

Jet angular correlation in vector-boson fusion processes at hadron colliders

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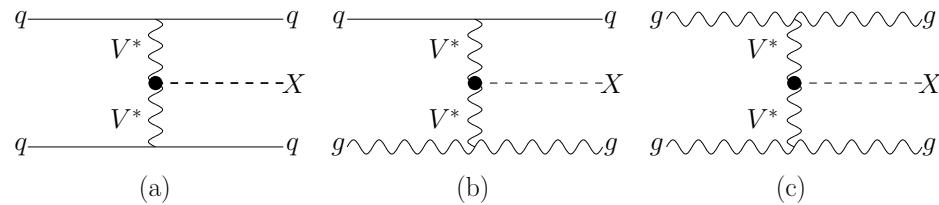
with Kaoru Hagiwara (KEK), Qiang Li (Karlsruhe U.)

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Contents

1. Introduction



2. Helicity formalism and kinematics

3. Helicity amplitudes for VBF (=WBF+GF) processes

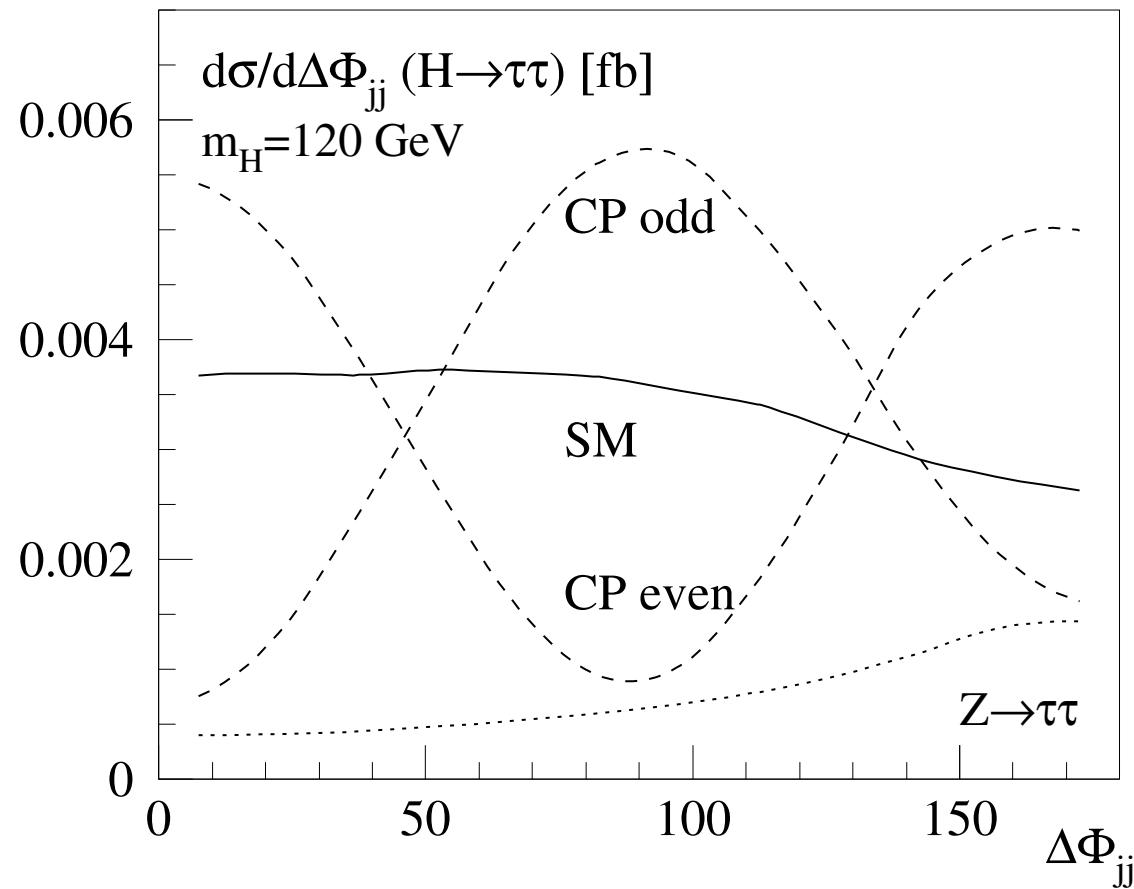
4. Azimuthal correlations between the two jets

- Higgs boson ($J = 0$) productions
- Massive graviton ($J = 2$) productions

5. Summary

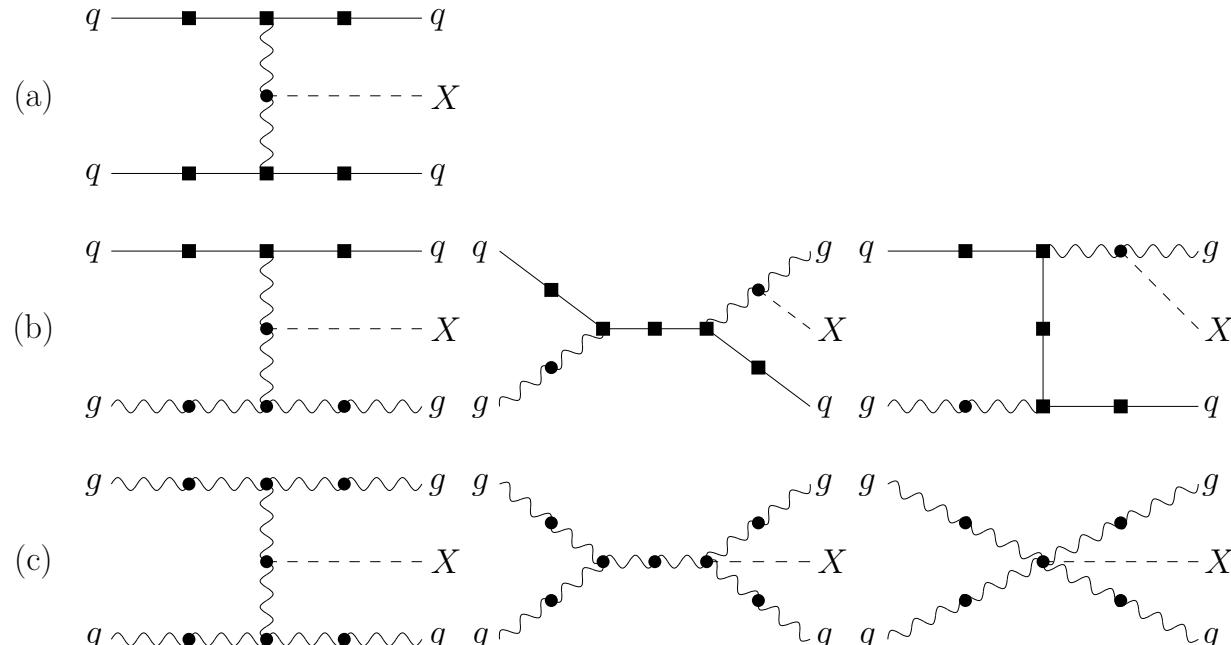
Azimuthal correlation between jets in Hjj events

T.Plehn, D.Rainwater, D.Zeppenfeld (2002)



- Azimuthal correlations reflect the tensor structures of the HVV coupling. Why does each tensor structure give such distributions?
- How about the correlation for spin-2 massive gravitons?

Subprocesses for $X + 2$ jet events

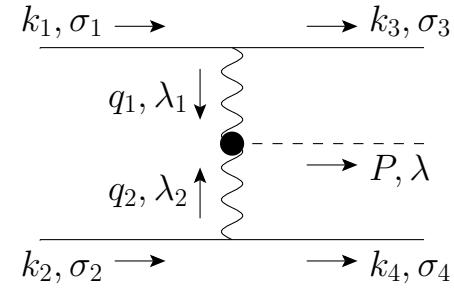


Higgs bosons: emitted from each of •

KK gravitons: emitted from each of • and □

Due to the t -channel propagators, the Xjj events via the VBF processes are dominantly produced when Q_i^2 are small, and hence the initial partons scatter to far forward and backward.

⇒ The large rapidity separation cut, or the VBF cut, can select the VBF diagram among the full diagrams.



The VBF helicity amplitudes

The helicity amplitudes for VBF processes

$$\mathcal{M}_{\sigma_1 \sigma_3, \sigma_2 \sigma_4}^{\lambda} = J^{\mu'_1}(k_1, k_3; \sigma_1, \sigma_3) \frac{-g_{\mu'_1 \mu_1} + \frac{q_{1\mu'_1} q_{1\mu_1}}{m_V^2}}{q_1^2 - m_V^2} J^{\mu'_2}(k_2, k_4; \sigma_2, \sigma_4) \frac{-g_{\mu'_2 \mu_2} + \frac{q_{2\mu'_2} q_{2\mu_2}}{m_V^2}}{q_2^2 - m_V^2} \Gamma_{XVV}^{\mu_1 \mu_2}(q_1, q_2; \lambda)^*$$

can be expressed by using

completeness relation

$$-g_{\mu' \mu} + \frac{q_i \mu' q_i \mu}{q_i^2} = \sum_{\lambda_i = \pm, 0} (-1)^{\lambda_i + 1} \epsilon_{\mu'}(q_i, \lambda_i)^* \epsilon_{\mu}(q_i, \lambda_i)$$

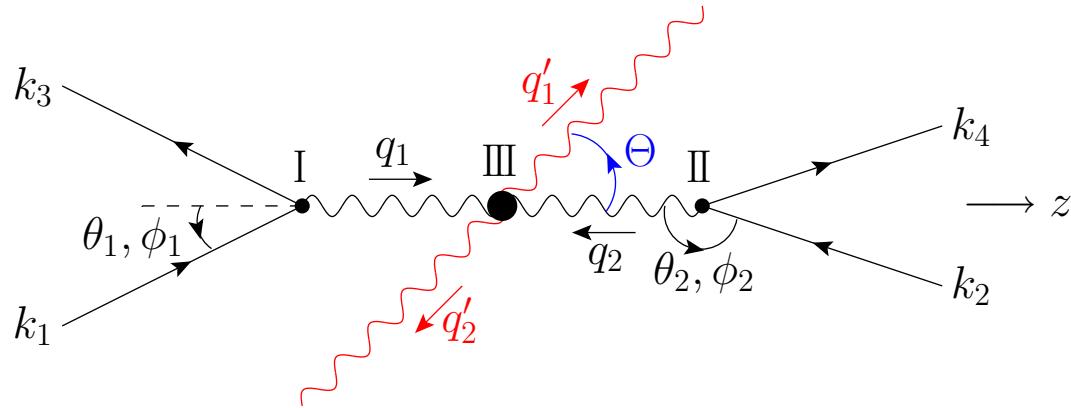
current conservation

$$q_i \mu J^{\mu}(k_i, k_{i+2}; \sigma_i, \sigma_{i+2}) = 0$$

as the product of the three helicity amplitudes summed over the polarization of the intermediate vector-bosons:

$$\begin{aligned} \mathcal{M}_{\sigma_1 \sigma_3, \sigma_2 \sigma_4}^{\lambda} &= \frac{1}{q_1^2 - m_V^2} J^{\mu'_1}(k_1, k_3; \sigma_1, \sigma_3) \sum_{\lambda_1 = \pm, 0} (-1)^{\lambda_1 + 1} \epsilon_{\mu'_1}(q_1, \lambda_1)^* \epsilon_{\mu_1}(q_1, \lambda_1) \\ &\quad \times \frac{1}{q_2^2 - m_V^2} J^{\mu'_2}(k_2, k_4; \sigma_2, \sigma_4) \sum_{\lambda_2 = \pm, 0} (-1)^{\lambda_2 + 1} \epsilon_{\mu'_2}(q_2, \lambda_2)^* \epsilon_{\mu_2}(q_2, \lambda_2) \\ &\quad \times \Gamma_{XVV}^{\mu_1 \mu_2}(q_1, q_2; \lambda)^* \\ &= \frac{1}{(q_1^2 - m_V^2)(q_2^2 - m_V^2)} \sum_{\lambda_1 = \pm, 0} \sum_{\lambda_2 = \pm, 0} \mathcal{J}_1^{\lambda_1}_{\sigma_1 \sigma_3} \mathcal{J}_2^{\lambda_2}_{\sigma_2 \sigma_4} \mathcal{M}_{X^{\lambda}}^{\lambda_{1,2}} \end{aligned}$$

Kinematics



I) q_1 Breit frame ($Q_1 = \sqrt{-q_1^2}$, $0 < \theta_1 < \pi/2$):

$$q_1^\mu = k_1^\mu - k_3^\mu = (0, 0, 0, Q_1)$$

$$k_1^\mu = \frac{Q_1}{2 \cos \theta_1} (1, \sin \theta_1 \cos \phi_1, \sin \theta_1 \sin \phi_1, \cos \theta_1)$$

$$k_3^\mu = \frac{Q_1}{2 \cos \theta_1} (1, \sin \theta_1 \cos \phi_1, \sin \theta_1 \sin \phi_1, -\cos \theta_1)$$

II) q_2 Breit frame ($Q_2 = \sqrt{-q_2^2}$, $\pi/2 < \theta_2 < \pi$):

$$q_2^\mu = k_2^\mu - k_4^\mu = (0, 0, 0, -Q_2)$$

$$k_2^\mu = -\frac{Q_2}{2 \cos \theta_2} (1, \sin \theta_2 \cos \phi_2, \sin \theta_2 \sin \phi_2, \cos \theta_2)$$

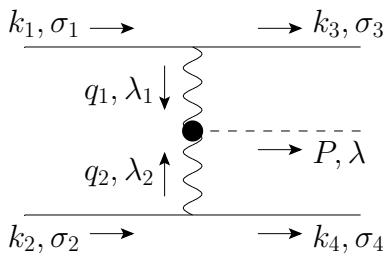
$$k_4^\mu = -\frac{Q_2}{2 \cos \theta_2} (1, \sin \theta_2 \cos \phi_2, \sin \theta_2 \sin \phi_2, -\cos \theta_2)$$

III) VBF frame (X rest frame):

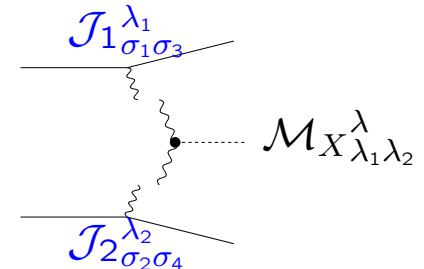
$$q_1^\mu + q_2^\mu = P^\mu = q'_1{}^\mu + q'_2{}^\mu = (M, 0, 0, 0)$$

$$q_1^\mu = \frac{M}{2} \left(1 - \frac{Q_1^2 - Q_2^2}{M^2}, 0, 0, \beta \right); \quad q'_1{}^\mu = \frac{M}{2} \left(1 + \frac{Q'_1{}^2 - Q'_2{}^2}{M^2}, \beta' \sin \Theta, 0, \beta' \cos \Theta \right)$$

$$q_2^\mu = \frac{M}{2} \left(1 - \frac{Q_2^2 - Q_1^2}{M^2}, 0, 0, -\beta \right); \quad q'_2{}^\mu = \frac{M}{2} \left(1 + \frac{Q'_2{}^2 - Q'_1{}^2}{M^2}, -\beta' \sin \Theta, 0, -\beta' \cos \Theta \right)$$



Current amplitudes



$$\mathcal{J}_{i\sigma_i\sigma_{i+2}}^{\lambda_i} = (-1)^{\lambda_i+1} \mathcal{J}^\mu(k_i, k_{i+2}; \sigma_i, \sigma_{i+2}) \epsilon_\mu(q_i, \lambda_i)^*$$

- Quark current vectors

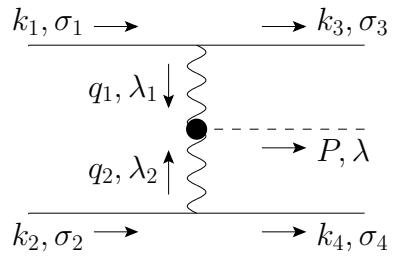
$$\mathcal{J}_{Vff'}^\mu(k_i, k_{i+2}; \sigma_i, \sigma_{i+2}) = g_{\sigma_i}^{Vff'} \bar{u}_{f'}(k_{i+2}, \sigma_{i+2}) \gamma^\mu u_f(k_i, \sigma_i)$$

- Gluon current vectors

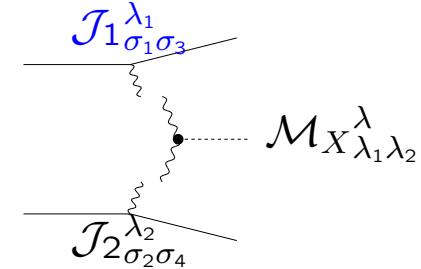
$$\begin{aligned} \mathcal{J}_{ggg}^\mu(k_i, k_{i+2}; \sigma_i, \sigma_{i+2}) &= g_s f^{abc} \epsilon_\alpha^b(k_i, \sigma_i) \epsilon_\beta^c(k_{i+2}, \sigma_{i+2})^* \\ &\times \left[-g^{\alpha\beta}(k_i + k_{i+2})^\mu - g^{\beta\mu}(-k_{i+2} + q_i)^\alpha - g^{\mu\alpha}(-q_i - k_i)^\beta \right] \end{aligned}$$

- Wavefunctions for the t -channel vector-bosons

$$\begin{array}{ll} \epsilon^\mu(q_1, \pm) = \frac{1}{\sqrt{2}}(0, \mp 1, -i, 0); & \epsilon^\mu(q_2, \pm) = \frac{1}{\sqrt{2}}(0, \mp 1, i, 0) \\ \epsilon^\mu(q_1, 0) = (1, 0, 0, 0); & \epsilon^\mu(q_2, 0) = (-1, 0, 0, 0) \end{array}$$



Current amplitudes

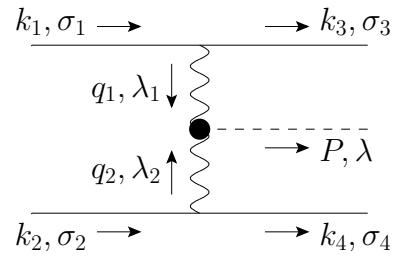


$\hat{\mathcal{J}}_1^{\lambda_1}_{\sigma_1 \sigma_3}$ (quark)

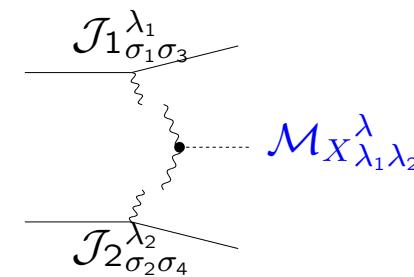
$$\begin{aligned}\hat{\mathcal{J}}_1^{+}_{++} &= -(\hat{\mathcal{J}}_1^{-}_{--})^* & \frac{1}{2 \cos \theta_1} (1 + \cos \theta_1) e^{-i\phi_1} \\ \hat{\mathcal{J}}_1^0_{++} &= \hat{\mathcal{J}}_1^0_{--} & -\frac{1}{\sqrt{2} \cos \theta_1} \sin \theta_1 \\ \hat{\mathcal{J}}_1^{-}_{++} &= -(\hat{\mathcal{J}}_1^{+}_{--})^* & -\frac{1}{2 \cos \theta_1} (1 - \cos \theta_1) e^{i\phi_1} \\ \hat{\mathcal{J}}_1^{\lambda_1}_{+-} &= \hat{\mathcal{J}}_1^{\lambda_1}_{-+} & 0\end{aligned}$$

$\hat{\mathcal{J}}_1^{\lambda_1}_{\sigma_1 \sigma_3}$ (gluon)

$$\begin{aligned}\hat{\mathcal{J}}_1^{+}_{++} &= -(\hat{\mathcal{J}}_1^{-}_{--})^* & \frac{1}{2 \sin \theta_1 \cos \theta_1} (1 + \cos \theta_1)^2 e^{-i\phi_1} \\ \hat{\mathcal{J}}_1^0_{++} &= \hat{\mathcal{J}}_1^0_{--} & -\frac{1}{\sqrt{2} \cos \theta_1} \\ \hat{\mathcal{J}}_1^{-}_{++} &= -(\hat{\mathcal{J}}_1^{+}_{--})^* & -\frac{1}{2 \sin \theta_1 \cos \theta_1} (1 - \cos \theta_1)^2 e^{i\phi_1} \\ \hat{\mathcal{J}}_1^{+}_{+-} &= -(\hat{\mathcal{J}}_1^{-}_{-+})^* & -\frac{2}{\tan \theta_1} e^{i\phi_1} \\ \hat{\mathcal{J}}_1^{0/-}_{+-} &= \hat{\mathcal{J}}_1^{0/+}_{-+} & 0\end{aligned}$$



XVV vertex



- $VV \rightarrow X$ fusion amplitudes:

$$\mathcal{M}_{X\lambda_1\lambda_2}^\lambda = \epsilon_\mu(q_1, \lambda_1) \epsilon_\nu(q_2, \lambda_2) \Gamma_{XVV}^{\mu\nu}(q_1, q_2; \lambda)^*$$

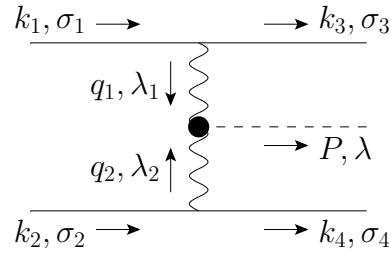
- Effective Lagrangian:

$$\begin{aligned} \mathcal{L}_{H,A} &= -\frac{1}{4}g_{Hgg}HF_{\mu\nu}^a F^{a,\mu\nu} - \frac{1}{4}g_{Agg}AF_{\mu\nu}^a \tilde{F}^{a,\mu\nu} \\ \mathcal{L}_G &= -\frac{1}{\Lambda}T^{\mu\nu}G_{\mu\nu} \end{aligned}$$

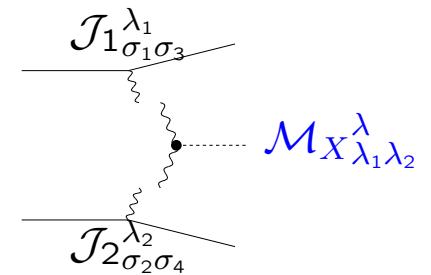
- XVV vertex:

X	(λ)	V	$\Gamma_{XVV}^{\mu\nu}/g_{XVV}$
H	(0)	W, Z	$g^{\mu\nu}$
H	(0)	$\gamma, Z/\gamma, g$	$q_1 \cdot q_2 g^{\mu\nu} - q_2^\mu q_1^\nu$
A	(0)	$\gamma, Z/\gamma, g$	$\epsilon^{\mu\nu\alpha\beta} q_{1\alpha} q_{2\beta}$
G	$(\pm 2, \pm 1, 0)$	W, Z, γ, g	$\epsilon_{\alpha\beta} \hat{\Gamma}_{GVV}^{\alpha\beta\mu\nu}$

* $\epsilon^{\alpha\beta}(P, \lambda)$: the polarization tensor; $\hat{\Gamma}_{GVV}^{\alpha\beta\mu\nu}(q_1, q_2)$: the GVV vertex



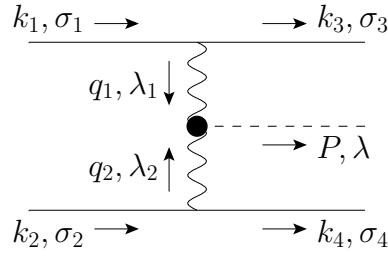
$V^*V^* \rightarrow H/A$ amplitudes



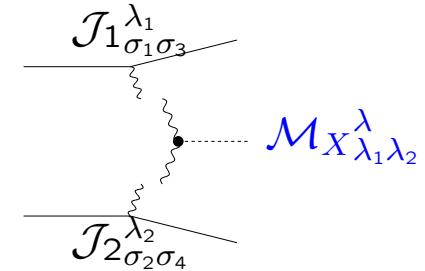
λ	$(\lambda_1 \lambda_2)$	$CP\text{-even}$		$CP\text{-odd}$
		$H(\text{WBF})$	$H(\text{loop-induced})$	A
0	$(\pm\pm)$	-1	$-\frac{1}{2}(M^2 + Q_1^2 + Q_2^2)$	$\mp\frac{i}{2}\sqrt{(M^2 + Q_1^2 + Q_2^2)^2 - 4Q_1^2Q_2^2}$
0	(00)	$\frac{M^2 + Q_1^2 + Q_2^2}{2Q_1Q_2}$	Q_1Q_2	0

For $Q_1, Q_2 \ll M$, where the VBF contributions dominant,

- WBF H : produced by the **longitudinally** polarized vector-bosons.
- GF H/A : produced by the **transversely** polarized vector-bosons.



$g^* g^* \rightarrow G$ amplitudes



λ	$(\lambda_1 \lambda_2)$	G
± 2	$(\pm \mp)$	$-(M^2 + Q_1^2 + Q_2^2)$
± 1	(± 0)	$\frac{1}{\sqrt{2}M} Q_2 (M^2 - Q_1^2 + Q_2^2)$
± 1	$(0 \mp)$	$\frac{1}{\sqrt{2}M} Q_1 (M^2 + Q_1^2 - Q_2^2)$
0	$(\pm \pm)$	$\frac{1}{\sqrt{6}M^2} [(Q_1^2 - Q_2^2)^2 + M^2(Q_1^2 + Q_2^2)]$
0	(00)	$-\frac{4}{\sqrt{6}} Q_1 Q_2$

For $Q_1, Q_2 \ll M$, the $\lambda = \pm 2$ states are dominantly produced through the collisions of the vector-bosons which have the **opposite-sign transverse polarization**.

Azimuthal correlations for Higgs bosons

The $J = 0$ VBF amplitudes are the sum of the three amplitudes:

$$\begin{aligned} \mathcal{M}_{\sigma_1\sigma_3,\sigma_2\sigma_4}^{\lambda=0} &= \frac{1}{(Q_1^2 + m_V^2)(Q_2^2 + m_V^2)} \sum_{\lambda_1=\pm,0} \sum_{\lambda_2=\pm,0} \mathcal{J}_1^{\lambda_1}_{\sigma_1\sigma_3} \mathcal{J}_2^{\lambda_2}_{\sigma_2\sigma_4} \mathcal{M}_X^{\lambda=0} \\ &\sim \hat{\mathcal{J}}_1^+_{\sigma_1\sigma_3} \hat{\mathcal{J}}_2^+_{\sigma_2\sigma_4} \hat{\mathcal{M}}_X^0_{++} e^{-i(\phi_1-\phi_2)} + \hat{\mathcal{J}}_1^0_{\sigma_1\sigma_3} \hat{\mathcal{J}}_2^0_{\sigma_2\sigma_4} \hat{\mathcal{M}}_X^0_{00} \\ &\quad + \hat{\mathcal{J}}_1^-_{\sigma_1\sigma_3} \hat{\mathcal{J}}_2^-_{\sigma_2\sigma_4} \hat{\mathcal{M}}_X^0_{--} e^{i(\phi_1-\phi_2)} \end{aligned}$$

The squared amplitudes are

$$\sum_{\sigma_1,\dots,4} |\mathcal{M}_{\sigma_1\sigma_3,\sigma_2\sigma_4}^{\lambda=0}|^2 = \Sigma_0 + \Sigma_1 \cos \Delta\phi + \Sigma_2 \cos 2\Delta\phi \quad (\Delta\phi \equiv \phi_1 - \phi_2)$$

The azimuthal correlation is manifestly expressed by the interference among different helicity states of the intermediate vector-bosons.

The different tensor structures of the XVV couplings give rise to the different azimuthal angle dependences:

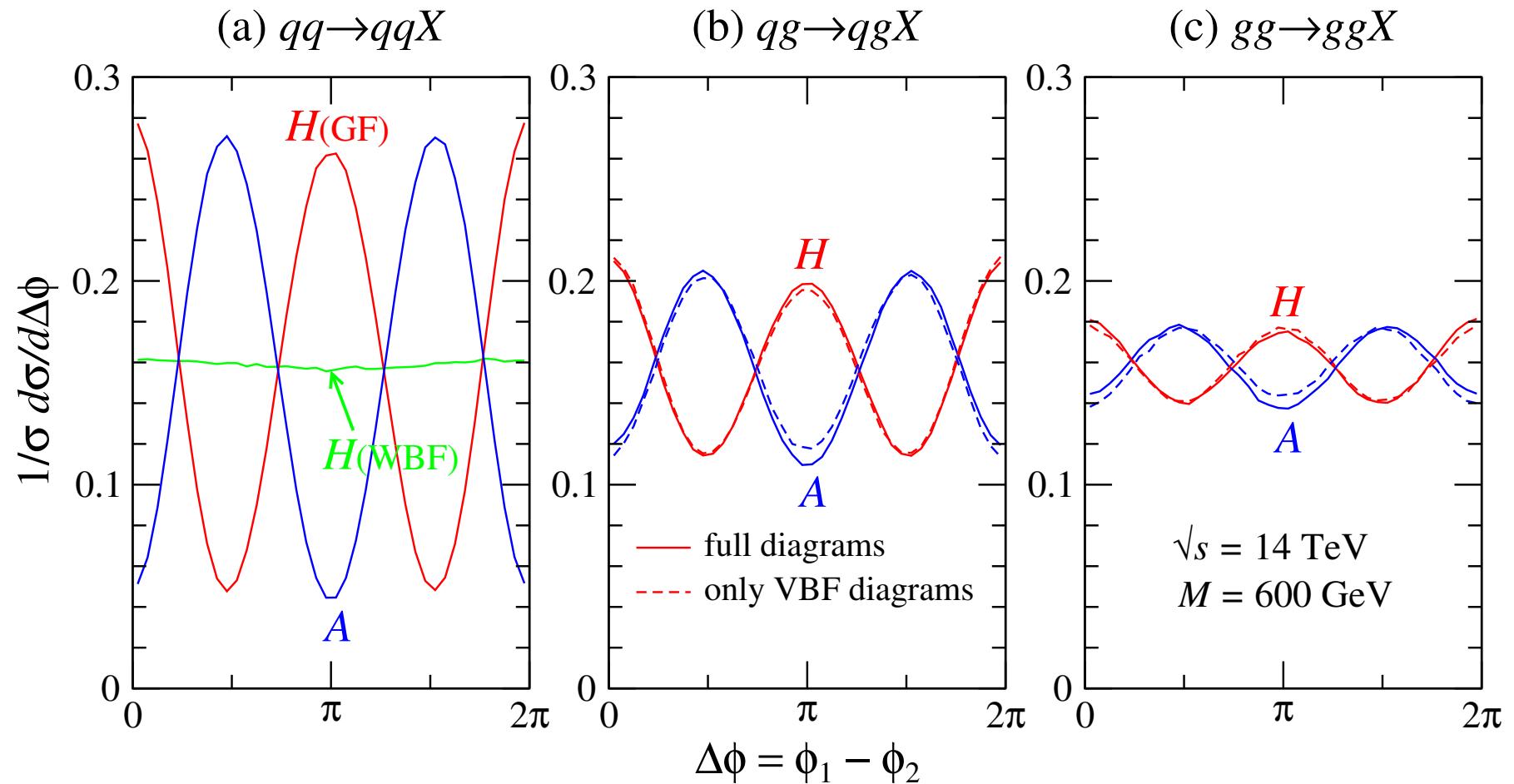
$$H(\text{WBF}) : \mathcal{M}_{00} \gg \mathcal{M}_{++} = \mathcal{M}_{--} \Rightarrow d\hat{\sigma}/d\Delta\phi \sim \text{constant}$$

$$H(\text{GF}) : \mathcal{M}_{00} \ll \mathcal{M}_{++} = \mathcal{M}_{--} \Rightarrow d\hat{\sigma}/d\Delta\phi \sim \Sigma_0 + |\Sigma_2| \cos 2\Delta\phi$$

$$A : \mathcal{M}_{00} = 0, \mathcal{M}_{++} = -\mathcal{M}_{--} \Rightarrow d\hat{\sigma}/d\Delta\phi \sim \Sigma_0 - |\Sigma_2| \cos 2\Delta\phi$$

$\Delta\phi$ distributions for Higgs bosons

The VBF cuts: $\eta_{j_1} > 0 > \eta_{j_2}$, $\Delta\eta_{jj} = \eta_{j_1} - \eta_{j_2} > 4$



➡ The VBF contributions can reproduce the distributions with the exact matrix elements very well even for the GF processes.

Azimuthal correlations for gravitons

The VBF G production plus its 2-body decay amplitudes are

$$\begin{aligned} \mathcal{M}_{\sigma_1, \dots, 4; \sigma_{5,6}} &= \frac{1}{Q_1^2 Q_2^2} \sum_{\lambda_1} \sum_{\lambda_2} \mathcal{J}_1^{\lambda_1}_{\sigma_1 \sigma_3} \mathcal{J}_2^{\lambda_2}_{\sigma_2 \sigma_4} \mathcal{M}_{G \lambda_1 \lambda_2}^{\lambda = \lambda_1 - \lambda_2} \frac{d_{\lambda, \lambda'}^2(\Theta)}{P^2 - M^2 + iM\Gamma} \mathcal{M}'_{G \sigma_5 \sigma_6}^{\lambda' = \sigma_5 - \sigma_6} \\ &\sim \hat{\mathcal{J}}_1^+_{\sigma_1 \sigma_3} \hat{\mathcal{J}}_2^-_{\sigma_2 \sigma_4} \hat{\mathcal{M}}_{G+-}^{+2} e^{-i(\phi_1 + \phi_2)} d_{+2, \lambda'}^2(\Theta) \\ &\quad + \hat{\mathcal{J}}_1^-_{\sigma_1 \sigma_3} \hat{\mathcal{J}}_2^+_{\sigma_2 \sigma_4} \hat{\mathcal{M}}_{G-+}^{-2} e^{i(\phi_1 + \phi_2)} d_{-2, \lambda'}^2(\Theta) \end{aligned}$$

The squared amplitudes are

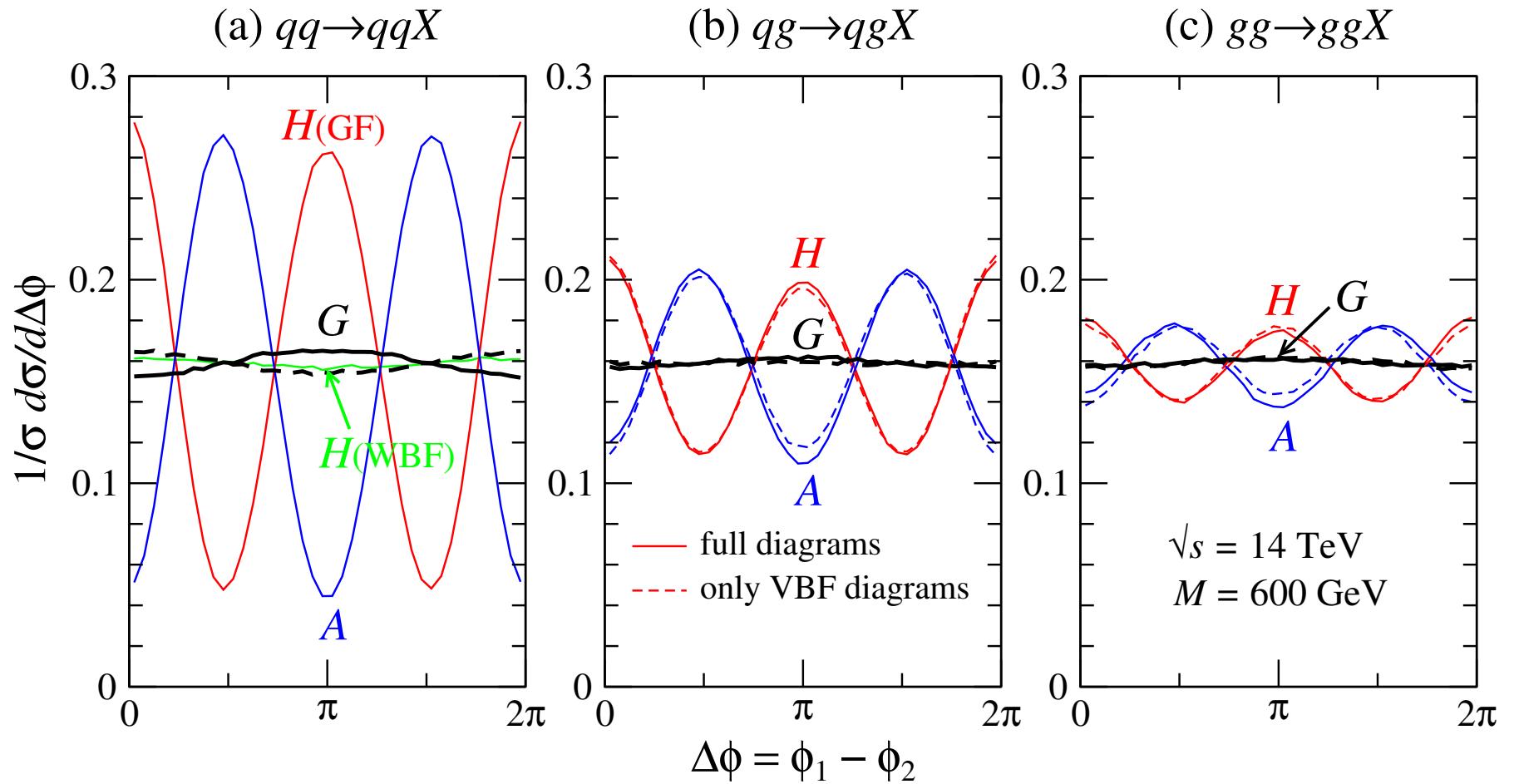
$$\sum_{\sigma_1, \dots, 4} |\mathcal{M}_{\sigma_1, \dots, 4; \sigma_{5,6}}|^2 = \Sigma_0 + \Sigma_1 \cos 2\Phi \quad (\Phi \equiv \phi_1 + \phi_2)$$

where

$$\begin{aligned} \Sigma_0 &\propto (d_{+2, \lambda'}^2(\Theta))^2 + (d_{-2, \lambda'}^2(\Theta))^2 = \begin{cases} \frac{1}{8}(1 + 6 \cos^2 \Theta + \cos^4 \Theta) & \text{for } \lambda' = \pm 2 \\ \frac{1}{2}(1 - \cos^4 \Theta) & \text{for } \lambda' = \pm 1 \\ \frac{3}{4} \sin^4 \Theta & \text{for } \lambda' = 0 \end{cases} \\ \Sigma_1 &\propto 2 d_{+2, \lambda'}^2(\Theta) d_{-2, \lambda'}^2(\Theta) = \begin{cases} +\frac{1}{8} \sin^4 \Theta & \text{for } \lambda' = \pm 2 \\ -\frac{1}{2} \sin^4 \Theta & \text{for } \lambda' = \pm 1 \\ +\frac{3}{4} \sin^4 \Theta & \text{for } \lambda' = 0 \end{cases} \end{aligned}$$

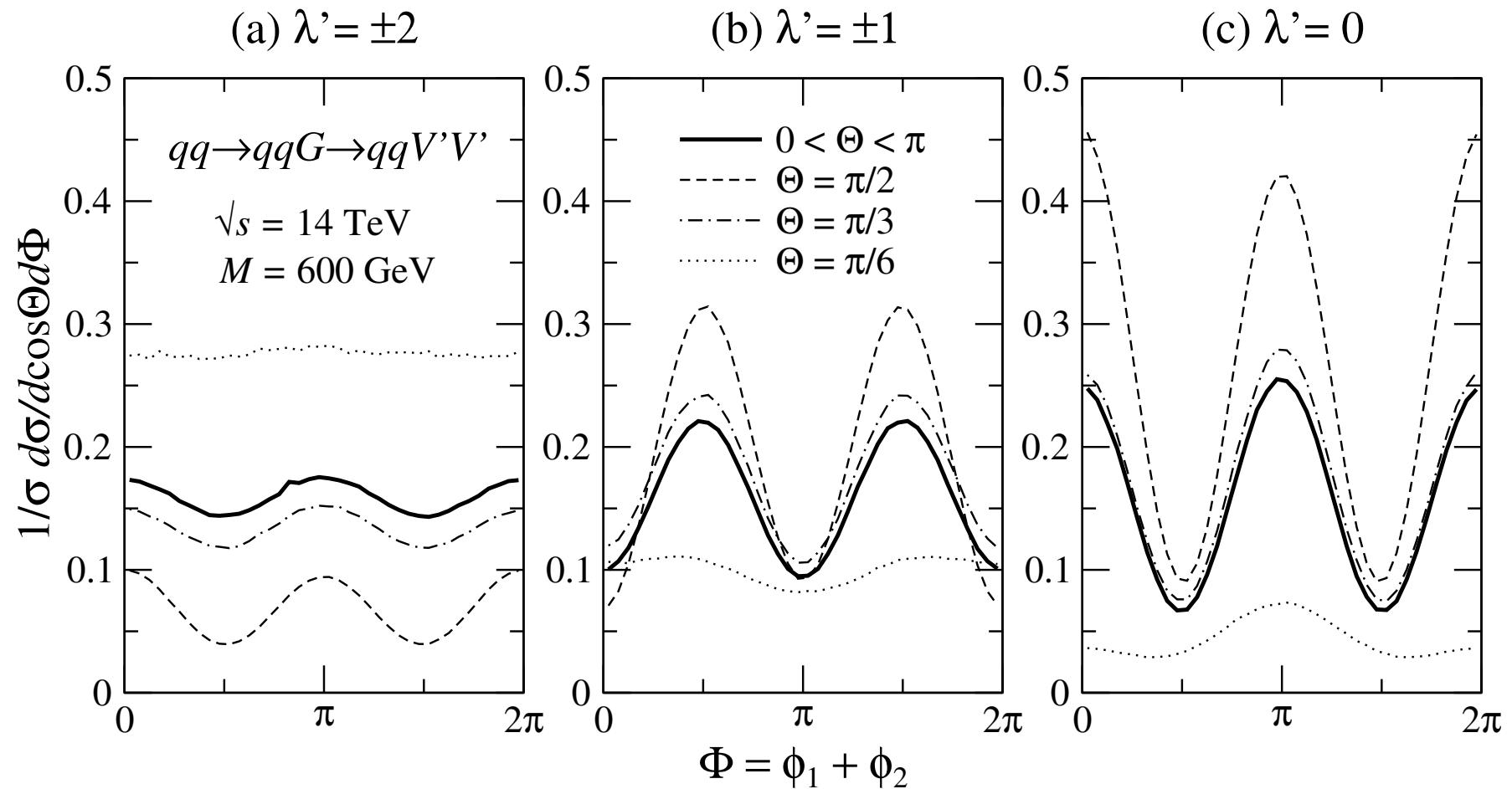
\implies The azimuthal Φ correlations depend on Θ and λ' .

($\phi_1 - \phi_2$) distributions for gravitons



"HELAS and MadGraph/MadEvent with spin-2 particles"
 K.Hagiwara, J.Kanzaki, Q.Li, KM, EPJC(2008)
 (The code is available at <http://madgraph.kek.jp/KEK/>.)

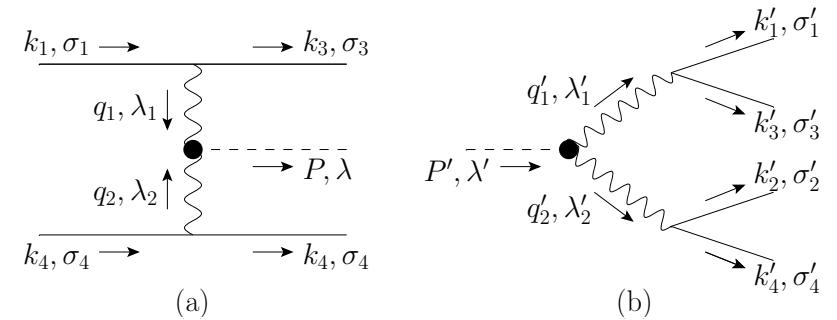
($\phi_1 + \phi_2$) distributions for gravitons



$$\sum_{\sigma_{1,\dots,4}} |\mathcal{M}_{\sigma_{1,\dots,4};\sigma_{5,6}}|^2 = \Sigma_0 + \Sigma_1 \cos 2\Phi; \quad \Sigma_1 \propto \begin{cases} +\frac{1}{8} \sin^4 \Theta & \text{for } \lambda' = \pm 2 \\ -\frac{1}{2} \sin^4 \Theta & \text{for } \lambda' = \pm 1 \\ +\frac{3}{4} \sin^4 \Theta & \text{for } \lambda' = 0 \end{cases}$$

The Θ and λ' dependent azimuthal Φ correlations !

Summary



- We have studied
 - heavy particle (*H/A* and *G*) productions in association with two jets via **VBF (=WBF+GF)** processes at the LHC.
 - (their decays into 4 leptons/jets via a vector-boson pair.)
- We showed
 - the **helicity amplitudes** explicitly for the VBF subprocesses.
 - the VBF amplitudes can reproduce the exact matrix elements by imposing the selection (**large rapidity separation**) cuts.
 - non-trivial azimuthal correlations of the jets are manifestly expressed as the quantum interference among different helicity states of the intermediate vector-bosons.
- These correlations reflect the spin and *CP* nature of the produced heavy particles.