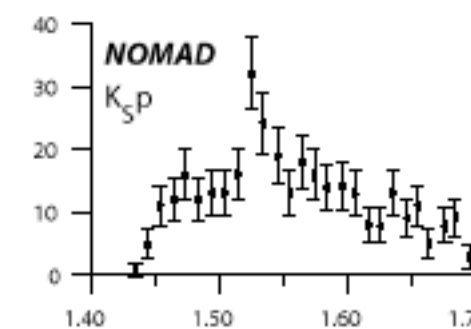
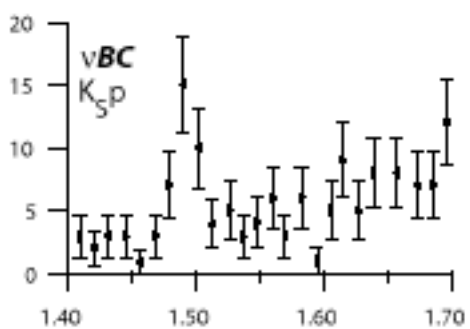
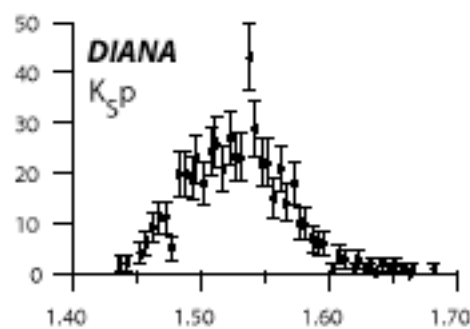
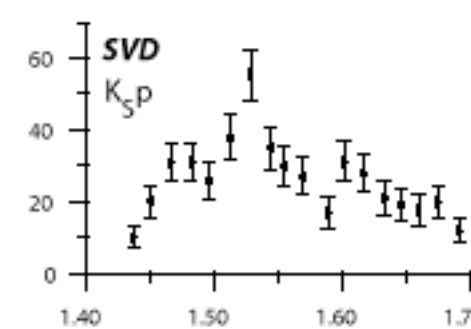
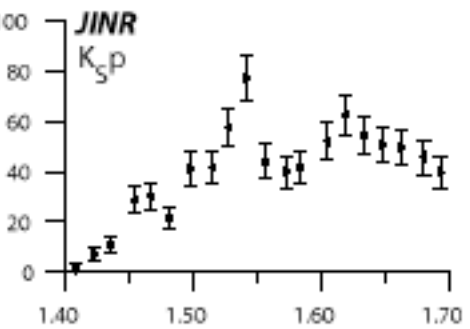
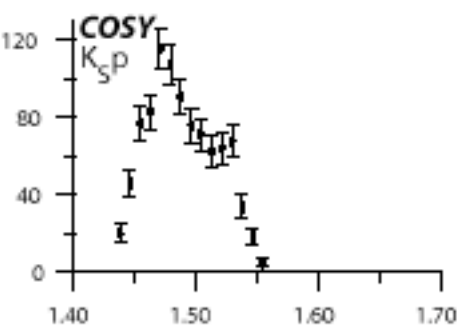
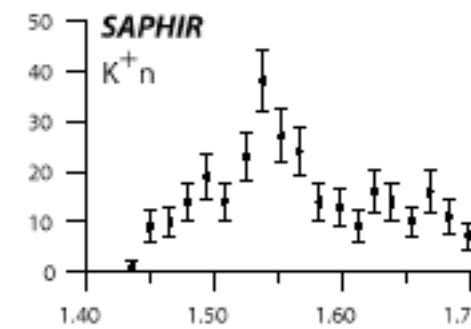
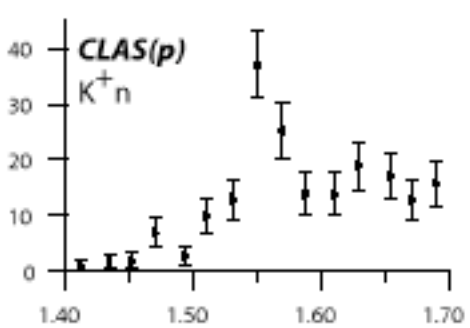
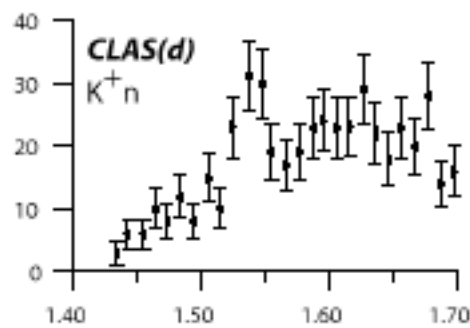
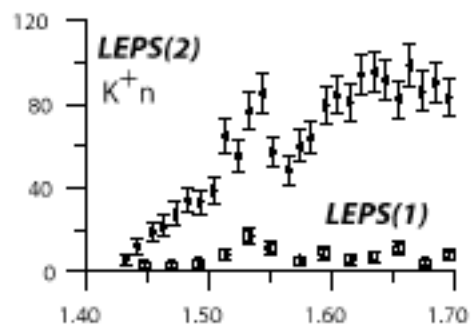
J. MENES and F. TURKOT

Brookhaven National Laboratory, Upton, New York, USA




# Pentaquark sightings

# 5q: positive results



$M(K^+n)$  or  $M(K_S^0 p)$   $GeV/c^2$

**Table 3.** A tabulation of statistics for the observations of the  $\theta^+$ . See text for descriptions of the statistical significance as quoted in the three columns of ratios. The column labeled Published is the significance quoted in the publication.

Experiment	Signal $s$	Background $b$	Significance 			
			Published	$\frac{s}{\sqrt{b}}$	$\frac{s}{\sqrt{s+b}}$	$\frac{s}{\sqrt{s+2b}}$
LEPS(1) [4]	19	17	4.6	4.6	3.2	2.6
LEPS(2) [5]	56	162		4.4	3.8	2.9
CLAS(d) [6]	43	54	5.2	5.9	4.4	3.5
CLAS(p) [7]	41	35	7.8	6.9	4.7	3.9
SAPHIR [8]	55	56	4.8	7.3	5.2	4.3
COSY [9]	57	95	4 – 6	5.9	4.7	3.7
JINR [10]	88	192	5.5	6.4	5.3	4.1
SVD [11]	35	93	5.6	3.6	3.1	2.4
DIANA [12]	29	44	4.4	4.4	3.4	2.7
$\nu$ BC [13]	18	9	6.7	6.0	3.5	3.0
NOMAD [14]	33	59	4.3	4.3	3.4	2.7
HERMES [15]	51	150	4.3 – 6.2	4.2	3.6	2.7
ZEUS [16]	230	1080	4.6	7.0	6.4	4.7

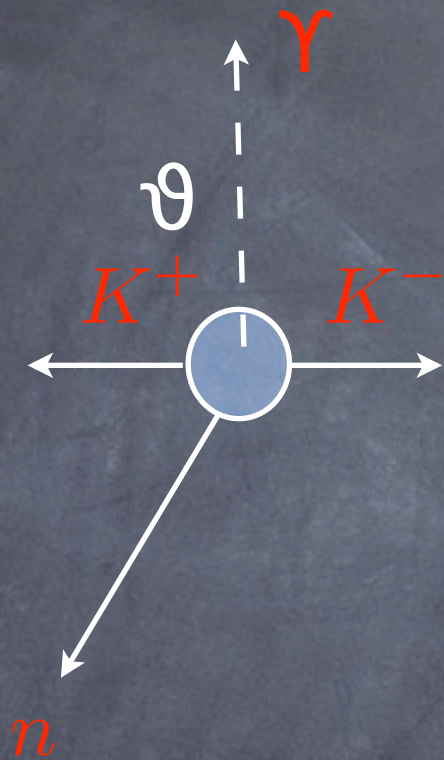


# 5q: negative results

**Table 2.** Recent negative searches for pentaquark states. For each pentaquark state ( $P$ ) we indicated with a  $-$  that the state was not included in the search while  $\Downarrow$  indicates that the state was searched for and not observed and  $\Uparrow$  indicates that the state was searched for and observed.

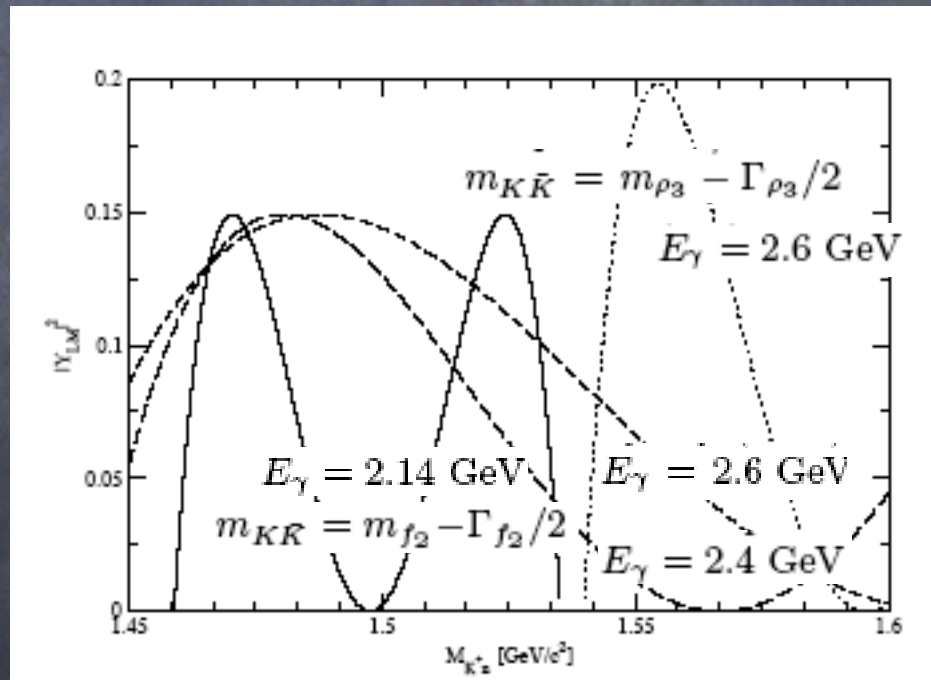
Experiment	Search Reaction	$\theta^+$	$\Xi_5$	$\theta_c$	Reference
ALEPH	Hadronic Z decays	$\Downarrow$	$\Downarrow$	$\Downarrow$	[19]
BaBar	$e^+e^- \rightarrow \Upsilon(4S)$	$\Downarrow$	$\Downarrow$	$-$	[20]
BELLE	$KN \rightarrow PX$	$\Downarrow$	$-$	$\Downarrow$	[21]
BES	$e^+e^- \rightarrow J/\psi(\psi(2S)) \rightarrow \theta\bar{\theta}$	$\Downarrow$	$-$	$\Downarrow$	[22]
CDF	$p\bar{p} \rightarrow PX$	$\Downarrow$	$\Downarrow$	$\Downarrow$	[23]
COMPASS	$\mu^+(\text{}^6\text{LiD}) \rightarrow PX$	$\Downarrow$	$\Downarrow$	$-$	[24]
DELPHI	Hadronic Z decays	$\Downarrow$	$-$	$-$	[25]
E690	$pp \rightarrow PX$	$\Downarrow$	$\Downarrow$	$-$	[26]
FOCUS	$\gamma p \rightarrow PX$	$\Downarrow$	$\Downarrow$	$\Downarrow$	[27]
HERA-B	$pA \rightarrow PX$	$\Downarrow$	$\Downarrow$	$-$	[28]
HyperCP	$(\pi^+, K^+, p)Cu \rightarrow PX$	$\Downarrow$	$-$	$-$	[29]
LASS	$K^+p \rightarrow K^+n\pi^+$	$\Downarrow$	$-$	$-$	[30]
L3	$\gamma\gamma \rightarrow \theta\bar{\theta}$	$\Downarrow$	$-$	$-$	[25, 31]
PHENIX	$AuAu \rightarrow PX$	$\Downarrow$	$-$	$-$	[32]
SELEX	$(\pi, p, \Sigma)p \rightarrow PX$	$\Downarrow$	$-$	$-$	[33]
SPHINX	$pC(N) \rightarrow \theta^+C(N)$	$\Downarrow$	$-$	$-$	[34]
WA89	$\Sigma^-N \rightarrow PX$	$-$	$\Downarrow$	$-$	[36]
ZEUS	$ep \rightarrow PX$	$\Uparrow$	$\Downarrow$	$\Downarrow$	[16, 37, 38]

# Kinematic reflections in $\gamma n \rightarrow K^+ K^- n$



A  $K^+K^-$  resonance in its rest frame distributes  $K$ 's according to its spin  $\sim Y_{SM}(\theta)$

3-body kinematics  $\cos(\theta) \sim M_{K+n}$



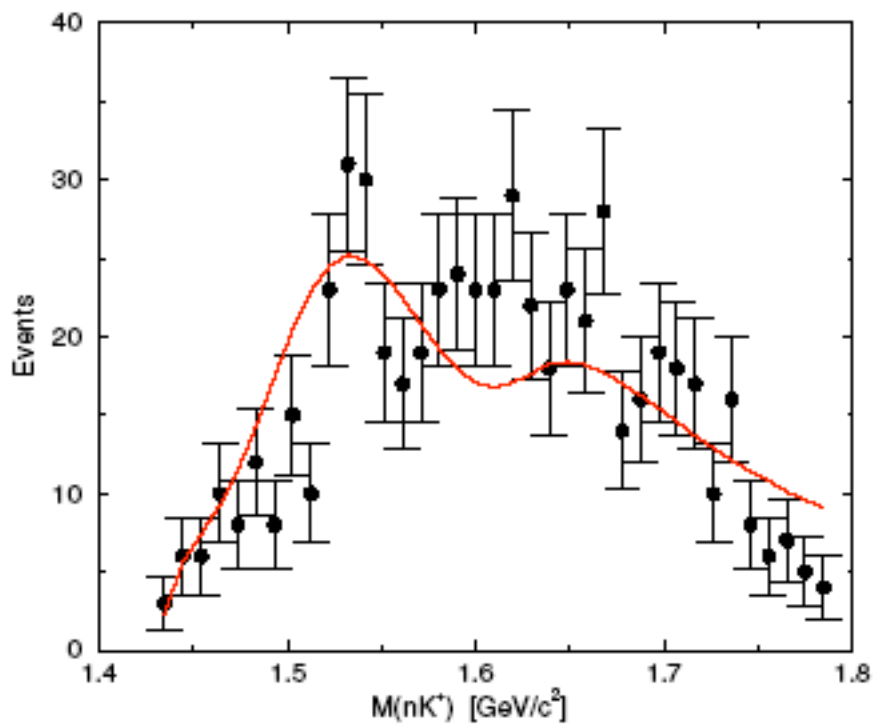
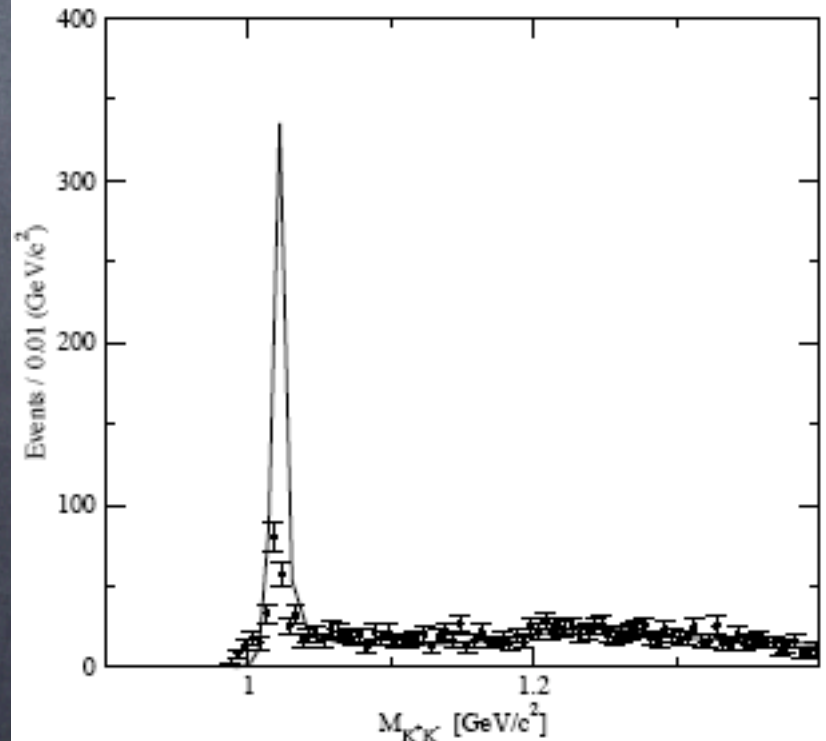


FIG. 3: The calculated (solid line)  $m_{KN}$  distribution, as described in the text, compared with the data from [2]

Physical background  
has structure >>  
reduces the statistical  
significance of the  
signal

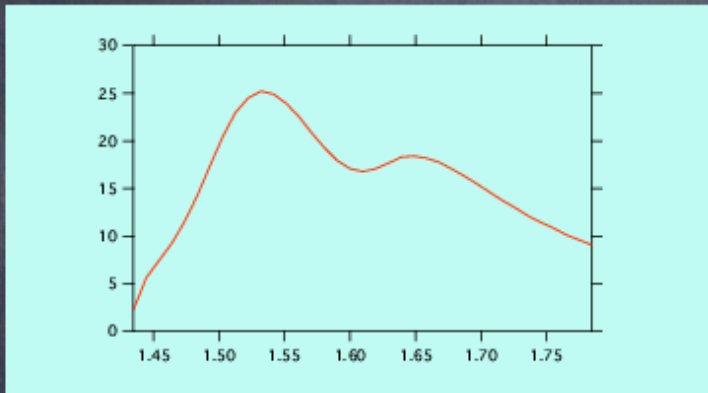
Reaction	Beam energy GeV	Cross Section $\mu\text{b}$	Ref
$\gamma\text{p} \rightarrow f_2\text{p}$	2.3-2.6	$1.3 \pm 0.37$	[6]
$\gamma\text{p} \rightarrow f_2\text{p}$	2.6-3.25	$0.39 \pm 0.13$	[6]
$\gamma\text{p} \rightarrow f_2\text{p}$	3.25-4.0	$0.19 \pm 0.06$	[6]
$\gamma\text{p} \rightarrow f_2\text{p}$	4.0-6.3	$0.1 \pm 0.1$	[6]
$\gamma\text{p} \rightarrow a_2^+\text{n}$	$4.2 \pm 0.5$	$1.14 \pm 0.43$	[7]
$\gamma\text{p} \rightarrow a_2^+\text{n}$	$5.25 \pm 0.55$	$0.85 \pm 0.43$	[7]
$\gamma\text{p} \rightarrow a_2^+\text{n}$	$7.5 \pm 0.7$	$0.43 \pm 0.43$	[7]
$\gamma\text{p} \rightarrow \text{K}^+\text{K}^-\text{p}$	2.8	$1.0 \pm 0.1$	[8]
$\gamma\text{p} \rightarrow \text{K}^+\text{K}^-\text{p}$	4.7	$0.7 \pm 0.1$	[8]

TABLE I: Photoproduction cross sections for the  $f_2(1275)$  and  $a_2(1320)$  resonances and the  $\text{K}^+\text{K}^-$  final state.

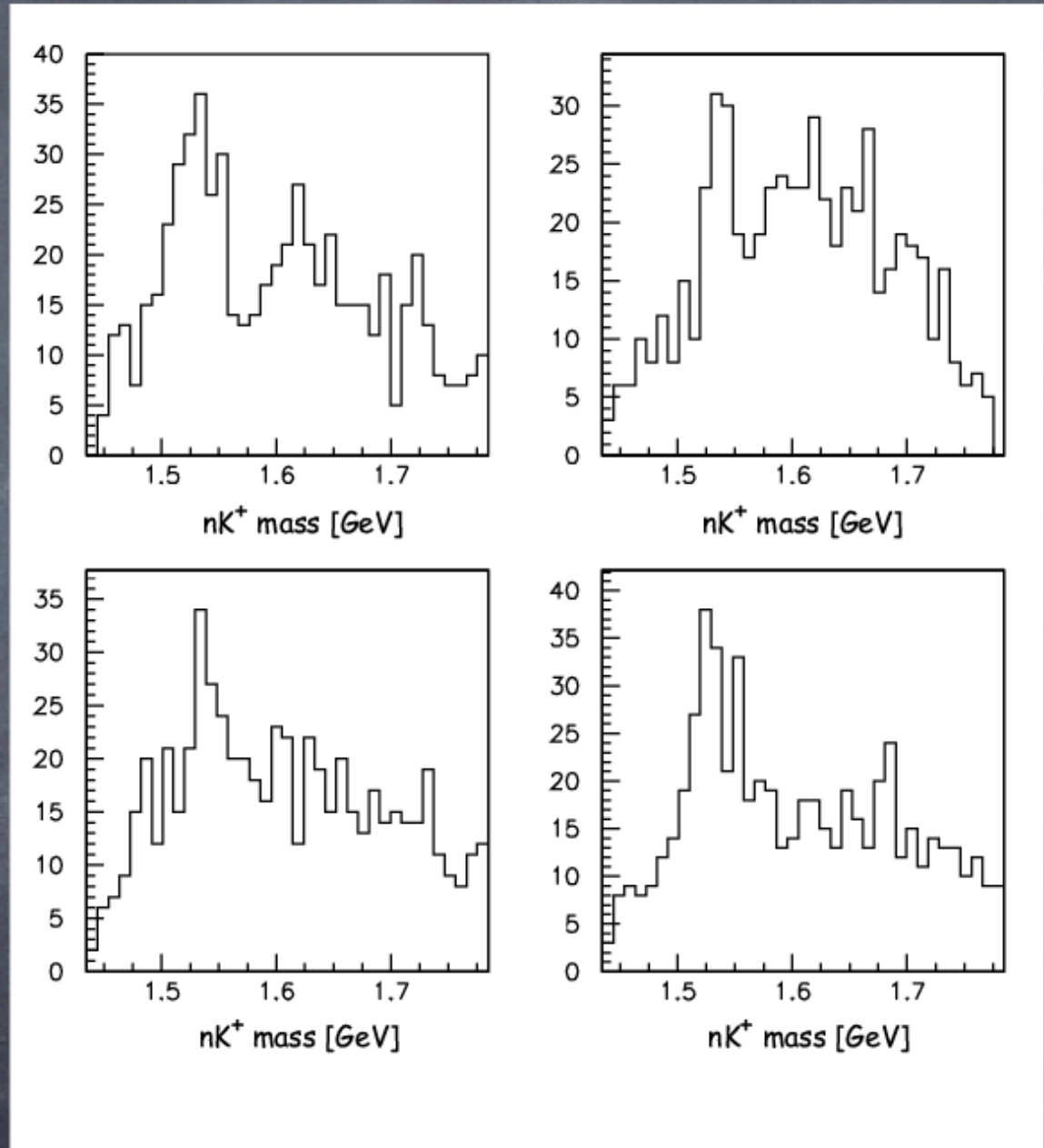


# Fake Peaks

Enhancement is broad  
- but starting with:

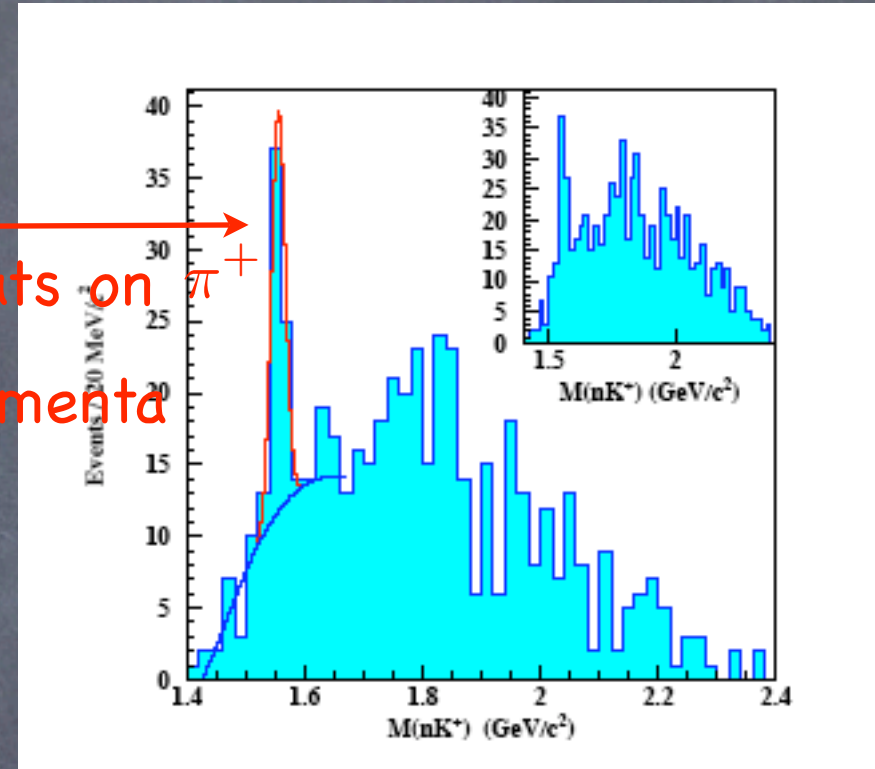
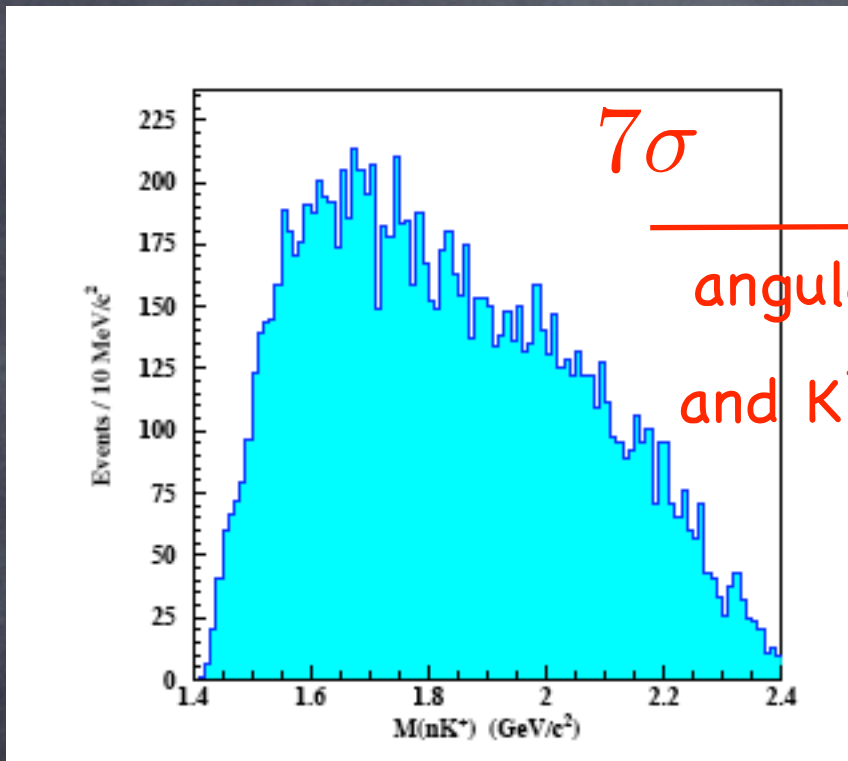


as a parent distribution  
generate 40 random  
histograms with 600  
events each - 3 of these  
along with CLAS results  
appear here

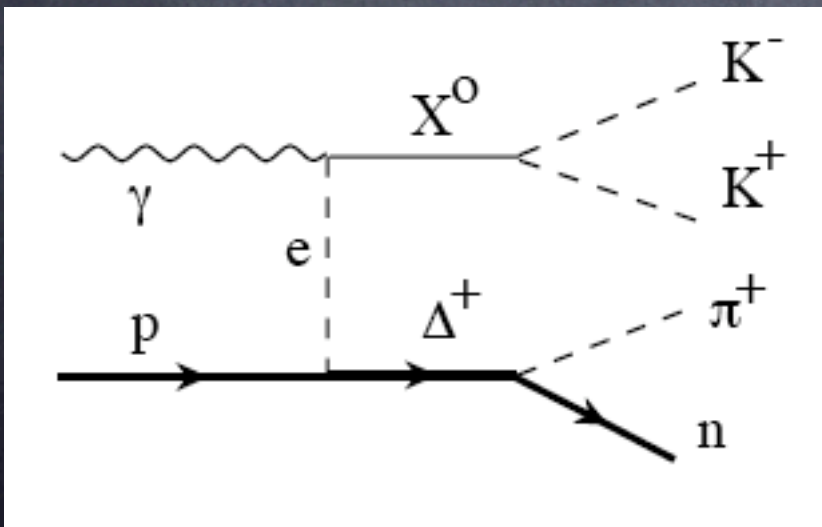


# CLAS (proton)

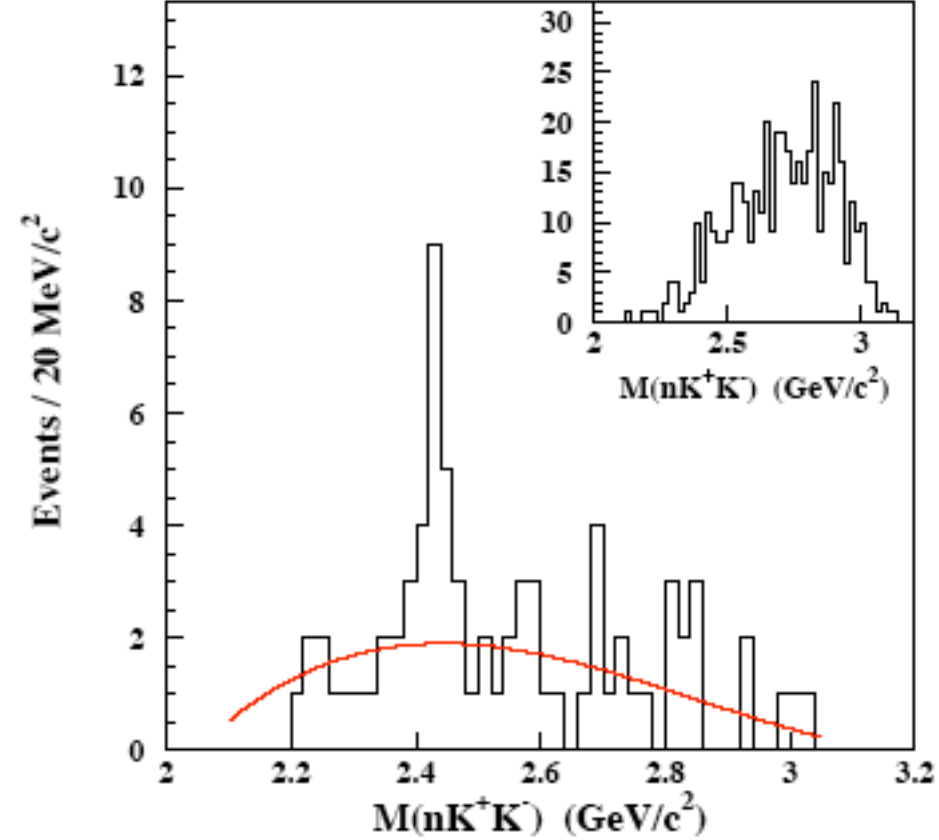
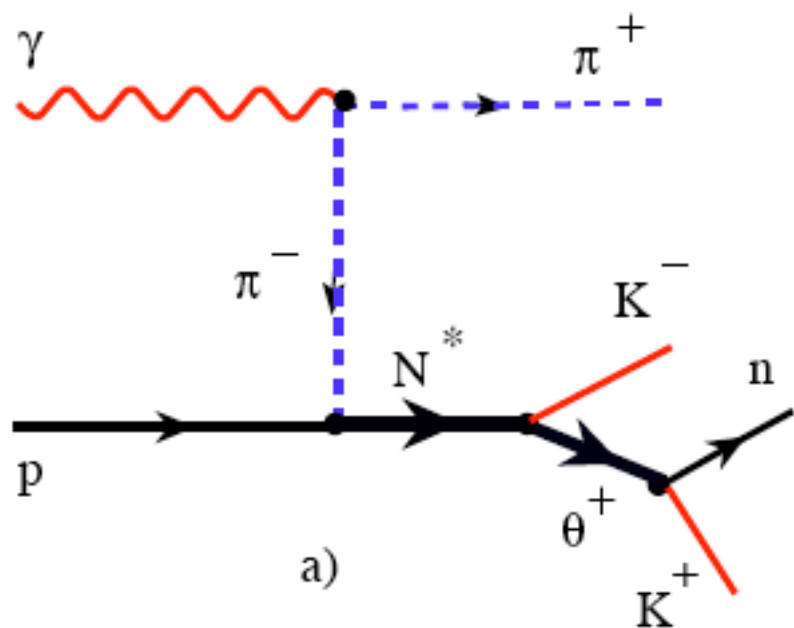
$$\gamma p \rightarrow \pi^+ K^- K^+ n$$



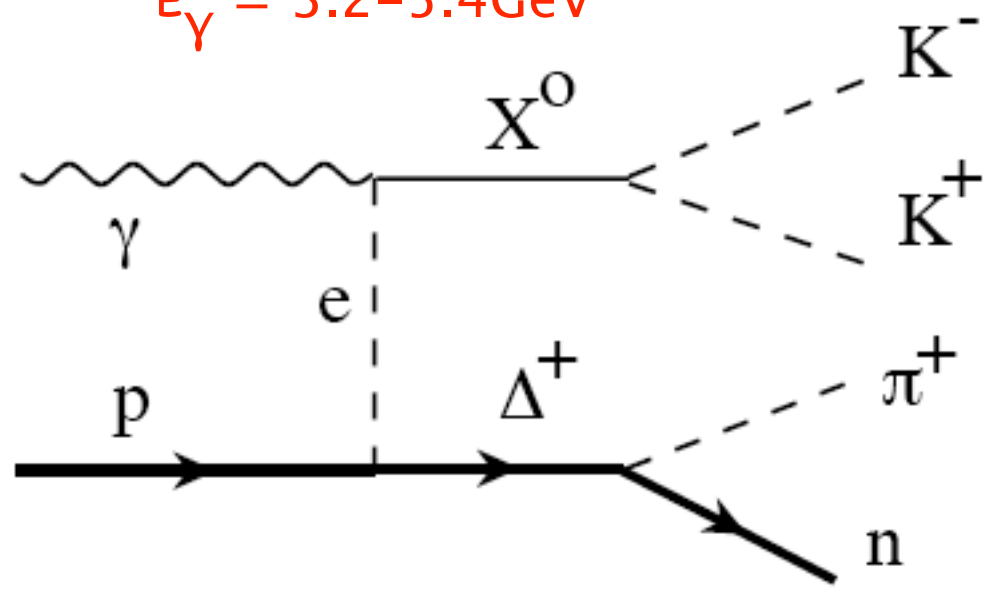
angular cuts on  
and  $K^+$  momenta



Can generate resonance-like structure in  $K^+K^-n$  spectrum and  $\pi^+$  momentum cut enhances kinematic reflections from decays of  $K^+K^-$  resonances



$E_\gamma = 3.2-5.4\text{GeV}$



### Threshold energies

- $X=f_2$        $W=2.51\text{GeV}$
- $X=a_2$        $W=2.55\text{GeV}$
- $X=\rho_3$       $W=3.31\text{GeV}$

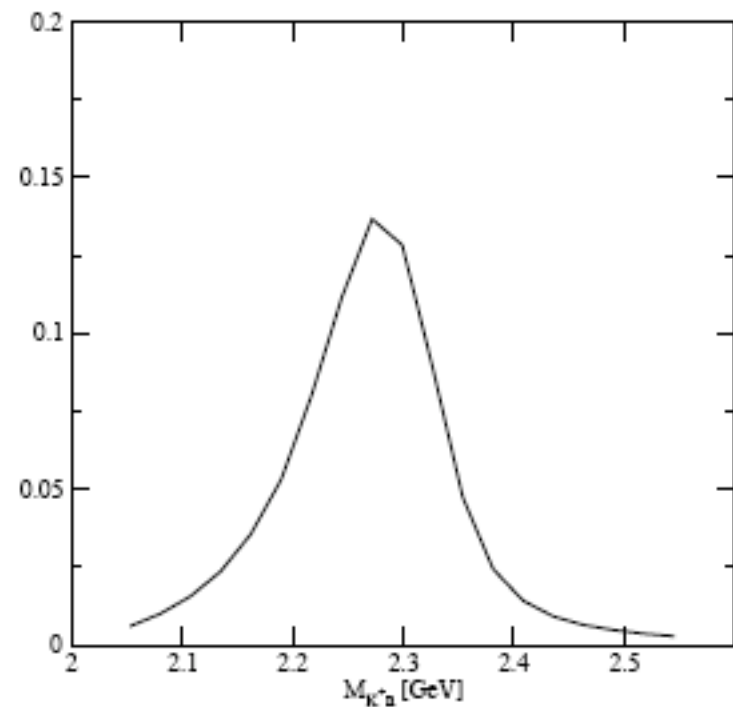
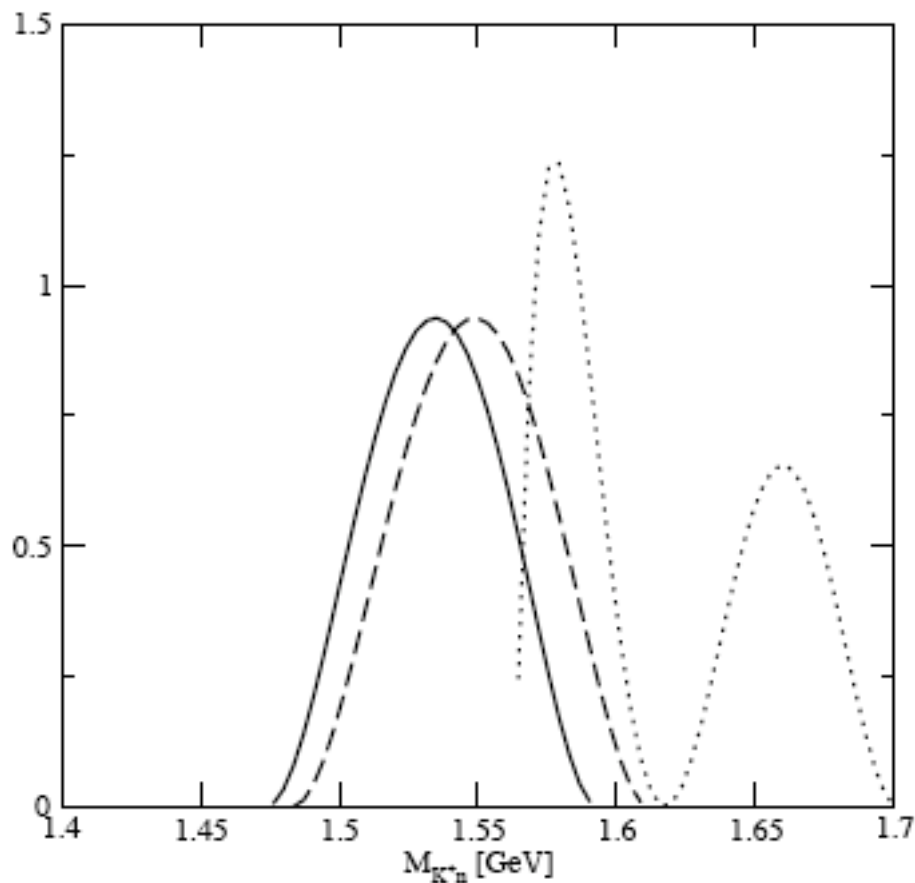


FIG. 3: The  $nK^+$  mass distribution as described by  $\int d\phi_{K^+} |Y_{J_X, \lambda_X}(\theta_{K^+n}, \phi_{K^+})|^2$ , for  $\Delta = \Delta(1232)$  and  $J_X = \lambda_X = 2$ ,  $X = f_2$ , (solid line),  $J_X = \lambda_X = 2$ ,  $X = a_2$ , (dashed line), and  $J_X = 3$ ,  $\lambda_X = 1$ ,  $X = \rho_3$  (dotted line). The  $M_{nK^+K^-}$  invariant masses for the three cases are 2.22, 2.27 and 2.64 GeV, respectively.

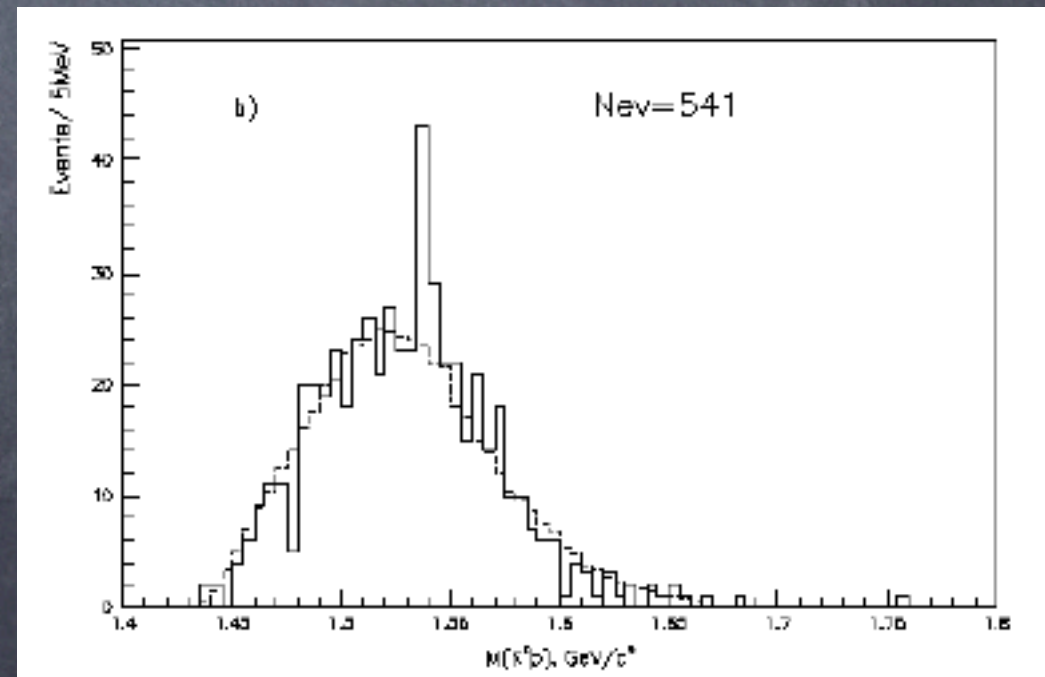
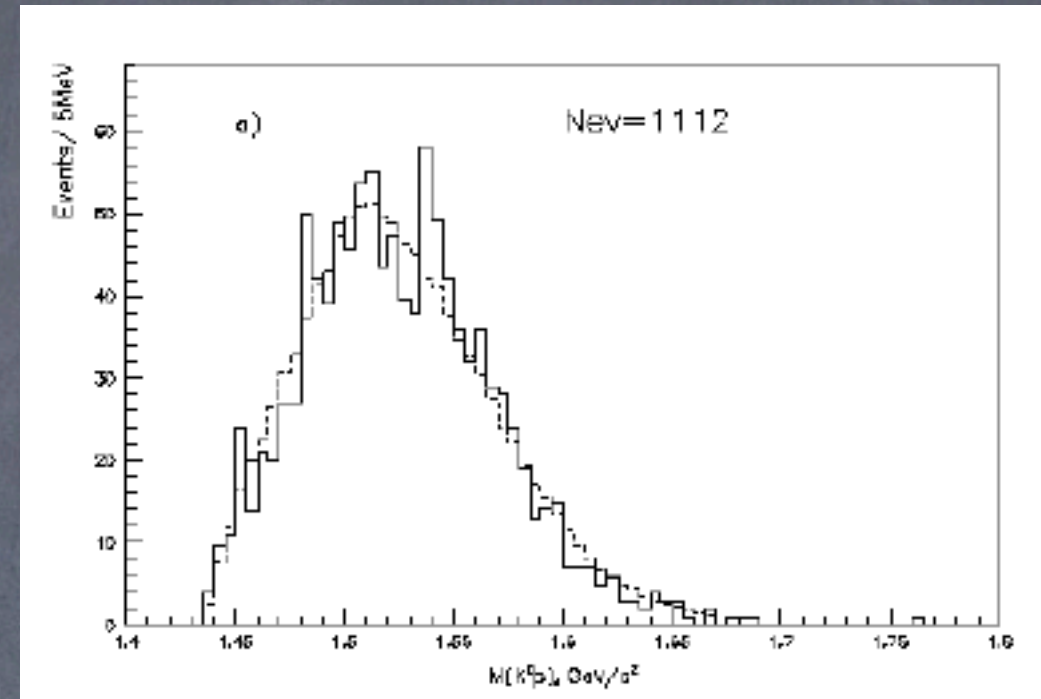
# DIANA (ITEP, Xe bubble chamber, 850MeV K-beam)



no magnetic field

particle identified by  
their range in Xe

angular cut, p and Ks  
in the forward direction





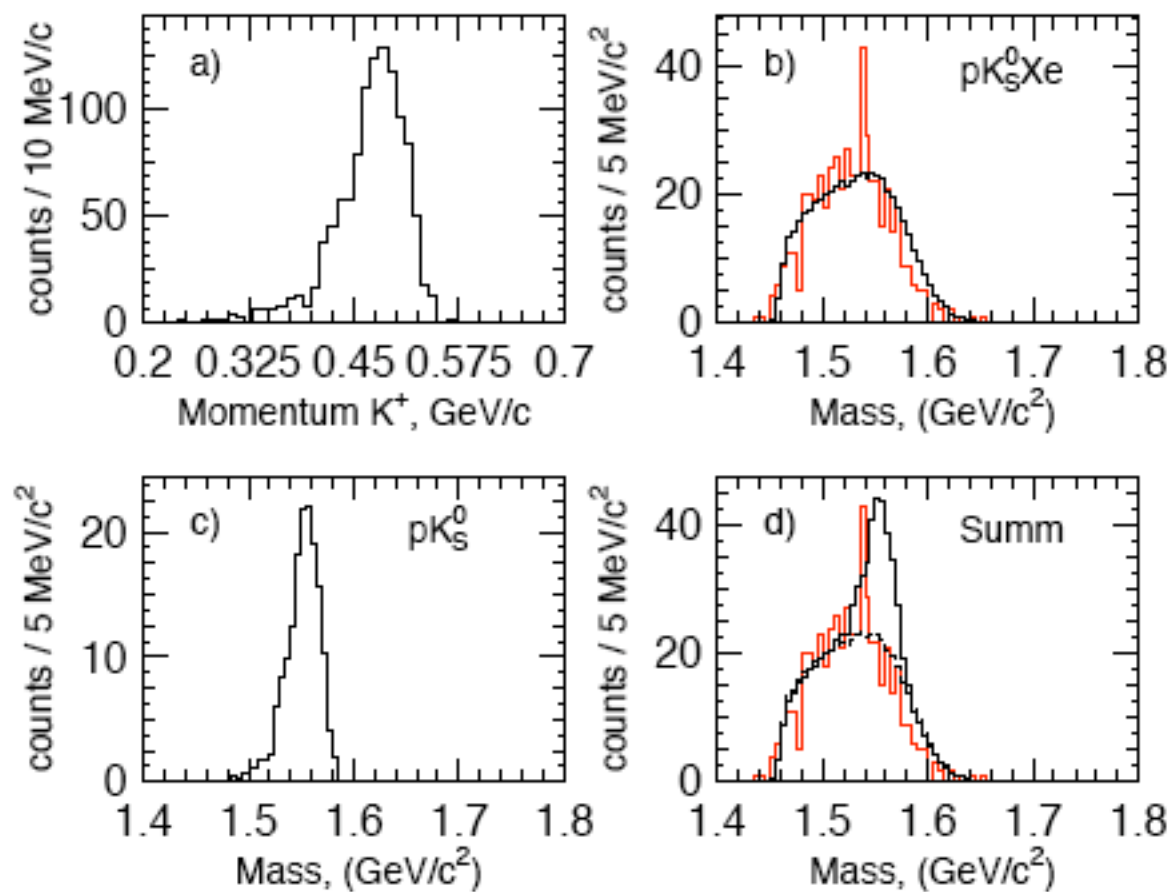
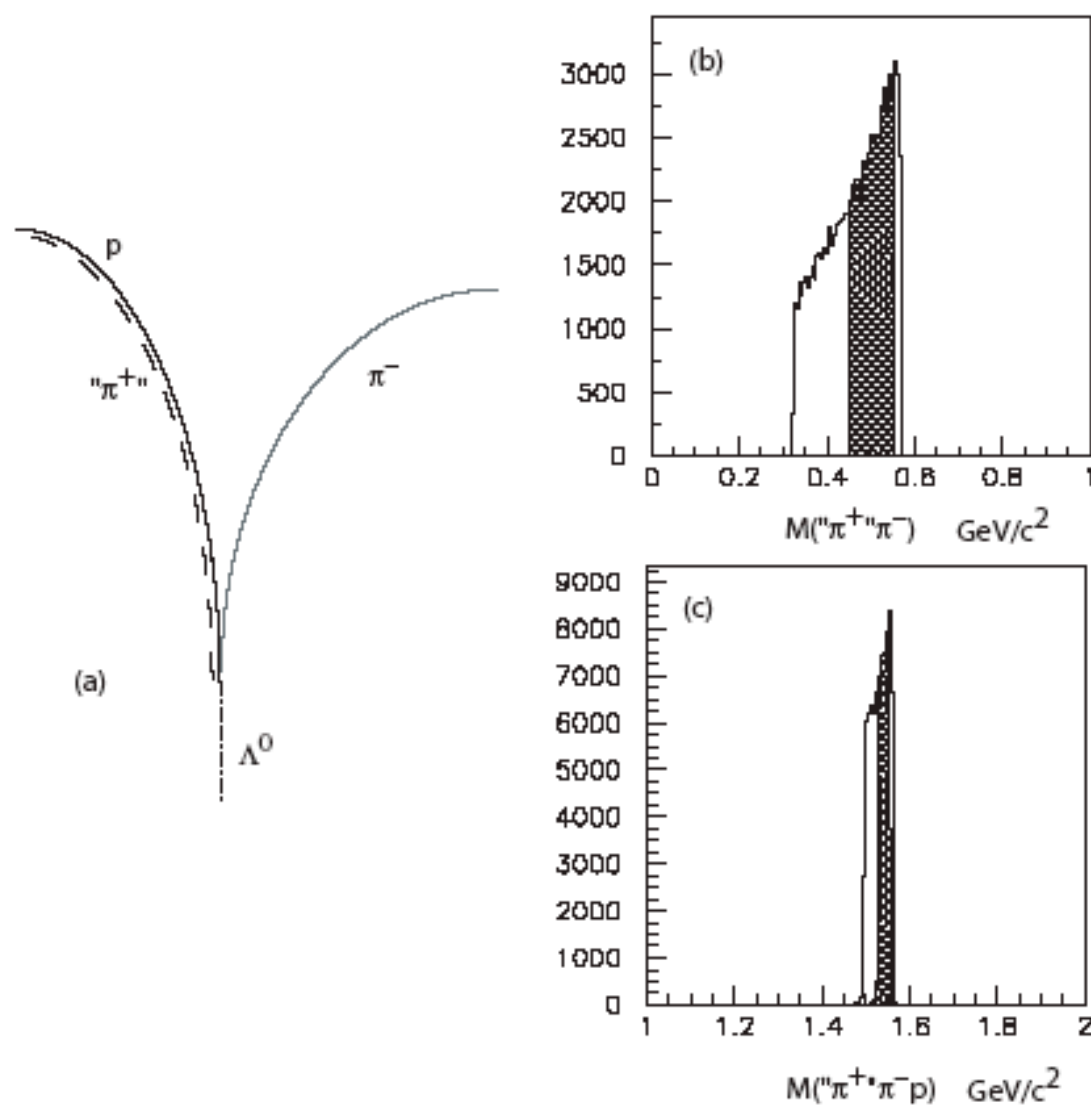
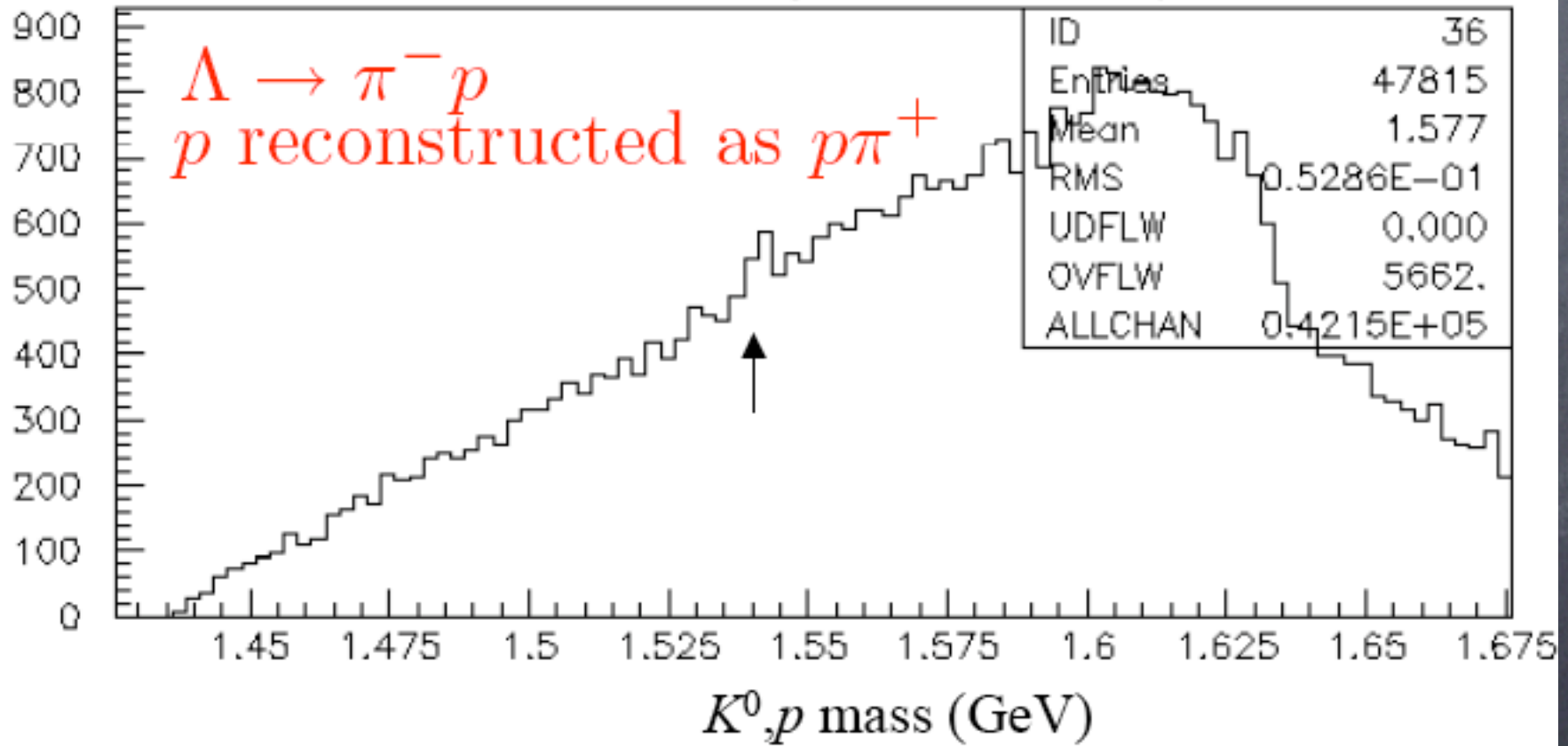


Figure 2: The experimental beam momentum [5] and MC mass spectra distribution corresponding to: b) reaction  $K^+Xe \rightarrow K_S^0 p X e'$ ; c) reaction  $K^+n \rightarrow K_S^0 p$ ; d) the summ of both b) and c); The histogram in red corresponds to the experimental mass distribution from [5].



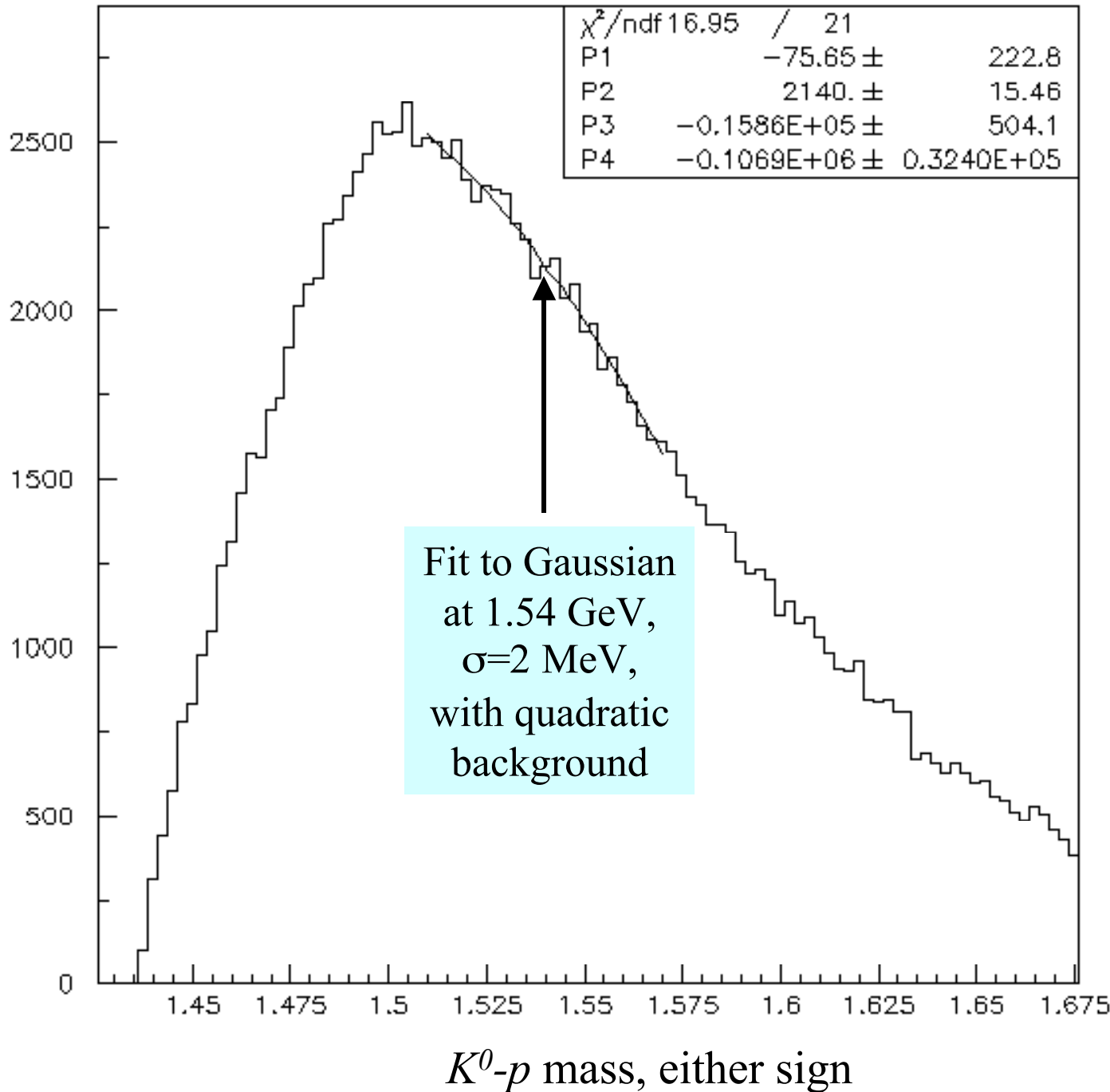
**Figure 5.** Figure (a) is a schematic of the decay  $\Lambda^0(1115) \rightarrow \pi^- p$ . The effect of spurious *ghost* tracks from the reconstruction software is considered. In this case a  $\pi^+$  track is generated. When combined with the  $\pi^-$  from the  $\Lambda^0$  the effective mass clusters about  $0.5 \text{ GeV}/c^2$  as in Figure (b) and when the ghost track is combined with the  $\Lambda^0$  decay products the effective mass clusters around  $1.5 \text{ GeV}/c^2$  as seen in Figure (c). In the shaded distributions the " $\pi^+\pi^-$ " mass is required to be near the  $K_S^0$ . The mean of the shaded portion of the distribution in Figure (c) is  $1.54 \text{ GeV}/c^2$ , the mass of the  $\theta^+$ . In this study the  $\Lambda^0$  momentum in the LAB frame was uniform from 2 to 100  $\text{GeV}/c$ .

POS BEAM,-50.It.Z It 150,MOM3.gt.0.4\*Ptot,NoGHOST/LAMBDA CUTS



Hyper CP @ FNAL

POS BEAM, -50.lt.Z.lt.150,MDM3.gt.0.5\*Ptot



E871/HyperCP,  
M.Longo @ QNP04

90% CL limit  
~370 events out  
of 150000  $K^0$ - $p$   
candidates.

P1 is the  
amplitude of  
the gaussian.  
Bins are 2 MeV

HyperCP Preliminary

Pentaquark sightings come from low statistics, low resolution, low-energy experiments with kinematically constrained final states after complicated cuts are imposed.

High resolution, high statistics, experiments with both low- and high- particle multiplicity do not report the pentaquarks.



# 3-particle Dalitz plot

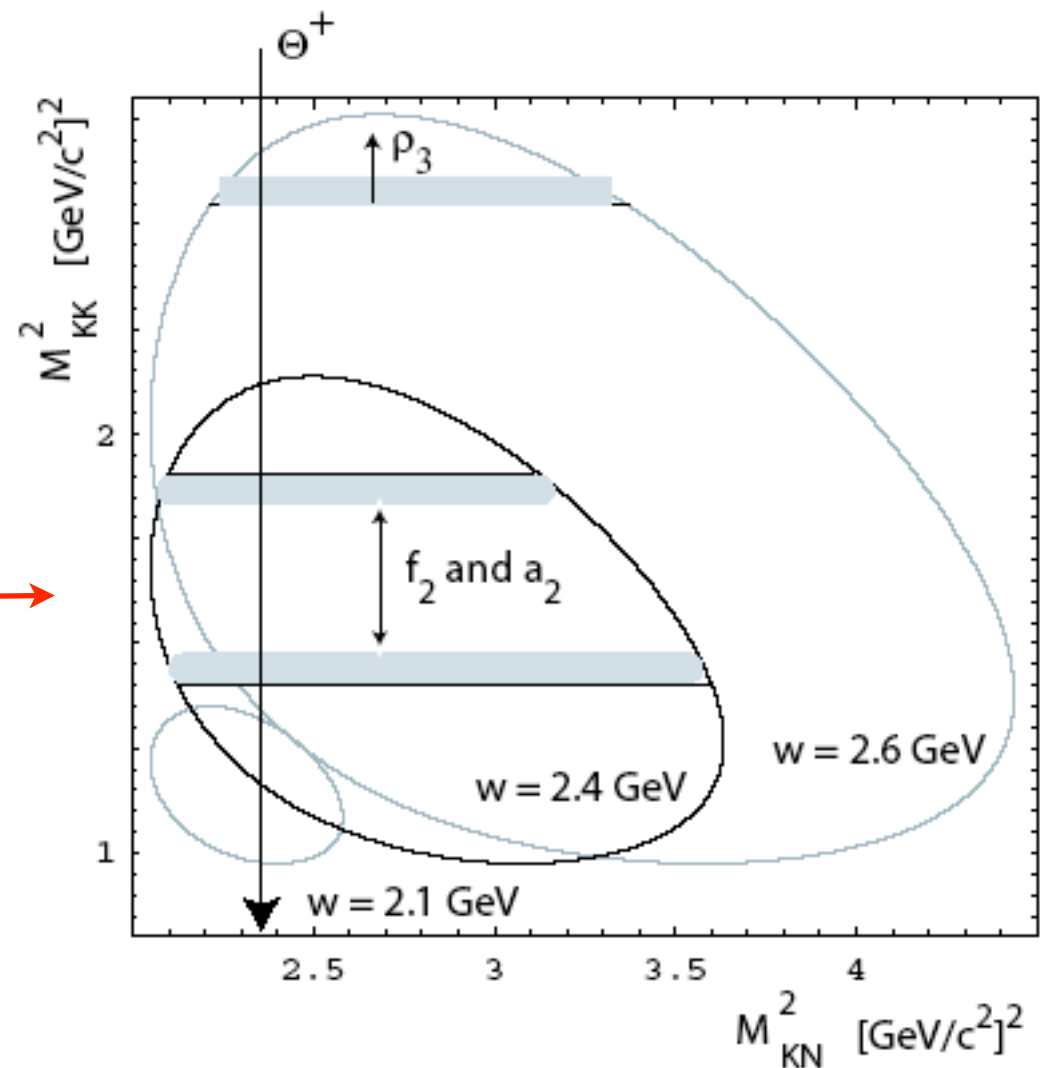
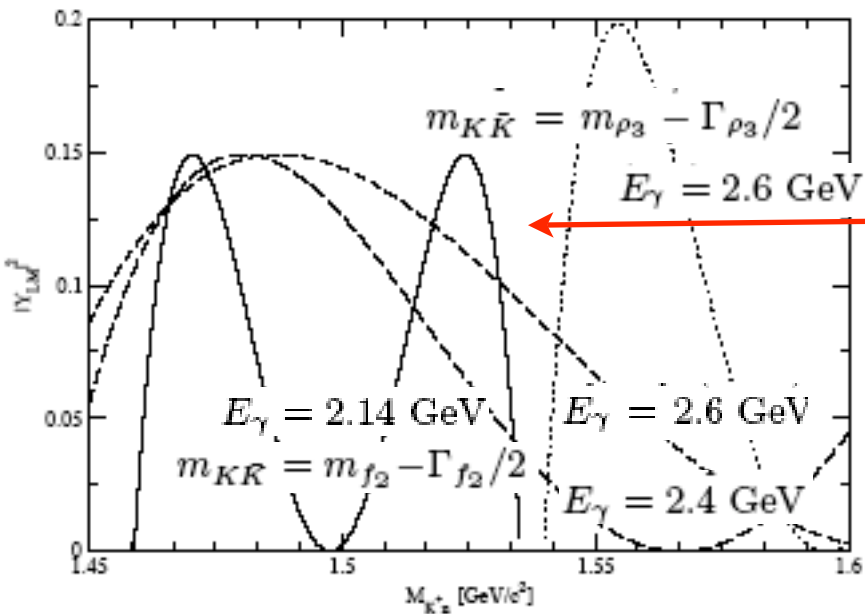


FIG. 1: Boundaries of the  $m_{KK}^2$  versus  $m_{KN}^2$  Dalitz plot for three different values of  $w$ , the energy available to the  $K\bar{K}N$  system, 2.1, 2.4 and 2.6 GeV. For the data of ref. [2], the observed distribution in  $w$  rises from 2.1 GeV, peaks at 2.4 and falls to zero near 2.6 GeV. Horizontal lines denote the region spanned by the  $f_2$  and  $a_2$  mesons defined by their half-widths and the region of the  $\rho_3$  starting with its central mass less its half-width. The vertical line denotes the square of the  $\Theta^+$  mass.

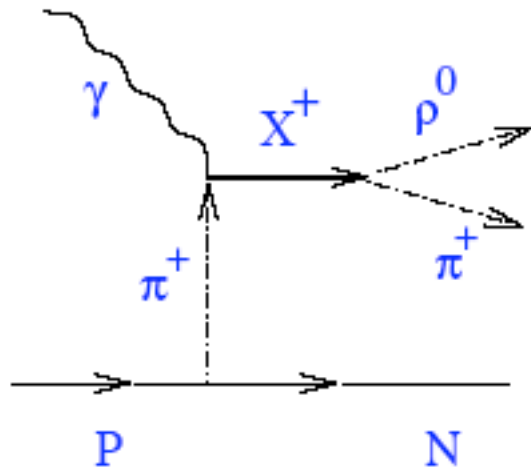
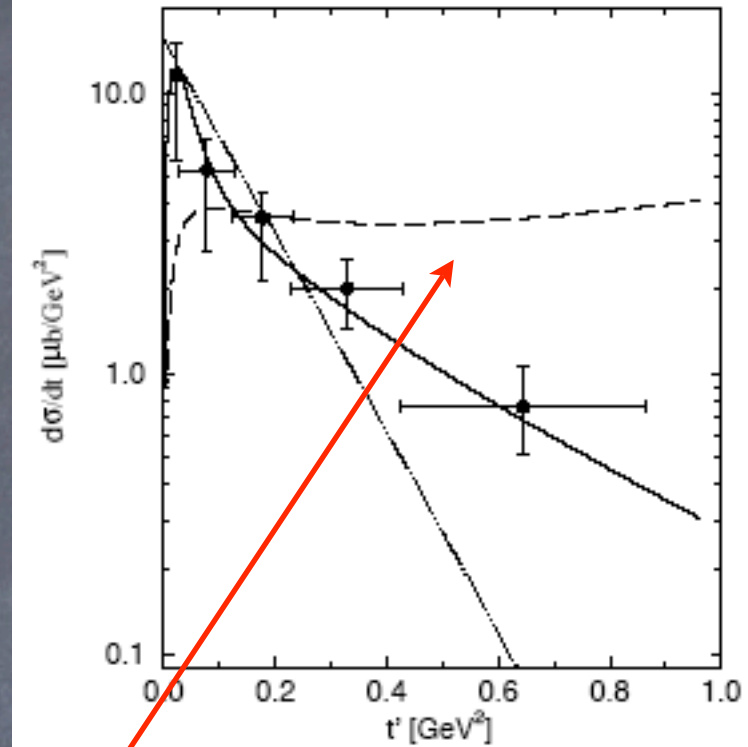


Fig. 1.  $\rho^0\pi^+$  photoproduction via one-pion-exchange.

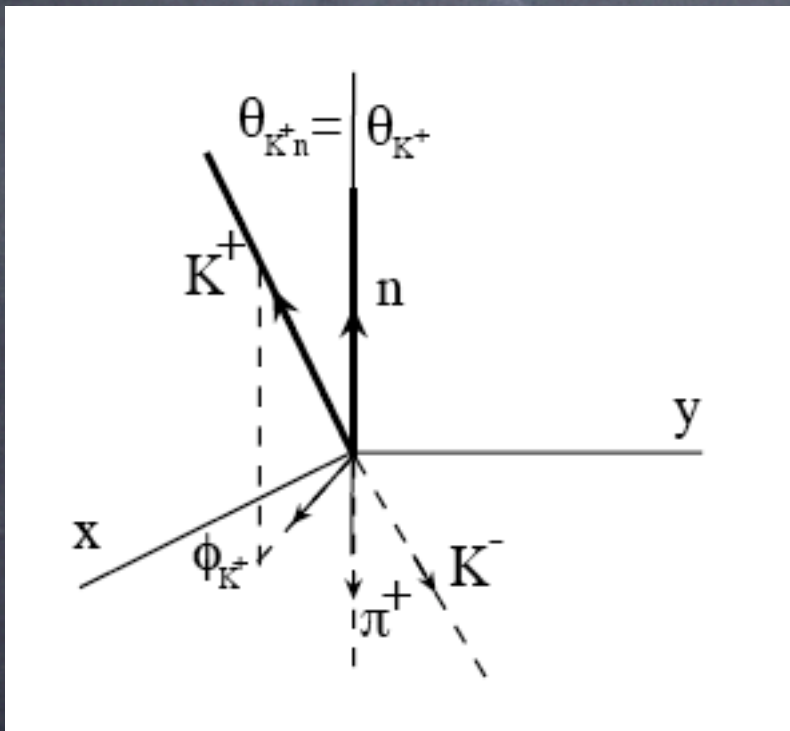
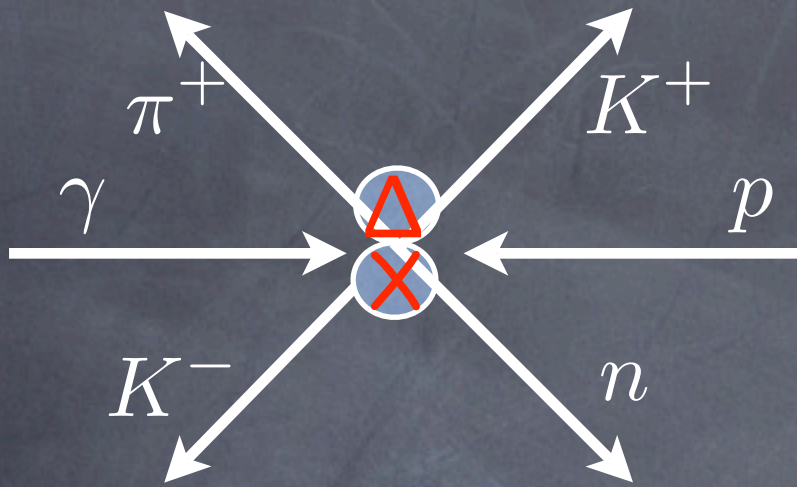


$$\frac{d\sigma}{dt}(\gamma p \rightarrow A_2^+ n) = \frac{\pi}{64} \frac{g_{\pi NN}^2}{4\pi} \frac{g_{A\pi\gamma}^2}{4\pi} \times \frac{1}{m_A^6 k^2 s} \frac{|t|(t-m_A^2)^4}{(t-\mu^2)^2},$$

There is no known method for "fine tuning" Regge theory

Fig. 3. Momentum transfer dependence of  $a_2^+$  photoproduction cross section. Data is from Ref. [15]. Solid line is the OPE prediction corrected to account for absorption. Dashed line is the pure OPE prediction and the dotted line is the  $A \exp(-bt)$  parameterization.



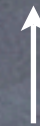


"N\*" mass

$$M_{N^*} = 2.23 \text{ GeV}$$

$$M_{N^*} = 2.27 \text{ GeV}$$

$$M_{N^*} = 2.64 \text{ GeV}$$



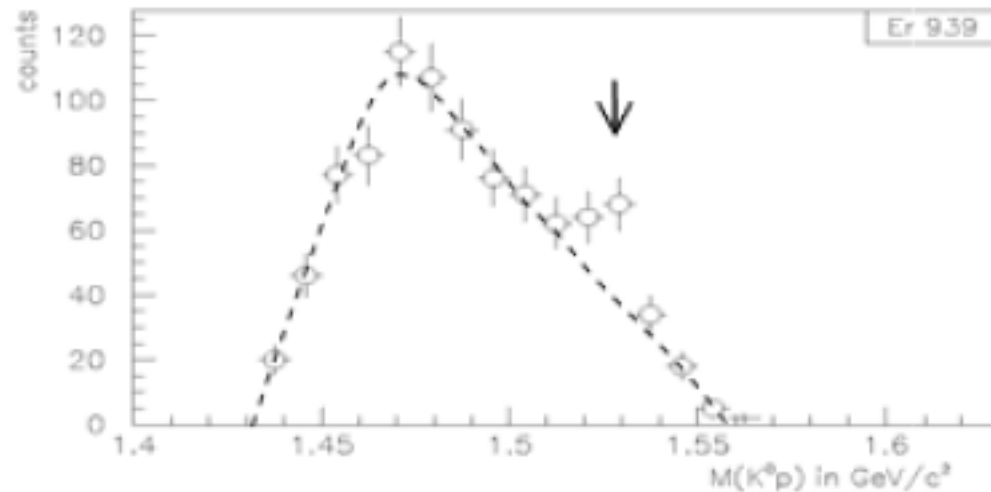
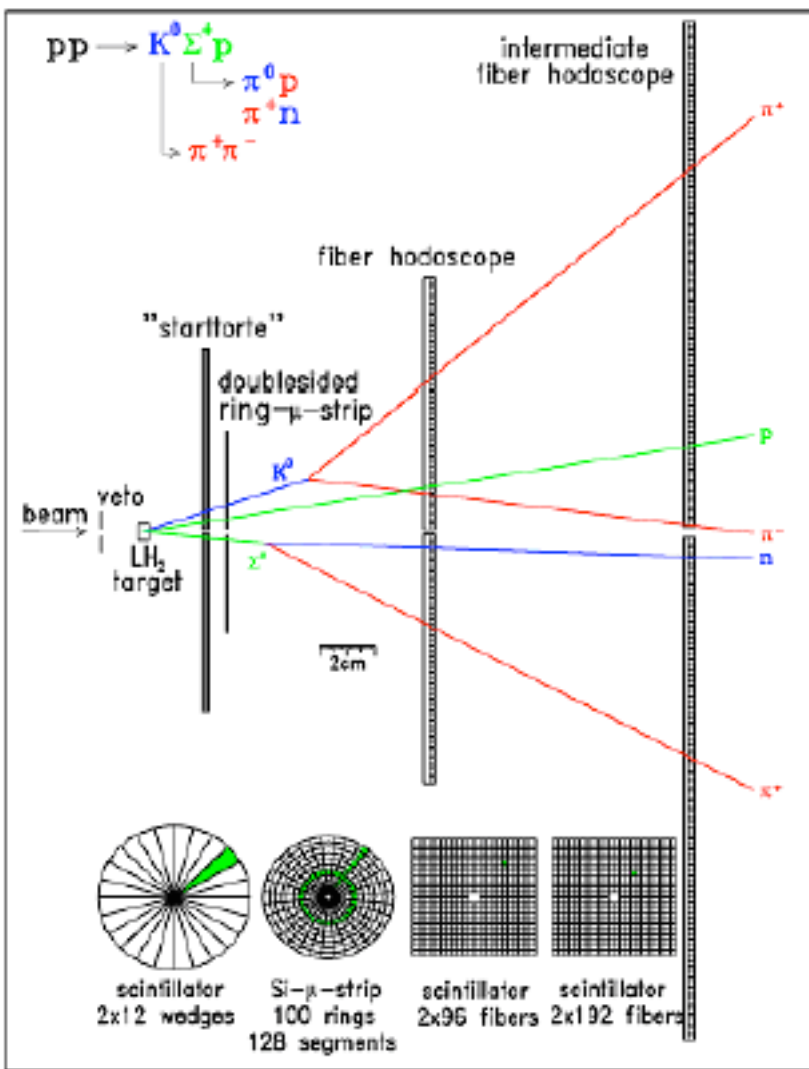
$$M_{nK^+K^-} = M_{N^*}$$

is sharp !

$$\cos \theta_{\pi}^* > 0.8$$

correlates  $n$  with  $K^+ K^-$  helicity  $\rightarrow$  possible kinematic reflection  
from  $K^+ K^-$  resonance

# COSY-TOF $pp \rightarrow \Sigma^+ K_S^0 p$



no magnetic field, PID,  
pure geometry TOF no  
used in this analysis !

