

# Flavour violations in type II SO(10)

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[ MF, P.Hosteins, S.Lavignac and A.Romanino, NPB 806 (2009) 84 ]

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# Outline

- **Supersymmetric Grand Unification (SUSY GUTs)** may account for non-zero neutrino masses; matter-antimatter asymmetry; dark matter; hierarchy problem; charge quantization; quark-lepton mass relations; ...
- **Type II SO(10)**: a new and predictive class of models, with no unknown flavour parameters at GUT scale
  - ▶ **Leptogenesis** directly related to neutrino parameters
- **SUSY flavour violating effects** in type II SO(10) have a specific dependence on fermion masses and mixing
  - ▶ Predictions for **BR( $\mu \rightarrow e\gamma$ )** waiting for the MEG result

# A new class of SUSY GUTs

We adopted a different route to embed the flexible SU(5) unification into the more constrained SO(10) unification:

SU(5)

$$Y_{ij}^U \ 10_i \ 10_j \ 5_U + Y_{ij}^D \ 10_i \ \bar{5}_j \ \bar{5}_D$$

type I  
SO(10)

$$Y_{ij}^U \ 16_i \ 16_j \ 10_U + Y_{ij}^D \ 16_i \ 16_j \ 10_D$$

type II SO(10)

$$Y_{ij}^U \ 16_i \ 16_j \ 10_U + Y_{ij}^D \ 16_i \ 10_j \ 16_D$$

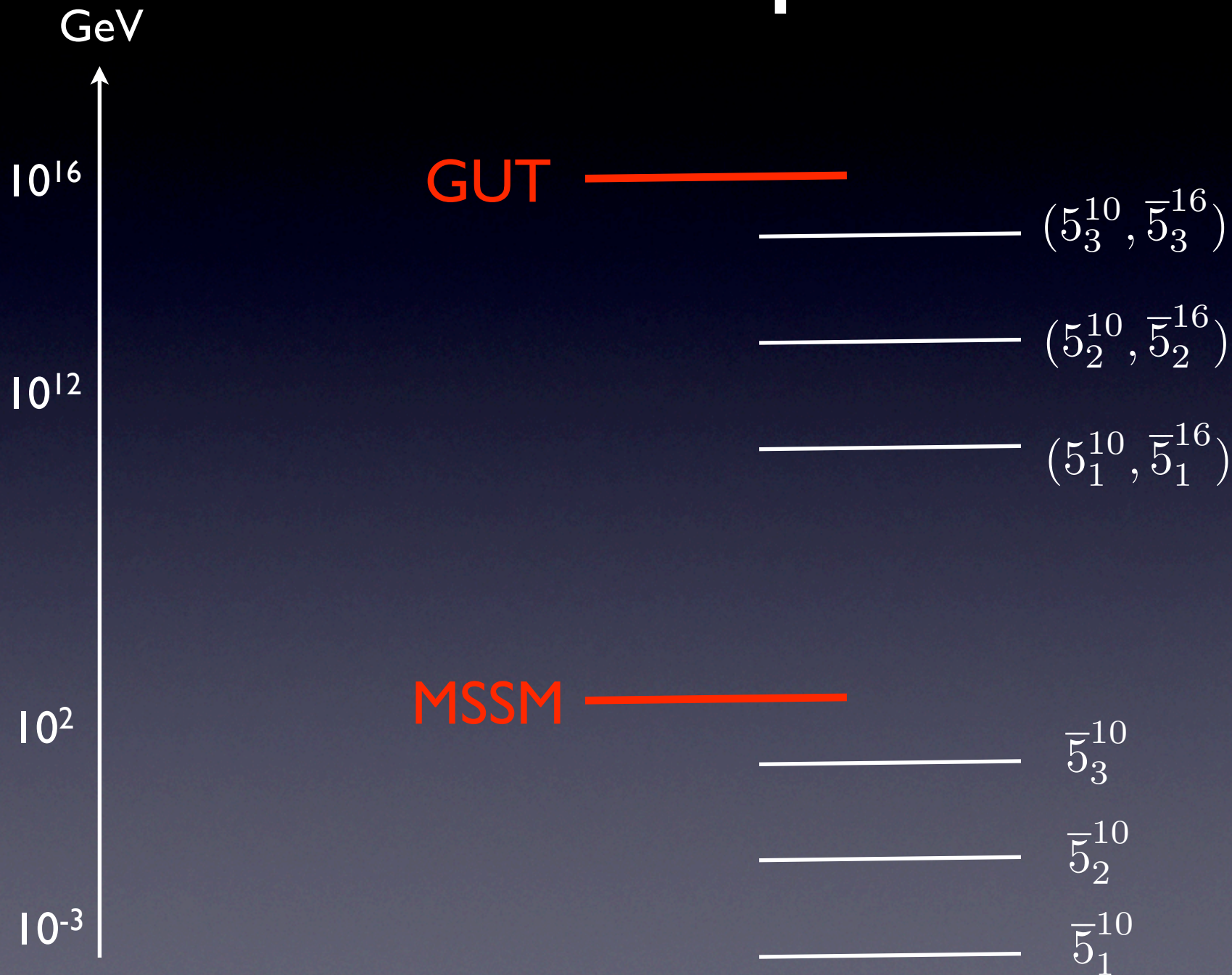
$$16 = (1 + \bar{5} + 10)_{SU(5)}$$

$$10 = (\bar{5} + 5)_{SU(5)}$$

Remarkably, the extra matter fields present in type II are automatically heavy:

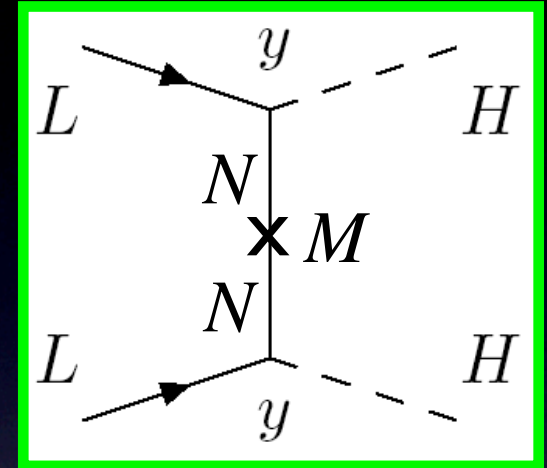
$$Y_{ij}^D \ \bar{5}_i^{16} \ 5_j^{10} \ \langle 1_D^{16} \rangle$$

# The mass spectrum

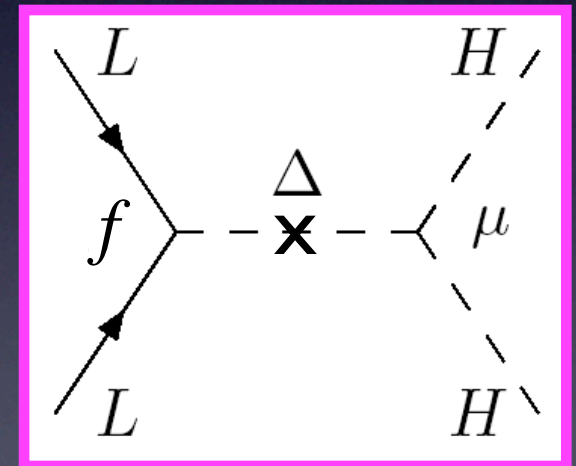


# Neutrino mass & the seesaw

In type I SO(10) models, light neutrinos couple through  $y_{ij}$  to gauge singlets N's, which have heavy Majorana masses  $M_{ij}$  :  
**two sets of flavour parameters**



In type II SO(10) models, **light neutrinos do not couple to N's !** They can acquire a mass only through a SU(2) triplet  $\Delta$



$$f_{ij} \ 10_i \ 10_j \ 54 \supset f_{ij} \ L_i \ L_j \ \Delta$$

The only flavour parameters are given by **the light neutrino mass matrix  $m_{ij}$**

$$m_{ij} = \frac{\mu v^2}{M_{\Delta}^2} f_{ij}$$

# Baryogenesis via leptogenesis

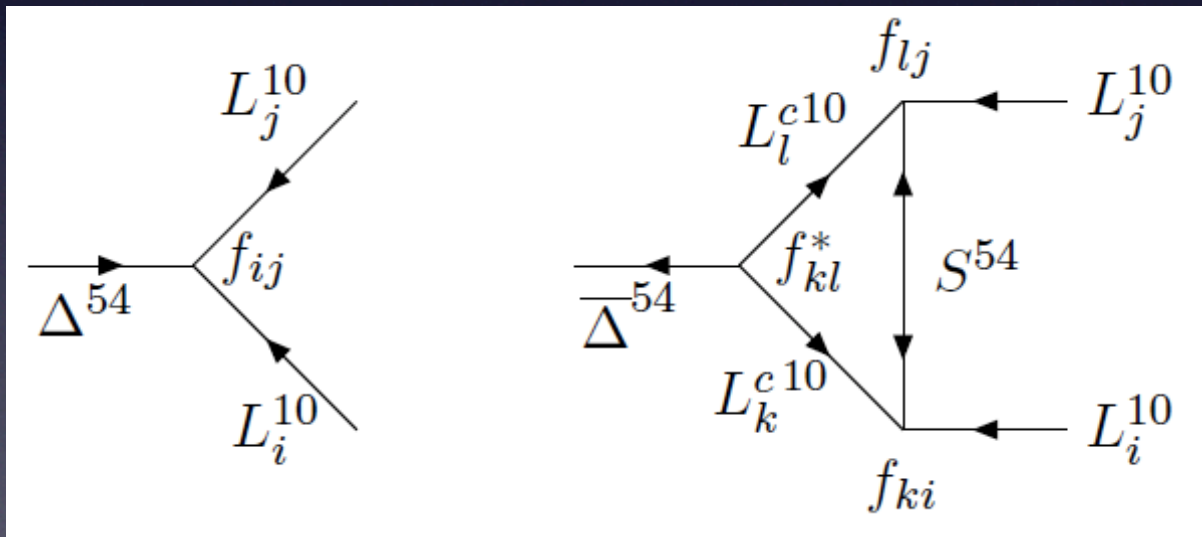
Sakharov

$$\frac{n_B}{s} \approx 0.9 \cdot 10^{-10}$$

WMAP

3 necessary conditions to generate the matter-antimatter asymmetry:

- (i) violation of B-L symmetry
- (ii) violation of CP symmetry
- (iii) epoch out of thermal equilibrium

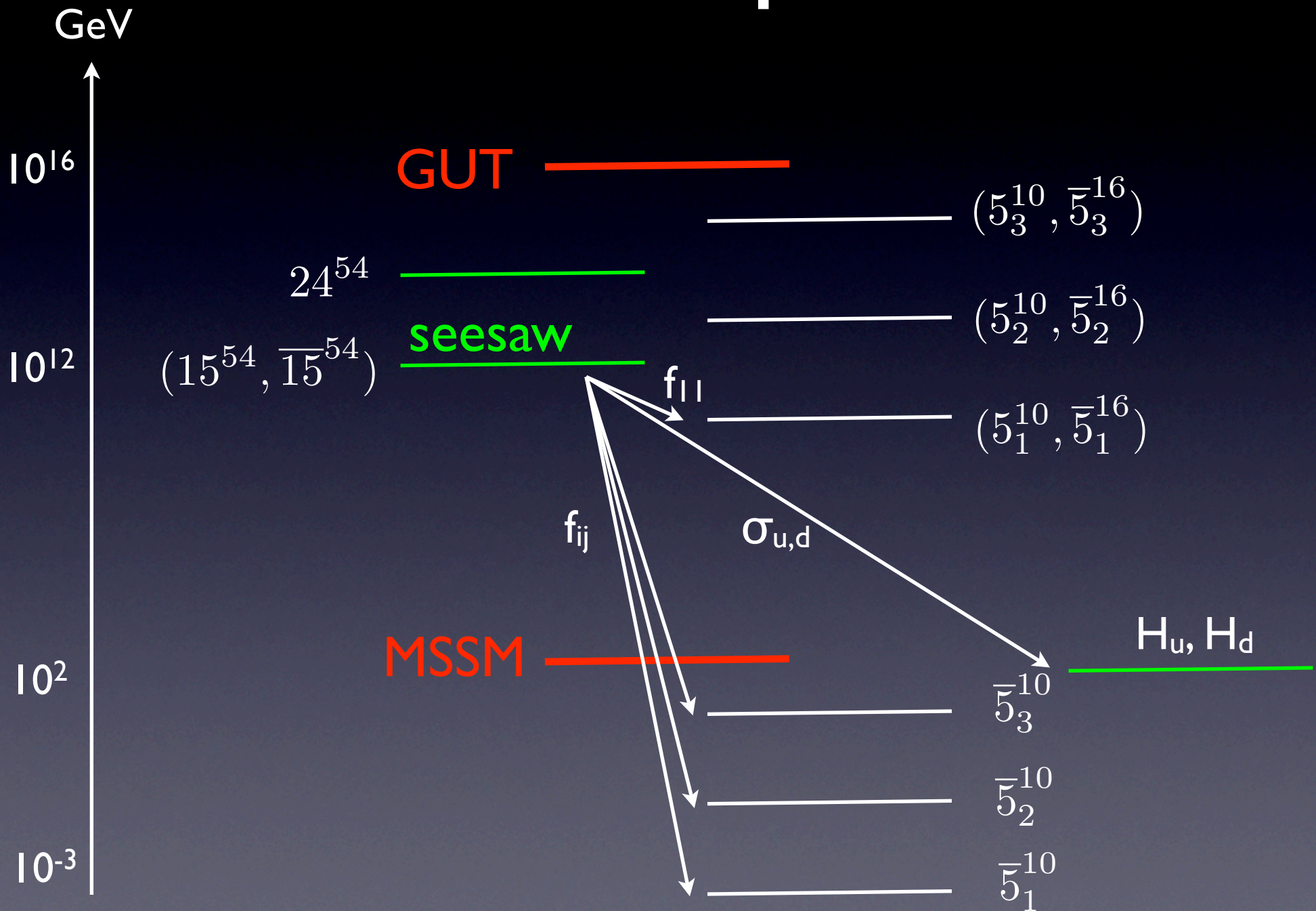


$$\begin{aligned}
 W_{SO(10)} &\supset f_{ij} 10_i 10_j 54 \\
 &\supset f_{ij} L_i L_j \Delta \\
 &+ f_{ij} L_i^c L_j^c \bar{\Delta} \\
 &+ f_{ij} L_i L_j^c S
 \end{aligned}$$

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A lepton asymmetry is produced  
by the observable couplings  $f_{ij}$  only !

# The mass spectrum



# Predictive leptogenesis

- Baryogenesis from the same **CP violating phases** observable at low energy in the lepton sector !

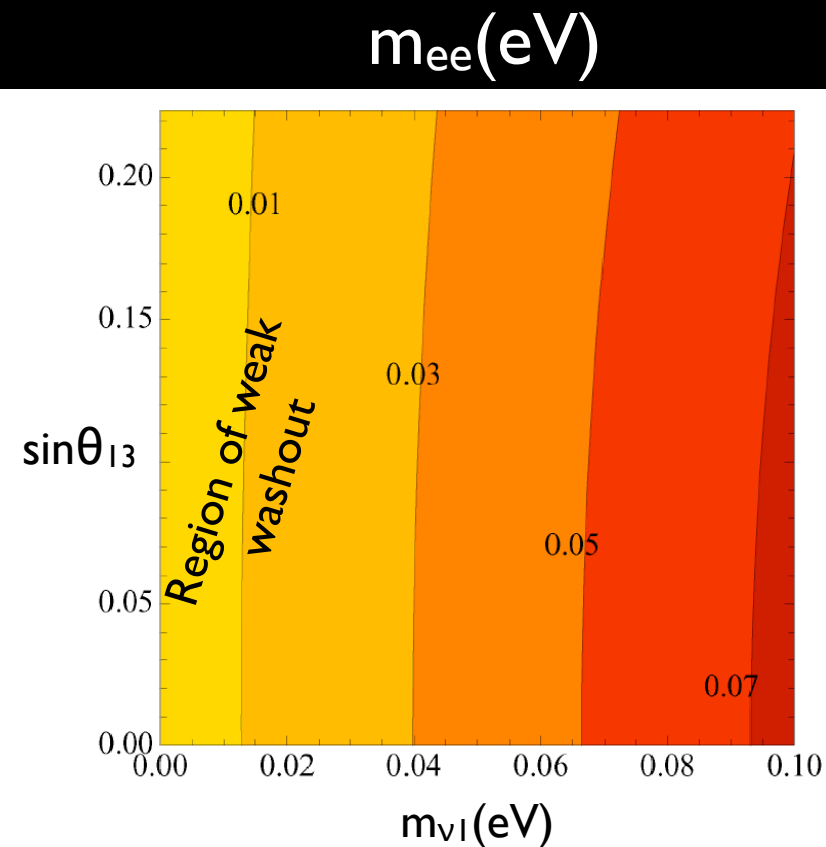
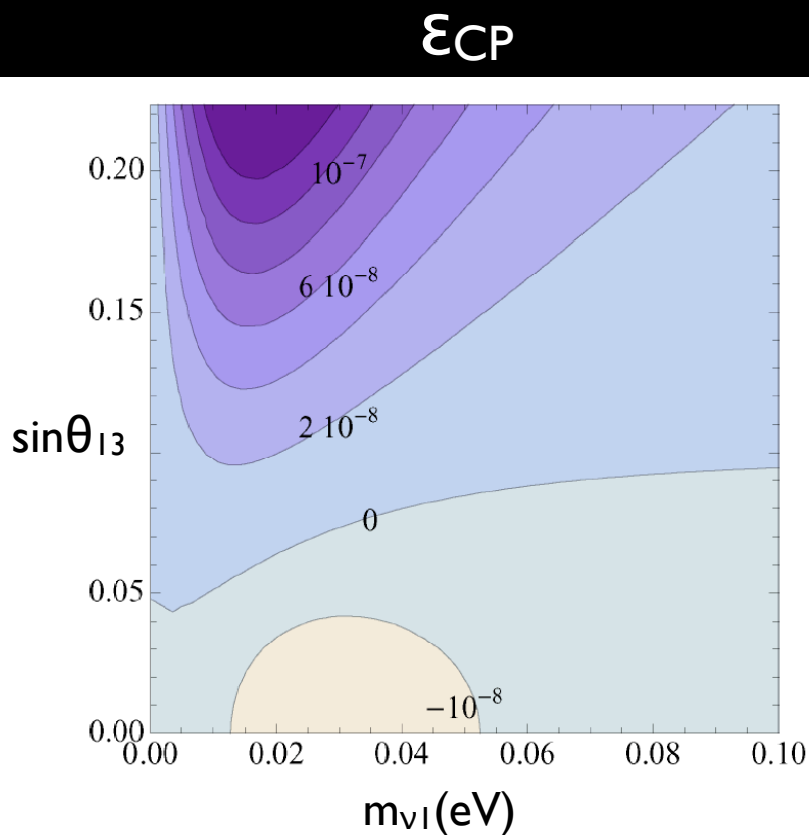
$$\frac{n_B}{s} \propto \frac{\text{Im}[m_{11}^* (mm^*m)_{11}]}{[\text{Tr}(m^*m)]^2}$$

- It turns out that **the washout is weak and the CP asymmetry is sufficiently large** for  $M_\Delta > 10^{11}\text{GeV}$  and specific  $\nu$  parameters:

Baryon asymmetry above  $10^{11}\text{GeV}$



Neutrinoless  $2\beta$  decay of heavy nuclei





# Soft SUSY breaking parameters

Suppose that **SUSY breaking mediation** occurs above GUT scale and it is flavour universal (mSUGRA boundary conditions at  $M_{GUT}$ ).

The RGE evolution through the scale of seesaw & leptogenesis leads to **flavour (and CP) violations in the soft parameters**.

$$(\tilde{m}_L^2)_{ij} \approx (\tilde{m}_{dc}^2)_{ji} \approx \frac{3m_0^2 + A_0^2}{16\pi^2} \sum_{a=1,2,3} f_{ia}^* \left[ 6 \log \frac{M_\Delta}{M_{GUT}} + \frac{24}{5} \log \frac{M_S + M_a}{M_{GUT}} \right] f_{aj}$$

type II seesaw à la SU(5)

$$(\tilde{m}_{ec}^2)_{ij} \approx \frac{3m_0^2 + A_0^2}{16\pi^2} \sum_{a=1,2,3} 4|\alpha_d|^2 y_{ia}^* \log \frac{M_a}{M_{GUT}} y_{aj}$$

3 heavy matter families from SO(10) breaking

MSSM like effects

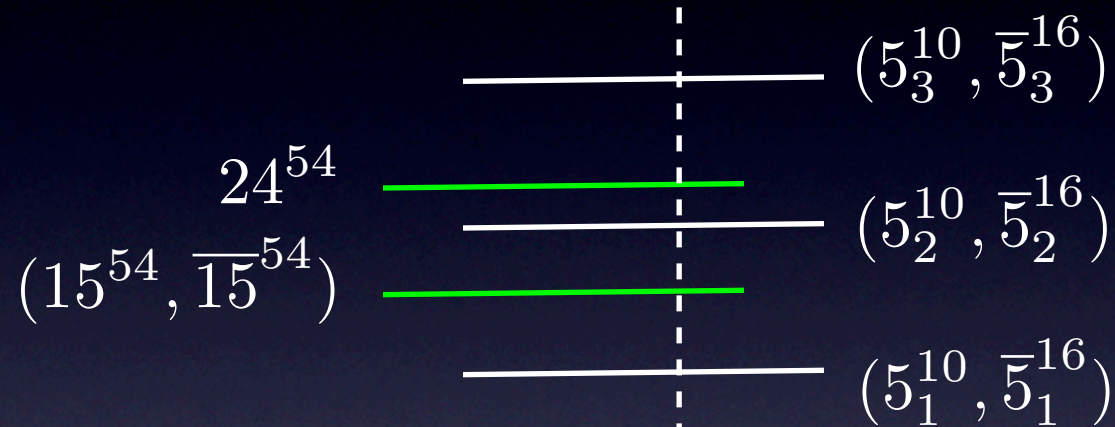
$$(\tilde{m}_Q^2)_{ij} \approx \frac{3m_0^2 + A_0^2}{16\pi^2} \sum_{a=1,2,3} y_{ia}^* \left[ 2|\alpha_u|^2 \log \frac{M_{SUSY}}{M_{GUT}} + 2|\alpha_d|^2 \log \frac{M_a}{M_{GUT}} \right] y_{aj}$$

# The mass spectrum

Flavour universal SUSY  
breaking mediation

Thresholds  
determined by seesaw  
and leptogenesis

**GUT** —————  $m_0, m_{1/2}, A_0$



TeV scale SUSY  
spectrum

**MSSM** —————  $m_{L,e,Q,d,u}, M_{1,2,3}, a_{e,d,u}$

Flavour and CP violating  
rare processes

—————

# Lepton flavour & CP violations

Rough estimates with **all equal soft masses** and the choice of **parameters that lead to successful leptogenesis** (a refined numerical analysis is ongoing ...)

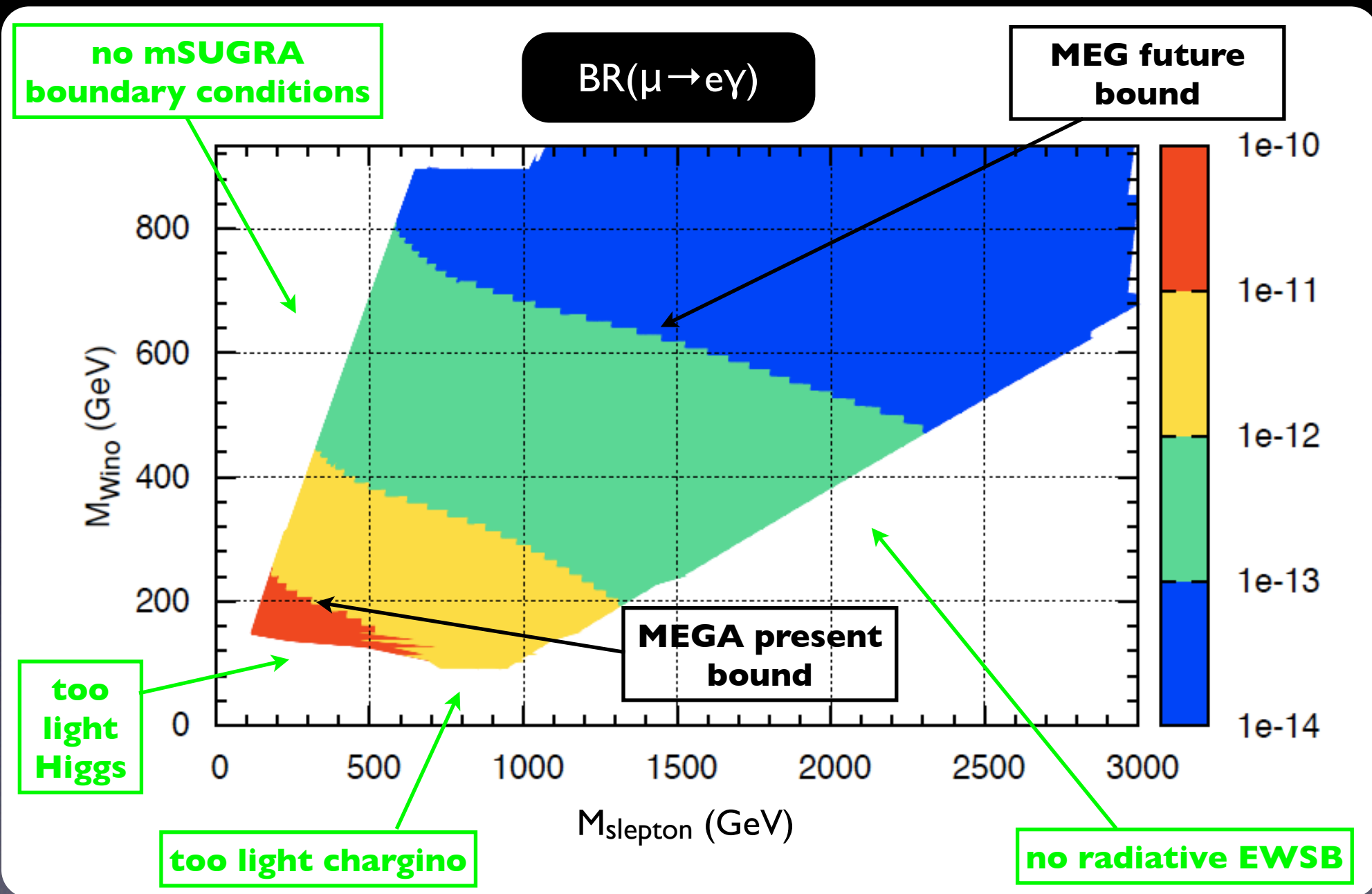
$$BR(\mu \rightarrow e\gamma) \sim 5 \cdot 10^{-11} \left( \frac{\tan \beta}{10} \right)^2 \left( \frac{500 \text{ GeV}}{M_S} \right)^4 \frac{\sin^2 \theta_{13}}{0.05}$$

The MEG experiment is taking data: **from  $10^{-11}$  to  $10^{-13}$  in 3y !**  
Strong correlations with  $\tau \rightarrow \mu\gamma, e\gamma$  (A.Rossi)

$$EDM_e \sim 5 \cdot 10^{-28} \text{ e cm} \frac{\tan \beta}{10} \left( \frac{500 \text{ GeV}}{M_S} \right)^2 \left( \frac{\sin^2 \theta_{13}}{0.05} \right)^{1/2} \sin \arg(U_{13} V_{31}^*)$$

The present bound is  **$7 \cdot 10^{-28} \text{ e cm}$** , prospects to reach  $10^{-30}$  ...

parameters leading to successful leptogenesis at  $10^{12}$  GeV,  $\tan \beta = 10$

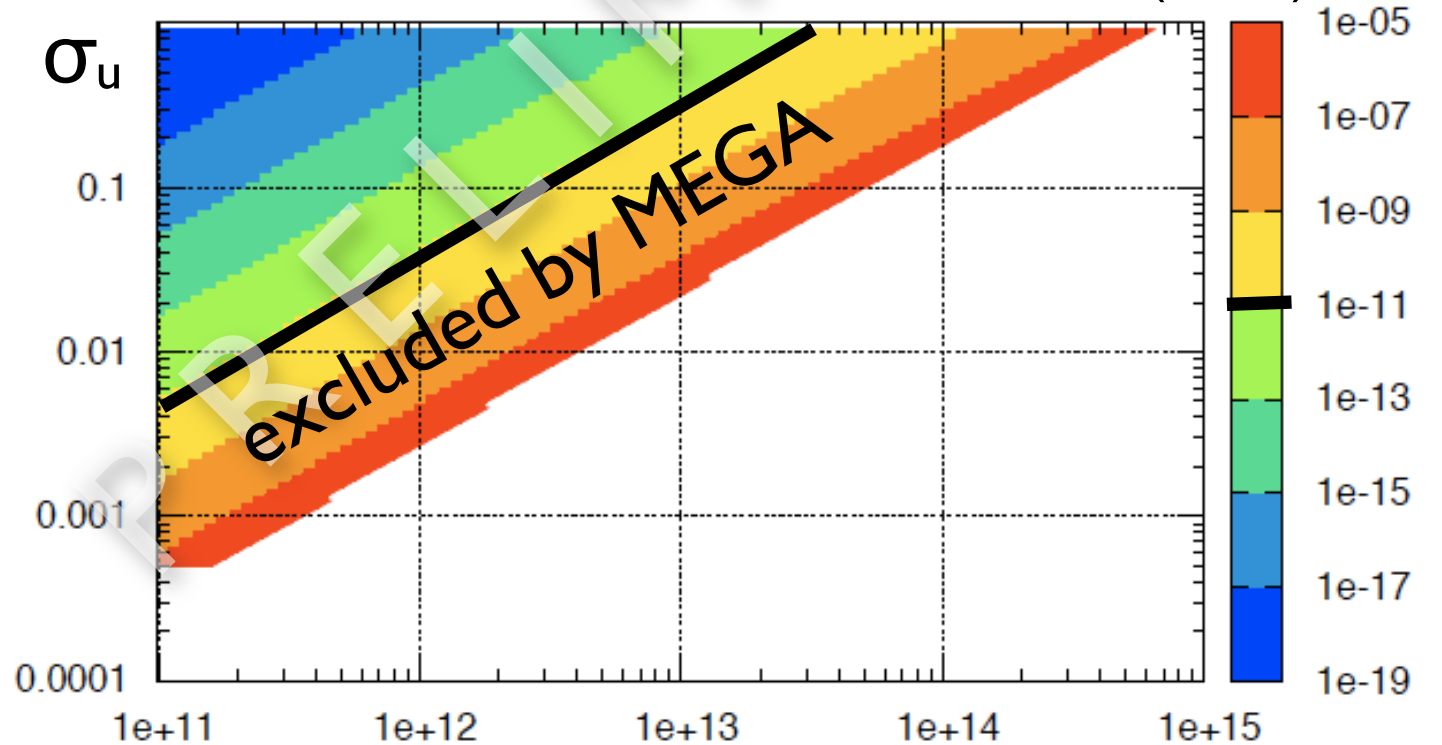
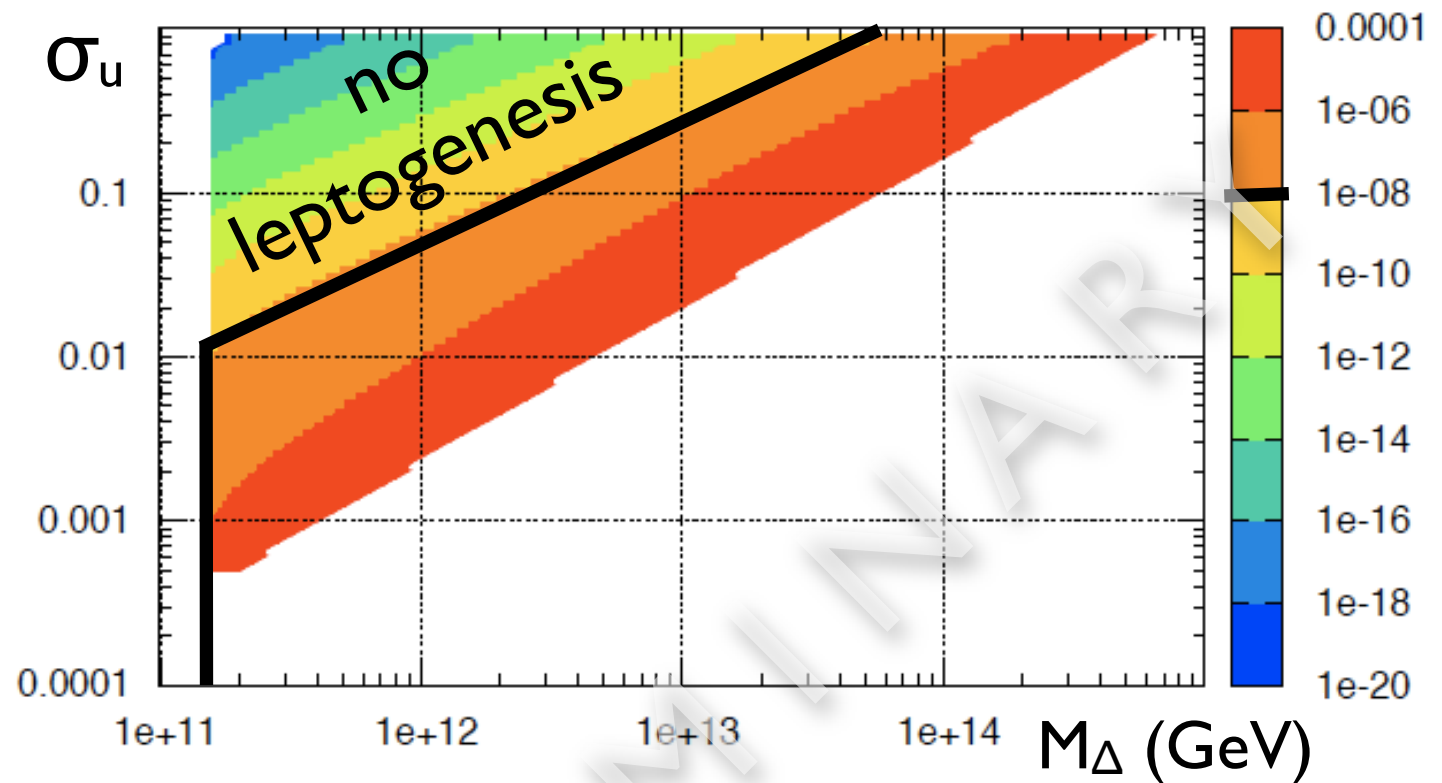


# $\xi_{CP}$

the slope of  
the contours,  
in both plots,  
is fixed by the  
size of neutrino  
masses

# $BR(\mu \rightarrow e\gamma)$

mSUGRA  
parameters  
fixed to  
 $\tan \beta = 10$   
 $m_0 = 450 \text{ GeV}$   
 $m_{1/2} = 500 \text{ GeV}$



# Quark flavour & CP violations

Correlated analysis of the **hadronic observables** gives weaker constraints.

Most noticeable difference with the MSSM is  $\delta^{RR}_d \neq 0$  at leading log.

$$BR(b \rightarrow s\gamma)|_{\tilde{g}} \sim \left(\frac{100 \text{ GeV}}{M_S}\right)^4 \left[ (3.9 \cdot 10^{-6})_{LL} + (1.9 \cdot 10^{-7})_{RR} \right] \\ + \left(\frac{100 \text{ GeV}}{M_S}\right)^2 \left[ (5.4 \cdot 10^{-7})_{LR} + (1.2 \cdot 10^{-8})_{RL} \right]$$

The presently allowed range is  **$(1.8 - 4.3) 10^{-4}$** .

RR and RL contributions can be enhanced by the factor  $(f_{ij} / 0.05)^4$ .

Other constraints from **CP violating observables** as  $\epsilon_K$  or  $EDM_n$ .

They are sensitive to both low and high energy CP phases.

# Conclusions

- \* Several upcoming experiments will provide new severe & complementary **tests of SUSY GUTs**
- \* **In type II SO(10) models**, the observable fermion masses & mixing angles are the only flavour parameters of the full theory. **Leptogenesis** is controlled directly by the neutrino masses.
- \* A specific pattern of **SUSY flavour violating effects**. Strong constraints from the present & future bound on  $\text{BR}(\mu \rightarrow e\gamma)$