

Electroweak corrections to Higgs production via gluon fusion

Stefano Actis

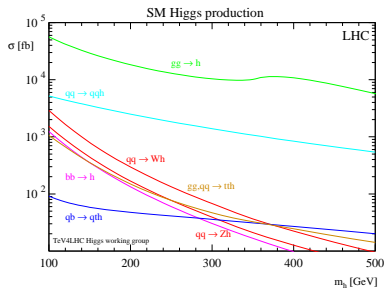
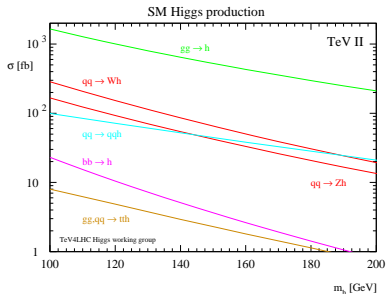
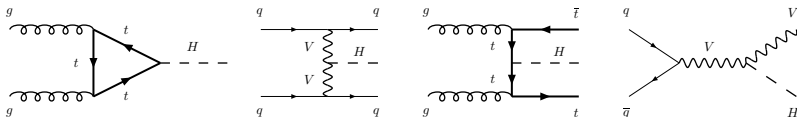
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Hadronic SM Higgs production

Gluon-fusion production channel has by far the **largest cross section** both at the **TEVATRON** and the **LHC**



QCD corrections

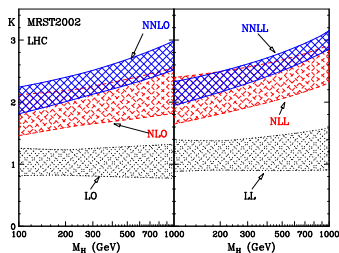
NLO and **NNLO** QCD corrections to the cross section **extremely large**

Dawson '91, Djouadi, Spira, Zerwas '91, Spira, Djouadi, Graudenz, Zerwas '95

Harlander, Kant '05, Anastasiou, Beerli, Bucherer, Daleo, Kunszt '06,
Aglietti, Bonciani, Degrossi, Vicini '06

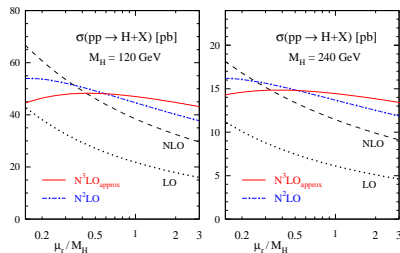
Harlander '00, Catani, de Florian, Grazzini '01, Harlander, Kilgore '01,

Anastasiou, Melnikov '02, Ravindran, Smith, van Neerven '03



Catani, de Florian, Grazzini, Nason

[hep-ph/0306211]



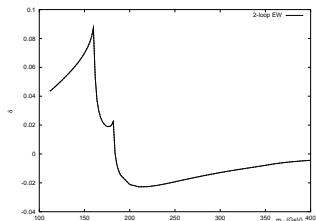
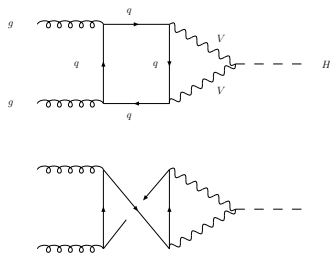
Moch, Vogt [hep-ph/0508265]

N^3LO soft limit \Rightarrow 5% uncertainty

also **NNLO** beyond the $M_t \rightarrow \infty$ approximation, talk by K. Ozeren at LoopFest

EW corrections

- Top diags by expansions Djouadi, Gambino '94; Degrassi, Maltoni '04
- Light-quark analytically Aglietti, Bonciani, Degrassi, Vicini '04



Aglietti, Bonciani, Degrassi, Vicini
[hep-ph/0404071]

- Full NLO above WW threshold SA, Passarino, Sturm, Uccirati '08
- NNLO QCD/EW effective Anastasiou, Boughezal, Petriello '08

Complex poles

Problem with the crossing of both WW and ZZ : **square-root divergencies**

$gg \rightarrow H$ amplitude \Rightarrow terms proportional to $1/\beta_V$, $\beta_V = \sqrt{1 - 4M_V^2/M_H^2}$

Cure problems with crossing of thresholds implementing the complex-mass scheme at 1 loop *Denner, Dittmaier, Roth, Wieders '05*

1) Minimal introduction of the complex-mass scheme

Decompose $A = A_{\text{div}}^{1,W}/\beta_W + A_{\text{div}}^{1,Z}/\beta_Z + A_{\text{fin}}$

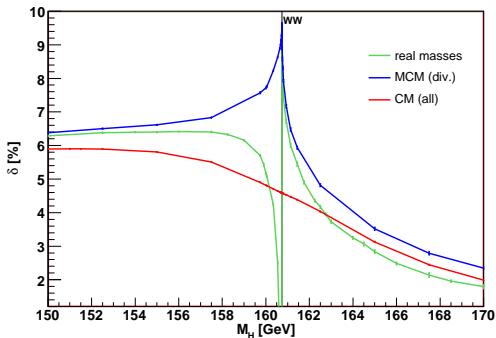
Introduce the CMS in both threshold factors β_V and coefficients $A_{\text{div}}^{1,2}$

2) Complete introduction of the complex-mass scheme

Introduce the CMS in all divergent and finite terms of the amplitude

Threshold behaviour for $gg \rightarrow H$

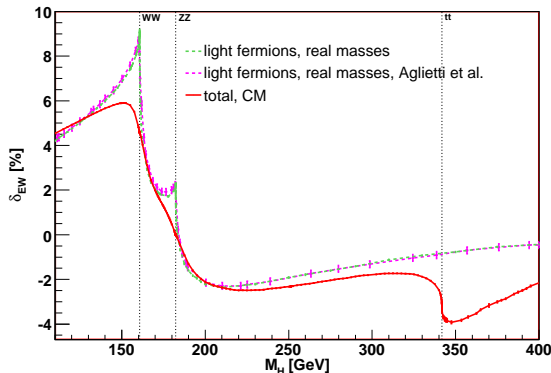
Comparison of EW corrections to $gg \rightarrow H$ around the WW threshold, obtained using **different schemes** for treating unstable particles



- Result obtained with real masses divergent at WW ; good approx. below/above
- MCM setup gives finite result at WW ; large effect 9.6 % associated with cusp
- CM setup smoothens singular behaviour; effects at threshold reduced to 4.6 %

EW corrections to $gg \rightarrow H$

Summary of EW corrections to $gg \rightarrow H$ for $100 \text{ GeV} < M_H < 400 \text{ GeV}$



- Light fermions dominate up to 300 GeV; top-quark diagrams relevant at $t\bar{t}$ threshold, with relative correction $\delta_{ew} \sim -4\%$
- CMs change the result around WW and ZZ thresholds, where cusps disappear

Inclusion of NLO EW effects

Partonic result convoluted with the **PDFs**:

$$\sigma(h_1 h_2 \rightarrow H) = \sum_{i,j} \int_0^1 dx_1 dx_2 f_{i,h_1}(x_1, \mu_F^2) f_{j,h_2}(x_2, \mu_F^2) \times \\ \times \int_0^1 dz \delta\left(z - \frac{M_H^2}{s x_1 x_2}\right) z \sigma^0 G_{ij}(z, \mu_R^2, \mu_F^2)$$

I) **Complete factorization** $G_{ij} \rightarrow (1 + \delta_{EW}) G_{ij}$

\Rightarrow multiply NNLO QCD result \times EW correction factor at NLO

II) **No factorization** $G_{ij} \rightarrow G_{ij} + \alpha_S^2 \delta_{EW} G_{ij}^{(0)}$

\Rightarrow add NLO EW to NNLO QCD corrections

- effective-theory computation of mixed three-loop EW and QCD effects by [Anastasiou, Boughezal, Petriello'08](#) supports the hypothesis of a complete factorization at the pragmatic level

Conclusions

- Performed a complete computation of the NLO EW corrections to $gg \rightarrow H$; all contributions evaluated for any value of M_H ; corrections range between +6% for $M_H = 150$ GeV (light fermions) and -4% for $M_H \sim 2 M_t$ (top-quark diagrams)

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- Full implementation of the complex-mass scheme needed to avoid large effects at two-particle thresholds; for $M_H = 2 M_W$, corrections reduced from +10% (almost naive introduction of finite-width effects) to +5% (CMS in all terms)

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- Full implementation of the complex-mass scheme needed to avoid large effects at two-particle thresholds; for $M_H = 2 M_W$, corrections reduced from +10% (almost naive introduction of finite-width effects) to +5% (CMS in all terms)
- Results included by Anastasiou-Boughezal-Petriello '08 and de Florian-Grazzini '09 for most updated prediction for σ_H at hadron colliders

Practical implementation of the CMS

Practical implementation of the complex-mass scheme through two steps:

1. Replace on-shell masses M_V^2 with complex poles $s_V = \mu_V(\mu_V - i\gamma_V)$
 2. Trade the **real parts** of the W and Z self-energies (mass renormalization at 1 loop) for the **complete self-energies, including imaginary parts**
- ⇒ Replace the **conventional on-shell mass renormalization** equations with the associated expressions for the **complex poles** of the W and Z bosons

$$m_i^2 = M_i^2 \left[1 + \frac{G_F M_W^2}{2\sqrt{2} \pi^2} \text{Re}\Sigma_i^{(1)}(M_i^2) \right] \Rightarrow m_i^2 = s_i \left[1 + \frac{G_F s_W}{2\sqrt{2} \pi^2} \Sigma_i^{(1)}(s_i) \right]$$

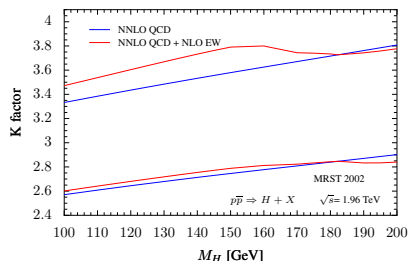
- ⇒ Insert the **full self-energy for the W boson** in the renormalization equation for the Fermi-coupling constant, expressed through the **complex mass of the W** , s_W

$$g = 2 \left(\sqrt{2} G_F s_W \right)^{1/2} \left[1 - \frac{G_F s_W}{4\sqrt{2} \pi^2} \Delta \right], \Delta = \Sigma_W^{(1)}(0) - \Sigma_W^{(1)}(s_W) + 6 + \frac{7 - 4s_\theta^2}{2s_\theta^2} \ln c_\theta^2$$

CMS → replacements done also at the level of the couplings ⇒ $s_\theta^2 = 1 - s_W/s_Z$

NLO EW corrections at the Tevatron

Impact of NLO EW effects at Tevatron II, $\sqrt{s} = 1.96$ TeV,
 $100 \text{ GeV} < M_H < 200 \text{ GeV}$ (using HIGGSNNLO, by M.Grazzini)

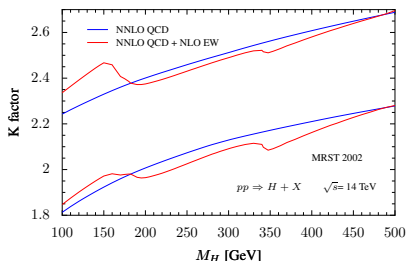


M_H [GeV]	δ_{CF} [%]	δ_{PF} [%]
120	+4.9	+1.6
140	+5.7	+1.8
160	+4.8	+1.5
180	+0.5	+0.1
200	-2.1	-0.6

- Uncertainty band shows stronger sensitivity on the Higgs mass, once NLO EW effects are included
- Impact of NLO EW corrections smaller respect to NNLL resummation Catani, de Florian, Grazzini, Nason'03 (+12% for $M_H = 120$ GeV)
- Effective-theory computation of **mixed three-loop EW and QCD effects** by Anastasiou, Boughezal, Petriello'08 supports the hypothesis of a complete factorization at the pragmatic level

NLO EW corrections at the LHC

Impact of NLO EW effects at LHC, $\sqrt{s} = 14$ TeV,
 $100 \text{ GeV} < M_H < 500 \text{ GeV}$ (using HIGGSNNLO, by M.Grazzini)



M_H [GeV]	δ_{CF} [%]	δ_{PF} [%]
120	+4.9	+2.4
150	+5.9	+2.8
200	-2.1	-1.0
310	-1.7	-0.9
410	-0.8	-0.8

- Uncertainty band shows stronger sensitivity on the Higgs mass, once NLO EW effects are included
- WW and $t\bar{t}$ thresholds visible, but smooth having introduced everywhere CMs
- Impact of NLO EW corrections comparable to that of NNLL resummation [Catani, de Florian, Grazzini, Nason'03](#) (+6% for $M_H = 120$ GeV); for large M_H NLO EW corrections turn negative, screening effect with NNLL resummation