

#### Outline

- Why is the forward region important?
- Forward jet selection
- Theoretical Calculations / MC Models
- Results
- Conclusions



Albert Knutsson - Forward Jets in DIS



Test QCD at small x. Signals of parton dynamics beyond DGLAP?





## **Kinematic range and Measurements**

#### Kinematic range

 $5 < Q^2 < 85 \text{ GeV}^2$ 0.1 < y < 0.7 $0.0001 < x_{Bj} < 0.004$  $10 \text{ GeV} < E'_e$ 

#### Measurements

Forward jet cross-sections  $\frac{d\sigma}{dx_{Bj}}$   $\frac{d\sigma}{d^3\sigma}$   $\frac{d^3\sigma}{dx_{Bj}dp_t^2 dQ^2}$  2+Forward jet cross-sections,  $\frac{d\sigma}{d\Delta\eta_2}$ 

As a function of the rapidity

between the forward jet and

the most forward di-jet.



PDF: CTEQ6L ,  $\gamma$ PDF: SaS1D Scales:  $\mu_r^2 = \mu_f^2 = Q^2 + p_t^2$ 

#### **QCD** Models continue...

CDM (ARIADNE): LO ME (QPM, BGF). Color Dipole Model (QCDC and higher orders). Random walk in  $k_t$ .



PDF: CTEQ6L

CASCADE: LO ME. Initial state CCFM partons showers with emissions ordered in angle.

# **Fixed Order Calculations**

DISENT: NLO di-jet  $(\alpha_s^2)$ . (Forward jet cross-sections.) NLOJET++: NLO 3-jet  $(\alpha_s^2)$ . (2+forward jet cross-sections.)



(Need to correct for hadronization effects.)

# $\frac{d\sigma}{dx_{Bj}}$

#### Comparison to Exact Calculations (DISENT)



$$egin{aligned} \mu_{r}^{2} &= p_{t}^{2} \ \mu_{f}^{2} &= \langle p_{t, ext{fwdjet}}^{2} 
angle &= 45 \; ext{GeV}^{2} \ 0.25 \mu_{r,f}^{2} &< \mu_{r,f}^{2} &< 4 \mu_{r,f}^{2} \ ext{PDF: CTEQ6M} \end{aligned}$$

- NLO di-jet ok for larger  $x_{Bj}$ .
- LO contribution  $(\alpha_s) \ll$  NLO contribution  $(\alpha_s^2)$

# $\frac{d\sigma}{dx_{Bj}}$

#### Comparison to QCD Models



- PS with DGLAP evolution similar to NLO.
- RG DIR+RES best.
- CDM and RG DIR+RES too low for lower  $x_{Bj}$ .
- CASCADE to low at lower  $x_{Bj}$ , to high at higher  $x_{Bj}$ .
- All models to low in lowest  $x_{Bj}$ -bin.





Cross-section as a function of  $x_{Bj}$ in  $3x3 p_t^2 \cdot Q^2$  bins. No  $\frac{p_t^2}{Q^2}$ -cut. (Different regions in  $\frac{p_t^2}{Q^2} = r.$ )

> Large  $x_{Bj}$ ,  $Q^2$  and  $p_t^2 \Rightarrow$ NLO describes data Smaller  $x_{Bj}$ ,  $Q^2$  and  $p_t^2 \Rightarrow$ NLO insufficient

Note different ranges in  $x_{Bj}!$ 





Comparison to QCD models.

 $p_T^2 < Q^2 \ (r < 1)$ -DGLAP-like dynamics  $p_T^2 \sim Q^2 \ (r \sim 1)$ -BFKL-like dynamics  $p_T^2 > Q^2 \ (r > 1)$ resolved  $\gamma$ -like dynamics

- RAPGAP DIR fails, but is closest to the data in the most DGLAP like region
- RAPGAP DIR+ RES  $\gamma$  Good
- CDM Alright, but problems in res.  $\gamma$  region.
- CASCADE -Goes in the right direction.

## 2+forward jet cross-section, $\frac{d\sigma}{d\Delta n_2}$

Select two hardest jets ( $p_t > 6 \text{ GeV}$ ) JET1 and JET2 in addition to the forward jet ( $p_t > 6 \text{ GeV}$ ) - 2+Forward Jet Event. (No  $\frac{p_t^2}{Q^2}$ -cut.)

 $\eta_e < \eta_{JET1} < \eta_{JET2} < \eta_{FWDJET}$ 



 $\Delta \eta_1 < 1$ : small  $\eta$  separation between the two hard jets - small  $x_g$  - room for many emissions - long ladder favoured

 $\Delta \eta_1 > 1$ : large  $\eta$  separation between the two hard jets - Shorter parton ladder



2+forward jet cross-section NLO 3-jet  $1 + \delta_{had}$  calculations (NLOJET++)

$$\mu_r^2 = \mu_f^2 = \frac{p_{t,JET1}^2 + p_{t,JET2}^2 + p_{t,FWDJET}^2}{3}$$
$$0.25\mu_{r,f}^2 < \mu_{r,f}^2 < 4\mu_{r,f}^2$$

Data within scale uncertainity for  $\Delta \eta_1 > 1$  ("short ladder"-region)



# 2+forward jet cross-section, $\frac{d\sigma}{d\Delta\eta_2}$ QCD Generators

- CDM close to describe the data.
- CASCADE closer to data than RG-DIR
- ME+PS fails, except for at high  $\Delta \eta_2$ where  $\Delta \eta_1 > 1$  (the "non-BFKLish"region), as is the case for the resolved photon model.



 $\Delta \eta_2$ 

# **Conclusions - Forward Jet Measurement**

- Large  $x_{Bj}$ ,  $Q^2$  and  $p_t^2 \to \text{NLO}$  dijet describes forward jet cross section. Small  $x_{Bj}$ ,  $Q^2$  and  $p_t^2 \to \text{NLO}$  dijet fails.
- - DGLAP LO ME+PS (RAPGAP) and NLO di-jet fail for fwd jet cross-sections
  - CDM and LO ME+PS DIR+RESolved  $\gamma$  OK (except 2+fwdjet)
  - CASCADE is in improvement compared to simple DGLAP evolution.
- 2+fwd cross-section -

Models not ordering the transverse momenta still predict a higher cross-section. CDM good.

- Data suggests that more hard radiation (CDM, RES- $\gamma$ , CASCADE) is needed compared to NLO and simple DGLAP evolution.
- Models that break the ordering of transverse momenta give better agreement with data (CDM, RES-γ, CASCADE), while simple DGLAP evolution restricts the phase space too much.