

MSSM light Higgs boson scenario and its test at hadron colliders

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Summary

- + The MSSM scenario with the CP-even Higgs boson as light as 60 GeV and above is not excluded by LEP2**
- + The MSSM parameter space corresponding to this Light higgs (Lh) scenario is generic and not fine-tuned**
- + The entire parameter space corresponding Lh scenario can be entirely covered by LHC**

Problems of the Standard Model

- Problem of large quantum corrections to the Higgs mass in SM (Hierarchy problem)

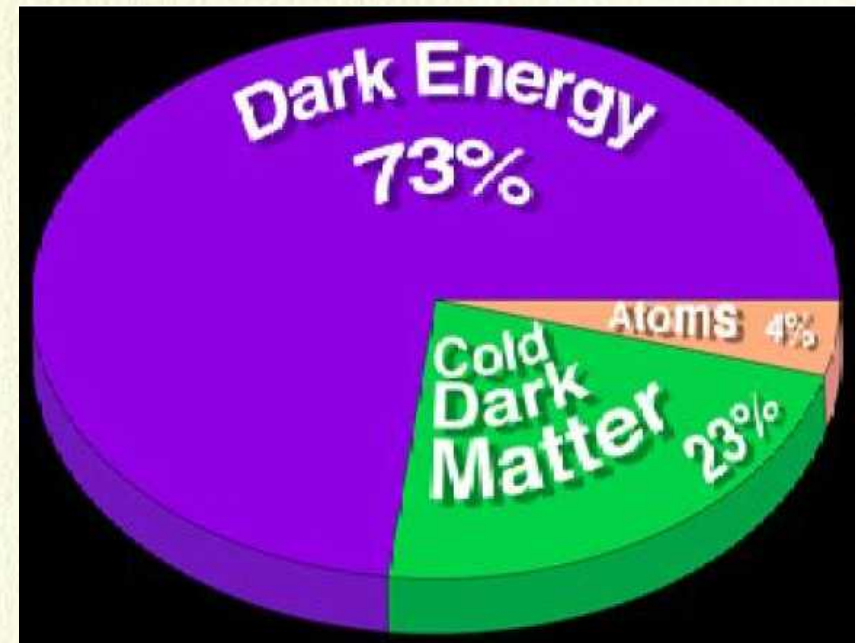
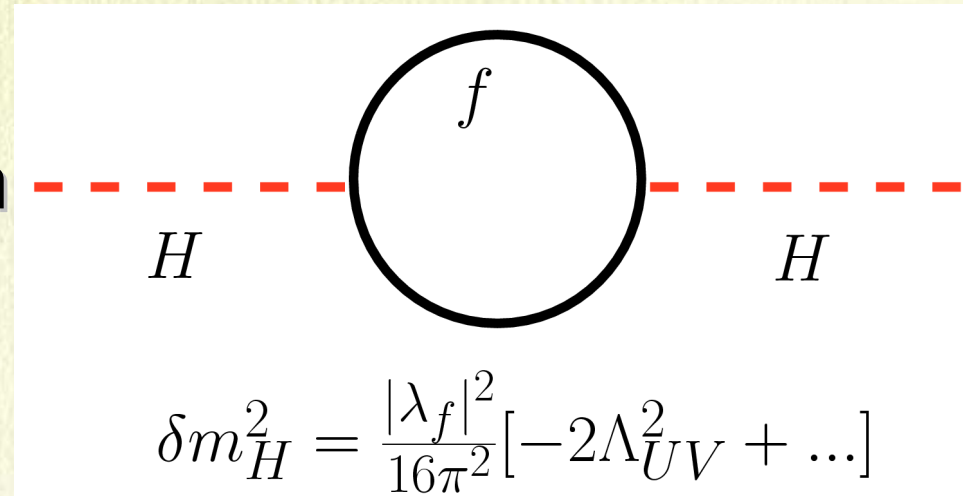
- Coupling Unification

- The origin of Electroweak Symmetry breaking.

Higgs boson is not found yet ...

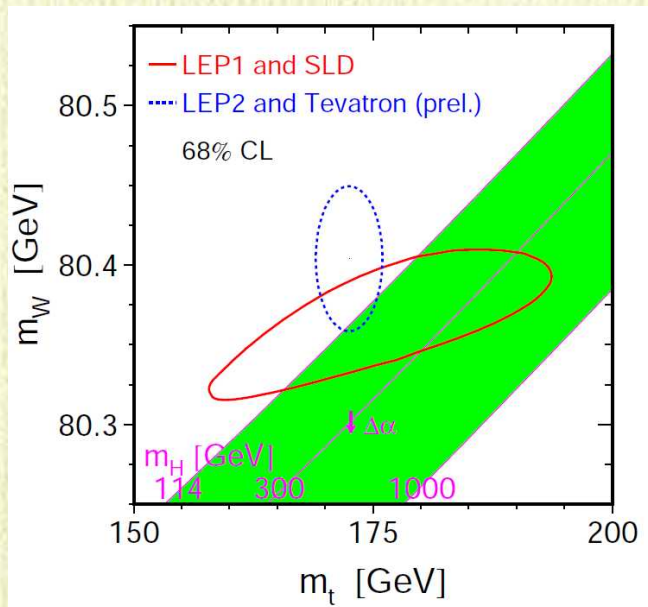
- The origin and Nature of Dark Matter and Dark Energy
No explanation within SM ...

- Baryogenesis problem



Constraints from Electroweak Data

LEP1+SLD+nN data are consistent with LEP2+Tevatron data and with SM, if Higgs mass is low



χ^2 versus M_H for SM Fit

$M_H = 89^{+42}_{-30}$

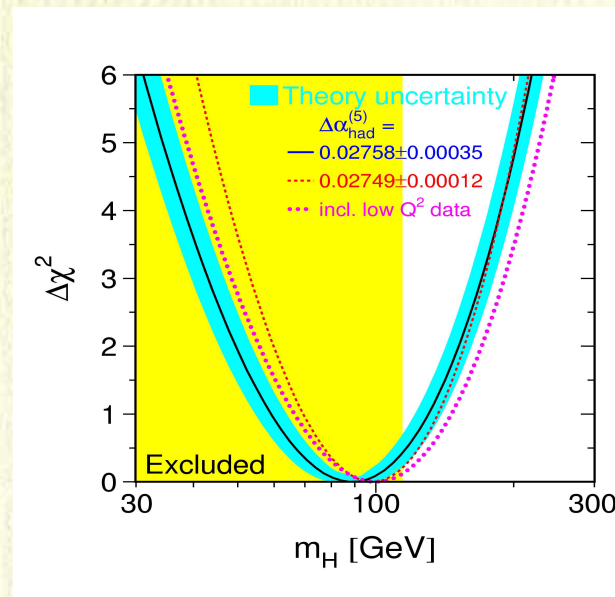
@68%CL

$M_H < 175$ GeV

@95%CL

for $m_{top} = 172.5$ GeV

by March 2006

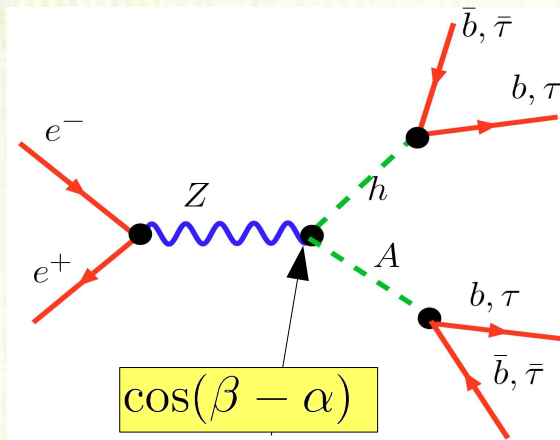
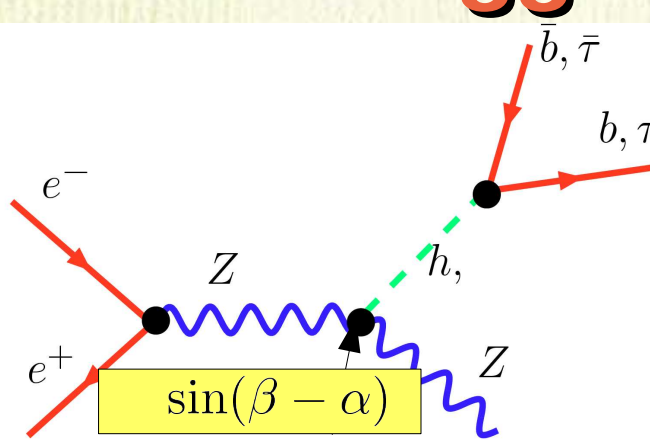


Current status of direct Higgs search

$M_h > 114.4$ GeV

$M_h > 114.4$ GeV

There are more processes in SUSY



MSSM HIGGS sector

- ✦ To provide masses to both up-type and down-type quarks, and to ensure anomaly cancellation, the MSSM has two Higgs complex-doublet superfields

$$\Phi_d = (\Phi_d^0, \Phi_d^-) \text{ and } \Phi_u = (\Phi_u^+, \Phi_u^0) \quad \langle \Phi_d \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} v_d \\ 0 \end{pmatrix}, \quad \langle \Phi_u \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_u \end{pmatrix},$$

where $\sqrt{v_d^2 + v_u^2} = 2M_W/g = 246 \text{ GeV}$

- ✦ Out of 8 DOF, 3 serve as GB, absorbed into longitudinal components of the W and Z, 5 DOF remains:

$$h = -(\sqrt{2}\text{Re } \Phi_d^0 - v_d) \sin \alpha + (\sqrt{2}\text{Re } \Phi_u^0 - v_u) \cos \alpha$$

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$$A = \sqrt{2}(\text{Im } \Phi_d^0 \sin \beta + \text{Im } \Phi_u^0 \cos \beta), \quad H^\pm = \Phi_d^\pm \sin \beta + \Phi_u^\pm \cos \beta$$

α is (h, H) mixing angle

$\tan \beta = v_u/v_d$ and M_A is the conventional choice to define the Higgs sector:

$$M_{H^\pm} = \sqrt{M_A^2 + M_W^2}$$

$$M_{h,H}^2 = \frac{1}{2} \left[(M_A^2 + M_Z^2) \mp \sqrt{(M_A^2 + M_Z^2)^2 - 4M_A^2 M_Z^2 \cos^2 2\beta} \right], \quad M_h < M_Z$$

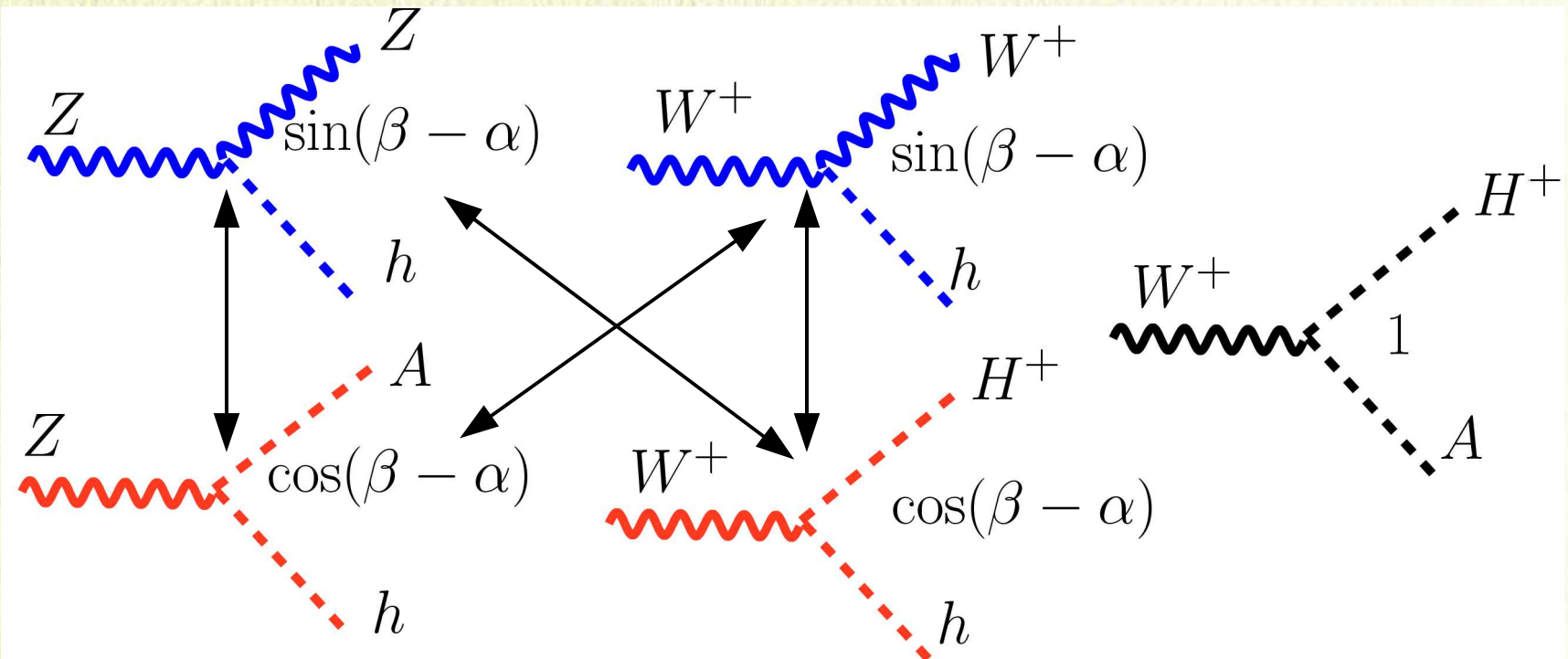
Higgs Interactions with vector bosons

$$\mathcal{L}_{H_i V V} = g M_W \left(W_\mu^+ W^{-\mu} + \frac{1}{2c_W^2} Z_\mu Z^\mu \right) g_{H_i V V} H_i$$

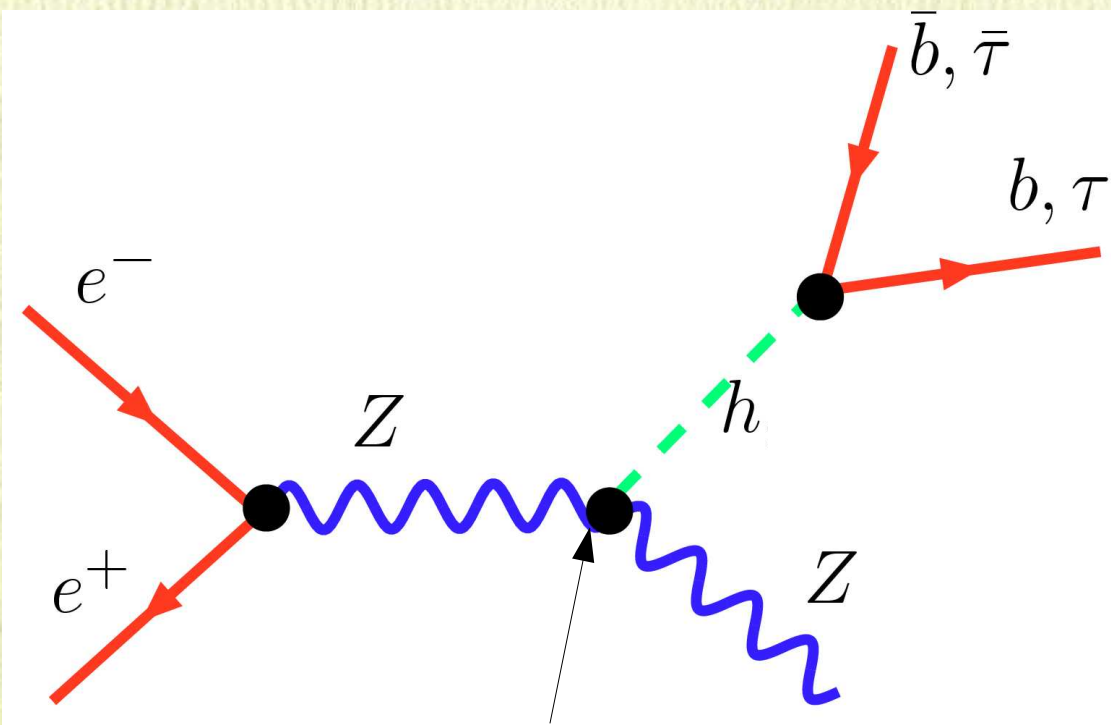
$$\mathcal{L}_{A H_i Z} = \frac{g}{4c_W} g_{A H_i Z} Z^\mu (H_i i \overleftrightarrow{\partial}_\mu A), \quad H_i = (h, H)$$

$$\mathcal{L}_{\mathcal{H} H^\pm W^\mp} = -\frac{g}{2} g_{\mathcal{H} H^\pm W^\mp} W^{-\mu} (\mathcal{H} i \overleftrightarrow{\partial}_\mu H^\pm) + \text{h.c.}, \quad \mathcal{H} = (h, H, A)$$

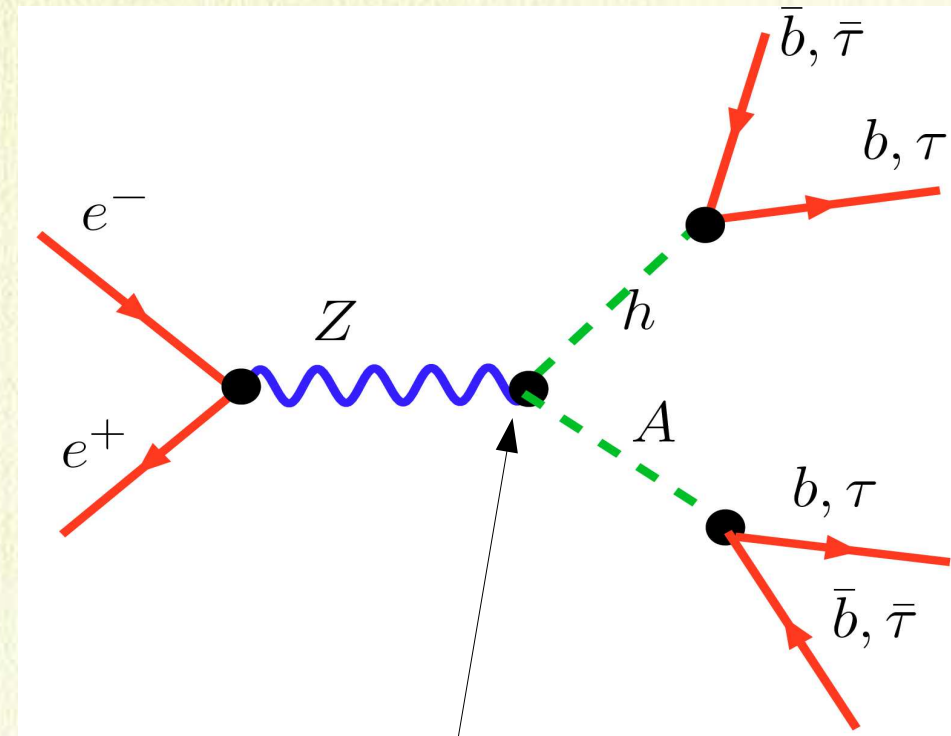
Sum rules



Will no-lose 'theorem' work?



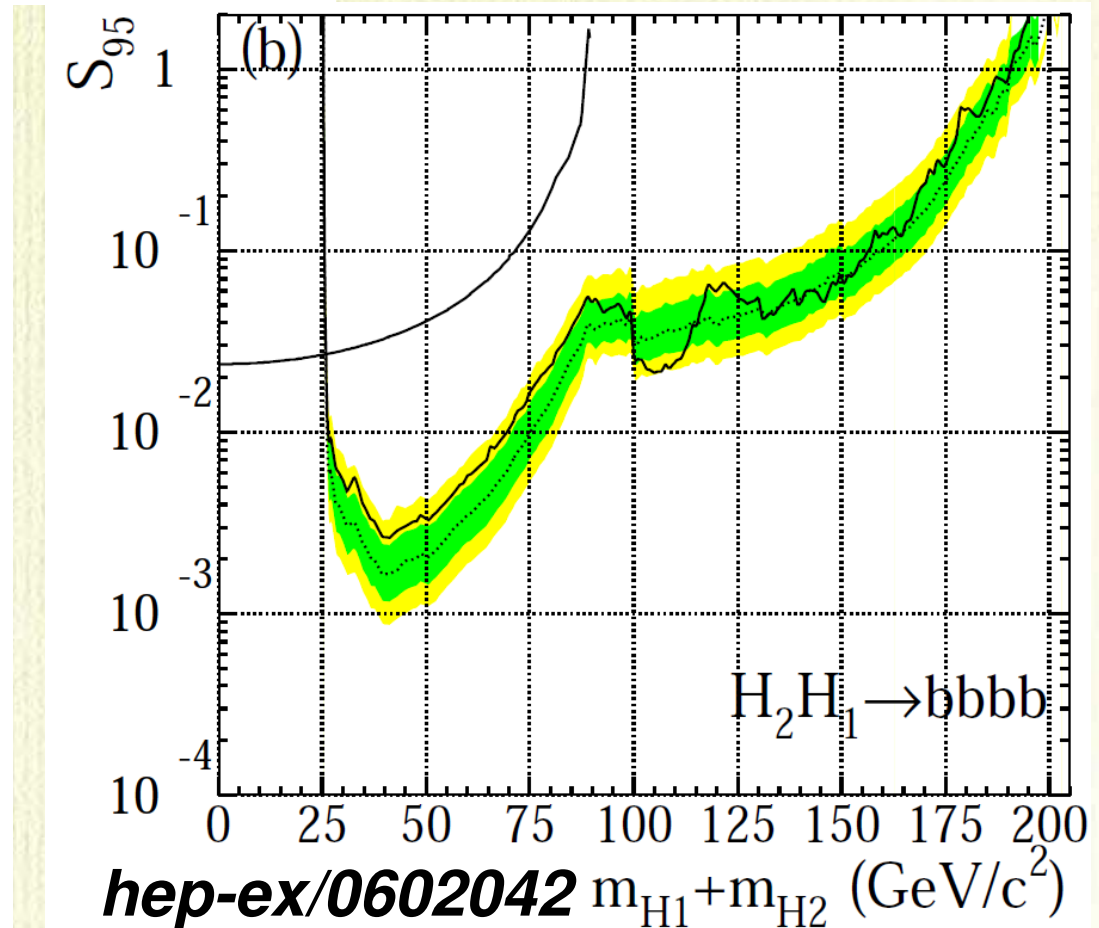
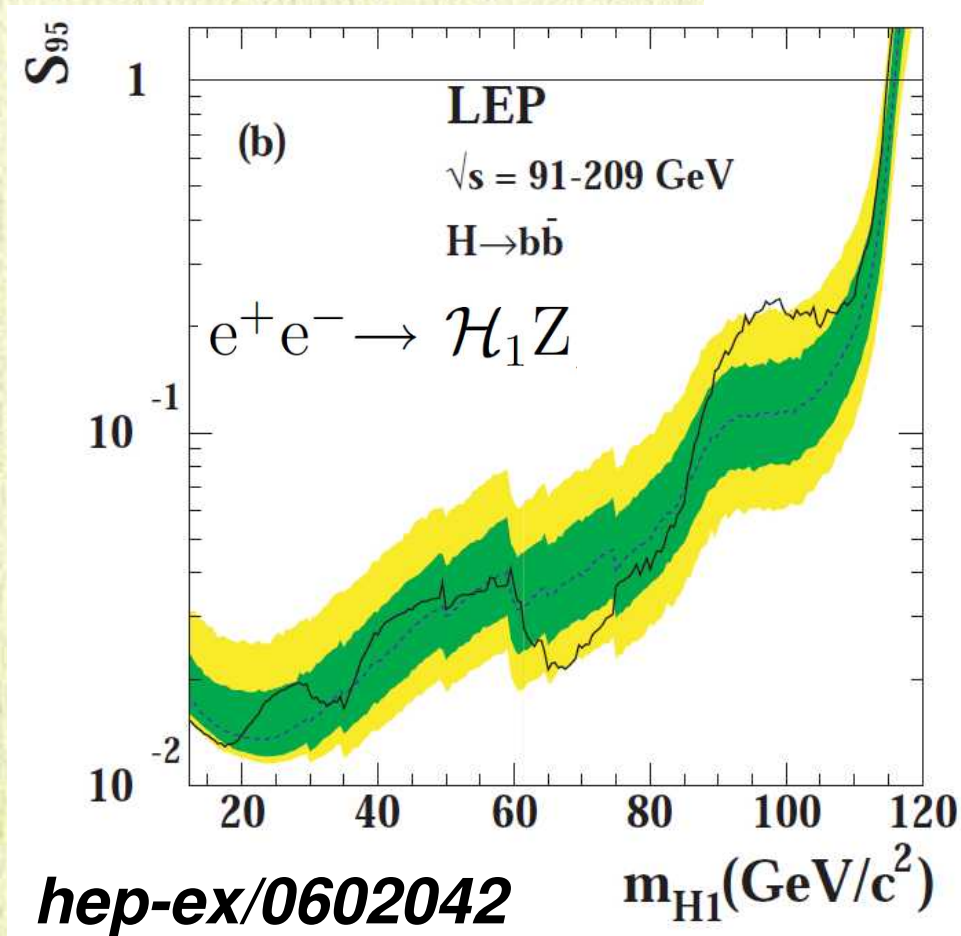
$$\sin(\beta - \alpha)$$



$$\cos(\beta - \alpha)$$

What do we know about MSSM Higgs boson?

$$S_{95} = \sigma_{\max} / \sigma_{\text{ref}}$$



Similar limits are for $H \rightarrow \tau\tau$ channel,

but $Br(H \rightarrow \tau\tau)$ is one order of magnitude smaller than $Br(H \rightarrow b\bar{b})$

Higgs mixing and radiative corrections

tree-level mixing matrix \mathcal{M}^2

$$\begin{pmatrix} M_A^2 s_\beta^2 + M_Z^2 c_\beta^2 & -(M_A^2 + M_Z^2) s_\beta c_\beta \\ -(M_A^2 + M_Z^2) s_\beta c_\beta & M_A^2 c_\beta^2 + M_Z^2 s_\beta^2 \end{pmatrix}$$

diagonalized by Higgs mixing angle

$$\begin{pmatrix} h \\ H \end{pmatrix} = \begin{pmatrix} -s_\alpha & -c_\alpha \\ c_\alpha & s_\alpha \end{pmatrix} \begin{pmatrix} Reh_d^0 \\ Reh_u^0 \end{pmatrix}$$

convention:

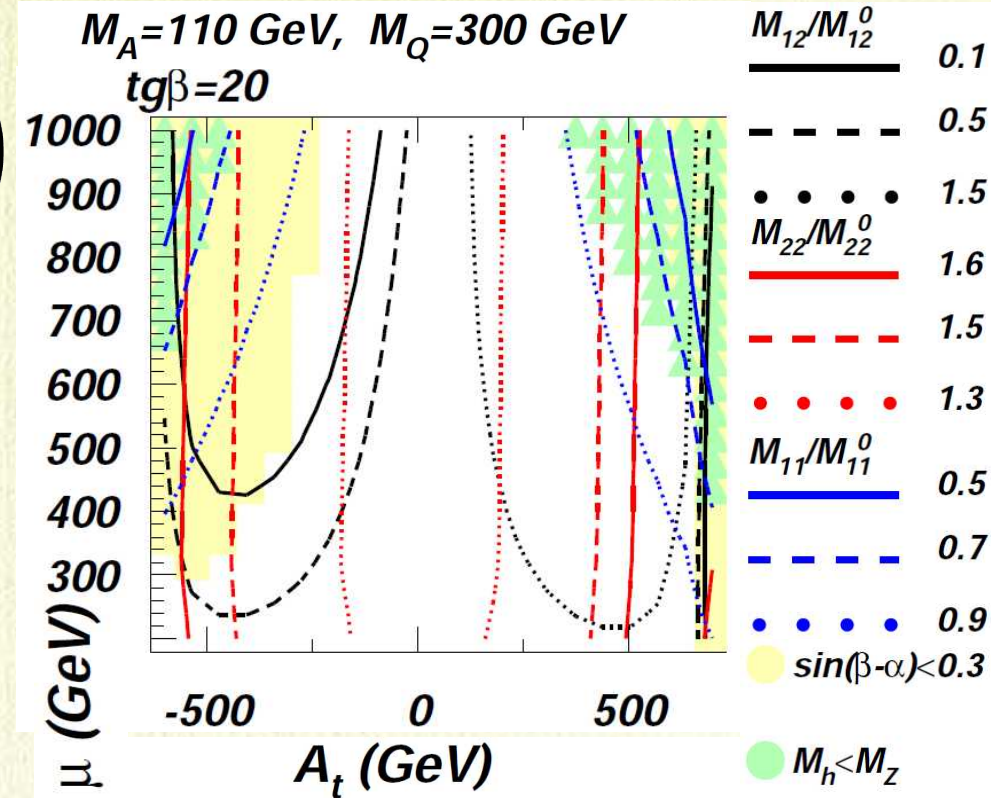
$$0 \leq \beta \leq \pi/2, \quad -\pi/2 \leq \alpha \leq 0$$

1-loop corrections

$$\delta\mathcal{M}_{11}^2 \propto -\tilde{\mu}^2(x_t^2 h_t^4 - a_b^2 h_b^4)$$

$$\delta\mathcal{M}_{12}^2 \propto -\tilde{\mu}[x_t h_t^4(6 - x_t a_t) + \tilde{\mu}^2 a_b h_b^4]$$

$$\delta\mathcal{M}_{22}^2 \propto h_t^4 \left[12 \ln \frac{M_S^2}{m_t^2} + x_t a_t (12 - x_t a_t) \right] - \tilde{\mu}^4 h_b^4$$



- At large A_t and small M_A , $\delta\mathcal{M}_{12}^2$ cancels tree-level mixing $\rightarrow \cos(\alpha) \simeq 0, \sin(\beta - \alpha) \simeq 0$
- light Higgs aligned along h_d – does not receive large corrections
- at large μ \mathcal{M}_{11}^2 is suppressed!

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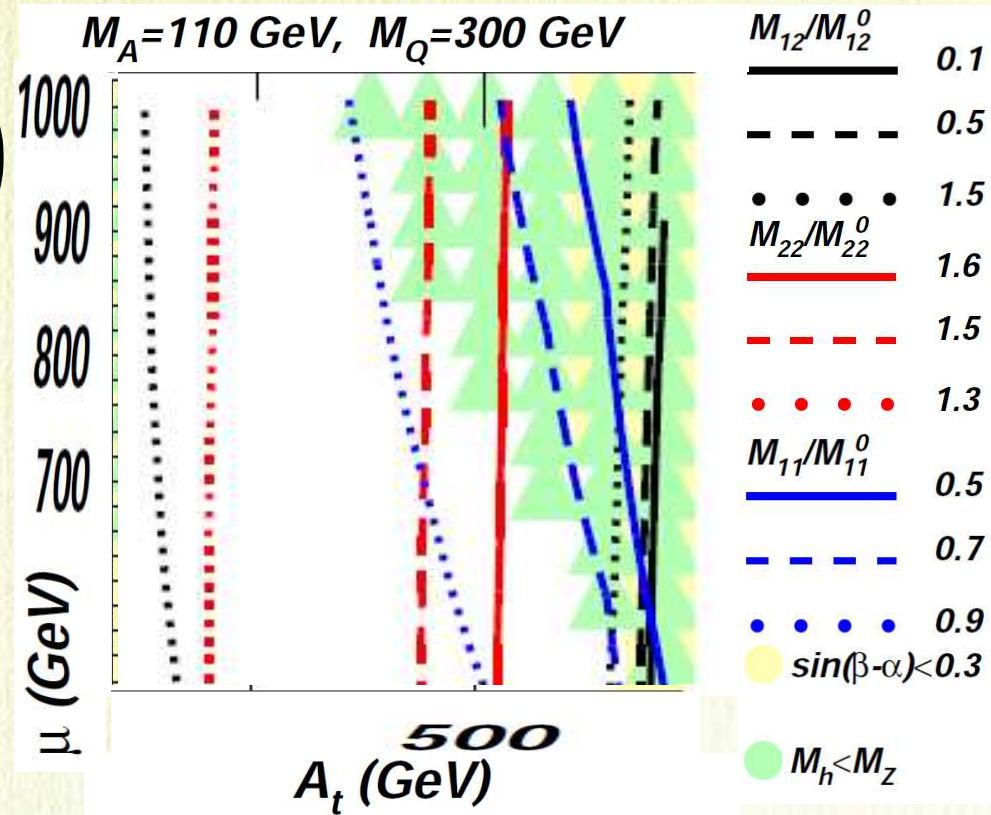
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If light Higgs boson preferred by nature, then how it could have escaped from LEP2 constraints?

✚ Let us check how light MSSM Higgs boson can be, escaping LEP2 constraints

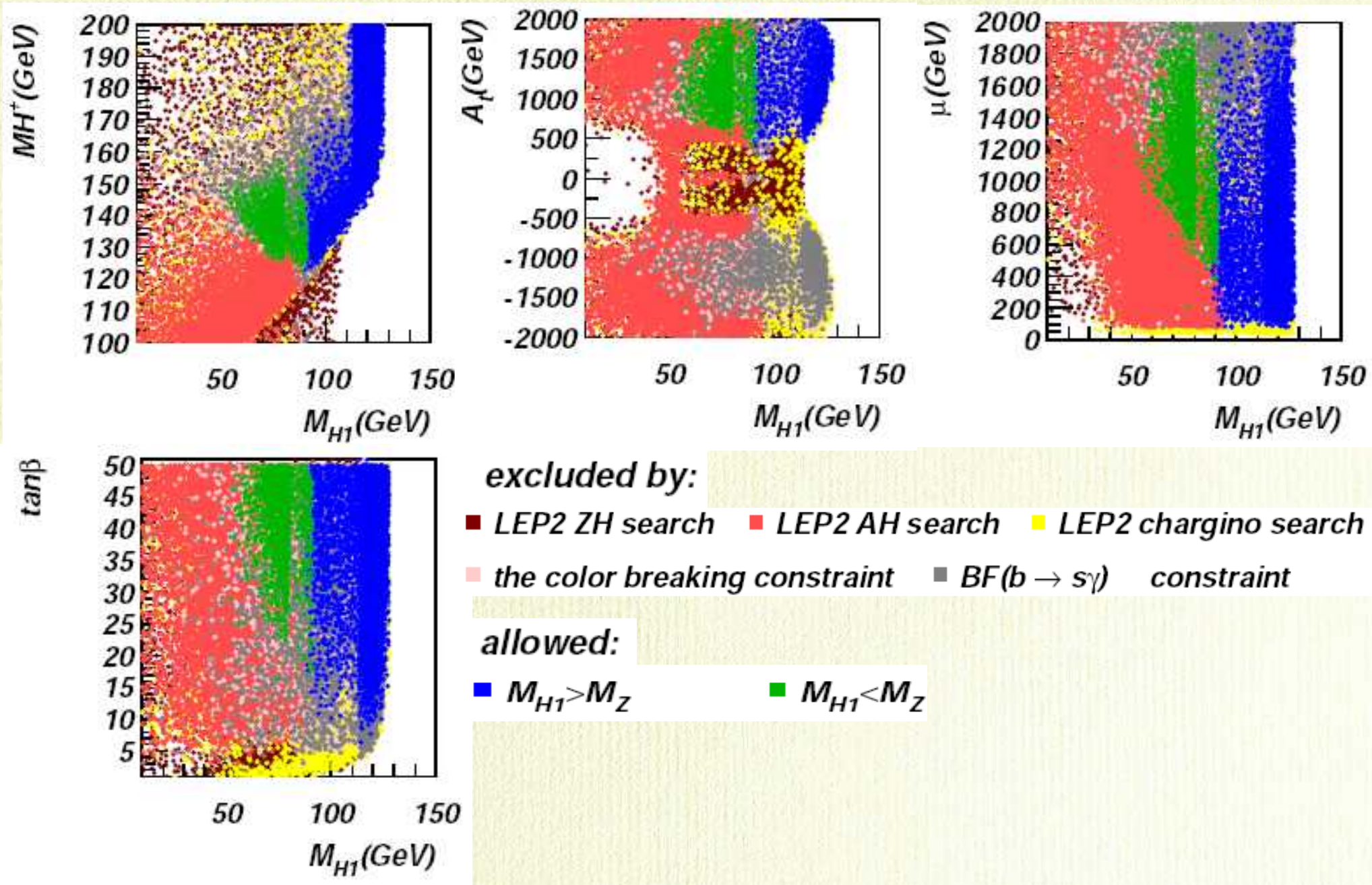
✚ EW parameters scanned with CPsuperH
(Lee, Pilaftsis, Carena, Choi, Drees, Ellis, Wagner)

Parameter space, CP conserving case

Constraints

parameter	lower limit	upper limit	
$\tan \beta$	1.1	50	LEP II $Z\mathcal{H}$ and $A\mathcal{H}$ constraint $\mathcal{H} = (h, H)$
M_{H^\pm}	100	200	$g_{ZZ\mathcal{H}}^2 \times Br(\mathcal{H} \rightarrow b\bar{b}) < F_{Z\mathcal{H}}(M_{\mathcal{H}})$
μ	50	2000	$g_{ZZh}^2 \times Br(A \rightarrow b\bar{b}) \times Br(H \rightarrow b\bar{b}) < F_{Ah}$
M_1	50	500	$g_{ZZH}^2 \times Br(A \rightarrow b\bar{b}) \times Br(h \rightarrow b\bar{b}) < F_{AH}$
M_2	50	500	$M_{\chi_1^\pm} > 100, M_{\tilde{t}_1} > 100$
M_3	50	1000	Color breaking constraints
A_t	0	2000	$\mu < 3m_{Q3}, A_t < 3m_{Q3}$
M_{Q3}	300	700	$\Delta\rho_{SUSY} < 2 \times 10^{-3}$
			$b \rightarrow s\gamma$ SUSY constraint: $ \Delta Br(b \rightarrow s\gamma) < 1 \times 10^{-4}$

Scan Results



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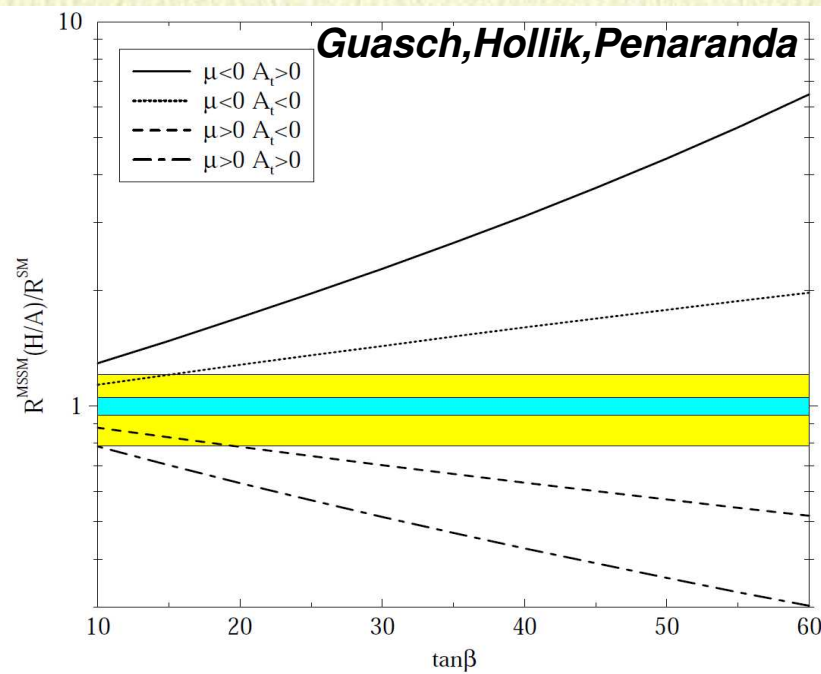
✚ There are points with light Higgs boson in the 60-100 GeV range escaping LEP II ZH and AH search!

✚ No-lose 'theorem' does not work?

✚ There are SUSY corrections suppressing $\tau\tau H$ and bbH couplings in non-universal way!

This is, actually well-studied and generic effect

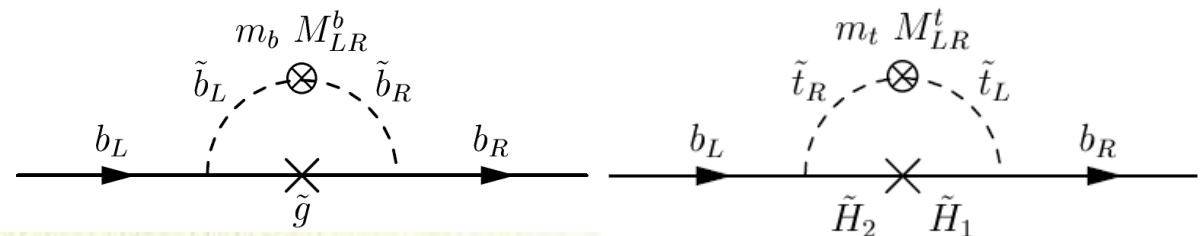
(Carena, Mrenna, Wagner; Borzumati, Farrar, Polonsky; Guasch, Hollik, Penaranda)



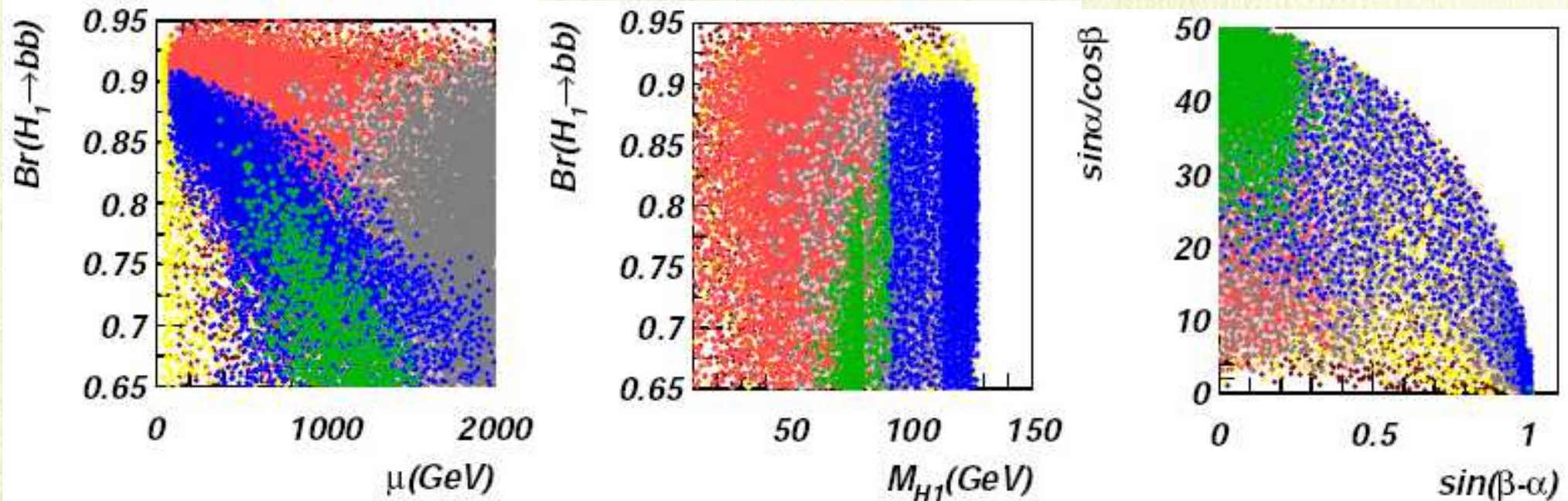
$$R = BR(H \rightarrow b\bar{b}) / BR(H \rightarrow \tau^+\tau^-)$$

$$m_b + \delta m_b = \frac{m_b}{1 + \Delta m_b}$$

$$(\Delta m_b)_{\text{SUSY-QCD}} \propto + \frac{2\alpha_S(M_S)}{3\pi} m_{\tilde{g}} \mu \tan \beta$$



Effect of non-universal $\tau\tau H$ and bbH SUSY corrections to $H \rightarrow bb$ partial decay width



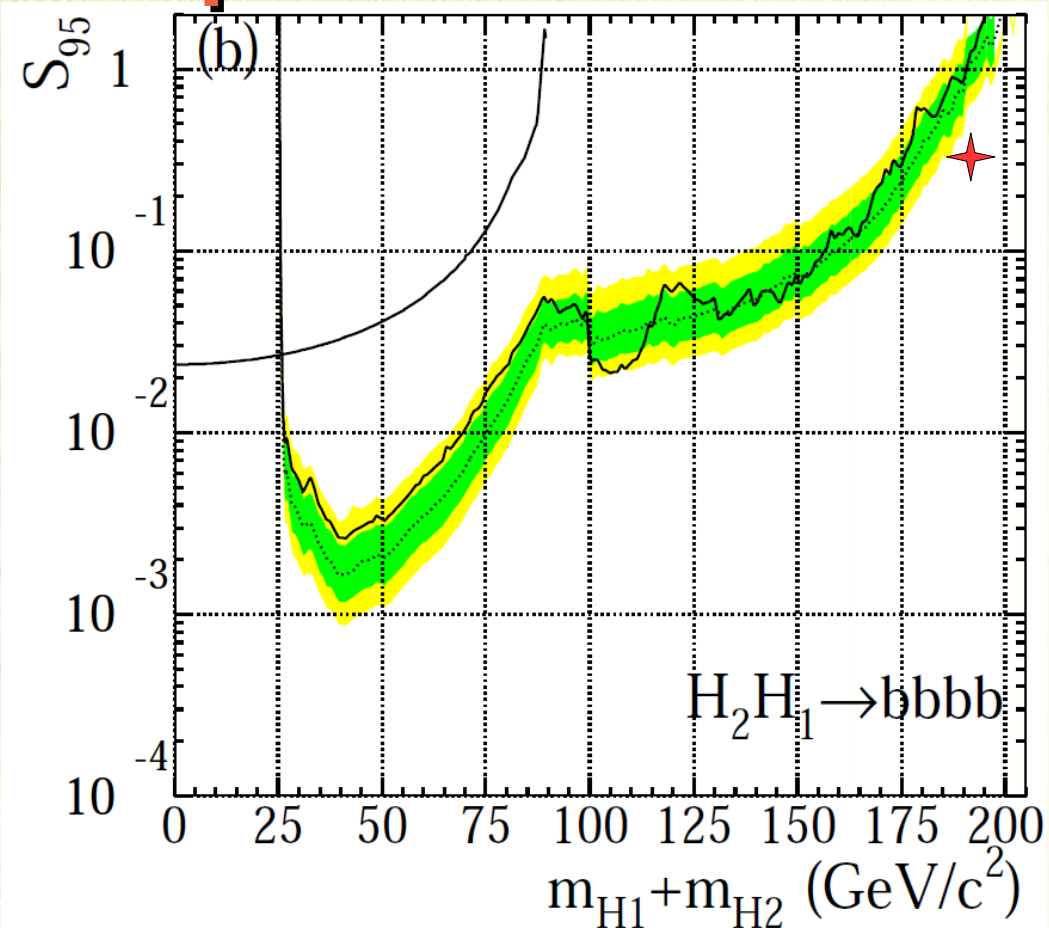
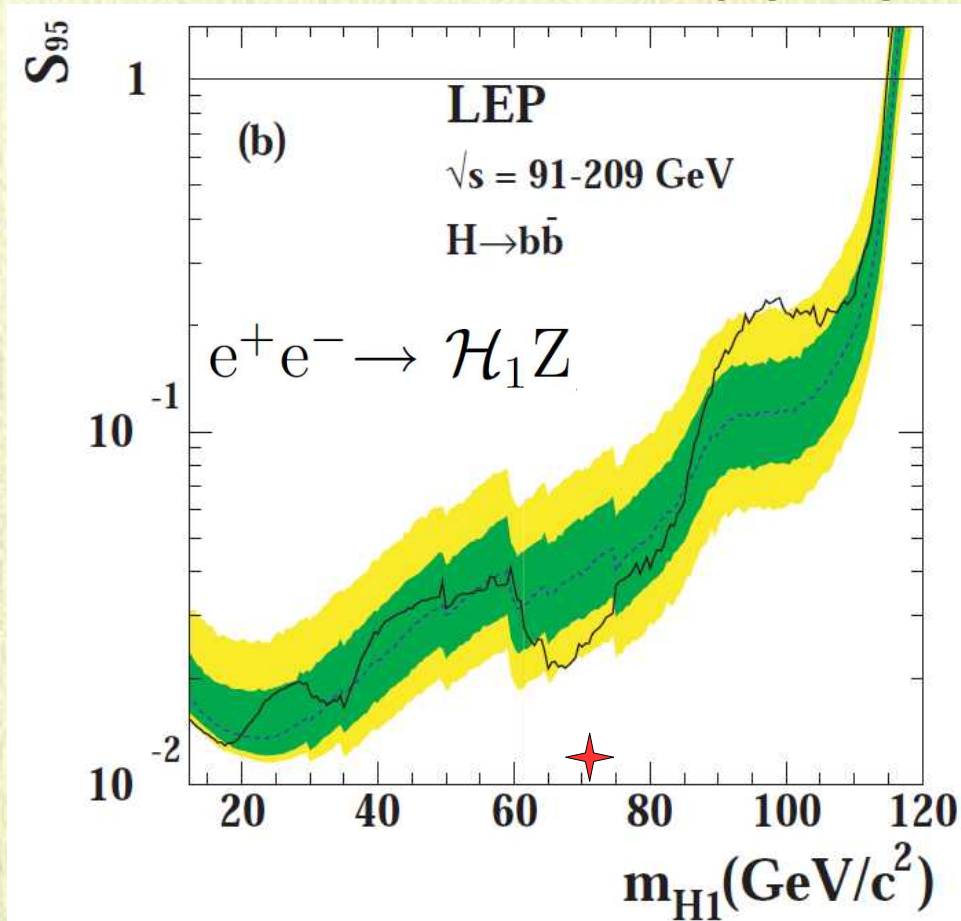
excluded by:

- LEP2 ZH search
- LEP2 AH search
- LEP2 chargino search
- the color breaking constraint
- $BF(b \rightarrow s\gamma)$ constraint

allowed:

- $M_{H_1} > M_Z$
- $M_{H_1} < M_Z$

Lh benchmark point



$\tan \beta$	M_H^+	μ	A_t	M_1/M_2	M_3	M_Q
35	140	1000	1000	100/200	700	400

$$M_h/M_A/M_H = 72/117/121\text{ GeV}$$

$$Br(h/A/H \rightarrow b\bar{b}) = 0.67/0.65/0.73$$

$$g_{ZZh}^2 = 0.011, g_{ZZH}^2 = 0.98, M_{\chi_1^+} = 198\text{ GeV}, M_{\tilde{t}_1} = 163\text{ GeV}$$

$$\Delta\rho = 0.9 \times 10^{-3}, Br(b \rightarrow s\gamma) = 3.9 \times 10^{-4}$$

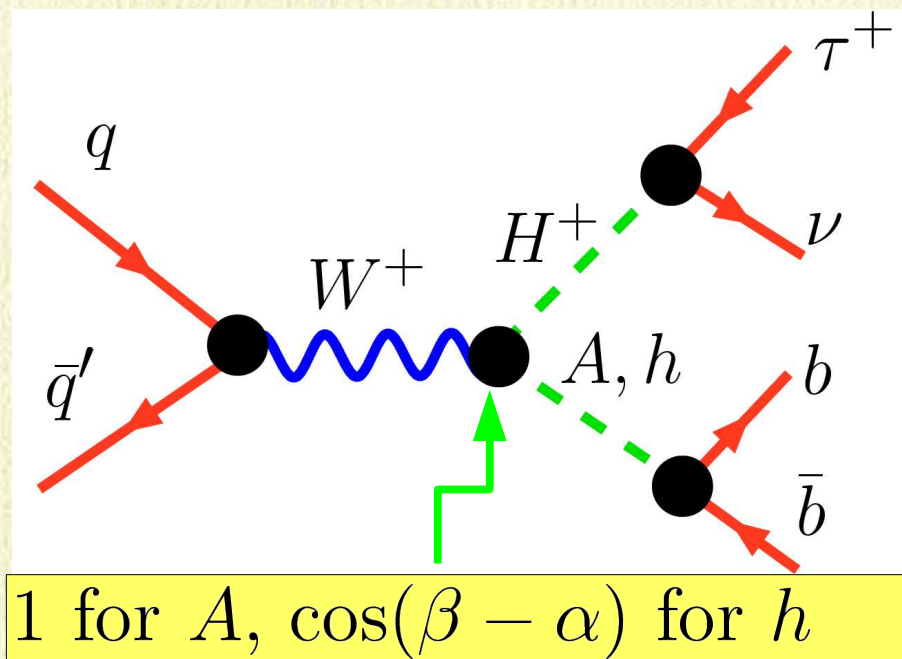
$$\sigma_{Zh}/\sigma_{Zh}^{exp} = 0.28, \sigma_{Ah}/\sigma_{Ah}^{exp} = 0.52$$

Generic features of the scenario

- ✦ Light Charged Higgs – essential non-decoupling regime – small ZZh coupling and large WH^+h coupling, Z-boson recoil Higgs constraints are safe
 - ✦ Intermediate – large μ and A_t
 - ✦ Large $\mu > 0$ and heavy gluino providing non-universal corrections to tau and bottom Yukawa couplings and suppressing Higgs partial decay width to bb
 - ✦ Light stop and chargino, intermediate-high $\tan\beta$ to cancel $O(\text{SM})$ H^+ contribution to $b \rightarrow s\gamma$ ($A_t > 0$).
- One more part of the exciting phenomenology!

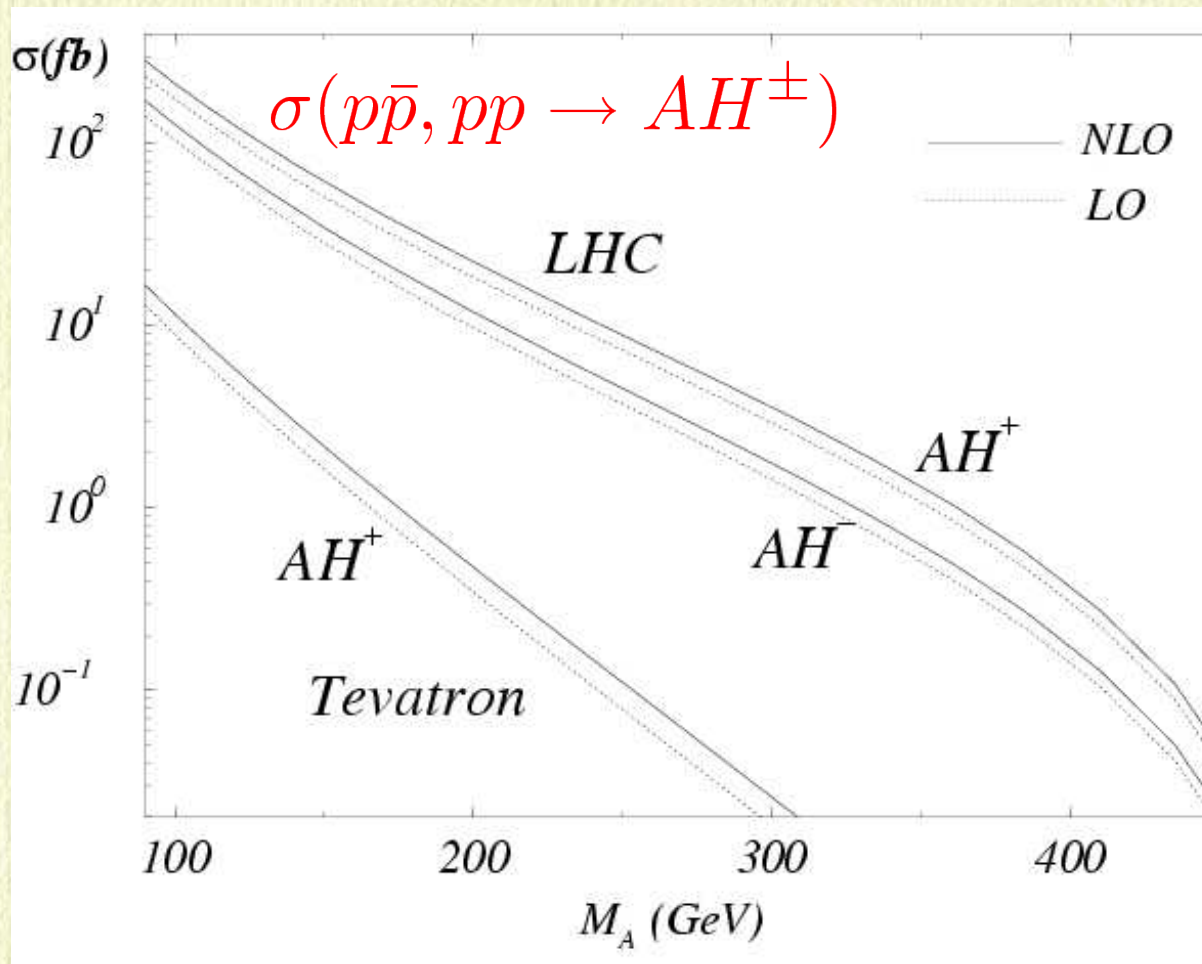
Associated production of Charged – Neutral Higgses as a test of the light Higgs scenario

- ✦ small ZZh coupling and large WH^+h coupling scenario makes H^+h or/and H^+A associate production very special: complementary to LEP II



- ✦ $g_{AH^+W^-} = 1$ and does not depend on SUSY parameters at tree-level

H^+A signal rate



Q.-H. Cao, S. Kanemura, C.-P. Yuan
hep-ph/0311083

NLO QCD correction is about 20%

Signal versus background study

✚ $q\bar{q} \rightarrow W^* \rightarrow A(\rightarrow b\bar{b})H^+(\rightarrow \tau^+\nu)$ process

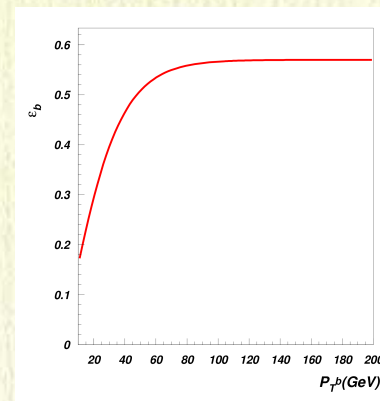
✚ we only consider the $\pi^+\nu$ decay mode of τ^+

✚ $b\bar{b}\pi^+ \cancel{E}_T$ signature

✚ backgrounds:

$$q\bar{q}' \rightarrow W^+ b\bar{b}, \quad q\bar{q}' \rightarrow t\bar{b},$$

$$q\bar{q} \rightarrow t\bar{t}, \quad qg \rightarrow q't\bar{b}$$



✚ Realistic b-tagging efficiency: $\epsilon_b = 0.57 \times \tanh\left(\frac{p_T^b}{35 \text{ GeV}}\right)$

✚ Basic cuts:

$$P_T(b, \bar{b}, \pi^+) > 15 \text{ GeV}, \quad |\eta(b, \bar{b}, \pi^+)| < 3.5, \quad \Delta R(b, \bar{b}, \pi^+) > 0.4$$

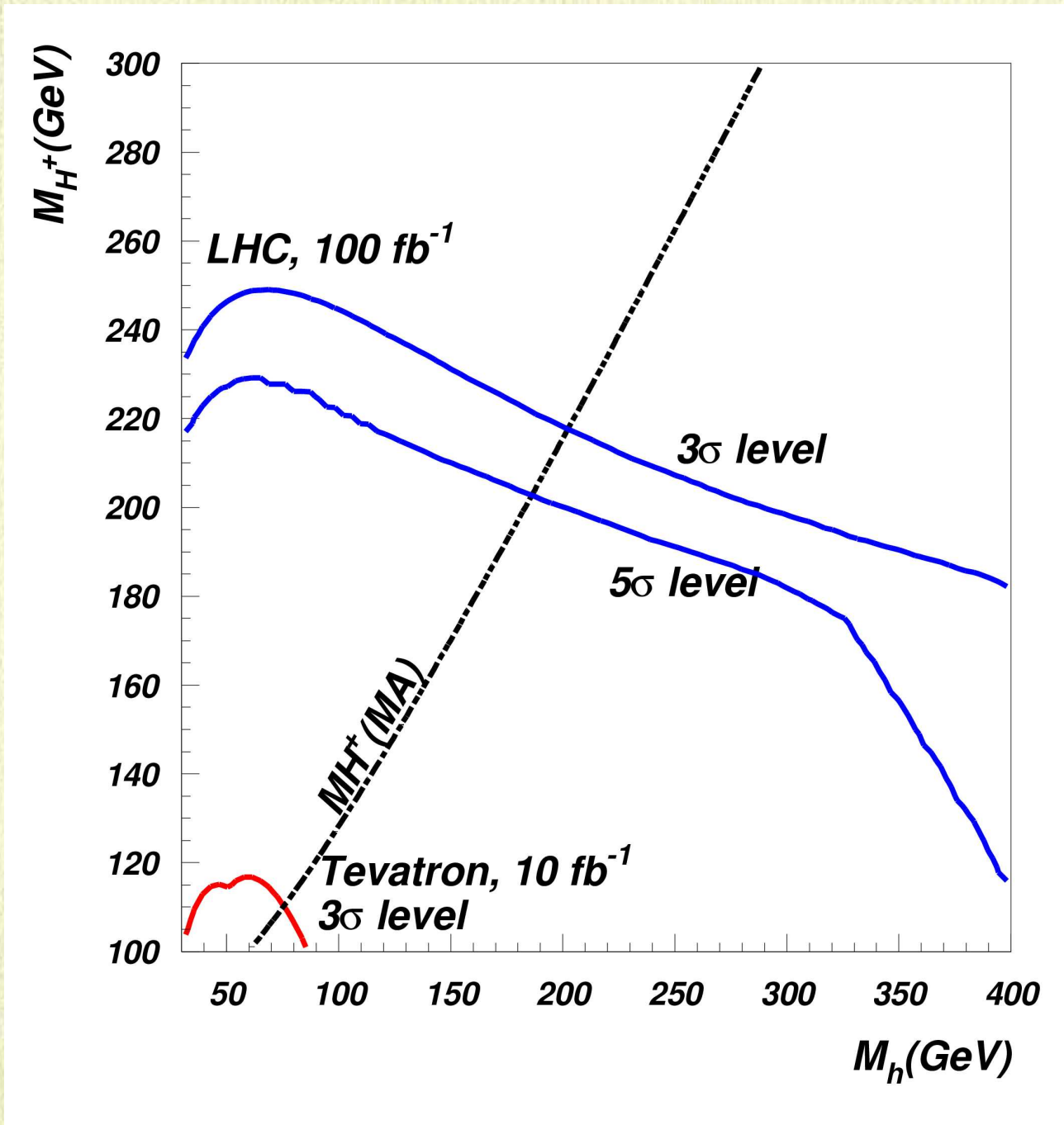
+ veto for jets and leptons in the central region:

$$p_T(\text{lepton}) > 10 \text{ GeV}, \text{ and } |\eta(\text{lepton})| < 3$$

$$p_T(\text{jet}) > 10 \text{ GeV}, \text{ and } |\eta(\text{jet})| < 3.5$$

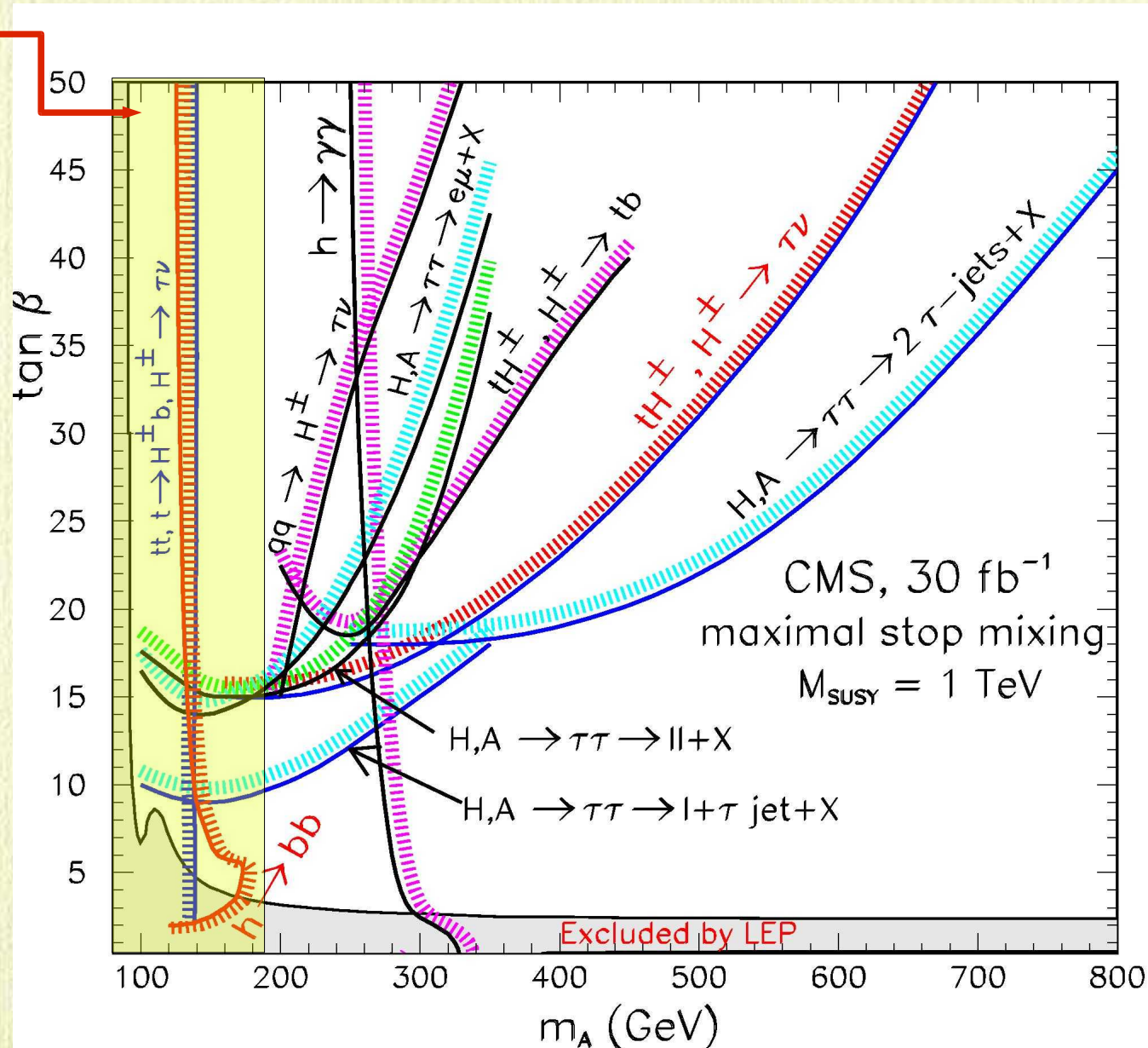
✚ Hard cuts: $\cancel{E}_T > 50 \text{ GeV}, \quad p_T^\pi > 40 \text{ GeV}, \quad |m_{b\bar{b}} - m_A| < 10 \text{ GeV}$

Tevatron/LHC reach for H^+A



Projecting on to $\tan\beta - M_A$ plane

$H^\pm A$



Conclusions

- ✦ **Light MSSM Higgs ~ 60 GeV mass is possible.**
It is realized at $M_{H^+} \sim 130-140$ GeV due to large SUSY corrections to Higgs mixing and due to non-universal SUSY corrections to bottom and tau-mass at for A_t and $\mu > 400$ GeV. It suggests reanalyzing LEP data by combining bb and $\tau\tau$ channels together.
- ✦ **The straightforward test is the search for H^+A**
LHC cover the whole Lh parameter space – complementary to LEP2
- ✦ **Possible solution for SUSY fine-tuning problem?**
It also predicts an exciting phenomenology: light stops and charginos.
- ✦ **LHC has a great potential for probing the H^+A even for heavy A : independent of $\tan\beta$!**