

# Constraints on B and Higgs Physics in MSSM

A. Menon

Argonne National Laboratory and  
the University of Chicago

May 16th, 2006

Based on:

M. Carena, A.M., R. Noriega-Papaqui, A. Szykman and  
C. Wagner, [arXiv:hep-ph/0603106];

# MSSM Higgs and Sfermion sector review

- The Higgs neutral components acquire VEV's  $v_1$  and  $v_2$  and their ratio is  $\tan \beta = v_2/v_1$ .
- Neglecting CP violation in the Higgs sector, electroweak breaking leaves one CP odd Higgs of mass  $M_A$  and two CP even Higgses with tree-level masses

$$M_{h,H}^2 = \frac{1}{2} \left( M_A^2 + M_Z^2 \mp \sqrt{(M_A^2 + M_Z^2)^2 - 4M_Z^2 M_A^2 \cos^2 2\beta} \right),$$

and one charged Higgs of mass

$$M_{H^\pm}^2 = M_A^2 + M_W^2$$

- Assuming a uniform trilinear for the different generations of squarks (and neglecting D-term contributions) the generic structure of the squark mass matrices is

$$M_U^2 = \begin{pmatrix} \hat{M}_{\tilde{u}_L}^2 & \left( A_u - \frac{\mu}{\tan \beta} \right) \frac{v_2}{\sqrt{2}} \hat{Y}_u \\ \left( A_u^* - \frac{\mu^*}{\tan \beta} \right) \frac{v_2}{\sqrt{2}} \hat{Y}_u^\dagger & M_{\tilde{u}_R}^2 \end{pmatrix}$$

$$M_D^2 = \begin{pmatrix} \hat{M}_{\tilde{d}_L}^2 & (A_d - \mu \tan \beta) \frac{v_1}{\sqrt{2}} \hat{Y}_d \\ \left( A_d^* - \mu^* \tan \beta \right) \frac{v_1}{\sqrt{2}} \hat{Y}_d^\dagger & M_{\tilde{d}_R}^2 \end{pmatrix}.$$

# The Effective Resummed MSSM Lagrangian

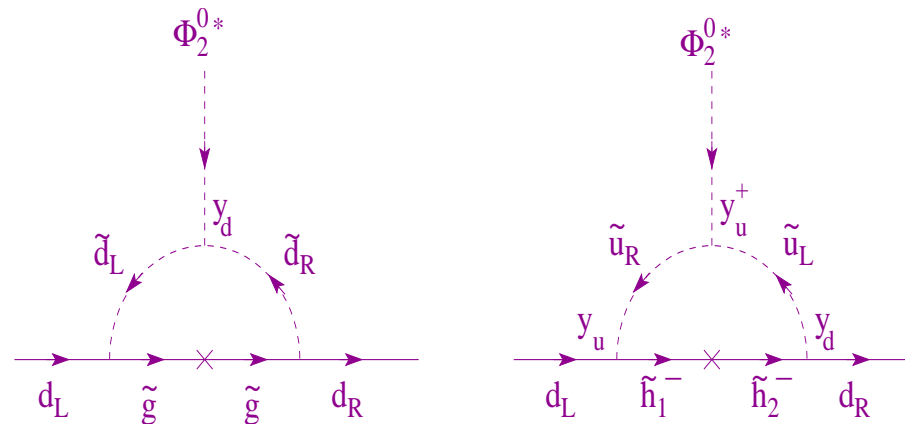
- Resumming the **SUSY loop corrections** to the quark masses leads to an effective mass Lagrangian for the down quarks.

$$-\mathcal{L}_m = \bar{d}_R \mathbf{m}_d [1 + \tan \beta (\epsilon_0 + \mathbf{V}_0^\dagger \epsilon_Y |\mathbf{Y}_u|^2 \mathbf{V}_0)] d_L + h.c.$$

where  $\mathbf{V}_0$  is the tree-level CKM matrix and for uniform squark masses

$$|\epsilon_0| \approx \frac{2\alpha_s}{3\pi} |M_3| |\mu| C_0(m_{\tilde{b}_1}^2, m_{\tilde{b}_2}^2, |M_3|^2)$$

$$|\epsilon_Y| \approx \frac{1}{16\pi^2} |A_t| |\mu| C_0(m_{\tilde{t}_1}^2, m_{\tilde{t}_2}^2, |\mu|^2)$$



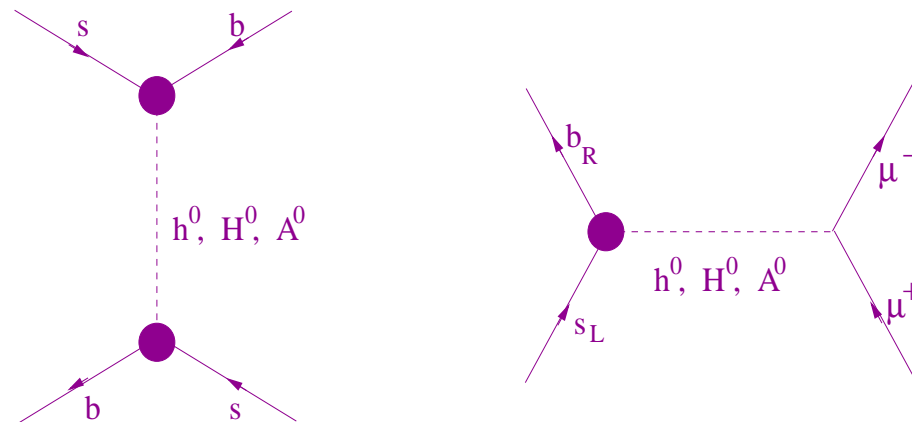
- The quark mass matrices need to be re-diagonalized. Thereby inducing **Flavor Changing Neutral Currents (FCNC)**  $\propto V^{3J*} V^{3I}$ .

# Constraints on B Physics in the MSSM

# Contributions to $\Delta M_s$ and $B_s \rightarrow \mu^+ \mu^-$ in MSSM

- At large  $\tan \beta$  the **double penguin** contribution to  $\Delta M_s$  is dominant and  $\propto |\epsilon_Y|^2 \tan^4 \beta / (|1 + \epsilon_3 \tan \beta|^2 M_A^2)$ , which interferes destructively with the **SM**.
- Similarly for large  $\tan \beta$  the dominant contribution to  $B_s \rightarrow \mu^+ \mu^- \propto |\epsilon_Y|^2 \tan^6 \beta / M_A^4$
- Therefore values of  $B_s \rightarrow \mu^+ \mu^-$  and  $\Delta M_s$  at large  $\tan \beta$  are correlated. So for uniform **squark** masses the only **SUSY** dependence in their ratio is

$$\frac{\Delta M_s}{\mathcal{BR}(B_s \rightarrow \mu^+ \mu^-)} \propto \frac{M_A^2}{\tan^2 \beta}$$



- For moderate or low  $\tan \beta$  the large contributions to  $\Delta M_s$  are possible for light squarks, charginos or gluinos.

# Experimental constraints and Standard Model values of $\Delta M_s$ and $B_s \rightarrow \mu^+ \mu^-$

- The SM contribution to  $\Delta M_s$  is dominated by **W**-Top box diagram and allows ranges

CKMfitter:  $\Delta M_s = 21.7_{-4.2}^{+5.9} \text{ps}^{-1}$

J. Charles *et al.* [CKMfitter Group], Eur. Phys. J. C **41**, 1 (2005)  
[arXiv:hep-ph/0406184];

UTfit:  $\Delta M_s = (21.5 \pm 2.6) \text{ps}^{-1}$

<http://www.utfit.org>

- The experimental values of  $\Delta M_s$  are:

D0:  $\Delta M_s = (19 \pm 2) \text{ps}^{-1}$ .

V. Abazov *et al.* [D0 Collaboration], [arXiv:hep-ex/0603029];

CDF  $\Delta M_s = (17.33_{-0.21}^{+0.42} \pm 0.07(\text{syst})) (\text{ps})^{-1}$ .

<http://www-cdf.fnal.gov/physics/new/bottom/060406.blessed-Bsmix/>

- The **Z**-penguins mediate the  $B_s \rightarrow \mu^+ \mu^-$  process in the **SM** and predicts a value

$$\mathcal{BR}(B_s \rightarrow \mu^+ \mu^-)_{SM} = (3.8 \pm 1) \times 10^{-9}$$

- The **CDF** experimental bound on  $\mathcal{BR}(B_s \rightarrow \mu^+ \mu^-) \leq 1.5 \times 10^{-7}$ .

R. Bernhard *et al.* [CDF Collaboration], [arXiv:hep-ex/0508058];

# How large can the Double Penguin SUSY contributions to $\Delta M_s$ be?

- Large SUSY contributions to  $\Delta M_s$  within the experimental bound on  $BR(B_s \rightarrow \mu^+ \mu^-)$

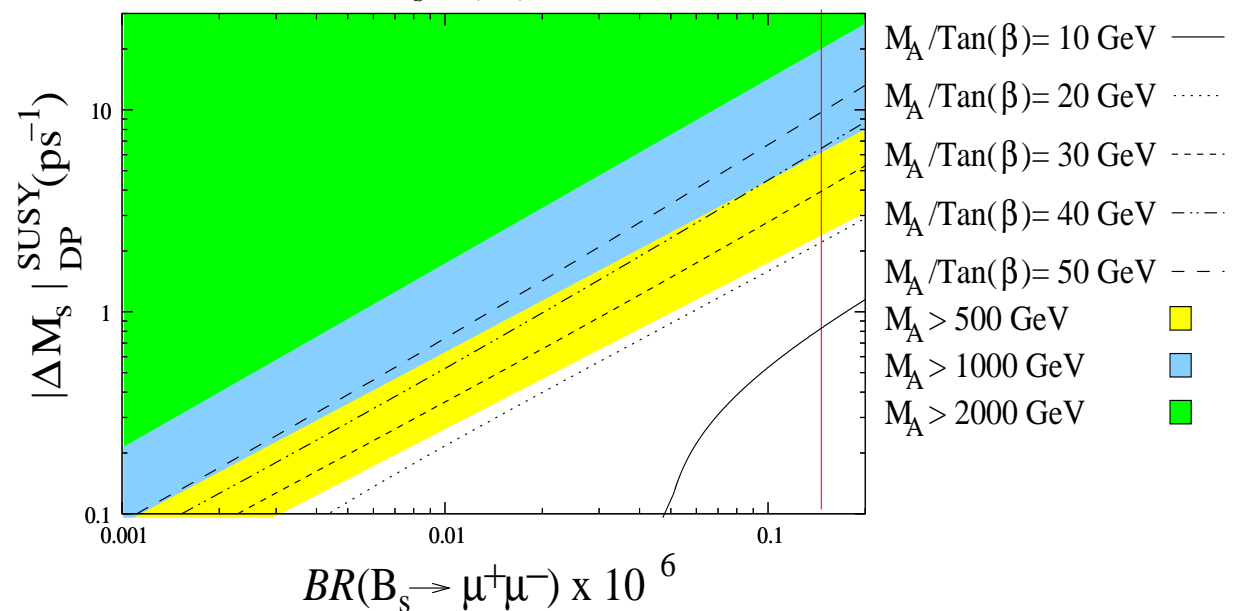
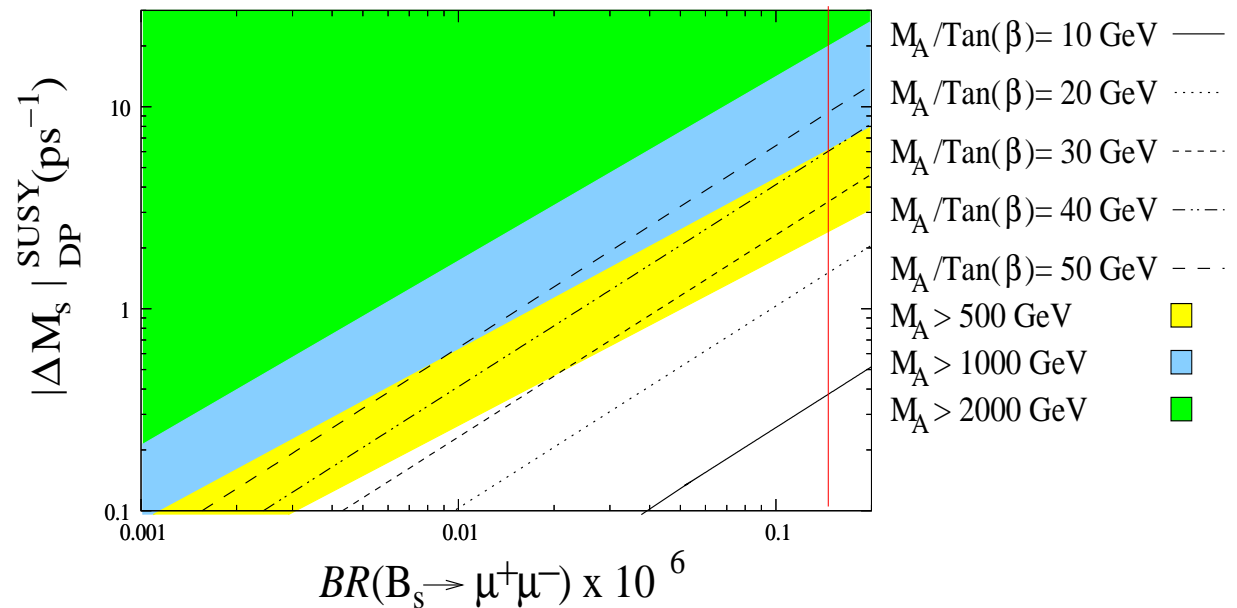
requires  $\mu \sim 2M_{\tilde{q}} \sim M_3$ .

- For natural values of  $M_A \leq 1000$  GeV the largest double penguin contributions can be at most a few  $ps^{-1}$ .

- For MFV, splitting the squark masses so that  $M_{\tilde{q}_1} = M_{\tilde{q}_2} = 10M_{\tilde{q}_3}$  still means a  $\Delta M_s$  of a few  $ps^{-1}$ .

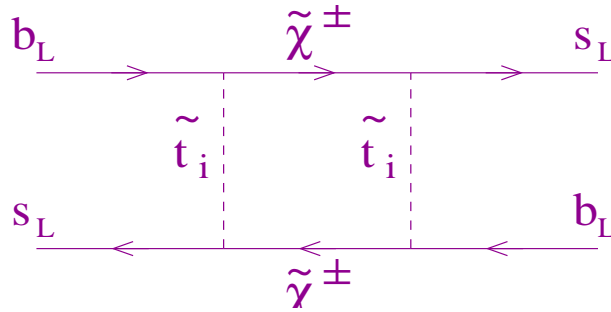
- Can resolve  $2\sigma$  discrepancy between SM and experiment G. Isidori and P. Paradisi, [arXiv:hep-ph/0605012];  $\Rightarrow$  a lower bound

$$BR(B_s \rightarrow \mu^+ \mu^-) \geq 3 \times 10^{-8}$$

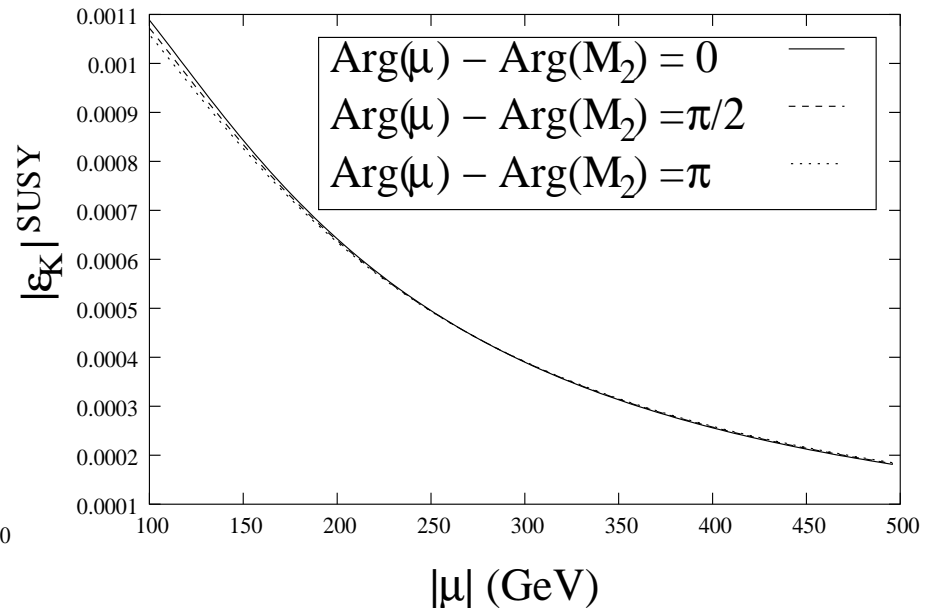
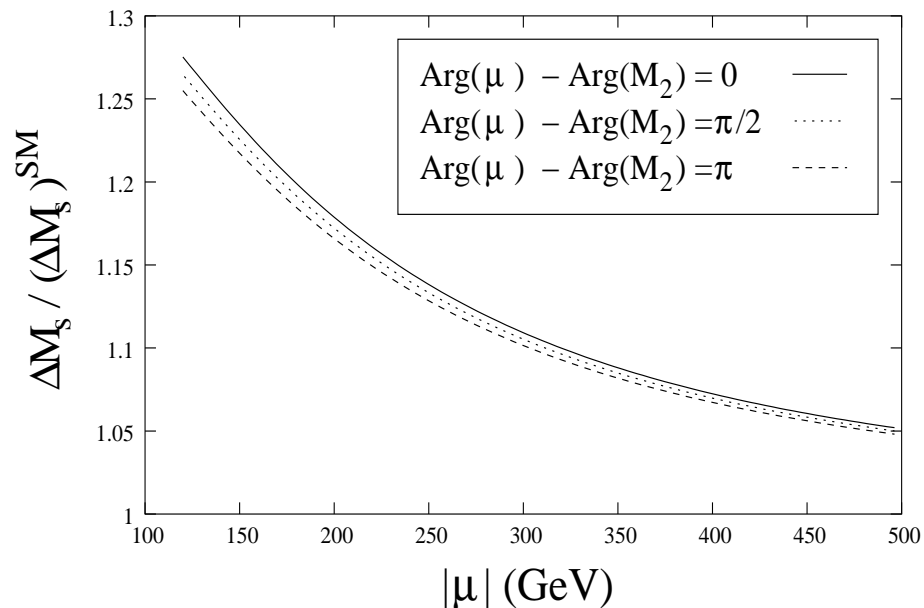


# Stop-Chargino Contributions to $\Delta M_s$ in MFV

- Light stops and charginos can give substantial contributions to  $\Delta M_s$  even for low values of  $\tan\beta$ .



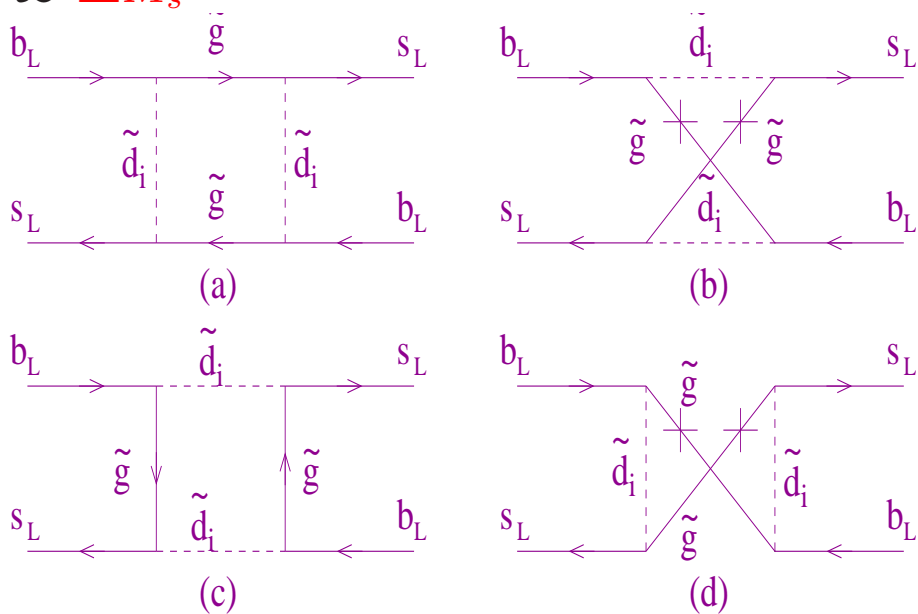
- However these kinds of SUSY particle spectra can also induce large contributions to  $\epsilon_K$  if SM CP phase is order  $\pi/3$ .
- The experimentally measured value of  $\epsilon_K = (2.282 \pm 0.014) \times 10^{-3}$



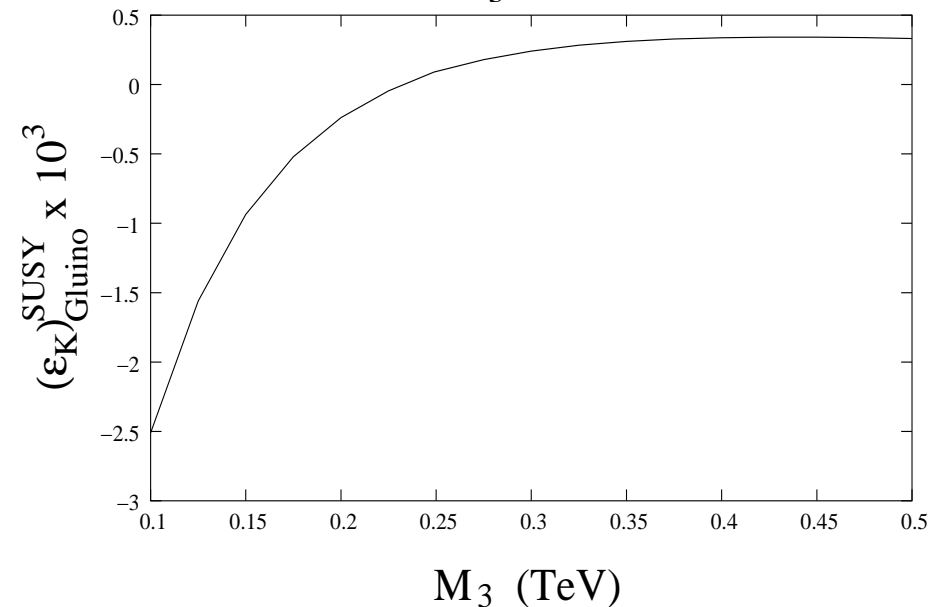
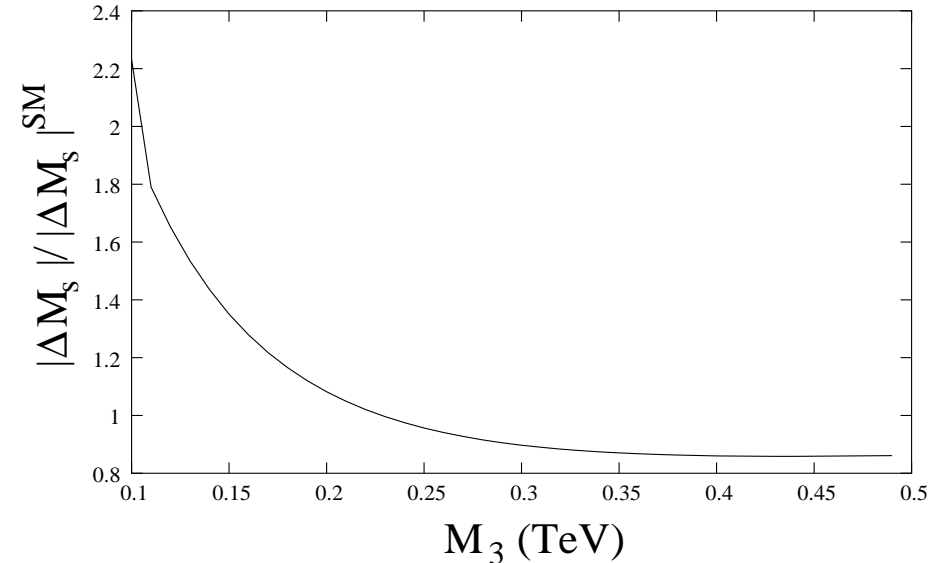


# Glino Contributions to $\Delta M_s$ for the Non Minimal Flavor Violation

- In Non Minimal Flavor Violation the gluino-quark-squark vertex is not diagonal and so box diagrams with light gluinos and sbottoms can give substantial contributions to  $\Delta M_s$



- Generating these large contributions needs extremely constrained SUSY parameter region.



# Constraints on Higgs Searches at the Tevatron

# $b \rightarrow s\gamma$ in the MSSM

- The experimental bound on  $\mathcal{BR}(b \rightarrow s\gamma) = 3.38_{-0.28}^{+0.3} \times 10^{-4}$ .
- The theoretical error on the SM value:  $\mathcal{BR}(b \rightarrow s\gamma)^{Exp} - \mathcal{BR}(b \rightarrow s\gamma)^{SM} \leq 1 \times 10^{-4}$ .  
M. Neubert, Eur. Phys. J. C **40**, 165 (2005), [arXiv:hep-ph/0408179]
- The Charged Higgs amplitude in the large  $\tan\beta$  limit is

$$\mathcal{BR}(b \rightarrow s\gamma)_{H^\pm} \propto \frac{h_t \cos\beta - \delta h_t \sin\beta}{\cos\beta(1 + \epsilon_3 \tan\beta)}$$

where

$$\delta h_t \propto h_t \frac{\alpha_s}{3\pi} \mu M_3$$

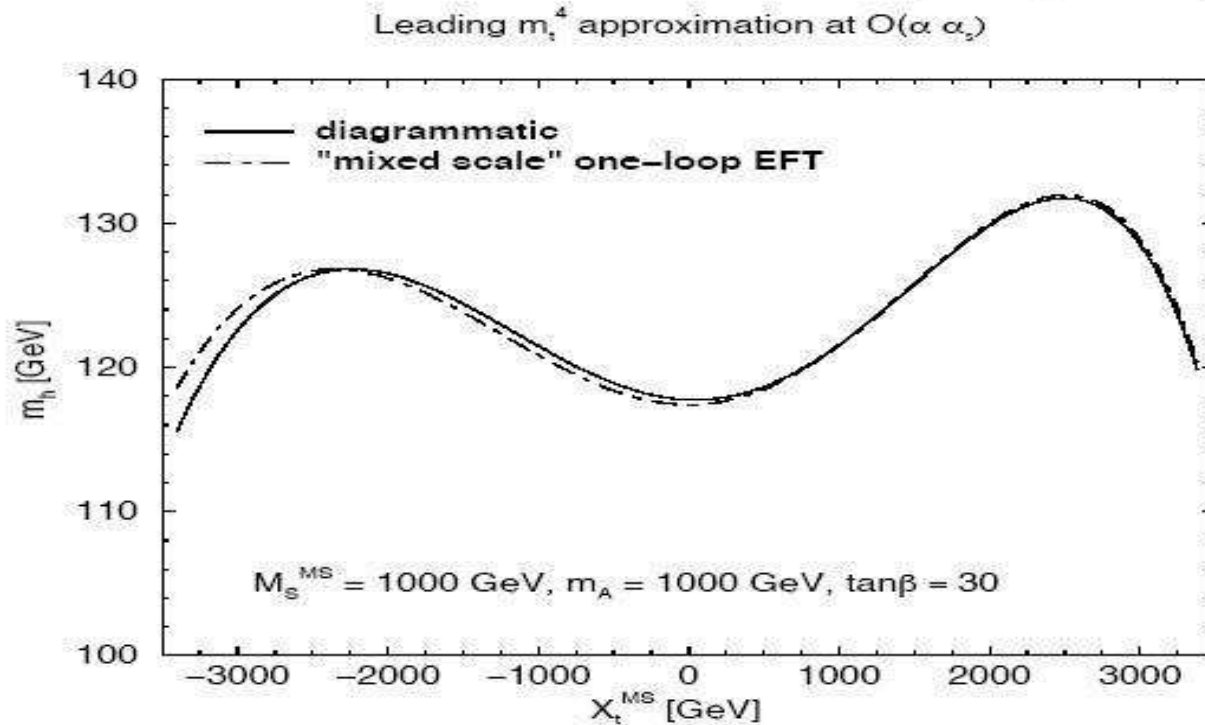
- While the Chargino-Stop amplitude is

$$\mathcal{BR}(b \rightarrow s\gamma)_{\chi^\pm} \propto \frac{\mu A_t \tan\beta}{1 + \epsilon_3 \tan\beta}$$

for large  $\tan\beta$

M. Carena, et. al., Phys. Lett. B **499** (2001) [arXiv:hep-ph/001003]  
G. Degrandi, et.al., JHEP **0012**, 009 (2000) [arXiv:hep-ph/0009337].

# The Higgs Bench Mark Scenarios in the MSSM



M. Carena et.al. Nucl. Phys. B **580**, 29 (2000) [arXiv:hep-ph/0001002].

- For large CP odd Higgs mass  $M_A$  and uniform squark mass  $M_S$  the SM like Higgs has

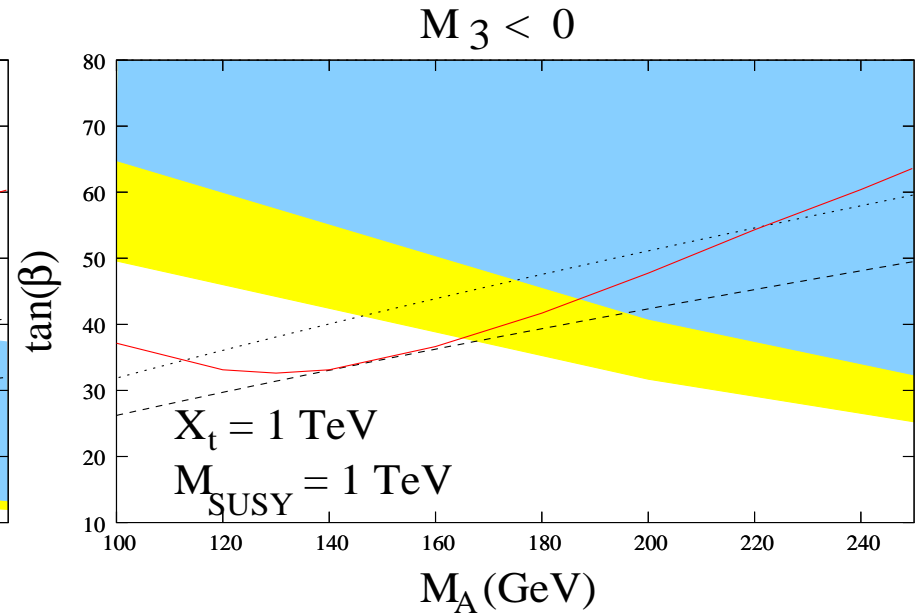
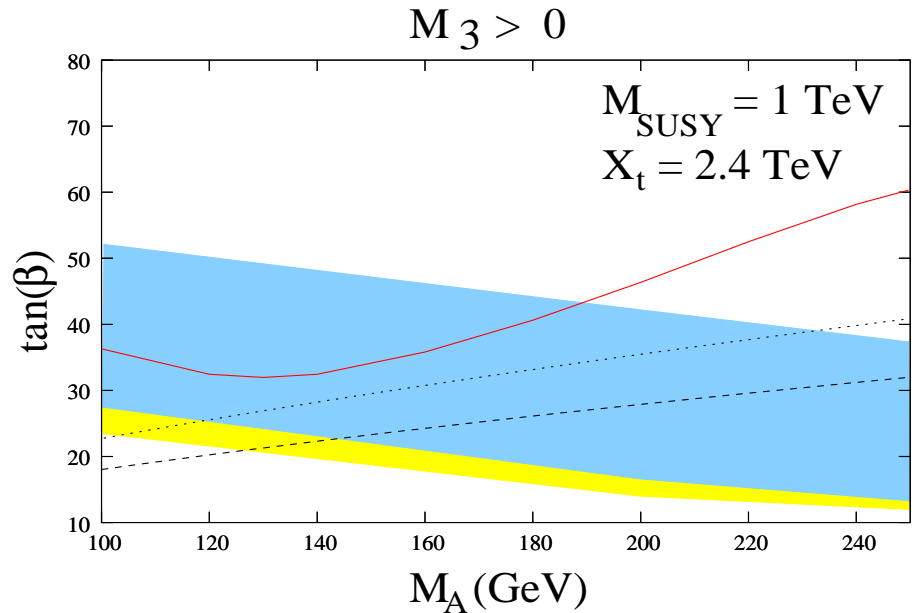
$$M_h^2 \approx M_Z^2 \cos^2 2\beta + \frac{3m_t^4}{4\pi^2 v^2} \left( \log \frac{M_S^2}{m_t^2} + \frac{X_t}{M_S} \left( 1 - \frac{X_t^2}{12M_S^2} \right) \right)$$

where  $X_t = A_t - \frac{\mu}{\tan\beta}$

- Maximal Mixing  $\Rightarrow X_t = \sqrt{6}M_{SUSY}$ , while Minimal Mixing  $\Rightarrow X_t = 0$ .
- Tevatron has greater sensitivity to for a low mass of  $M_h$ .

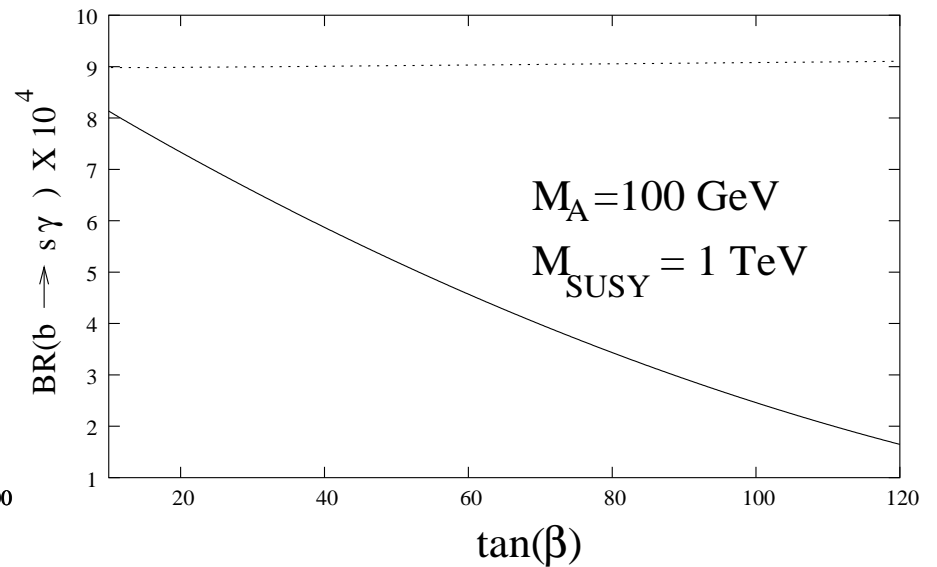
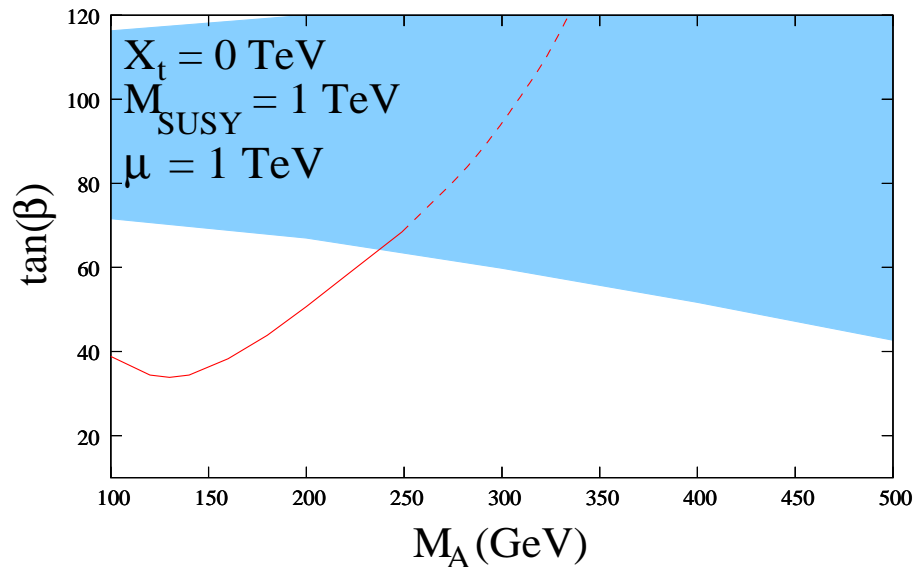
# Tevatron Higgs searches with moderate to large $X_t$

- $BR(B_s \rightarrow \mu^+ \mu^-) \propto \epsilon_\gamma \propto \mu A_t$ . So experimental bound  $\Rightarrow$  small  $\mu$  for  $X_t \geq 500$  GeV.
- For small negative  $\mu \Rightarrow$  approximately constant **Charged Higgs** contribution and growing negative **Chargino Stop** contribution to  $b \rightarrow s\gamma$ .



# Tevatron Higgs searches with small $X_t$

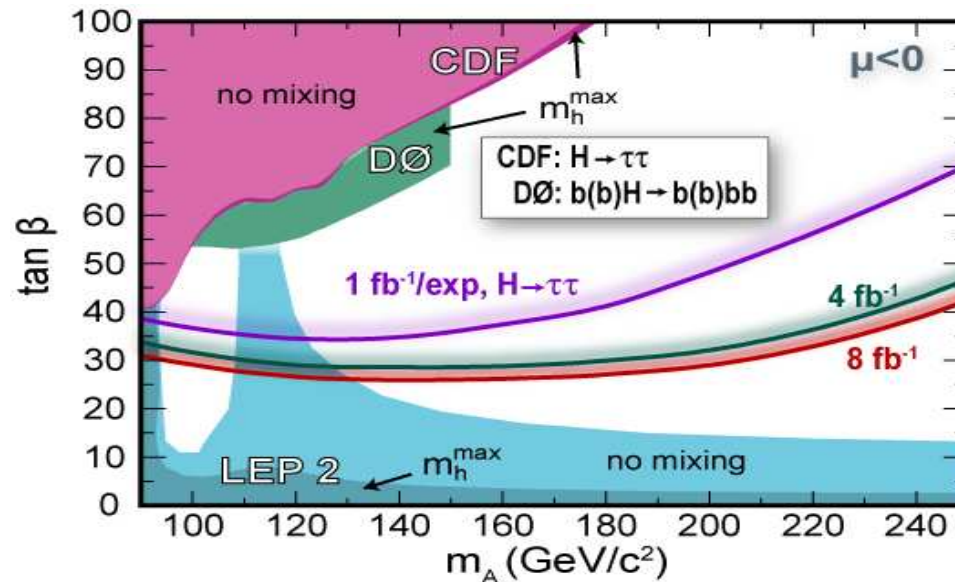
- $X_t \sim 0 \Rightarrow A_t$  small.  $\Rightarrow$  a small contribution to  $b \rightarrow s\gamma$  from the **Charginos and Stops**.
- But also a large **Charged Higgs** contribution to  $b \rightarrow s\gamma$ , unless  $\mu$  is large so that  $\delta h_t \sim h_t$ . In which case  $b \rightarrow s\gamma$  puts not constraint on  $M_A$ .
- $BR(B_s \rightarrow \mu^+ \mu^-)$  puts no constraint on the  $M_A - \tan \beta$  plane as  $A_t$  is small.



# Conclusions

- Within the **MSSM** the measurements of  $\Delta M_s$  at **D0** and **CDF** are consistent with the bound on  $B_s \rightarrow \mu^+ \mu^-$ .
- The assumption that  $2\sigma$  difference between the **SM** and the experiment is due to large  $\tan\beta$  **SUSY** effects can be tested by improving the bound on  $B_s \rightarrow \mu^+ \mu^-$ .
- Searches for **Non Standard Model Higgses** at the **Tevatron** are highly constrained for large  $X_t$ . The Tevatron can only probe regions of low to moderate  $X_t$ .
- In addition the small  $X_t$  scenario looks much more promising for the **Tevatron** as it is more sensitive for lower values of  $M_h$ .
- Observation of a **Non Standard Model Higgs** at the **Tevatron** would imply either moderate  $X_t$  small  $\mu$  or large  $\mu$  small  $X_t$  or a deviation from **Minimal Flavor Violation**.

# Estimating the Tevatron Reach for Higgs Searches



[http://www-cdf.fnal.gov/physics/exotic/r2a/20050519.mssm\\_htt/index.htm](http://www-cdf.fnal.gov/physics/exotic/r2a/20050519.mssm_htt/index.htm)

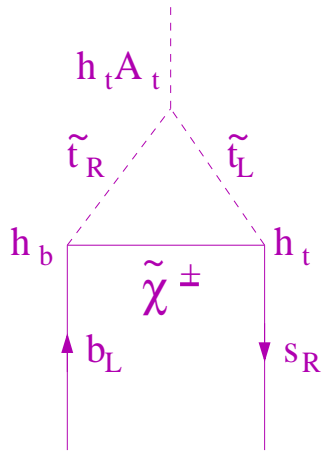
- The approximate relation between the Standard Model production cross-section of  $\tau$  pairs and that in the MSSM at large  $\tan \beta$  allows us to estimate the Tevatron reach.

$$\sigma(gg, b\bar{b} \rightarrow A) \times \mathcal{BR}(A \rightarrow \tau^+\tau^-) \sim \sigma(gg, b\bar{b} \rightarrow A)_{SM} \frac{\tan^2 \beta}{(1 + \epsilon_3 \tan \beta)^2 + 9}$$

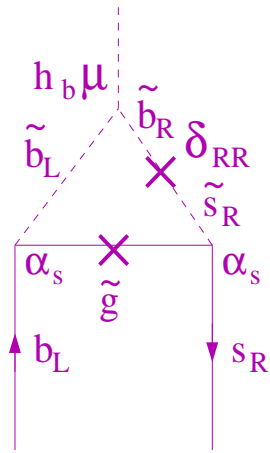
M. Carena *et al.*, [arXiv:hep-ph/0511023]

- For the Tevatron we have used the  $1 \text{ fb}^{-1}$  luminosity curve for  $H \rightarrow \tau\tau$ .

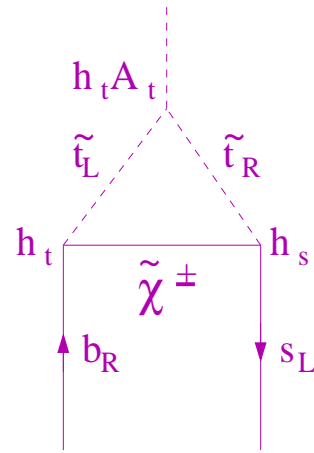




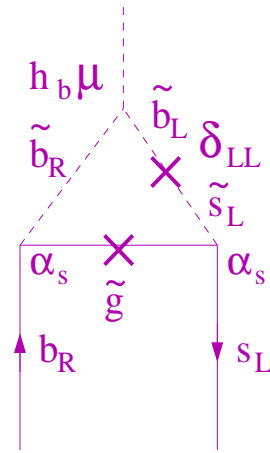
$$\sim m_b \epsilon_Y$$



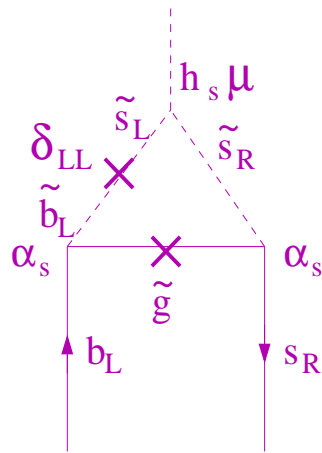
$$\sim m_b \delta_{RR} \epsilon_{RR}$$



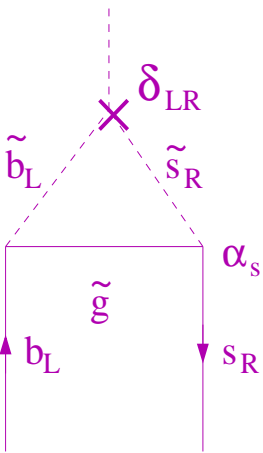
$$\sim m_s \epsilon_Y$$



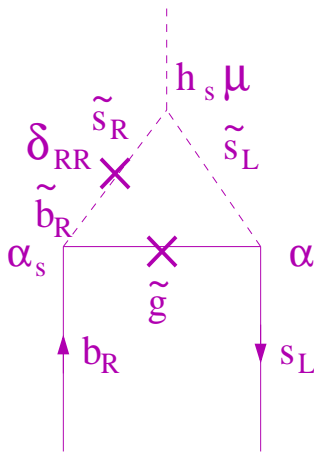
$$\sim m_b \delta_{LL} \epsilon_{LL}$$



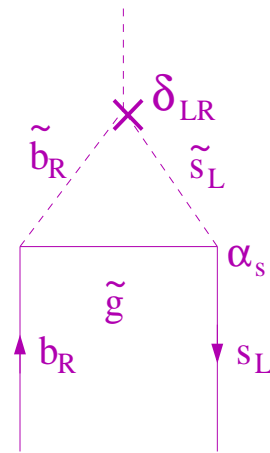
$$\sim m_s \delta_{LL} \epsilon_{LL}$$



$$\sim \delta_{LR} \epsilon_{LR}$$



$$\sim m_s \delta_{RR} \epsilon_{RR}$$



$$\sim \delta_{LR} \epsilon_{LR}$$