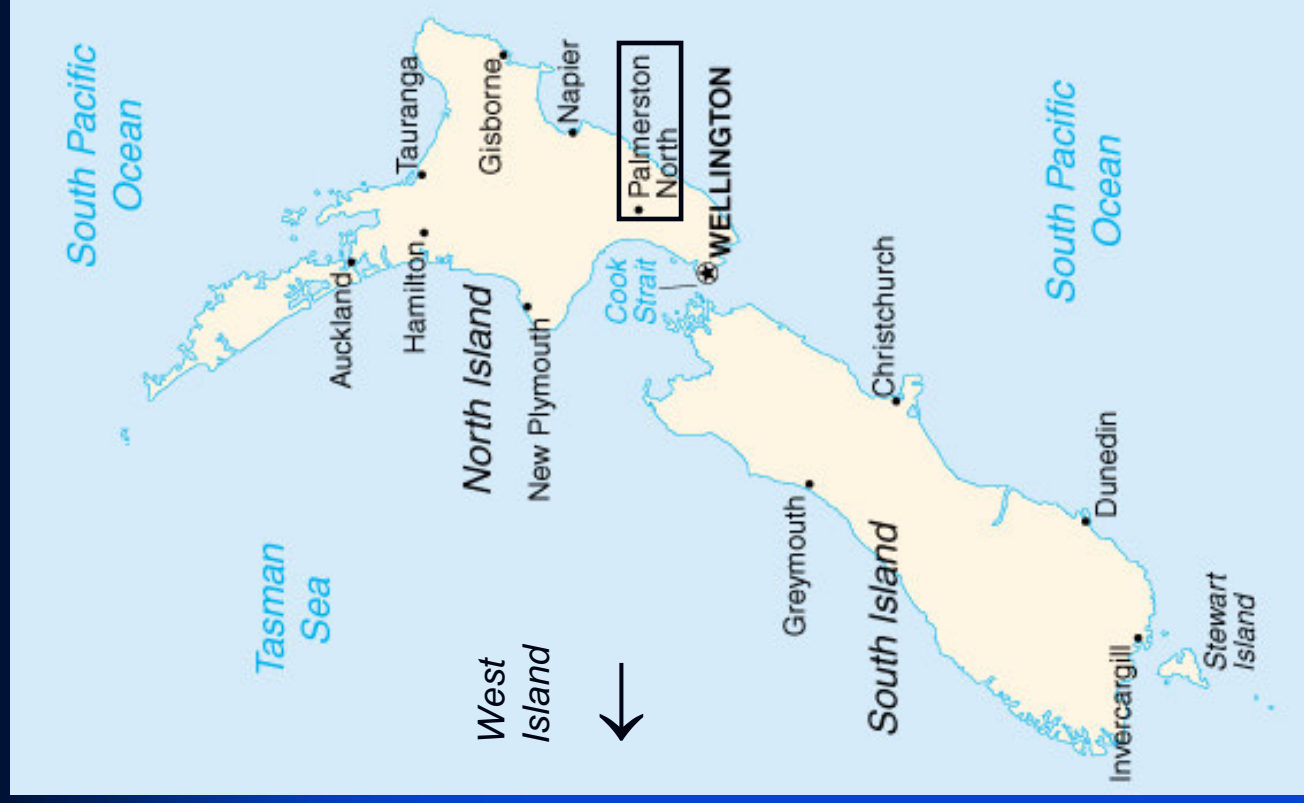


# $g_1(x)$ and $g_2(x)$ in the Meson Cloud Model

Tony Signal  
*Institute of Fundamental Sciences*  
*Massey University*  
*New Zealand*



# Overview

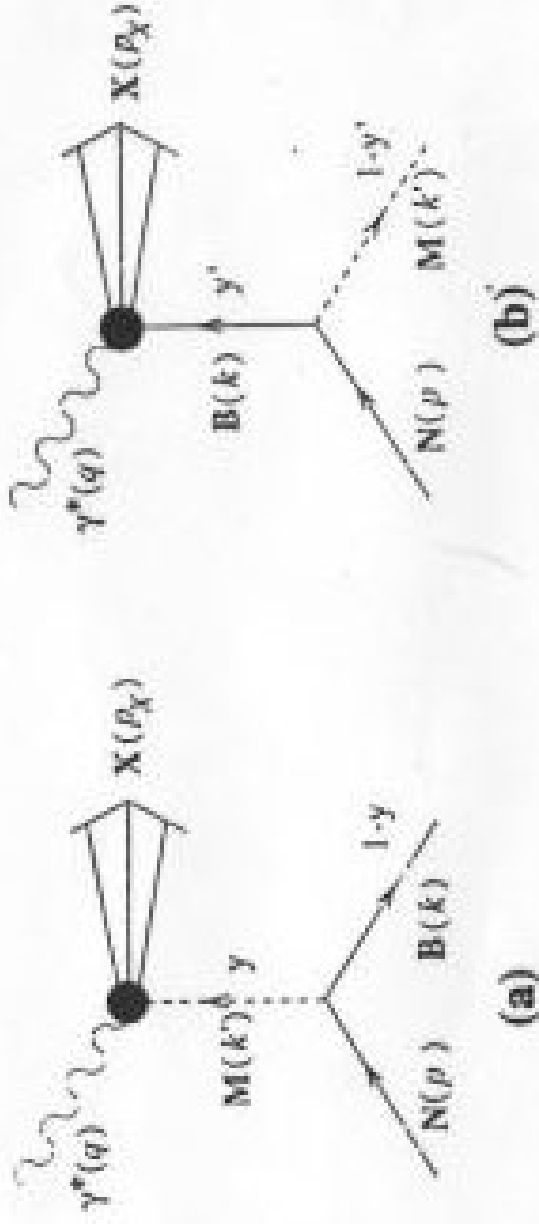
- Meson Cloud model
- Meson cloud contributions to spin structure functions
- Conclusion

# Meson Cloud Model

- Crucial observation (Sullivan 72) -
  - Pion cloud contribution to DIS scales
  - Implies quark dists of proton modified
  - Convolution

$$\delta q^p(x) = \int_x^1 \frac{dy}{y} f_{p\pi}(y) q^\pi\left(\frac{x}{y}\right)$$

# Meson Cloud Model



DIS from the virtual (a) meson, and (b) baryon components of a physical nucleon.

# Meson Cloud Model

- Fock expansion of proton wavefn.

$$|p\rangle_{\text{phys}} = \sqrt{Z}|p\rangle_{\text{bare}} + \sum_{BM} \int dy dk_{\perp}^2 \phi_{BM}(y, k_{\perp}^2) |B; M\rangle$$

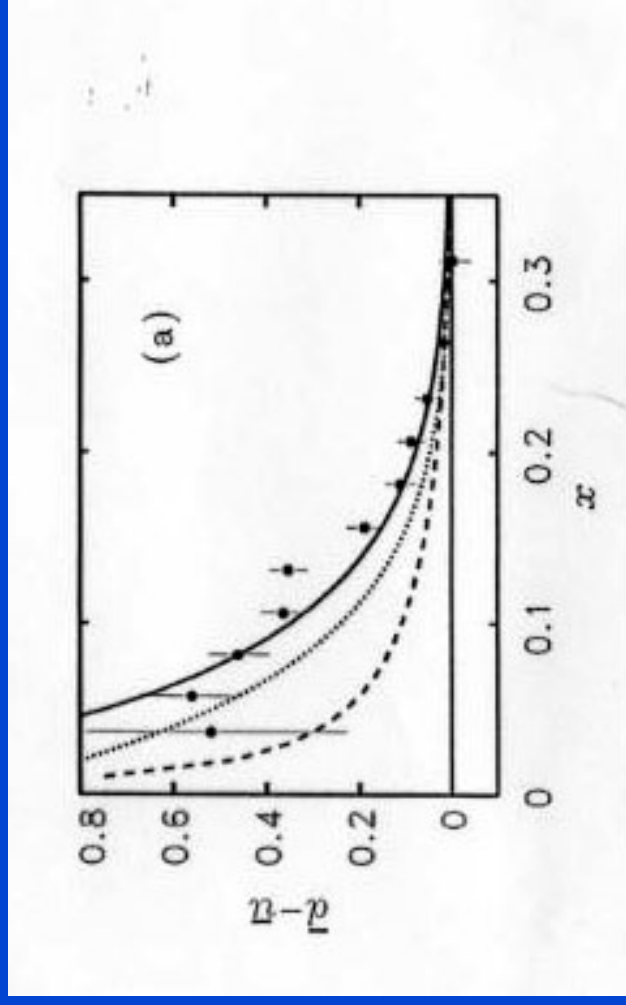
- Bare states are SU(6) symmetric
- $p \rightarrow BM$  vertices described by  $L_{int}$  plus form factor
- FF constrained by elastic cross-sec
- Quick convergence  $\Leftrightarrow$  Small prob. of high mass states
- Model incorporates structure + interactions
- Can investigate high-energy  $\leftrightarrow$  low-energy pictures, symmetry breaking etc.

# Gottfried Sum Rule

- Isospin broken in sea

$$\begin{aligned} p &\rightarrow n(ud\bar{d}) + \pi^+(u\bar{d}) \\ p &\rightarrow \Delta^{++}(uuu) + \pi^-(d\bar{u}) \end{aligned}$$

- MCM gives good fit to  $F_2(x) - F_2(x)$

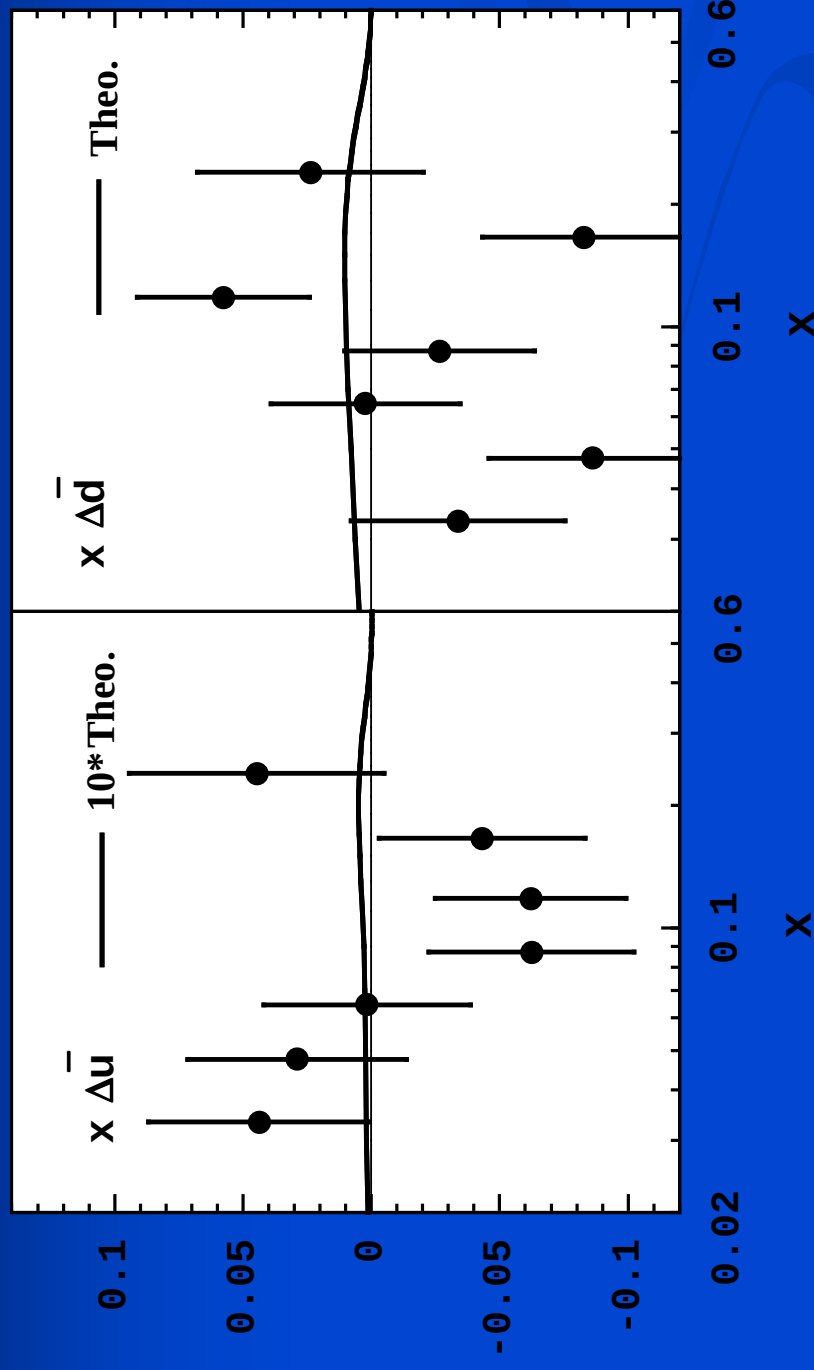


# Spin dependent Quark Dists.

- Extend MCM to include vector mesons
  - $\pi$  cloud dilutes proton spin
  - $\rho$ ,  $\omega$ ,  $K^*$  able to carry spin
- Include interference terms
- Get reasonably good agreement with HERMES semi-inclusive data for sea distributions



# Spin Dependent Sea Dists.



- Data from Hermes
- Small symmetry breaking

# Spin Dependent Structure Functions

- Dominated by valence distributions
  - $N \rightarrow N\pi$ ,  $N \rightarrow \Delta\pi$  most important fluctuations
$$\mathcal{L}_{int} = ig_{NN\pi}\bar{\psi}\gamma_5\pi\psi, \quad f_{N\Delta\pi}\bar{\psi}\pi\partial_\mu\chi^\mu + \text{h.c.}$$
- At finite  $Q^2$  spin of cloud hadrons are not parallel with initial nucleon spin
- Both longitudinal and transverse spin components of cloud contribute to observed structure functions

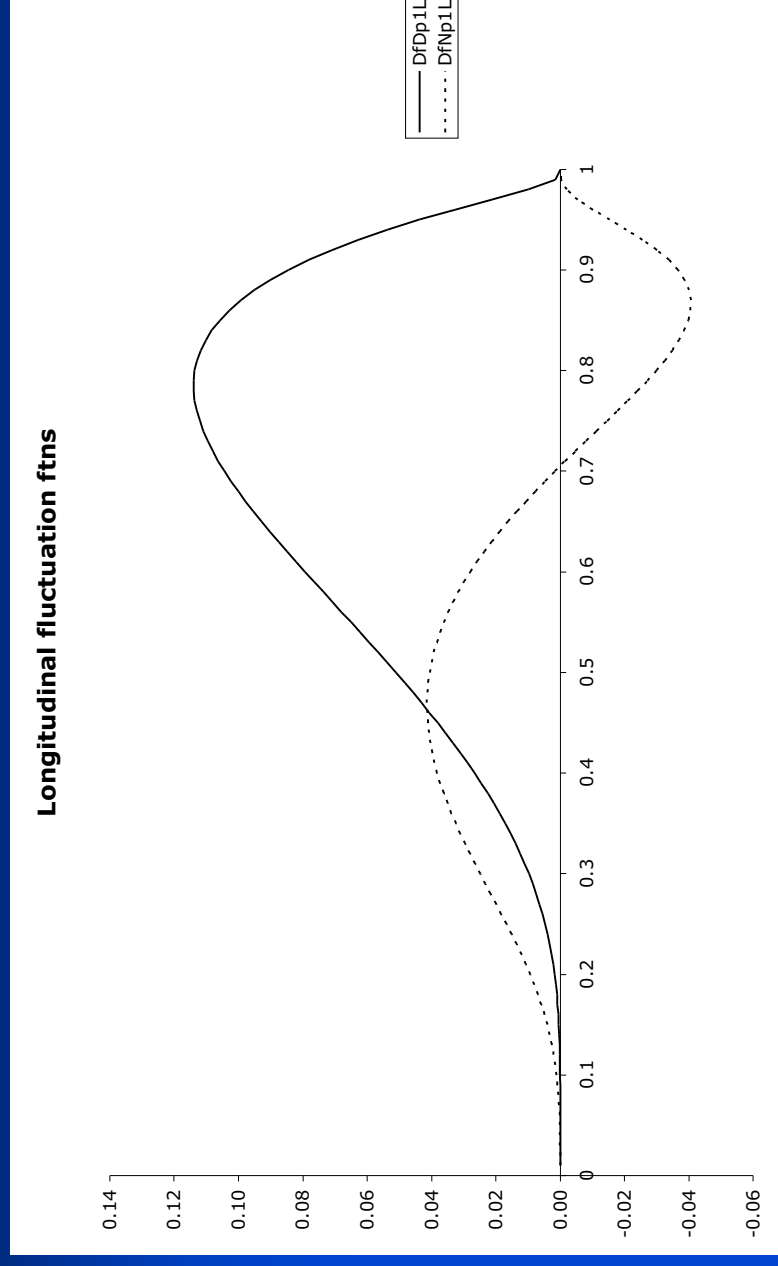
# Spin Dependent Structure Functions

$$\delta g_1(x, Q^2) = \frac{1}{1+\gamma^2} \int_x^1 \frac{dy}{y} \left( [\Delta f_{1L}(y) + \Delta f_{1T}(y)] g_1^B\left(\frac{x}{y}, Q^2\right) + [\Delta f_{2L}(y) + \Delta f_{2T}(y)] g_2^B\left(\frac{x}{y}, Q^2\right) \right)$$

$$\delta g_2(x, Q^2) = -\frac{1}{1+\gamma^2} \int_x^1 \frac{dy}{y} \left( [\Delta f_{1L}(y) - \Delta f_{1T}(y)] / \gamma^2 g_1^B\left(\frac{x}{y}, Q^2\right) - [\Delta f_{2L}(y) - \Delta f_{2T}(y)] / \gamma^2 g_2^B\left(\frac{x}{y}, Q^2\right) \right)$$

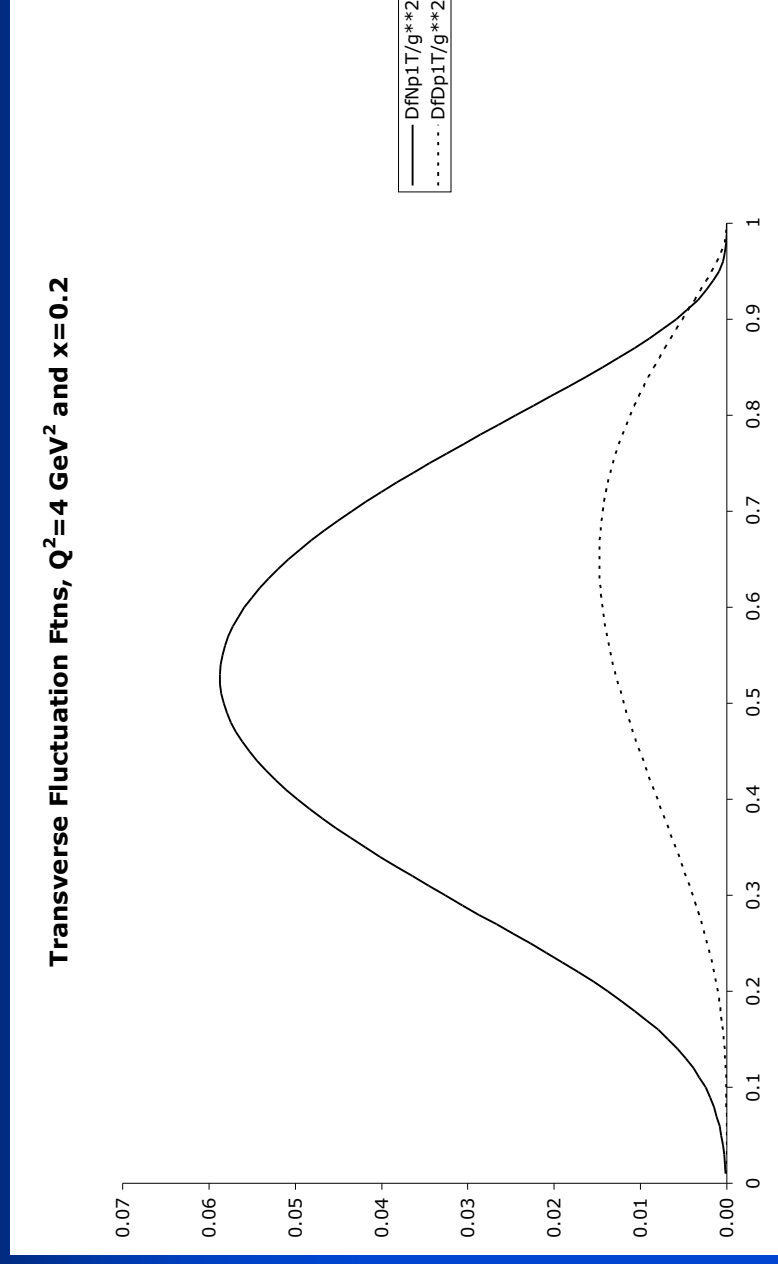
$$\gamma^2 = \frac{4x^2 m_N^2}{Q^2}$$

# Spin Dependent Fluctuations



- Long. Fluctuations require both  $N$  and  $\Delta$ 
  - $s = 3/2$  state important

# Spin Dependent Fluctuations



- N is more important for transverse fluct.
- n.b  $\gamma \approx 0.19$

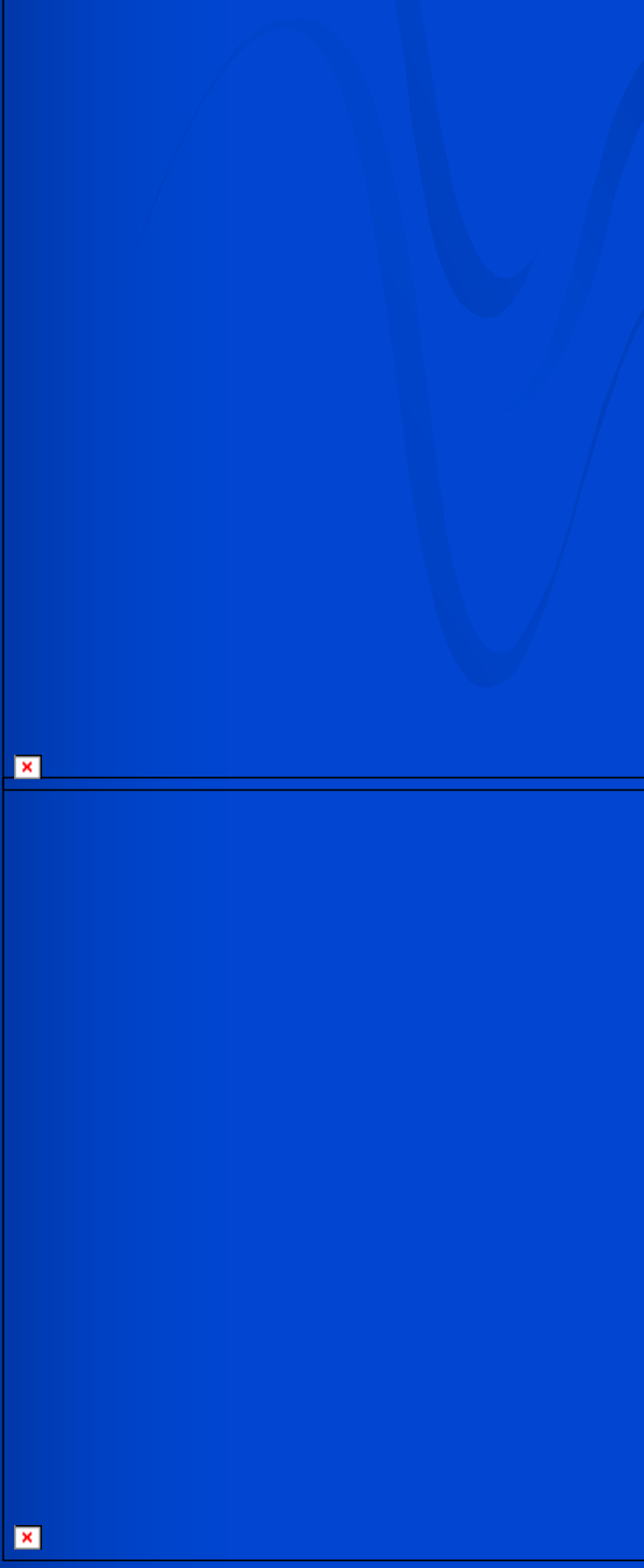
# ‘Bare’ Hadron SFs

- Use bag model for N,  $\Delta$  parton dists
  - Add  $\Delta g(x)$  ‘by hand’
  - Hyperfine splitting between N and  $\Delta$
  - Use NLO evolution
  - Unpol. dists agree with DIS data
- $g_2(x)$  from Wandzura-Wilczek

$$g_2^{WW}(x) = -g_1(x) + \int_x^1 \frac{dy}{y} g_1(y)$$

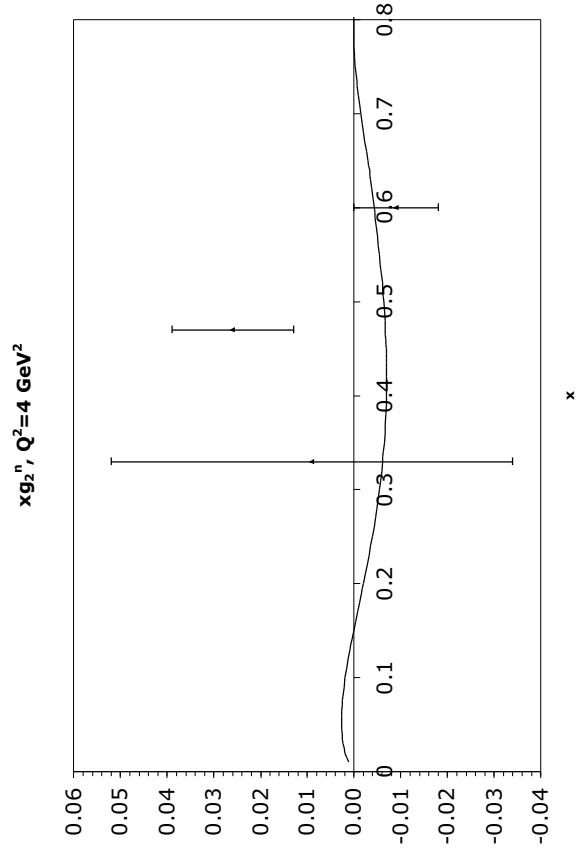
- No higher twist component

# ‘Bare’ Hadron $g_1(x)$



- Data from Hermes

# 'Bare' Hadron $g_2(x)$



- Data from E155, Jlab E-99-117



# MCM Contributions to $g_1^p$



# MCM Contributions to $g_1^n$



# MCM Contributions to $g_2^p$



# MCM Contributions to $g_2^n$



# Summary

- Longitudinal ( $g_1$ ) structure ftns of cloud hadrons affect observed transverse ( $g_2$ ) structure ftns
- MCM contributions to  $g_1$  and  $g_2$  of proton are small
- MCM contributions to  $g_1$ ,  $g_2$  of neutron are 10%
  - Similar size to higher twist in  $g_2^n$
  - Theorists have to be careful!

# Thanks

- Fu-Guang Cao (Massey)
- François Bissey (Massey)