

*Perturbative QCD for collider physics:
recent developments*

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May 2006

PHENO 2006, Madison, WI

Outline

- Introduction
 - Challenges at the LHC
- All orders/leading order
 - Showers and matrix elements
 - CKKW: harder showers
- NLO:
 - examples and problems
 - Higgs production with $b\bar{b}$: choose the right scale
 - no sbottoms in $p\bar{p} \rightarrow B + X$
 - MC@NLO
- NNLO
 - PDFs
 - Z, W production
 - Higgs production at the LHC
 - Higgs coupling extractions
- Conclusions

Introduction: challenges

- In about a year, LHC begins its first physics run offering unprecedented opportunities.
- Two distinct features: **high luminosity and high energy**.
- Enormous rates for SM processes; can be used to study SM; have to be understood since are backgrounds to New Physics.
- Factorization theorem

$$\sigma^{\mathcal{O}} = D_k^{\mathcal{O}} \otimes \sigma_{kj} \otimes F_j.$$

- F_j describes hadron-parton transition \rightarrow Data;
 - σ_{kj} describes parton-parton transition \rightarrow pQCD;
 - D_k describes “fragmentation” \rightarrow models, data, etc.
- **pQCD is central for hadron collider phenomenology.**

Introduction: challenges

- extraction of parton distribution functions
 - reliability
 - precision
- shower event generators
 - harder showers
 - combining with fixed order computations
 - hadronization models
- resummations
 - analytic resummations; numeric resummations
- NLO computations
 - higher multiplicity processes
- NNLO computations
 - general algorithms for NNLO calculations
 - NNLO phenomenology

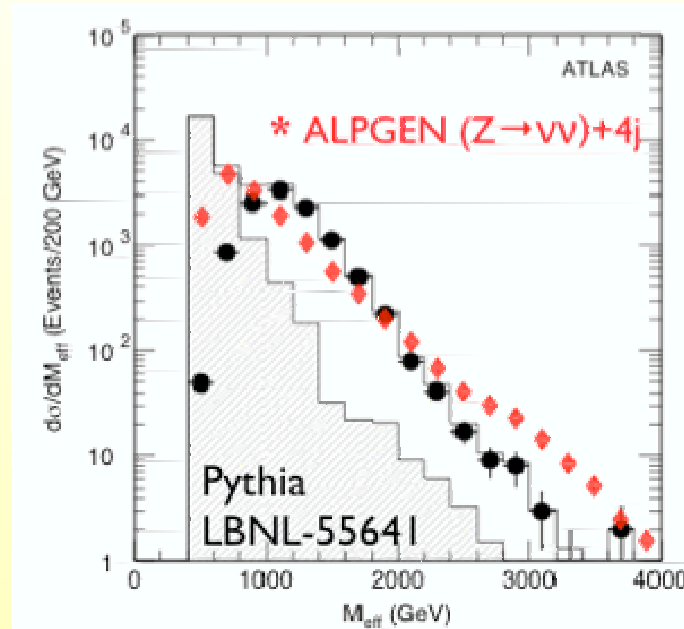
All orders/leading order

- $pp \rightarrow N \text{ jets} + X$, $N \leq 10$ is a typical background process at the LHC.
- To deal with these multi-jet processes, we use all-purpose shower event generators, e.g. PYTHIA, HERWIG. **Are these descriptions accurate?**
- Showers are based on **collinear emissions**.
- Collinear emissions are independent \Rightarrow probabilistic description.
- Showers are good for processes dominated by soft/collinear radiation.
- Showers generate large transverse momenta by emissions of many jets with moderate p_{\perp} $\Rightarrow \alpha_s$ suppression of high p_{\perp} radiation.
- Showers do not change normalizations of total cross-sections

$$\int d\sigma_{\text{LO}} \times \text{MC} = \sigma_{\text{LO}}.$$

- **An alternative:** exact matrix elements for $ij \rightarrow N \text{ jets}$. How do these things compare?

All orders/leading order

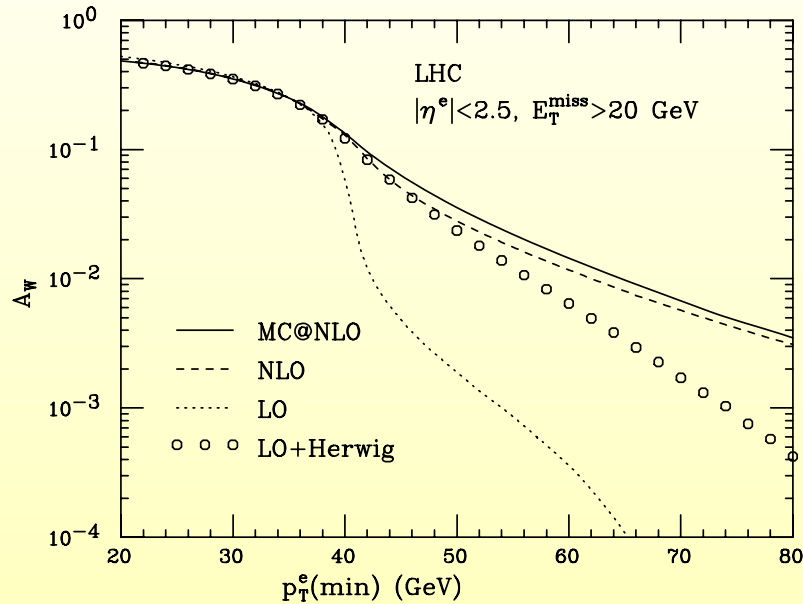


$$M_{\text{eff}} = \sum_{\text{jets}} p_{\perp} + E_{\perp}^{\text{miss}}$$

Mangano

- ALPGEN: exact matrix elements; correct hard emissions built in.
- PYTHIA: emulates hard emissions by producing large number of softer jets.
- **PYTHIA underestimates the background significantly.**

All orders/leading order



Acceptances for $pp \rightarrow W^- \rightarrow e\bar{\nu}$.

$$A_W = \frac{1}{\sigma_{\text{tot}}} \int_{p_{\perp}^{e,\text{min}}} dp_{\perp}^e \frac{d\sigma}{dp_{\perp}^e}.$$

Mangano, Frixione

- NLO is just LO ($pp \rightarrow W + \text{jet} \rightarrow e\bar{\nu} + \text{jet}$) for $p_{\perp}^{e,\text{min}} > m_W/2$.

$$\frac{A_W[\text{NLO}]}{A_W[\text{HERWIG}]} \sim 2 - 10, \quad \text{for } p_{\perp}^{e,\text{min}} > 50 \text{ GeV}.$$

All orders/leading order: CKKW

- An $N + 1$ -jet event is obtained from an N -jet event either by
large angle hard emission or shower.
- Event generators can do a better job for multi-jet processes if both mechanisms are taken into account.
- Catani-Krauss-Kuhn-Webber (CKKW) procedure:
 - calculate $pp \rightarrow m$ HARD jets, with $m < N$. Determine probability of an event with m hard jets using the cross-section values,

$$P_m = \frac{\sigma_m}{\sigma_0 + \sigma_1 + \sigma_2 + \dots + \sigma_N}, \quad \sigma_m = \sigma_m(y_{\text{cut}}).$$

- Generate hard jet configuration according to the probability distribution; shower it.
 - Requires introduction of a measure to distinguish between hard jet and shower jet.
- This procedure is being currently implemented in major shower event generators, such as PYTHIA and HERWIG.

Mrenna, Richardson

Leading order: uncertainties

- Any leading order prediction has the renormalization and factorization scales uncertainty.
- $pp \rightarrow \nu\bar{\nu} + N \text{ jets}; p_{\perp}^j > 80 \text{ GeV}; |\eta| < 2.5.$
- $\mu = \sqrt{M_z^2 + \sum_{\text{jets}} p_{\perp}^2}; \mu_r = \mu_f = \mu/2 \dots 2\mu.$

N	$\sigma(2\mu)\text{pb}$	$\sigma(\mu/2)\text{pb}$	variation
1	182	216	17%
2	47.1	75.4	46%
3	6.47	13.52	70%
4	0.90	2.48	93%

Next-to-leading order computations are necessary.

Next-to-leading order

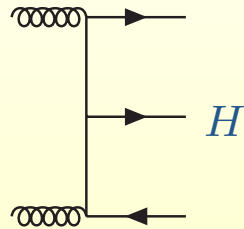
- The NLO prediction is often the **first quantitative prediction**.
- Typical background $(t\bar{t})^n (WZ)^m \text{ jets}^l$, $n, m, l > 0$.
- Current state of the art is $2 \rightarrow 3$ processes:
 - NLOJET++ [Nagy] $pp \rightarrow (2, 3)j$, $ep \rightarrow 3j$, $e^+e^- \rightarrow 3, 4j$, $\gamma^*p \rightarrow (2, 3)j$;
 - AYLEN/EMILIA [de Florian, Dixon, Kunszt, Signer] $pp \rightarrow (W, Z) + (W, Z, \gamma)$;
 - MCFM [Campbell, Ellis] $pp \rightarrow (W, Z) + (0, 1, 2)j$, $pp \rightarrow (W, Z) + b\bar{b}$;
 - DIPHOX/EPHOX [Aurinche et. al] $pp \rightarrow \gamma + 1j$, $pp \rightarrow \gamma\gamma$, $\gamma^*p \rightarrow \gamma + 1j$;
 - VBFNLO [Figy, Zeppenfeld, Oleari] $pp \rightarrow (W, Z, H) + 2j$.
- Flexible programs: arbitrary restrictions on the final state can be applied.
- We want to extend the NLO computations to $2 \rightarrow 4, 5$, etc. processes.
- Problem: one-loop $5, 6, 7 \dots n$ -point functions.
 - Direct numerical integration is not possible because those functions have soft and collinear divergences.
 - Simplifications of many-point functions produce fictitious singularities that are hard to handle.

Next-to-leading order

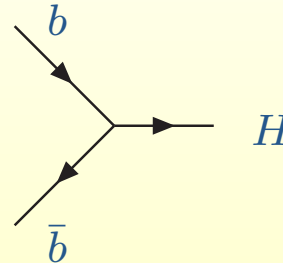
- Recent progress (technical):
 - Mellin-Barnes transform Anastasiou, Daleo;
 - IBP's, sector decomposition, numerics Binoth, Heinrich;
 - Numerical solutions of IBP's Glover, Giele;
 - Bernstein-Tkachov theorem Passarino et al.;
 - Integration in momentum space Soper, Krämer.
- Recent progress (calculations):
 - $pp \rightarrow H \rightarrow 2$ jets (virtual), Zanderighi, Giele, Ellis;
 - $pp \rightarrow t \rightarrow Wb$, Ellis, Campbell;
 - $pp \rightarrow Hb\bar{b}, Ht\bar{t}$, Dawson, Jackson, Wackerroth, Reina, Spira, Krämer;
 - $pp \rightarrow W^+W^-(ZZ) + 2j$, [VBF] Jäger, Oleari, Zeppenfeld.
- **First complete $2 \rightarrow 4$ computation:** $e^+e^- \rightarrow 4$ fermions, Denner, Dittmaier et al.
- **Flexible methods are needed; must be easily adaptable to New Physics models.**

Next-to-leading order

- Consider Higgs production in association with b quarks. Two options:



$$\text{PT in } \frac{\alpha_s}{\pi} \ln(m_H^2/m_b^2)$$

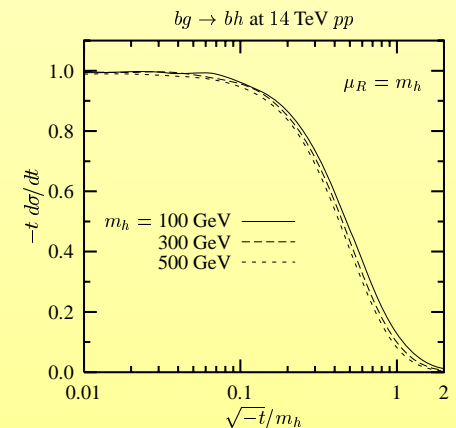
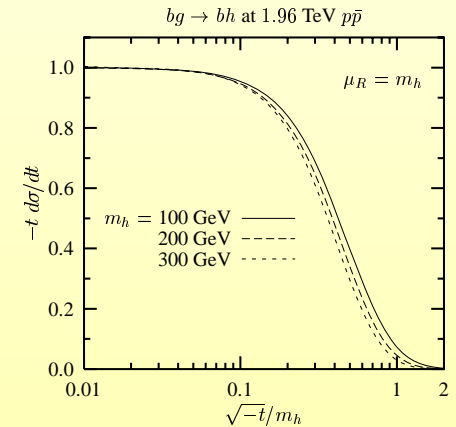


$$\text{PT in } \frac{\alpha_s}{\pi}$$

- Puzzle: $\sigma_{\text{LO}}(gg \rightarrow b\bar{b}H) \sim 0.1 \sigma_{\text{LO}}(b\bar{b} \rightarrow H)$.
- Resolution: $\mu_F = m_H/4$ is an appropriate scale (kinematics).

Willenbrock, Maltoni, Plehn, Boos

- This prediction is confirmed by explicit (later) higher order calculations.



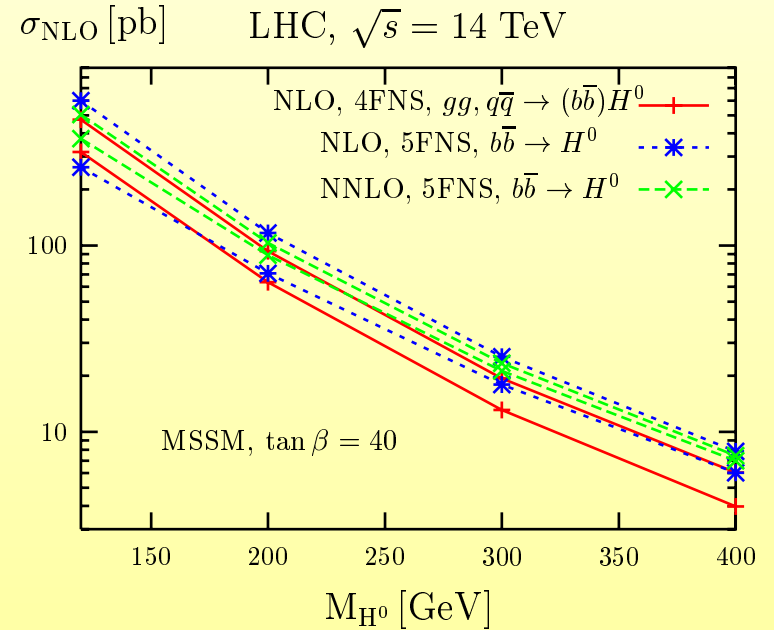
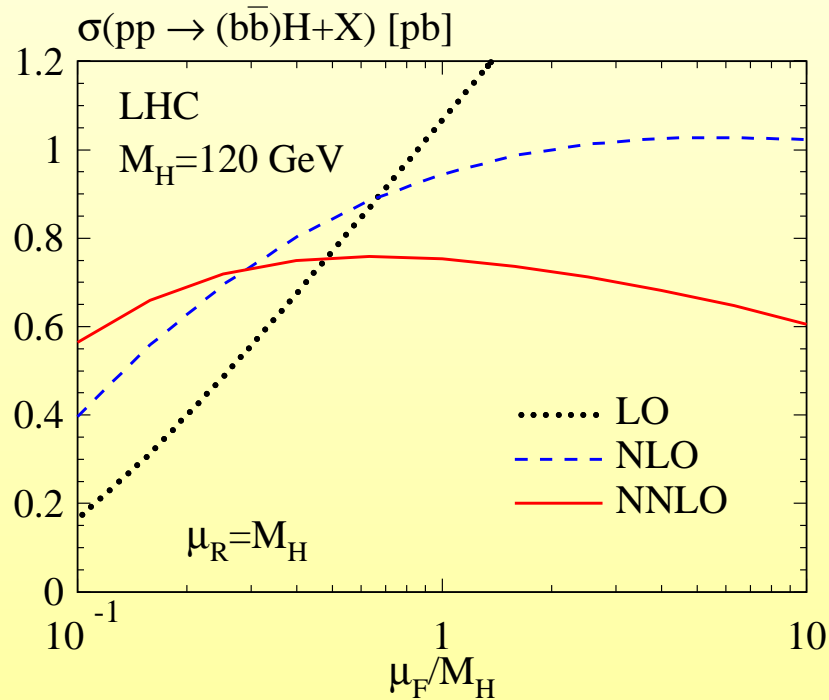
Next-to-leading order

- $b\bar{b} \rightarrow H$ is currently known through NNLO; $\mu_F = m_H/4$ is the right scale!

Harlander, Kilgore

- $gg \rightarrow b\bar{b}H$ is currently known through NLO; compares well with $b\bar{b} \rightarrow H$.

Dawson, Jackson, Reina, Wackerroth, Krämer, Spira



- Gain confidence from looking at the same process in different ways.

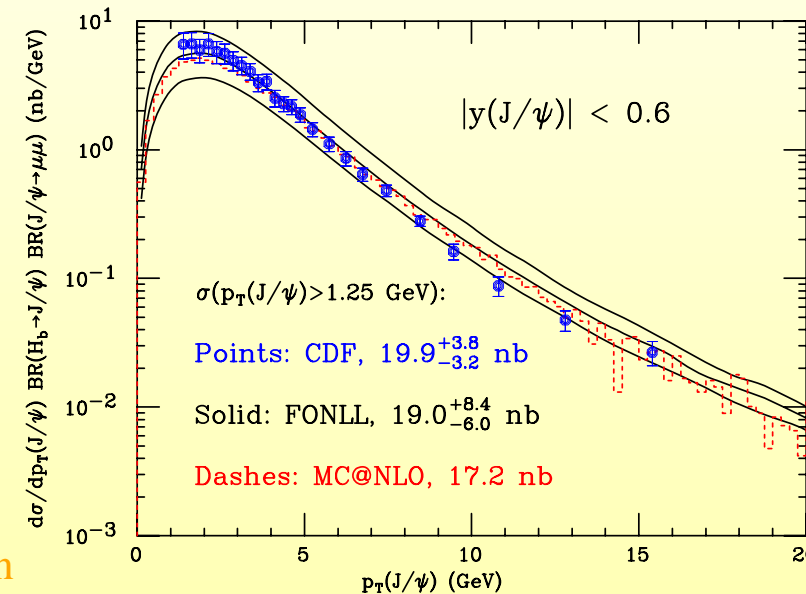
NLO: bottom production

- Bottom production in hadron collisions: $p\bar{p} \rightarrow B + X$ was a long-standing problem for pQCD with discrepancy often quoted as a **factor 2-4**
- New Physics explanations, e.g. light gluinos, sbottoms

NLO QCD prediction for p_{\perp}^B is non-trivial:

- $b \rightarrow B$ fragmentation function;
- large uncertainties due to PDFs;
- large NLO QCD corrections;
- σ_{tot} is dominated by $p_{\perp} \sim m_b$.

Cacciari, Nason



- Excellent agreement of the total cross-sections

Cacciari et al.

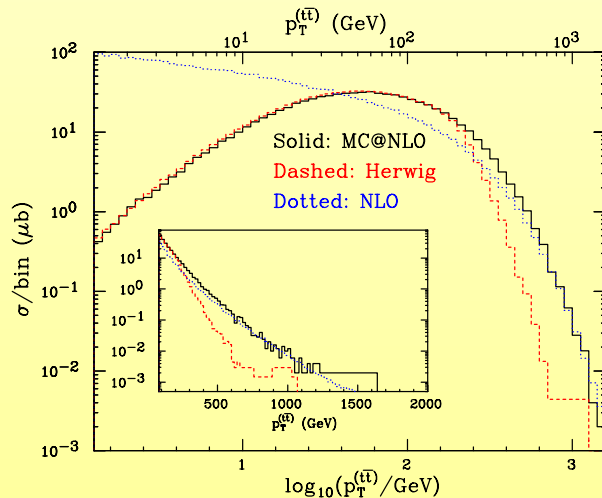
$$\sigma_{J/\psi}^{\text{CDF}} = 19.9^{+3.8}_{-3.2} \text{ nb}, \quad \sigma_{J/\psi}^{\text{pQCD}} = 19.0^{+8.4}_{-6.0} \text{ nb}.$$

- Large $\pm 50\%$ theory uncertainty remains.

Event generators and higher orders

- Shower event generators and perturbative calculations **are complimentary**:
 - **Showers**: universal, realistic jets, automatic resummations, hadronization;
 - **PT**: correct rates, correct description of hard emissions, improvable errors.
- **Combining MC's and perturbative computations is a good (old) idea** Dobbs
- The **most advanced** implementation is called MC@NLO (based on HERWIG shower): Frixione, Webber

$$\text{MC@NLO} = \text{MC} (1 + \alpha_s [\text{NLO} - \text{MC}_{\alpha_s}]) .$$



Features:

outputs unweighted events;
no double counting;
total rates are accurate through NLO.

Processes included:

H , W , Z , VV , HZ , $t\bar{t}$, $b\bar{b}$ and single top.

Alternative implementations would be most useful Krämer, Nagy, Soper

NNLO

- NNLO calculations are desirable for:
 - processes where good estimate of the uncertainty is required;
 - processes with large NLO corrections.
- This leaves us with $H, W, Z, 2$ jets, heavy quarks.
- What is known through NNLO for hadron colliders:
 - $W, Z, gg \rightarrow H, gg \rightarrow A, b\bar{b} \rightarrow H$ production; total cross-sections;
van Neerven, Matsuura, Kilgore, Harlander, Anastasiou, K.M., Ravindran, Smith
 - W, Z, γ^* rapidity distribution;
Anastasiou, Dixon, K.M., Petriello
 - $gg \rightarrow H, Z, W$ production, fully differential with spin correlations;
Anastasiou, K.M., Petriello
- Generalization to $2 \rightarrow 2$ processes (jets, heavy quarks) is highly non-trivial.

NNLO: PDFs

- A consistent implementation of NNLO calculations requires NNLO PDFs and NNLO evolution kernels.
- NNLO Altarelli-Parisi splitting kernels known. Vermaseren, Moch, Vogt
- NNLO PDFs extractions exist. MRST, Alekhin.
- Broad measure of PDFs fits reliability:

$$\alpha_s^{\text{Alekhin}}(M_Z) = 0.114(1), \quad \alpha_s^T(M_Z) = 0.121(1).$$

NNLO effects increase the disagreement.

- For hard processes at the LHC, PDF uncertainty is

$$\frac{\delta\sigma}{\sigma} \approx 5\%, \quad M \sim 100 \text{ GeV}, \quad |Y| < 2.$$

- For larger $|Y|$, $\ln(1/x)$ terms may require resummations (BFKL, saturation)

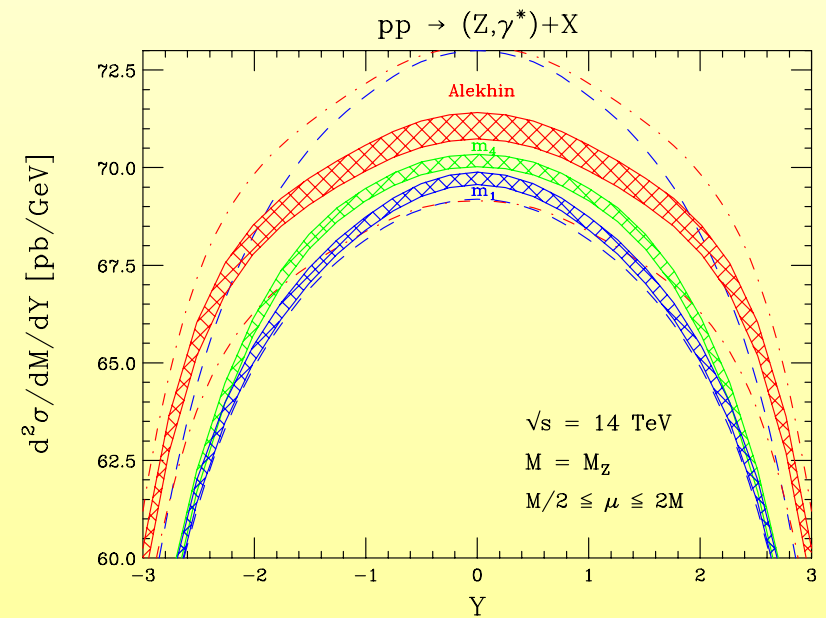
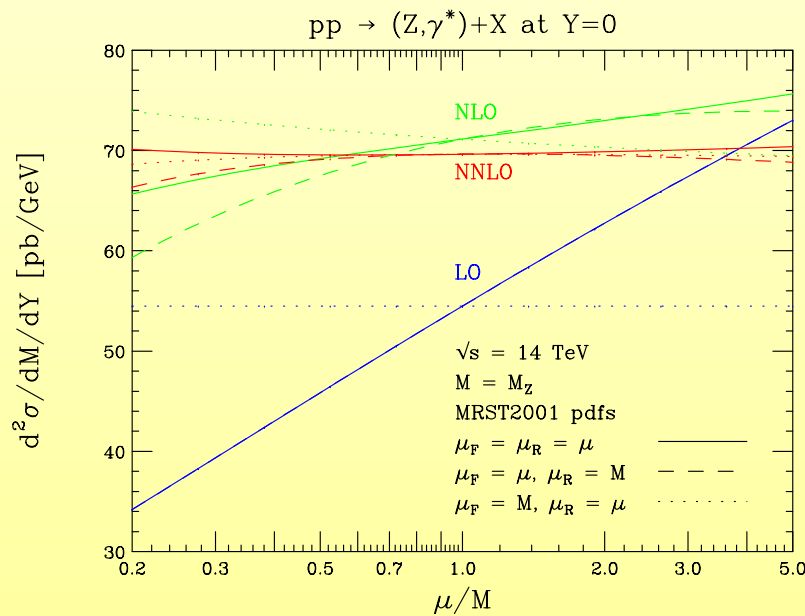
NNLO: Z and W production

- Use the Z, W production to measure L .
- Partonic luminosities \leftrightarrow rapidity of gauge bosons

Dittmar et al.

$$\frac{d\sigma}{dM dY} \sim q_1(x_1)q_2(x_2), \quad x_{1,2} = \frac{M}{\sqrt{S}} e^{\pm Y}.$$

- NNLO results: scale stability and PDF sensitivity



Anastasiou, Dixon, Petriello, K.M.

NNLO: W^- production

- The knowledge of rapidity distributions of Z, W bosons is insufficient for deriving lepton distributions because of spin correlations.
- The fully differential NNLO QCD calculation for $pp \rightarrow e + \bar{\nu} + X$ is now available. Cuts of the form (ATLAS, CMS)

$$\text{Cut1 } p_{\perp}^e > 20 \text{ GeV}, \quad |\eta_e| < 2.5, \quad E_{\text{miss}} > 20 \text{ GeV}$$

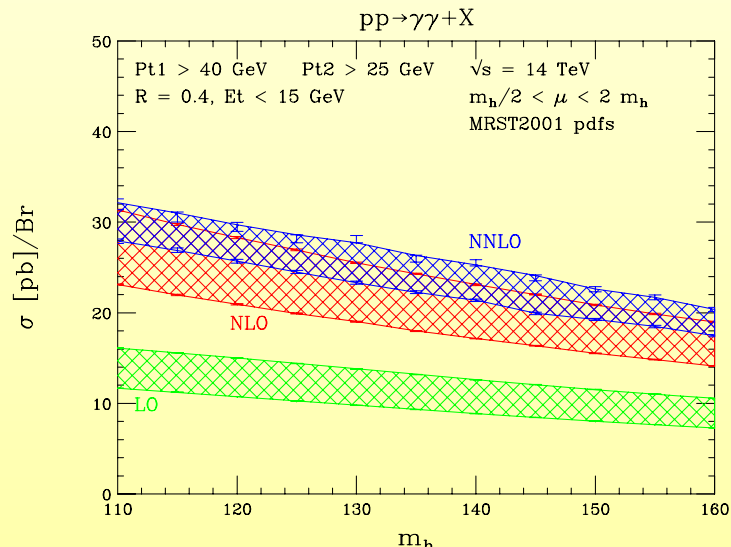
$$\text{Cut2 } p_{\perp}^e > 40 \text{ GeV}, \quad |\eta_e| < 2.5, \quad E_{\text{miss}} > 40 \text{ GeV}$$

LHC	A(MC@NLO)	$\frac{\sigma_{\text{MC@NLO}}}{\sigma_{\text{NLO}}}$	A(NNLO)	$\frac{\sigma_{\text{NNLO}}}{\sigma_{\text{NLO}}}$
Cut1	0.485	1.02	0.492	0.983
Cut2	0.133	1.03	0.155	1.21

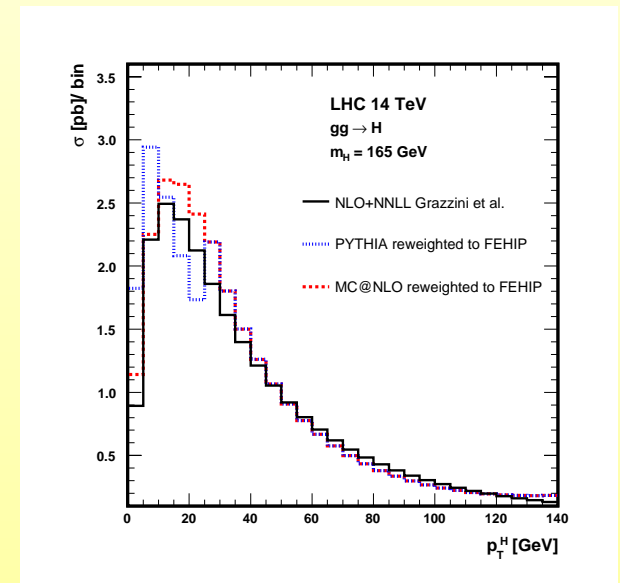
- 1 – 2 percent NNLO effects for $p_{\perp}^{e,\text{min}} > 20 - 30 \text{ GeV}$;
10 – 20 percent NNLO effects for $p_{\perp}^{e,\text{min}} > 40 - 50 \text{ GeV}$. Petriello, K.M.
- For Cut2, MC@NLO gets the acceptance wrong since second hard emission is important.

NNLO: Higgs boson signal at the LHC

- QCD effects increase the inclusive $gg \rightarrow H$ production cross-section by a factor **two**.
- For $H \rightarrow \gamma\gamma$, the following cuts on the final photons are imposed (ATLAS,CMS):
 - $p_{\perp}^{(1)} \geq 25 \text{ GeV}, p_{\perp}^{(2)} \geq 40 \text{ GeV}, |\eta_{1,2}| \leq 2.5$.
 - Isolation cuts, e.g. $E_{T,\text{hadr}} \leq 15 \text{ GeV}, \delta R = \sqrt{\delta\eta^2 + \delta\phi^2} < 0.4$.
- **Do the conclusions based on inclusive calculations change when those cuts are imposed?**



C. Anastasiou, K.M., F. Petriello



Re-weighting MC@NLO and PYTHIA to double differential distribution in Higgs p_{\perp} and rapidity. [Davatz et al.]

Higgs coupling extractions

- Analyses of Higgs coupling use relation

$$\sigma(H) \times \text{Br}(H \rightarrow X) = \frac{\sigma_{gg}^{\text{SM}}}{\Gamma_{gg}^{\text{SM}}} \times \frac{\Gamma_{gg}\Gamma_X}{\Gamma_{\text{tot}}}.$$

- Calculate and assign theoretical uncertainty to $\sigma_{gg}^{\text{SM}}/\Gamma_{gg}^{\text{SM}}$, extract $\Gamma_{gg}\Gamma_X/\Gamma_{\text{tot}}$; new states in loops drop out.
- Studies assign $\pm 20\%$ uncertainty to σ/Γ for $gg \rightarrow H$ production mode. **Dührssen et al.**

$$\begin{aligned}\Gamma^{\text{SM}} &= \alpha_s(\mu_r)^2 C_1(\mu_r)^2 [1 + \alpha_s(\mu_r) X_1 + \dots]; \\ \sigma^{\text{SM}} &= \alpha_s(\mu_r)^2 C_1(\mu_r)^2 [1 + \alpha_s(\mu_r) Y_1 + \dots].\end{aligned}$$

- Scale variation correlated; large μ_r variations cancel; $\Delta(\sigma/\Gamma) = \pm 5\%$.
- Recent developments:
 - N³LO soft+virtual corrections to $\sigma_{gg \rightarrow H}$ **Moch, Vermaseren, Vogt**
 - N³LO corrections to Γ_{gg} **Baikov, Chetyrkin**
 - $\Delta\sigma : \pm 10\% \rightarrow \pm 4\%$; $\Delta\Gamma : \pm 5\% \rightarrow \pm 2\%$.

Conclusions

- Good understanding of pQCD is an important pre-requisite for the successful LHC physics program.
- Recent developments include
 - making showers more realistic (harder);
 - large-scale NLO computations;
 - merging shower event generators and NLO computations;
 - emerging NNLO phenomenology.
- From existing computations and comparison with data we should learn
 - to appreciate uncertainties;
 - to understand when popular techniques are applicable;
 - to choose “right” scales in perturbative predictions;
 - to avoid rash conclusions if something does not add up.
- There are plenty of challenges, room for new ideas and unorthodox approaches even in Old Physics. A significant progress that occurred in pQCD in the last few years will be very useful once the LHC turns on.