

# Latest Results on Unpolarized and Helicity PDFs

## Chris Cocuzza (Temple U.) August 30, 2022













## **Current State of Unpolarized Global Analyses**



## **Current State of Unpolarized Global Analyses**













SeaQuest in Global Analyses
 LHC and NNPDF4.0
 Helicity Sea Asymmetry
 Gluon Helicity





## Spin-Averaged Sea Asymmetry (2021-2022)

Bayesian Monte Carlo extraction of sea asymmetry with SeaQuest and STAR data

Christopher Cocuzza, Wally Melnitchouk, Andreas Metz, Nobuo Sato

NNLO constraints on proton PDFs from the SeaQuest and STAR experiments and other developments in the CTEQ-TEA global analysis Marco Guzzi, T. J. Hobbs, Tie-Jiun Hou, Xiaoxian Jing, Keping Xie, Aurore Courtoy, Sayipjamal Dulat, Jun Gao, Joey Huston, Pavel M. Nadolsky, Carl Schmidt, Ibrahim Sitiwaldi, Mengshi Yan, C.-P. Yuan

CJ15 global PDF analysis with new electroweak data from the STAR and SeaQuest experiments

Sanghwa Park, Alberto Accardi, Xiaoxian Jing, J.F. Owens

https://arxiv.org/abs/2108.05786



https://arxiv.org/abs/2109.00677 C. Cocuzza *et al.*, Phys. Rev. D **104**, no. 7, 074031 (2021).

https://arxiv.org/abs/2108.06596

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M. Guzzi et al., SciPost Phys. Proc. 8, 005 (2022).

## Spin-Averaged Sea Asymmetry (2021-2022)



## Spin-Averaged Sea Asymmetry (2021-2022)



## Spin-Averaged Sea Asymmetry (2021-2022)



## Spin-Averaged Sea Asymmetry (2021-2022)



JAM and CJ find increase in central value at x > 0.2 6

JAM finds significant reduction in uncertainties

> CT finds small reduction in uncertainties



## Spin-Averaged Sea Asymmetry (2021-2022)





## Spin-Averaged Sea Asymmetry (2021-2022)



 $\rightarrow$  Jae Nam, "Recent STAR Results on the Unpolarized Light Quark Flavor Structure at RHIC", PDF: Tuesday 4:00 PM  $\rightarrow$  Eric Moffat, "Fragmentation Functions using JAM methodology", PDF: Saturday 3:30 PM

# SeaQuest in Global Analyses LHC and NNPDF4.0 Helicity Sea Asymmetry Gluon Helicity



## Latest LHC Results (2022)

#### The Path to Proton Structure at One-Percent Accuracy

Richard D. Ball, Stefano Carrazza, Juan Cruz-Martinez, Luigi Del Debbio, Stefano Forte, Tommaso Giani, Shayan Iranipour, Zahari Kassabov, Jose I. Latorre, Emanuele R. Nocera, Rosalyn L. Pearson, Juan Rojo, Roy Stegeman, Christopher Schwan, Maria Ubiali, Cameron Voisey, Michael Wilson

• di-jet production

Kinematic coverage Fixed-target DIS Collider DIS Fixed-target D gauge boson productio 10 gauge boson production+je Fop-guark pair production Single-inclusive iet production Di-iet production Single top-quark production 106 Black edge: new in NNPDF4.0 **NNPDF** 105 Q<sup>2</sup> (GeV<sup>2</sup>)  $10^{3}$ 10<sup>2</sup>  $10^{1}$ 

 $10^{-2}$ 

х

 $10^{-1}$ 

 $10^{0}$ 

 $10^{-3}$ 

 $10^{-4}$ 



https://arxiv.org/abs/2109.02653 R. D. Ball *et al.*, Eur. Phys. J. C. **82**, no. 5, 428 (2022).

## LHC Results (2021-2022)



## LHC Results (2021-2022)

3% suppression 0.01 < *x* < 0.1



## LHC Results (2021-2022)

3% suppression 0.01 < x < 0.1

Slight suppression



## LHC Results (2021-2022)



## LHC Results (2021-2022)









## LHC Results (2021-2022)

 New CTEQ global analysis of quantum chromodynamics with high-precision data from the LHC
 https://arxiv.org/abs/1912.10053

 Tie-Jiun Hou, Jun Gao, T. J. Hobbs, Keping Xie, Sayipjamal Dulat, Marco Guzzi, Joey Huston, Pavel Nadolsky, Jon Pumplin, Carl Schmidt, Ibrahim Sitiwaldi, Daniel Stump, C.-P. Yuan
 T.J. Hou et al., Phys. Rev. D 103, no. 1, 014013 (2021).

#### Parton distributions from LHC, HERA, Tevatron and fixed target data: MSHT20 PDFs

#### S. Bailey, T. Cridge, L. A. Harland-Lang, A. D. Martin, R.S. Thorne







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No SeaQuest, LHCb 13 TeV in CT18, MSHT20

#### https://arxiv.org/abs/2012.04684 S. Bailey *et al.*, Eur. Phys. J. C. **81**, no. 4, 341 (2021).



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## LHC Results (2021-2022)



### **Current State of Polarized Global Analyses** Data space



## Current State of Polarized Global Analyses Data space






# **Current State of Polarized Global Analyses**

Data space



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Data space



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# **Current State of Polarized Global Analyses**



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# **Current State of Polarized Global Analyses**



# SeaQuest in Global Analyses LHC and NNPDF4.0 Helicity Sea Asymmetry Gluon Helicity





# Helicity Sea Asymmetry (2009-2022)

**Extraction of Spin-Dependent Parton Densities and Their Uncertainties** 

Daniel de Florian, Rodolfo Sassot, Marco Stratmann, Werner Vogelsang

A first unbiased global determination of polarized PDFs and their uncertainties

Emanuele R.Nocera, Richard D.Ball, Stefano Forte, Giovanni Ridolfi, Juan Rojo (The NNPDF Collaboration)

Polarized Antimatter in the Proton from Global QCD Analysis

C. Cocuzza, W. Melnitchouk, A. Metz, N. Sato

<u>https://arxiv.org/abs/0904.3821</u> D. de Florian *et al.*, Phys. Rev. D **80**, 034030 (2009).

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**DSSV (2009):** polarized SIDIS data **NNPDFpol (2014):** priors from DSSV09 + STAR *W* asymmetry data (2012 run, 86 pb<sup>-1</sup>) **JAM (2022):** polarized SIDIS + STAR *W* asymmetry data (2013 run, 250 + 86 pb<sup>-1</sup>)

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$$A_L^{W^+}(y_W) \propto \frac{\Delta \bar{d}(x_1)u(x_2) - \Delta u(x_1)\bar{d}(x_2)}{\bar{d}(x_1)u(x_2) + u(x_1)\bar{d}(x_2)}$$
$$A_L^{W^-}(y_W) \propto \frac{\Delta \bar{u}(x_1)d(x_2) - \Delta d(x_1)\bar{u}(x_2)}{\bar{u}(x_1)d(x_2) + d(x_1)\bar{u}(x_2)}$$

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# SeaQuest in Global Analyses LHC and NNPDF4.0 Helicity Sea Asymmetry Gluon Polarization





# **Gluon Polarization (2014-2022)**

A first unbiased global determination of polarized PDFs and their uncertainties

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Monte Carlo sampling variant of the DSSV14 set of helicity parton densities

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How well do we know the gluon polarization in the proton?

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NNPDFpol (2014): used single-jet data from RHIC (up to 2009 runs) DSSV (2019): used single and di-jet data from RHIC (up to 2009 runs) JAM (2022): used single-jet data from RHIC (up to 2015 runs) and examined impact of positivity constraints

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# **Gluon Polarization** (2014-2022)







# **Gluon Polarization** (2014-2022)



### $\left|\Delta f(x,Q^2)\right| < f(x,Q^2)$

Can  $\overline{MS}$  parton distributions be negative? Alessandro Candido, Stefano Forte and Felix Hekhorn

Positivity and renormalization of parton densities

John Collins, Ted C. Rogers, Nobuo Sato

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#### Positivity and renormalization of parton densities

John Collins, Ted C. Rogers, Nobuo Sato

 $\rightarrow$  Nobuo Sato, "Progress in the exploration of nucleon's spin structures", PDF: Wednesday 2:30 PM

#### Global Analyses Highlights

# Lattice in Global Analyses (2021-The future!)

Confronting lattice parton distributions with global QCD analysis

J. Bringewatt, N. Sato, W. Melnitchouk, Jian-Wei Qiu, F. Steffens, M. Constantinou

https://arxiv.org/abs/2010.00548 J. Bringewatt *et al.*, Phys. Rev. D **103**, no.1, 016003 (2021).



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Combining experiment and lattice in a global QCD analysis is feasible!

# **Summary and Outlook**





#### Summary and Outlook

# Summary

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NNLO constraints on proton PDFs from the SeaQuest and STAR experiments and other developments in the CTEQ-TEA global analysis

CJ15 global PDF analysis with new electroweak data from the STAR and SeaQuest experiments





#### Summary and Outlook

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# Summary

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### Summary and Outlook

## Summary

Extraction of Spin-Dependent Parton Densities and Their UncertaintiesA first unbiased global determination of polarized PDFs and their uncertaintiesPolarized Antimatter in the Proton from Global QCD Analysis





#### Summary and Outlook



### Summary



## Outlook

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Jefferson Lab 12 GeV will provide new information on helicity PDFs and nuclear effects at high *x* 

EIC will provide new information on helicity PDFs at low x

Continued input from lattice QCD





## Outlook

25

Jefferson Lab 12 GeV will provide new information on helicity PDFs and nuclear effects at high *x* 

EIC will provide new information on helicity PDFs at low x

Continued input from lattice QCD





 $\rightarrow$  Timothy Hobbs, "PDFs from EIC, lattice, and the LHC", HE: Tuesday 2:00 PM

#### Collaboration



### Collaboration

### Andreas Metz



### Wally Melnitchouk



#### Nobuo Sato



#### Thank you to Jacob Ethier, Yiyu Zhou, and Patrick Barry for helpful discussions





## Extra

## **JAM Collaboration**

- 3-dimensional structure of nucleons:
  - Parton distribution functions (PDFs)
  - Fragmentation functions (FFs)
  - Transverse momentum dependent distributions (TMDs)
  - Generalized parton distributions (GPDs)

Collinear factorization in perturbative QCD

Simultaneous determinations of PDFs, FFs, etc.

Monte Carlo methods for Bayesian inference







## A Global Analysis

# *Simultaneous* extractions of spin-averaged PDFs, helicity PDFs, and FFs







DIS	BCDMS, NMC, SLAC, HERA, JLab	3863
Drell-Yan	Fermilab E866, E906	205
W/Z Boson	CDF/D0, STAR, LHCb, CMS	153
Jets	CDF/D0, STAR	198



Spin-Averaged PDFs
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Helicity PDFs

DIS	BCDMS, NMC, SLAC, HERA, JLab	3863
Drell-Yan	Fermilab E866, E906	205
W/Z Boson	CDF/D0, STAR, LHCb, CMS	153
Jets	CDF/D0, STAR	198
Polarized DIS	COMPASS, EMC, HERMES, SLAC, SMC	365
Polarized W/Z Boson	STAR, PHENIX	18
Polarized Jets	STAR, PHENIX	83







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Polarized W/Z Boson	STAR, PHENIX	18
Polarized Jets	STAR, PHENIX	83
SIDIS	COMPASS, EMC, HERMES, SLAC, SMC	1490
Polarized SIDIS	COMPASS, HERMES, SMC	231
SIA	ARGUS, BABAR, BELLE, TASSO, TPC, TOPAZ, SLD, ALEPH, OPAL, DELPHI	564



 $10^{-}$ 

 $10^{-2}$ 



0.7 2

0.3

0.5

0.2

0.4

0.6

0.7  $\boldsymbol{x}$ 

 $10^{-2}$ 

0.5

 $z_h$ 

0.8



## **Parameters to Observables**

Parameterize PDFs at input scale  $Q_0^2 = m_c^2$ 

$$f_i(x) = N x^{\alpha} (1-x)^{\beta} (1+\gamma \sqrt{x}+\eta x)$$

### **Parameters to Observables**

Parameterize PDFs at input scale  $Q_0^2 = m_c^2$ 

$$f_i(x) = N x^{\alpha} (1-x)^{\beta} (1+\gamma \sqrt{x}+\eta x)$$

Evolve PDFs using DGLAP  

$$\frac{d}{d \ln(\mu^2)} f_i(x,\mu) = \sum_j \int_x^1 \frac{dz}{z} P_{ij}(z,\mu) f_j(\frac{x}{z},\mu)$$



### **Parameters to Observables**

Parameterize PDFs at input scale  $Q_0^2 = m_c^2$ 

$$f_i(x) = N x^{\alpha} (1-x)^{\beta} (1+\gamma \sqrt{x}+\eta x)$$

$$\frac{\mathrm{d}}{\mathrm{d}\,\ln(\mu^2)}f_i(x,\mu) = \sum_j \int_x^1 \frac{\mathrm{d}z}{z} P_{ij}(z,\mu)f_j(\frac{x}{z},\mu)$$

### Calculate Observables

$$d\sigma_{\rm DY} = \sum_{i,j} H_{ij}^{\rm DY} \otimes f_i \otimes f_j$$





## The $\chi^2$ function

$$\chi^2(\boldsymbol{a}) = \sum_{i,e} \left( \frac{d_{i,e} - \sum_k r_e^k \beta_{i,e}^k - T_{i,e}(\boldsymbol{a})/N_e}{\alpha_{i,e}} \right)^2 + \sum_k \left( r_e^k \right)^2 + \left( \frac{1 - N_e}{\delta N_e} \right)^2$$



## The $\chi^2$ function





## The $\chi^2$ function





## The $\chi^2$ function





## The $\chi^2$ function





## The $\chi^2$ function





## **Bayes' Theorem**

Now that we have calculated  $\chi^2(a, data)...$ 

Likelihood Function

$$\mathcal{L}(\boldsymbol{a}, \text{data}) = \exp\left(-\frac{1}{2}\chi^2(\boldsymbol{a}, \text{data})\right)$$



## **Bayes' Theorem**

Now that we have calculated  $\chi^2(a, data)...$ 

Likelihood Function

$$\mathcal{L}(\boldsymbol{a}, \text{data}) = \exp\left(-\frac{1}{2}\chi^{2}(\boldsymbol{a}, \text{data})\right)$$

$$\begin{array}{c} \text{Posterior Beliefs} \\ \mathcal{P}(\boldsymbol{a}|\text{data}) \\ \mathcal{P}(\boldsymbol{a}|\text{data}) \\ \sim \mathcal{L}(\boldsymbol{a}, \text{data}) \pi(\boldsymbol{a}) \end{array}$$

$$\begin{array}{c} \text{Posterior Beliefs} \\ \mathcal{P}(\boldsymbol{a}|\text{data}) \\ \mathcal{P}(\boldsymbol{a}|\text{data}) \\ \text{Prior Beliefs} \end{array}$$



 $\left| \tilde{\sigma} = \sigma + N(0,1) \alpha \right|$ 





























Cannot be explained from gluons splitting into quark-antiquark pairs











## **Kinematic Coverage (Spin-Averaged)**

<b>Deep Inelastic Scattering</b>	BCDMS, NMC, SLAC, HERA, Jefferson Lab	3863	points
Drell-Yan	Fermilab E866, E906	205	points
W/Z Boson Production	CDF/D0, STAR, LHCb, CMS	153	points
Jets	CDF/D0, STAR	200	points
• SeaQuest * CMS/LHCb W • STAR W * CDF/D0 jets			





## **Kinematic Coverage (Spin-Averaged)**



## 36 1

## **Kinematic Coverage (Spin-Averaged)**



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## SeaQuest and NuSea Quality of Fit



$$\frac{\sigma_{pD}}{2\sigma_{pp}}\Big|_{x_1 \gg x_2} \approx \frac{1}{2} \Big[ 1 + \frac{\bar{d}(x_2)}{\bar{u}(x_2)} \Big]$$


### SeaQuest and NuSea Quality of Fit



process	$N_{\rm dat}$	$\chi^2/N_{\rm dat}$
Drell-Yan		
$\operatorname{NuSea}$ $pp$	184	1.21
${ m NuSea}  pD/2pp$	15	1.30
SeaQuest $pD/2pp$	6	0.82

 $\left. \frac{\sigma_{pD}}{2\sigma_{pp}} \right|_{x_1 \gg x_2} \approx \frac{1}{2} \left[ 1 + \frac{\bar{d}(x_2)}{\bar{u}(x_2)} \right]$ 

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### SeaQuest and NuSea Quality of Fit



process	$N_{ m dat}$	$\chi^2/N_{\rm dat}$
Drell-Yan		
$\operatorname{NuSea}$ $pp$	184	1.21
${ m NuSea}  pD/2pp$	15	1.30
SeaQuest $pD/2pp$	6	0.82

$$\frac{\sigma_{pD}}{2\sigma_{pp}}\Big|_{x_1 \gg x_2} \approx \frac{1}{2} \Big[ 1 + \frac{\bar{d}(x_2)}{\bar{u}(x_2)} \Big]$$

Well-known tension between NuSea and SeaQuest



### Impact from STAR and SeaQuest



**STAR:** Moderate reduction of uncertainties

SeaQuest: Large reduction of uncertainties, especially at x > 0.2.  $\overline{d}/\overline{u} > 1$  up to  $x \approx 0.4$ , in agreement with models

### **Comparison to other fits and pion cloud model**



### Comparison to other fits and pion cloud model





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Good agreement with pion cloud model



### **Kinematic Coverage (Helicity)**

<b>Deep Inelastic Scattering</b>	COMPASS, EMC, HERMES, SLAC, SMC	365	points
W/Z Boson Production	STAR, PHENIX	18	points
Jets	STAR, PHENIX	61	points





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### Small x Global Analysis (2021)

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First analysis of world polarized DIS data with small-x helicity evolution

Daniel Adamiak,<sup>1,\*</sup> Yuri V. Kovchegov,<sup>1,†</sup> W. Melnitchouk,<sup>2</sup> Daniel Pitonyak,<sup>3,‡</sup> Nobuo Sato,<sup>2,§</sup> and Matthew D. Sievert<sup>4,¶</sup>

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### Small x Global Analysis (2021)



#### Collaboration



### Collaboration

### Andreas Metz Wally Melnitchouk





Nobuo Sato



Hanjie Liu



#### Anthony Thomas



#### Thia Keppel



#### Thank you to Yiyu Zhou and Patrick Barry for helpful discussions



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### **Error Quantification**

For a quantity O(a): (for example, a PDF at a given value of  $(x, Q^2)$ )

 $\begin{vmatrix} E[O] = \int d^n a \ \rho(\boldsymbol{a} \mid data) \ O(\boldsymbol{a}) \\ V[O] = \int d^n a \ \rho(\boldsymbol{a} \mid data) \ \left[ O(\boldsymbol{a}) - E[O] \right]^2 \end{vmatrix}$ 

Exact, but  $n = \mathcal{O}(100)!$ 

# 43 **][**

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 $E[O] = \int d^{n}a \ \rho(a \mid data) \ O(a)$  $V[O] = \int d^{n}a \ \rho(a \mid data) \ \left[O(a) - E[O]\right]^{2}$ Build an MC ensemble

Exact, but  $n = \mathcal{O}(100)!$ 

### **Error Quantification**

For a quantity O(a): (for example, a PDF at a given value of  $(x, Q^2)$ )

 $E[O] = \begin{bmatrix} d^n a \ \rho(\boldsymbol{a} \mid data) \ O(\boldsymbol{a}) \end{bmatrix}$  $V[O] = \left[ d^n a \ \rho(\boldsymbol{a} \,|\, data) \ \left[ O(\boldsymbol{a}) - E[O] \right]^2 \right]$ Build an MC ensemble  $\left| E[O] \approx \frac{1}{N} \sum_{k} O(a_{k}) \right|$  $V[O] \approx \frac{1}{N} \sum_{k}^{k} \left[ O(a_{k}) - E[O] \right]^{2}$ Average over k sets of the parameters (replicas)

Exact, but  $n = \mathcal{O}(100)!$ 

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For a quantity O(a): (for example, a PDF at a given value of  $(x, Q^2)$ )

$$E[O] = \int d^{n}a \ \rho(a \mid data) \ O(a)$$
  

$$V[O] = \int d^{n}a \ \rho(a \mid data) \ \left[O(a) - E[O]\right]^{2}$$
  
Build an MC ensemble  

$$E[O] \approx \frac{1}{N} \sum_{k}^{k} O(a_{k})$$
  

$$V[O] \approx \frac{1}{N} \sum_{k}^{k} \left[O(a_{k}) - E[O]\right]^{2}$$
  
Average over k sets of the parameters (replicas)

0.4 JAM15  $(\mathbf{a})$ 0.30.20.10.0 -0.1 $- x\Delta u^+$ (**b**) 0.4 $x \Delta d^+$ 0.3 $x\Delta s^+$ 0.2 $- x \Delta g$ 0.10.0 -0.1 $10^{-3}$   $10^{-2}$  0.1 0.3 0.5 0.7





### **Multi-Step Strategy**

























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## **STAR Quality of Fit**



### **STAR Quality of Fit**



process	$N_{ m dat}$	$\chi^2/N_{ m dat}$
W-lepton		
STAR $W^+/W^-$	9	2.02



### **STAR Quality of Fit**



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### **STAR Quality of Fit**





#### Part 3: Helicity Sea Asymmetry



### **Quark and Antiquark Polarizations**



### EIC Impact on Helicity PDFs (2021)

Revisiting quark and gluon polarization in the proton at the EIC

Y. Zhou,<sup>1</sup> C. Cocuzza,<sup>2</sup> F. Delcarro,<sup>3</sup> W. Melnitchouk,<sup>3</sup> A. Metz,<sup>2</sup> and N. Sato<sup>3</sup>

https://arxiv.org/abs/2105.04434



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			CTT(a)	GTT(a)
scena	rio ex	trapolation	n $SU(2)$	SU(3)
1		low	$\checkmark$	
2		mid	$\checkmark$	
3		high	$\checkmark$	
4		low	$\checkmark$	$\checkmark$
5		mid	$\checkmark$	$\checkmark$
6		high	$\checkmark$	$\checkmark$

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scenario	extrapolation	SU(2)	SU(3)
1	low	$\checkmark$	
2	mid	$\checkmark$	
3	high	$\checkmark$	
4	low	$\checkmark$	$\checkmark$
5	mid	$\checkmark$	$\checkmark$
6	high	$\checkmark$	$\checkmark$

$$\Delta G_{\rm trunc}(Q^2) \equiv \int_{x_{\rm min}}^1 dx \,\Delta g(x, Q^2),$$
$$\Delta \Sigma_{\rm trunc}(Q^2) \equiv \int_{x_{\rm min}}^1 dx \,\sum_q \Delta q^+(x, Q^2)$$

### EIC Impact on Helicity PDFs (2021)



### **Impact of Parity Violating DIS (2021)**



### **Impact of Parity Violating DIS (2021)**

$$A_{UL} = \frac{G_F x Q^2}{2\sqrt{2}\pi\alpha} \left( \frac{g_A^e Y^- g_1^{\gamma Z} + g_V^e Y^+ g_5^{\gamma Z}}{xy^2 F_1 + (1-y)F_2} \right)$$

### **Impact of Parity Violating DIS (2021)**

$$\begin{aligned} g_1^{\gamma Z} &\approx \frac{1}{9} (\Delta u^+ + \Delta d^+ + \Delta s^+) \\ A_{UL} &= \frac{G_F x Q^2}{2\sqrt{2}\pi\alpha} \left( \frac{g_A^e Y (g_1^{\gamma Z} + g_V^e Y^+ g_5^{\gamma Z})}{xy^2 F_1 + (1-y) F_2} \right) \end{aligned}$$

### **Impact of Parity Violating DIS (2021)**


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### https://arxiv.org/abs/2102.06159





50

 $10^{-1}$ 



50

 $10^{-1}$ 

## **Current State of Helicity PDFs**

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Proton spin puzzle:

$$\left|\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g\right|$$

### **Current State of Helicity PDFs**

Proton spin puzzle:  
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# **Current State of Helicity PDFs**

 $dx \sum \Delta q^+$ 

 $dx\Delta g$ 

 $\Delta\Sigma =$ 

 $\Delta G =$ 

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 $dx \sum \Delta q^+$ 

 $dx\Delta g$ 

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Still a lot to learn about helicity PDFs at low x and the helicity sea quark PDFs!



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