

Extra Dimensions at the LHC

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Outline and Summary

- **Warped** extra dimensions address **Planck-weak** and **flavor** hierarchies: new (KK) particles at a **few TeV** (precision tests)
- **Challenging** for LHC: techniques to detect highly **boosted top/W/Z** (experimentalists' input!) required
- **Relax** constraints by **KK parity**: **no** coupling of single (lightest) new particle to SM

WARPED EXTRA DIMENSION

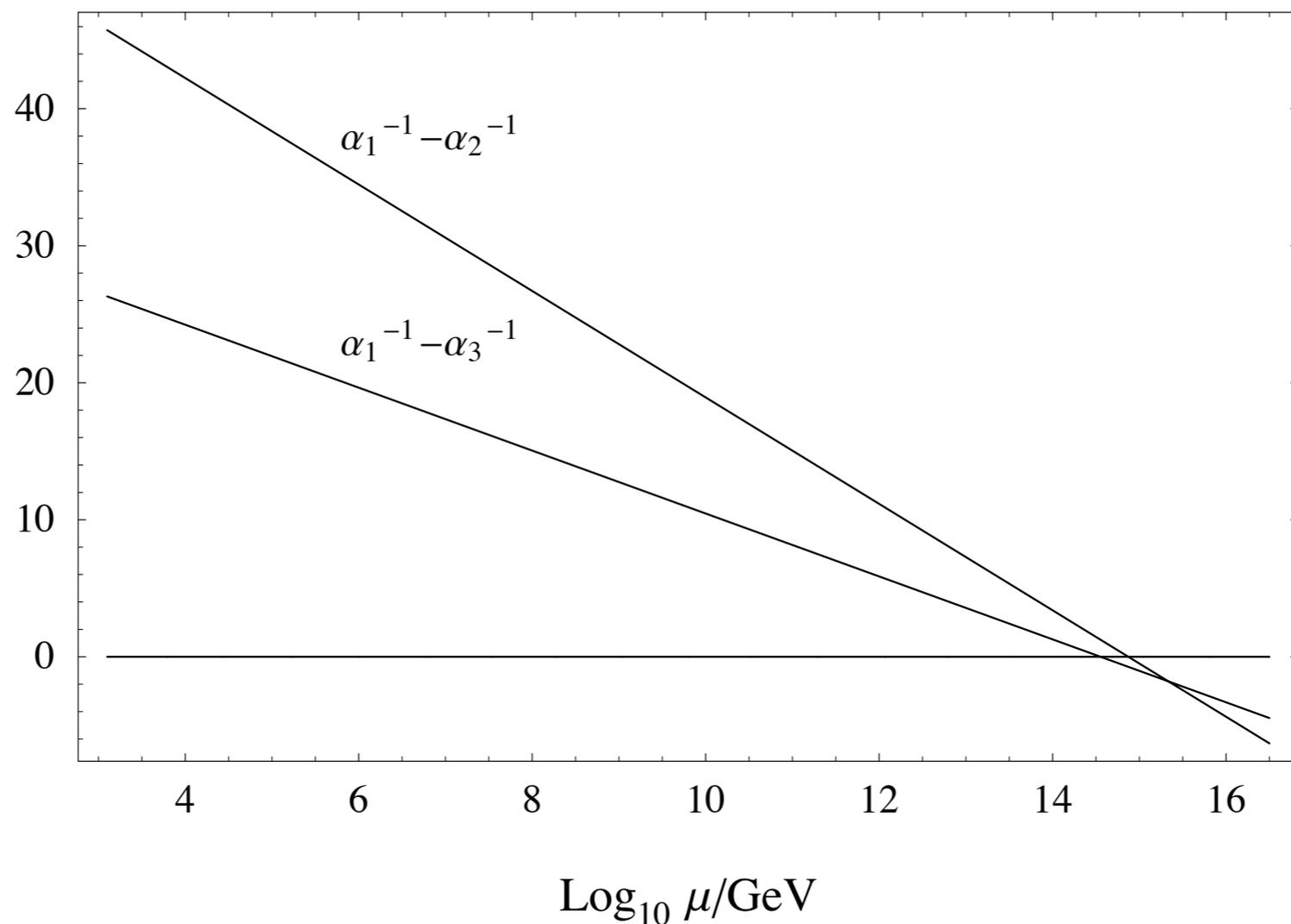
Motivations

- Planck-weak and flavor hierarchy (without severe flavor problem)
- Weakly-coupled "tool" for 4D strong dynamics: dual to 4D composite Higgs (AdS/CFT)
- GUT's: (i) dark matter from proton stability (KA, Servant); (ii) gauge coupling unification with precision \sim SUSY (KA, Contino, Sundrum)

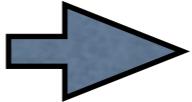
Tantalizing unification: **magic** of

β -function: $SM - 2t_R - H$

(KA, Contino, Sundrum)

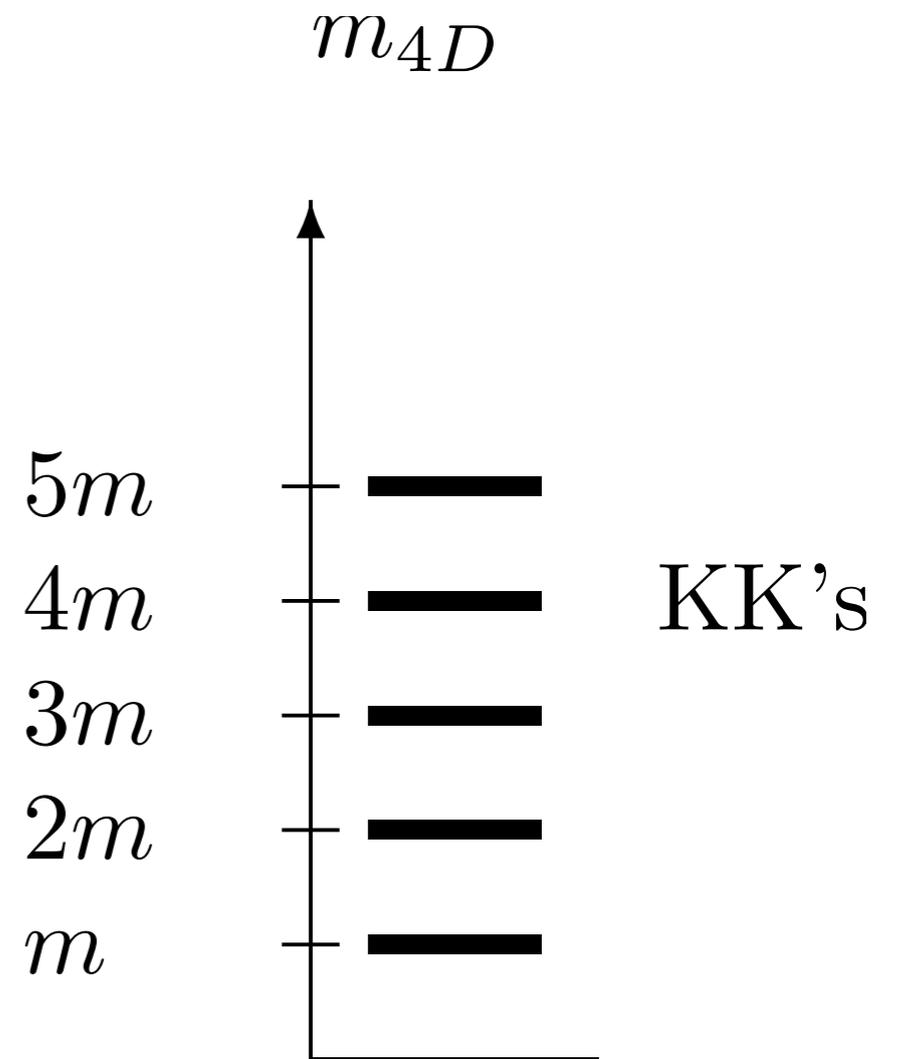
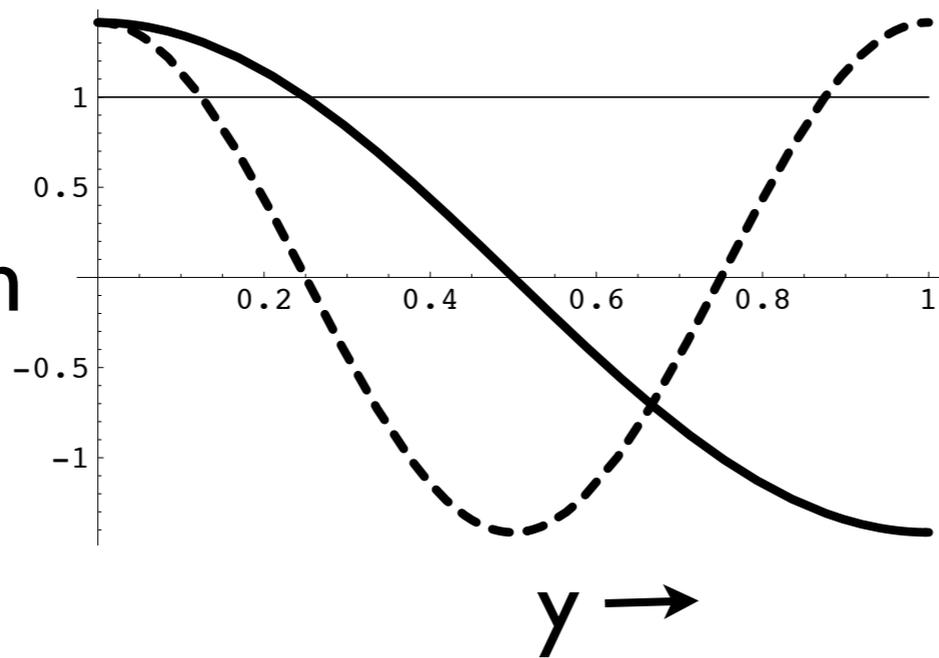


Basics of extra dimensions

- Particle in 5D: SM (x_μ, y)  Fourier expand y (a la 1D box)

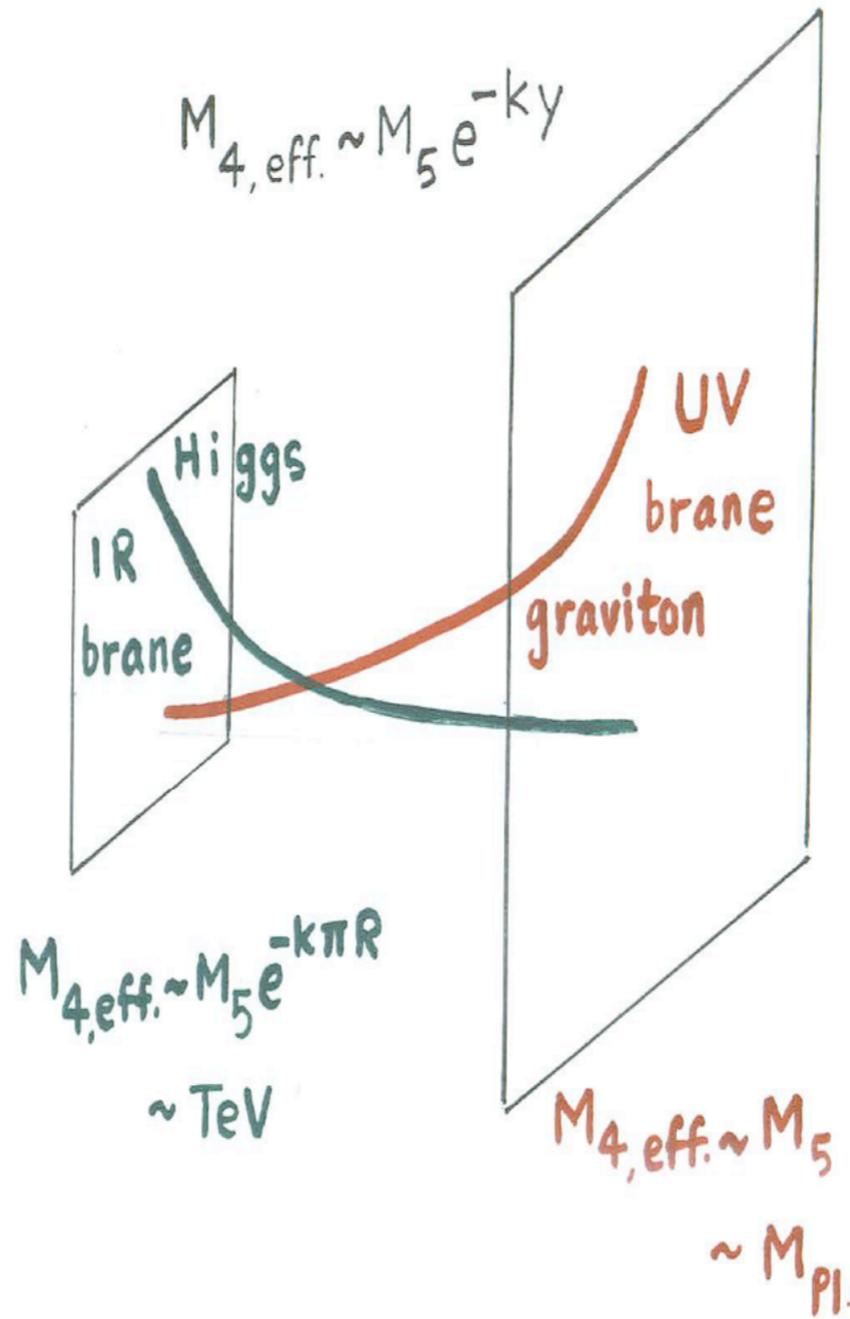
- Lightest mode (SM) + heavier (Kaluza-Klein: KK) with profiles

↑
wavefunction



Gravity and Higgs

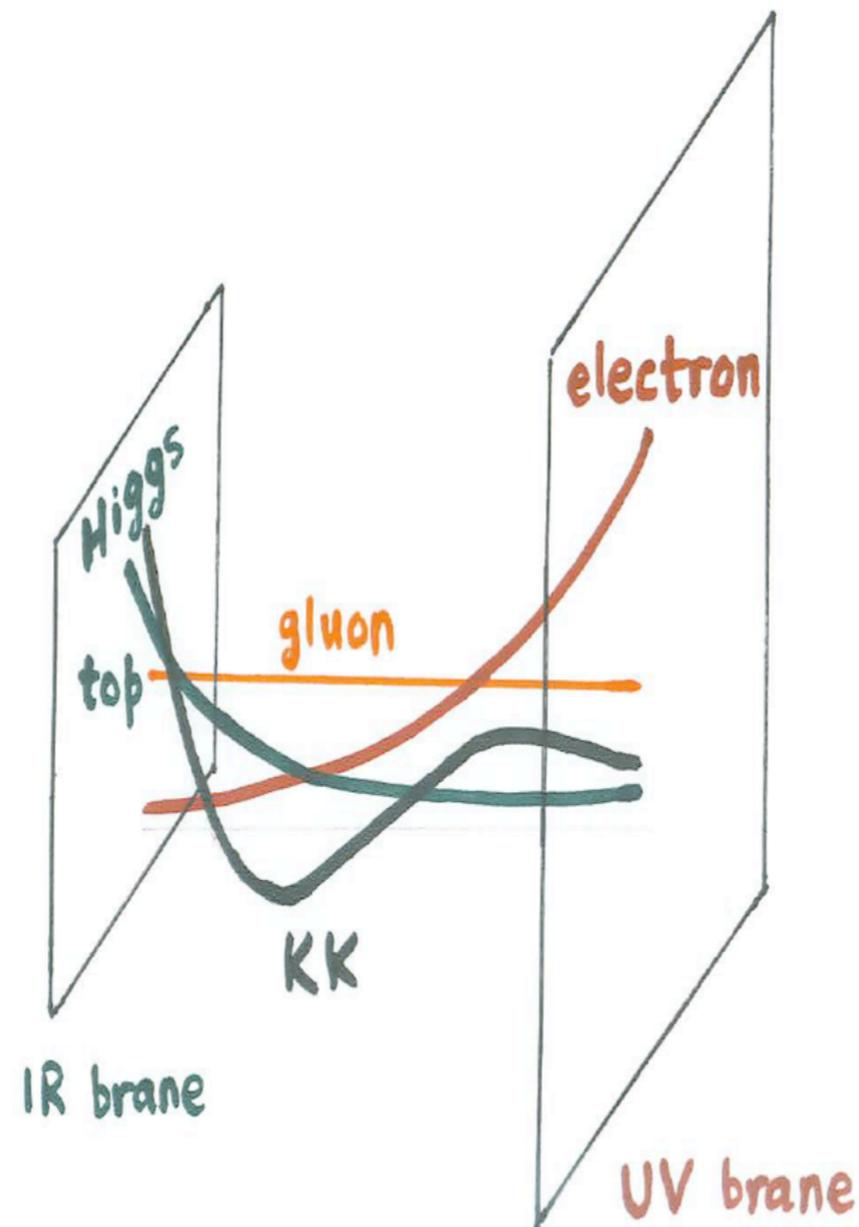
(Randall, Sundrum)



$$kR \sim \log (M_{Pl}/\text{TeV}) / \pi \sim 10$$

SM in bulk

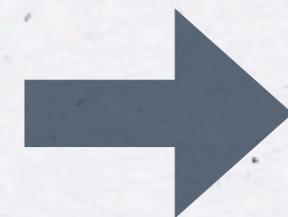
(Davoudiasl, Hewett, Rizzo; Pomarol; Grossman, Neubert; Chang, Hisano, Nakano, Okada, Yamaguchi; Gherghetta, Pomarol)



Couplings from overlap of profiles

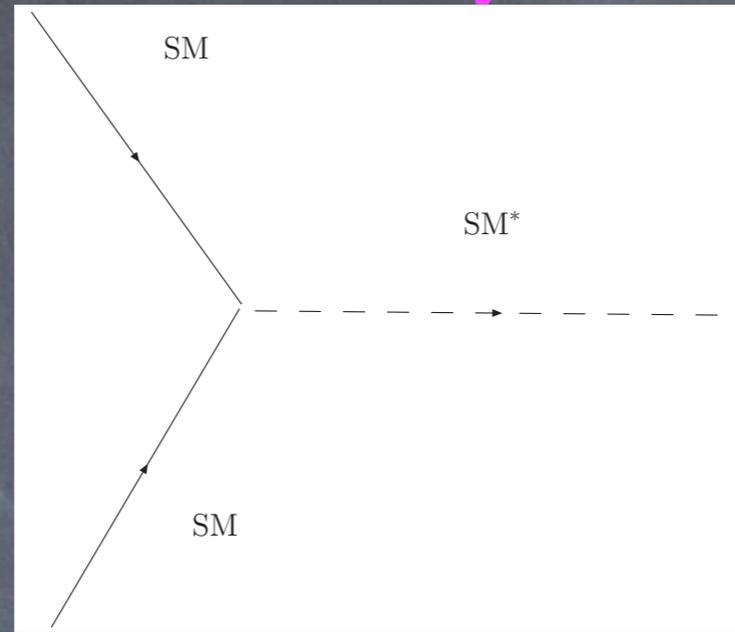
- Flavor hierarchy (fermion-Higgs) without hierarchy in 5D parameters (5D Yukawa, 5D mass M):
fermion profile $\sim e^{-k\pi R M} \dots$...related to Planck-weak hierarchy
- Couplings to KK large (small) for top (electron)

NO PARITY, PRECISION TESTS
NEW PARTICLES FEW TEV

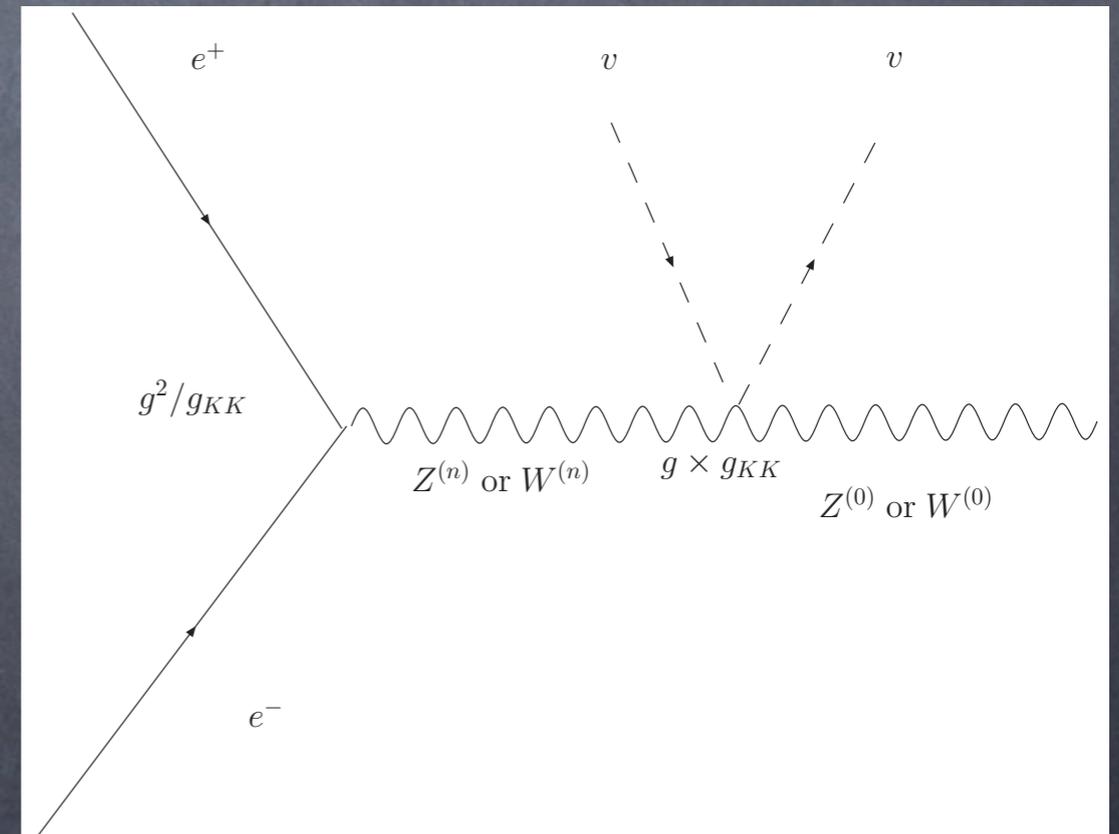
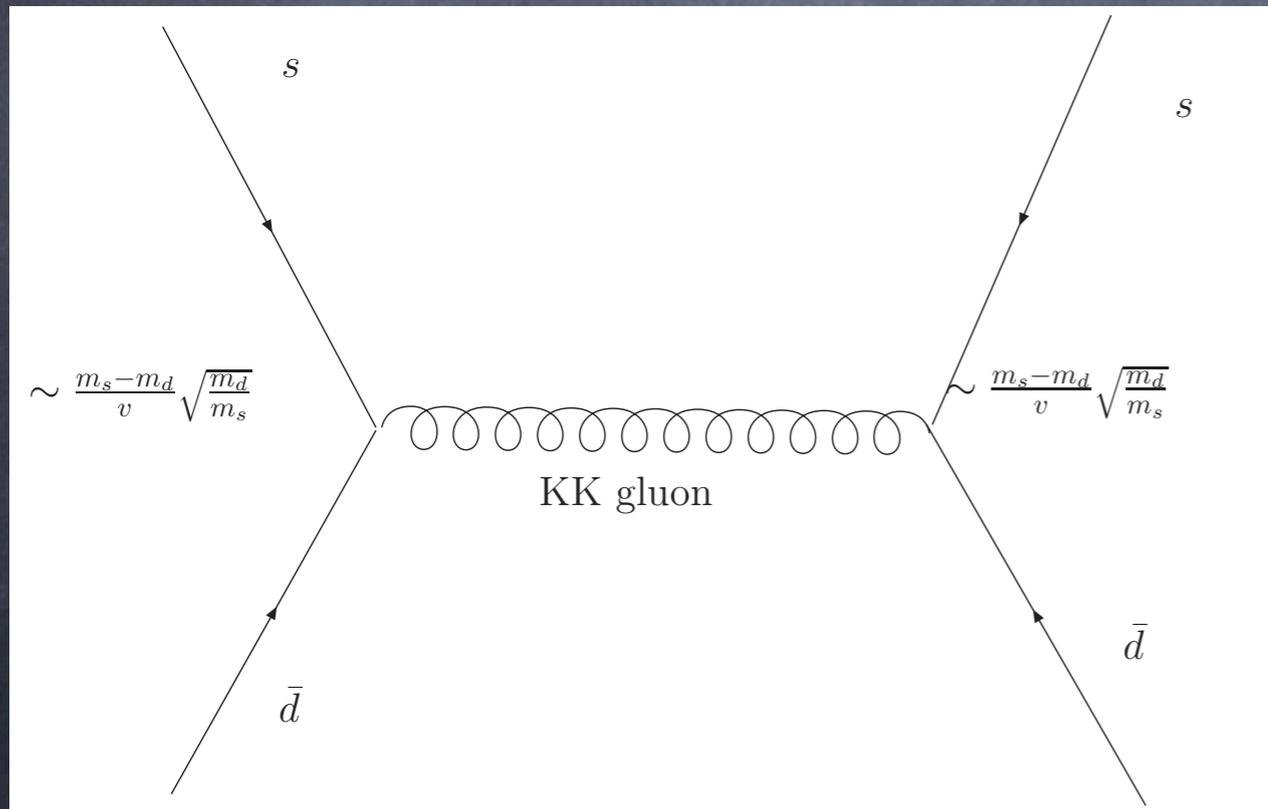


Summary (rough)

no parity



tree-level contributions to flavor and EW precision tests



lower limit on KK mass scale: $\sim O(3)$ TeV (built-in mechanism + model-building)

EW PRECISION TESTS

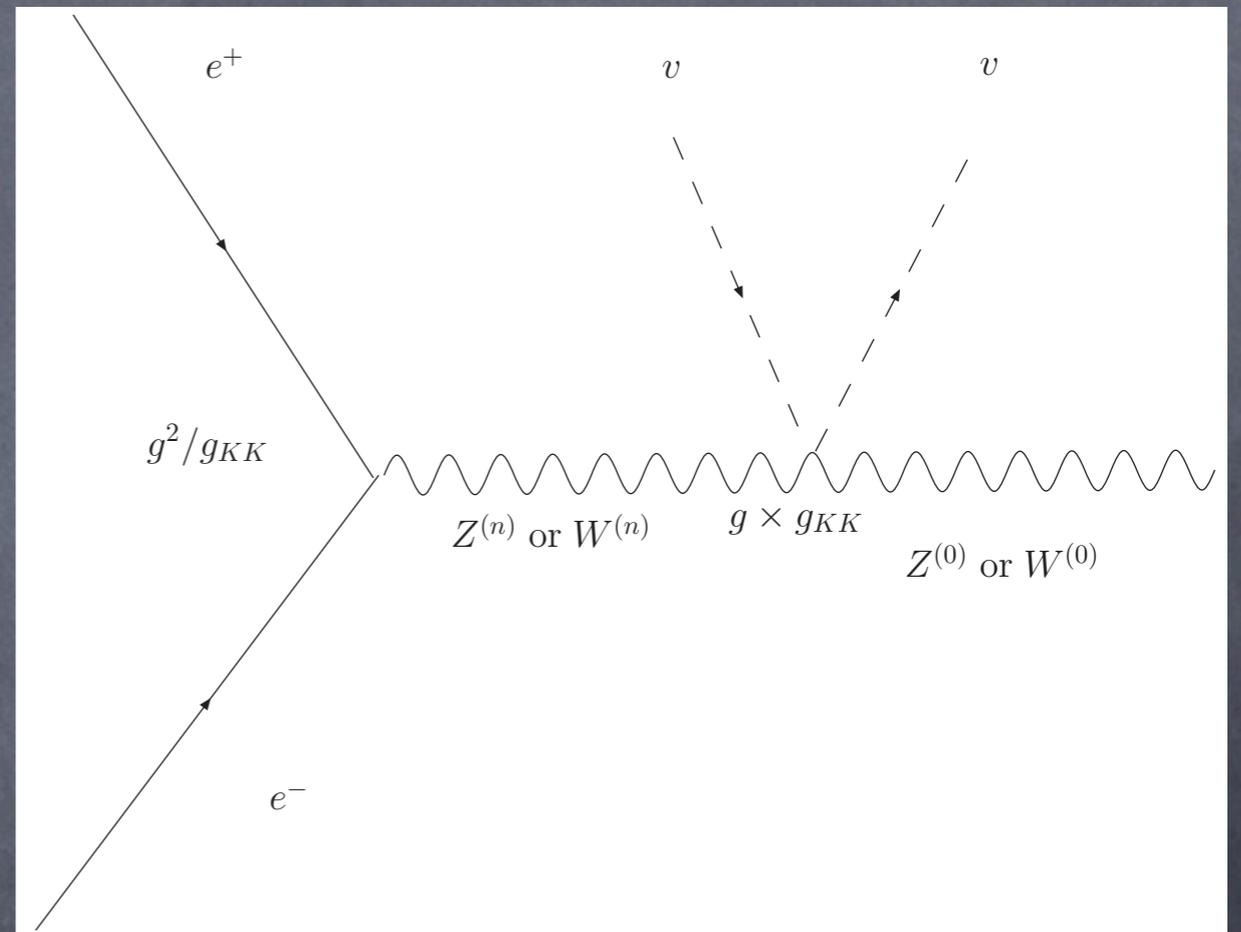
S parameter

• Equivalent to shift in coupling:

$$\frac{\delta g_Z}{g_Z} \sim \frac{M_Z^2}{M_{KK}^2}$$

$$\lesssim 0.1\%$$

$$\Rightarrow M_{KK} \gtrsim 3\text{TeV}$$



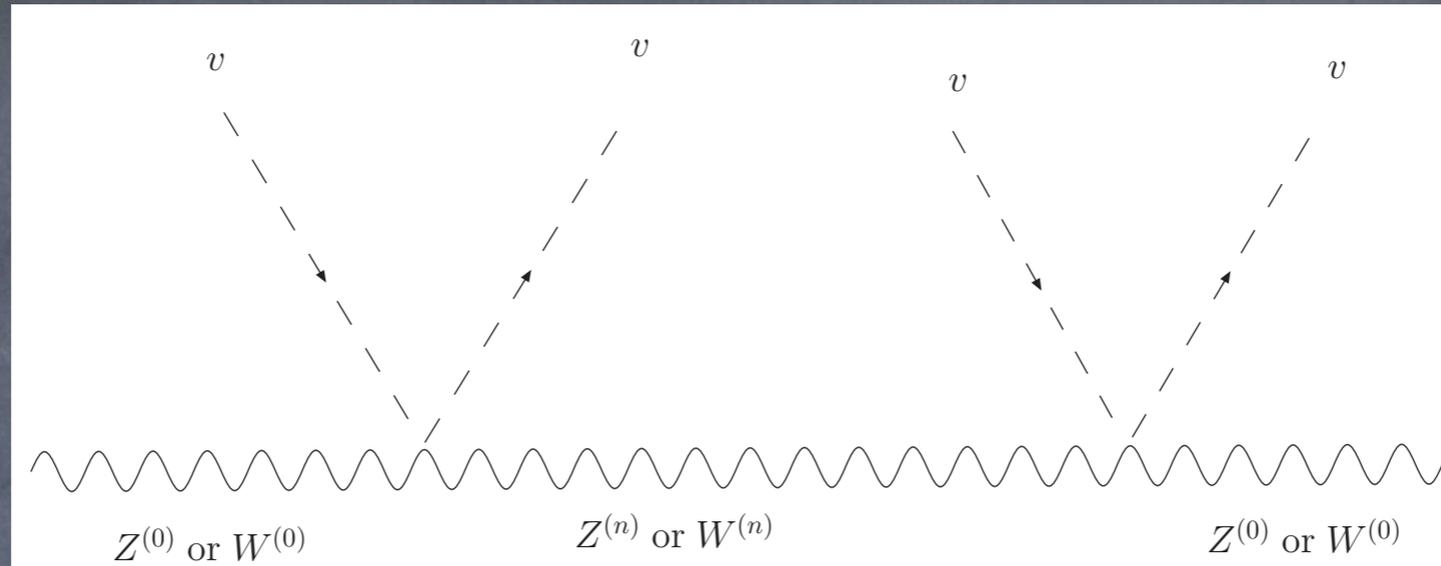
5D warped Higgsless models (breaking by boundary condition)

(Csaki, Grojean, Pilo, Terning)

- Flat profiles for fermions \Rightarrow suppression in S
(Cacciapaglia, Csaki, Grojean, Terning)
- < 1 TeV KK's unitarize WW scattering

(See talks by N. Christensen and K. Hsieh)

Custodial symmetries



- **T parameter** (KA, Delgado, May, Sundrum) and **Zbb** (KA, Contino, Da Rold, Pomarol)
- EW fit with ~ 3 TeV KK masses (Carena, Ponton, Santiago, Wagner)

About “ \sim ” in ~ 3 TeV

...due to model-**variations** (all explain hierarchies)

- **brane-localized** terms (Davoudiasl, Hewett, Rizzo; Carena, Delgado, Ponton, Tait, Wagner)
- **Higgs profile** (Davoudiasl, Lillie, Rizzo; Cacciapaglia, Csaki, Marandella, Terning)
- **“soft” wall** (metric **not** AdS near IR “brane” (McGuirk, Shiu, Zurek; Falkowski, Perez-Victoria; Batell, Gherghetta, Sword; Delgado, Diego) see talks

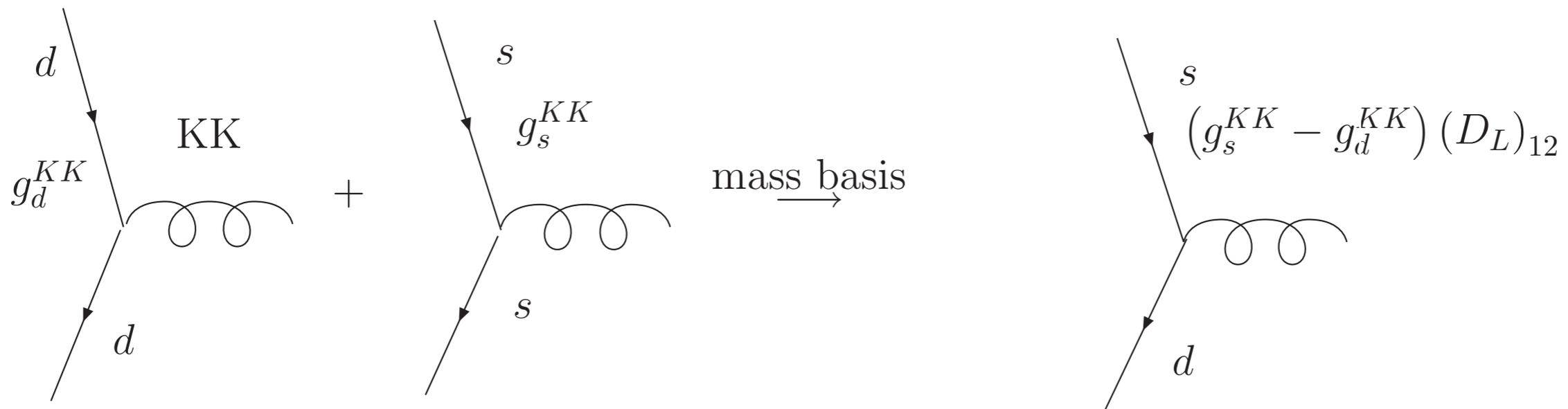
FLAVOR PRECISION TESTS

Flavor **hierarchy** from profiles \rightarrow

flavor **violation** from KK's

- Non-universal, but diagonal coupling to gauge KK's in gauge/weak basis...

$$(\bar{d}_{L \text{ weak}} \quad \bar{s}_{L \text{ weak}}) \begin{pmatrix} g_d^{KK} & 0 \\ 0 & g_s^{KK} \end{pmatrix} \gamma^\mu A_\mu^{(n)} \begin{pmatrix} d_{L \text{ weak}} \\ s_{L \text{ weak}} \end{pmatrix}$$

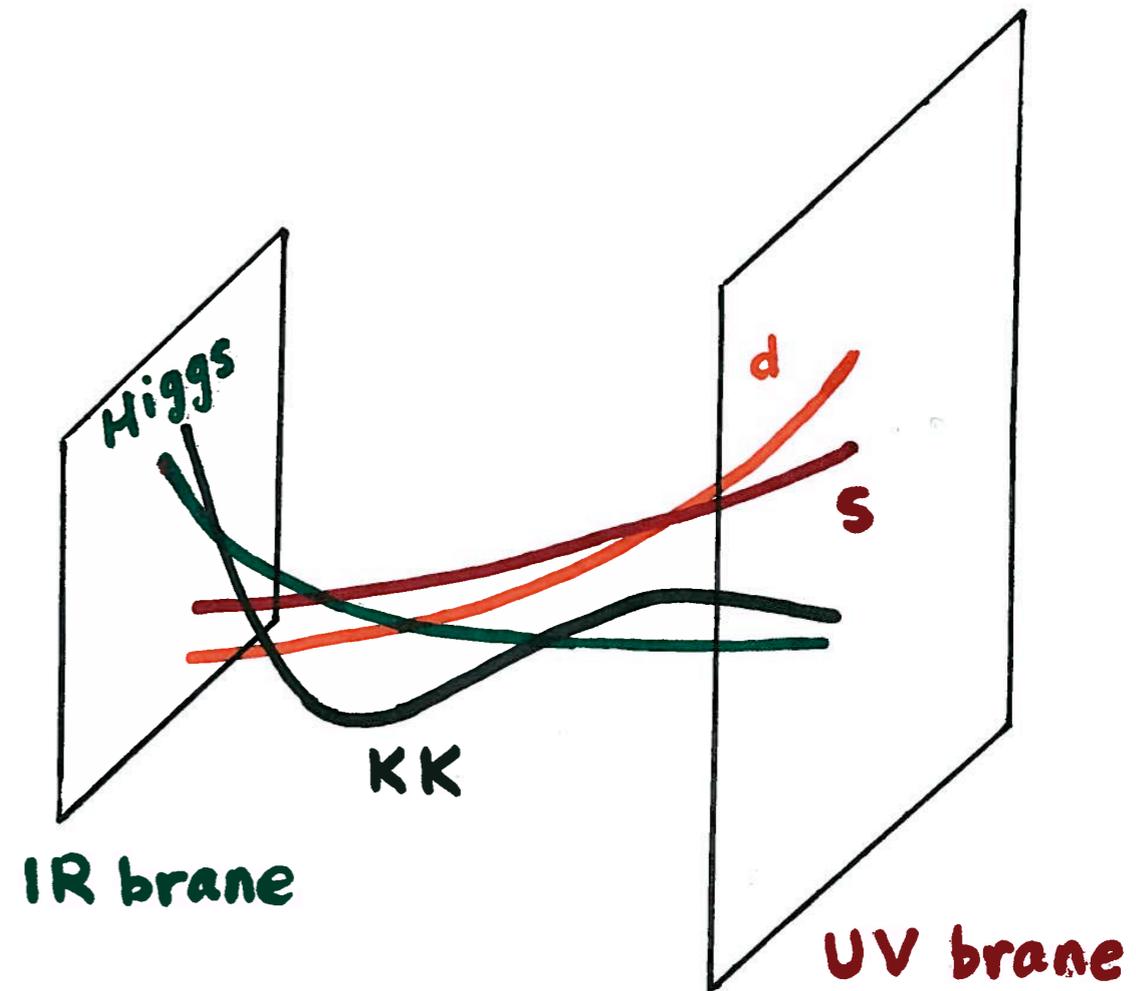


- off-diagonal in mass basis (in general):

$$\dots D_L^\dagger \text{diag} (g_d^{KK}, g_s^{KK}) D_L \dots \rightarrow (g_s^{KK} - g_d^{KK}) (D_L)_{12} \times \bar{d}_{L \text{ mass}} \gamma^\mu A_\mu^{(n)} s_{L \text{ mass}}$$

Warped **GIM**: built-in suppression mechanism...

- **Non**-universality in gauge KK coupling \propto (difference of) 4D Yukawa:
Higgs profile \sim KK
(Gherghetta, Pomarol; Huber, Shafi; KA, Perez, Soni)



- Mixing angles $\sim \sqrt{\frac{m_d}{m_s}}$
➔ **O(TeV)**-scale new physics still alive (**not** in flat)!

Summary (rough) of quark and lepton sectors:

warped GIM, but 1 or 10 TeV?

- $\sim O(10)$ TeV from ϵ_K (Csaki, Falkowski, Weiler) and from LFV including **neutrino** mixings (Perez, Randall; KA)

...but...

- room from **multiple** " $O(1)$ " factors: e.g. Higgs **profile**/size of 5D Yukawa for **quarks** (KA, Azatov, Zhu: see talk by A. Azatov); "decoupling" neutrino mixing from charged **leptons** using Dirac (KA, Okui, Sundrum) or **new** $SU(2)_R$ representations (KA) $\longrightarrow \sim O(5)$ TeV allowed
- **flavor symmetries** (Fitzpatrick, Perez, Randall; Santiago; Csaki, Falkowski, Weiler; Csaki, Grossman, Perez, Surujon, Weiler); **smaller** than Planck-weak UV-IR hierarchy (Davoudiasl, Perez, Soni) for **parametric** suppression

About “ $\sim \bigcirc$ ” in $\sim \mathcal{O}(5 \text{ or } 10) \text{ TeV}$

...due to...

- “ $\sim \dots$ ” : soft wall etc. like for EW precision tests
- “ $\bigcirc \dots$ ” : **scan** over 5D Yukawa entries (**intrinsic** to solution to flavor puzzle) \Rightarrow **mild** tuning allows lower KK scale (Blanke, Buras, Duling, Gori, Weiler)

anarchic

$$4\text{D Yukawa} \propto \text{LH profiles} \times \begin{pmatrix} 1 & 2e^{i\pi/3} & 1/3e^{-\pi/4} \\ 3i & -1 & \dots \\ \dots & 1/2 & \dots \end{pmatrix} \times \text{RH profiles}$$

hierarchical

Other sources of flavor violation

- **Higgs** exchange: see talk by **L. Zhu**
- **Radion** (“fluctuations of size of extra dimension”) exchange: see talk by **M. Toharia**

Don't give up on ~ 3 TeV
KK scale!!!

LHC SIGNALS FOR KK PARTICLES

Couplings of gauge KK's

...from profiles ($\xi \equiv \sqrt{\log(\text{UV}/\text{IR})} \sim \sqrt{\log(M_{Pl}/\text{TeV})} \sim 5$)
 Gherghetta, Pomarol; Davoudiasl, Hewett, Rizzo

$$\frac{g_{RS}^{q\bar{q}, l\bar{l} A^{(1)}}}{g_{SM}} \simeq \xi^{-1} \approx \frac{1}{5},$$

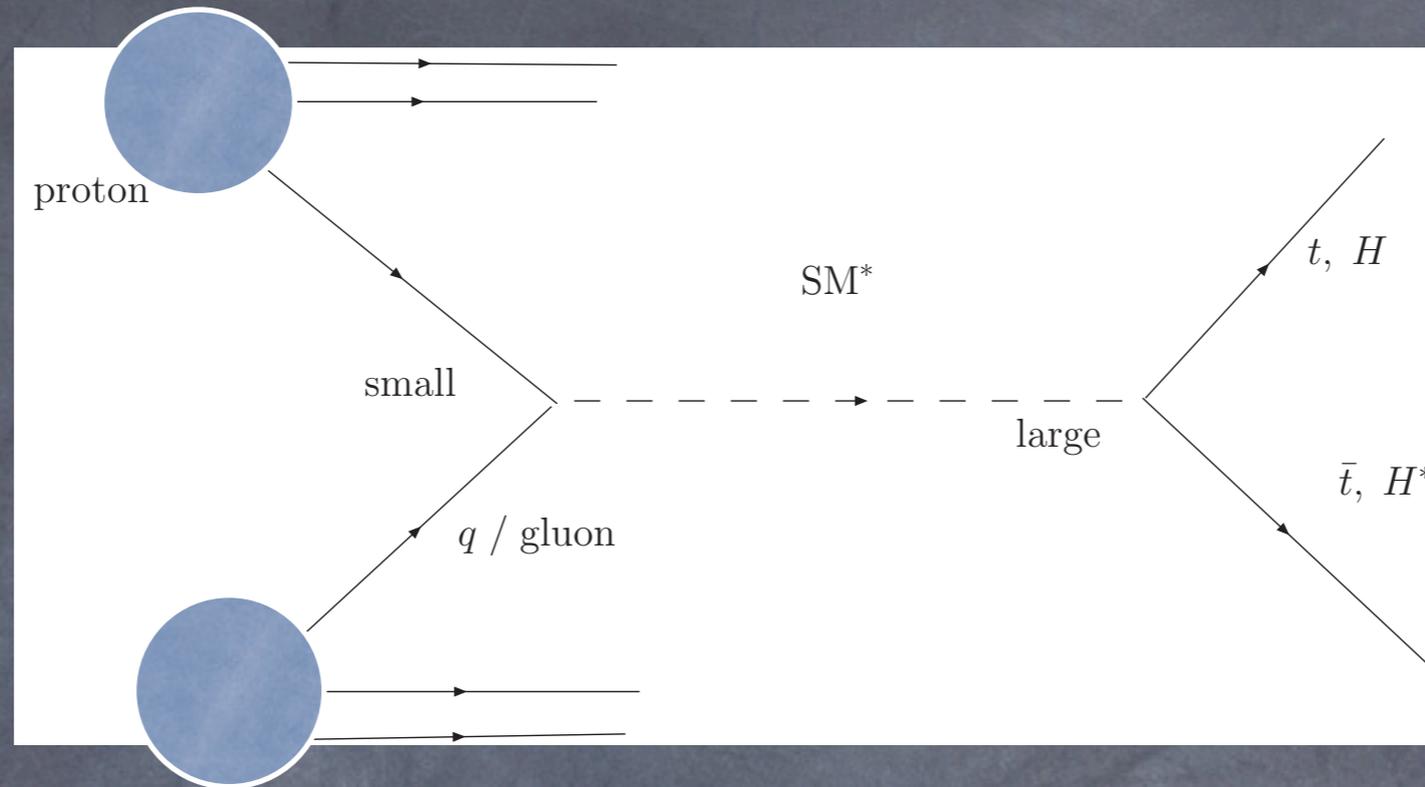
$$\frac{g_{RS}^{Q^3 \bar{Q}^3 A^{(1)}}}{g_{SM}}, \frac{g_{RS}^{t_R \bar{t}_R A^{(1)}}}{g_{SM}} \simeq 1 \text{ to } \xi \approx 1 \text{ to } 5,$$

$$\frac{g_{RS}^{HH A^{(1)}}}{g_{SM}} \simeq \xi \approx 5,$$

$$\frac{g_{RS}^{A^{(0)} A^{(0)} A^{(1)}}}{g_{SM}} \simeq 0$$

Model-independent approach: Contino, Kramer, Son, Sundrum;
 Giudice, Grojean, Pomarol, Rattazzi

Composite/Warped SM @ LHC: 3 strikes...



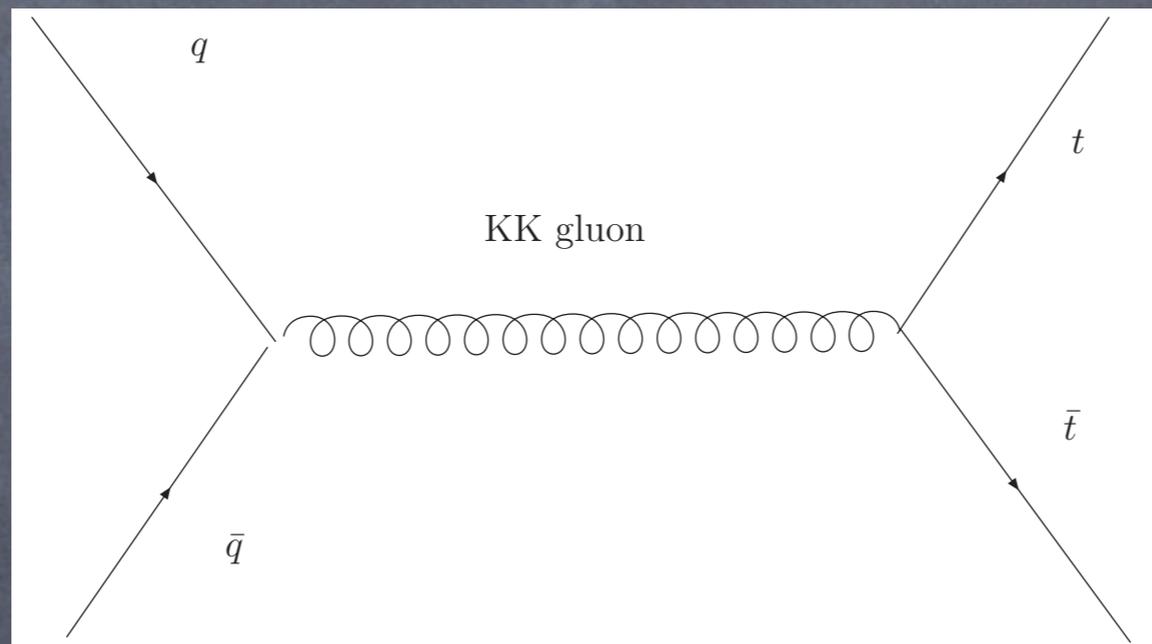
- Production suppressed: weak coupling to constituents of **proton**
- Decays to top/W/Z/Higgs: **golden** channels (leptons, photons) **suppressed**
- Strong coupling \Rightarrow **broad** resonances
...but **not** out!

KK gluon (and boosted tops)

(KA, Belyaev, Krupovnickas, Perez, Virzi)

(See also Lillie, Randall, Wang; Lillie, Shu, Tait;
Guchait, Mahmoudi, Sridhar; Djouadi, Moreau, Singh; Baur, Orr; Bai,
Han; Kumar, Tait, Vega-Morales; Evans, Luty ...+ talk by K.
Kumar)

Production and Decay

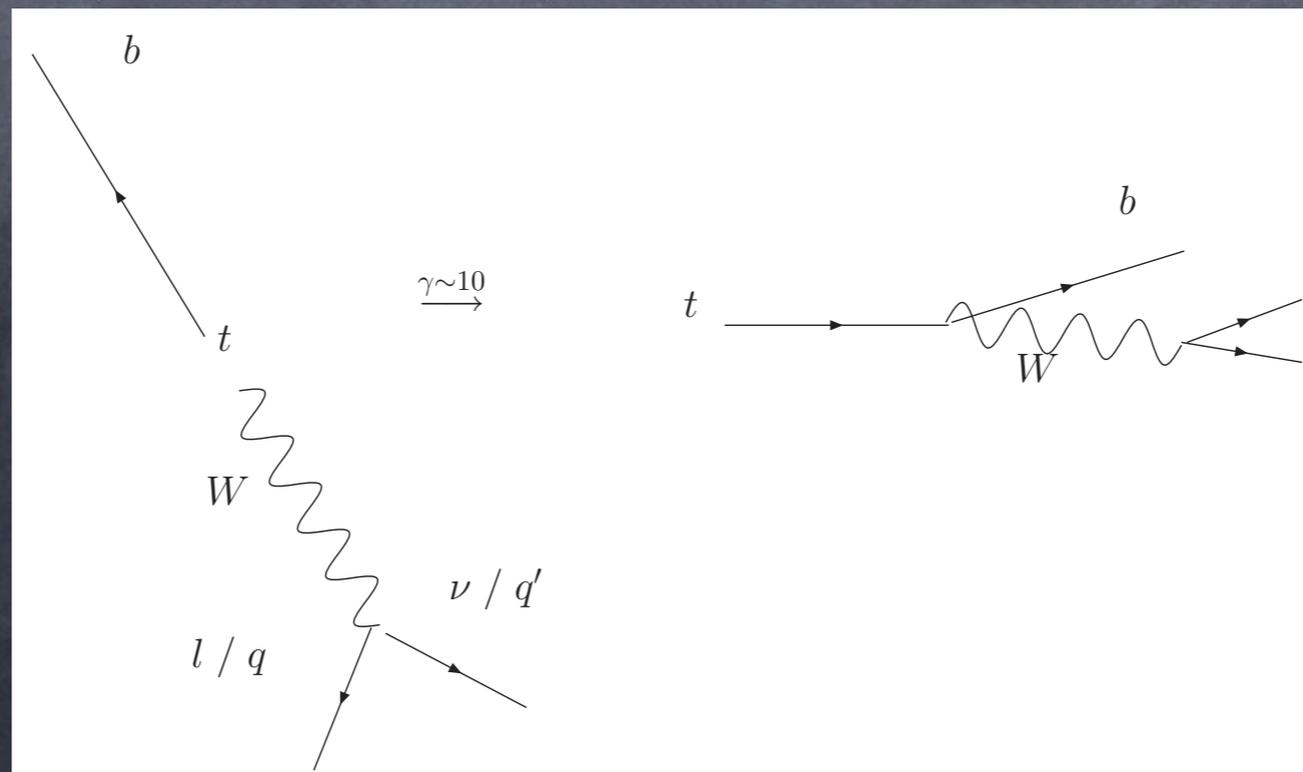


Problem: collimation of tops

- opening angle $\sim m_t/E \sim 0.1$

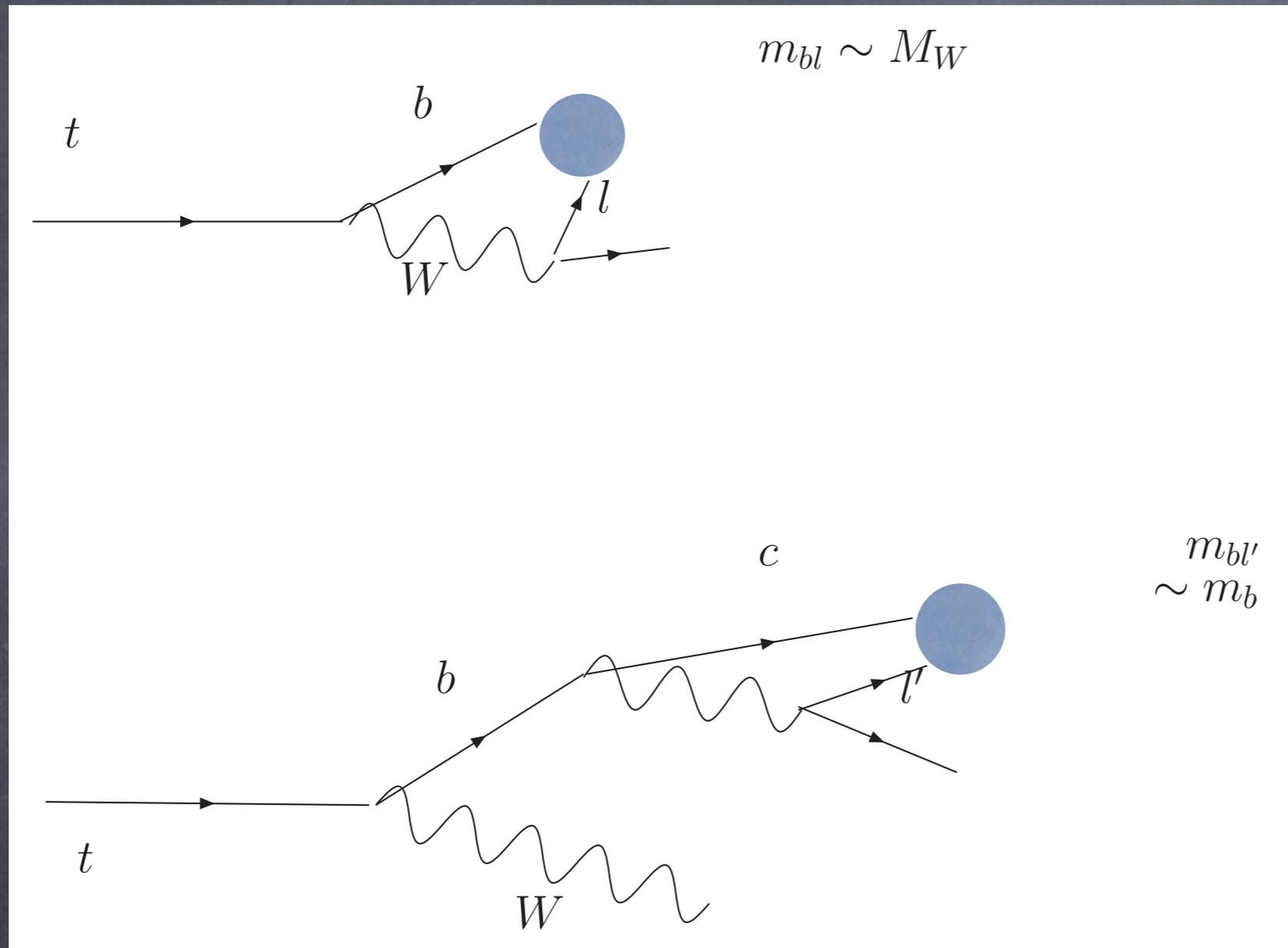
vs.

usual $\Delta R \gtrsim 0.4$ between lepton and b-jet and 2 jets from W



Solution: cut on lepton-b invariant mass

- Improved lepton and b-jet isolation cut: $m_{bl} > 40 \text{ GeV}$



- Jet mass/substructure/event shapes (Thaler, Wang; Kaplan, Rehermann, Schwartz, Tweedie; Almeida, Lee, Perez, Sterman, Sung, Virzi...+ experimental talks/notes)...

Summary of polarization asymmetry

- SM QCD: equal LH and RH top quarks $\Rightarrow P_{LR} = 0$
- Warped extra dimension: KK gluon coupling to LH and RH top quark different $\Rightarrow P_{LR} \sim \pm O(1)$
- Measure polarization of top quark by correlating direction of **lepton** in top quark **rest** frame with direction of boost of top quark in parton **center-of-mass** frame

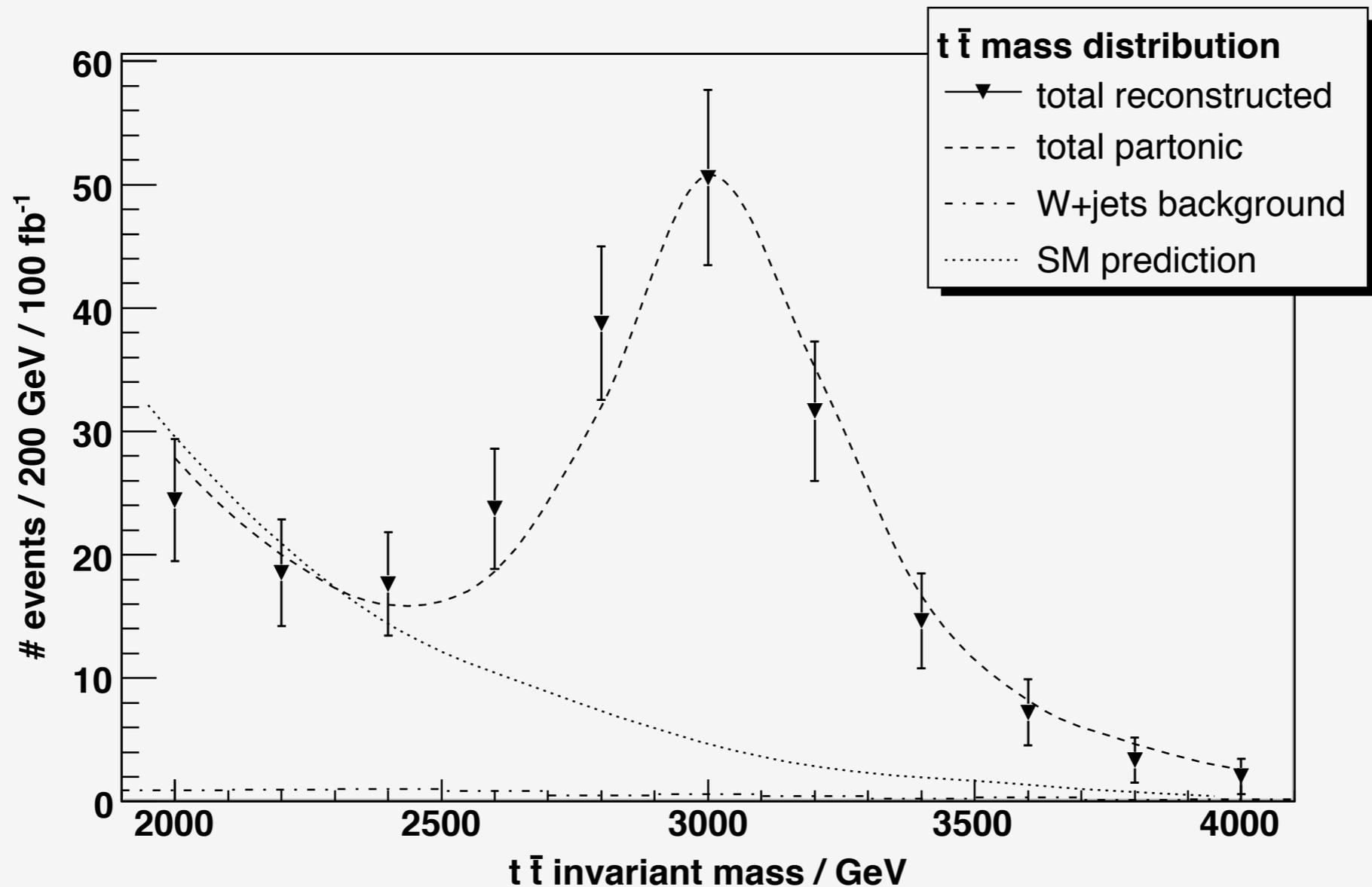
Discovery for 4 TeV with 100 / fb

- “Bump” in differential cross-section
(100 fb before 1% efficiency for 3 TeV)

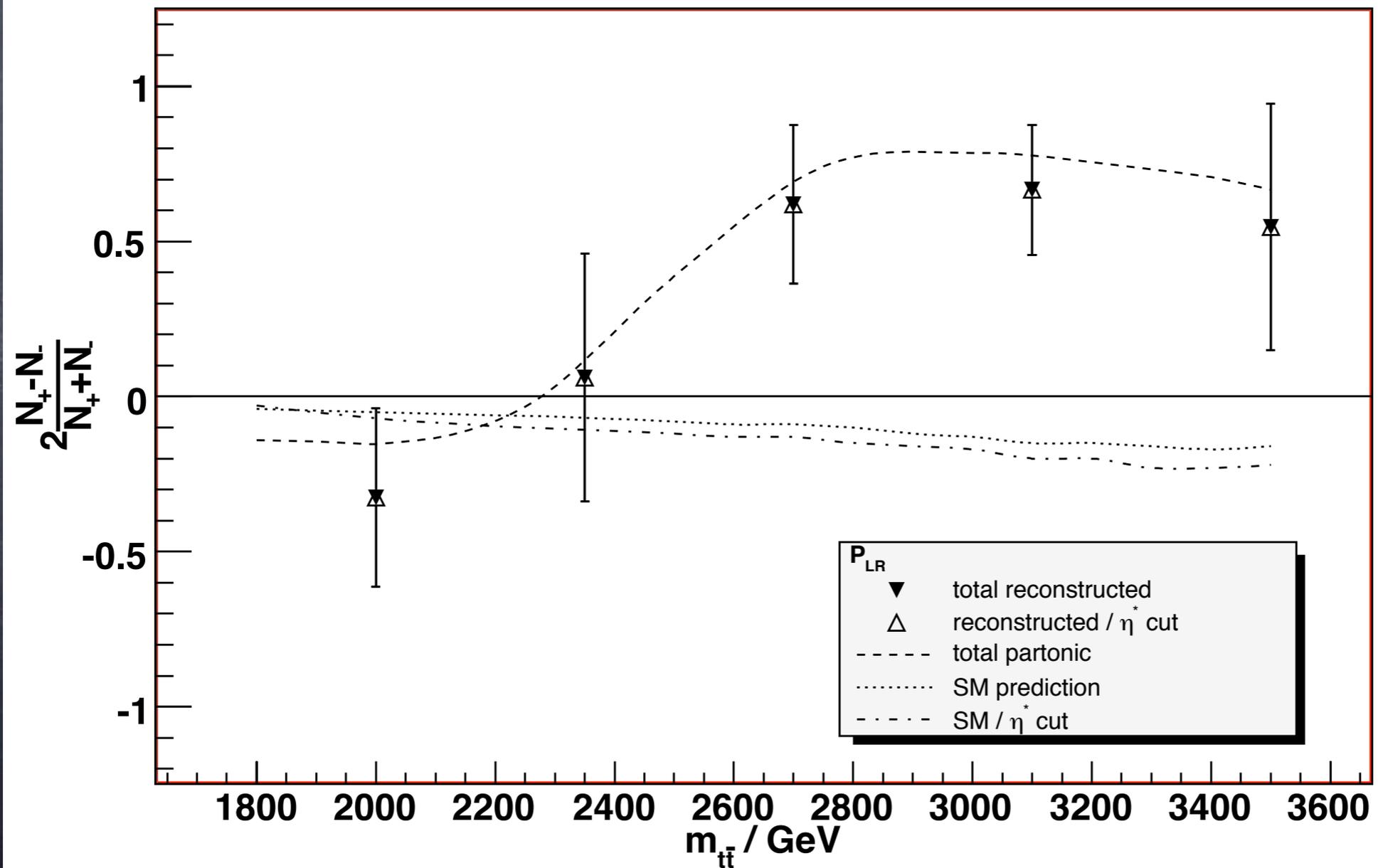
correlated with

- Deviation in P_{LR} from SM

Differential cross-section



Polarization asymmetry



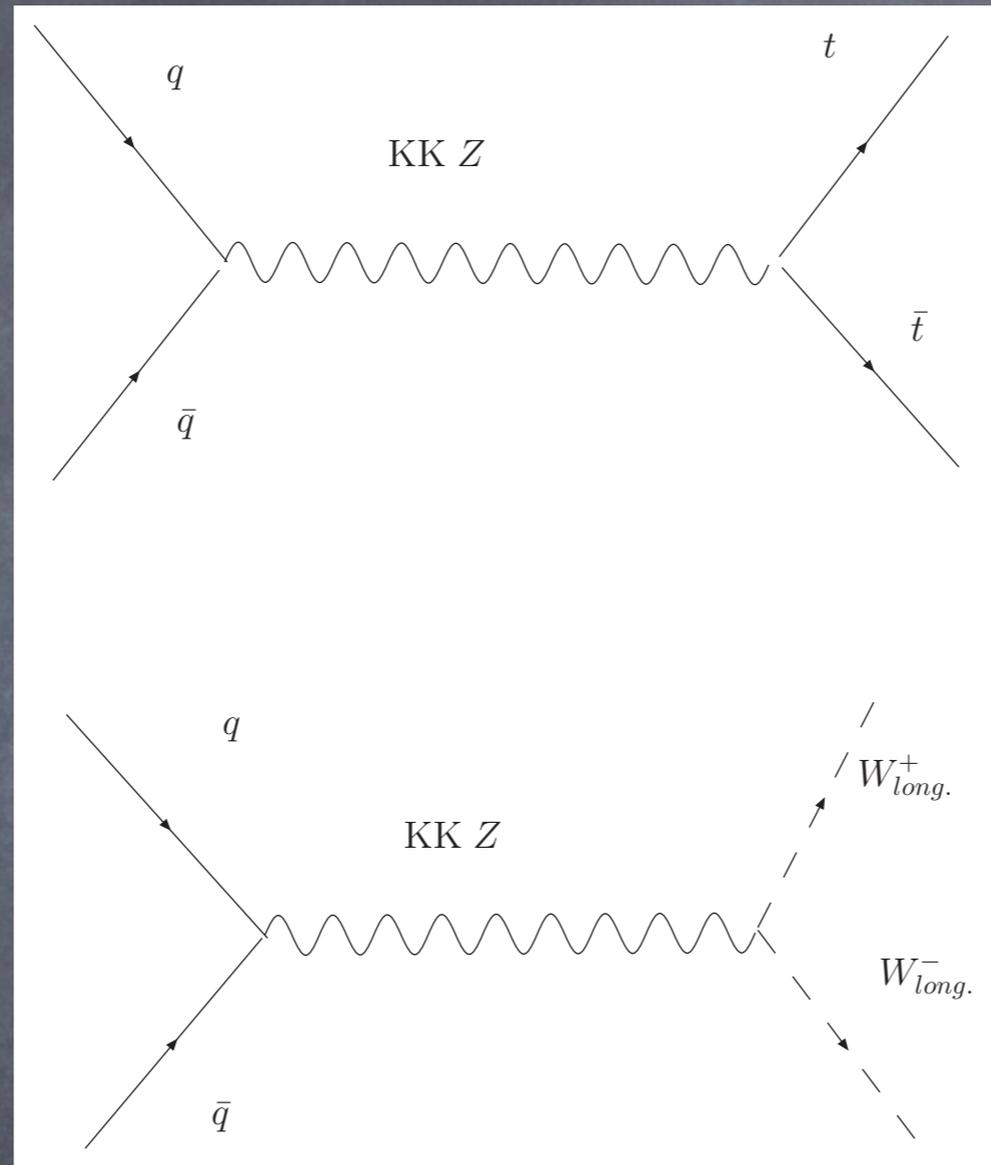
...DON'T FORGET BOOSTED
W/Z!

KK Z

(KA, Davoudiasl, Gopalakrishna, Han, Huang, Perez,
Si, Soni)

(See also Djouadi, Moreau, Singh)

Production and Decay



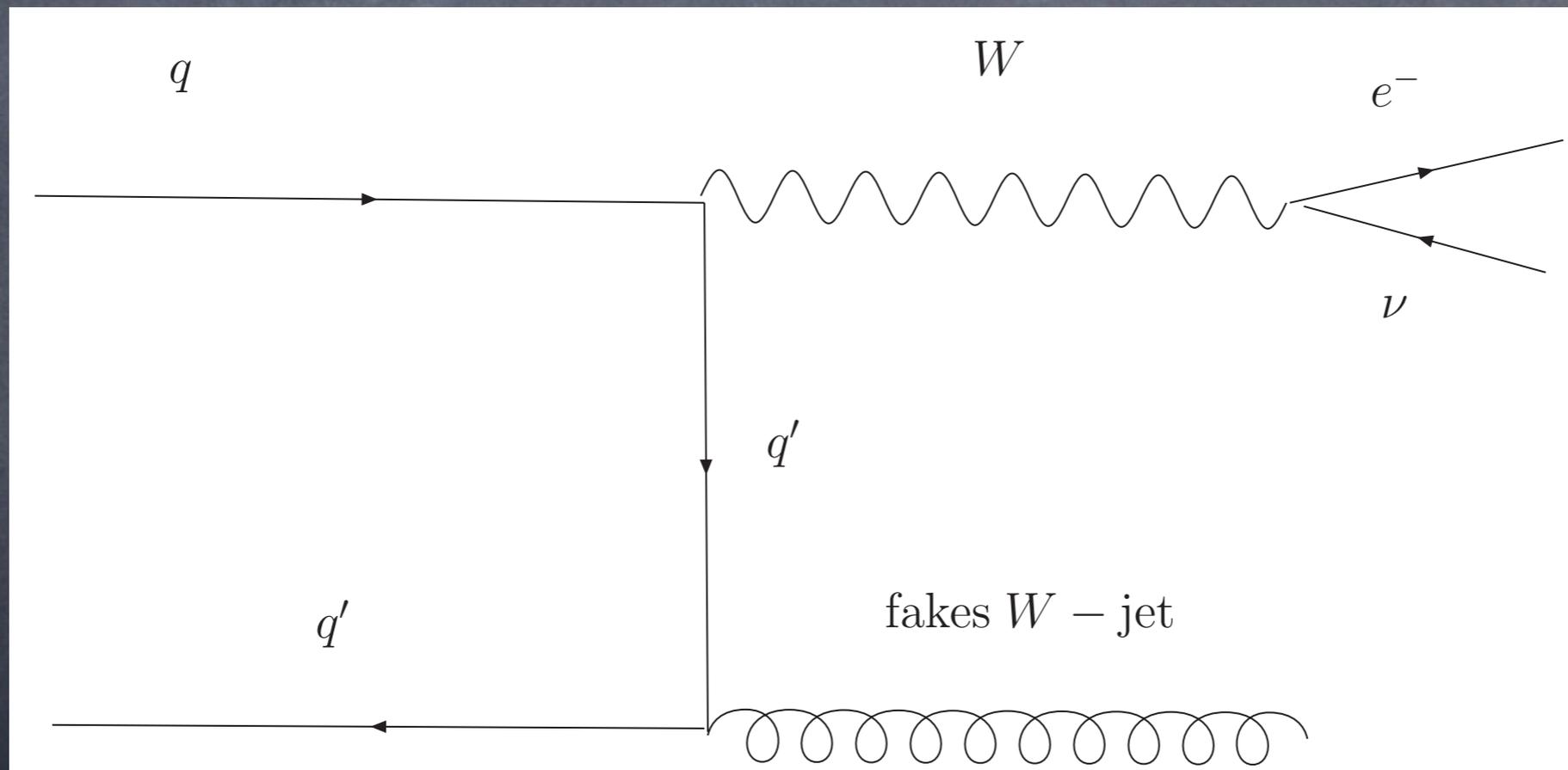
Decays to tops swamped
by KK gluon

KK $Z \rightarrow W^+W^- \rightarrow l^+l'^-\nu\bar{\nu}'$: clean, but...

- cannot reconstruct WW invariant mass
- neutrinos back-to-back

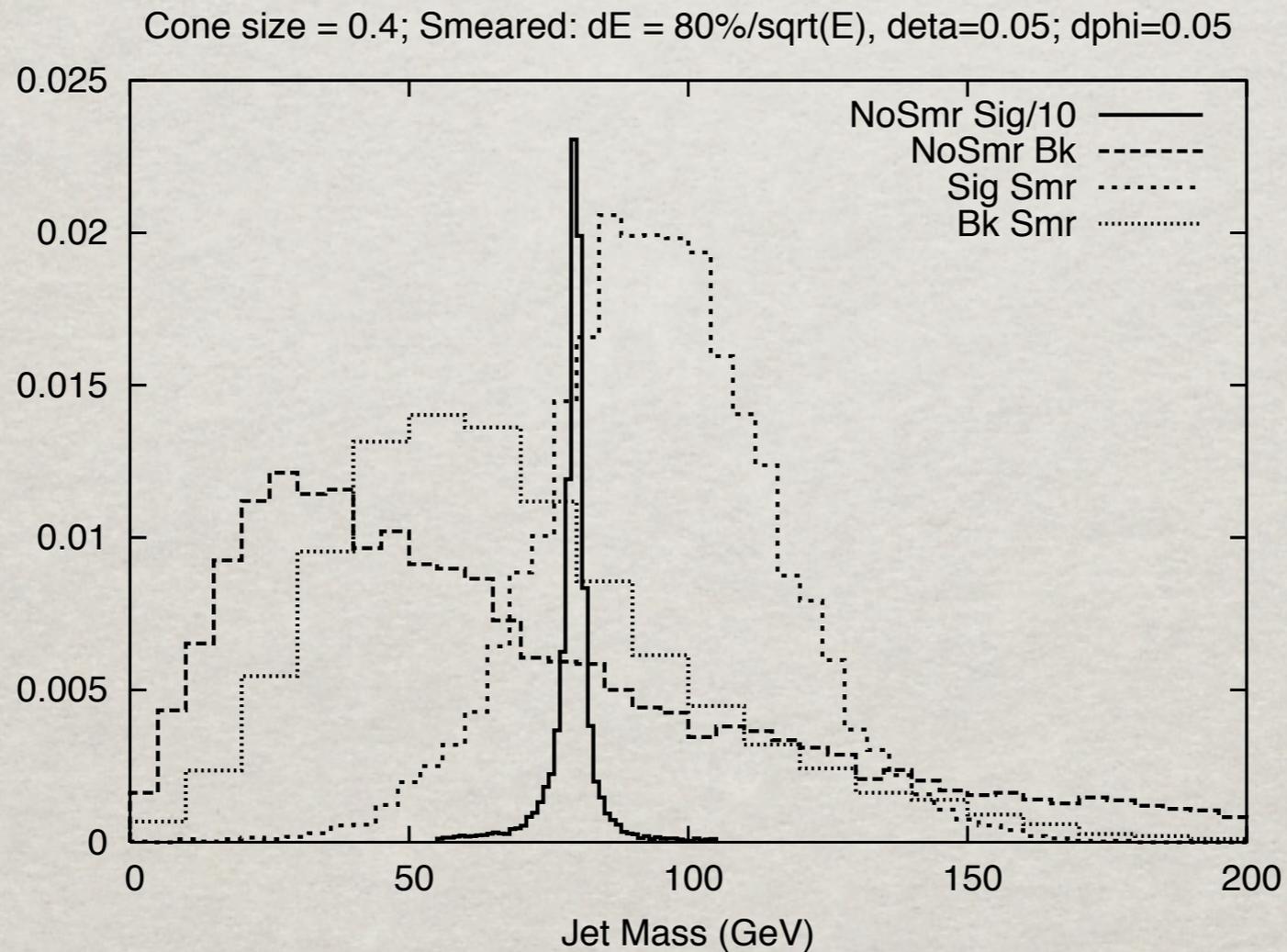
KK $Z \rightarrow W^+W^- \rightarrow l^+\nu jj$: can reconstruct, but...

- W + jet SM **background**



SOLUTION: JET MASS CUT

(SEE ALSO SMITH, SKIBA; HOLDOM; BUTTERWORTH,
COX, FORSHAW; BUTTERWORTH, ELLIS, RAKLEV;
BUTTERWORTH, DAVISON, RUBIN, SALAM...+
EXPERIMENTAL TALKS/NOTES)



Results for KK Z

- Reach of 2 (3) TeV for 100/fb (1000/fb) from semileptonic WW
- Similar from $KK Z \rightarrow Zh$

**BOOSTED TOP (VETO) AND
W/Z!**

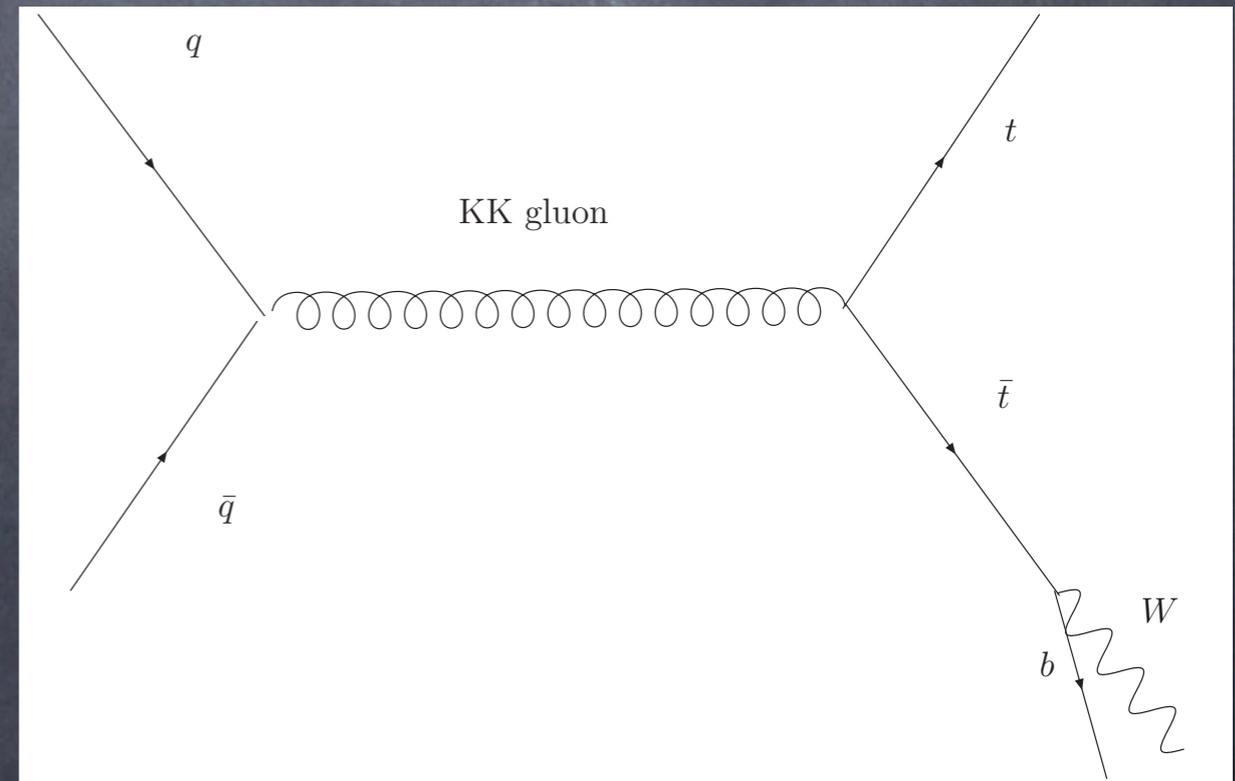
KK W

(KA, Gopalakrishna, Han, Huang, Soni)

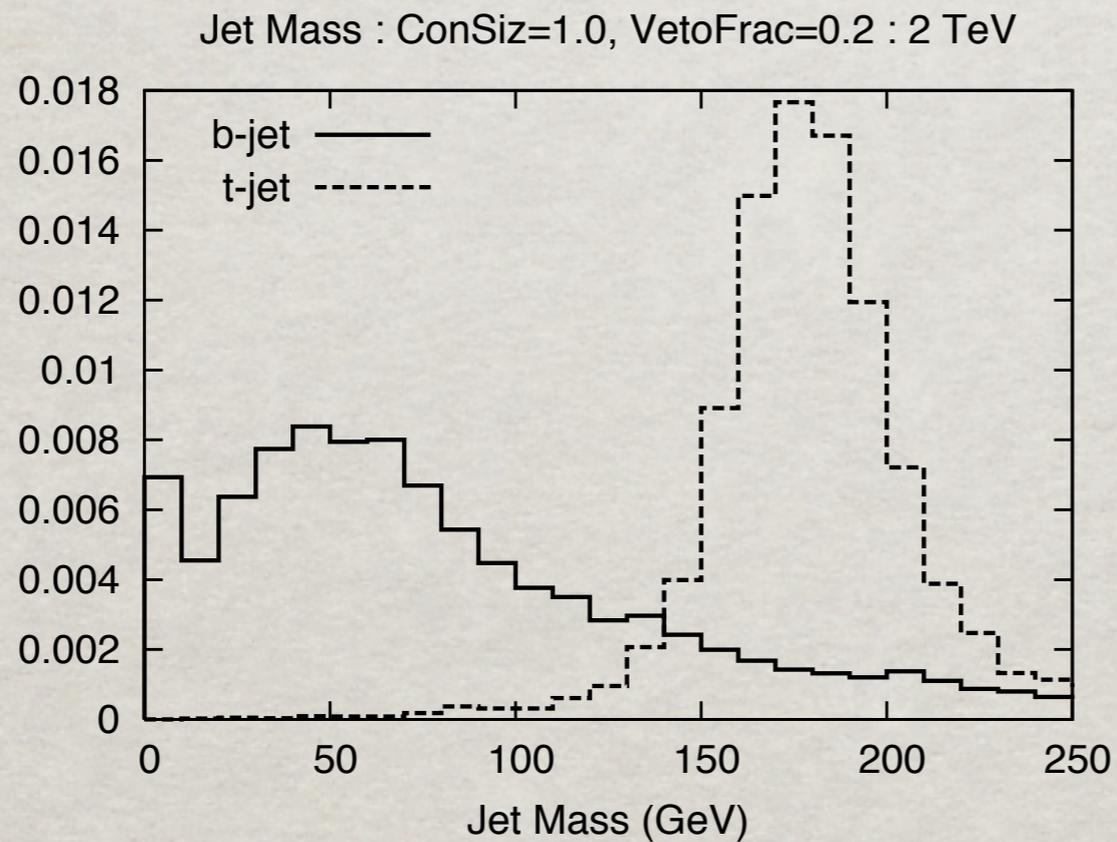
- $KK W \rightarrow WZ \rightarrow l^+ l^- l' \bar{\nu}'$
(clean) can be reconstructed

$KK W \rightarrow WZ \rightarrow l^+ \nu$ (or $l^+ l^-$) + jets
(like $KK Z$)

- Decays to top + bottom:
KK gluon background
(boosted top!)



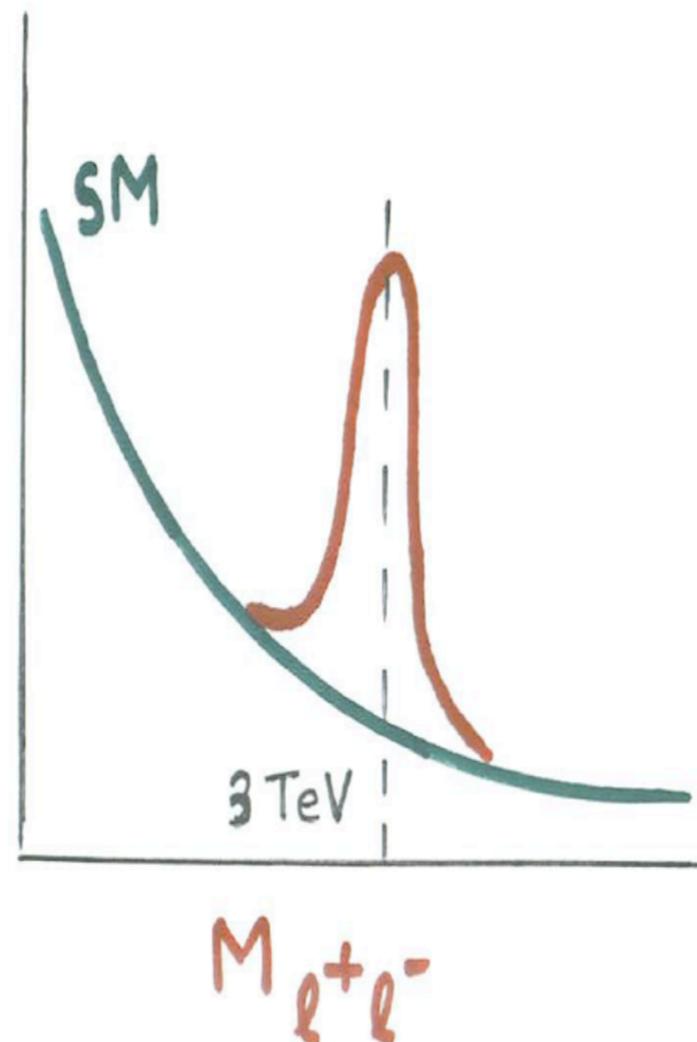
●●● REDUCIBLE BY JET MASS CUT
(BOOSTED TOP VETO!)



“ORIGINAL” RS1: BRANEWORLD

Golden decays:

KK graviton $\rightarrow l^+l^-$, $\gamma\gamma$ (Davoudiasl, Hewett, Rizzo)

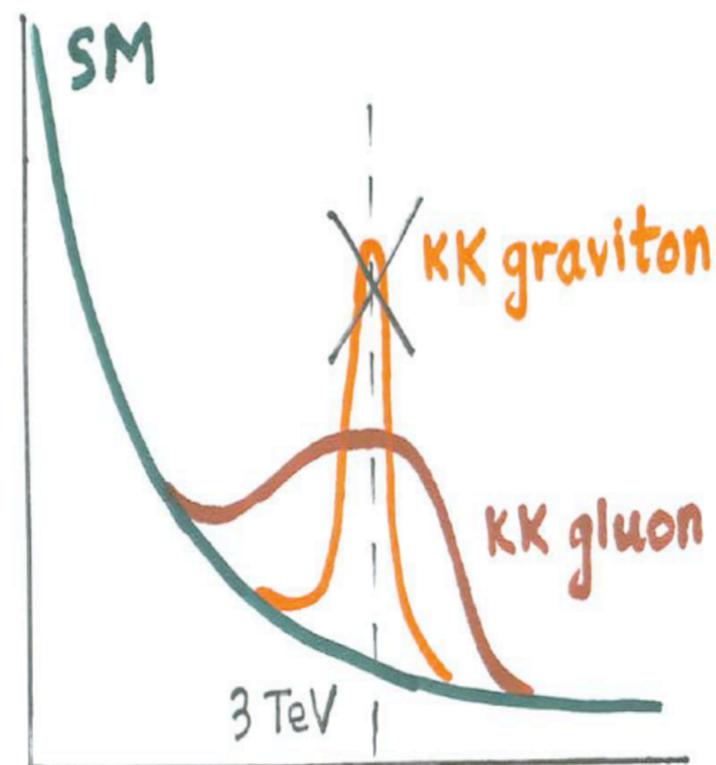


CF. SM (– HIGGS) IN THE BULK

KK graviton $\rightarrow l^+l^-$ ~~$\gamma\gamma$~~

$\rightarrow t\bar{t}, WW$ (boosted)

+ KK gluon, W, Z, γ



~~$M_{l^+l^-}$~~ $M_{t\bar{t}}$

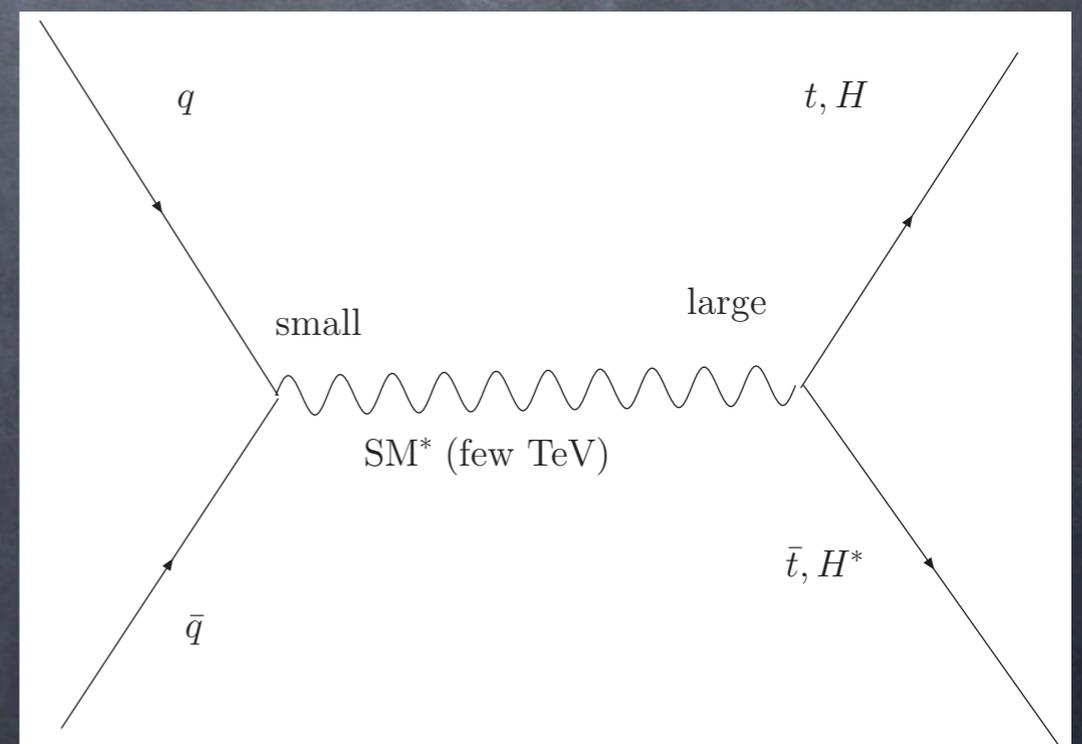
SIGNALS FOR A *CLASS* OF MODELS, *NOT* JUST WARPED EXTRA DIMENSION

Top quark and Higgs (*longitudinal W/Z*) “special”:
mechanism of electroweak symmetry breaking

couple strongly to *new* particles

- New particles couple *singly* to SM:
precision tests $\Rightarrow \sim$ a few TeV

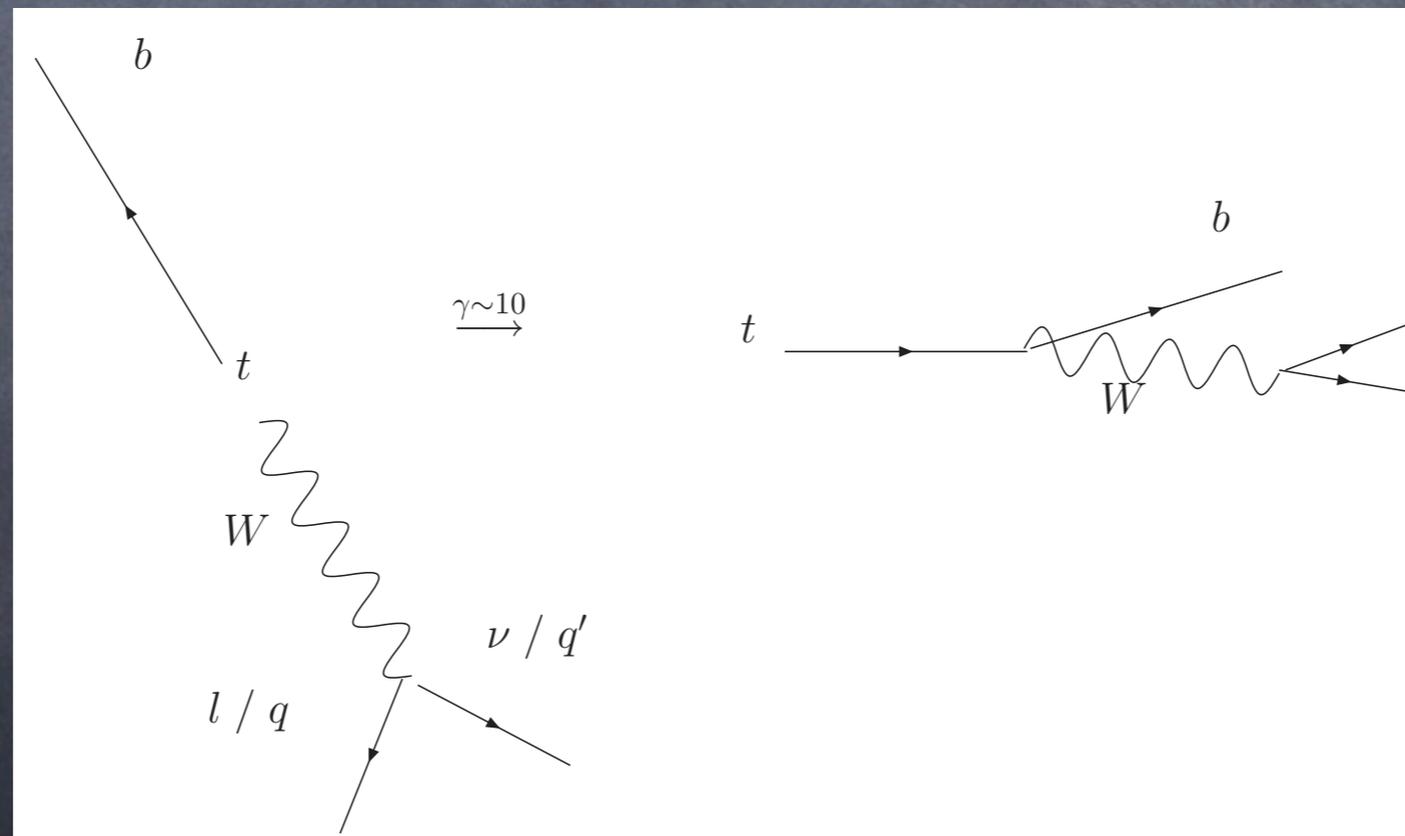
Resonance production:
decays to top and *H/W/Z*
(highly boosted!)



DETECTION OF BOOSTED ($\gamma \gtrsim 10$) TOP, W , Z , H ...

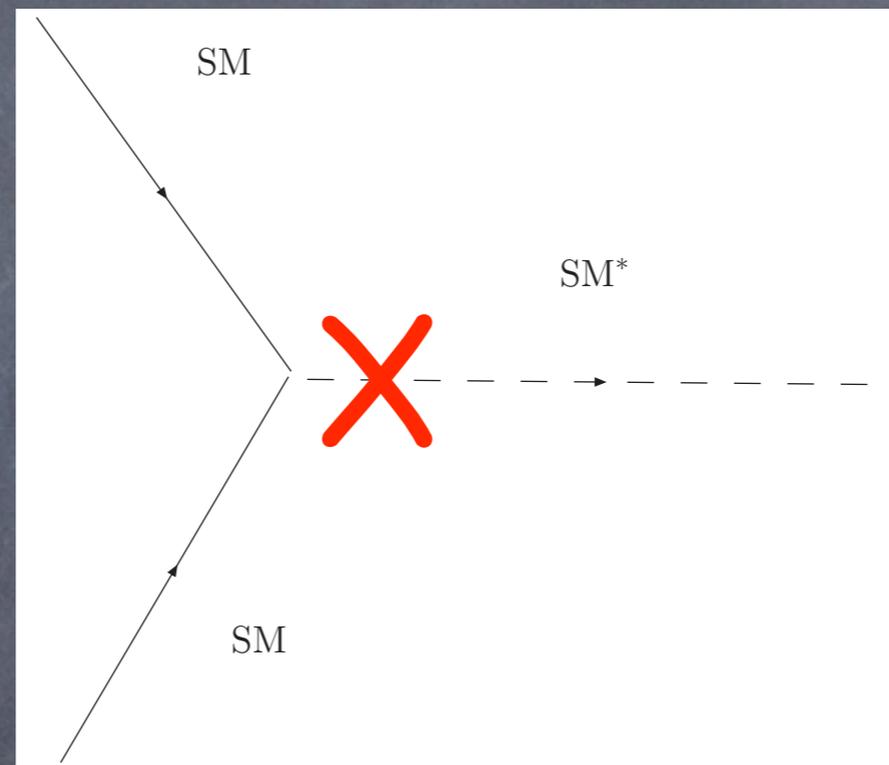
(More) Studies needed...

Detector-level simulation of m_{bl} , substructure, jet mass...



**KK PARITY IN WARPED
EXTRA DIMENSION**

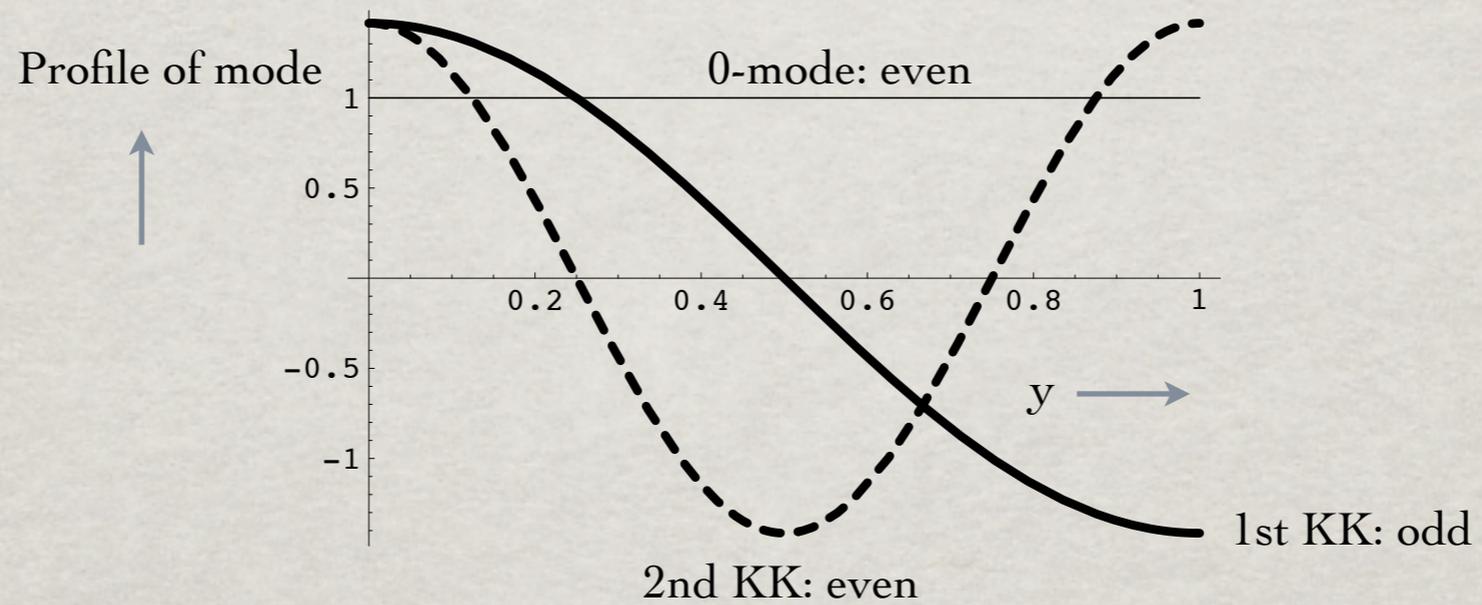
KK parity in flat universal extra
dimensions (UED),
T-parity in Little Higgs



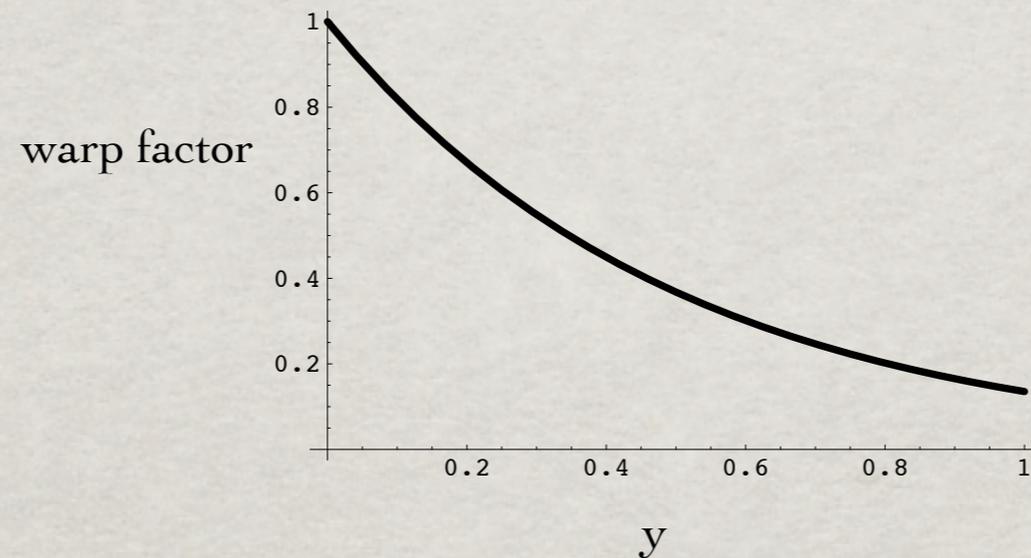
- valid only up to 10's TeV

KK PARITY IN UED

☼ Reflection about midpoint



NO KK PARITY IN SINGLE ADS SLICE

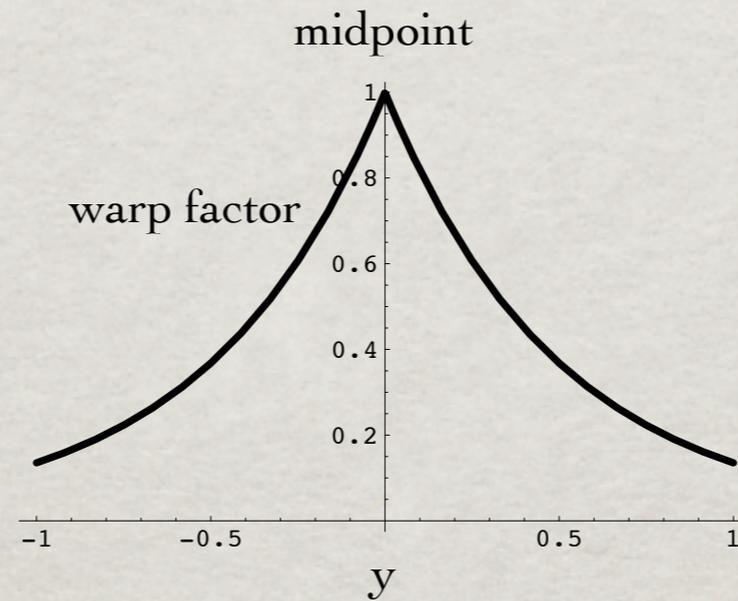


- ✱ Warp factor **not** symmetric about midpoint
(cf. **flat** metric)

JOIN 2 ADS SLICES

(KA, FALKOWSKI, LOW, SERVANT)

(SEE ALSO THALER, YAVIN; PANICO, PONTON, SANTIAGO, SERONE; CSAKI, HEINONEN, PERELSTEIN, SPETHMANN: DOUBLE FIELDS IN SINGLE SLICE)

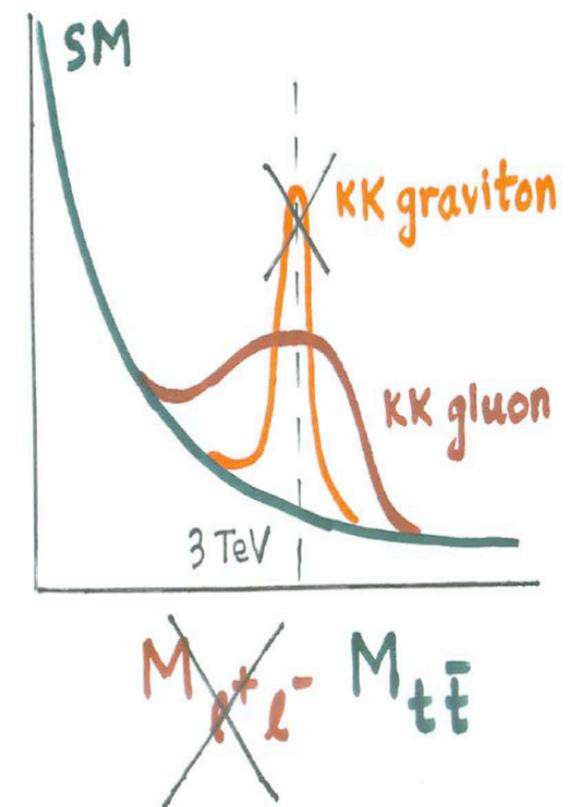


☀ KK parity interchanges 2 slices

Conclusions

- can't wait for LHC to start!
- keep open mind...

well-motivated models with
a few TeV broad resonances
decaying into highly boosted
(collimated) top/W/Z/Higgs!



Back-up slides

Warped Gauge-Higgs unification

(Contino, Nomura, Pomarol)

4D scalar

- Higgs from 5D gauge fields: $A_M = A_\mu + A_5$
- Higgs **localized** near TeV brane, potential from loops (calculable):
heavy top $\Rightarrow m_H^2 < 0$ (KA, Contino, Pomarol...)

Quark flavor constraints for anarchy

- **Non**-universality in coupling to gauge KK \propto **4D Yukawa**:
analog of **GIM** (Gherghetta, Pomarol; Huber, Shafi; KA,
Perez, Soni)

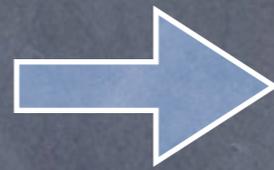
...but...

- \sim **$O(20)$** TeV from ϵ_K for Higgs **on TeV brane**, **tree**-level
matching (Csaki, Falkowski, Weiler; see also Fitzpatrick,
Perez, Randall; Davidson, Isidori, Uhlig)

...but...

Model dependence (cf. EW precision tests)...

- “O(1) room” in **each of profile** for Higgs (size of 5D Yukawa), **loop-level 5D gauge** coupling (not so relevant for EW precision tests)...



- \sim **O(5)** TeV scale allowed **even with anarchy** by ϵ_K [**and** $b \rightarrow s\gamma$] (KA, Azatov, Zhu)
- SM uncertainties: $m_{d,s}$; matrix elements (**different** Lorentz structure than SM); also for lepton flavor violation: conversion in nuclei!

Flavor symmetries

- Mixing angles smaller by **a few** vs. "natural" size (ratio of profiles) \Rightarrow ~ 3 **TeV** allowed (even if ~ 20 TeV for natural size) \Rightarrow (mild) tuning (Blanke, Buras, Duling, Gori, Weiler)?

...or...

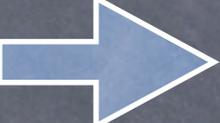
- flavor **symmetries** for **naturally** small mixing angles: relate (**same** as in anarchic) 5D mass to 5D Yukawas (**still anarchic**) (Fitzpatrick, Perez, Randall; Csaki, Grossman, Perez, Surujon, Weiler)

Lepton sector: anarchy with large

LH charged lepton mixing

- **See-saw** model (Huber, Shafi): Dirac masses (charged leptons, quarks) + Majorana masses for **RH** neutrinos on UV brane
- Large LH neutrino mixings \Rightarrow **non**-hierarchical profiles for LH leptons (cf. hierarchical for quarks with anarchy)???
- profiles as "input" (fit to data)
- LH charged lepton mixing large \Rightarrow ~ 10 TeV from lepton **flavor violation** with minimal $SU(2)_R$ representations (Perez, Randall; KA)
- \sim **$O(5)$ TeV** KK scale using **non**-minimal choice of representations (custodial symmetry: KA)

Lepton sector: flavor symmetries

- **non**-hierarchical profiles for LH leptons (cf. quarks) 
flavor symmetry (Perez, Randall; Csaki, Delaunay,
Grojean, Grossman)
- Flavor symmetries suppress flavor **violation** (see also
Chen, Yu)

Lepton sector: **decoupling** charged LH lepton mixing from neutrinos

- **Dirac** masses (KA, Okui, Sundrum) from overlap near **Planck** brane: **smallness** from Higgs profile
LH lepton profiles **small/hierarchical** near **TeV** brane, **large/non-hierarchical** near **Planck** brane
  $\sim O(5)$ TeV KK scale (with **minimal** representations:
 KA, Blechman, Petriello)
- **non-minimal** representations (KA): LH lepton "made of" **2** components (one for neutrino mass; other for charged) with **different** profiles + custodial symmetry 
- KK scale $\sim O(3)$ TeV

Cannot suppress S with non-AdS

- Hirn, Sanz: general Higgs profile and warp factor
- **Pathology**: $v_{\text{ev}}^2 < 0$ to suppress S (KA, Csaki, Grojean, Reece; see also McGuirk, Shiu, Zurek)

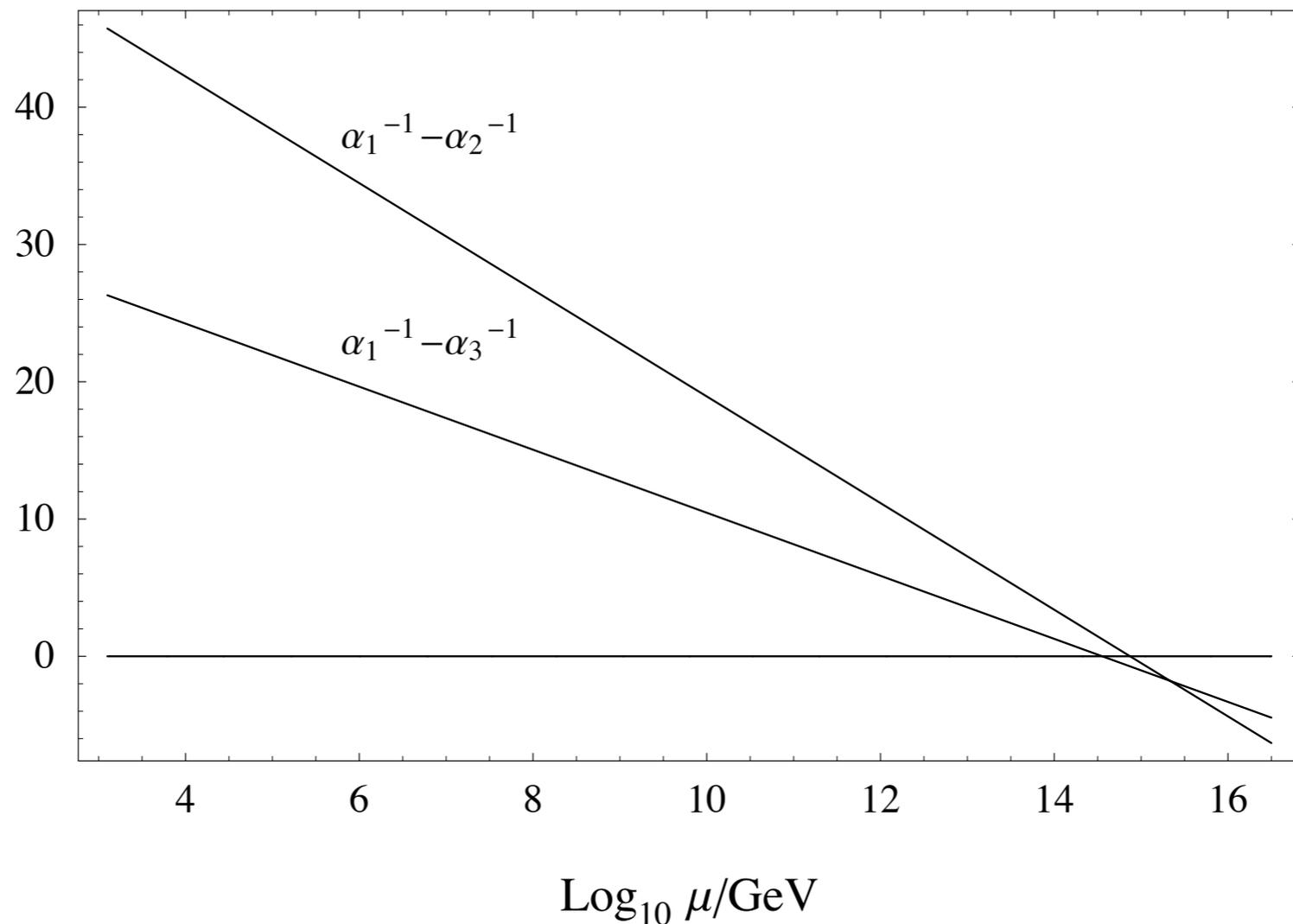
"Running" of Gauge Coupling

(Pomarol; Randall, Schwartz; Goldberger, Rothstein; KA, Delgado, Sundrum; Choi, Kim; Contino, Creminelli, Trincherini)

- **Subtle**: gauge bosons flat \Rightarrow loops span extra dimension, sensitive to Planck and TeV cut-off scales (AdS/CFT more intuitive)
- **Gauge boson** loops: non-universal; effectively cut-off at high scale (a la SM)
- **Fermion** loops non-universal (unlike SM): t_R & H (near TeV brane) loop cut-off at **TeV**; other fermion (near UV brane) loops cut-off at high scale

LO unification: **magic** of β -function: SM $-2t_R - H$

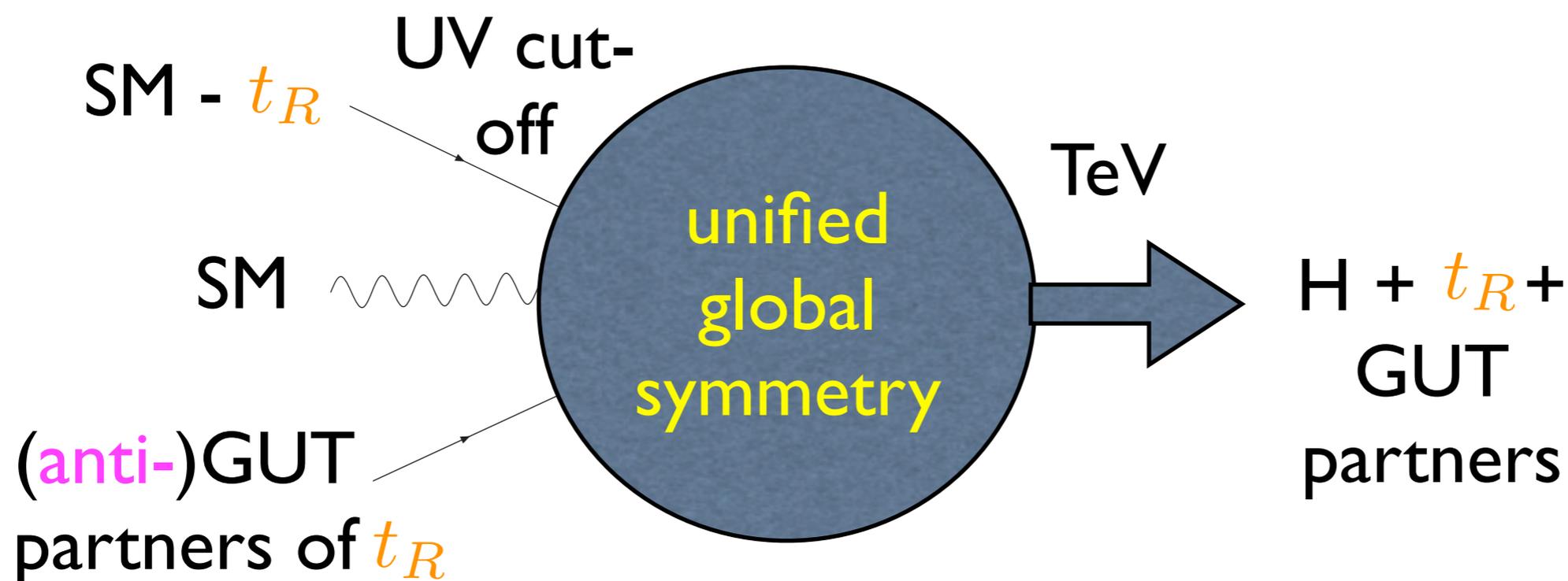
(KA, Contino, Sundrum)



(2nd $- t_R$: running due to **light** GUT partners)

Unification in CFT picture

- Global **unified** symmetry for CFT \Rightarrow LO running of SM gauge couplings from CFT loops universal
- **Composite** t_R and H \Rightarrow above TeV, replace running due to t_R and H by CFT
- Add **external** fermions to make composite GUT partners of t_R heavy



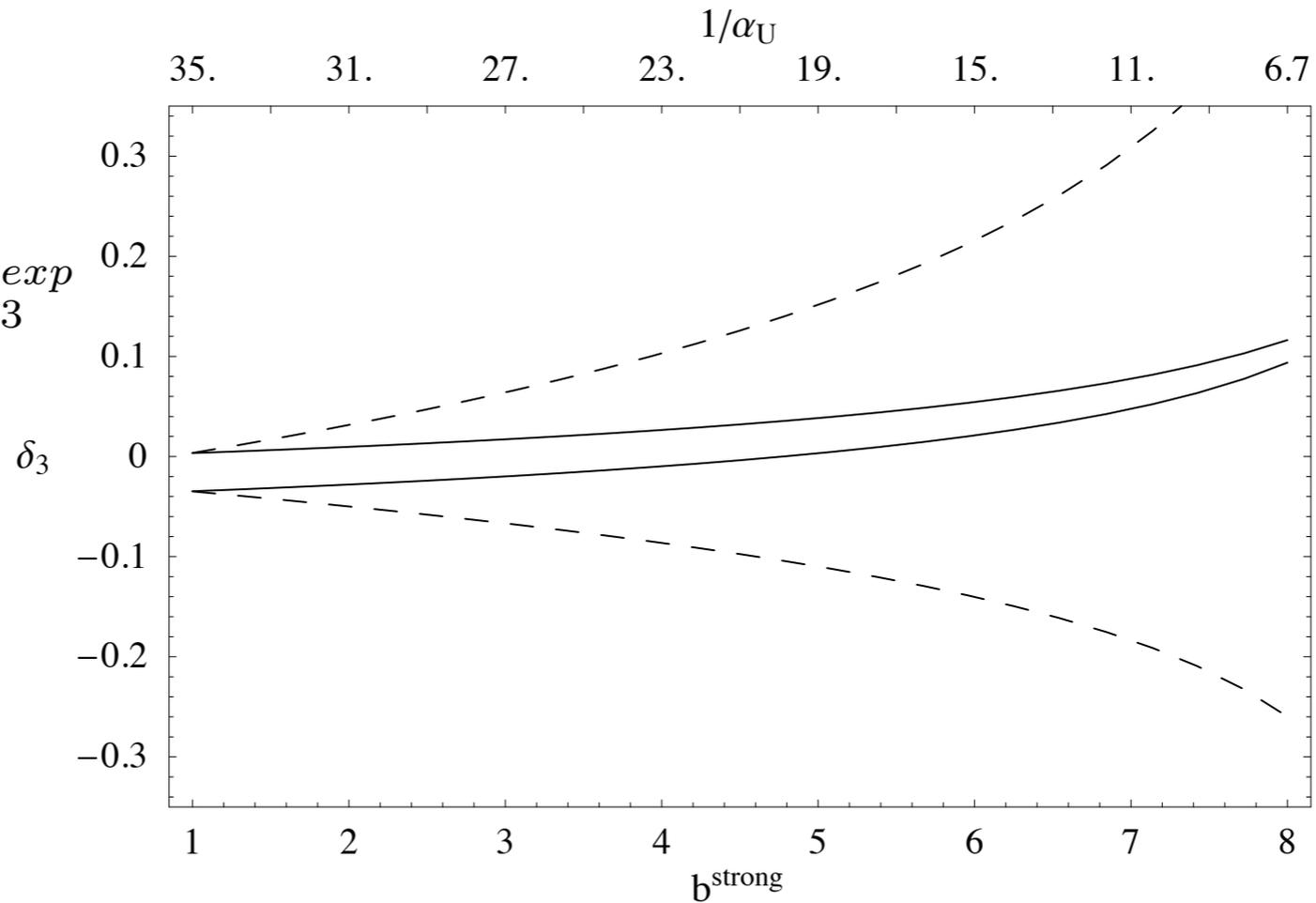
Assumptions

- Bulk **unified gauge** symmetry \longleftrightarrow CFT has **global** unified symmetry
- Localization parameter (bulk mass) of t_R :
unification improved relative to SM in **entire**
range (preferred by precision data); **precision**
unification for sizable range

NLO precision \sim SUSY

$$\delta_3 = \left(\alpha_3^{theory} - \alpha_3^{exp} \right) / \alpha_3^{exp}$$

~ 0.1 in SUSY
(α_3 at M_Z)



(size of 4D strong sector)

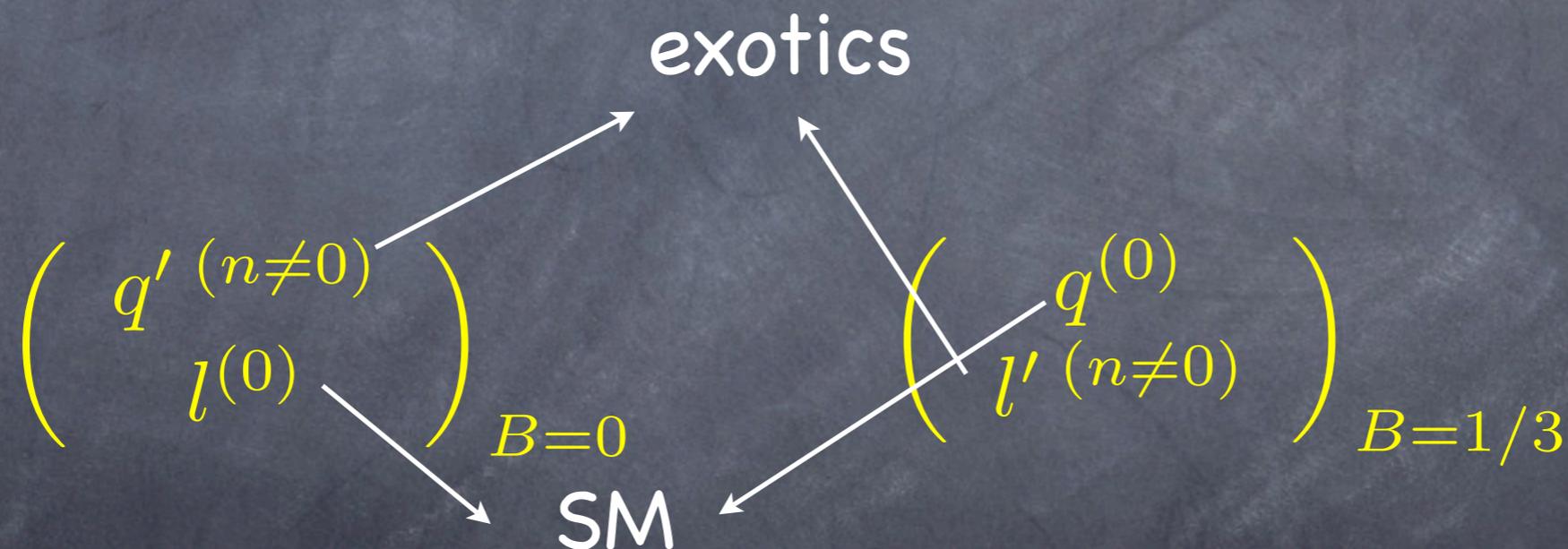
→ Landau pole
below GUT
scale

Signals

- **Complete** GUT multiplets at few TeV scale (KK gauge bosons and fermions)
- **light** GUT partners of t_R for precision unification

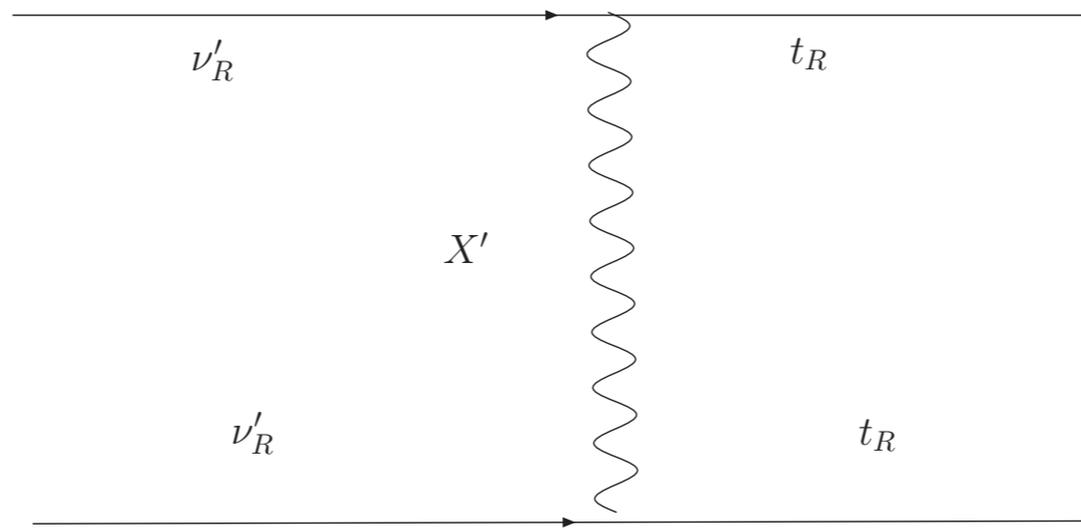
Stable particle from Proton stability (KA, Servant)

- Orbifold GUT's (GUT breaking on boundary: Hall, Nomura): quark and lepton zero-modes from different multiplets; assign multiplets baryon-number of zero-mode (split multiplets for proton stability)

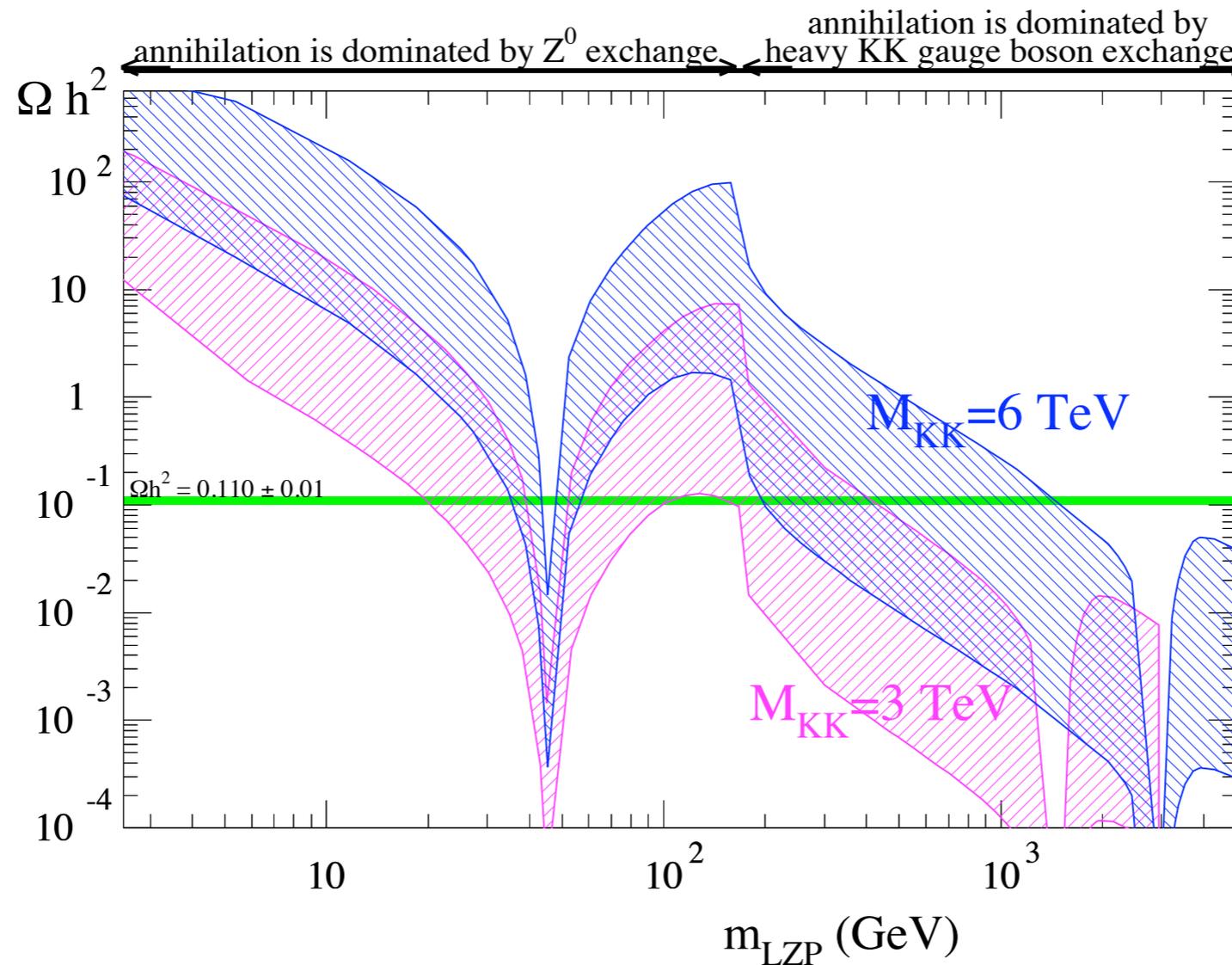


- Extra particles (no zero-modes) are "exotic" ("wrong" combination of B and color: SM have right...) \Rightarrow lightest stable

Exotic ν'_R partner of t_R as **WIMP** dark matter: I

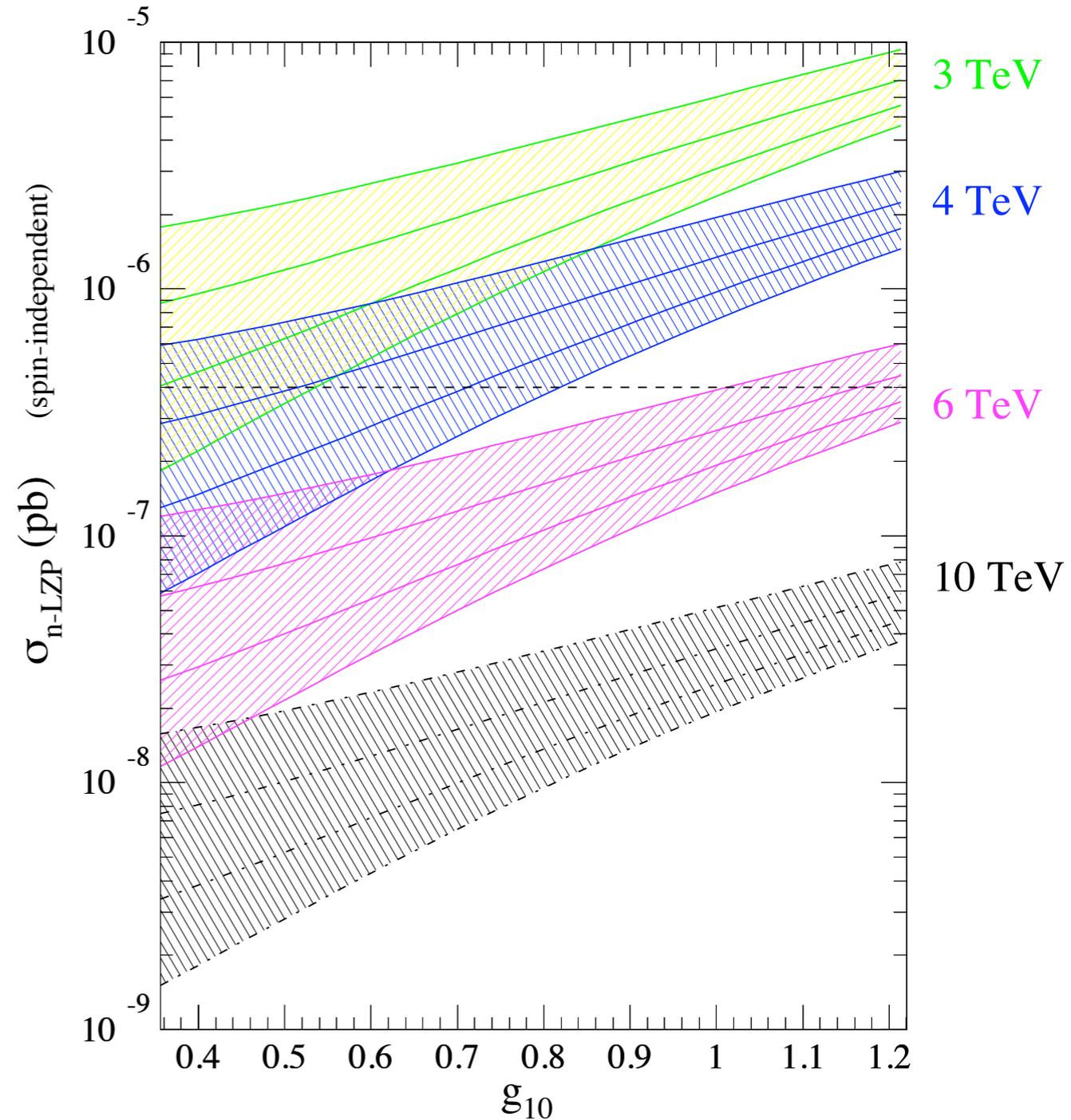
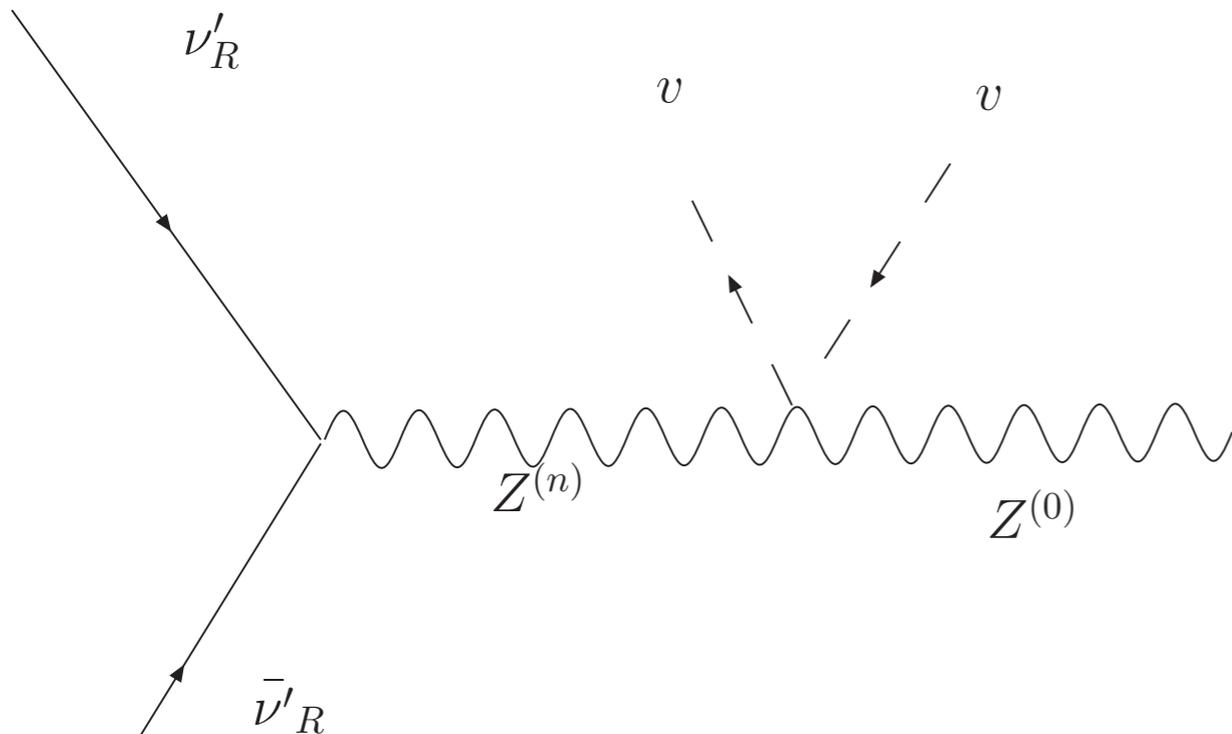


- **Annihilation:**

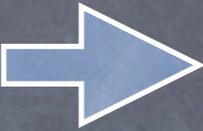


Exotic ν'_R partner of t_R as **WIMP** dark matter: II

- Direct detection (**small** coupling to Z):



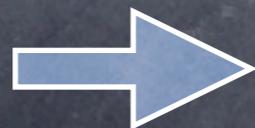
Polarization asymmetry: definition

- Positron in direction of top spin 
"forward-backward" asymmetry

$$P_{LR} \equiv 2 \times \frac{N_+ - N_-}{N_+ + N_-}$$

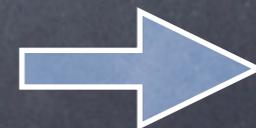
RH (LH) top: $P_{LR} = \pm 1$

LH top



t spin

RH top



t spin



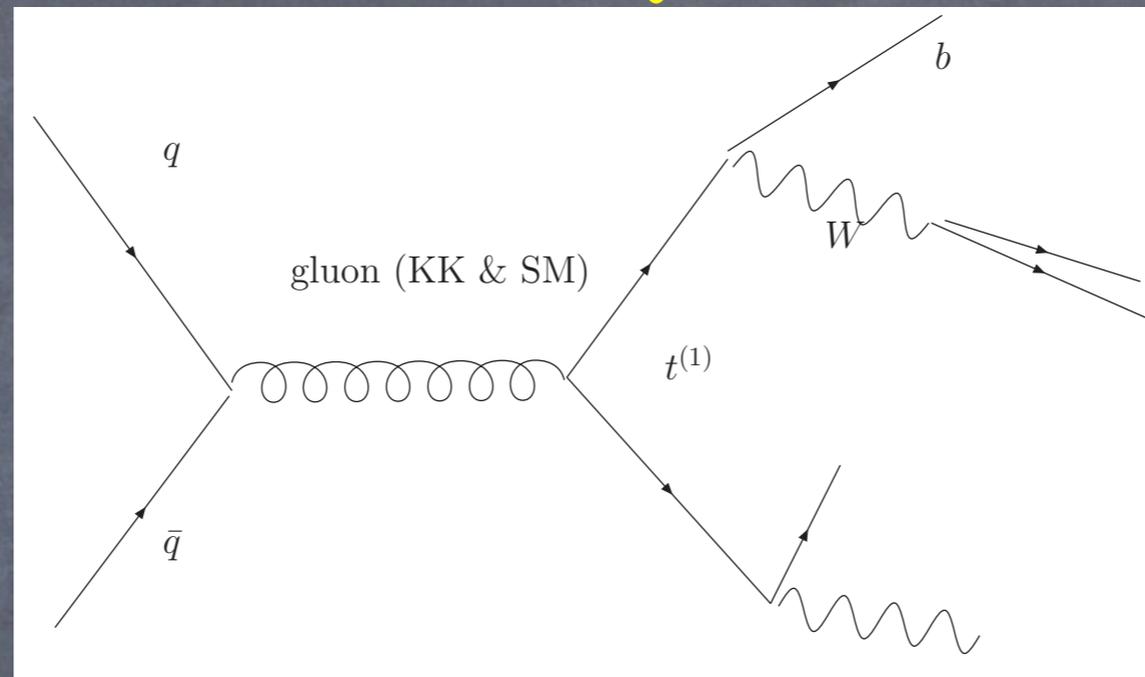
Polarization asymmetry: SM vs. Warped

• SM: $P_{LR} \sim g_Z^4 / g_{QCD}^4$ and < 0
(pure QCD gives 0)

vs.

$O(1)$ for warped extra dimension (KK
gluon decays to RH or LH top)

KK gluon decays to KK tops



- KK tops (1 TeV) not boosted, decay into Wb (well-separated, but 2 jets from W still collimated)
(Carena, Medina, Panes, Shah, Wagner)

Other Signals

- KK graviton decays to tops, WW, ZZ: 2 to 3 TeV with 100–1000 /fb (Fitzpatrick, Kaplan, Randall, Wang; KA, Davoudiasl, Perez, Soni; Antipin, Atwood, Soni; Antipin, Soni)
- Heavy KK fermions: via KK gluon (Davoudiasl, Rizzo, Soni); via longitudinal W/Z-bottom fusion (a la in little Higgs)?
- Light KK fermions (Dennis, Karagoz Unel, Servant, Tseng; Contino, Servant; Atre, Carena, Han, Santiago: see talk by A. Atre)
- **Virtual** effects: $t \rightarrow cZ$ with BR of 10^{-5} (KA, Perez, Soni)

(+ low-energy flavor violation + DM direct detection..)

Motivation and Spectrum for warped KK parity

- Odd KK's at 1 TeV, cut off Higgs mass
- Even KK's at few TeV pass precision tests
- Lightest KK particle (LKP) stable:
Dark Matter

("Complete" models: flavor, custodial isospin...to be done)

Phenomenology

- Odd KK's **pair**-produced
- Large Brane Kinetic terms
KK **Z** Dark Matter
(cf. KK **photon** in UED)

