



New Jet Fragmentation Results at CDF



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for CDF collaboration

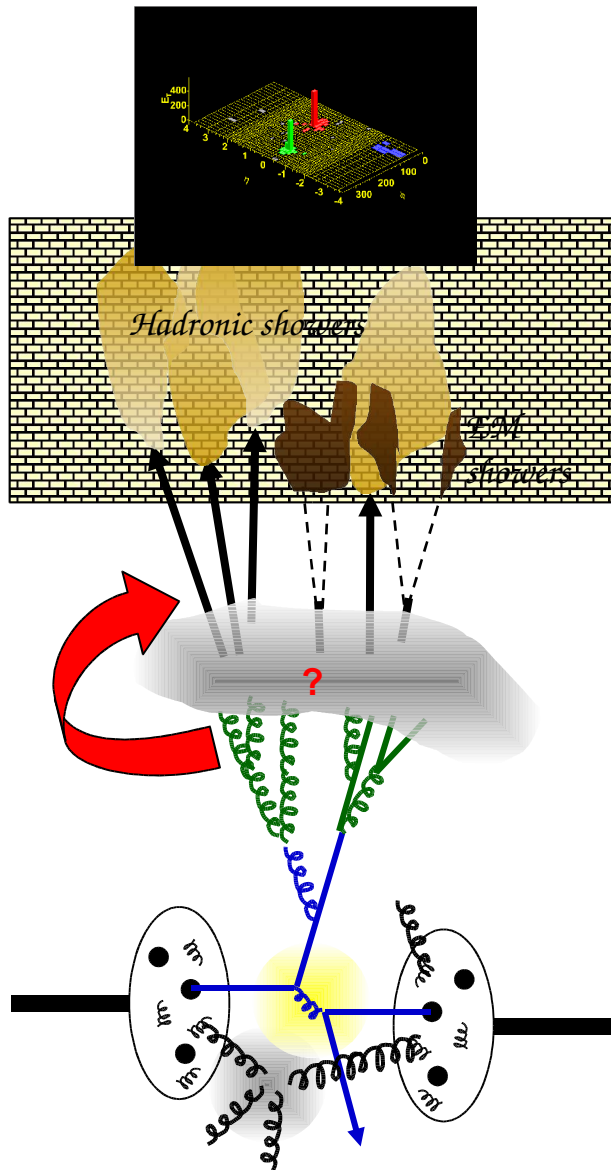
Pheno'06

May 15 – 17, 2006, Madison, WI

Jet fragmentation vs analytical pQCD

- Momentum distribution of particles in jets;
- Multiplicity of charged particles in jets;
including g/q jet differences
- Momentum correlation of particles in jets;
- k_T -distributions of particles in jets;
(k_T -transverse momentum with respect to jet axis)
- Forthcoming results: (not public yet)
→ Global Event Shapes;

Partons, Hadrons, Jets



Pick two partons and their momenta:
-phenomenological parton density functions, PDF

Hard Scattering:

-pQCD exact matrix element at LO, some at NLO,...

Soft final state radiation:

-pQCD approximate resummation in all orders:
LLA (leading log approximation), NLLA

Underlying event:

-phenomenological models

Hadronization:

-phenomenological models

Calorimeter response:

-electromagnetic shower for photons

-hadronic shower for “stable” hadrons

Jet identification:

-jet finding algorithms

Particle momenta and average multiplicity

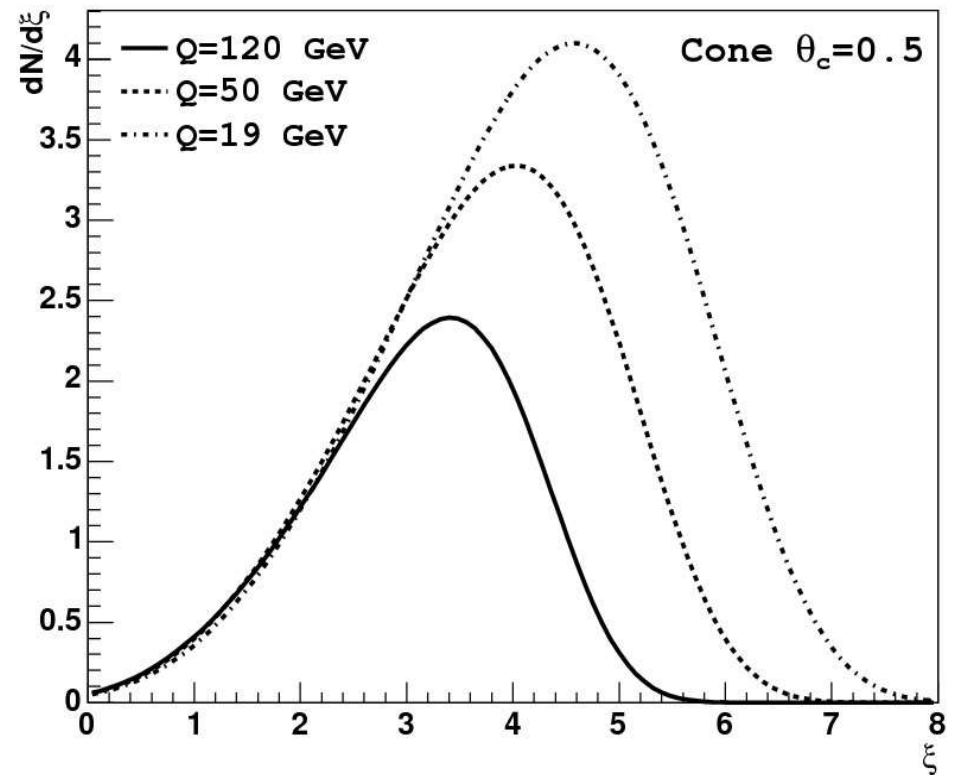
Partons: NLLA resummation

- Mueller (1983)
- Dokshitzer, Troyan (1984)
- Malaza, Webber (1984)
- plus subsequent corrections

$$dN/d\xi = D(Y, \xi)$$

$$\xi = \ln(1/x) = \ln(E_{\text{jet}}/p_{\text{parton}})$$

$$Y = \ln(Q/Q_{\text{eff}}), \quad \begin{aligned} Q &= E_{\text{jet}} \theta_{\text{cone}} \\ Q_{\text{eff}} &= Q_{\text{cutoff}} = \Lambda_{\text{QCD}} \end{aligned}$$



From partons to hadrons: Local Parton-Hadron Duality

- Azimov, Dokshitzer, Khoze, Troyan (1985)

Hadron observables follow patterns predicted for partons

- $N_{\text{hadrons}} \sim N_{\text{partons}} ?$
- Momentum distributions?
- Momentum correlations?
- ...

Particle momenta and average multiplicity

Momentum distribution of charged particles in jets:

- dijet events with well-balanced E_T
- 15-30° cone around dijet axis

Two parameter fit (MLLA+LPHD):

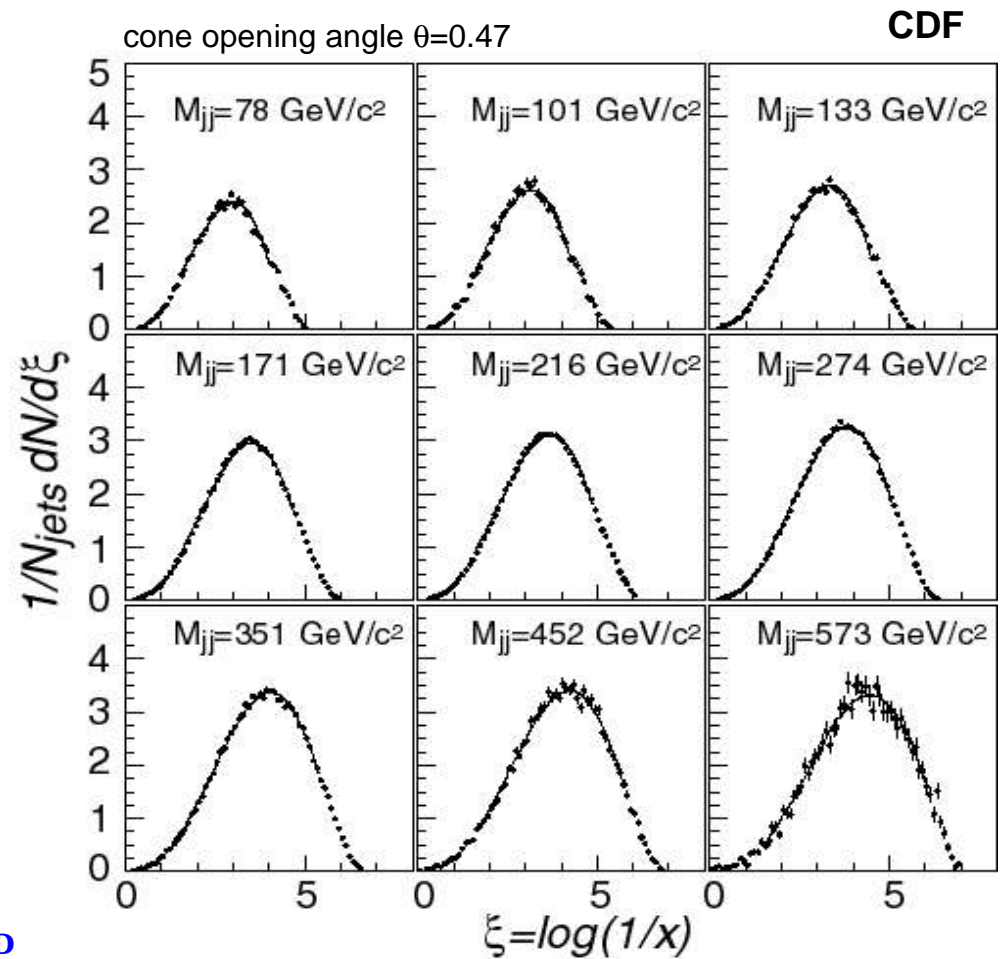
- works surprisingly well in wide range of dijet masses

- MLLA $Q_{\text{eff}} = 230 \pm 40$ MeV

k_T -cutoff can be set as low as Λ_{QCD}

- $K_{\text{LPHD}(\pm)} = 0.56 \pm 0.10$

$$N_{\text{hadrons}} \approx N_{\text{partons}}$$



$$x = \frac{p_{\text{particle}}}{E_{\text{jet}}} \quad \xi = \ln(1/x) = \ln\left(\frac{E_{\text{jet}}}{p_{\text{particle}}}\right)$$

Gluon/Quark Jet Differences

Charged particle multiplicities in gluon and quark jets:

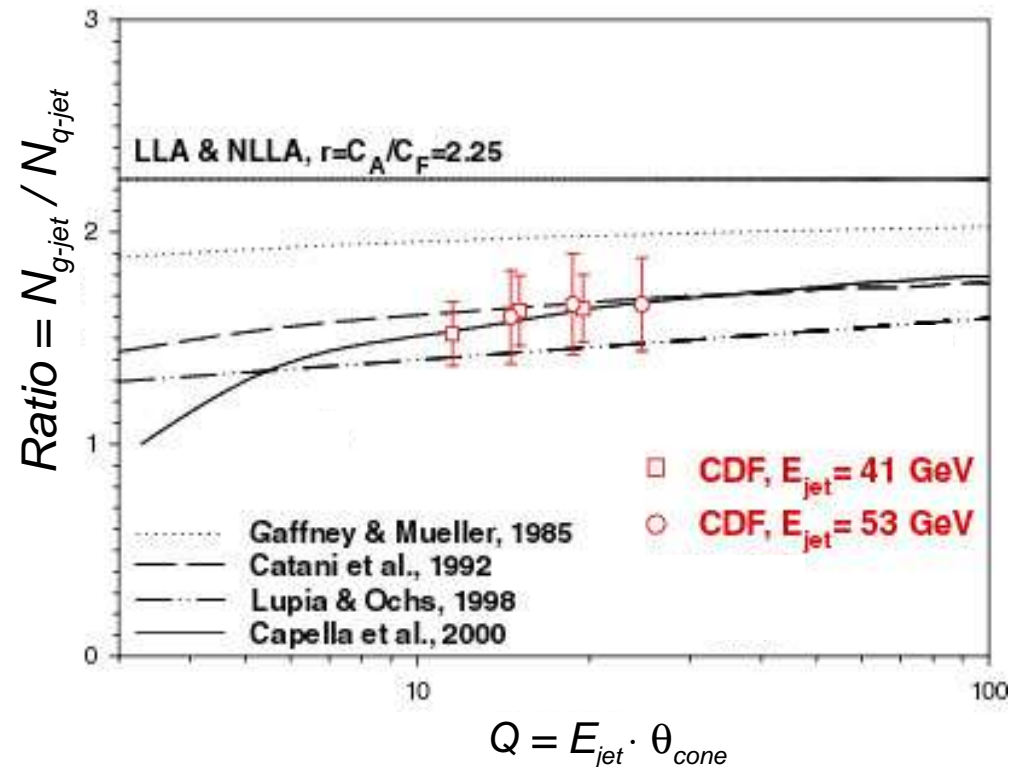
- Measured multiplicities in di-jet and γ -jet events can be resolved for multiplicities in quark and gluon jets;

Results agree with NNLLA:

$$r = 1.64 \pm 0.17 \text{ at } Q = 20 \text{ GeV}$$

Most recent LEP result (OPAL):

$$r = 1.51 \pm 0.04 \text{ at } Q = 90 \text{ GeV}$$



Momentum Correlations

Theory: C.Fong, B.Webber (1990)

- Momentum distributions normalized to # of partons N:

$$R(\xi_1, \xi_2) = \frac{\left(\frac{dN}{d\xi_1 d\xi_2}\right)}{\left(\frac{dN}{d\xi_1}\right)\left(\frac{dN}{\xi_2}\right)} \quad \left. \vphantom{\frac{dN}{d\xi_1 d\xi_2}} \right\} \begin{array}{l} \text{mixes together:} \\ - \text{momentum correlations} \\ - \text{multiplicity fluctuations} \end{array}$$

- To decouple momentum correlations and multiplicity fluctuations effects we used distributions normalized to unity:

$$C(\xi_1, \xi_2) = \frac{\left(\frac{dn}{d\xi_1 d\xi_2}\right)}{\left(\frac{dn}{d\xi_1}\right)\left(\frac{dn}{\xi_2}\right)} = \frac{\langle N \rangle^2}{\langle N(N-1) \rangle} R(\xi_1, \xi_2) = \frac{1}{F} R(\xi_1, \xi_2)$$

where $F = \frac{\langle N(N-1) \rangle}{\langle N \rangle^2}$ - binomial moments taken from theory

Momentum Correlations

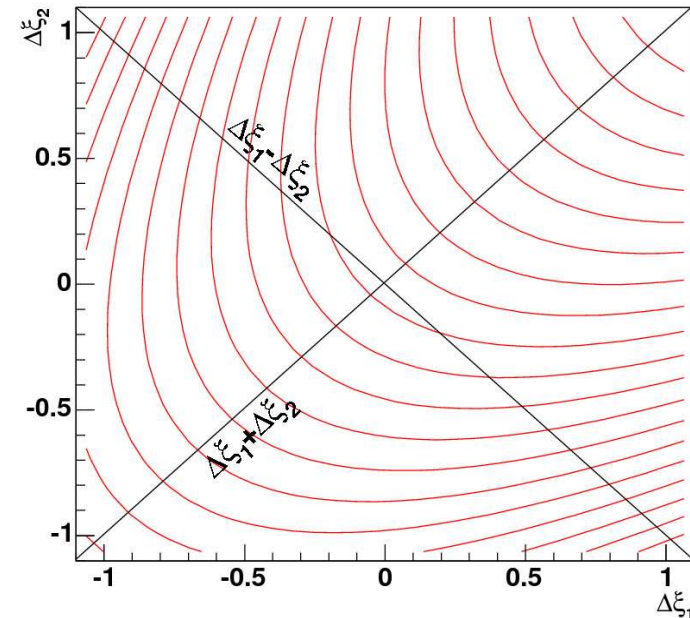
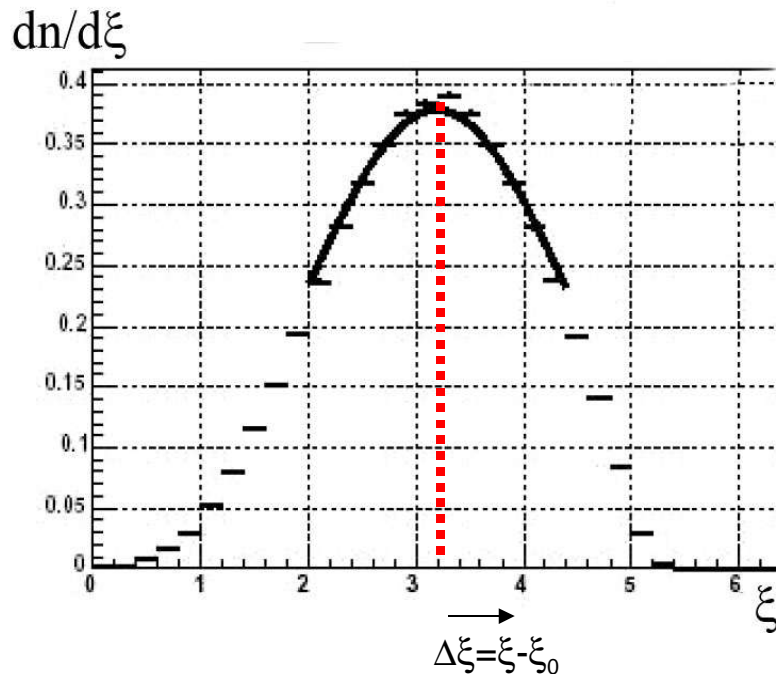
Theory: C.Fong, B.Webber (1990)

- All particles in the cone $\theta_c=0.5$ around jet axis:

Around the peak of inclusive momentum distribution, $C(\xi_1, \xi_2)$ is predicted by NLLA:

$$C(\xi_1, \xi_2) = \frac{\left(\frac{dn}{d\xi_1 d\xi_2} \right)}{\left(\frac{dn}{d\xi_1} \right) \left(\frac{dn}{d\xi_2} \right)} = c_0(E_{jet}) + c_1(E_{jet}) \cdot (\Delta\xi_1 + \Delta\xi_2) + c_2(E_{jet}) \cdot (\Delta\xi_1 - \Delta\xi_2)^2$$

- C_0 , C_1 and C_2 depend on $Y = \ln(E_{jet} \theta_c / Q_{eff})$



Momentum Correlations

Theory: C.Fong, B.Webber (1990)

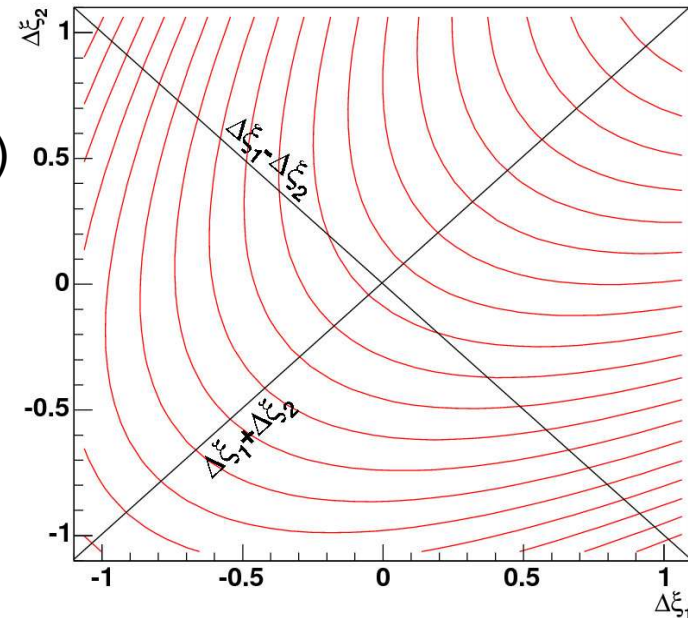
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- C_0 , C_1 and C_2 depend on $Y = \ln(E_{jet} \theta_c / Q_{eff})$

- C_0 is always > 1 ;
(depends on the point of the expansion)
- C_1 is always positive ;
- C_2 is always negative ;



Experimental Features

Measurement:

- Well balanced di-jet events with M_{jj} ranging 60-600 GeV;
- Jet axis in the central region $|\eta| < 0.9$;
- Events with only one vertex;
- Measurement done in the dijet center-of-mass frame;
- Cone jet algorithm with $R=1.0$;

- Charged particles in the cone with $\theta_c = 0.5$;
- Unfold the small underlying event contribution;
- Remove secondaries (conversions,)

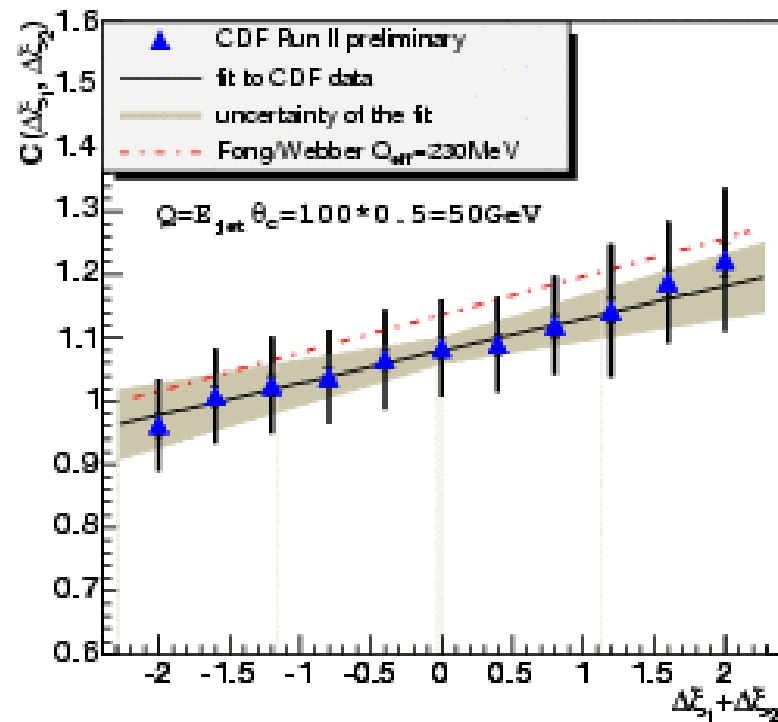
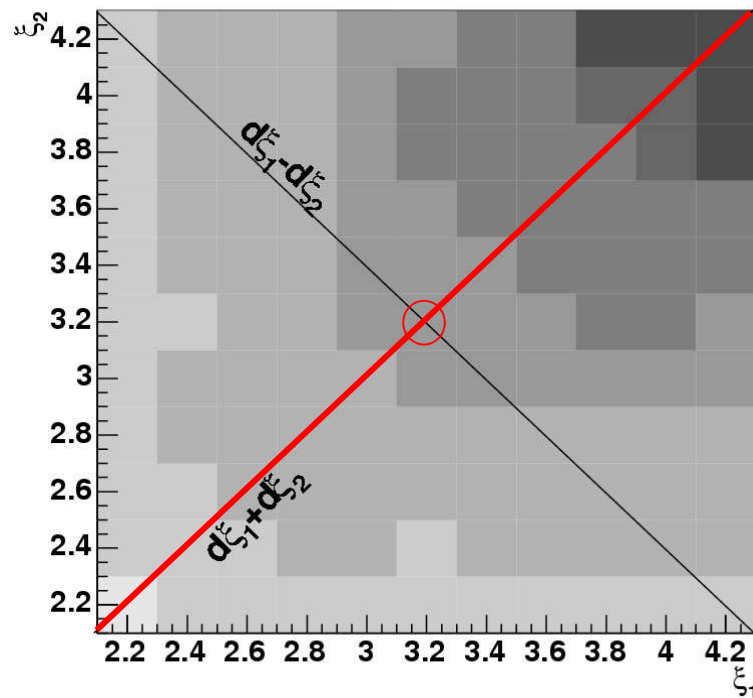
Theory(to make compare to data):

- produce correlation function for a mixture of quark and gluon jets;
- get fraction of gluon jets in the sample from Pythia Tune A Monte-Carlo;

Momentum Correlations

- Hadron correlations follow the pattern expected for partons;

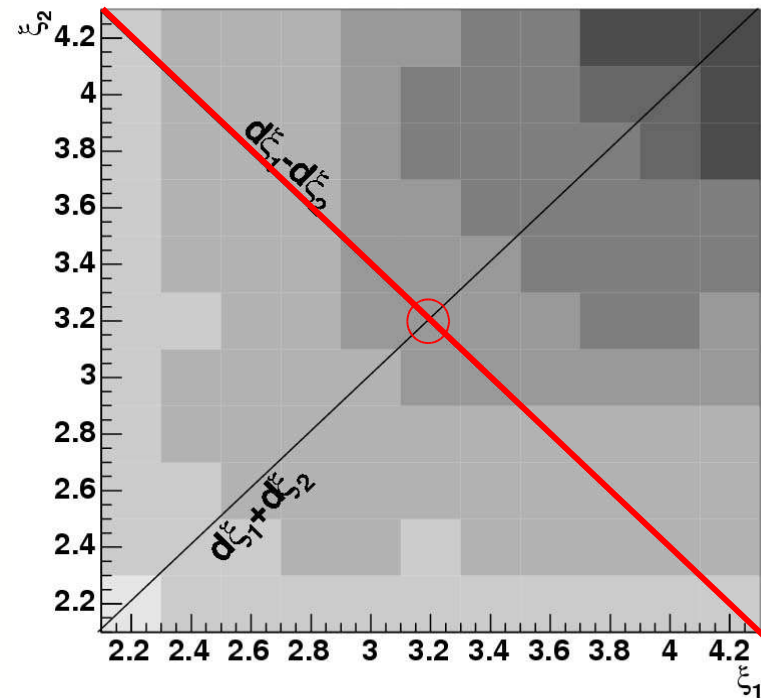
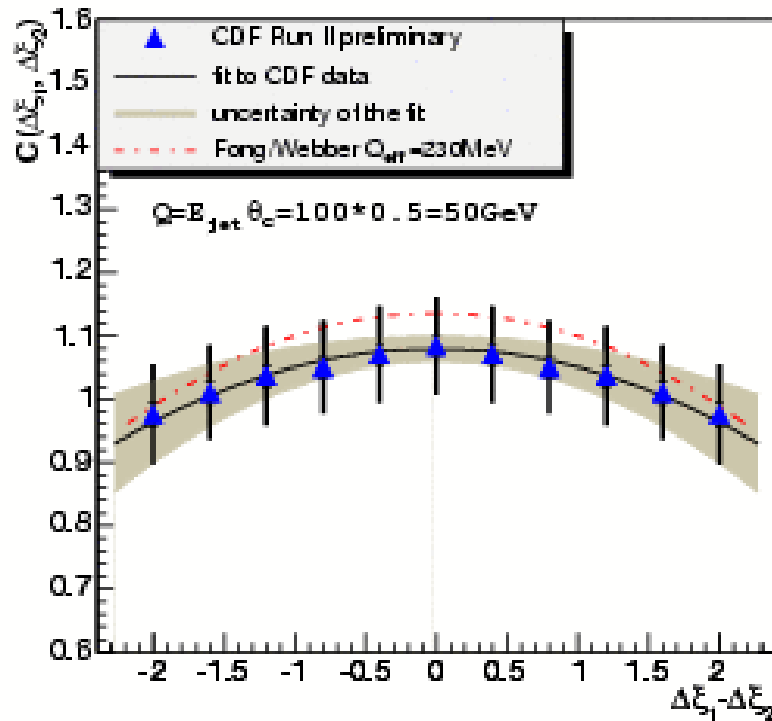
$$C(\xi_1, \xi_2) = c_0(E_{jet}) + c_1(E_{jet}) \cdot (\Delta\xi_1 + \Delta\xi_2) + c_2(E_{jet}) \cdot (\Delta\xi_1 - \Delta\xi_2)^2$$



Momentum Correlations

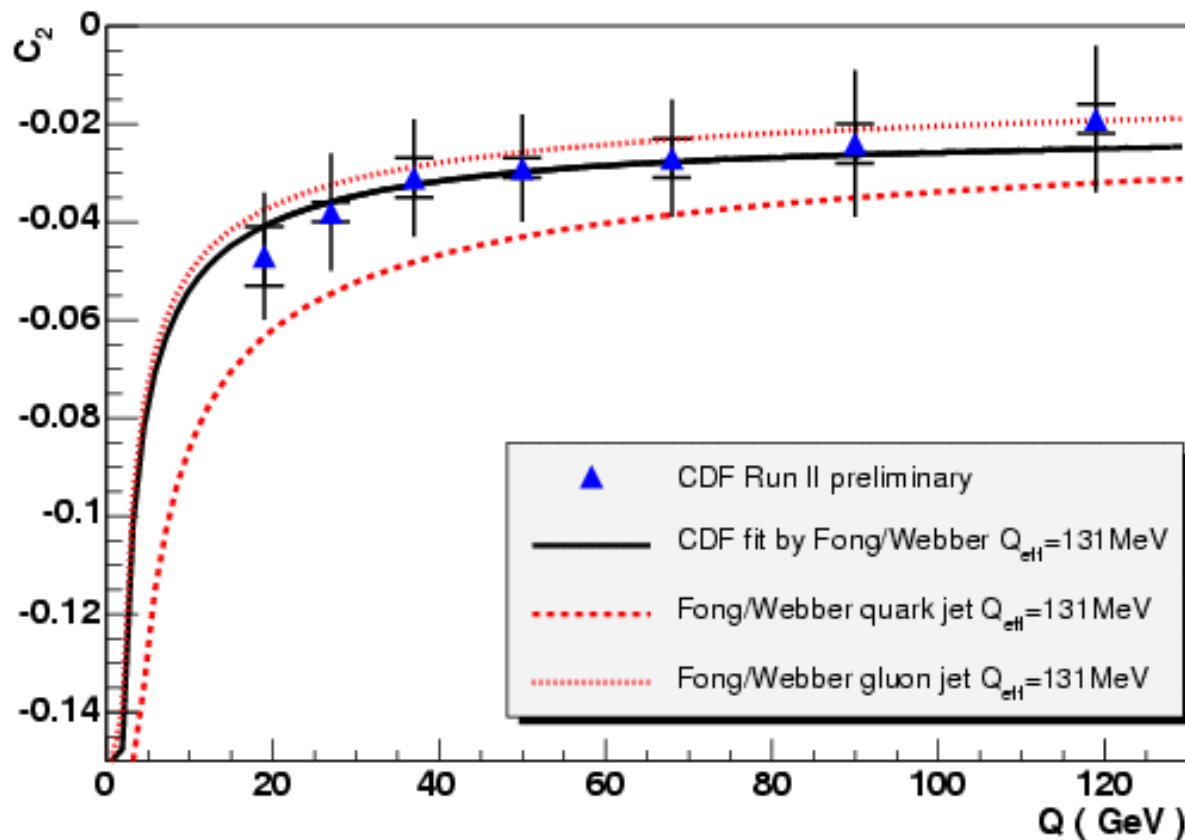
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$$C(\xi_1, \xi_2) = c_0(E_{jet}) + c_1(E_{jet}) (\Delta\xi_1 + \Delta\xi_2) + c_2(E_{jet}) \cdot (\Delta\xi_1 - \Delta\xi_2)^2$$



Momentum Correlations

- Fit C_2 vs. Q gives $Q_{\text{eff}} \sim 130 \pm 80$ MeV;
- Data and theory show same trends;



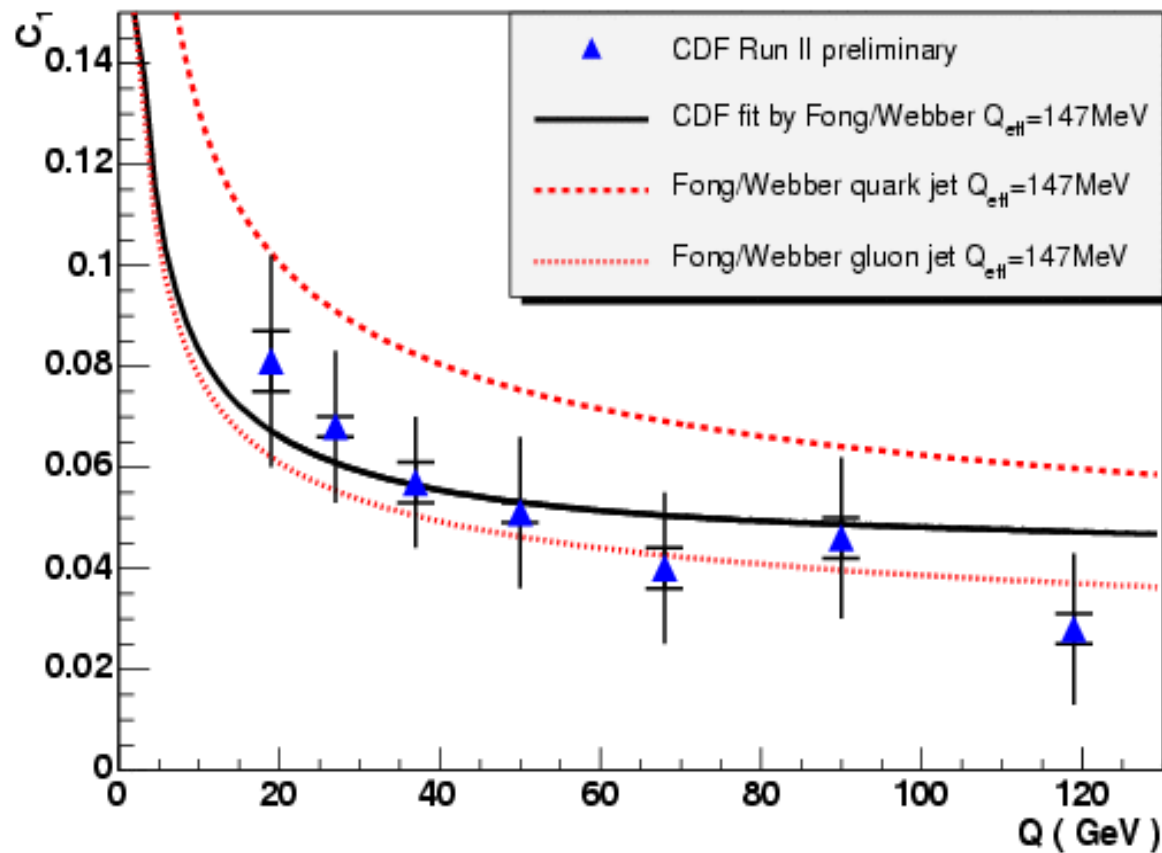
$$c_2 = -\frac{a_2}{Y^2} + \dots$$

$$Y = \ln \left(\frac{E_{jet} \theta_{cone}}{Q_{eff}} \right)$$

← mixed q/g jets

Momentum Correlations

- Fit C_1 vs. Q gives $Q_{\text{eff}} \sim 150 \pm 80$ MeV;
- Data and theory show same trends;



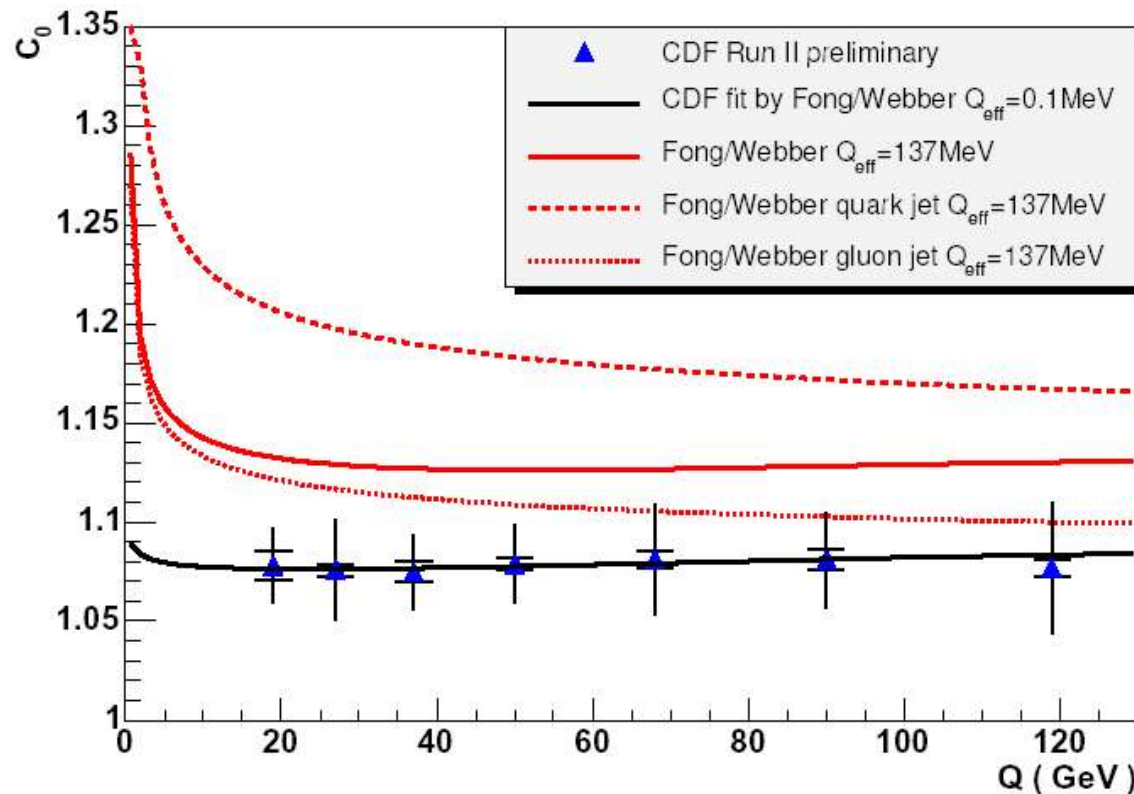
← mixed q/g jets

$$C_1 = \frac{a_1}{Y^{1.5}} + \dots$$

$$Y = \ln \left(\frac{E_{\text{jet}} \theta_{\text{cone}}}{Q_{\text{eff}}} \right)$$

Momentum Correlations

- C_0 is too small if compared to theory;
- However, it's almost independent of energy, as expected;
- Theoretically, this parameter has some issues...



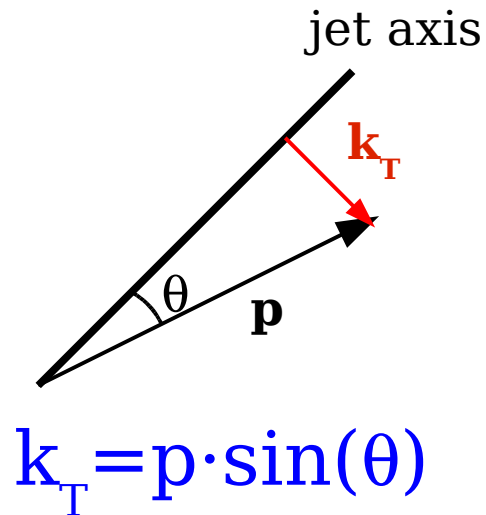
$$c_0 = 1 + \Delta - \frac{a_0}{\sqrt{Y}} + \dots$$

$$Y = \ln \left(\frac{E_{jet} \theta_{cone}}{Q_{eff}} \right)$$

Kt distributions

R.Perez-Ramoz & B.Machet (2006)

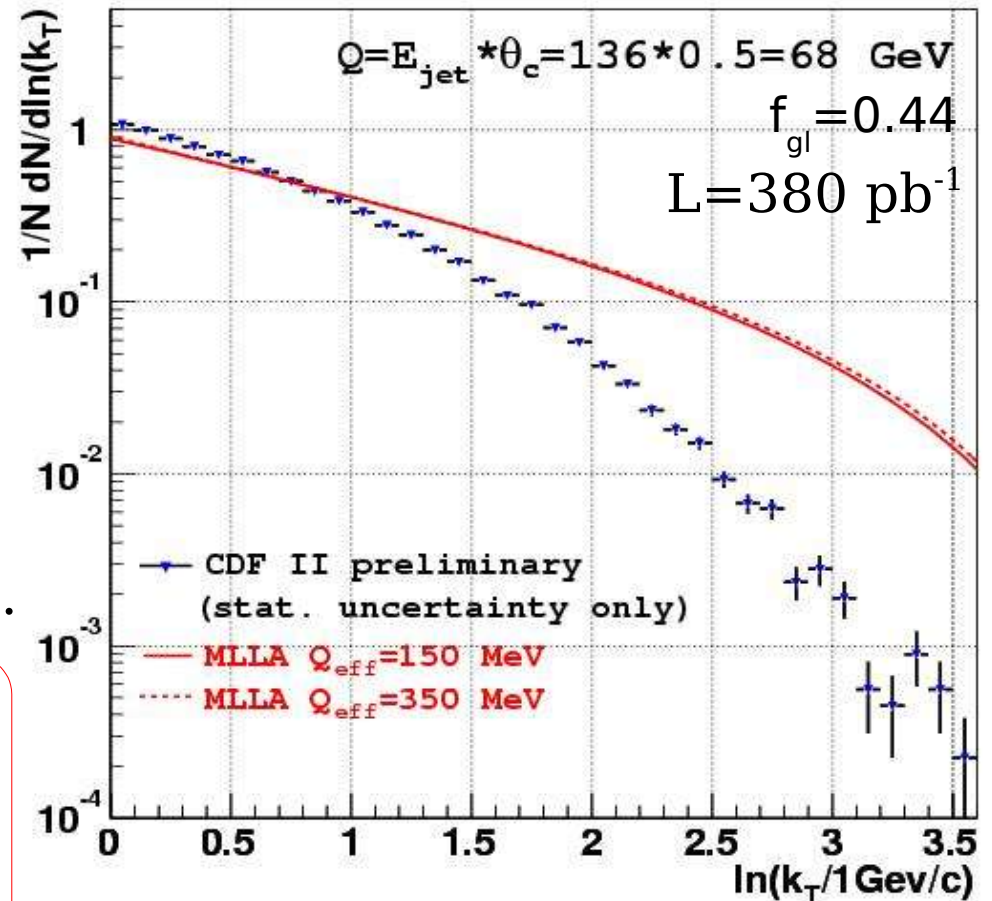
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In theory $dN/d\ln(k_T)$ are produced.

- Theory predicts more particles with high K_t

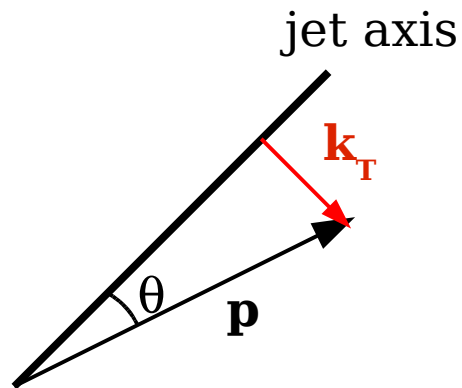
Distributions are normalized to unity



Kt distributions

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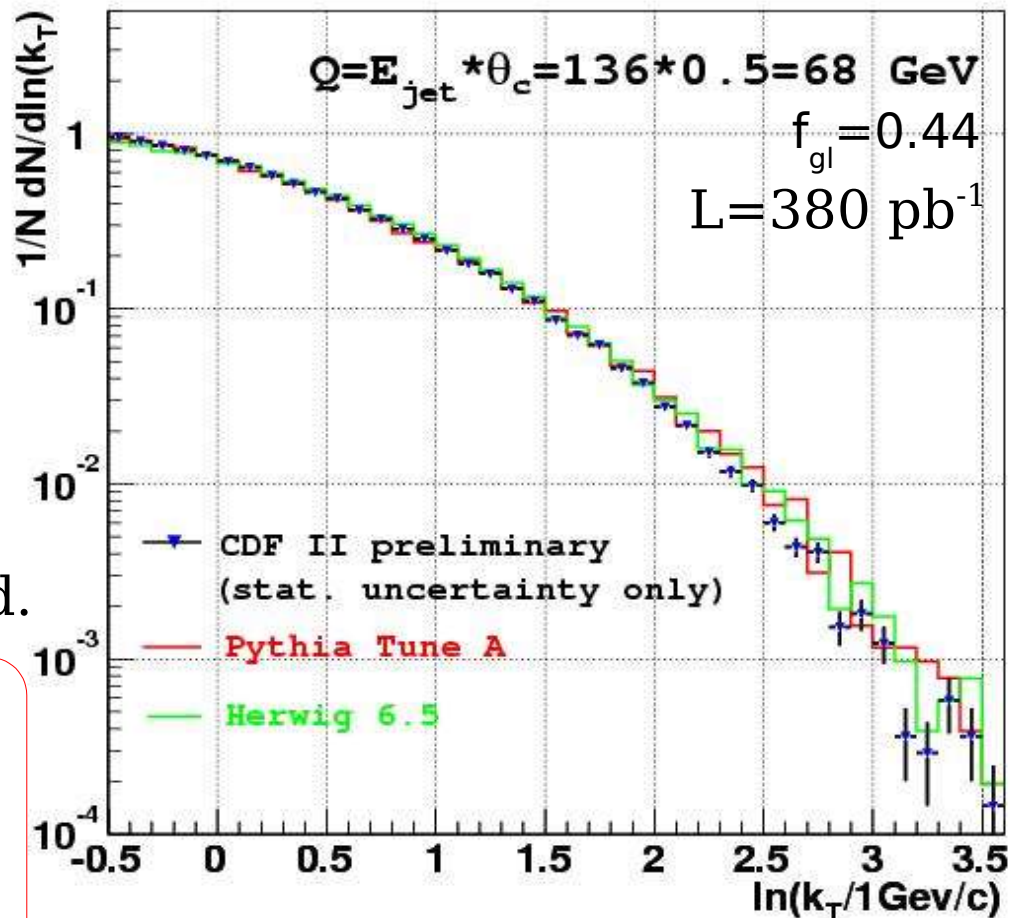


$$k_T = p \cdot \sin(\theta)$$

In theory $dN/d\ln(k_T)$ are produced.

- Theory predicts more particles with high K_t
- Data and MC are in agreement

Distributions are normalized to unity



Summary

Momentum distributions of particles in jets:

- Consistent with parton distribution predicted by MLLA;
- $Q_{\text{eff}} = 240 \pm 40$ MeV over the entire range of dijet masses;

Multiplicity of particles in jets:

- $N_{\text{hadrons}} = K_{\text{LPHD}} \cdot N_{\text{partons}}$
- $K_{\text{LPHD}} = 0.56 \pm 0.10$ for charged particles;
- Ratio of multiplicities in g/q jets $r = 1.6 \pm 0.2$;

Momentum correlations:

- Hadron correlations follow the pattern expected for partons;
- The constant term is much smaller than predicted by pQCD...;
- $Q_{\text{eff}} = 140 \pm 80$ MeV from linear and parabolic terms;

Kt distributions:

- Less hard particles than predicted by MLLA;
- Very good agreement between data and Monte-Carlo ;

Forthcoming results:

- Event shapes;

Backup

CDF results

Pythia Tune A and Herwig 6.5

- Both MC generators reproduce correlation in data fairly well;

