

SUSY Phenomenology – Precise predictions from the MSSM for colliders

W. HOLLIK



Max-Planck-Institut für Physik
(Werner-Heisenberg-Institut)

PHENO 2009 SYMPOSIUM

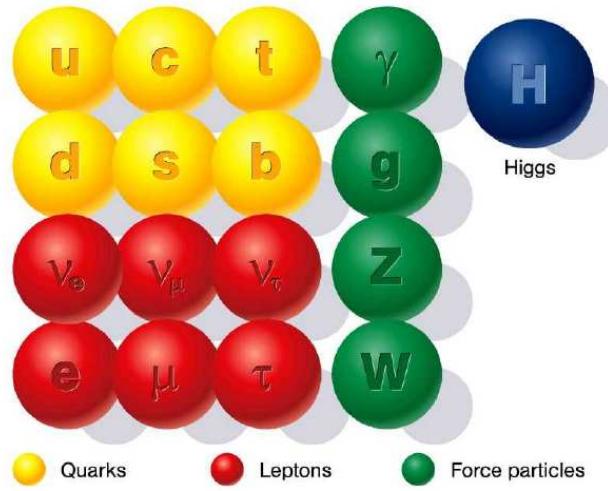
UNIVERSITY OF WISCONSIN, MADISON

11 - 13 MAY 2009

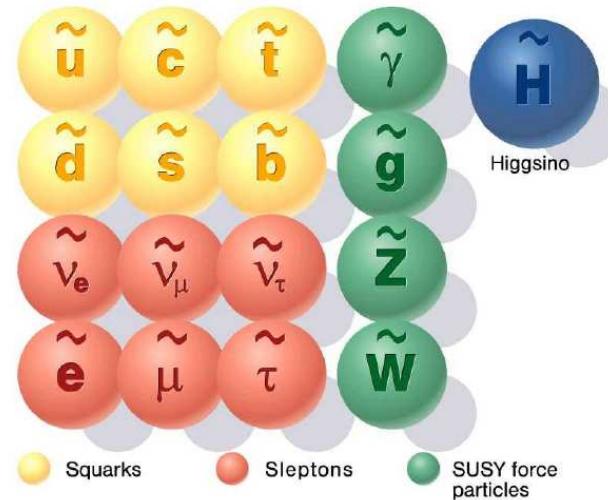
Outline

- Indirect SUSY search through precision observables
- Implications on Higgs bosons
- Direct study of SUSY particles
- Summary

Standard particles



SUSY particles



- gauge coupling unification
- stabilization of the electroweak scale
- dark matter candidate (lightest SUSY particle)
- lightest Higgs boson $h^0 < 135 \text{ GeV}$
physical Higgs bosons: h^0, H^0, A^0, H^\pm

The Minimal Supersymmetric Standard Model (MSSM)

Superpartners for Standard Model particles:

$$[u, d, c, s, t, b]_{L,R} \quad [e, \mu, \tau]_{L,R} \quad [\nu_{e,\mu,\tau}]_L \quad \text{Spin } \frac{1}{2}$$

$$[\tilde{u}, \tilde{d}, \tilde{c}, \tilde{s}, \tilde{t}, \tilde{b}]_{L,R} \quad [\tilde{e}, \tilde{\mu}, \tilde{\tau}]_{L,R} \quad [\tilde{\nu}_{e,\mu,\tau}]_L \quad \text{Spin } 0$$

$$g \quad \underbrace{W^\pm, H^\pm} \quad \underbrace{\gamma, Z, H_1^0, H_2^0} \quad \text{Spin 1 / Spin 0}$$

$$\tilde{g} \quad \tilde{\chi}_{1,2}^\pm \quad \tilde{\chi}_{1,2,3,4}^0 \quad \text{Spin } \frac{1}{2}$$

Enlarged Higgs sector: two Higgs doublets, physical states:
 h^0, H^0, A^0, H^\pm

masses and mixing of SUSY particles through soft-breaking

model parameters

- gaugino masses: M_1, M_2, M_3
- sfermion masses: $M_L, M_{\tilde{u}_R}, M_{\tilde{d}_R}$
for each doublet of squarks and sleptons
- trilinear coupling: $A_{\tilde{f}}$ for each \tilde{f}
→ L - R sfermion mixing
- supersymmetric Higgsino mass parameter: μ
- Higgs sector parameters: $M_A, \tan \beta = v_2/v_1$

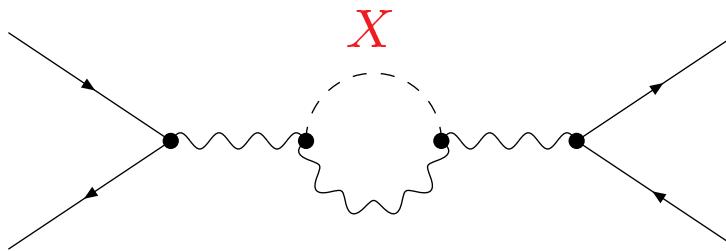
Precision analysis required for

- indirect tests of SUSY through
 - virtual SUSY effects in precision observables
- precision studies for SUSY particles
 - determination of masses & couplings
 - reconstruction of model parameters
- direct *versus* indirect tests
 - precision observables for precisely measured SUSY parameters
 - consistency check

Processes with external

- (i) standard particles
- (ii) Higgs bosons, especially light Higgs h^0
- (iii) SUSY particles

precision observables in the MSSM



X = Higgs bosons, SUSY particles

- μ lifetime: $M_W \leftrightarrow M_Z, G_F$
- Z observables: $g_V, g_A, \sin^2 \theta_{\text{eff}}, \Gamma_Z, M_Z, \dots$

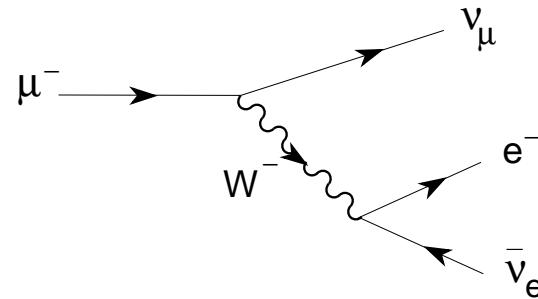
[Heinemeyer, WH, Weiglein, Phys. Rep. 425 (2006) 265]

2-loop terms $\mathcal{O}(\alpha\alpha_s, \alpha_t^2, \alpha_b^2, \alpha_t\alpha_b)$
and complex parameters

[Heinemeyer, WH, Stöckinger, A. Weber, Weiglein 06]

[Heinemeyer, WH, A. Weber, Weiglein 07]

$M_W - M_Z$ correlation



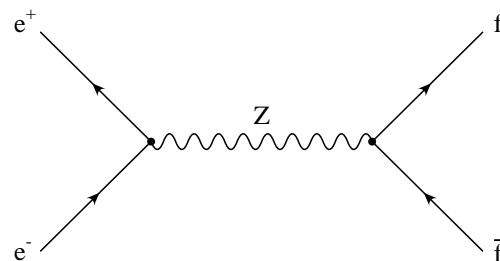
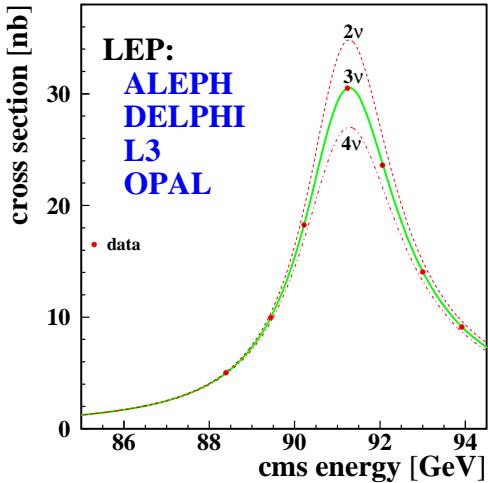
$$\frac{G_F}{\sqrt{2}} = \frac{\pi\alpha}{M_W^2 (1 - M_W^2/M_Z^2)} (1 + \Delta r)$$

Δr : quantum correction, $\Delta r = \Delta r(m_t, X_{\text{SUSY}})$

$\rightarrow M_W = M_W(\alpha, G_F, M_Z, m_t, X_{\text{SUSY}})$

X_{SUSY} = set of non-standard model parameters

Z resonance



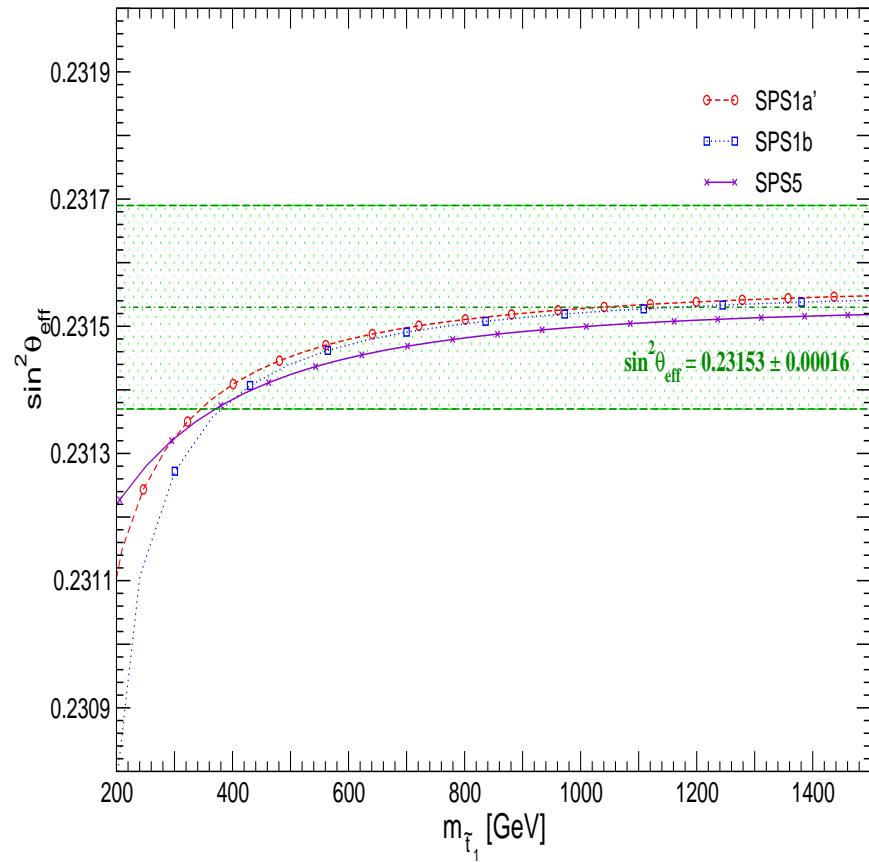
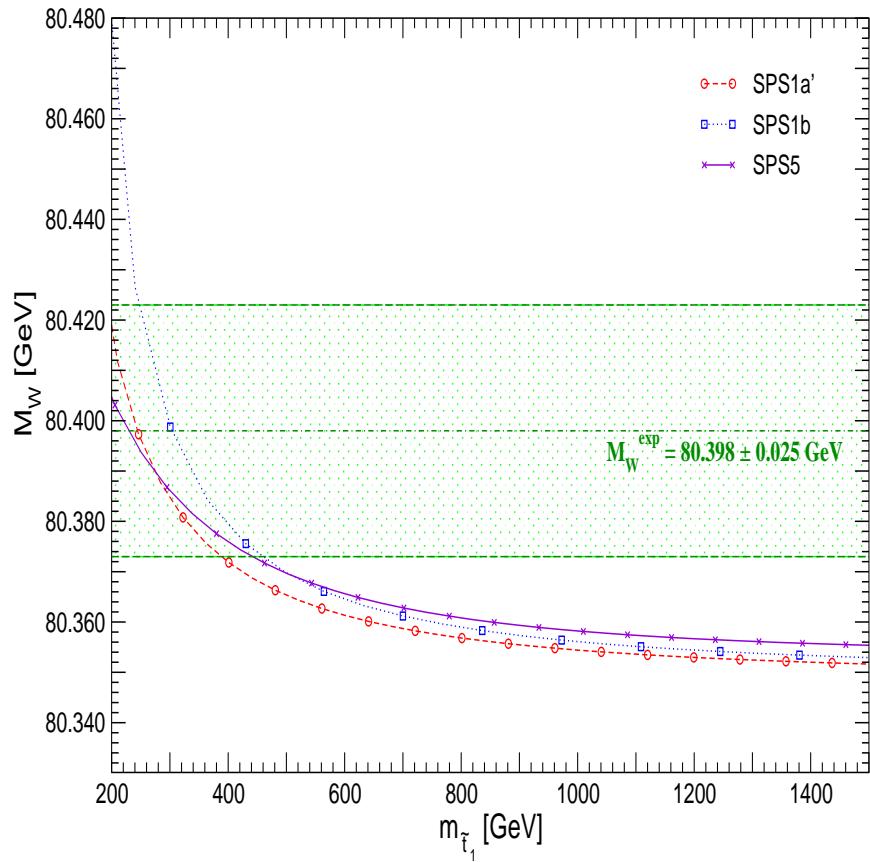
effective Z boson couplings

$$g_V^f \rightarrow g_V^f + \Delta g_V^f, \quad g_A^f \rightarrow g_A^f + \Delta g_A^f$$

with higher order contributions $\Delta g_{V,A}^f(m_t, X_{\text{SUSY}})$

$$\sin^2 \theta_{\text{eff}} = \frac{1}{4} \left(1 - \text{Re} \frac{g_V^e}{g_A^e} \right) = \kappa \cdot \left(1 - \frac{M_W^2}{M_Z^2} \right)$$

M_W and $\sin^2 \theta_{\text{eff}}$ for varied SUSY-scale



Fortran Code SUSYPOPE [A. Weber, PhD thesis, Munich 2008]

also used in recent fits by AbdusSalam, Allanach, Quevedo, Feroz, Hobson,
arxiv:0904.2548

Benchmark scenarios

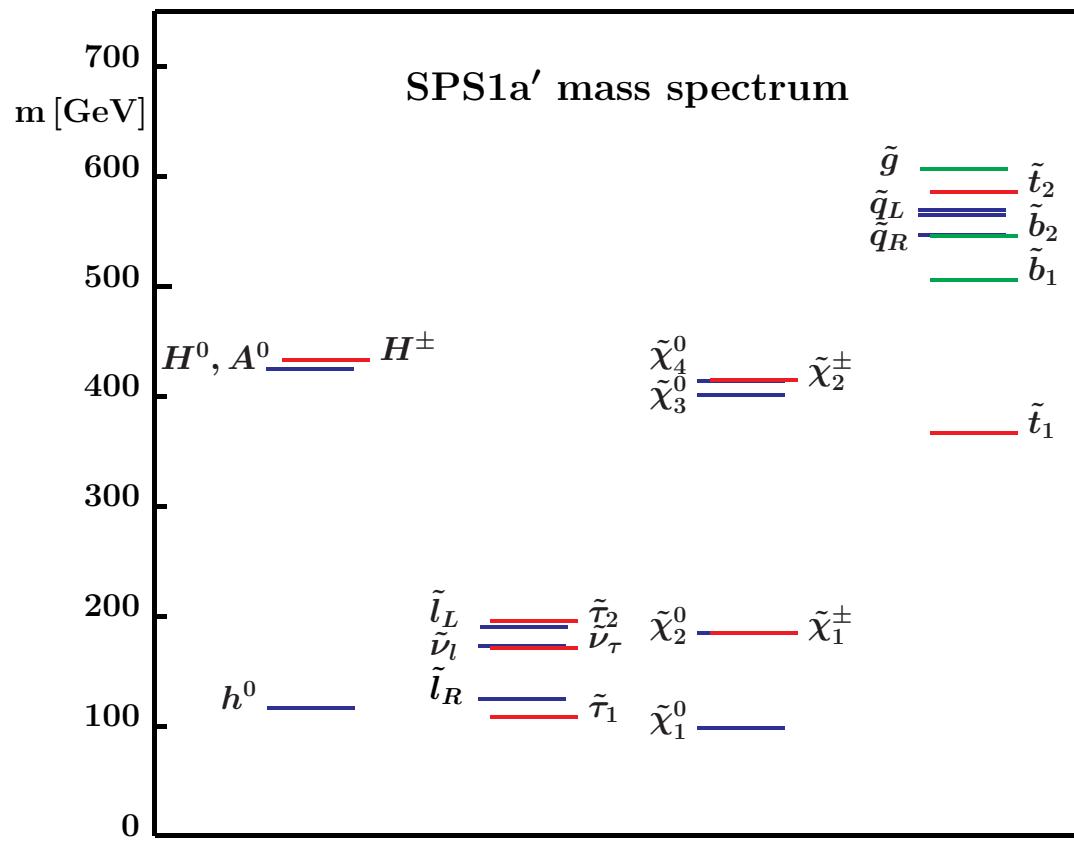
“Snowmass points and slopes” (SPS),
hep-ph/0202233

examples (mSUGRA):

- SPS1a: $m_0 = 100 \text{ GeV}$, $m_{1/2} = 250 \text{ GeV}$, $A_0 = -100$,
 $\tan \beta = 10$, $\mu > 0$.
- SPS1b: $m_0 = 200 \text{ GeV}$, $m_{1/2} = 400 \text{ GeV}$, $A_0 = 0$,
 $\tan \beta = 30$, $\mu > 0$.

SPS1a' scenario [SPA Report, hep-ph/0511344]

$M_{1/2}$	=	250 GeV	$\text{sign}(\mu)$	=	+1
M_0	=	70 GeV	$\tan \beta(\tilde{M})$	=	10
A_0	=	-300 GeV			



Scatter plots for M_W & $\sin^2 \theta_{\text{eff}}$

■ SUSY parameters:

sleptons : $M_{\tilde{F}, \tilde{F}'} = 100 \dots 2000 \text{ GeV}$

light squarks : $M_{\tilde{F}, \tilde{F}'_{\text{up/down}}} = 100 \dots 2000 \text{ GeV}$

\tilde{t}/\tilde{b} doublet : $M_{\tilde{F}, \tilde{F}'_{\text{up/down}}} = 100 \dots 2000 \text{ GeV}$

$A_{t,b} = -2000 \dots 2000 \text{ GeV}$

gauginos : $M_{1,2} = 100 \dots 2000 \text{ GeV}$

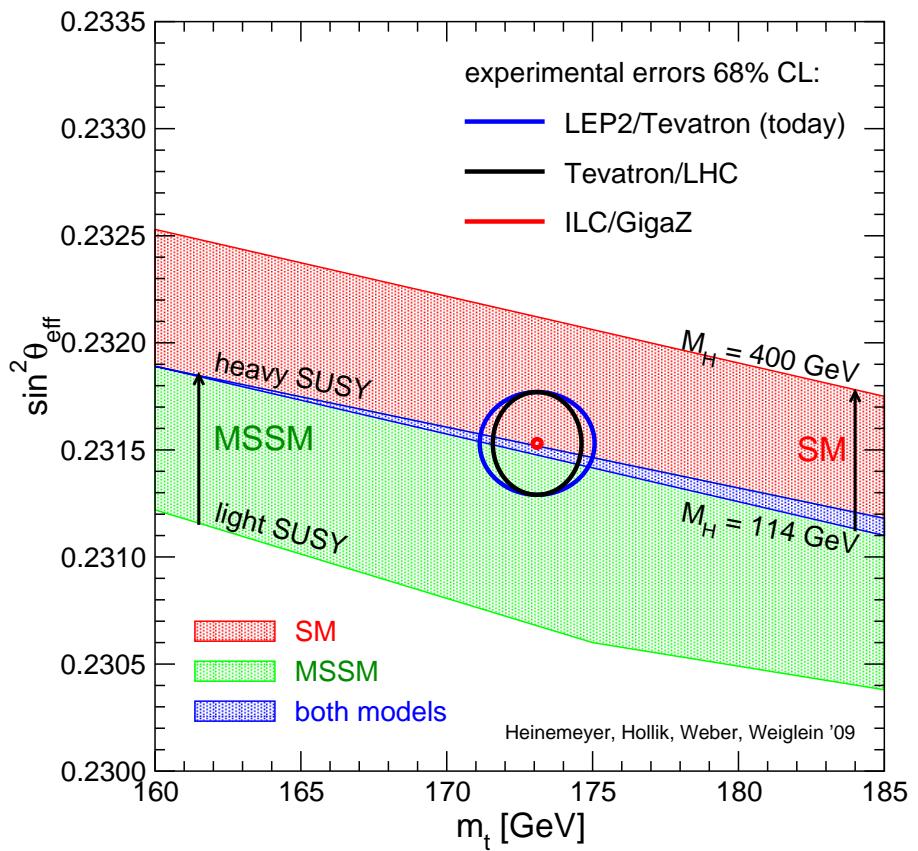
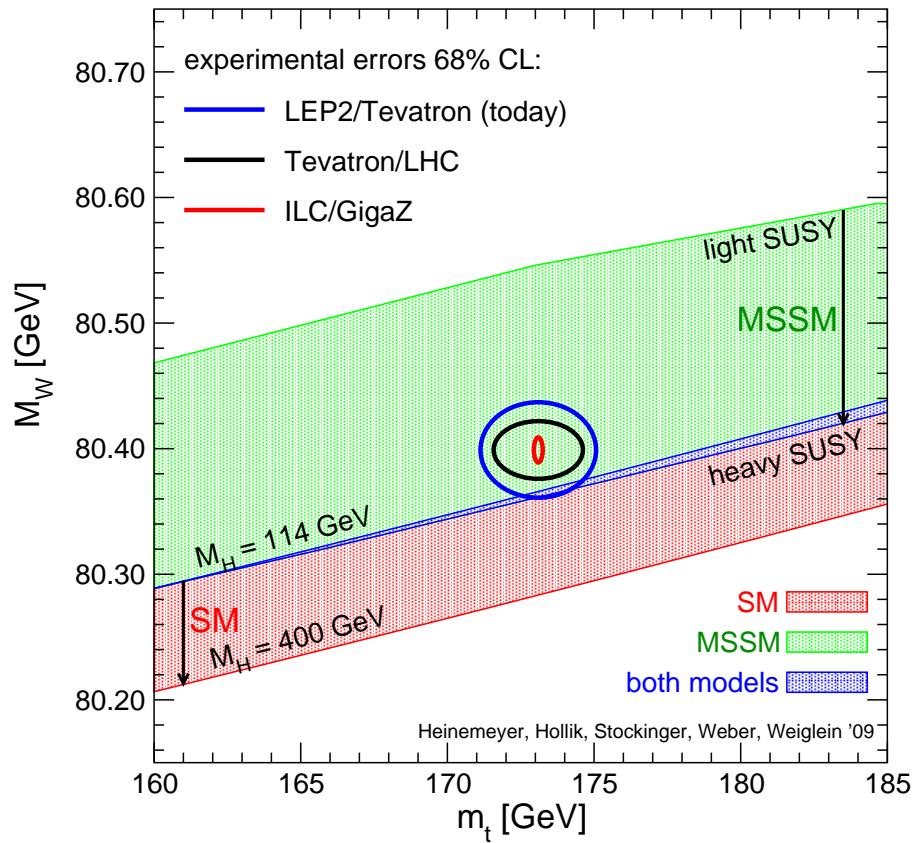
$m_{\tilde{g}} = 195 \dots 1500 \text{ GeV}$

$\mu = -2000 \dots 2000 \text{ GeV}$

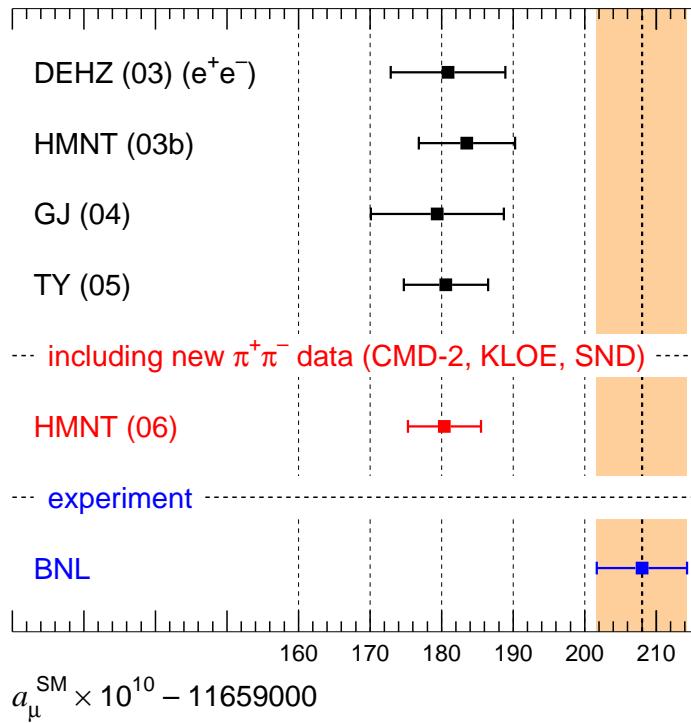
Higgs : $M_A = 90 - 1000 \text{ GeV}$

$\tan \beta = 1.1 \dots 60$

■ Unconstrained scan, only Higgs mass required to be in agreement with LEP data.



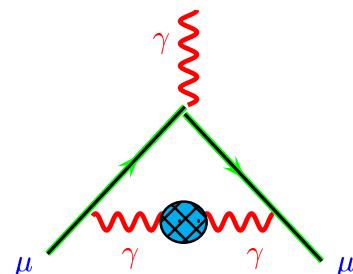
Anomalous g-factor of the muon



Hagiwara, Martin, Nomura, Teubner

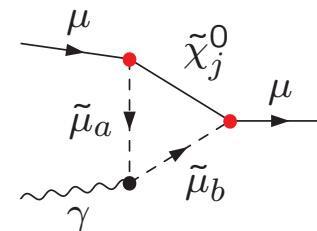
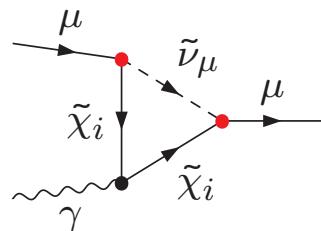
e^+e^- data based SM prediction: 3.4σ below exp. value

theory uncertainty from hadronic vacuum polarization



$g - 2$ with supersymmetry

new contributions from virtual SUSY partners of μ, ν_μ
and of W^\pm, Z



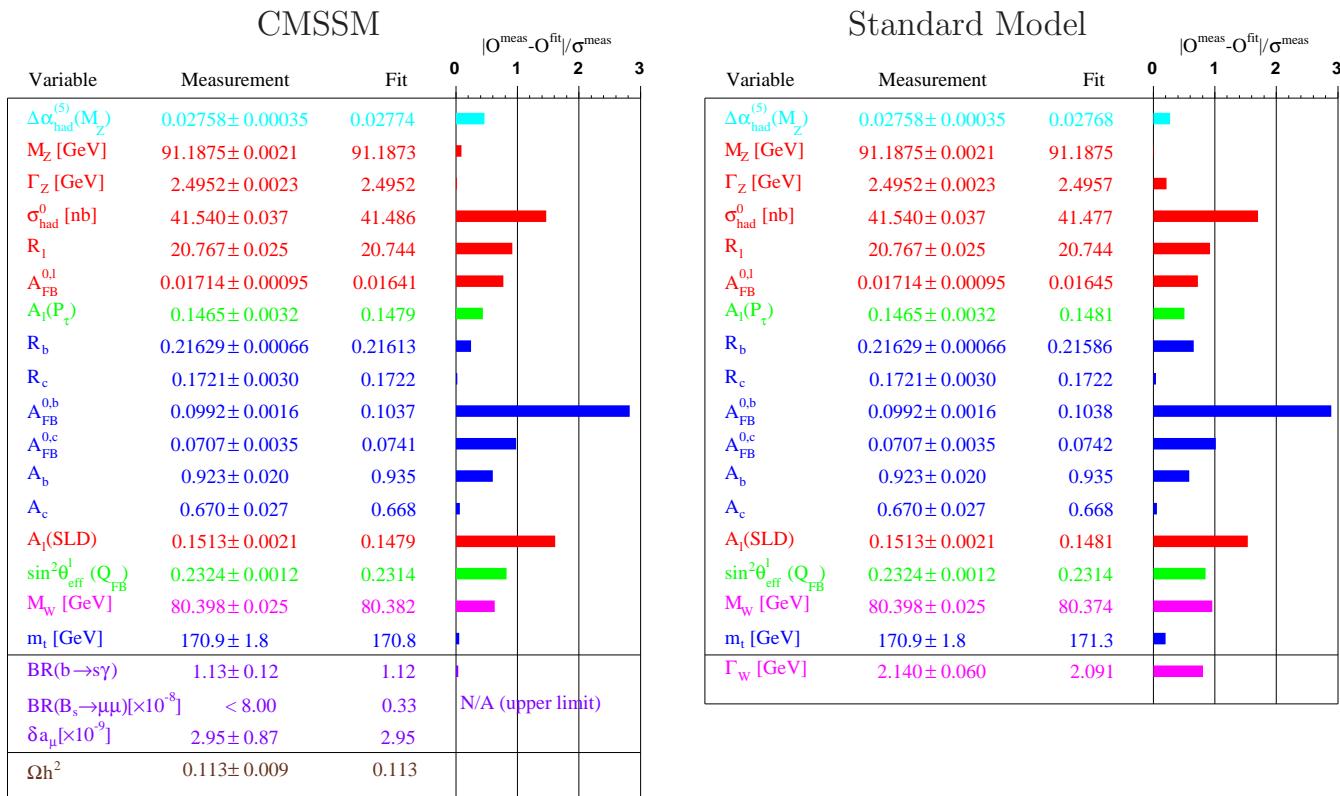
extra terms [Czarnecki, Marciano]

$$+ \frac{\alpha}{\pi} \frac{m_\mu^2}{M_{\text{SUSY}}^2} \cdot \frac{v_2}{v_1}$$

can provide missing contribution for

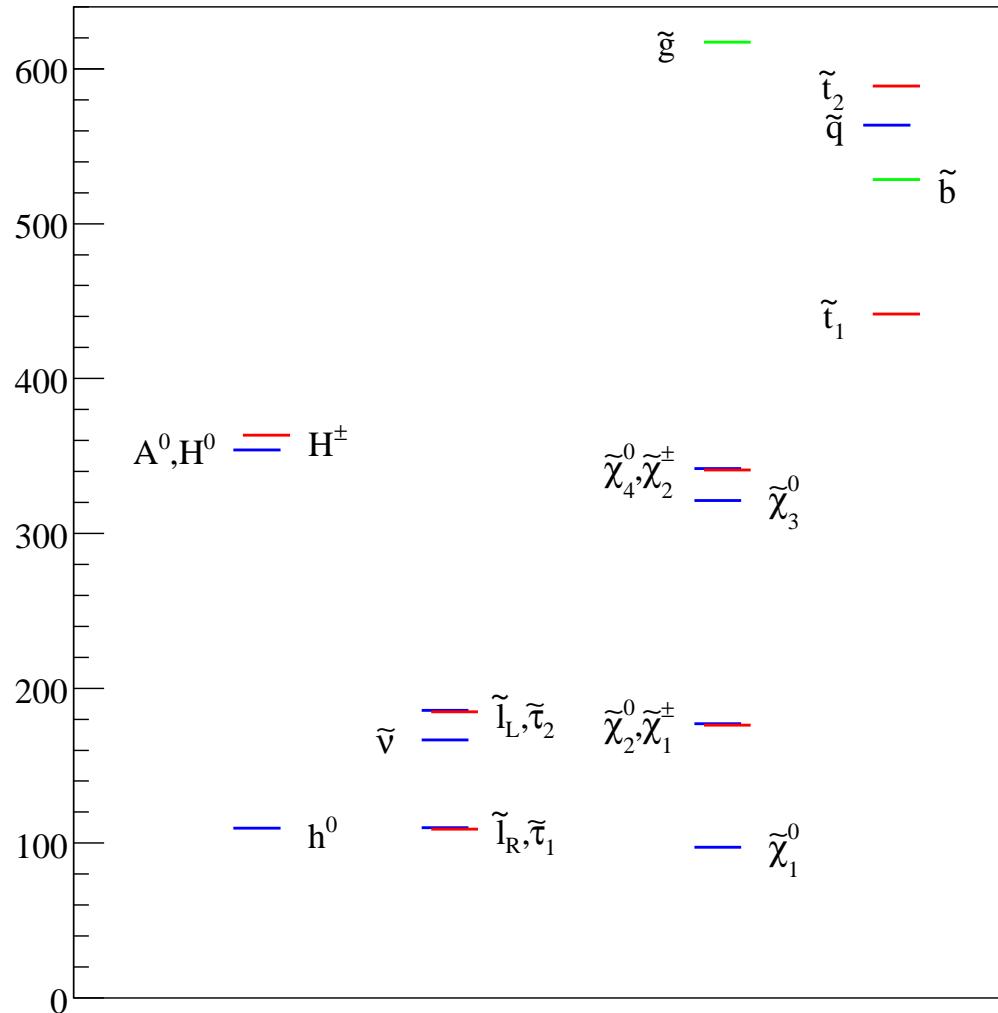
$$M_{\text{SUSY}} = 200 - 600 \text{ GeV}$$

2-loop calculation [Heinemeyer, Stöckinger, ...]



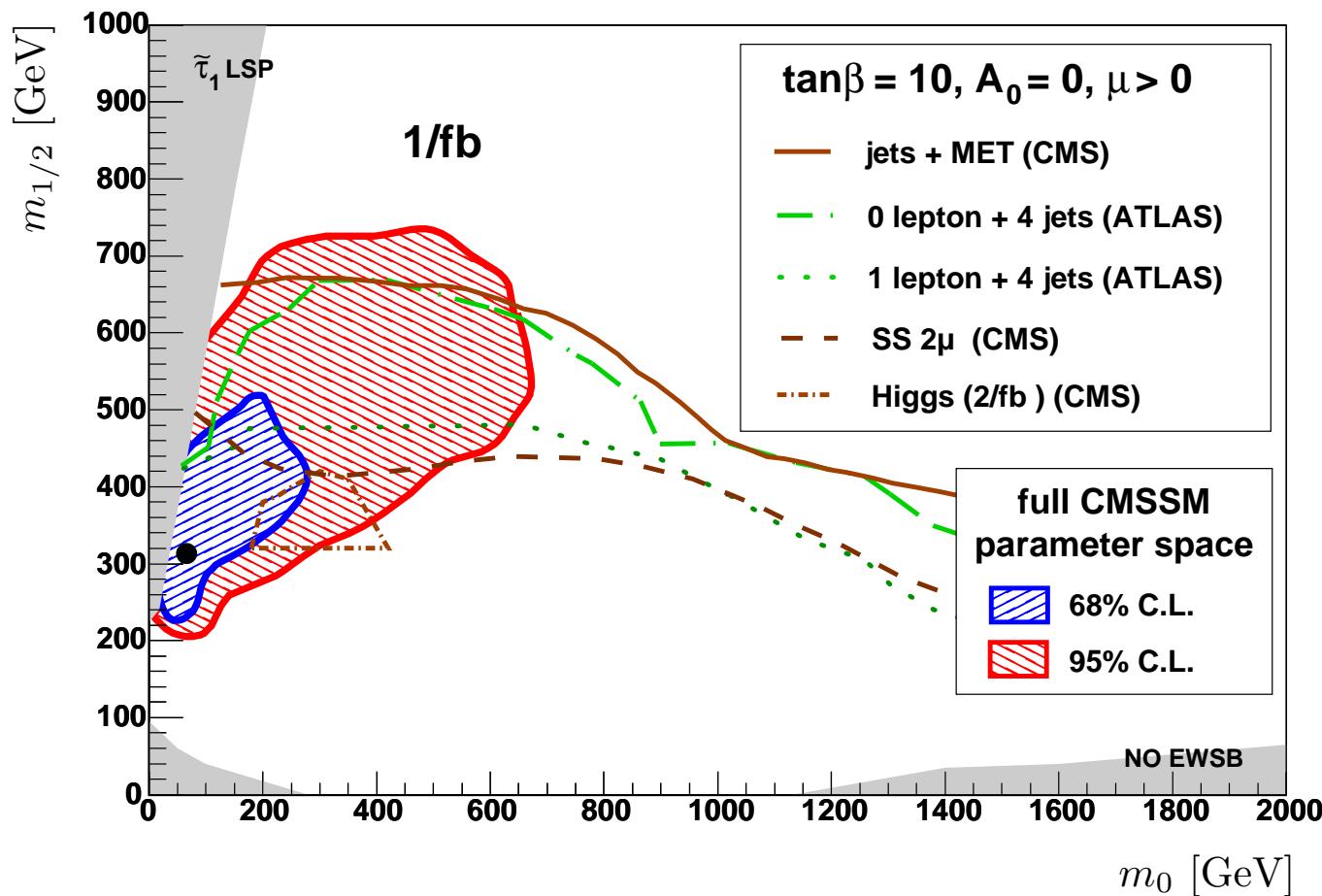
global fit in the constrained MSSM including data from $g - 2$, B physics, and cosmic relic density

[*O. Buchmüller, . . . , Weber, Weiglein*]

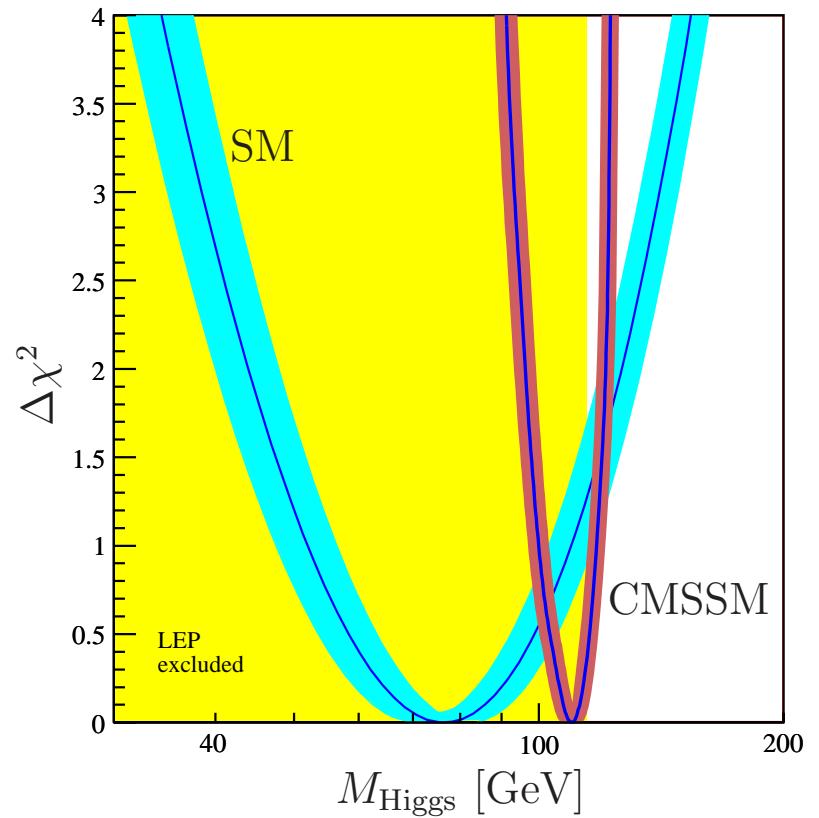
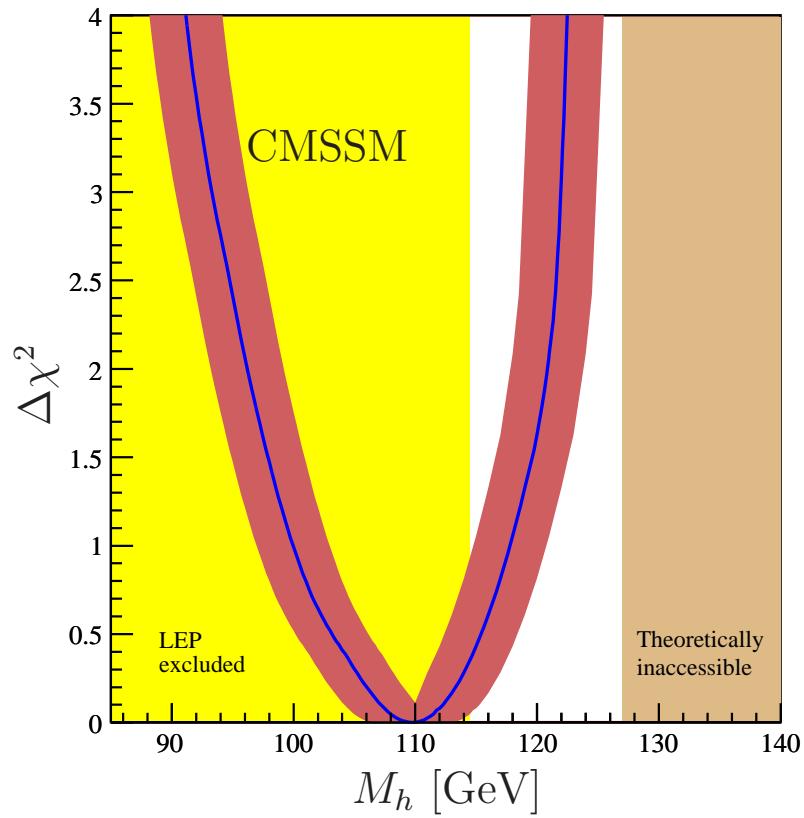


best fit particle spectrum

95% C.L. area in the $(m_{1/2}, m_0)$ plane to largest extend in the region that can be explored at the LHC with 1 fb^{-1}



[Buchmüller et al. 2008]



$$M_h = 110^{+8}_{-10} \text{ GeV}$$

SM Higgs:

- λH^4 term ad hoc
- Higgs boson mass: free parameter $\sim \sqrt{\lambda}$
- no a-priori reason for a light Higgs boson

SUSY Standard Model avoids these questions

$$H_2 = \begin{pmatrix} H_2^+ \\ v_2 + H_2^0 \end{pmatrix}, \quad H_1 = \begin{pmatrix} v_1 + H_1^0 \\ H_1^- \end{pmatrix}$$

couples to u couples to d

- SUSY gauge interaction $\rightarrow H^4$ terms
- self coupling remains weak

Higgs bosons

MSSM Higgs potential contains two Higgs doublets:

$$\begin{aligned} V = & m_1^2 H_1 \bar{H}_1 + m_2^2 H_2 \bar{H}_2 - m_{12}^2 (\epsilon_{ab} H_1^a H_2^b + \text{h.c.}) \\ & + \underbrace{\frac{g'^2 + g^2}{8}}_{\text{red}} (H_1 \bar{H}_1 - H_2 \bar{H}_2)^2 + \underbrace{\frac{g^2}{2}}_{\text{red}} |H_1 \bar{H}_2|^2 \end{aligned}$$

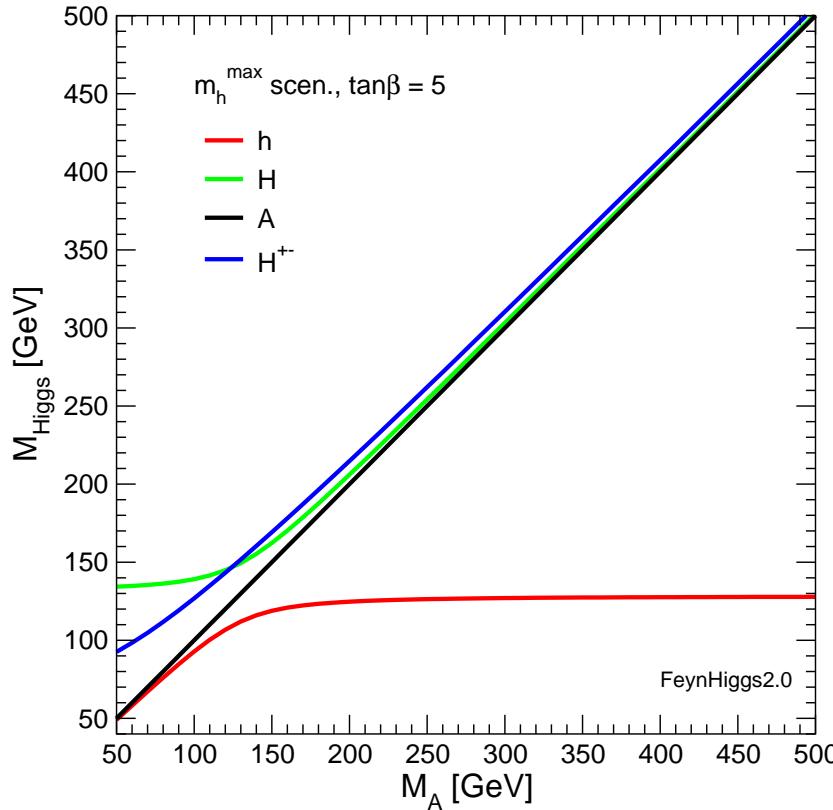
gauge couplings, in contrast to SM

Five physical states: h^0, H^0, A^0, H^\pm

Input parameters: $\tan \beta = \frac{v_2}{v_1}, M_A$

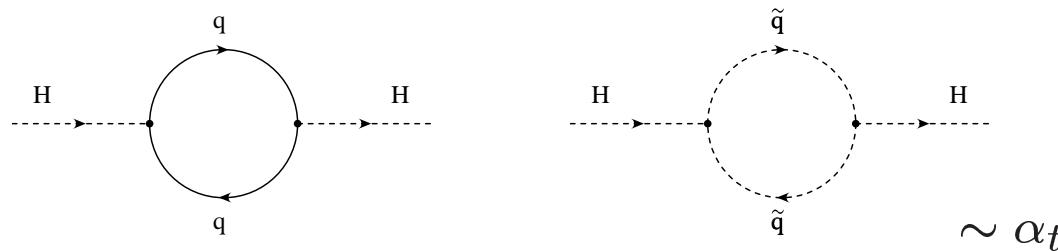
$\Rightarrow m_h, m_H, \text{mixing angle } \alpha, m_{H^\pm}$: no free parameters

Spectrum of Higgs bosons in the MSSM (example)



large M_A : h^0 like SM Higgs boson \sim decoupling regime

m_h^0 strongly influenced by quantum effects, e.g.



masses and couplings at higher order

dressed h, H propagators

$$(\Delta_{\text{Higgs}})^{-1} = \begin{pmatrix} q^2 - m_H^2 + \hat{\Sigma}_H(q^2) & \hat{\Sigma}_{hH}(q^2) \\ \hat{\Sigma}_{Hh}(q^2) & q^2 - m_h^2 + \hat{\Sigma}_h(q^2) \end{pmatrix}$$

- $\det = 0 \rightarrow m_{h,H}^{\text{pole}}$
 - diagonalization \rightarrow effective couplings, q^2 -dep.
- $\hat{\Sigma}(q^2) \rightarrow \hat{\Sigma}(0)$: rediagonalization with α_{eff}
 $\alpha \rightarrow \alpha_{\text{eff}}$ in tree-level couplings

1-loop: complete

2-loop:

- QCD corrections $\sim \alpha_s \alpha_t, \alpha_s \alpha_b$
- Yukawa corrections $\sim \alpha_{t,b}^2$

theoretical uncertainty:

$$\delta m_h \simeq 3\text{-}4 \text{ GeV}$$

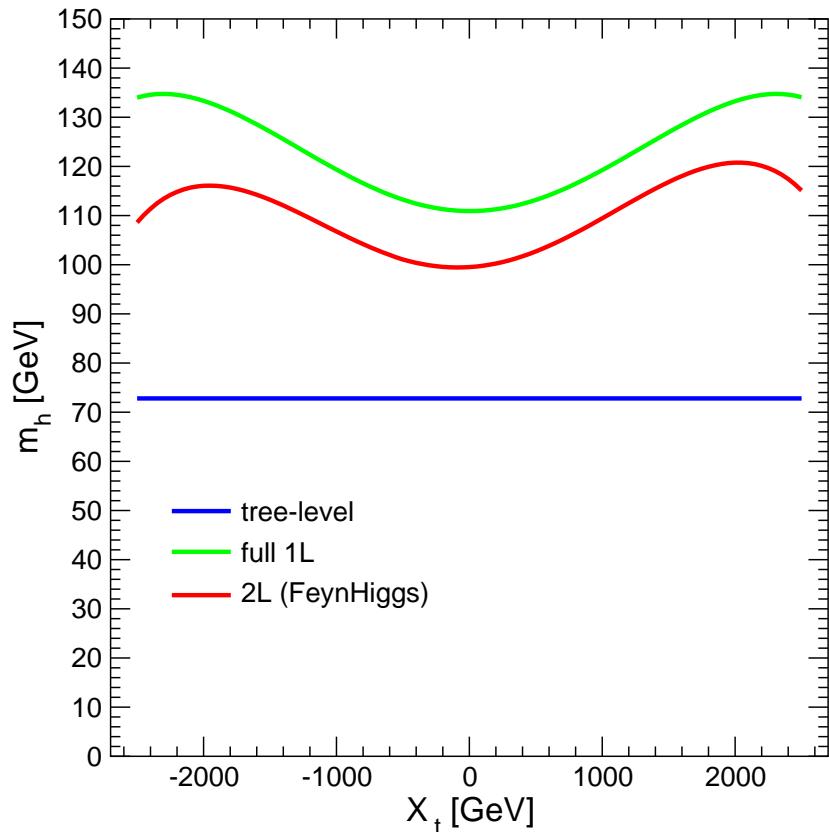
[Degrassi, Heinemeyer, WH, Slavich,
Weiglein]

public code

FeynHiggs2.6

latest version [arxiv:0710.4891]

m_{h^0} prediction at different levels of accuracy:



$$\tan \beta = 3, \quad M_{\tilde{Q}} = M_A = 1 \text{ TeV}, \quad m_{\tilde{g}} = 800 \text{ GeV}$$

X_t : top-squark mixing parameter

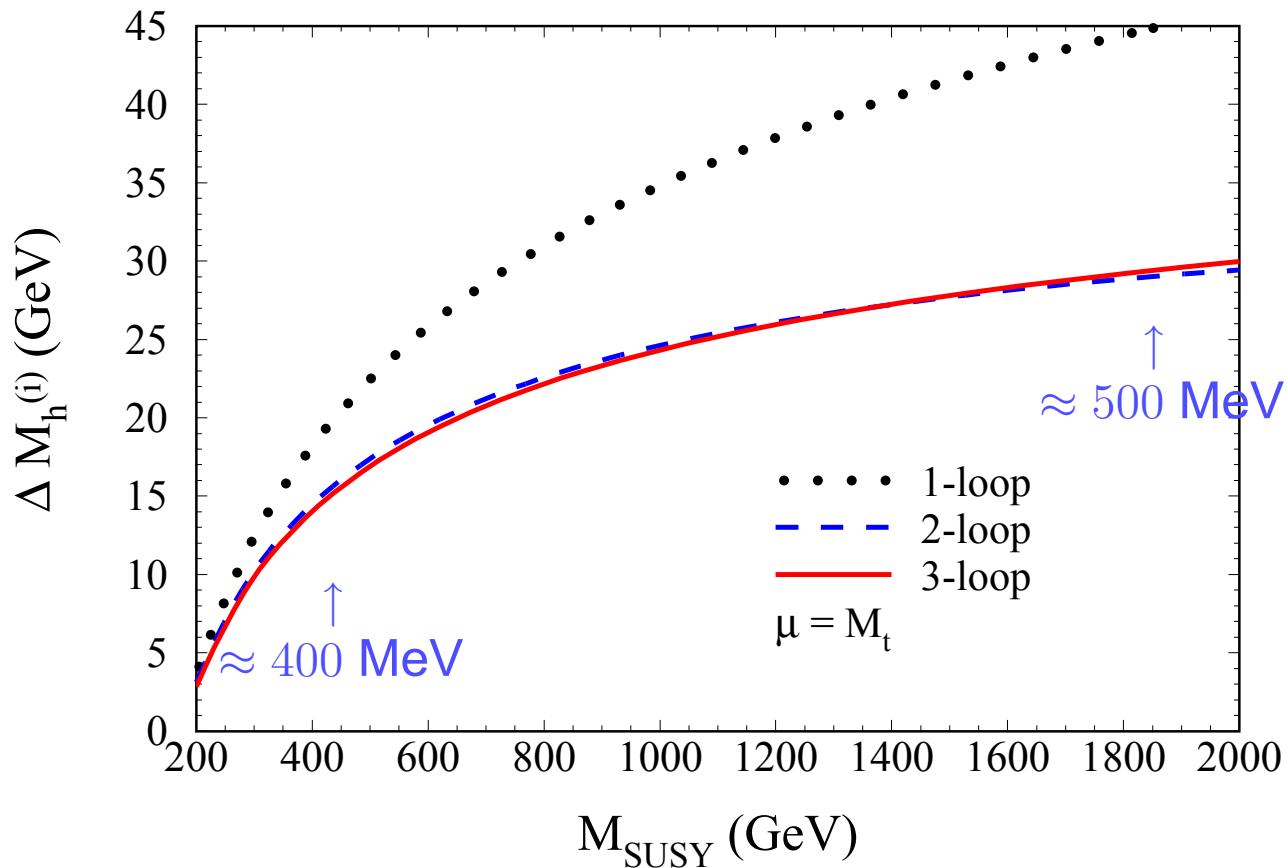
$$X_t = A_t - \mu \cot \beta$$

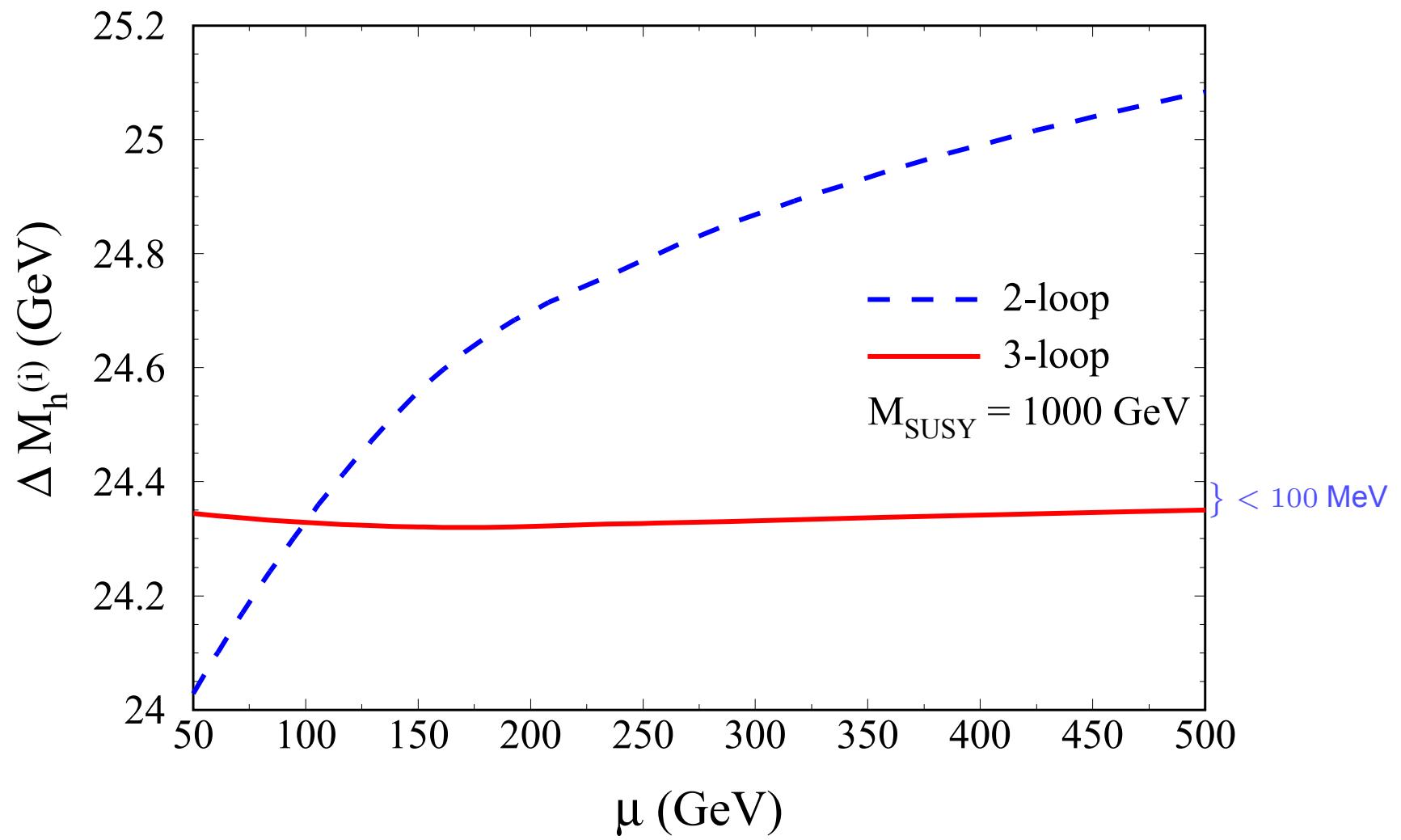
**full 2-loop contribution, effective potential approximation
3-loop EPA, LL and NLL**

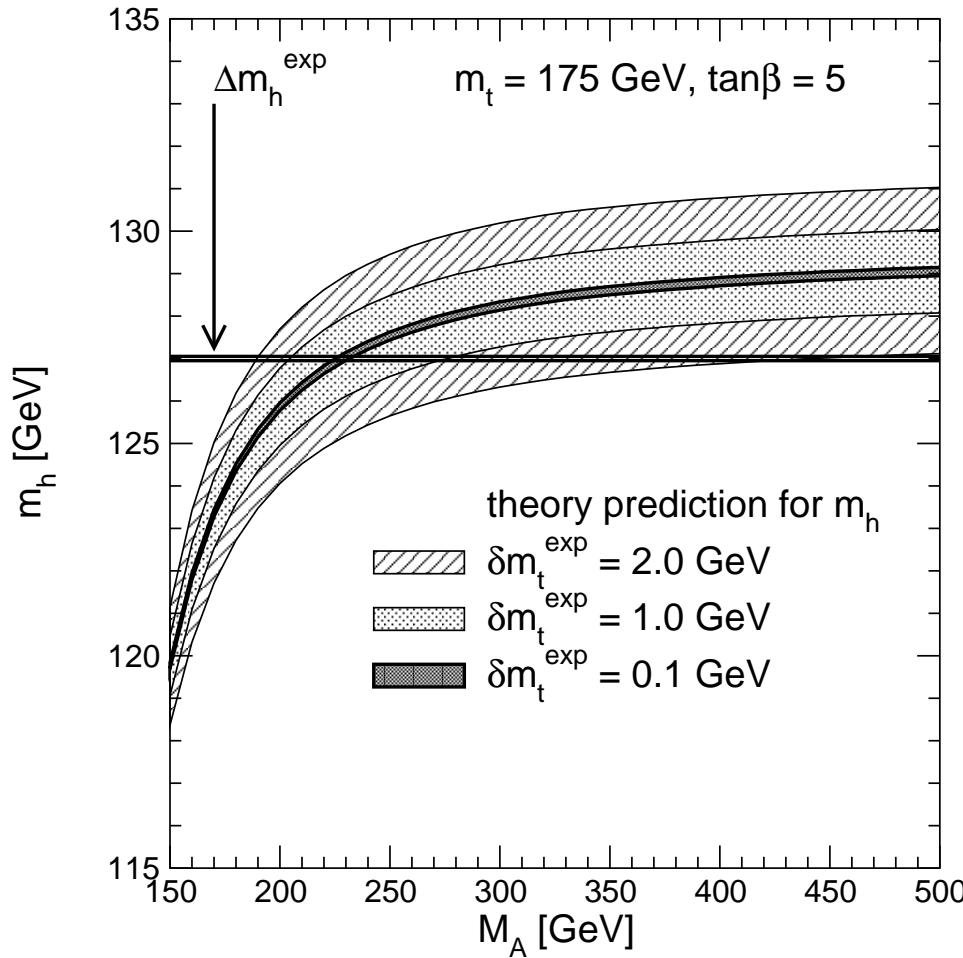
[*S. Martin*]

3-loop contributions $\sim \alpha_s^2 \alpha_t$

[*Harlander, Kant, Mihaila, Steinhauser*]







[Kraml et al.]

dependent on all SUSY particles and masses/mixings
through Higgs self-energies

Higgs bosons in the complex MSSM

Complex parameters enter via loop corrections:

- μ : Higgsino mass parameter
- $A_{t,b,\tau}$: trilinear couplings $\Rightarrow X_{t,b,\tau} = A_{t,b,\tau} - \mu^* \{\cot \beta, \tan \beta\}$ complex
- $M_{1,2}$: gaugino mass parameter (one phase can be eliminated)
- M_3 : gluino mass parameter

\Rightarrow can induce \mathcal{CP} -violating effects

Result:

$$(A, H, h) \rightarrow (h_3, h_2, h_1)$$

with

$$m_{h_3} > m_{h_2} > m_{h_1}$$

present status:

effective potential approximation + RGE

[Carena, Ellis, Pilaftsis, Wagner]

complete at one-loop order

[Frank, Hahn, Heinemeyer, WH, Rzehak, Weiglein]

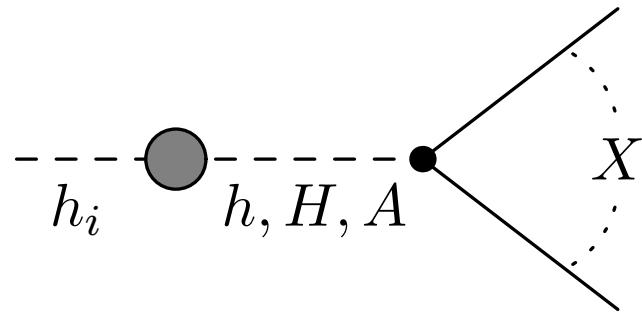
leading two-loop contributions of $\mathcal{O}(\alpha_s \alpha_t)$

[Heinemeyer, WH, Rzehak, Weiglein]

leading two-loop terms $\mathcal{O}(\alpha_t^2)$ by interpolation

$$\hat{\Sigma}(q^2) = \hat{\Sigma}^{(1\text{-loop})}(q^2) + \hat{\Sigma}^{(2\text{-loop})}(0)$$

couplings at higher order



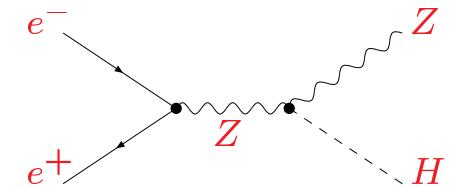
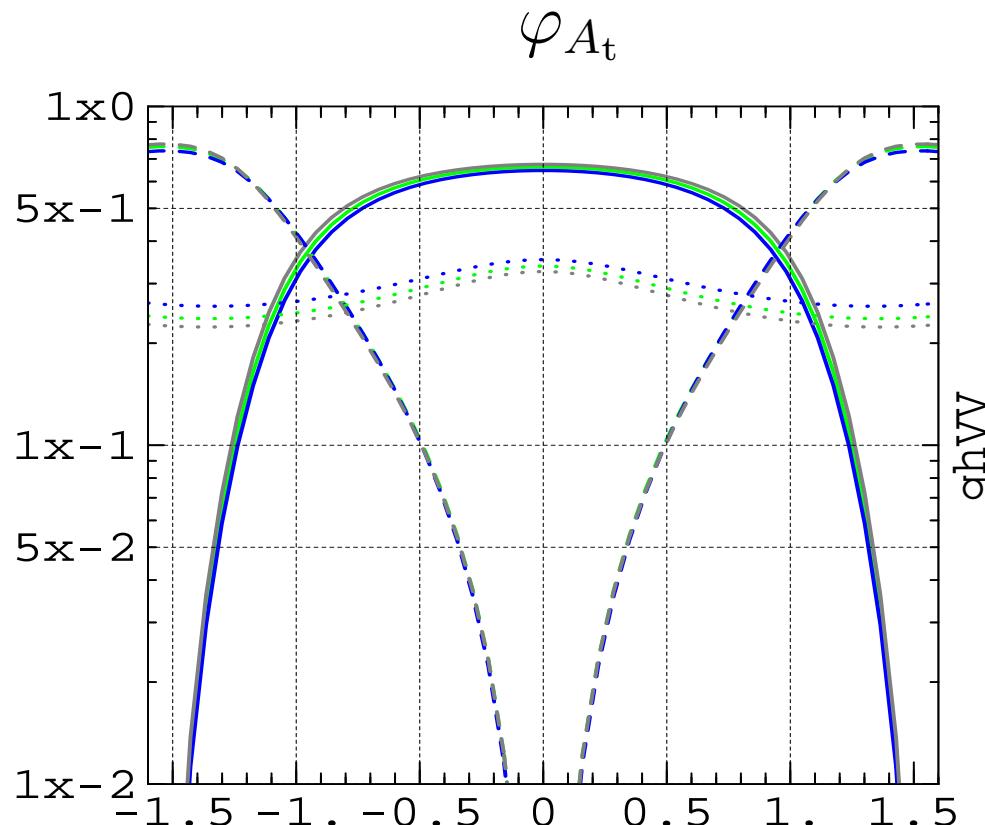
$$\Gamma_{h_1} = \sqrt{Z_h} (\Gamma_h + Z_{hH}\Gamma_H + Z_{hA}\Gamma_A)$$

$$\Gamma_{h_2} = \sqrt{Z_H} (Z_{Hh}\Gamma_h + \Gamma_H + Z_{HA}\Gamma_A)$$

$$\Gamma_{h_3} = \sqrt{Z_A} (Z_{Ah}\Gamma_h + Z_{AH}\Gamma_H + \Gamma_A)$$

approximation: $\hat{\Sigma}(0)$ effective couplings

couplings to vector bosons



full: h_1 , dashed: h_2 , dotted: h_3

Parameters:

$M_{\text{SUSY}} = 500 \text{ GeV},$

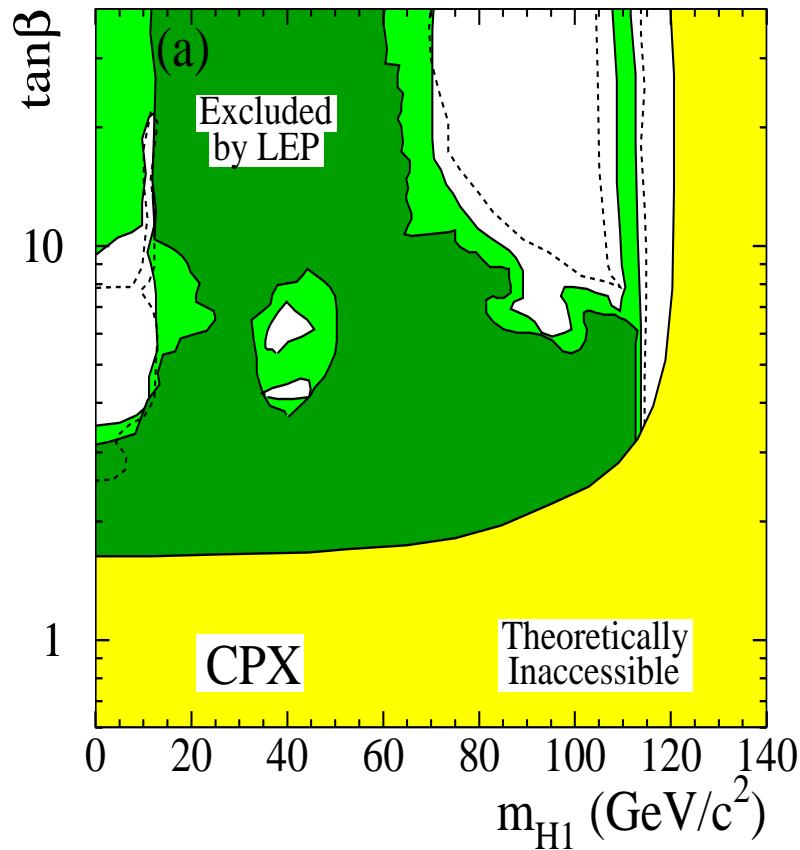
$M_2 = 500 \text{ GeV},$

$\mu = 2000 \text{ GeV},$

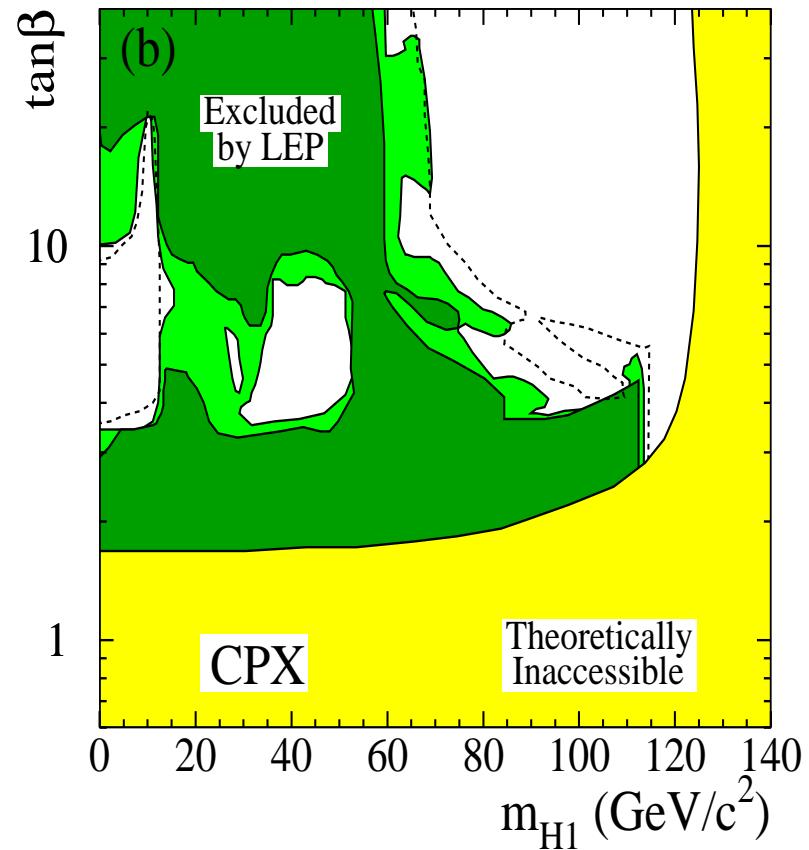
$|A_t| = 1000 \text{ GeV},$

$M_{H^\pm} = 150 \text{ GeV}, \tan \beta = 5$

$m_t = 169.3 \text{ GeV}$



$m_t = 174.3 \text{ GeV}$



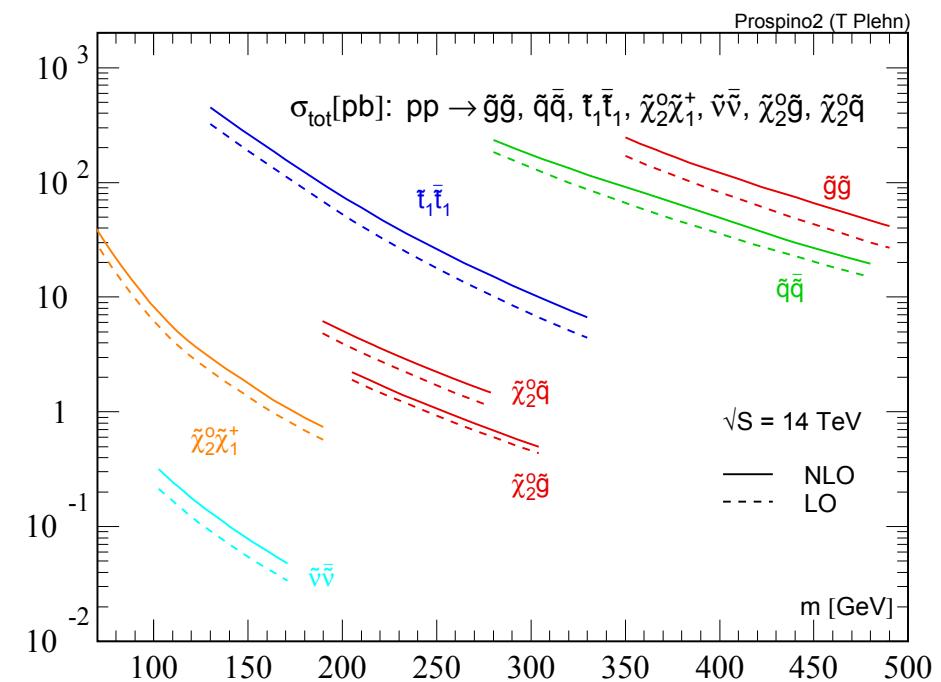
no lower limit on M_{h_1} : light SUSY Higgs not ruled out!

SUSY particle production

LHC: predominantly colored SUSY particles produced

- pair production of gluinos and squarks proceeds via **strong interaction**
→ **large cross sections**

- large top-Yukawa coupling:
top-squark \tilde{t}_1 candidate for
lightest squark
→ **high production rate**



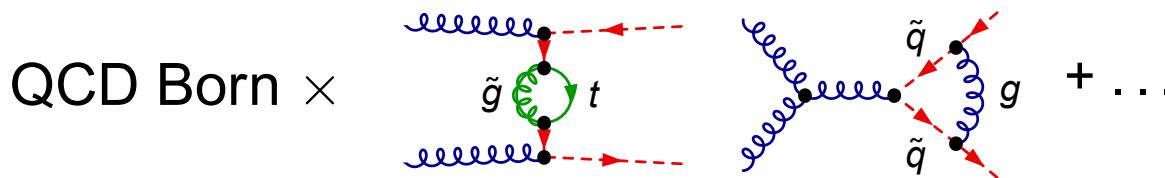
- **cross section depend** essentially **on final state masses**

Important higher order effects due to QCD corrections:

[Beenakker, Höpker, Spira, Zerwas '95 & '97] &
[Beenakker, Krämer, Plehn, Spira, Zerwas '98]

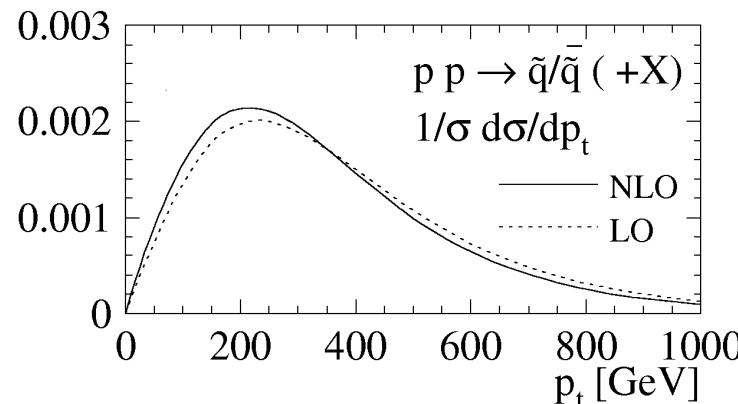
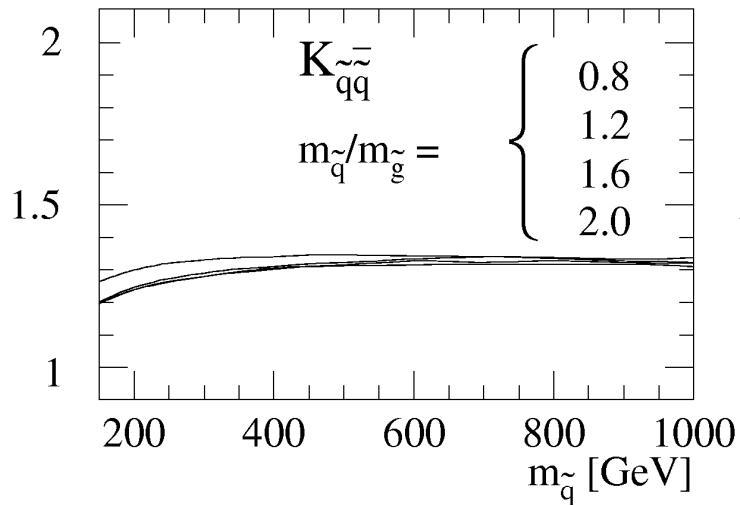
→ PROSPINO, also for $\tilde{g}\tilde{q}$, $\tilde{g}\tilde{g}$

- $\mathcal{O}(\alpha_s^3)$: QCD NLO corrections



+ real gluon & real quark radiation

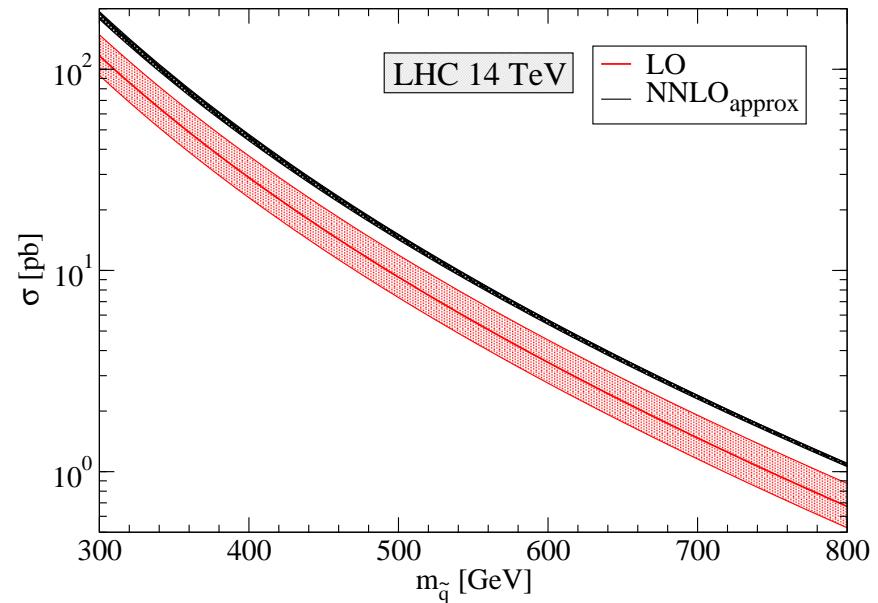
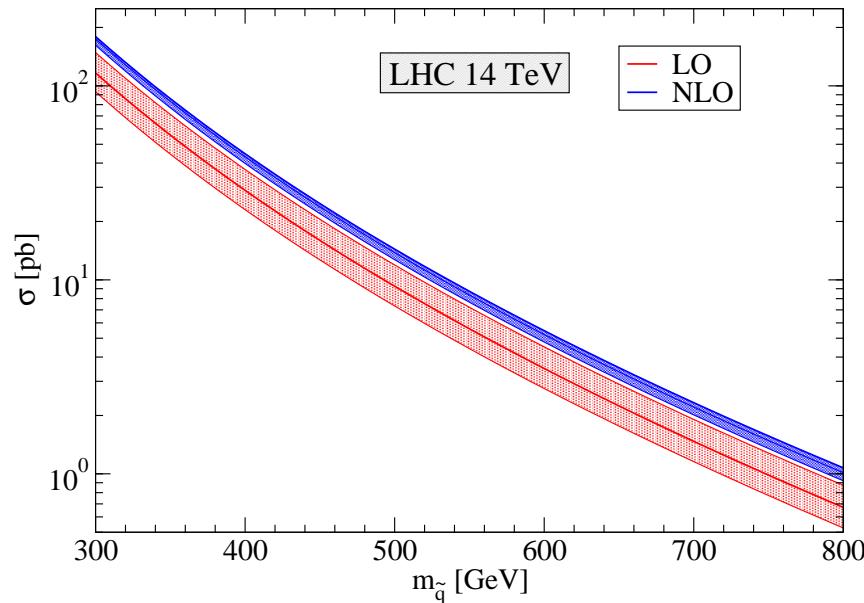
$[\tilde{q}\tilde{q}^*$ production:]



- large positive corrections
- reduced scale dependence
- negligible in normalized distributions

NNLO for squark production, dominant soft corrections

[Langenfeld, Moch 2009]



- improved theoretical prediction
- reduction of scale uncertainty

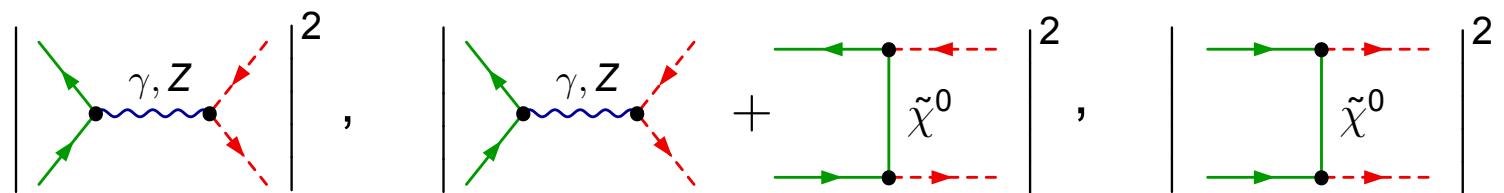
NNLO QCD contributions \sim electroweak contributions

EW tree level contributions to squark pair production

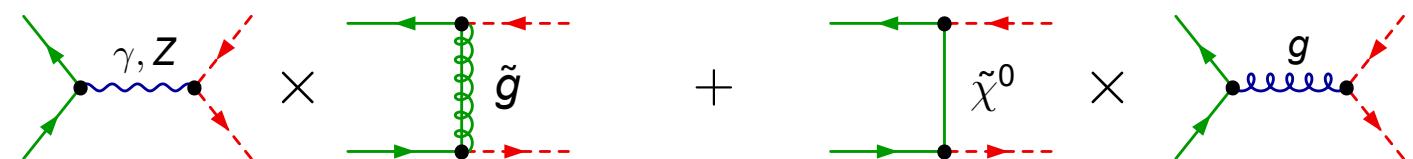
Bornhauser, Drees, Dreiner, Kim 2007

Bozzi, Fuks, Herrmann, Klasen 2007

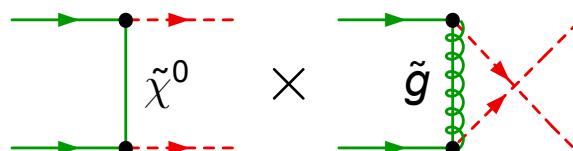
- $\mathcal{O}(\alpha^2)$: pure EW tree-level contributions ($\tilde{t}\tilde{t}^*$, $\tilde{q}\tilde{q}^*$, $\tilde{q}\tilde{q}$ prod.)



- $\mathcal{O}(\alpha_s \alpha)$: – EW-QCD tree-level interferences to $\tilde{q}\tilde{q}^*$ production



- EW-QCD tree-level interferences to $\tilde{q}\tilde{q}$ production

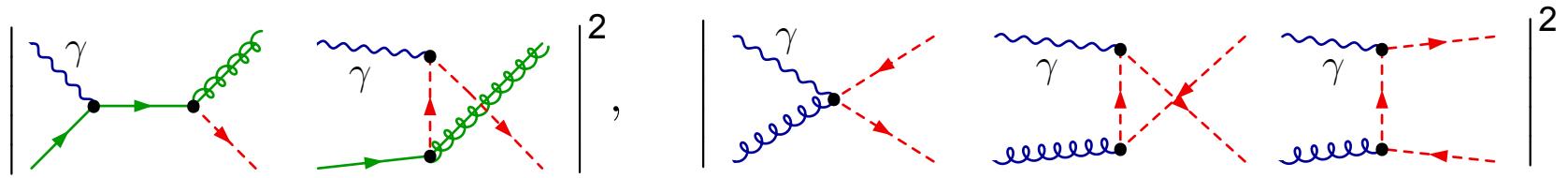


new production channel:

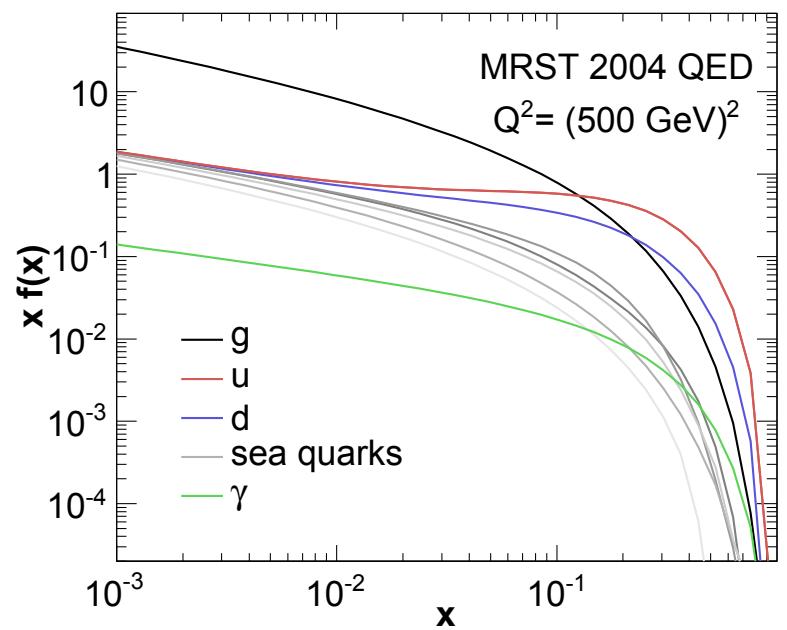
WH, Kollar, Trenkel 2007

WH, Mirabella 2008

- $\mathcal{O}(\alpha_s \alpha)$: photon induced processes



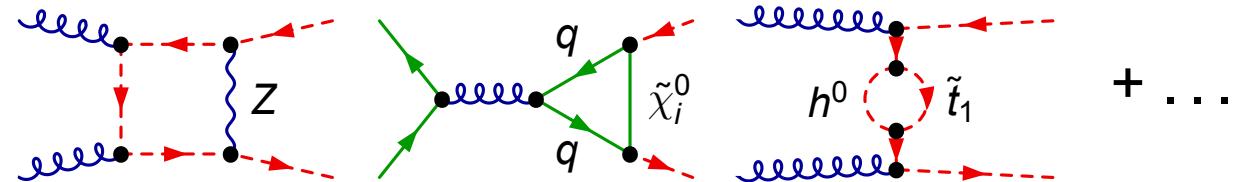
- not present at LO at the hadronic level
- **MRST 2004 QED**: inclusion of **NLO QED effects** in the evolution of PDFs
 - non-zero photon distribution
 - non-zero hadronic contributions



- $\mathcal{O}(\alpha_s^2 \alpha)$: NLO EW contributions

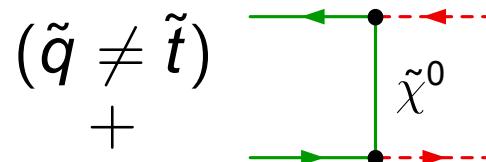
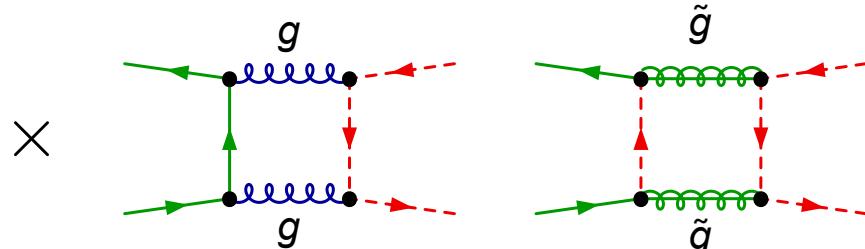
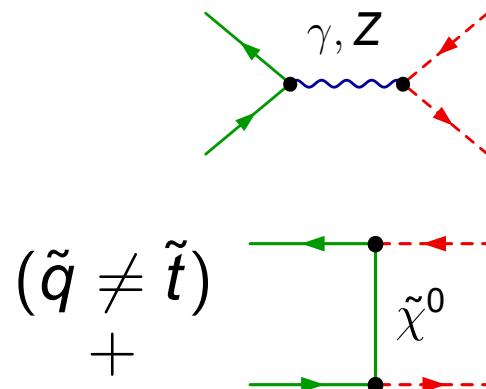
WH, Kollar, Mirabella, Trenkel 07,08

QCD Born \times



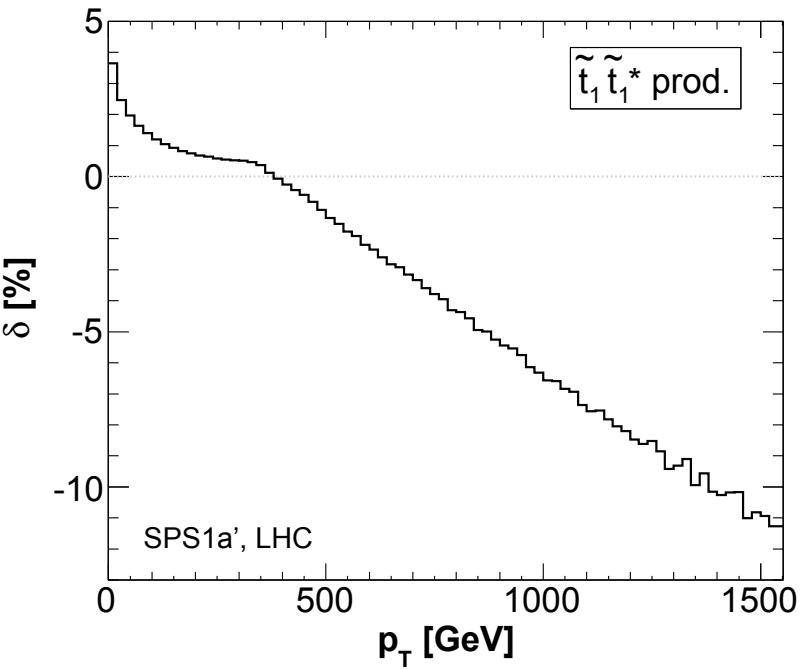
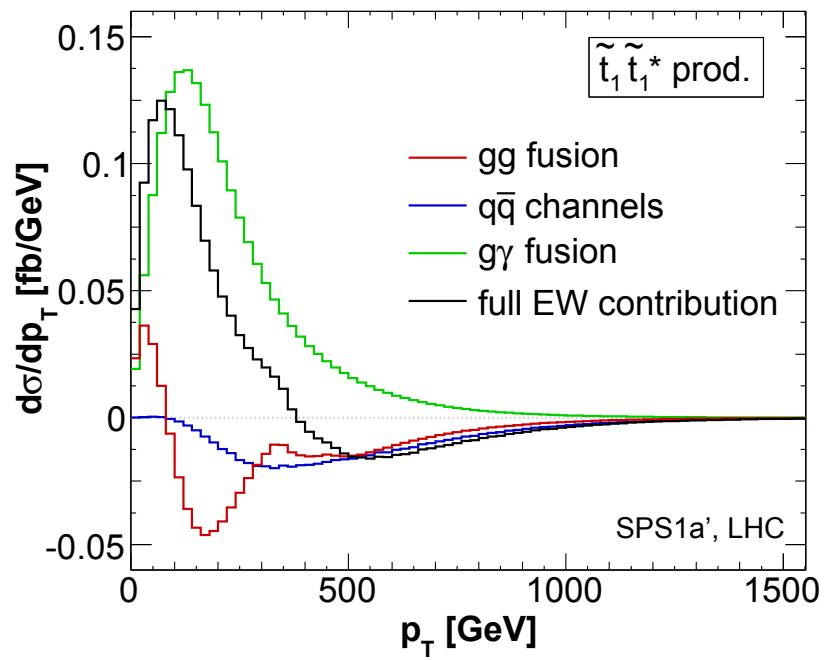
+ ...

- + EW-QCD one-loop interferences



\times full QCD 1-loop amplitude

- + real photon, gluon, and quark radiation



Overview: Squark and Gluino Production @ LHC

	$\mathcal{O}(\alpha_s^2)$	$\mathcal{O}(\alpha_s^3)$	$\mathcal{O}(\alpha^2)$	$\mathcal{O}(\alpha_s \alpha)$	$\mathcal{O}(\alpha_s \alpha)$	$\mathcal{O}(\alpha_s^2 \alpha)$
$\tilde{g}\tilde{g}$	+	+	-	-	-	+
$\tilde{g}\tilde{q}$	+	+	-	-	+	+
$\tilde{t}\tilde{t}^*$	+	+	+	-	+	+
$\tilde{q}\tilde{q}^*$	+	+	+	+	+	+
$\tilde{q}\tilde{q}$	+	+	+	+	-	+

EW contributions are chirality/flavour dependent

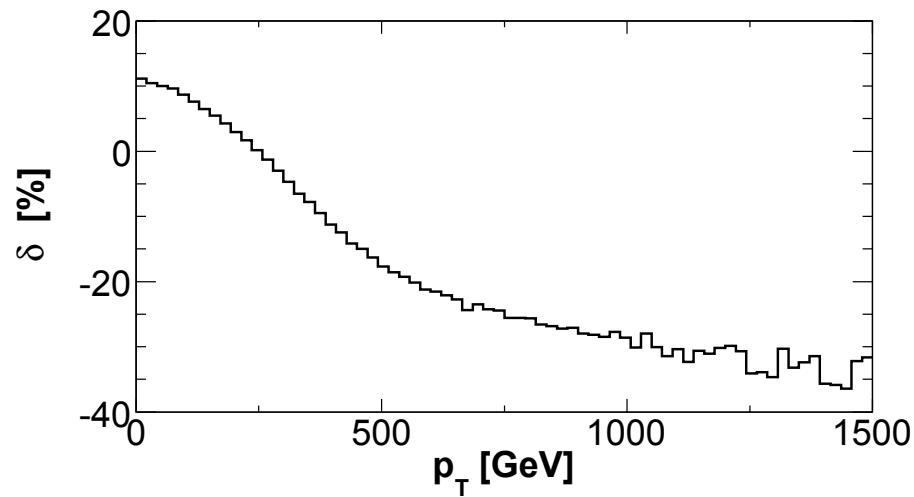
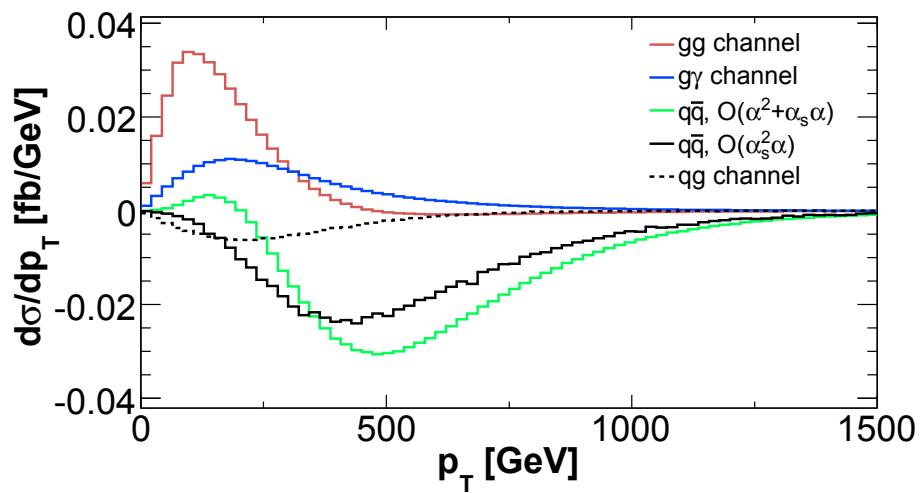
(xsection in pb, SPS1a')

	$\tilde{u}^R \tilde{u}^{R*}$	$\tilde{u}^L \tilde{u}^{L*}$	$\tilde{d}^L \tilde{d}^{L*}$	$\tilde{c}^L \tilde{c}^{L*}$
$\mathcal{O}(\alpha_s^2)$	$(36.83 \pm 0.03) \cdot 10^{-2}$	$(31.31 \pm 0.01) \cdot 10^{-2}$	$(25.89 \pm 0.01) \cdot 10^{-2}$	$(22.65 \pm 0.01) \cdot 10^{-2}$
$\mathcal{O}(\alpha_s \alpha)$	$(-9.00 \pm 0.01) \cdot 10^{-3}$	$(-3.54 \pm 0.01) \cdot 10^{-2}$	$(-3.83 \pm 0.01) \cdot 10^{-2}$	$(-2.82 \pm 0.01) \cdot 10^{-3}$
$\mathcal{O}(\alpha^2)$	$(-2.42 \pm 0.01) \cdot 10^{-3}$	$(-2.39 \pm 0.01) \cdot 10^{-2}$	$(-3.20 \pm 0.01) \cdot 10^{-2}$	$(-2.11 \pm 0.01) \cdot 10^{-3}$
$\mathcal{O}(\alpha_s^2 \alpha)$	$(-3.09 \pm 0.05) \cdot 10^{-3}$	$(-1.05 \pm 0.01) \cdot 10^{-2}$	$(-7.82 \pm 0.07) \cdot 10^{-3}$	$(-5.89 \pm 0.01) \cdot 10^{-3}$
$\delta(\%)$	-2.6	-7.0	-5.5	4.8

and fairly model dependent [example: $u_L u_L^*$]

	SPS5	SU1	SU4
$\mathcal{O}(\alpha_s^2)$	$(10.62 \pm 0.01) \cdot 10^{-2}$	$(51.77 \pm 0.02) \cdot 10^{-3}$	$(16.14 \pm 0.01) \cdot 10^{-1}$
$\mathcal{O}(\alpha_s \alpha)$	$(-1.37 \pm 0.01) \cdot 10^{-2}$	$(-7.22 \pm 0.01) \cdot 10^{-3}$	$(-1.45 \pm 0.01) \cdot 10^{-1}$
$\mathcal{O}(\alpha^2)$	$(-9.11 \pm 0.01) \cdot 10^{-3}$	$(-4.73 \pm 0.01) \cdot 10^{-3}$	$(-10.16 \pm 0.01) \cdot 10^{-2}$
$\mathcal{O}(\alpha_s^2 \alpha)$	$(-4.83 \pm 0.03) \cdot 10^{-3}$	$(-2.75 \pm 0.02) \cdot 10^{-3}$	$(-2.61 \pm 0.01) \cdot 10^{-2}$
$\delta(\%)$	-8.9	-10.1	-4.3

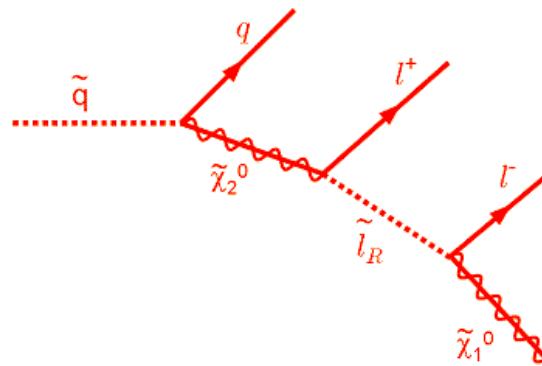
$u_L u_L^*$, $SPS1a'$



measurements at colliders

- LHC

- direct production $pp \rightarrow \tilde{q}\tilde{q}, \tilde{q}\tilde{g}, \tilde{g}\tilde{g}$
- decay chains $\tilde{q} \rightarrow q\tilde{\chi}_2^0 \rightarrow q(\ell\ell)\tilde{\chi}_1^0$



- ILC/CLIC

- separate study for individual s-particles

$$e^+ e^- \rightarrow \tilde{\chi}\tilde{\chi}$$

$$e^+ e^- \rightarrow \tilde{\ell}\tilde{\ell}$$

$$e^+ e^- \rightarrow \tilde{t}\tilde{t}$$

Accuracy of measurements

SPA Report, SPS1a' scenario]

LHC/ILC Report [Weiglein et al.]

Parameter	SPS1a' value	Fit error [exp]
M_1	103.3	0.1
M_2	193.4	0.1
M_3	568.9	7.8
μ	400.4	1.1
$M_{\tilde{e}_L}$	181.3	0.2
$M_{\tilde{e}_R}$	115.6	0.4
$M_{\tilde{\tau}_L}$	179.5	1.2
$M_{\tilde{u}_L}$	523.2	5.2
$M_{\tilde{u}_R}$	503.9	17.3
$M_{\tilde{t}_L}$	467.7	4.9
m_A	374.9	0.8
A_t	-525.6	24.6
$\tan \beta$	10.0	0.3

High Scale Extrapolations

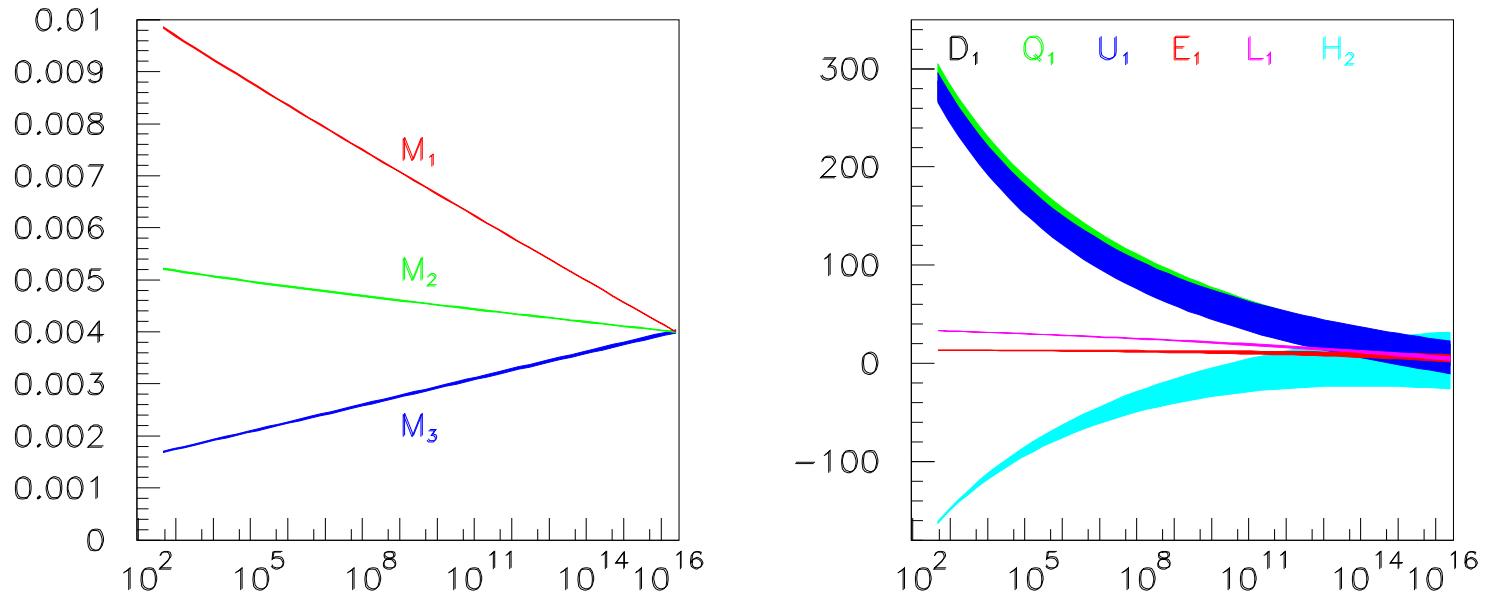


Fig. 1. Running of the gaugino and scalar mass parameters in SPS1a' [SPheno 2.2.2]. Only experimental errors are taken into account; theoretical errors are assumed to be reduced to the same size in the future.

SUSY particles

from experiment:

- precision analyses of masses and couplings LHC \oplus ILC

from theory:

- accurate theoretical predictions to match exp. data
- loop contributions to Lagrangian param \leftrightarrow observables
- reconstruction of fundamental SUSY parameters and breaking mechanism
- RGEs for extrapolation to high scales

Summary

- precise calculations for SUSY (MSSM) are well advanced
- electroweak precision observables with indirect sensitivity to SUSY parameters
 - global fits of similar quality as in standard model indirect sensitivity to SUSY parameters
- m_{h^0} is another precision observable
 - dependent on all SUSY sectors
 - accurate theoretical evaluation available,
but to be further improved
- progress for calculating SUSY processes at LHC and ILC,
future precision will allow tests of breaking scenarios