

# Azimuthal angular spin determination: towards the LHC

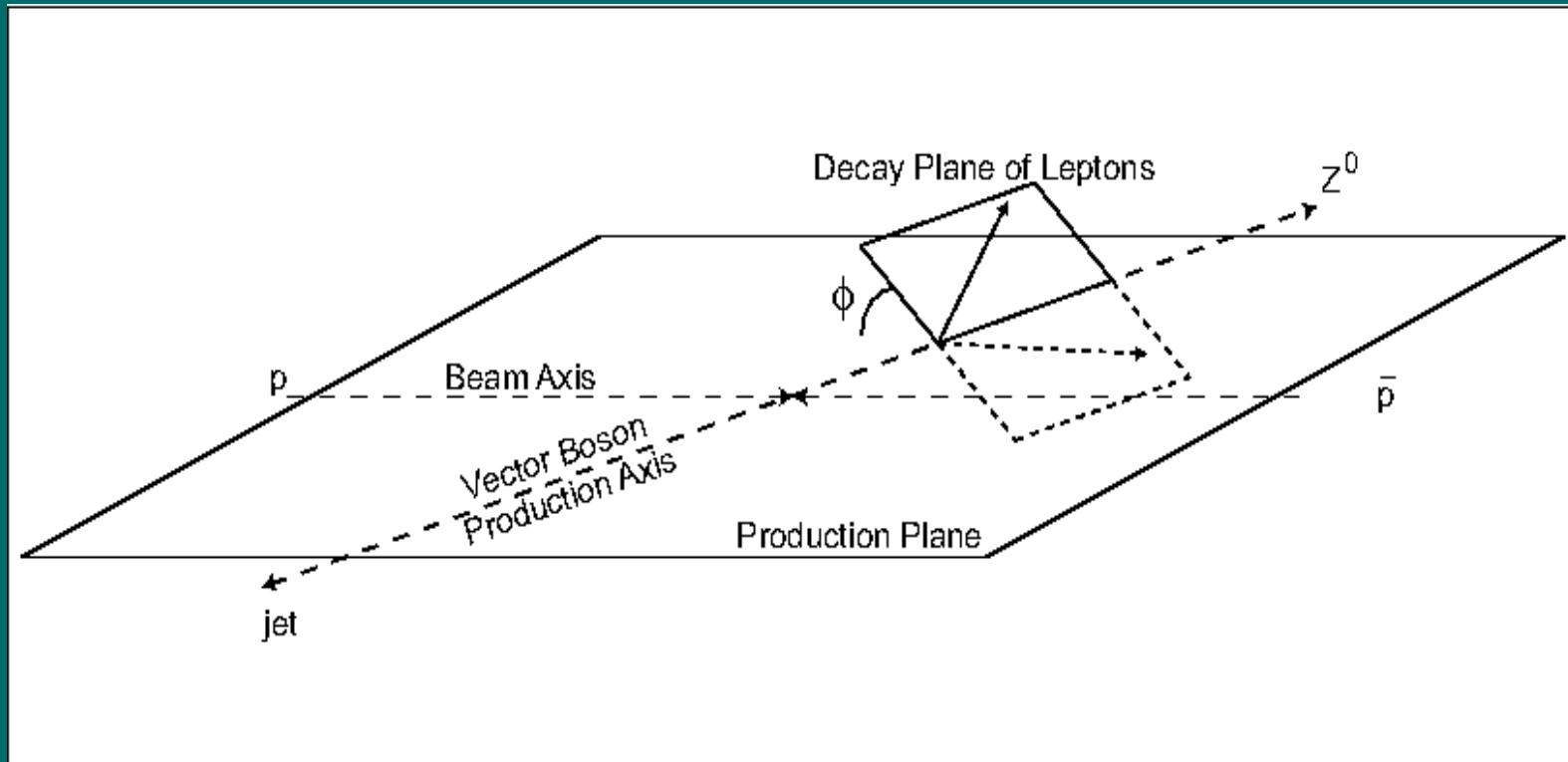
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# Outline

- Brief Review
- $Z + \text{jet}$  at Tevatron
  - Rotationally invariant cuts
- $Z + \text{jet}$  at LHC
  - Dealing with identical beams
- $Z'$

# Our Technique



# Our Technique

- Particle produced in multiple helicities

$$\sigma \propto \left| \sum_h M_{production}(h) e^{i h \phi} M_{decay}(h, \phi=0) \right|^2$$

- Helicity states interfere!

$$\frac{d N}{d \phi} = \frac{d \sigma}{d \phi} \times L = A_0 + A_1 \cos(\phi) + \dots + A_n \cos(n \phi); n = \Delta h$$

- Measuring distribution places limit on spin

$$s \geq \frac{n_{meas}}{2}$$

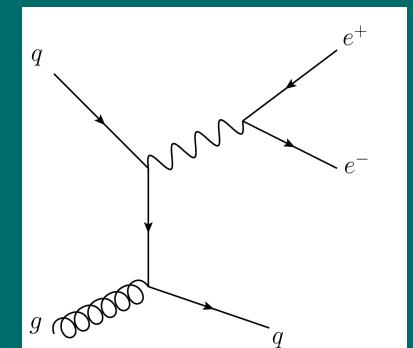
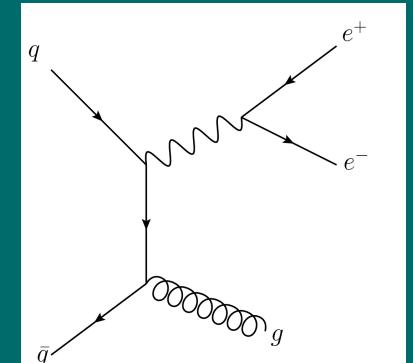
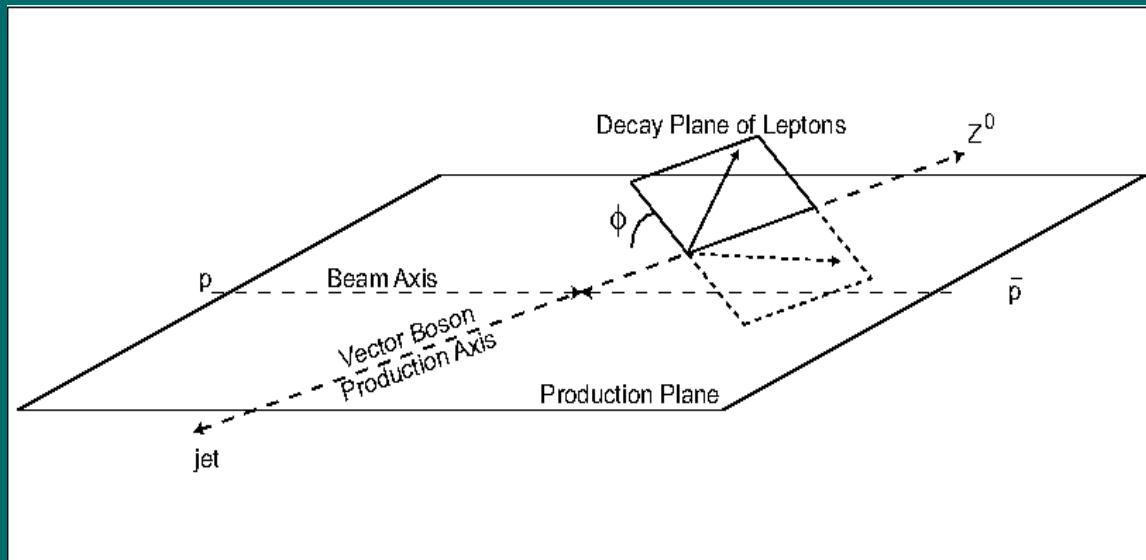
*scalar* :  $A_0$

*spinor* :  $A_0 + A_1 \cos(\phi)$

*vector* :  $A_0 + A_1 \cos(\phi) + A_2 \cos(2\phi)$

# Example: Z+jet at Tevatron

- Fully reconstructible
- Z produced in multiple helicity states



# Initial results

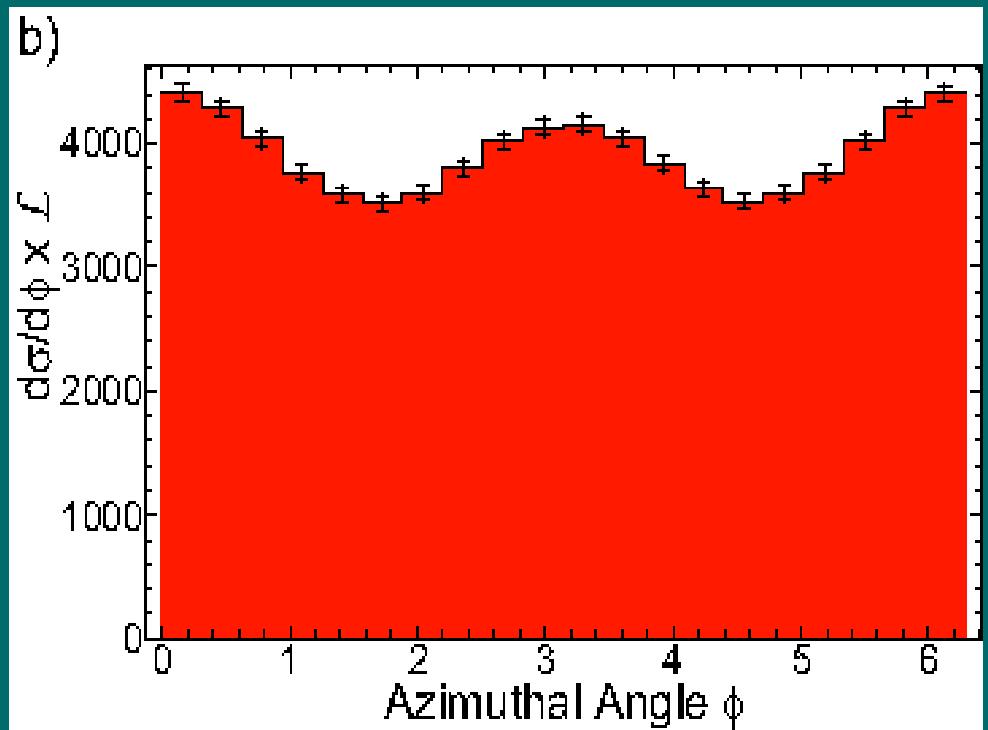
- The Z is a vector boson!

$$A_1/A_0 = 0.036$$

$$A_2/A_0 = 0.100$$

$$A_3/A_0 = 0.000$$

$$A_4/A_0 = 0.000$$



Cuts on jet:  $p_T > 30\text{ GeV}$ ,  $|\eta| < 2.1$

# Detector Cuts

- Selection cuts necessary to improve sample, deal with detector limitations.
- CDF: 6203 events from  $1.7 \text{ fb}^{-1}$  luminosity at 1.96 TeV beam energy (after cuts)

Jet transverse momentum	$p_{T,j} > 30 \text{ GeV}$
Jet $\eta$	$ \eta  < 2.1$
Invariant mass of lepton pair	$66 < m_{\ell\ell} < 116 \text{ GeV}$
Central electron $\eta$	$ \eta  < 1$
Second electron $\eta$	$ \eta  < 1 \text{ or } 1.2 <  \eta  < 2.8$
Electron $E_T$	$E_T > 25 \text{ GeV}$
Electron isolation cuts	$\Delta R_{ej} > 0.7$

# Detector Cuts

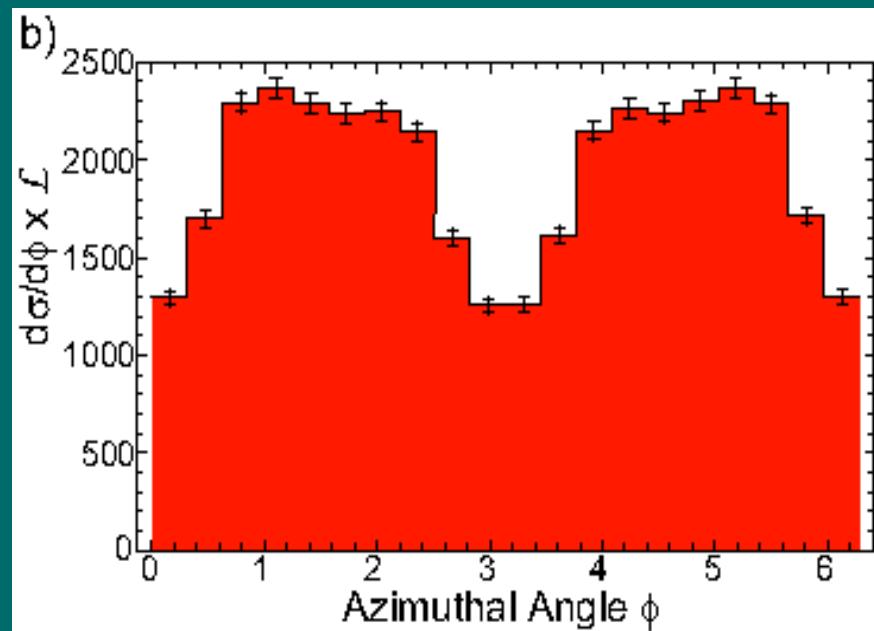
- Spurious higher order modes from the cuts

$$A_1/A_0 = 0.029$$

$$A_2/A_0 = -0.277$$

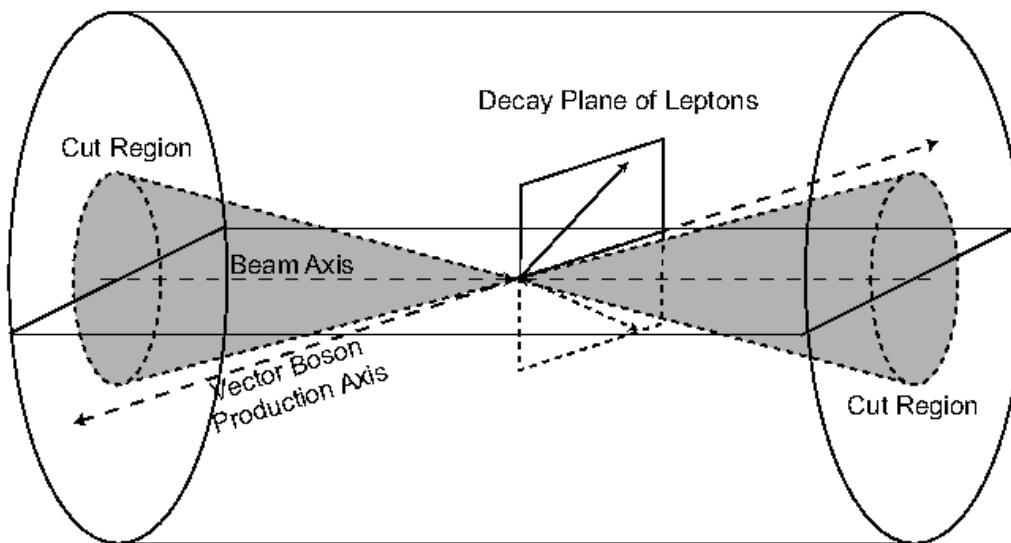
$$A_3/A_0 = -0.021$$

$$A_4/A_0 = -0.123$$

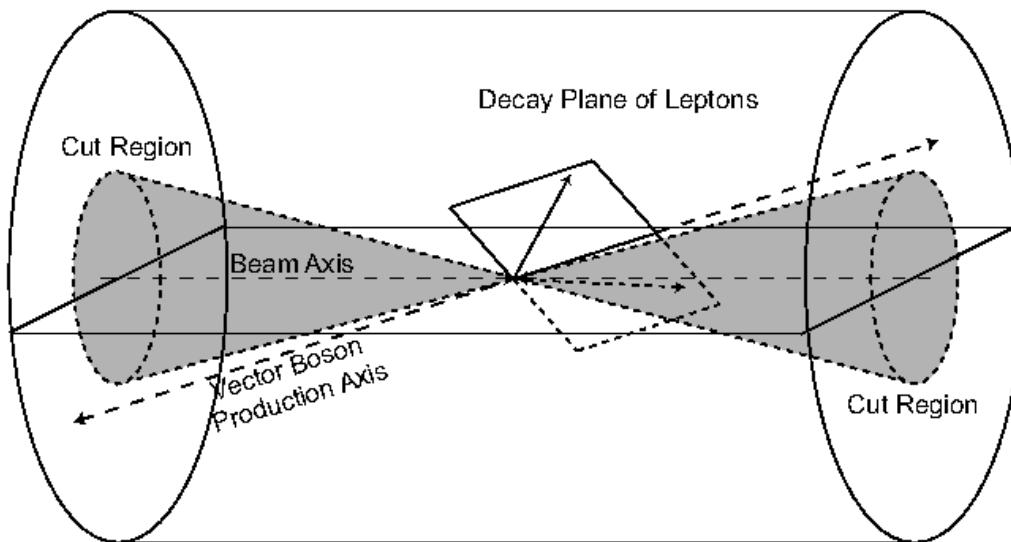


# Rotationally Invariant cuts

a)



b)



# Revised results

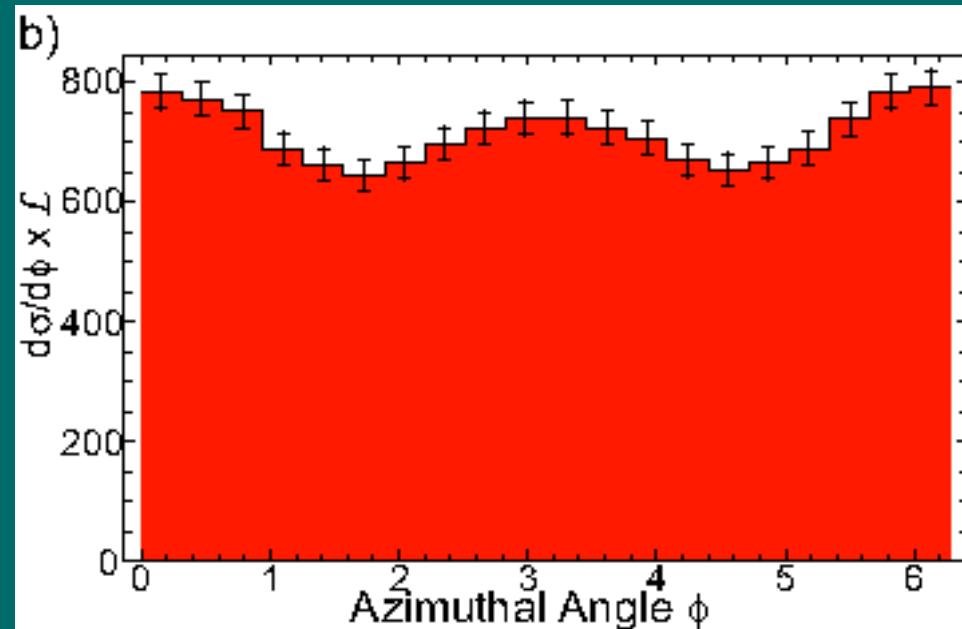
- New cuts restore expected behavior
- Inefficient -> loosened cuts

$$A_1/A_0 = 0.039 \pm 0.022$$

$$A_2/A_0 = 0.083 \pm 0.021$$

$$A_3/A_0 = 0.000 \pm 0.022$$

$$A_4/A_0 = 0.000 \pm 0.023$$



- More data collection – smaller error bars

# Z+jet at the LHC

- What physics can be done with the early LHC data?  
 $(E_{beam}=5\,TeV, \sim 100\ pb^{-1} integrated luminosity)$
- Even at low luminosity, very high production rate
- Cuts:
  - $jet: p_T > 40\,GeV, |\eta| < 3.2$
  - $lepton: one\ p_T > 10\,GeV, one\ p_T > 20\,GeV$
  - $lepton: |\eta| < 2.5$
  - $jet - lepton: \Delta R > 0.7$
  - $lepton\ pair: 66 < m_{ll} < 116\,GeV$

# Z+jet at the LHC: Results

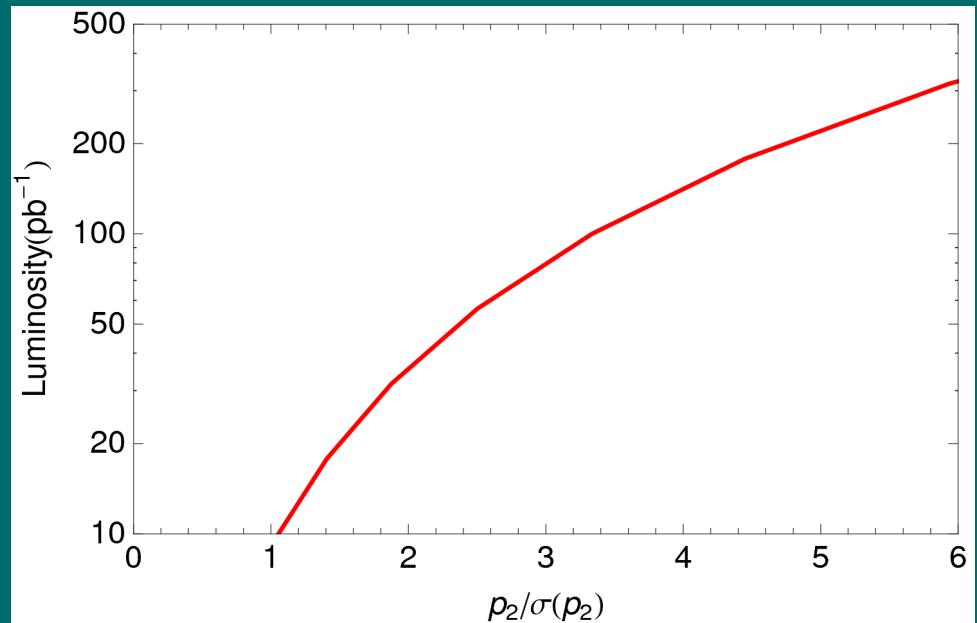
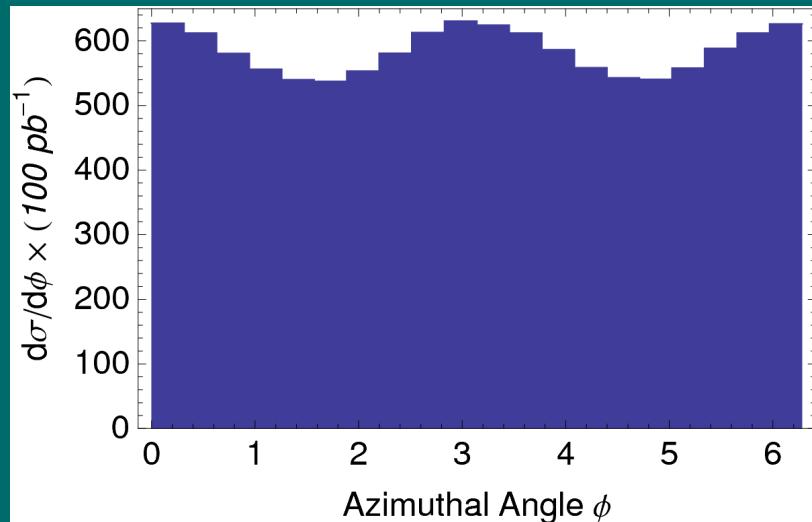
- Better than 3 sigma for  $100 \text{ pb}^{-1}$

$$A_1/A_0 = 0.000 \pm 0.024$$

$$A_2/A_0 = 0.079 \pm 0.024$$

$$A_3/A_0 = 0.000 \pm 0.024$$

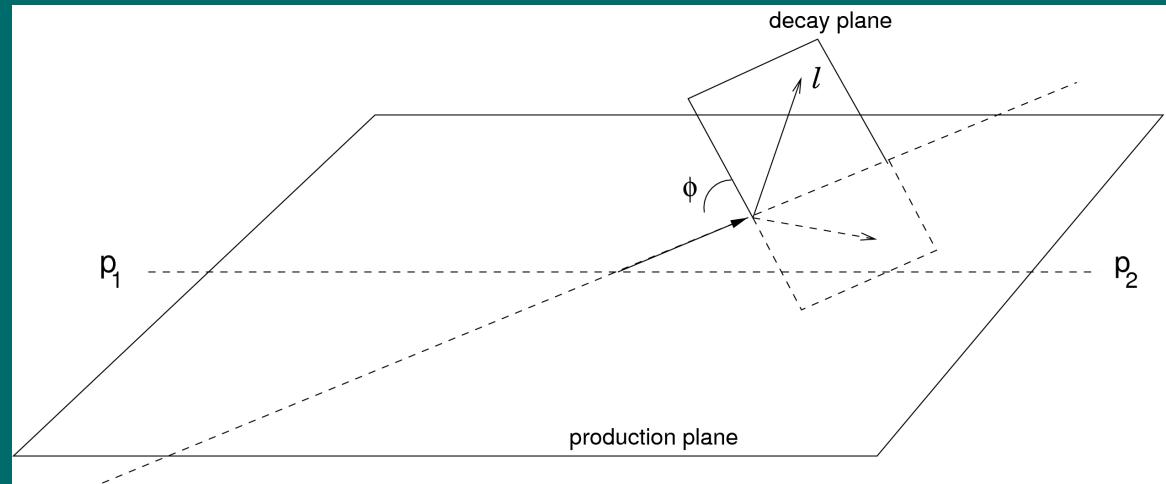
$$A_4/A_0 = 0.000 \pm 0.025$$



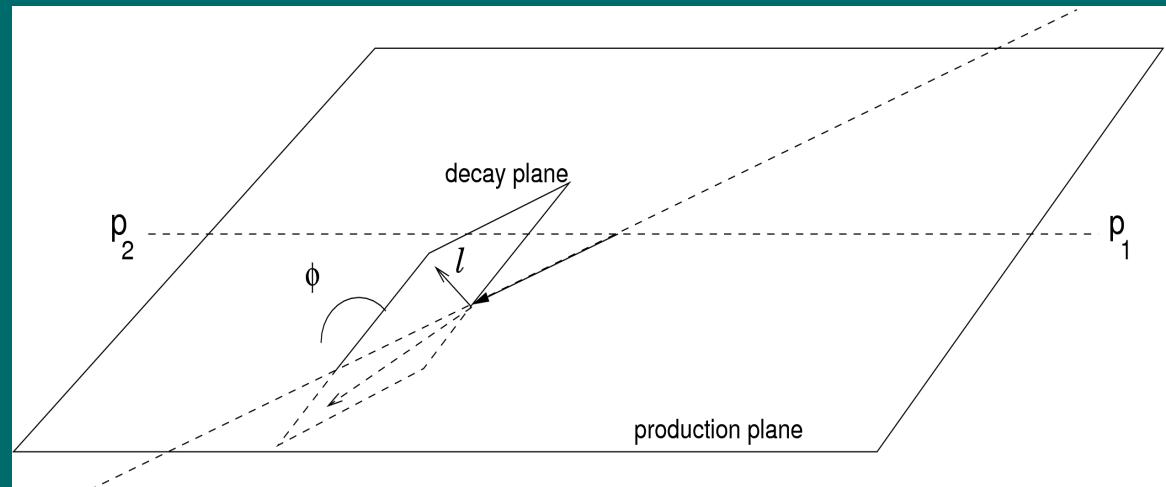
# Challenges at the LHC

- Identical beams
- Missing Energy

$$\cos(\phi) = \frac{\hat{z} \times \vec{p}_Z}{|\hat{z} \times \vec{p}_Z|} \cdot \frac{\vec{p}_Z \times \vec{p}_l}{|\vec{p}_Z \times \vec{p}_l|}$$



$$\phi \rightarrow \pi - \phi$$



$$\frac{dN}{d\phi}(p_1 p_2, \phi) = \frac{dN}{d\phi}(p_2 p_1, \pi - \phi)$$

# Challenges at the LHC

$$\frac{dN}{d\phi}(p_1 p_2, \phi) = \frac{dN}{d\phi}(p_2 p_1, \pi - \phi)$$

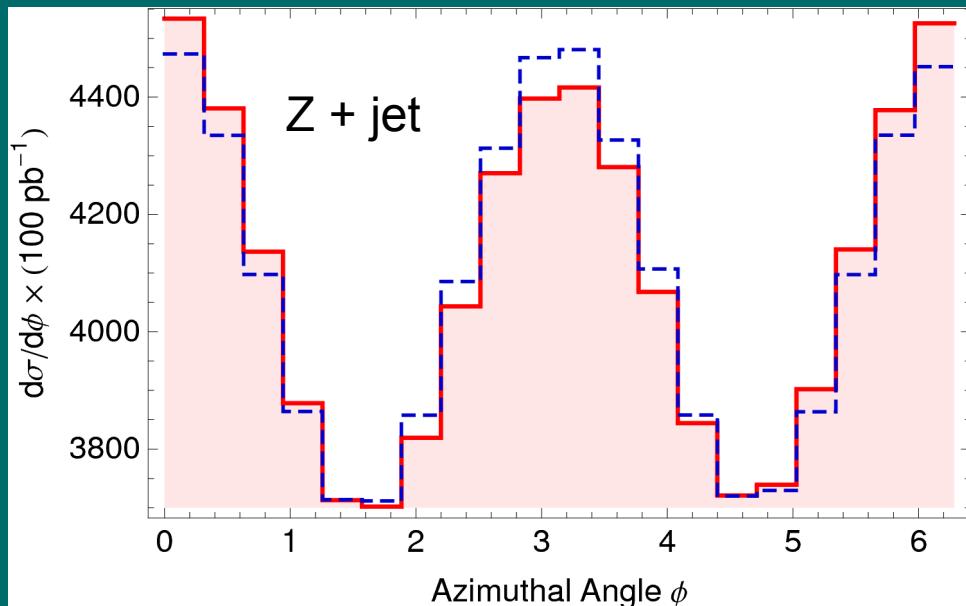
$$\frac{dN}{d\phi}(p_1 p_2) = a_0 + a_1 \cos(\phi) + a_2 \cos(2\phi)$$

$$\begin{aligned} \frac{dN}{d\phi}(p_2 p_1) &= a_0 + a_1 \cos(\pi - \phi) + a_2 \cos(2(\pi - \phi)) \\ &= a_0 - a_1 \cos(\phi) + a_2 \cos(2\phi) \end{aligned}$$

$$\frac{dN}{d\phi}(p_1 p_2 + p_2 p_1) = 2a_0 + 0 \cos(\phi) + 2a_2 \cos(2\phi)$$

- Odd modes disappear

# Odd modes: If we knew everything



$Z + \text{jet}$

Blue: no filter

$$A_1/A_0 = 0.000$$

$$A_2/A_0 = 0.096$$

$$A_3/A_0 = 0.000$$

$$A_4/A_0 = 0.000$$

Red: idealized filter

$$\begin{aligned}\phi(q\bar{q}, qg, g\bar{q}) &\rightarrow \phi \\ \phi(\bar{q}q, gq, \bar{q}g) &\rightarrow \pi - \phi\end{aligned}$$

$$A_1/A_0 = 0.015$$

$$A_2/A_0 = 0.096$$

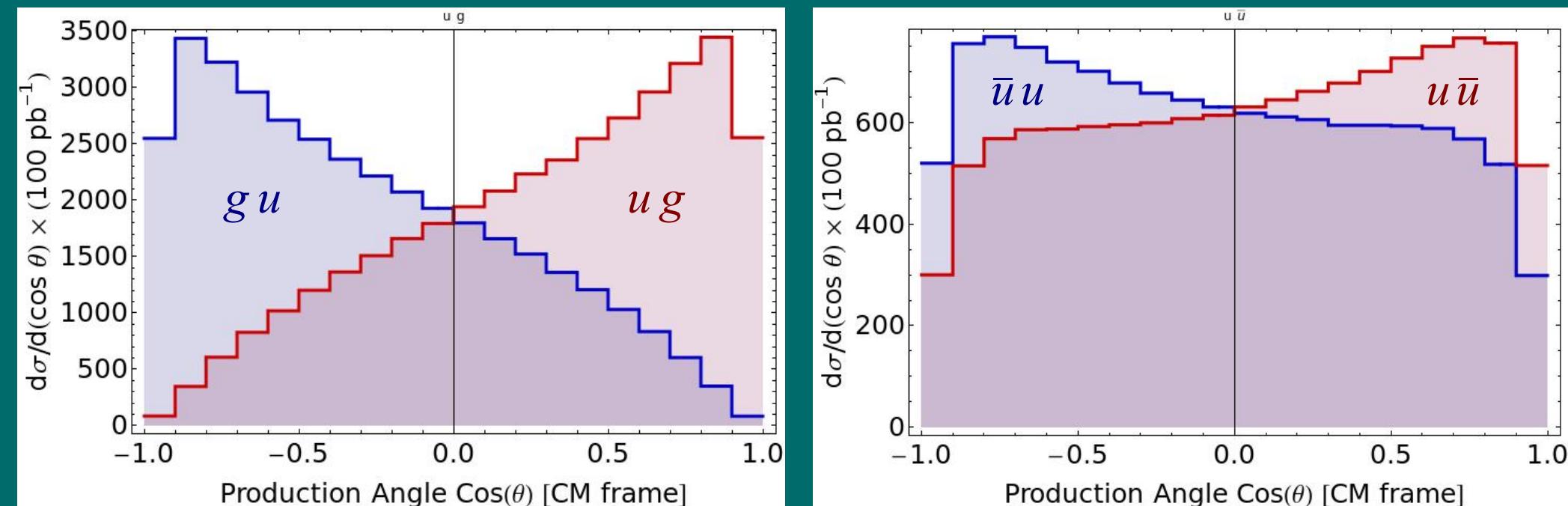
$$A_3/A_0 = 0.000$$

$$A_4/A_0 = 0.000$$

# Odd modes

- Production angle differentiates initial partons

$p_1 p_2 \rightarrow Z \text{ jet}$

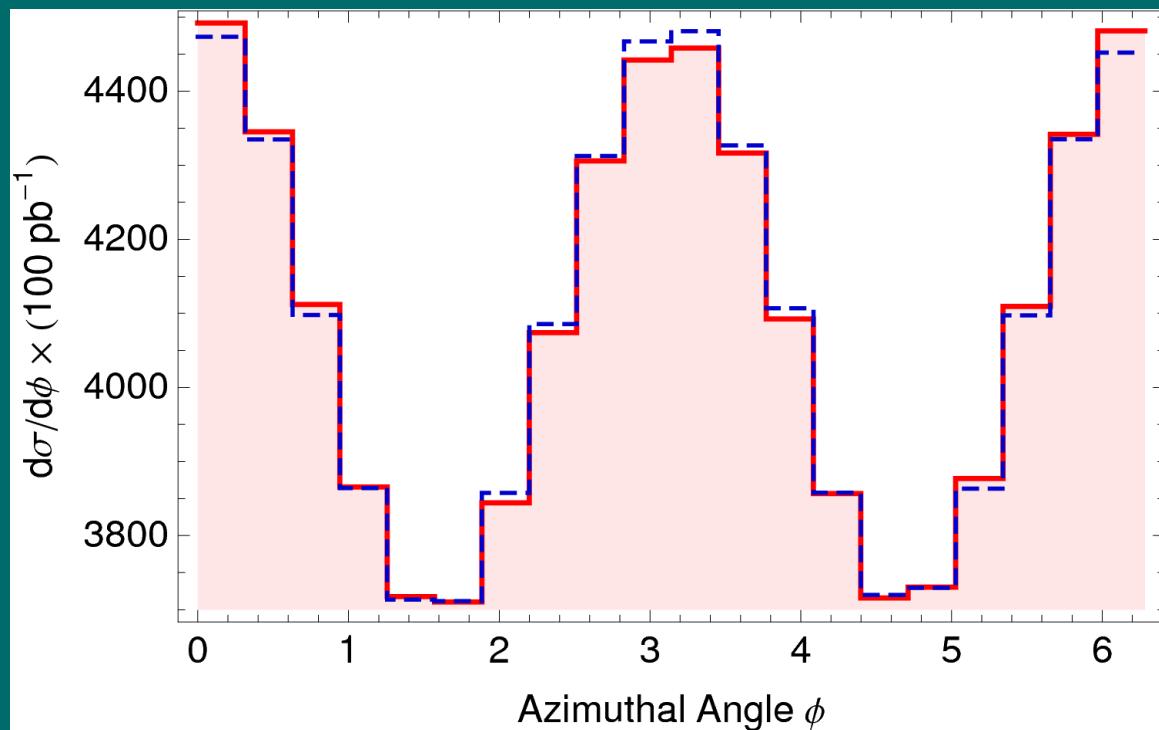


Filter:

$$\phi(\cos(\theta) > 0) \rightarrow \phi$$
$$\phi(\cos(\theta) < 0) \rightarrow \pi - \phi$$

# Odd modes

- Success (in principle)



$$A_1/A_0 = 0.005$$

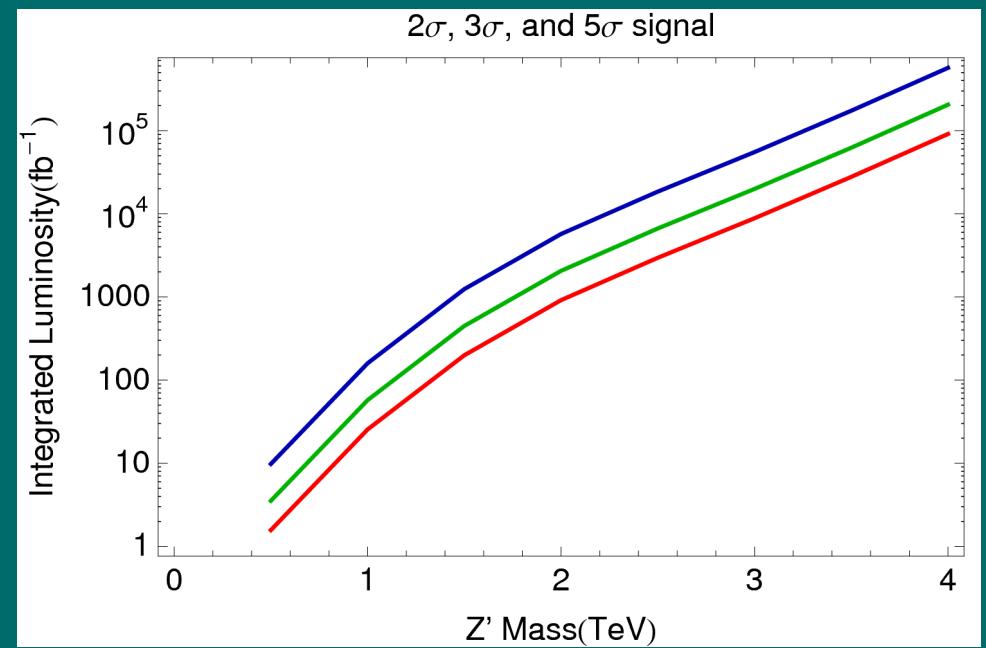
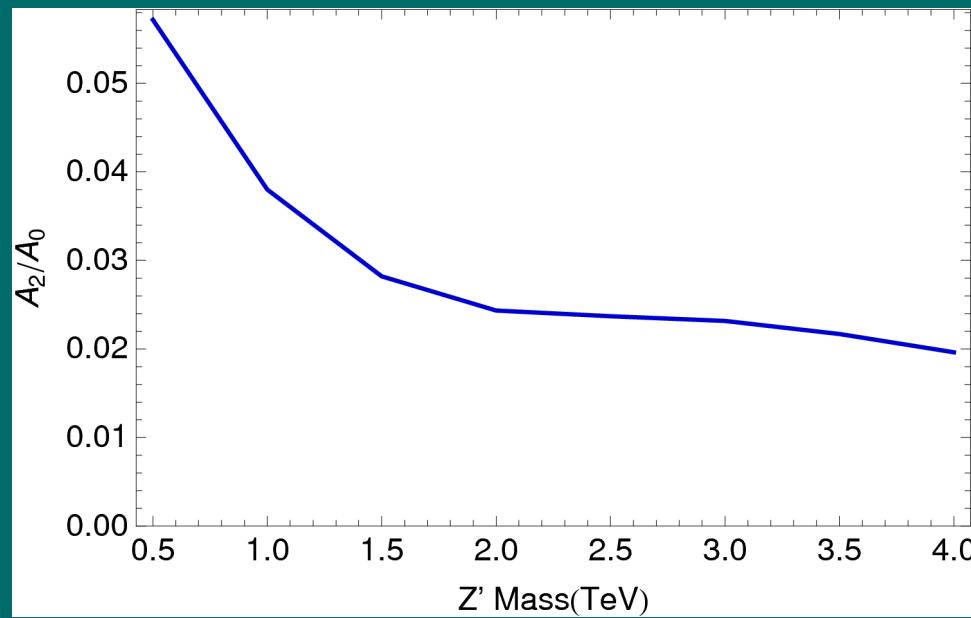
$$A_2/A_0 = 0.096$$

$$A_3/A_0 = 0.000$$

$$A_4/A_0 = 0.000$$

# $Z' + \text{jet}$

- Model:  $Z'$  with SM couplings
- Simulation at 14 TeV
- Same cuts as  $Z + \text{jet}$  (with sliding invariant mass window)



with H. Murayama

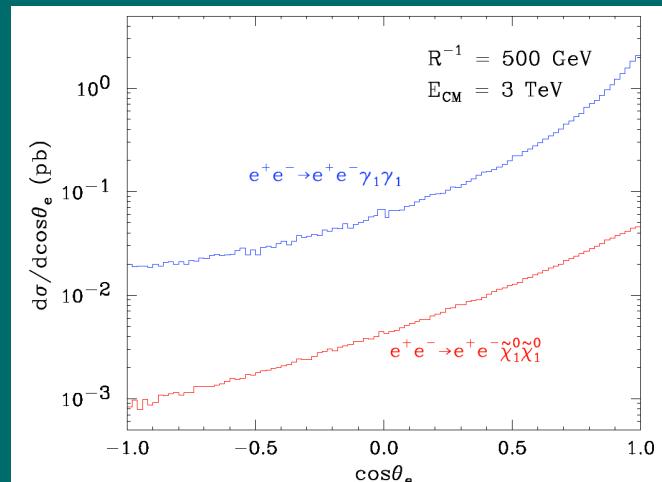
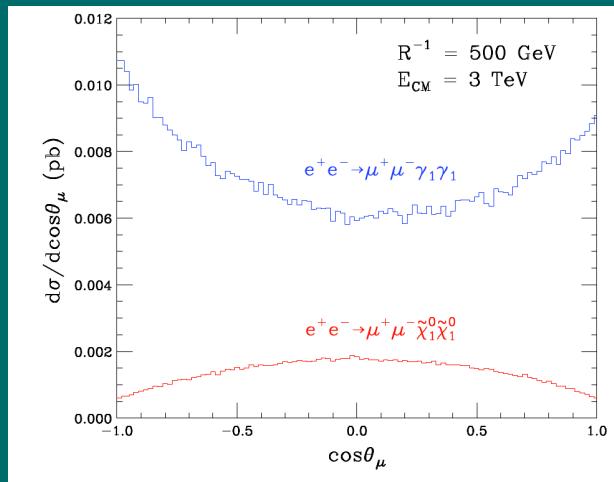
# Conclusions

- Model-independent spin measurement
- Selection cuts must be made 'rotationally invariant' to preserve form of distribution
- Technique can be tested using existing data and early LHC data
- $Z'$  spin determination
- Identical beams at LHC necessitate careful treatment of odd modes
- Processes with missing energy require a better solution

END

# Spin Measurement Techniques

- Linear collider
  - Threshold scans:  $\sigma_{scalar} \sim \beta^3$ ,  $\sigma_{spinor/vector} \sim \beta$
  - Production angle (s-channel pair production):  
$$\sigma_{scalar} \sim \sin^2(\theta), \quad \sigma_{spinor} \sim 1 + \frac{E^2 - m^2}{E^2 + m^2} \cos^2(\theta)$$



- Linear and Hadron Collider
  - Polar decay angle – requires chiral couplings, full reconstruction

# Our Technique

- Particle with momentum  $\vec{p}$  and helicity  $h$  decays
- Rotations generated by  $U(\phi) = e^{i\vec{J}\cdot\vec{\phi}} \rightarrow e^{iJ_z\phi}$
- Define z-axis with momentum of decaying particle

$$J_z = \frac{(\vec{s} + \vec{x} \times \vec{p}) \cdot \vec{p}}{|\vec{p}|} = \frac{\vec{s} \cdot \vec{p}}{|\vec{p}|} = h$$

- Matrix element of decay carries angle as a phase

$$M_{decay}(h, \phi) = e^{ih\phi} M_{decay}(h, \phi=0)$$