

**Precise Results on g_1^p and g_1^d
and First Measurement of the
Tensor Structure Function b_1^d
with the HERMES-Experiment**

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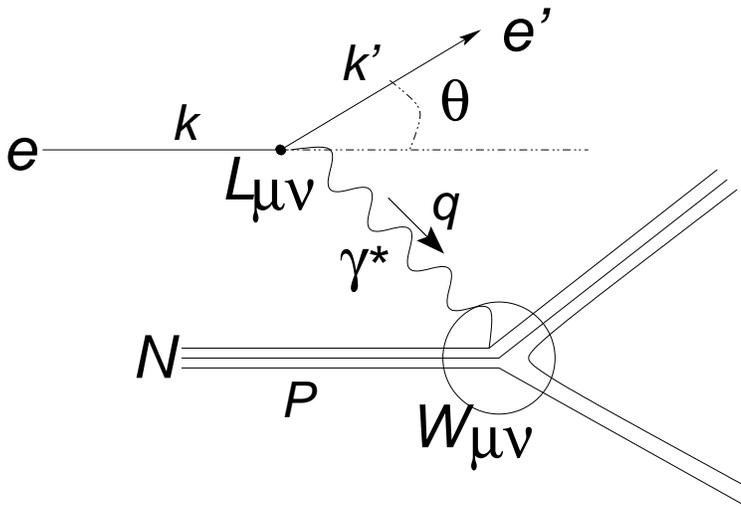
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-Collaboration, DESY - Hamburg

DIS 2005 27 April - 1 May 2005 Madison, USA

Polarized DIS



Kinematics

$$Q^2 = -q^2 \stackrel{\text{Lab.}}{\simeq} 2EE'(1 - \cos \Theta)$$

$$x = \frac{Q^2}{2pq} = \frac{Q^2}{2M\nu}$$

$$\nu = \frac{pq}{M} \stackrel{\text{Lab.}}{\simeq} E - E'$$

$$y = \frac{pq}{pk} \stackrel{\text{Lab.}}{=} \frac{\nu}{E}$$

Cross Section

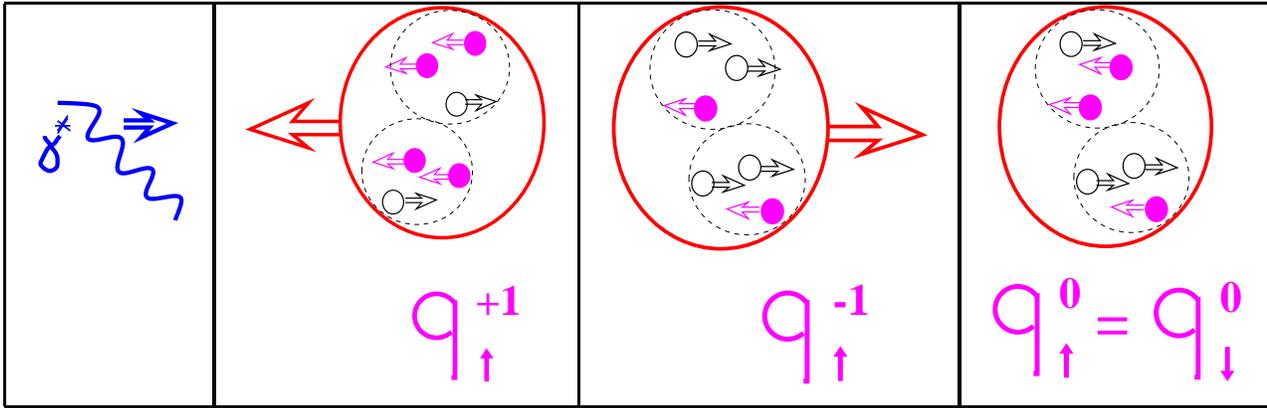
$$\left. \frac{d^2\sigma}{dE' d\Omega} \right|_{\text{Born}} = \frac{\alpha^2}{2MQ^4} \frac{E'}{E} L_{\mu\nu} W^{\mu\nu}$$

Hadronic Tensor

$$W^{\mu\nu} = W_s^{\{\mu\nu\}}(F_1, F_2, \underbrace{b_1, b_2, b_3, b_4}_{\text{target spin 1}}) + W_a^{[\mu\nu]}(g_1, g_2)$$

Structure Functions in the QPM

Quark densities $q(x, Q^2)$:



Structure functions:

Spin-1/2 (proton)	Spin-1 (deuteron)
$F_1 = \frac{1}{2} \sum_q e_q^2 (q_{\uparrow}^{1/2} + q_{\downarrow}^{1/2})$	$F_1 = \frac{1}{3} \sum_q e_q^2 (q_{\uparrow}^1 + q_{\downarrow}^1 + q^0)$
$g_1 = \frac{1}{2} \sum_q e_q^2 (q_{\uparrow}^{1/2} - q_{\downarrow}^{1/2})$	$g_1 = \frac{1}{2} \sum_q e_q^2 (q_{\uparrow}^1 - q_{\downarrow}^1)$
	$b_1 = \frac{1}{2} \sum_q e_q^2 (2q^0 - (q_{\uparrow}^1 + q_{\downarrow}^1))$

Measured Inclusive Asymmetries

- Measured DIS Yield proportional to

$$\sigma = \sigma_{\text{unpol}} \left[1 + P_B P_z A_{\parallel} + \frac{1}{2} P_{zz} A_{zz} \right]$$

- Inclusive **vector asymmetry**

$$A_{\parallel} := \frac{\sigma^{\leftarrow} - \sigma^{\rightarrow}}{\sigma^{\leftarrow} + \sigma^{\rightarrow}} = \frac{1}{P_B P_z} \cdot \frac{\frac{N^{\leftarrow}}{L^{\rightarrow}} - \frac{N^{\rightarrow}}{L^{\rightarrow}}}{\frac{N^{\leftarrow}}{L^{\leftarrow}} + \frac{N^{\rightarrow}}{L^{\rightarrow}}}$$

$$\frac{g_1}{F_1} = \frac{1}{1 + \gamma^2} \cdot \left(\frac{A_{\parallel}}{D} + (\gamma - \eta) A_2 \right)$$

Kinematic variables

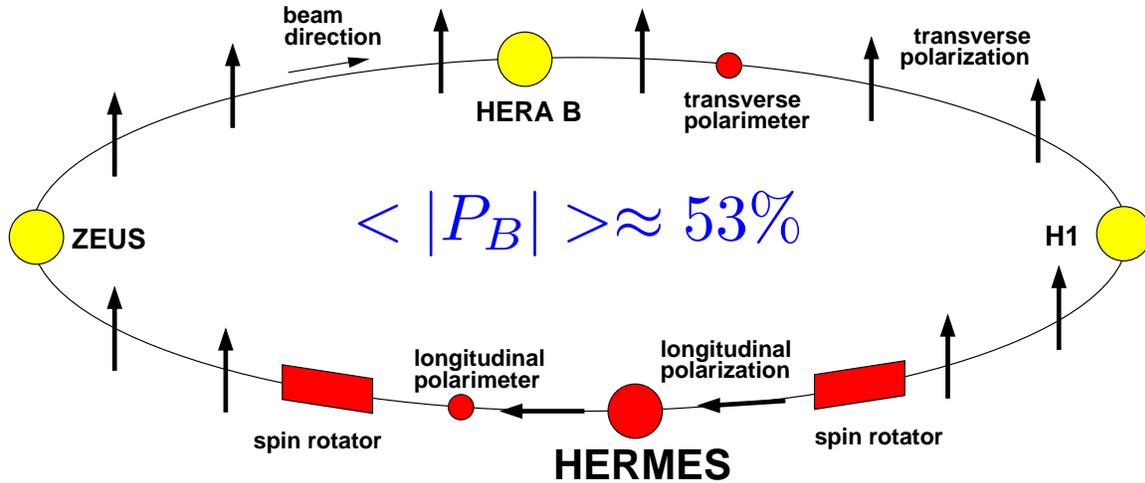
$$\gamma = \frac{\sqrt{Q^2}}{\nu}, \quad \eta = \eta(x, Q^2), \quad D = \frac{P_{\gamma^*}}{P_B}$$

- Inclusive **tensor asymmetry**

$$A_{zz} := \frac{(\sigma^{\leftarrow} + \sigma^{\rightarrow}) - 2\sigma^0}{\sigma^{\leftarrow} + \sigma^{\rightarrow} + \sigma^0} = -\frac{2b_1}{3F_1}$$

The HERMES Experiment

Longitudinally Polarized e-Beam (27.6 GeV)



Longitudinally Polarized Internal H/D Gas Target

Single Hyperfine States
can be Injected!

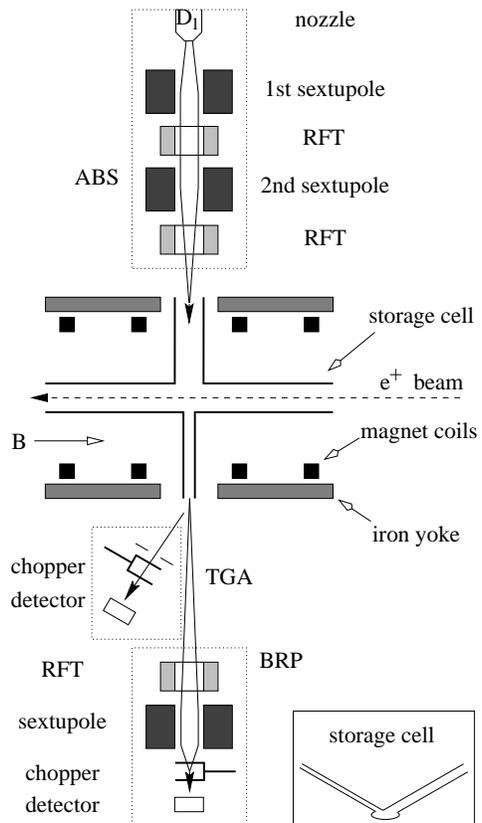
Polarizations:

vector
$$V = \frac{n^+ - n^-}{n^+ + n^- + n^0}$$

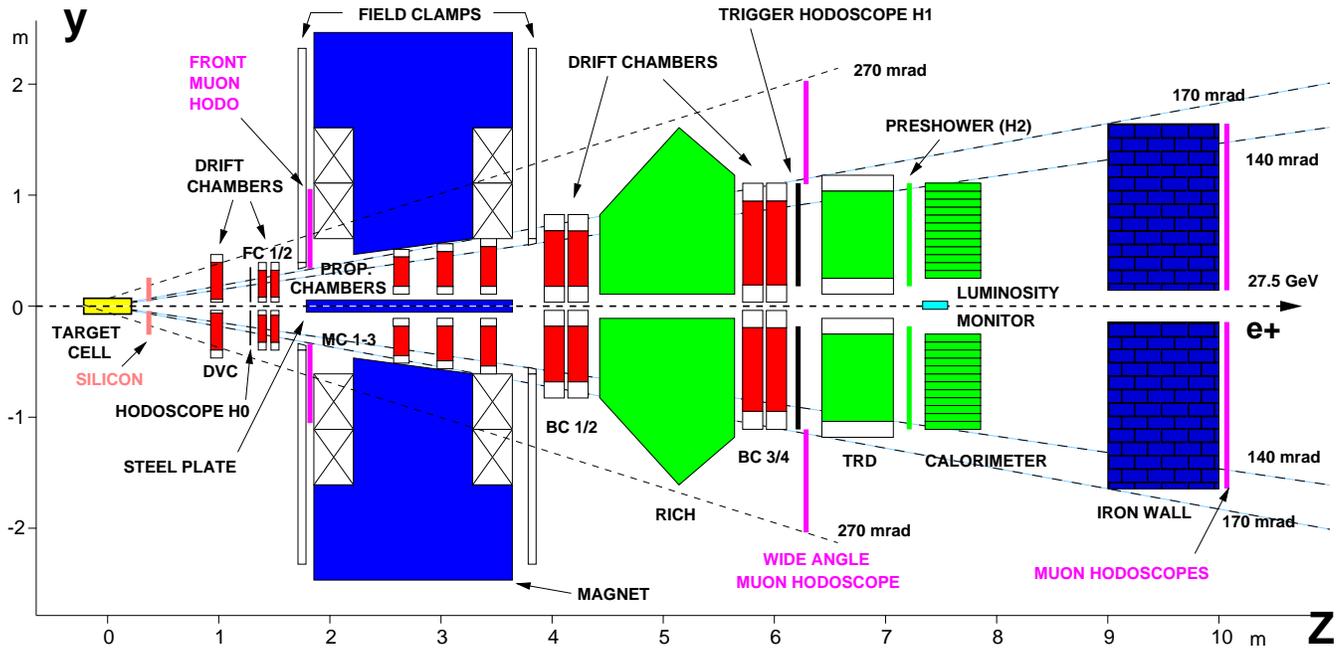
tensor
$$T = \frac{(n^+ + n^-) - 2n^0}{n^+ + n^- + n^0}$$

$\langle |P_z| \rangle \approx 85\%$

$\langle |P_{zz}| \rangle \approx 83\%$ $\langle |P_z| \rangle \approx 0$

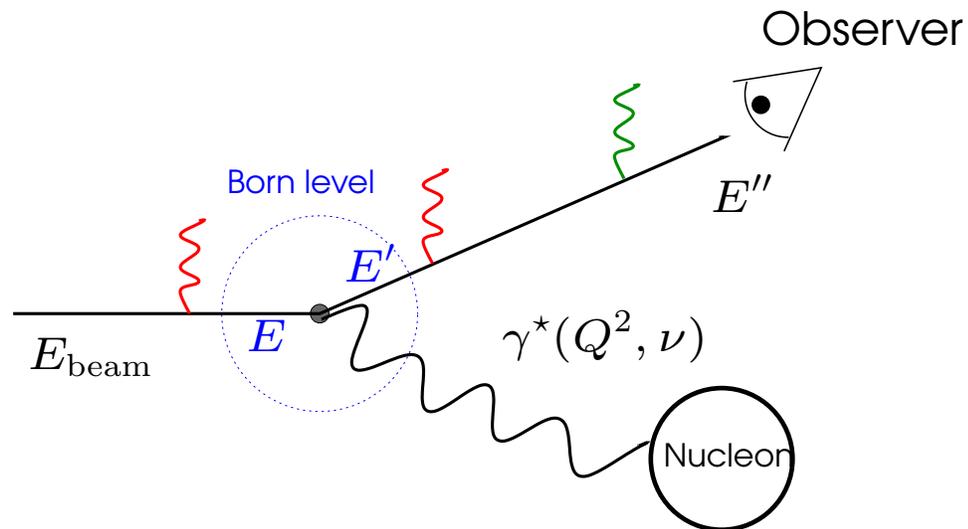


The HERMES Spectrometer



- Acceptance: $40 < \theta < 220$ mrad
- Momentum resolution: $\frac{\delta p}{p} \approx 2\%$
Angular resolution: $0.3 - 0.6$ mrad
- PID: RICH, TRD, preshower, calo
 - Efficiency of electron ID: 98-99 %
 - Hadron contamination: $< 1\%$

Radiative and Smearing Effects



- Background Tail
 - Radiation from (Quasi)-Elastic
- Intra-Bin Events Migration
 - Radiation from DIS
 - Detector Smearing

Unfolding Technique

If only (Quasi)-Elastic Background

$$A_{||}^{\text{Born}} = A_{||}^{\text{Meas}} \frac{n_{\text{unpol}}^{\text{X}}}{n_{\text{unpol}}^{\text{B}}} - \frac{bg_{\text{pol}}^{\text{X}}}{n_{\text{unpol}}^{\text{B}}}$$

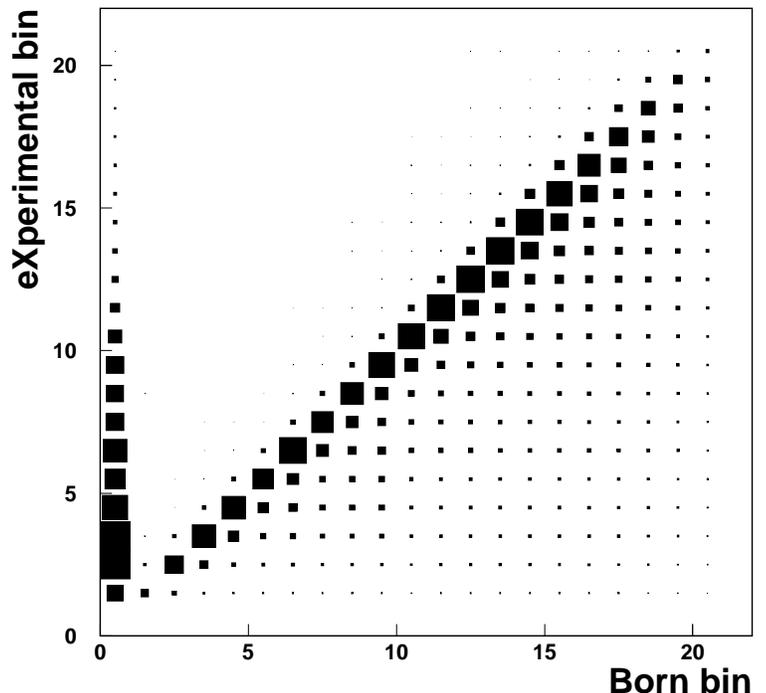
- $n_{\text{unpol}}^{\text{X}}$ Unpol. experimental distribution
- $n_{\text{unpol}}^{\text{B}}$ Unpol. Born distribution
- $bg_{\text{pol}}^{\text{X}}$ Polarized radiative tail

Intra-Bin Migration

- **Smearing Matrix**

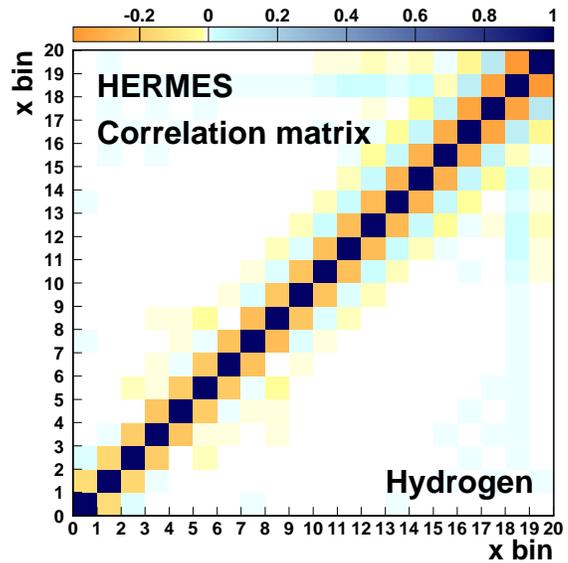
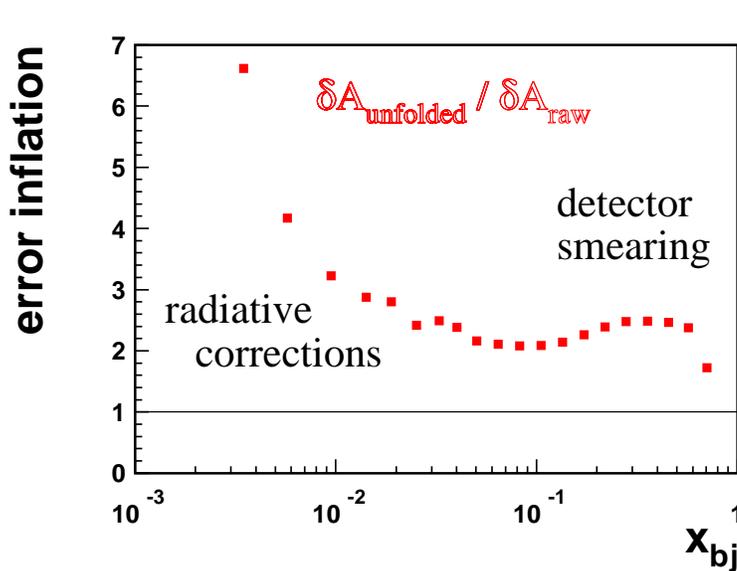
$$S_{ij} = \frac{n(i, j)}{n^{\text{B}}(j)}$$

**Model-Independent
Approach**



Error Inflation

$$\frac{\partial A_{\parallel}^{\text{Born}}(j)}{\partial A_{\parallel}^{\text{Meas}}(i)} = D(i, j) > 1$$



Unfolding

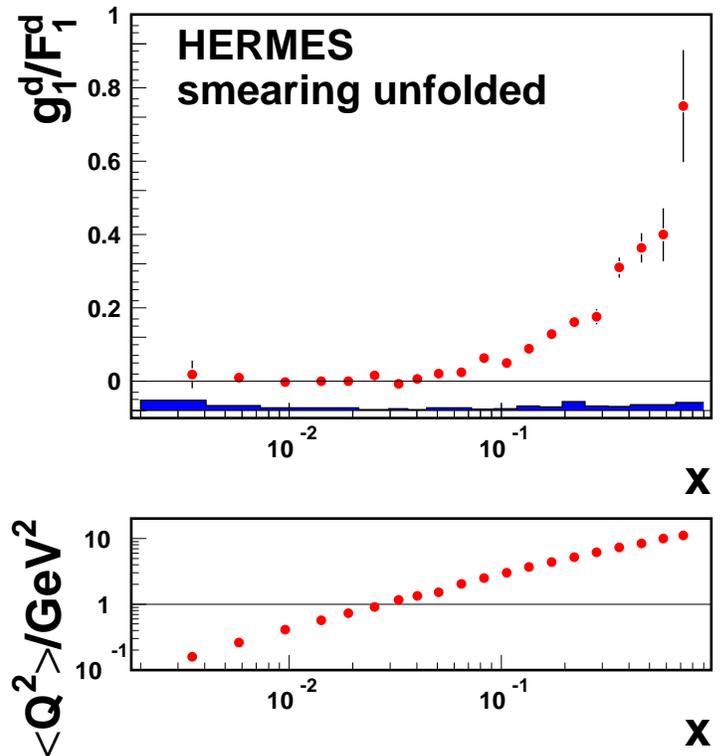
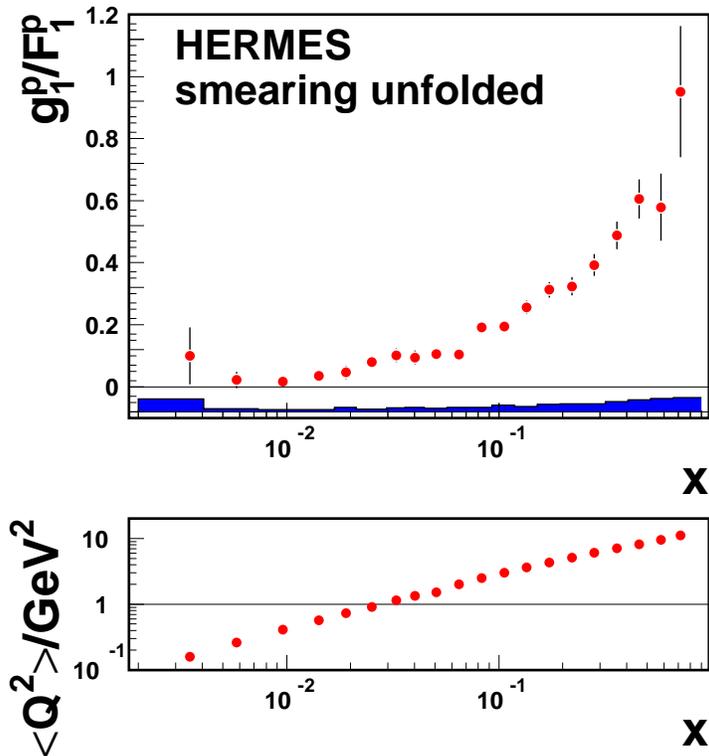
- Removes **Systematic Correlations** between data points
- Introduces **Statistical Correlation**

For correct interpretation and usage of error bars:

⇒ **Correlation Matrix**

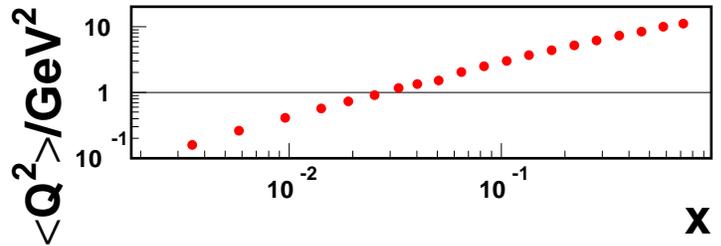
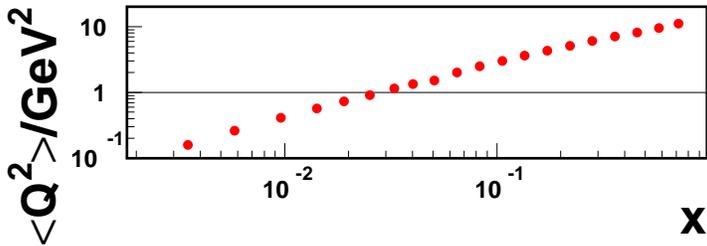
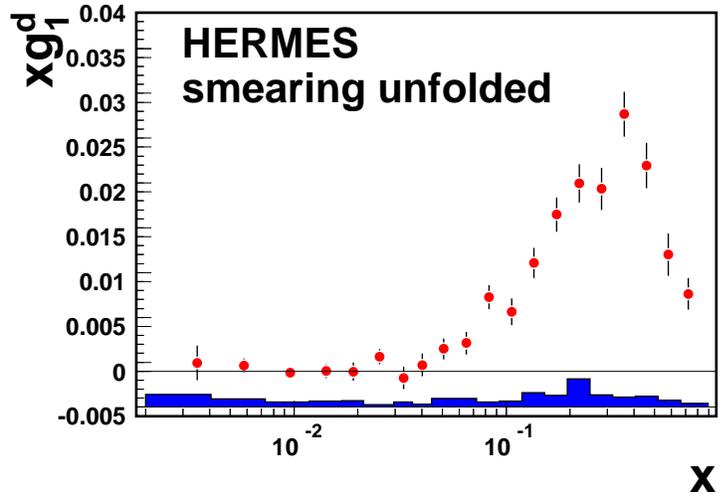
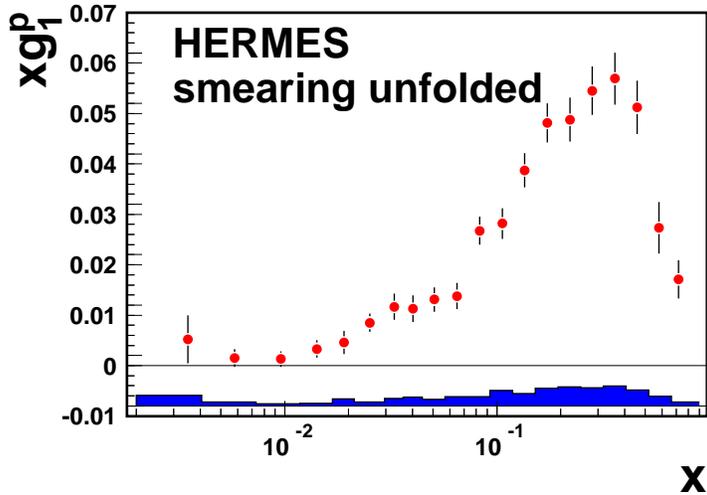


Results: g_1/F_1 of Proton and Deuteron



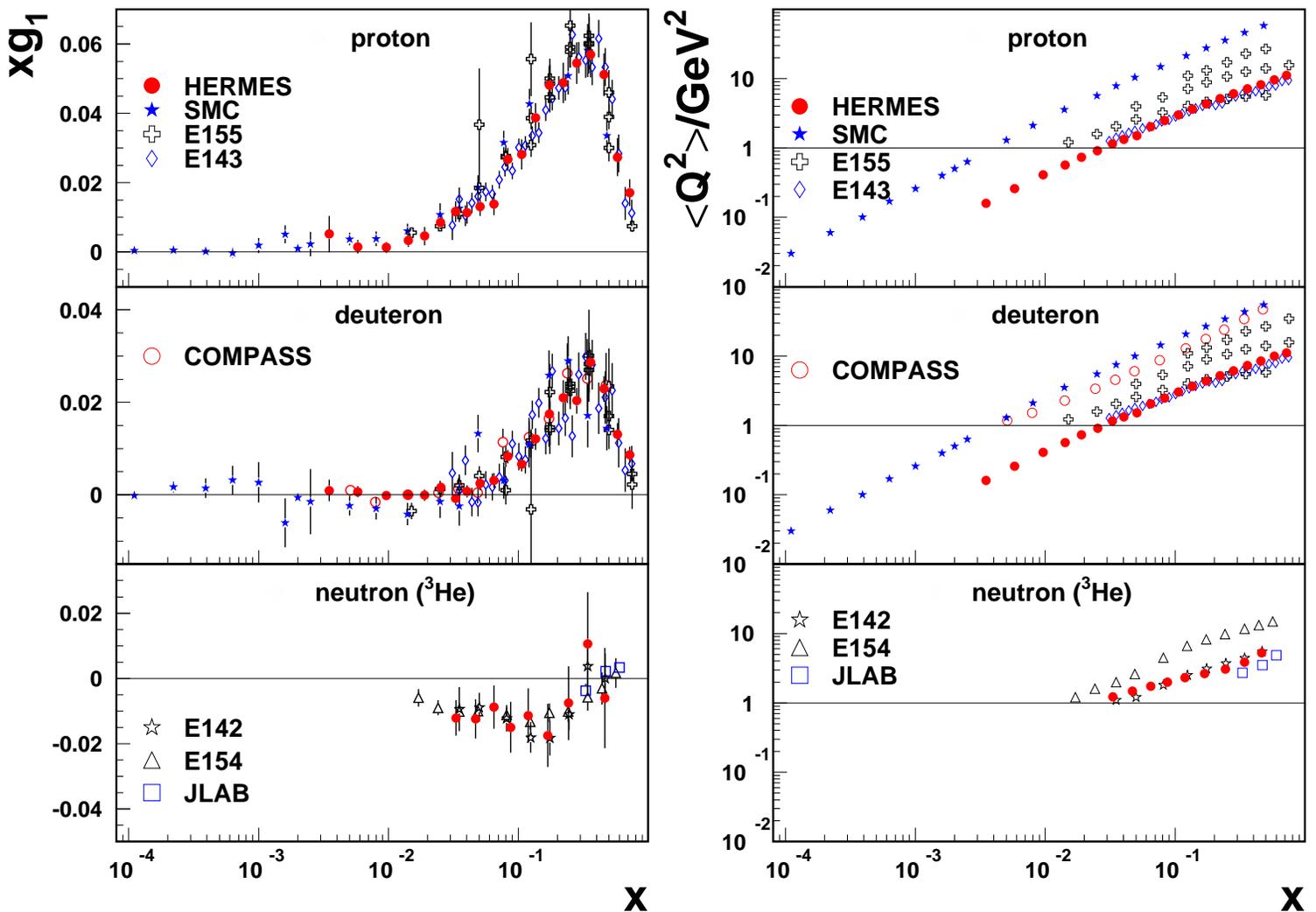
- **Statistical** Error-bars
Diagonal Elements of Covariance Matrix
- **Systematic** Errors
Dominated by Target and Beam Polarization

Results: xg_1 of Proton and Deuteron



- **Statistical** Error-bars
Diagonal Elements of Covariance Matrix
- **Systematic** Errors
Dominated by Target and Beam Polarization

Comparison to World Data



First Moments Calculation

Exp.	$Q^2 (\text{GeV}^2)$	x range	Target	Moment	HERMES Moment
SMC	5	0.03-0.7	p	0.128 ± 0.006	0.1141 ± 0.0026
E143	5	0.03-0.8	p	0.117 ± 0.003	0.1174 ± 0.0027
SMC	5	0.03-0.7	d	0.043 ± 0.007	0.0416 ± 0.0013
E143	5	0.03-0.8	d	0.043 ± 0.003	0.0433 ± 0.0013

Full Statistical Power of the HERMES Data!



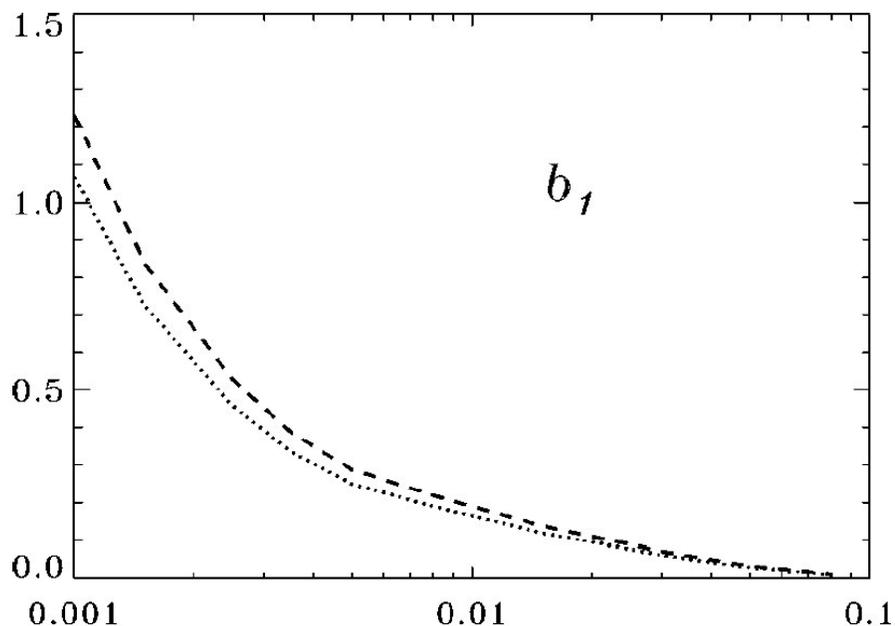
b_1^d Model Calculations

- Deuteron: D-state admixture
 - Elastic Scattering
 - El. Quadrupole Moment $\neq 0$
 - DIS
 - Shadowing Effect
 - \Rightarrow Double Scattering Mechanisms
 - Significant contribution to b_1 at small x

Nikolaeva and Schäfer, *Phys. Lett. B* **398** (1997) 245

Edelmann, Piller and Weise, *Phys. Rev. C* **57** (1998) 3392

Bora and Jaffe, *Phys. Rev. D* **57** (1998) 6906



Results: A_{zz} and b_1^d

- HERMES

First measurement ever

- $A_{zz} \neq 0$

- $A_{zz} = \mathcal{O}(1\%)$

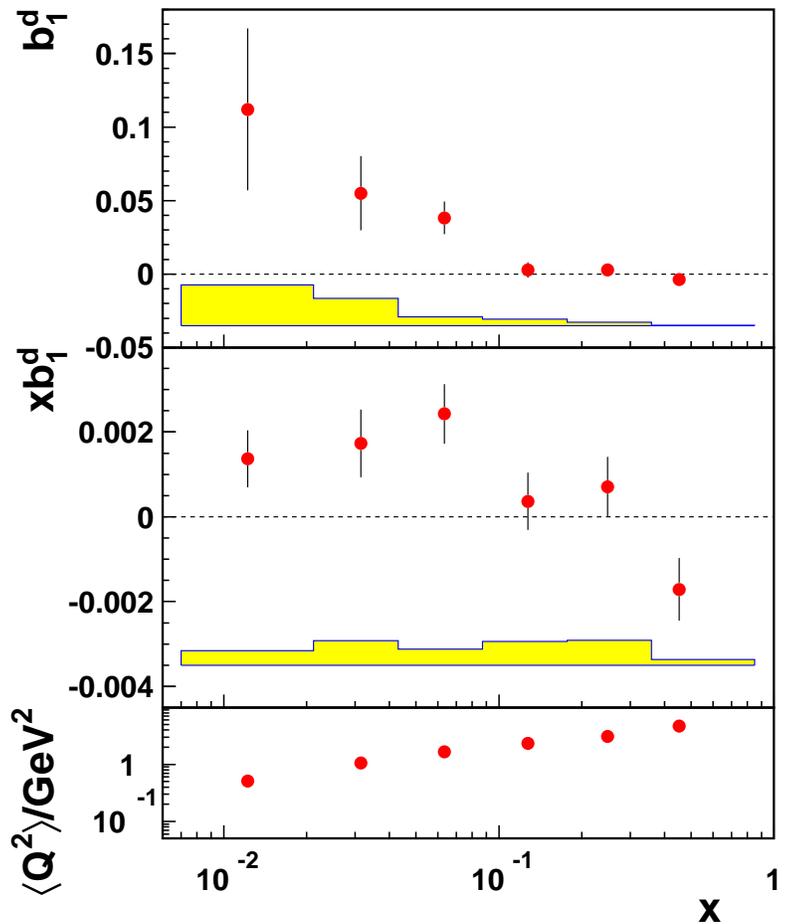
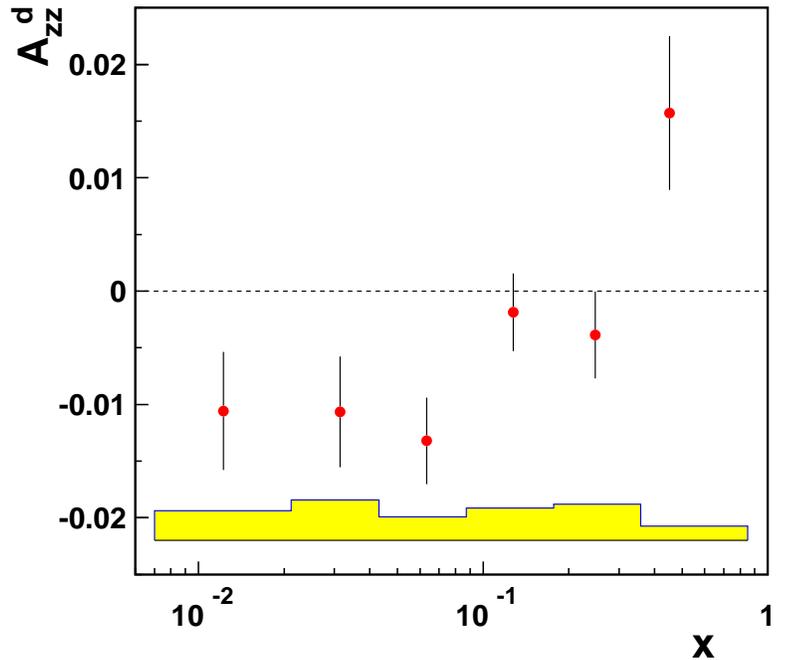
\Rightarrow Small Impact on g_1

- First Moment $\neq 0$:

$$1.05 \pm 0.34_{\text{stat}} \pm 0.35_{\text{sys}}$$

- Qualitative

Agreement with
Double Scattering
Models



Summary and Outlook

- **Final Results** of the g_1 structure function for proton and deuteron from the HERMES data
- Data points of spin structure function now **systematically uncorrelated**, but **statistically correlated**
⇒ **Correlation matrix** for correct calculation of QCD fits and moments
- **First measurement** of tensor structure function b_1^d by HERMES
⇒ b_1^d different from zero at small x
- **To come:** HERMES publications on spin and tensor structure functions