
How large are Electroweak Radiative Corrections at High Energies?

all results are preliminary

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1 – Introduction

- In the past few years calculations of electroweak (EW) radiative corrections at high energies ($\gg M_{W,Z}$) have been performed for a number of processes
 - ➔ $f' \bar{f} \rightarrow \ell' \ell$ (Kühn et al.)
 - ➔ $p \bar{p} \rightarrow \ell^\pm \nu, p \bar{p} \rightarrow \ell^+ \ell^-$ (UB, D. Wackerath, Dittmaier and Krämer)
 - ➔ prompt photon and Zj production at hadron colliders (Kühn et al.)
 - ➔ di-boson production (Accomando et al., Hollik and Meier)
 - ➔ inclusive jet production at hadron colliders (Norton et al.)
 - ➔ $p \bar{p} \rightarrow t \bar{t}$ (Norton et al., Kühn et al.)

- These calculations show that EW corrections become **large and negative** at high energies, due to the presence of **Sudakov-like logarithms** ($((\alpha/\pi) \log(\hat{s}/M_{W,Z}^2))$).
- **Where are these logarithms coming from?**
 - ☞ IN QED, these logarithms cancel between virtual and real corrections (**KLN theorem**); observables which are inclusive over soft final states (ie. photons) are infrared safe (**Bloch-Nordsieck (BN) theorem**)
 - ☞ In the EW case, the incoming $q'\bar{q}$ system does have a non-zero $SU(2) \times U(1)$ charge, and, due to the non-abelian character of the gauge group, the BN-theorem is violated (**remark**: In QCD the BN-theorem is also violated, but one sums/averages over colors. This effectively restores the BN-theorem)

➡ Furthermore, since the EW symmetry is broken and the massive W and Z bosons decay, the real EW radiative corrections (ie. W and Z radiation) lead to a different final state, and thus are often ignored

- The existing calculations thus are applicable to **exclusive searches/reactions**
- However, in experiment, one rarely considers exclusive reactions; in most cases processes are (semi-)inclusive
- Real EW corrections (W and Z radiation) thus have to be included in the calculation.
- This results in a partial compensation of the large negative corrections originating from the Sudakov-like logarithms
- **So, how large are EW radiative corrections when realistic experimental conditions are taken into account?**

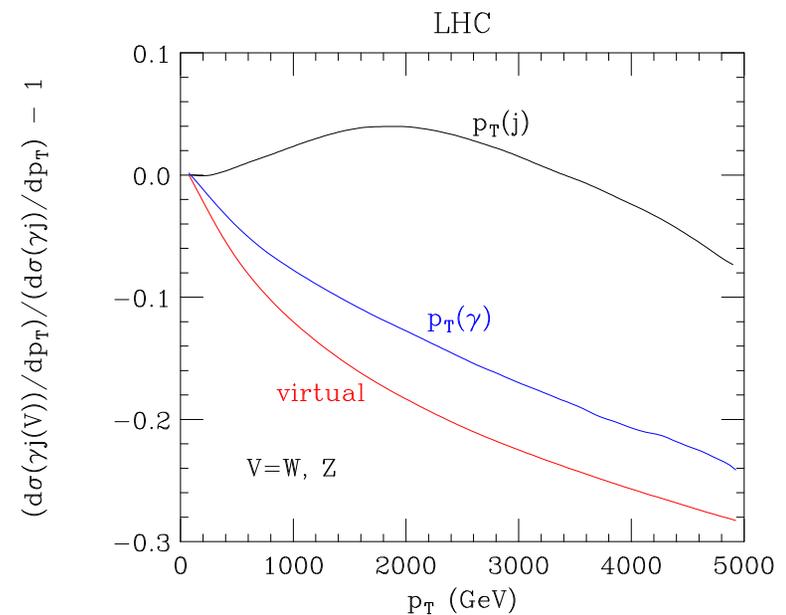
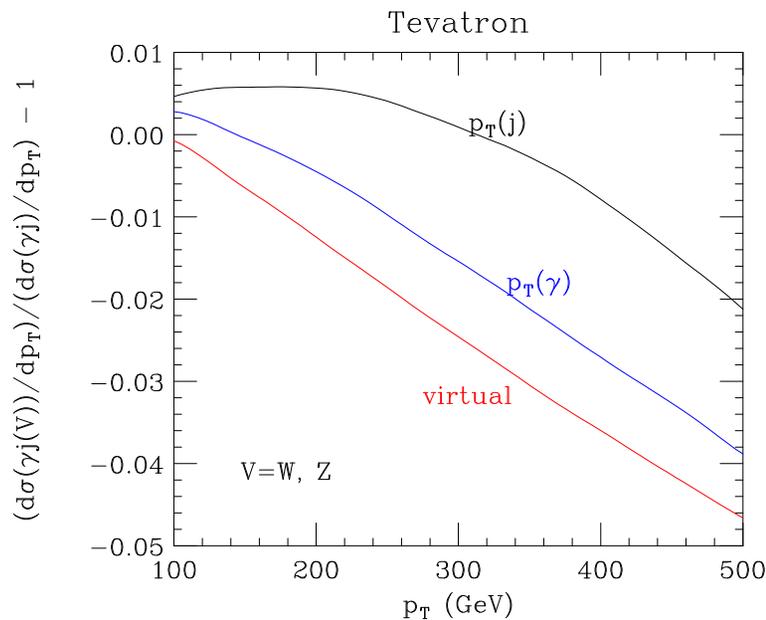
2 – Prompt Photon Production

- LO process: $p\bar{p} \rightarrow \gamma j$
- typical CDF/DØ selection criteria:
 - ☞ require a hard ($p_T(\gamma) > 10 \text{ GeV}$), isolated ($\Delta R > 0.4$) photon
 - ☞ some analyses also require the missing E_T in the event to be small ($\cancel{p}_T < 20 \text{ GeV}$) to reject events with large calorimeter noise
 - ☞ there is no restriction on the number of jets or leptons in the event
- The one-loop NLL weak corrections have a very compact form and can easily be included in a γj parton level MC program (Kühn et al.) they agree at the percent level with the full weak one-loop corrections

- Real EW radiative corrections: $W\gamma j$ and $Z\gamma j$ production
- To find out how big these are begin by imposing cuts **only** on the photon and jet:

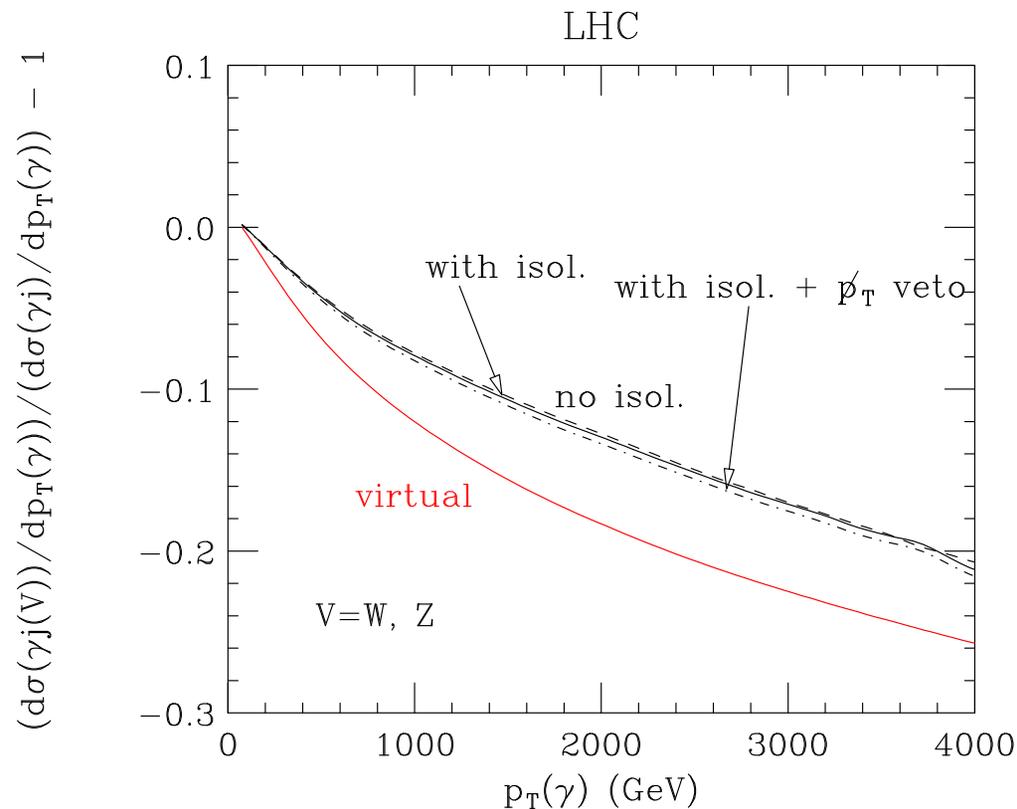
$$p_T(\gamma), p_T(j) > 25 (50) \text{ GeV} \quad \text{at Tevatron (LHC),}$$
$$|\eta(\gamma)|, |\eta(j)| < 2.5 \quad \Delta R(\gamma, j) > 0.4$$

- No W and Z decays are included at this point.
- This gives the **maximum possible** effect of the real EW radiative corrections
- only include NLL weak one-loop corrections (i.e. photonic corrections are not included)



- At LO, the $p_T(\gamma)$ and $p_T(j)$ distributions are equal, but this is not the case for $W\gamma j$ production
- Tevatron: the $V\gamma j$ ($V = W, Z$) differential cross section approaches 0.5% (2.5%) at large $p_T(\gamma)$ ($p_T(j)$)
- LHC: the $V\gamma j$ differential cross section approaches 5% (22%) at large $p_T(\gamma)$ ($p_T(j)$)

- the one-loop EW corrections are a few percent at most at the Tevatron, but can reach 20 – 30% at the LHC
- real W , Z emission may reduce the effect of the $\mathcal{O}(\alpha)$ 1-loop radiative corrections **somewhat** for the $p_T(\gamma)$ distribution, and **substantially** for the $p_T(j)$ distribution
- for the $p_T(\gamma)$ distribution at the LHC they are of the same size as the $\mathcal{O}(\alpha_s^2)$ corrections (at large $p_T(\gamma)$)
- however, the $p_T(j)$ distribution is not a good observable as there can be additional jets in the event from gluon bremsstrahlung or $V \rightarrow jj$
- Now add W , Z decays and require that photon is isolated from W , Z decay products (except ν): $\Delta R(\gamma, j) > 0.4$, $\Delta R(\gamma, \ell) > 0.4$
(This assumes that selection criteria for prompt photon events at the LHC will be similar to those used at the Tevatron)
- focus on LHC

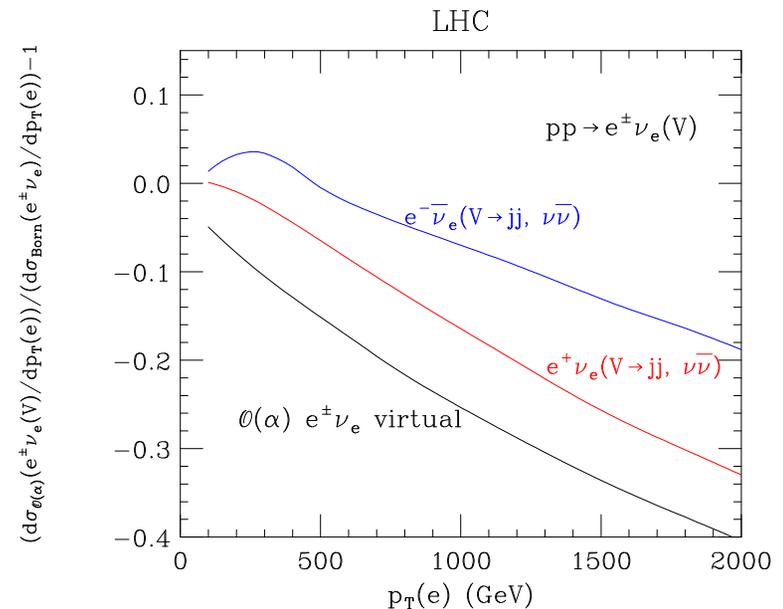
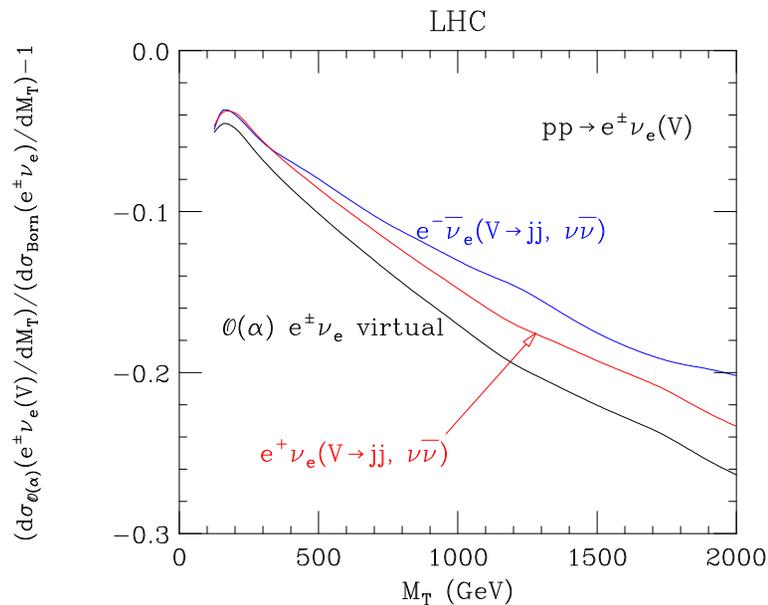


- p_T veto: require $p_T < 5 \text{ GeV}^{1/2} \sqrt{\sum p_T}$
- W, Z decay effects hardly change the picture
- Conclusion: real W, Z radiation moderately reduces the effect of the $\mathcal{O}(\alpha)$ one-loop corrections in prompt photon production

3 – Drell-Yan Production

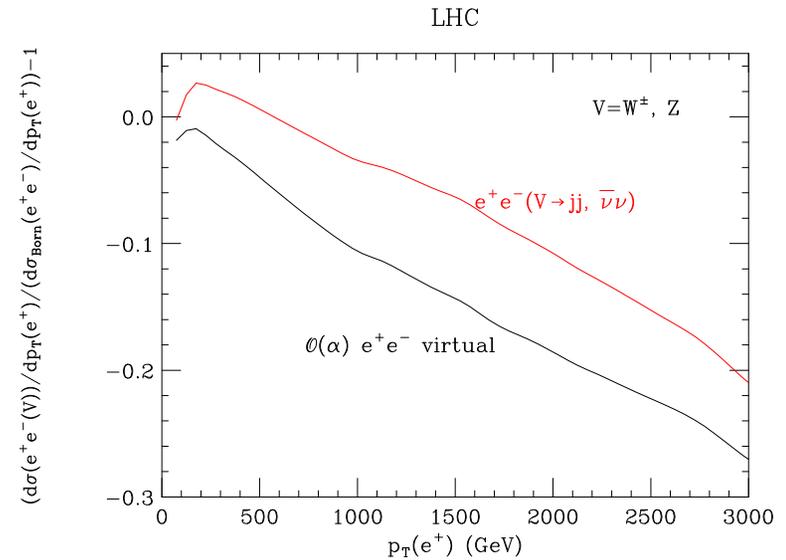
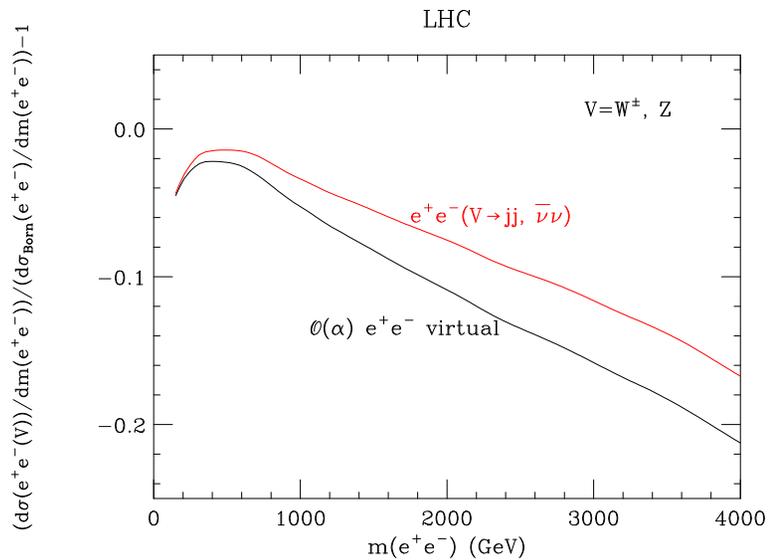
- start with charged channel: $p\bar{p}^{(-)} \rightarrow \ell\nu$
- used to search for new heavy charged vector bosons
- selection criteria:
 - ☞ **one** high p_T charged lepton: events with two or more charged leptons are classified as di-boson events
 - ☞ missing transverse momentum $\cancel{p}_T > 25 \text{ GeV}$
 - ☞ any number of jets
- real EW radiative corrections: $W^\pm\ell\nu$ and $Z\ell\nu$ production (WW , WZ and W, Z bremsstrahlung diagrams)

- virtual corrections: full one-loop $\mathcal{O}(\alpha)$ (including photonic corrections)
- focus on LHC and $\ell = e$; recombine photons and electrons for small opening angles
 - ☞ necessary because photons and electrons which are collinear cannot be discriminated
 - ☞ minimizes the effect of the photonic corrections (we are not interested in them)
- for μ final state relative effects are smaller because photonic corrections play a larger role (no recombination with photon; hard photons close to μ are vetoed)
- consider $e\nu$ transverse mass (M_T) and $p_T(e)$ distributions



- The real EW radiative corrections reach **3%** (**6%**) for W^+ (W^-) production in the M_T , and **10%** (**20%**) in the $p_T(e)$ distribution
- They are larger for the $p_T(e)$ distribution because W resonance region is excluded in M_T distribution
- They reduce the effect of the $\mathcal{O}(\alpha)$ one-loop corrections somewhat in the M_T distribution but significantly (up to a factor 2) in the $p_T(e)$ distribution

- Finally look at neutral channel: $p\bar{p}^{(-)} \rightarrow \ell^+\ell^-$
- used to search for new heavy neutral gauge bosons
- selection criteria:
 - ☞ **two** same flavor opposite charge high p_T charged leptons: events with three or more are classified as di-boson events
 - ☞ missing transverse momentum \cancel{p}_T small (we use $< 5\sigma$)
 - ☞ any number of jets
- real EW radiative corrections: $W^\pm\ell^+\ell^-$ and $Z\ell^+\ell^-$ production (WZ , ZZ and W, Z bremsstrahlung diagrams)
- virtual corrections: full one-loop $\mathcal{O}(\alpha)$ (including photonic corrections)
- focus on LHC and $\ell = e$; look at di-lepton invariant mass and $p_T(e)$ distribution



- the real EW corrections reach about 6% at large p_T 's and invariant masses

4 – Conclusions

- The size of the EW radiative corrections at hadron colliders depends on the experimental selection criteria
- In (partially) inclusive reactions, real EW radiative corrections may significantly reduce the effect of the $\mathcal{O}(\alpha)$ one-loop corrections
- Details depend on the process considered, and the distribution which is studied.