

PEN Update: A Precision Measurement of $\pi \rightarrow e\nu(\gamma)$ Branching Ratio

Charles Glaser

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PEN Collaboration

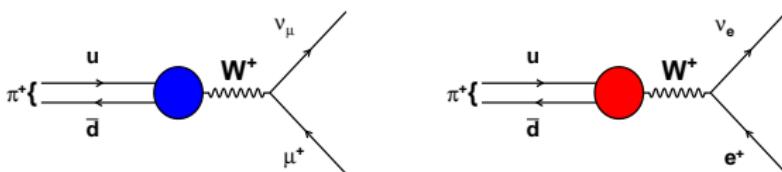


Overview

- Theory/Motivation
- PEN Detector
- Monte Carlo Simulations
- Radiative Decays
- Statistics and Systematics
- Summary

Theory/PEN

Explore the (V–A) interaction through a precision measurement



$$\frac{\Gamma(\pi^+ \rightarrow e^+ \nu_e (\gamma))}{\Gamma(\pi^+ \rightarrow \mu^+ \nu_\mu (\gamma) \rightarrow e^+ \nu_e \bar{\nu}_\mu)} = \left(\frac{g_e}{g_\mu} \right)^2 \left(\frac{m_e}{m_\mu} \right)^2 \frac{\left(1 - \left(\frac{m_e}{m_\mu} \right)^2 \right)^2}{\left(1 - \left(\frac{m_\mu}{m_\pi} \right)^2 \right)^2} (1 + \delta_R)$$

Theoretical BR: $(1.2352 \pm 0.0001) \times 10^{-4}$ *

Experimental BR: $(1.2327 \pm 0.0023) \times 10^{-4}$

δ_R rad/loop corrections in SM, non V–A extensions

$$\left(\frac{g_e}{g_\mu} \right)^2 = 1.0021 \pm 0.0016 \text{ (experimental)}$$

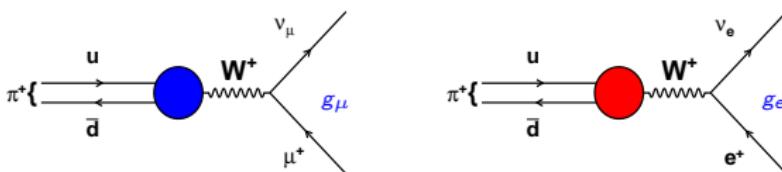
Goal: relative uncertainty 5×10^{-4} or better



*For Review see: D.Počanić et al J. Physics G 41 2014 11
PEN($\pi^+ \rightarrow e^+ \nu_e (\gamma)$)

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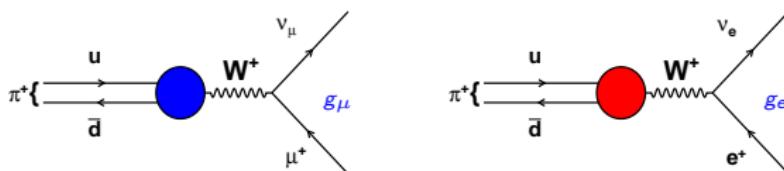
CIPANP

2022

3 / 27

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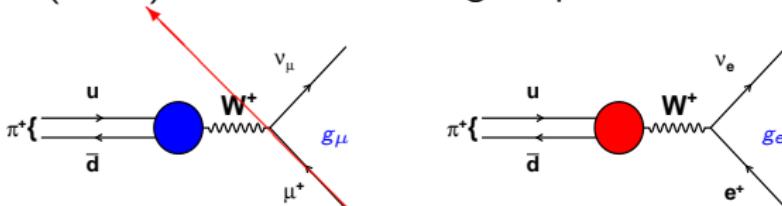
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$\sim 2.5 \times 10^{-5}$

Theoretical BR: $(1.2352 \pm 0.0001) \times 10^{-4}$ Pure PS ~5.4*

Experimental BR: $(1.2327 \pm 0.0023) \times 10^{-4}$

δ_R rad/loop corrections in SM, non V–A extensions

$$\left(\frac{g_e}{g_\mu} \right)^2 = 1.0021 \pm 0.0016 \text{ (experimental)}$$

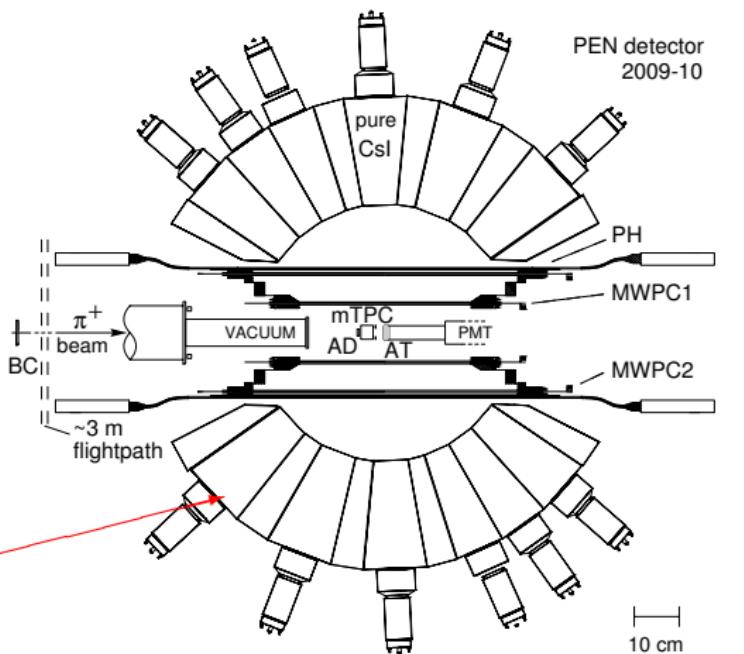
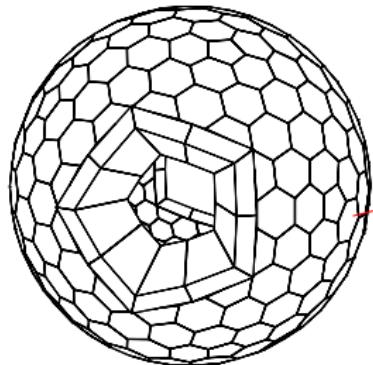
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 PEN($\pi^+ \rightarrow e^+ \nu_e (\gamma)$)

Detector Setup

- π^- beamline at PSI
- stopped π^+ beam
- active target counter
- 240 module spherical pure CsI calorimeter
- central tracking
- beam tracking
- digitized waveforms



BC: Beam Counter

AD: Active Degrader

AT: Active Target

PH: Plastic Hodoscope (20 stave cylindrical)

MWPC: Multi-Wire Proportional Chamber (cylindrical)

mTPC: mini-Time Projection Chamber

Experimental Branching Ratio (B)

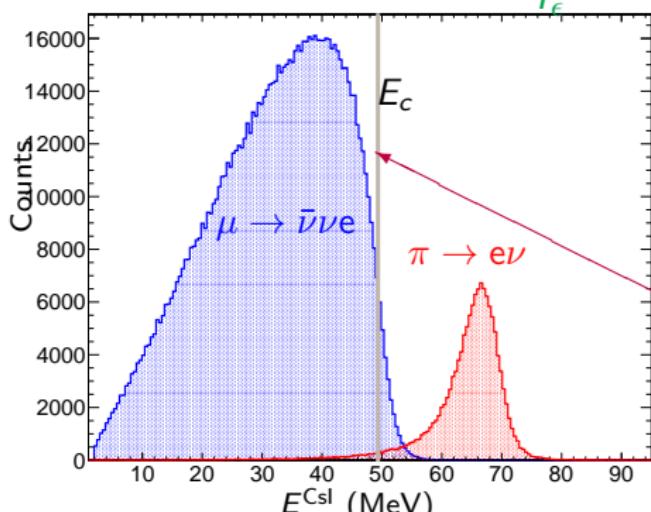
Naively, $B = \frac{N_{\pi \rightarrow e\nu} A_{\pi \rightarrow \mu \rightarrow e}}{N_{\pi \rightarrow \mu\nu} A_{\pi \rightarrow e\nu}}$ Too simplistic!

MWPC efficiency depends on energy

Timing gates affect number of observations

Monte Carlo

$$B = \frac{N_{\pi \rightarrow e\nu}^{\text{peak}} (1 + \epsilon_{\text{tail}})}{N_{\pi \rightarrow \mu\nu}} \frac{\epsilon(E_{\mu \rightarrow e\nu\bar{\nu}})_{\text{MWPC}}}{\epsilon(E_{\pi \rightarrow e\nu})_{\text{MWPC}}} \frac{f_{\pi \rightarrow \mu \rightarrow e}(T_e)}{f_{\pi \rightarrow e\nu}(T_e)} \frac{A_{\pi \rightarrow \mu \rightarrow e}}{A_{\pi \rightarrow e\nu} r_A}$$



E_c = cutoff energy

N = number of events

A = acceptance

$\epsilon_{\text{tail}}(E_c)$ = tail to peak ratio

$\epsilon(E)_{\text{MWPC}}$ = efficiency of MWPC

$f(T_e)$ = probability from time

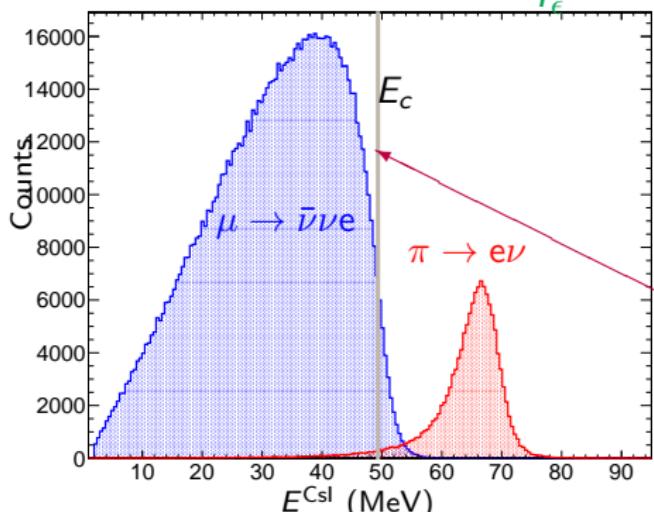
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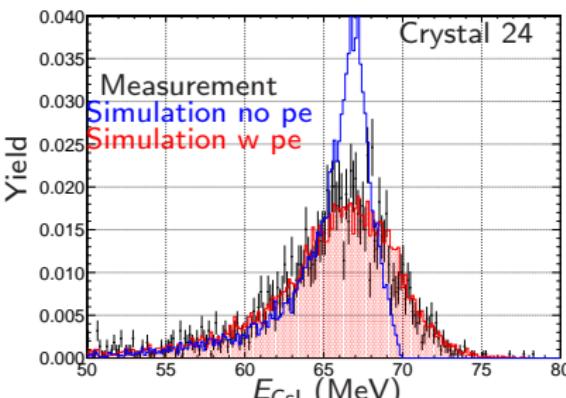
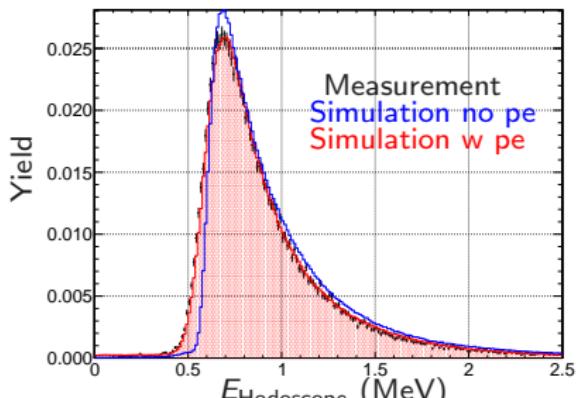
Creating realistic simulations

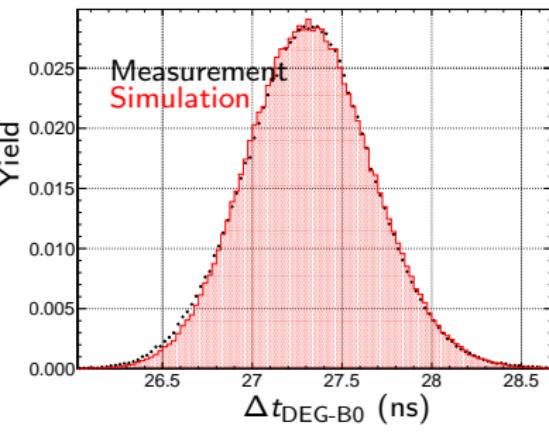
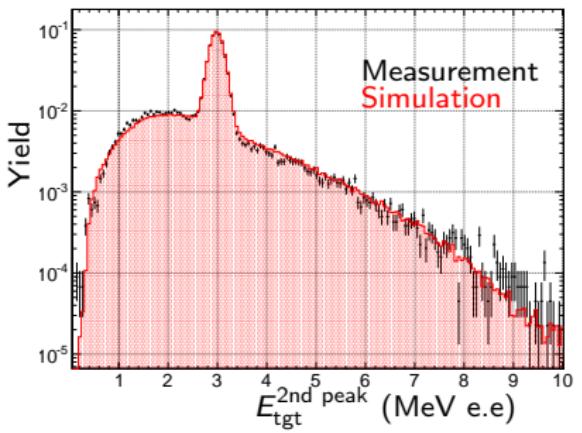
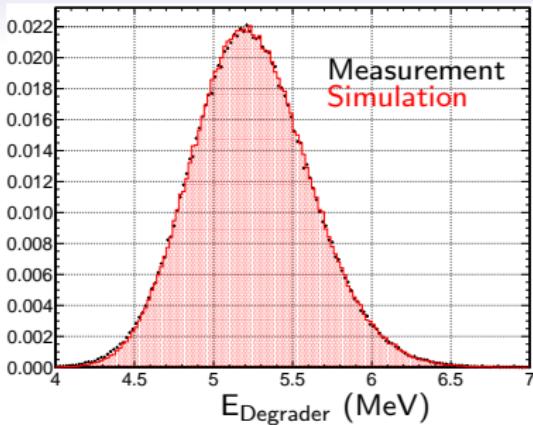
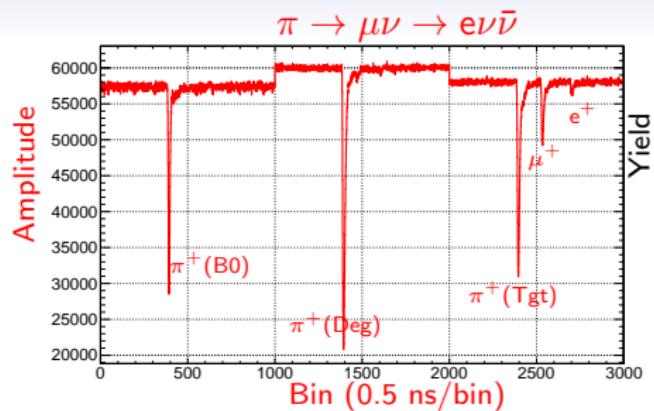
Geant gives energies, timings, and positions

Requires additional physics input to simulate full detector response

In the Experiment:

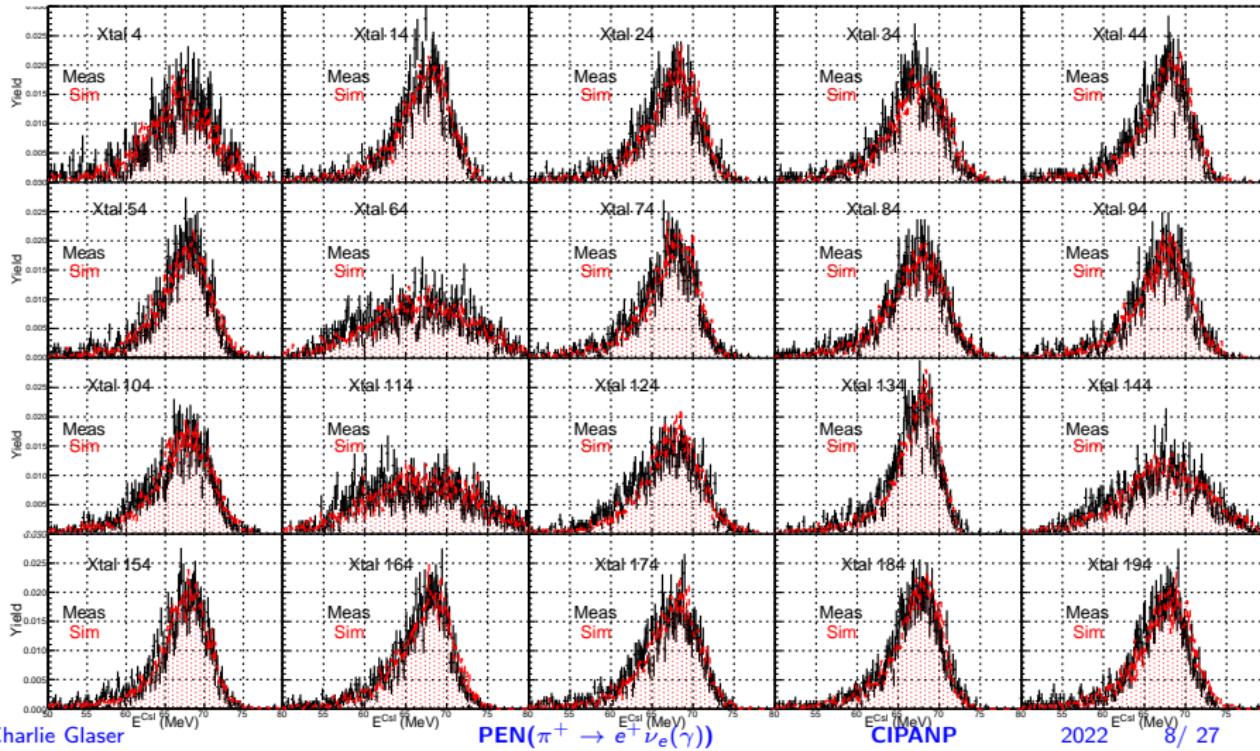
- digitized energies and timings of detector elements
- mTPC, beam counters, and target waveforms
- photoelectron (pe) statistics smear signal





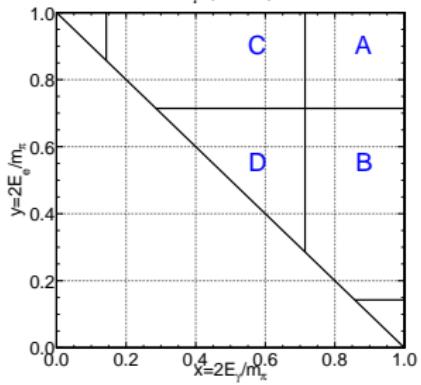
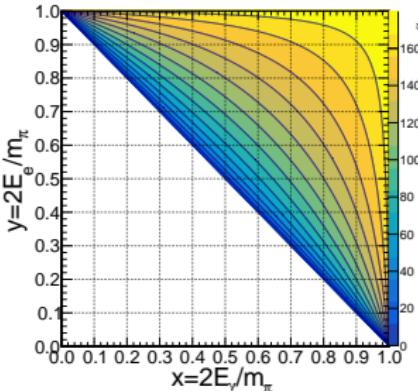
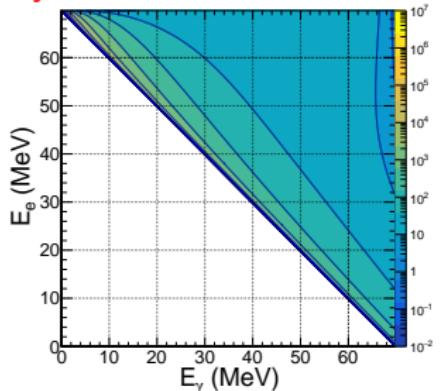
CsI challenges - unique xtals

- Light collection non-uniformities, $\Delta\Omega$ Coverage
- 240 PMTs = 240 different quantum efficiencies



Regions of $\pi \rightarrow e\nu\gamma$

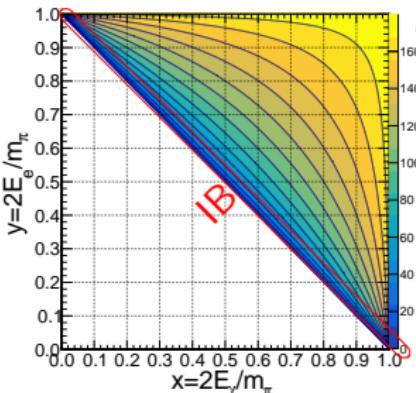
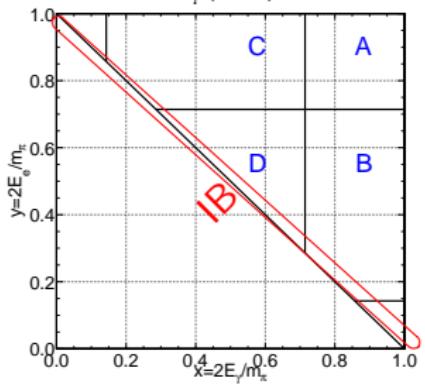
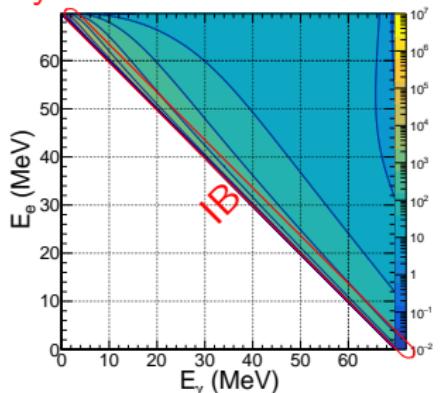
All decays are radiative



Phase space broken into regions

Regions of $\pi \rightarrow e\nu\gamma$

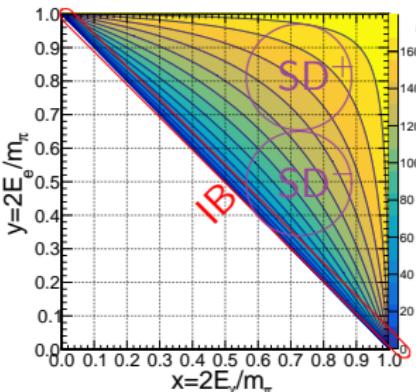
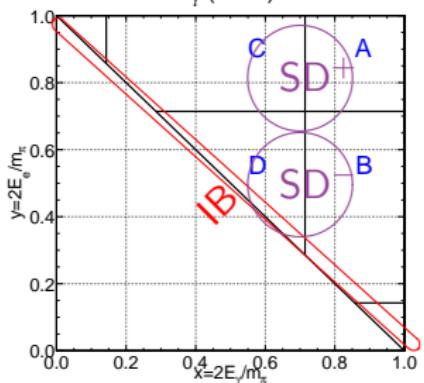
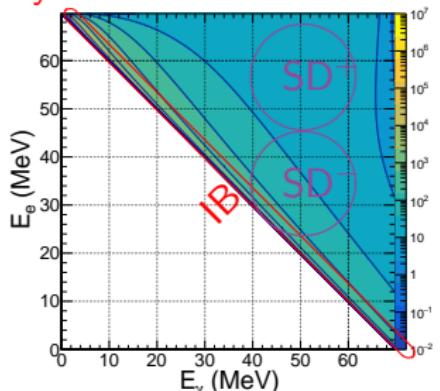
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Inner Bremsstrahlung dominated

Regions of $\pi \rightarrow e\nu\gamma$

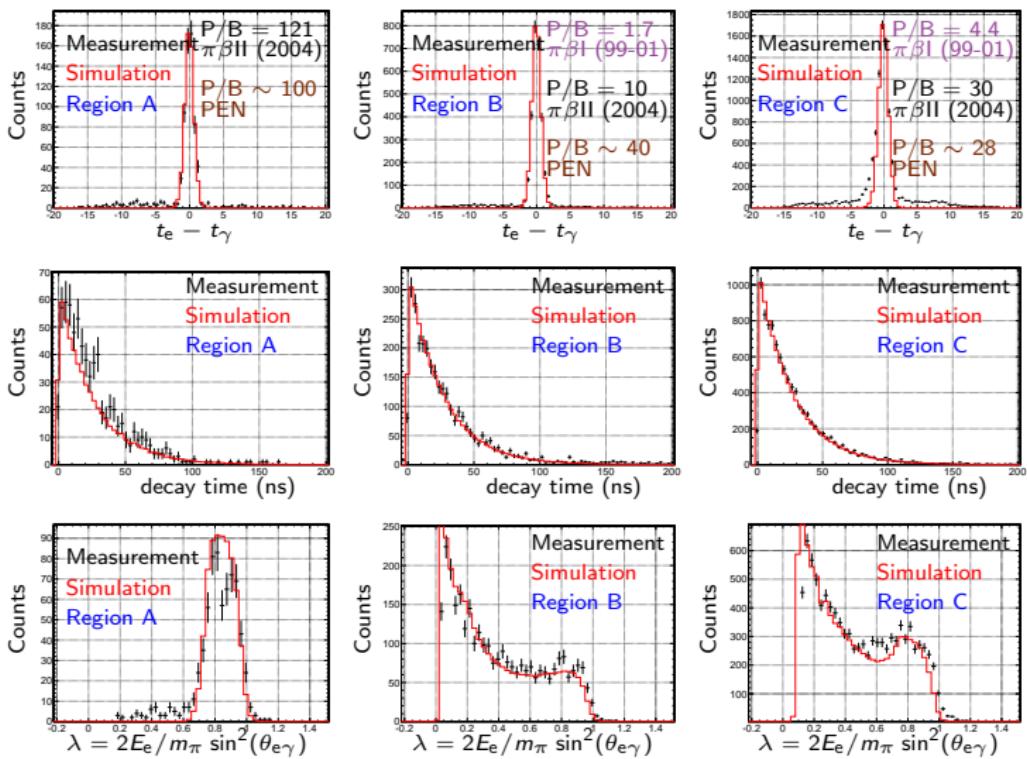
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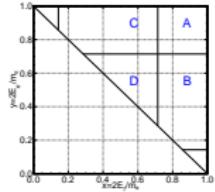
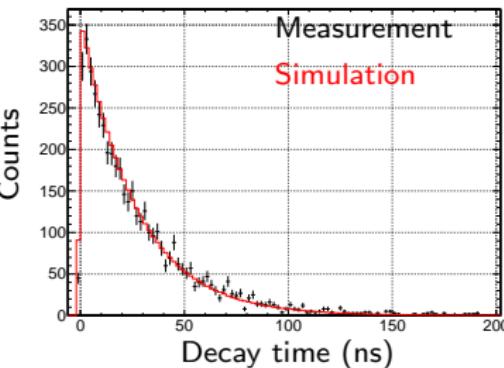
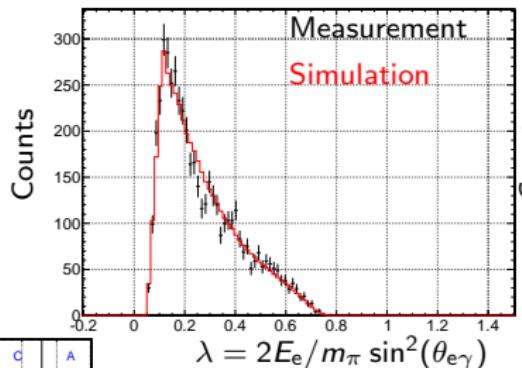
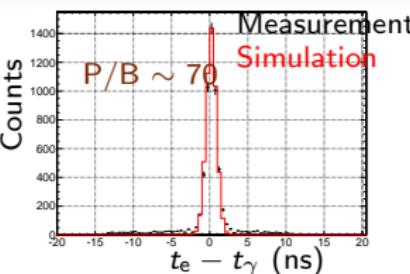
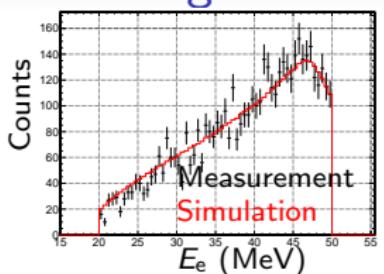
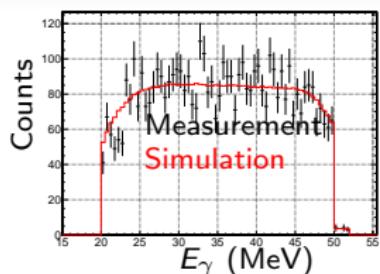
Inner Bremsstrahlung dominated

Structure Dependent
 $SD^+ \sim (F_V + F_A)^2$
 $SD^- \sim (F_V - F_A)^2$

Radiative Decays $\pi \rightarrow e\nu\gamma$

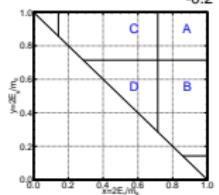
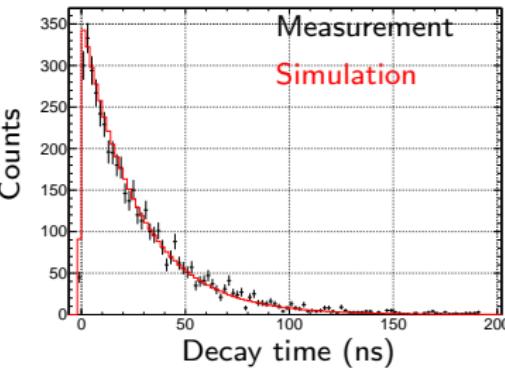
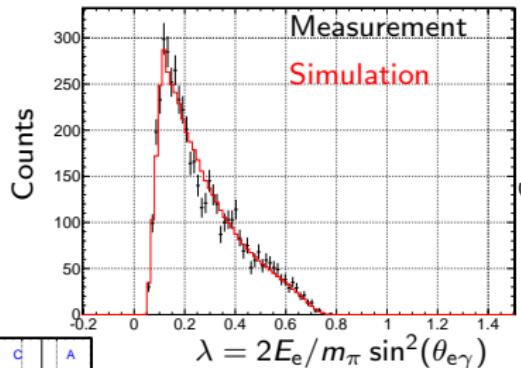
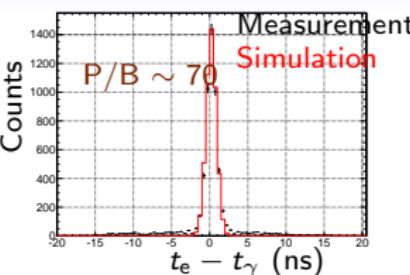
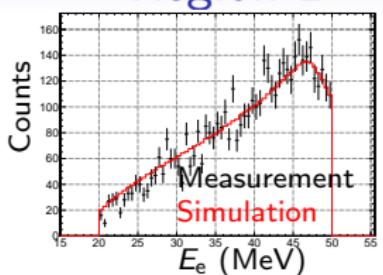
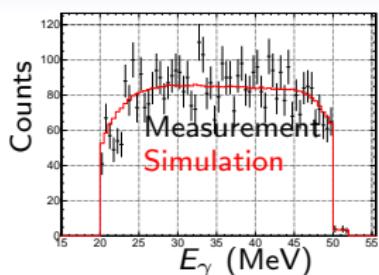


Region D



PEN: First experiment to examine Region D in detail

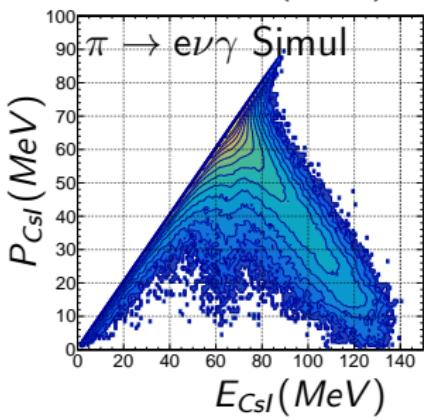
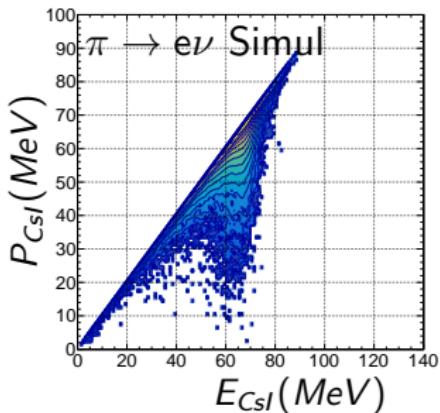
Region D



A chance to evaluate $SD^- (F_V, F_A)$ independently

Invariant mass-inclusion of radiative decays

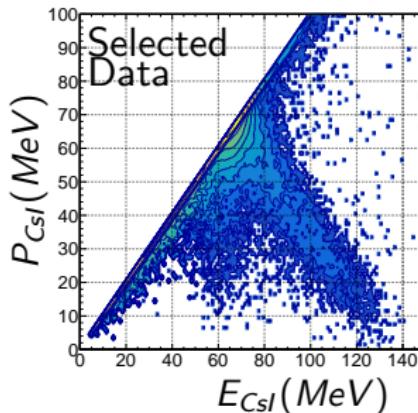
PEN indirectly measure p_ν



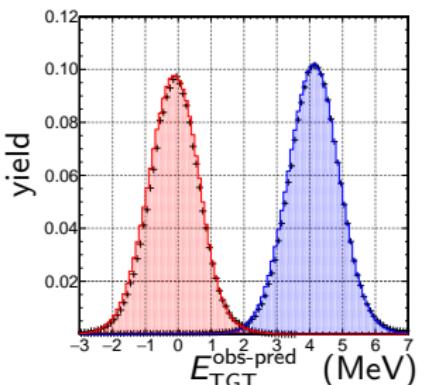
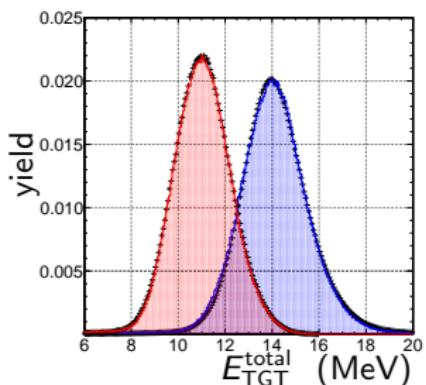
$$\vec{p}_e + \vec{p}_\gamma = -\vec{p}_\nu$$

$$\underbrace{E_\gamma + E_e}_{E_{\text{obs}}} + \underbrace{E_\nu}_{p_\nu c} = m_\pi c^2$$

$$E_{\text{obs}} + p_\nu c = m_\pi c^2$$

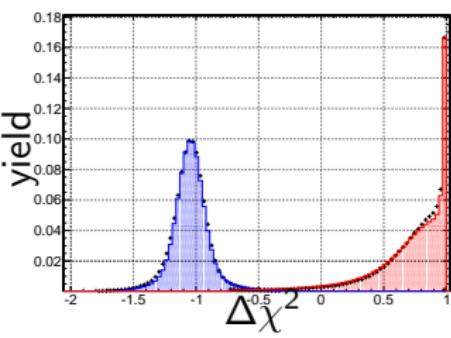
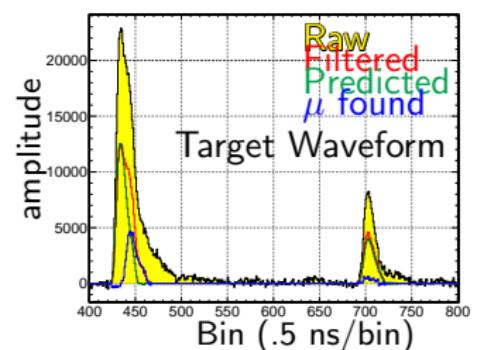


Waveform selections



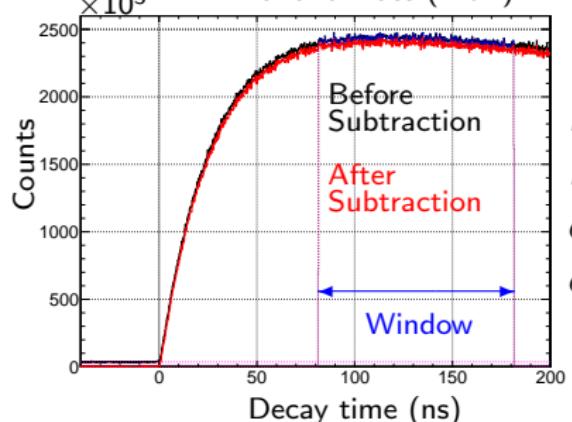
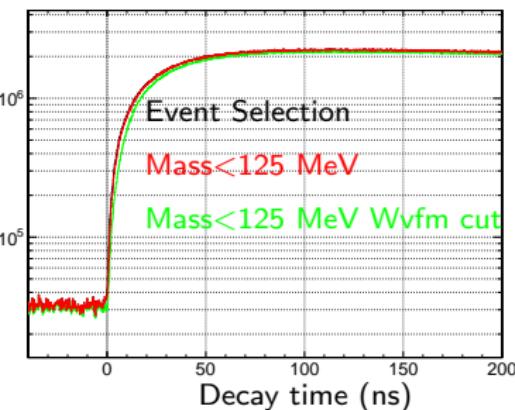
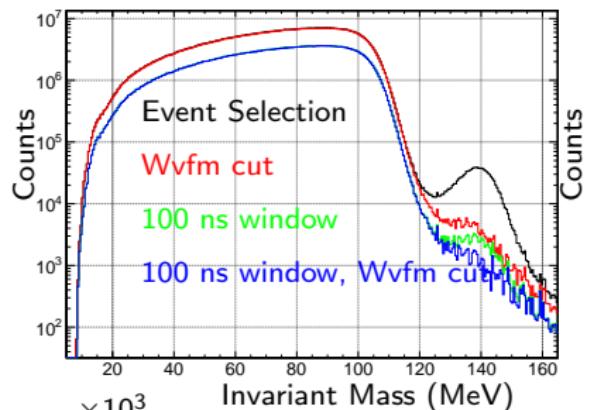
Measurement
 $\pi \rightarrow \mu\nu(\gamma)$ Simul
 $\pi \rightarrow e\nu(\gamma)$ Simul

Predicted energies
and
predicted timings
lead to
predicted waveforms



Get χ_2^2
Get χ_3^2
 $\Delta\chi^2 = \frac{\chi_2^2 - \chi_3^2}{\text{constant}}$

Number of $\pi \rightarrow \mu \rightarrow e$ events



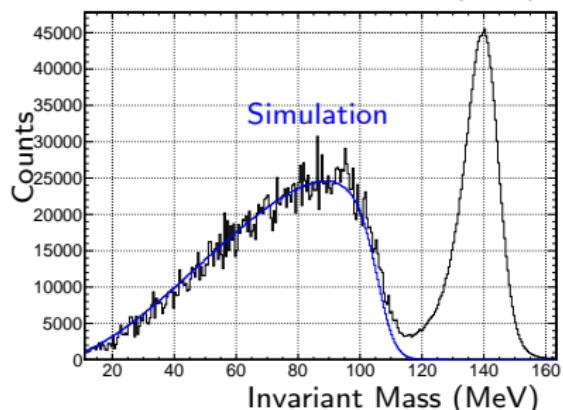
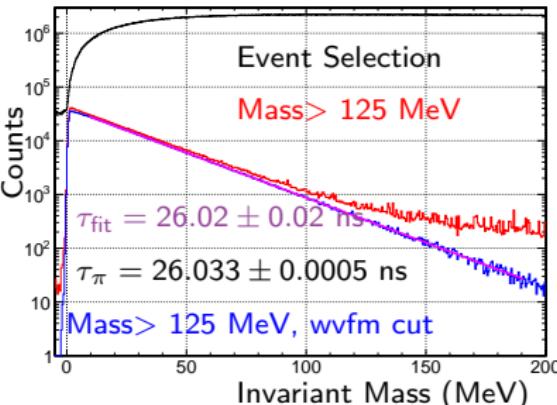
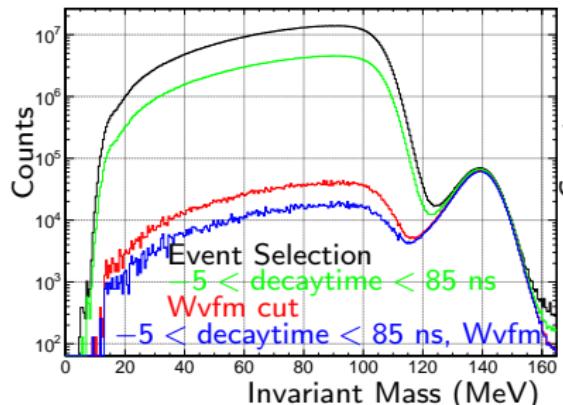
$$N_{\text{michel, run 2}} = (5225.68 \pm 0.23) \times 10^5$$

$$N_{\text{michel, run 3}} = (9545.50 \pm 0.33) \times 10^5$$

$$\delta N_{\text{michel, run 2}} / N_{\text{michel, run 2}} = 4.4 \times 10^{-5}$$

$$\delta N_{\text{michel, run 3}} / N_{\text{michel, run 3}} = 3.5 \times 10^{-5}$$

Number of $\pi \rightarrow e\nu(\gamma)$



Wvfm cut is needed.

$$N_{\pi \rightarrow e\nu(\gamma), \text{run 2}} = (1409.33 \pm 1.18) \times 10^3$$

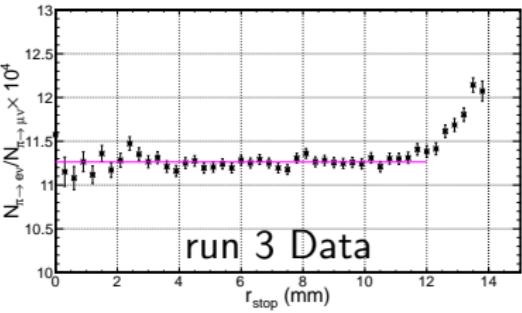
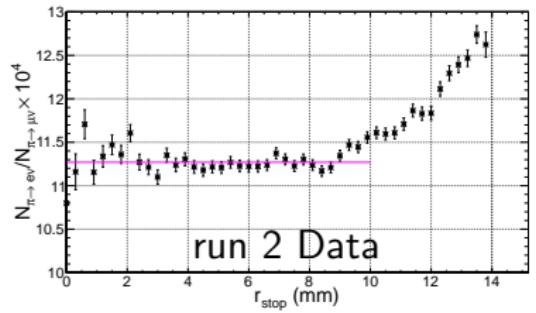
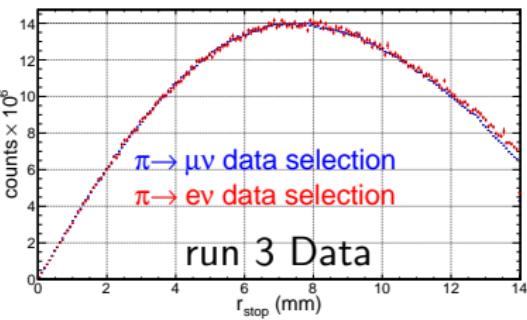
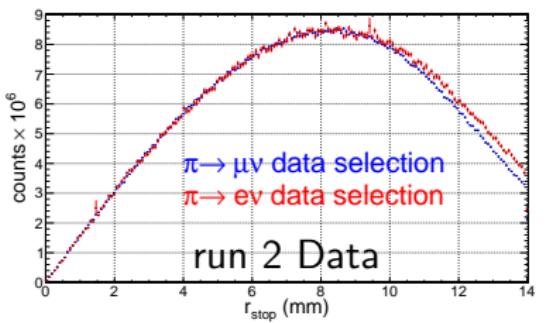
$$N_{\pi \rightarrow e\nu(\gamma), \text{run 3}} = (2413.81 \pm 1.63) \times 10^3$$

$$\delta N_{\pi \rightarrow e\nu(\gamma)} / N_{\pi \rightarrow e\nu(\gamma), \text{run 2}} = 8.50 \times 10^{-4}$$

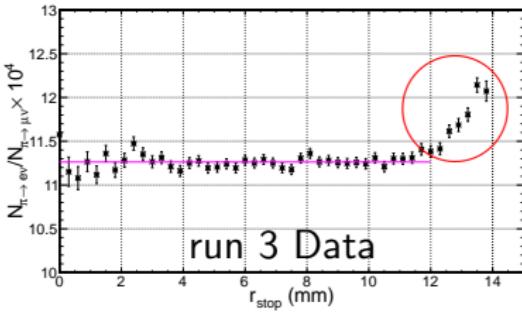
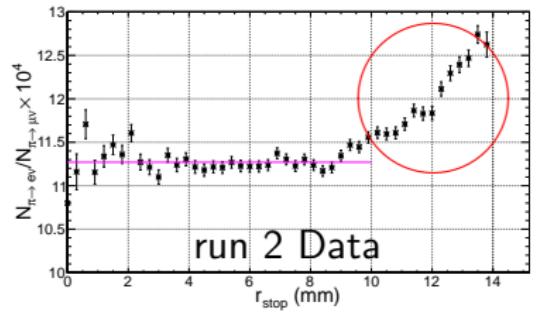
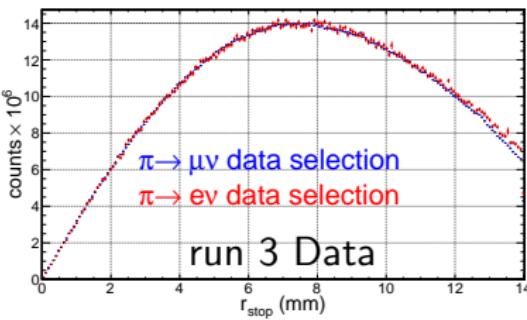
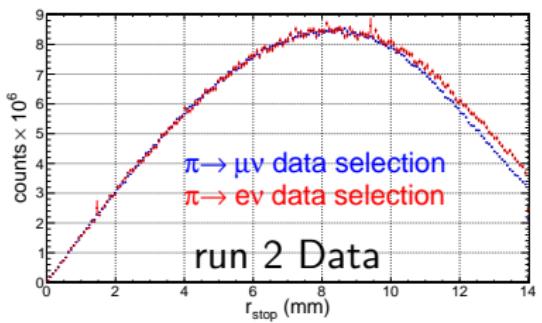
$$\delta N_{\pi \rightarrow e\nu(\gamma)} / N_{\pi \rightarrow e\nu(\gamma), \text{run 3}} = 6.49 \times 10^{-4}$$

$$\delta N_{\pi \rightarrow e\nu(\gamma)} / N_{\pi \rightarrow e\nu(\gamma)} = 5.26 \times 10^{-4}$$

Target energy requirements



Target energy requirements



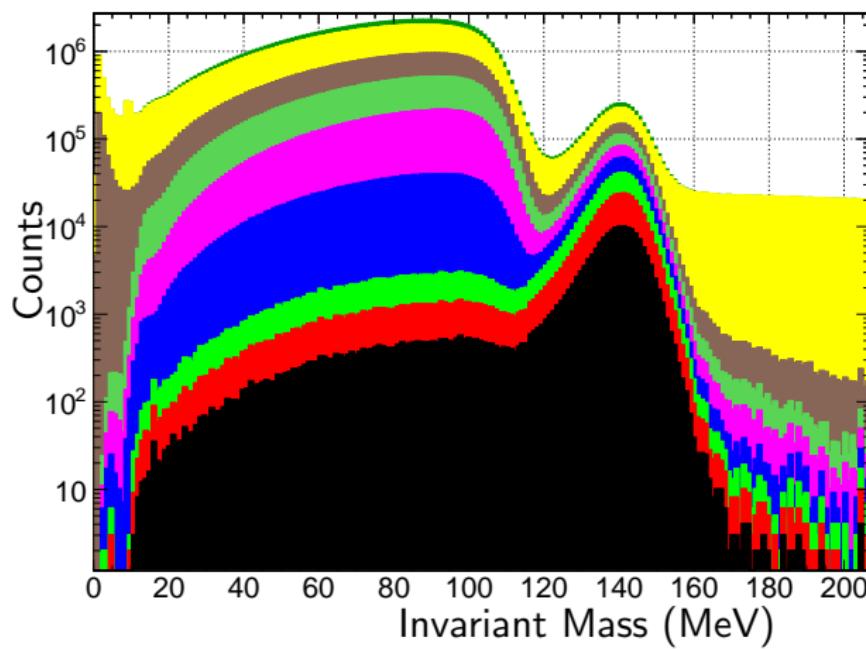
run 3 data $\sim 50\%$

$$\delta N/N \sim 4.13 \times 10^{-4}$$

run 3 data $\sim 25\%$



Tail trigger - studying the tail



Trigger events

Good π stop

Track Constructed

Good Track

$E_{\text{tgt}} < 12 \text{ MeV}$

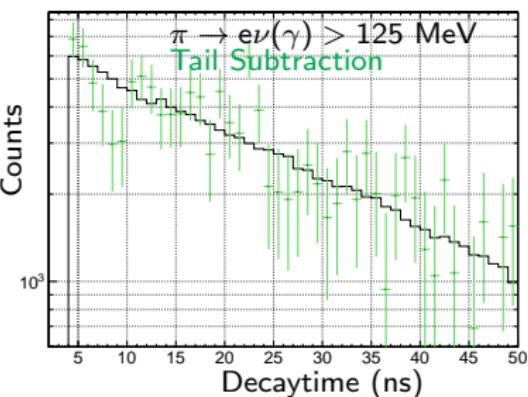
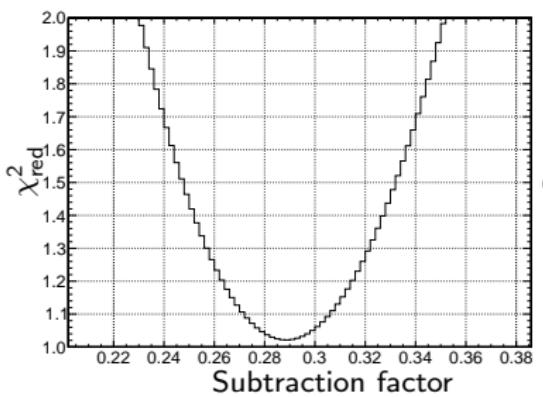
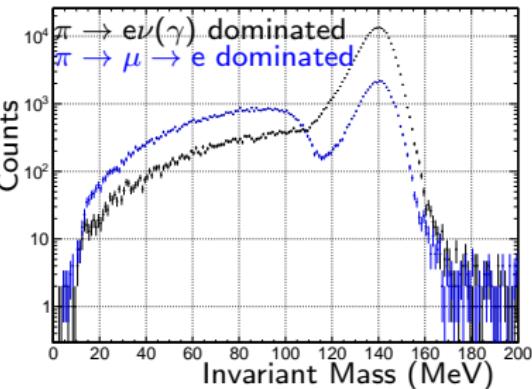
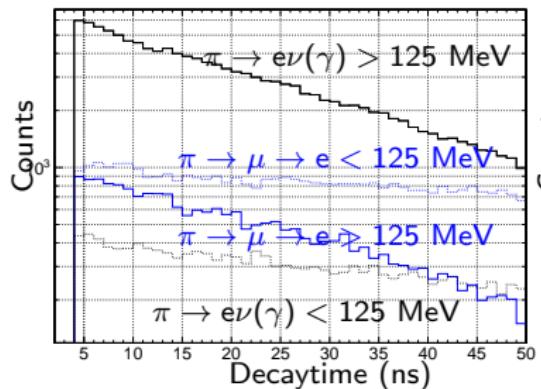
$E_{\text{tgt}}^{\text{pred-obs}} < 1$

$\Delta\chi^2 > .55$

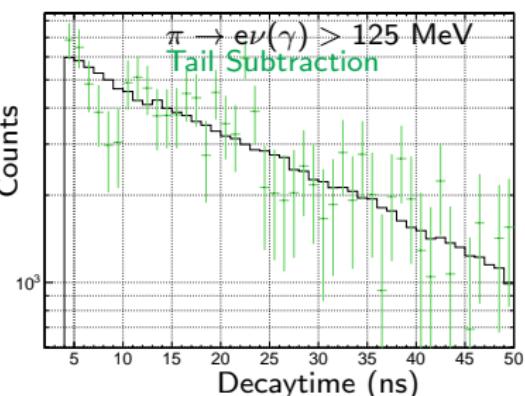
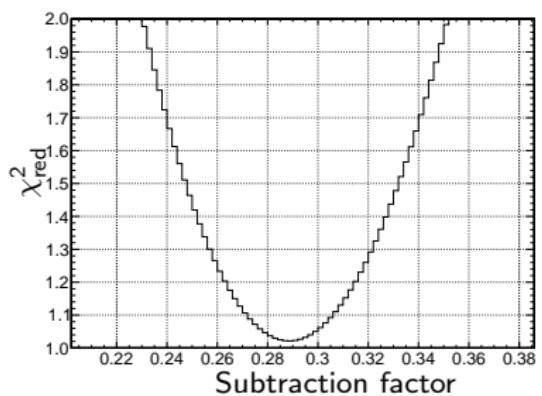
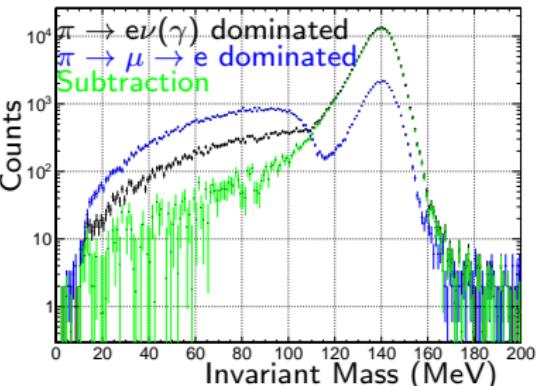
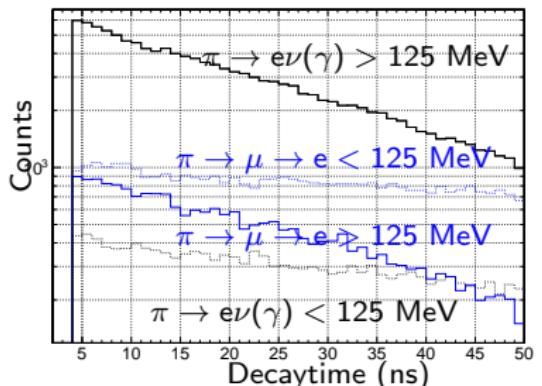
Good Vertex

Tgt dEdx

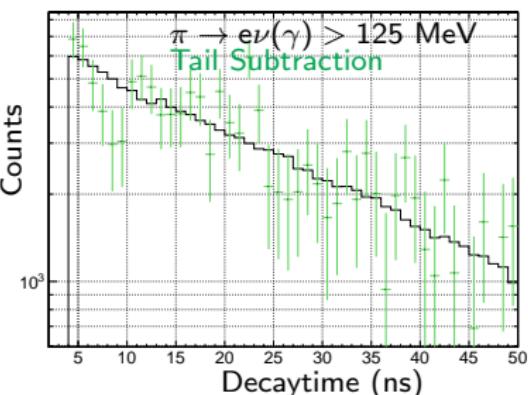
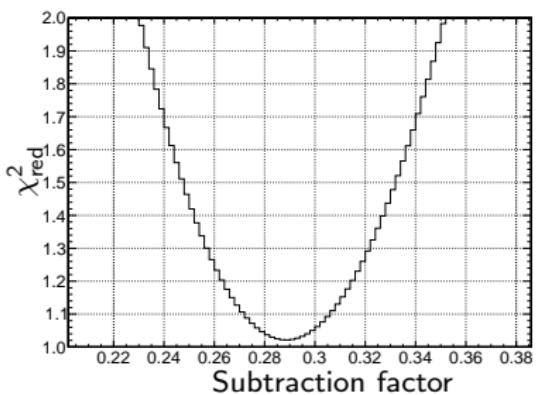
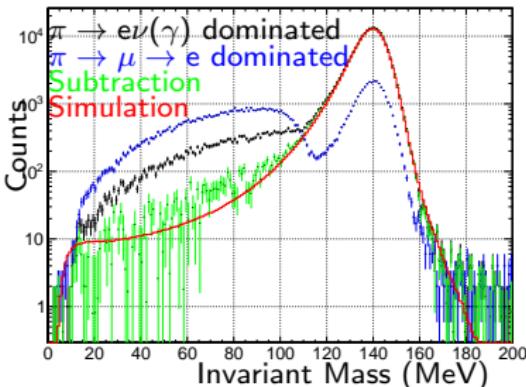
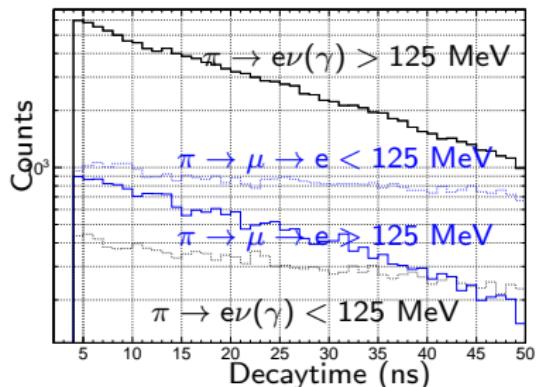
$\pi \rightarrow \mu \rightarrow e$ subtraction from tail



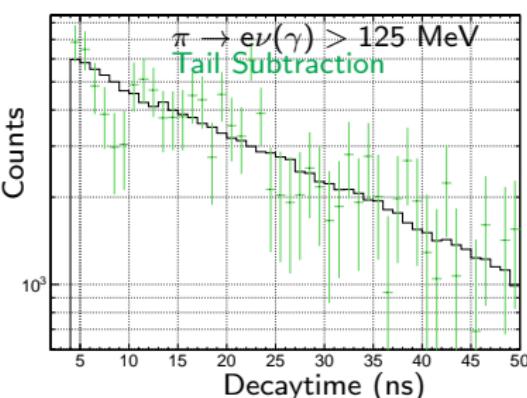
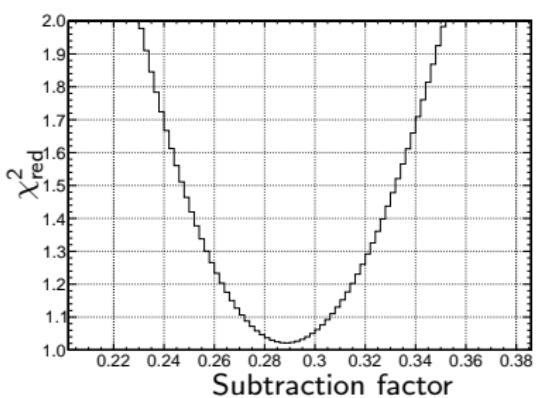
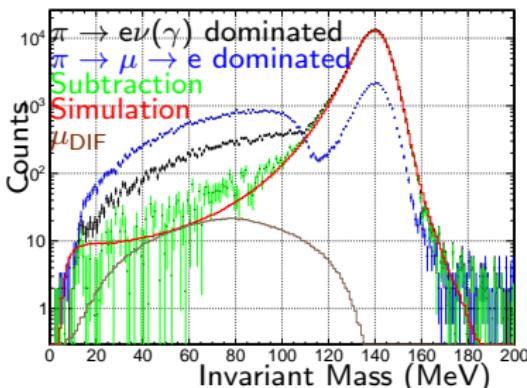
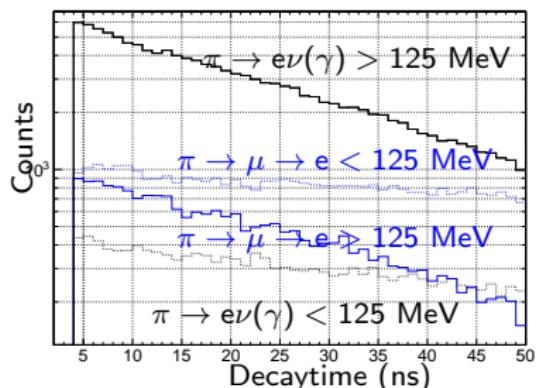
$\pi \rightarrow \mu \rightarrow e$ subtraction from tail



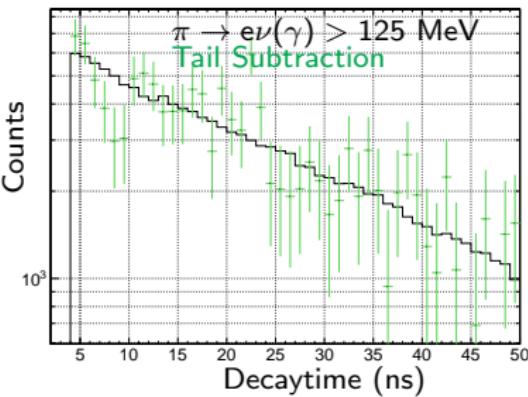
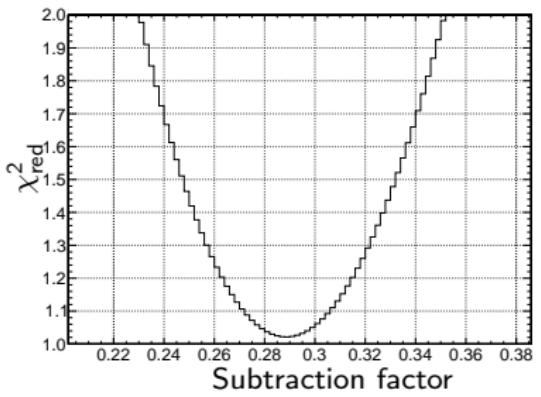
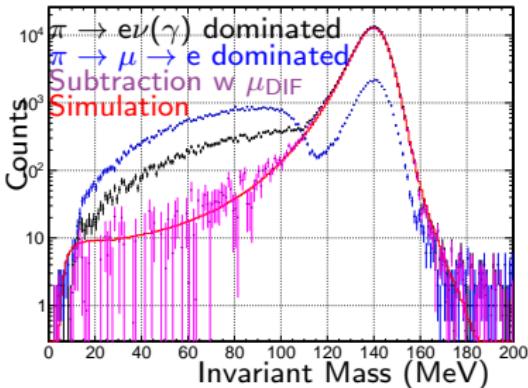
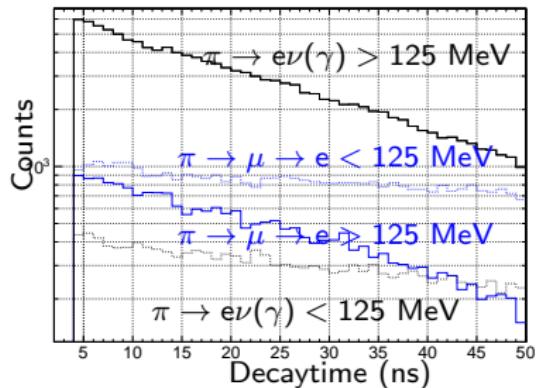
$\pi \rightarrow \mu \rightarrow e$ subtraction from tail



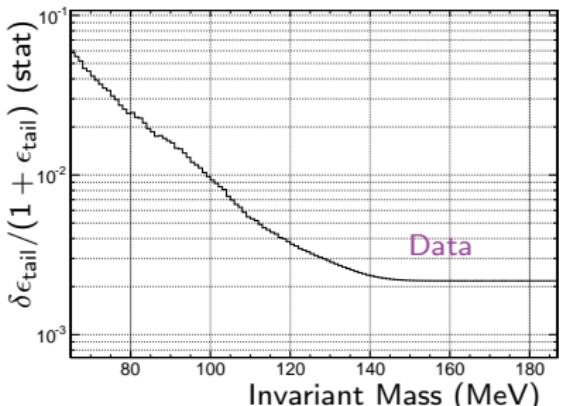
$\pi \rightarrow \mu \rightarrow e$ subtraction from tail



$\pi \rightarrow \mu \rightarrow e$ subtraction from tail



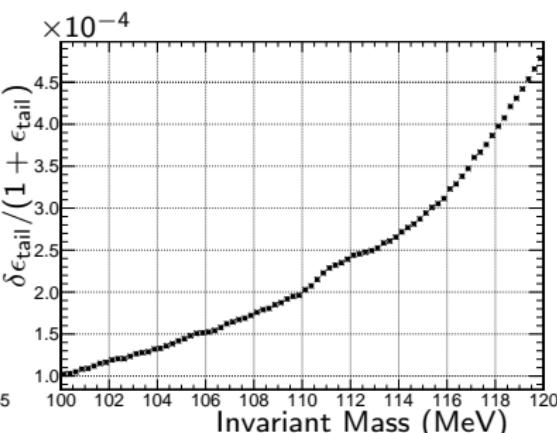
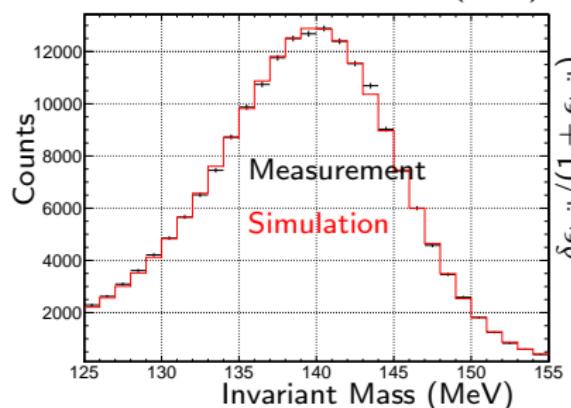
$$\delta\epsilon_{\text{tail}}/(1 + \epsilon_{\text{tail}})$$



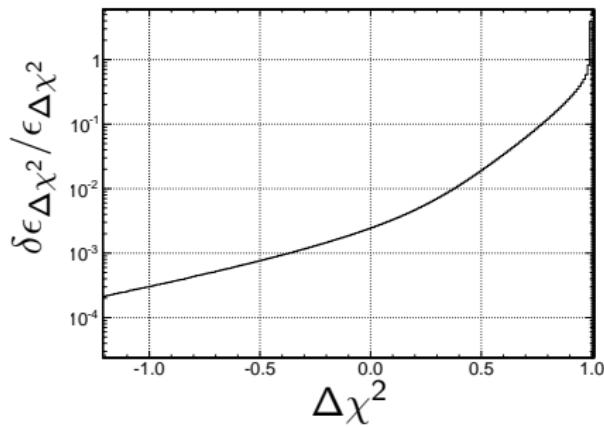
Statistical uncertainty too high
Relay on precise simulation

Systematics from :

- Peak positions
- Photo-nuclear physics

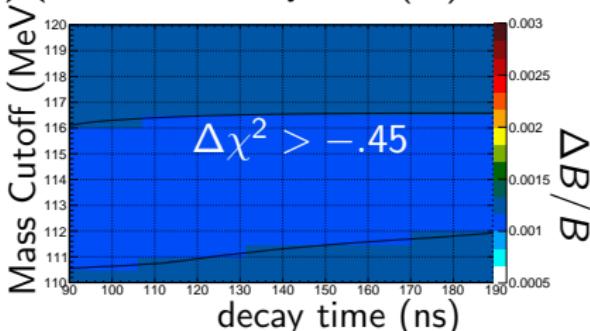
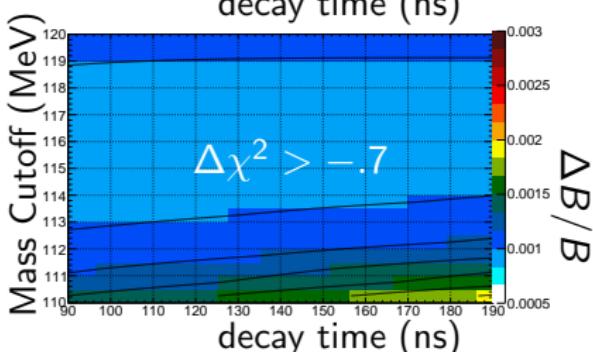
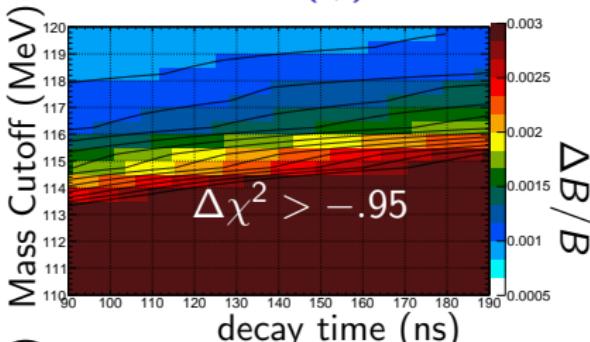
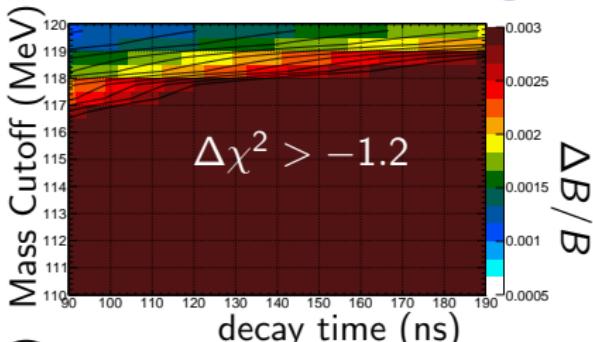


Minimizing Error for $\pi \rightarrow e\nu(\gamma)$



$\Delta\chi^2$ and decay time affect $N_{\pi \rightarrow e\nu(\gamma)}$ and $\delta N_{\pi \rightarrow e\nu(\gamma)}$
Balance between tail/peak cutoff, decay time and $\Delta\chi^2$

Minimizing Error for $\pi \rightarrow e\nu(\gamma)$



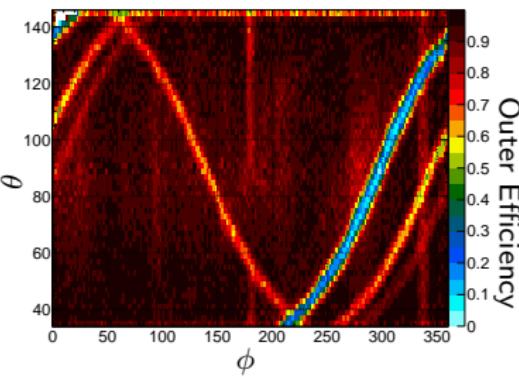
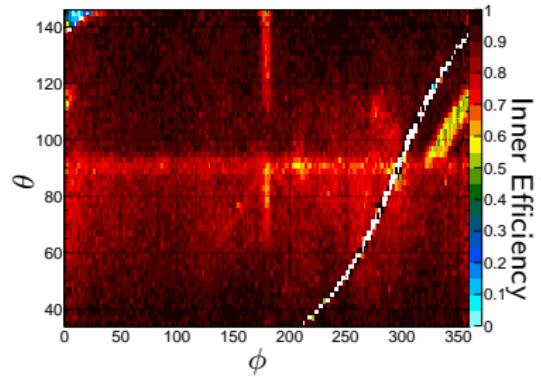
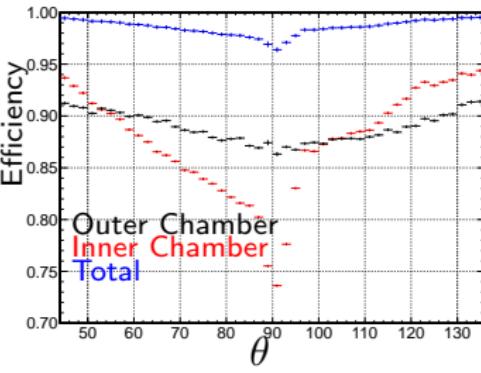
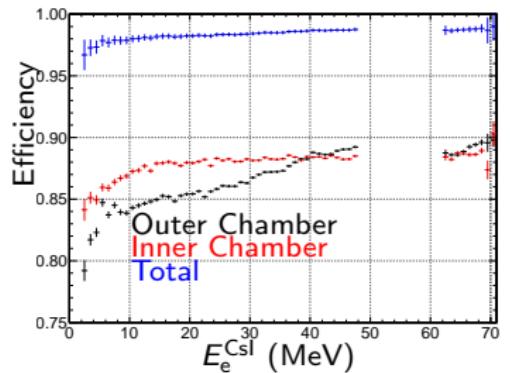
Cutoff = 117.5 MeV

Decay time = 93.5 ns

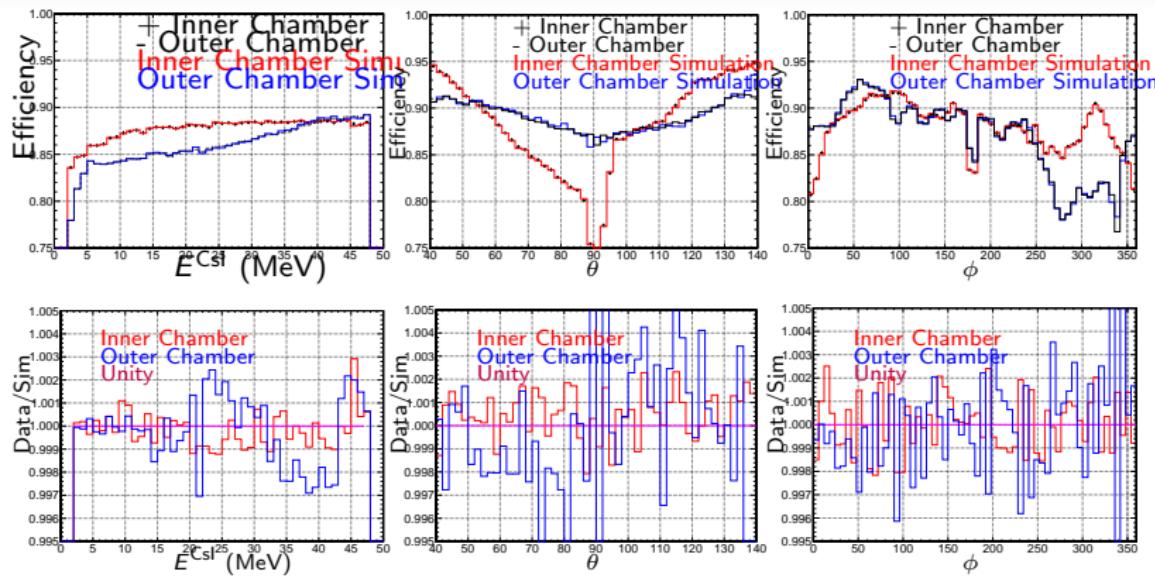
$\Delta\chi^2 > -0.8$



Chamber Efficiencies



Simulation Chamber Efficiencies



$dE/dx = f(E)$ in Chamber Gas

$\pi \rightarrow e^+ \nu_e$ 70 MeV monoenergetic
 $\mu \rightarrow e \nu \bar{\nu}$ 0-52.5 MeV spectrum

Monte Carlo is weighted to simulate chamber efficiencies
 Absorbed into Acceptances (Blinded)

Table of Uncertainties

$$B = \frac{N_{\pi \rightarrow e\nu}^{\text{peak}}}{N_{\pi \rightarrow \mu\nu}} (1 + \epsilon_{\text{tail}}) \frac{A_{\pi \rightarrow \mu \rightarrow e}}{A_{\pi \rightarrow e\nu}} \frac{\epsilon(E_{\mu \rightarrow e\nu\bar{\nu}})_{\text{MWPC}}}{\epsilon(E_{\pi \rightarrow e\nu})_{\text{MWPC}}} \frac{f_{\pi \rightarrow \mu \rightarrow e}(T_e)}{f_{\pi \rightarrow e\nu}(T_e)}$$

 r_A r_e r_f

Systematics	Value	$\Delta B/B$
ϵ_{tail}	$(3.804 \pm 0.040) \times 10^{-2}$	3.8×10^{-4}
r_f	0.0440926	8×10^{-5}
$* r_A r_e$	*	$\simeq 10^{-4}$
Statistical:		
$N_{\pi \rightarrow \mu\nu}$	$(5225.68 \pm 0.23) \times 10^5$	4.4×10^{-5} (run 2)
	$(9545.50 \pm 0.33) \times 10^5$	3.4×10^{-5} (run 3)
$N_{\pi \rightarrow e\nu}$	$(1409.43 \pm 1.18) \times 10^3$	8.37×10^{-4} (run 2)
	$(2413.81 \pm 1.63) \times 10^3$	6.75×10^{-4} (run 3)
$\Delta N_{\pi \rightarrow e\nu}/N_{\pi \rightarrow e\nu}$	4.13×10^{-4} (possible)	5.26×10^{-4} (run 2/3)
	5×10^{-4} (Goal)	7.6×10^{-4}

* Blinded



Family

Current and former PIBETA and PEN collaborators

L. P. Alonzi , K. Assamagan , V. A. Baranov , W. Bertl ,
C. Broennimann , S. Bruch , M. Bychkov , Yu.M. Bystritsky , M. Daum ,
T. Fl "ugel , E. Frlež , C. Glaser, R. Frosch, K. Keeter, V.A. Kalinnikov ,
N.V. Khomutov , J. Koglin , A.S. Korenchenko , S.M. Korenchenko ,
M. Korolija , T. Kozlowski, N.P. Kravchuk , N.A. Kuchinsky,
D. Lawrence , M. Lehman, W. Li , J. S. McCarthy , R. C. Minehart ,
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, S. Ritt , P. Robmann , O.A. Rondon-Aramayo , A.M. Rozhdestvensky
, T. Sakhelashvili , P. L. Slocum , L. C. Smith , N. Soić RB,
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H.-P. Wirtz , K. Ziock .

Home pages: <http://pibeta.phys.virginia.edu>
<http://pen.phys.virginia.edu>



Thanks for listening!

Questions?

$\Delta\chi^2$

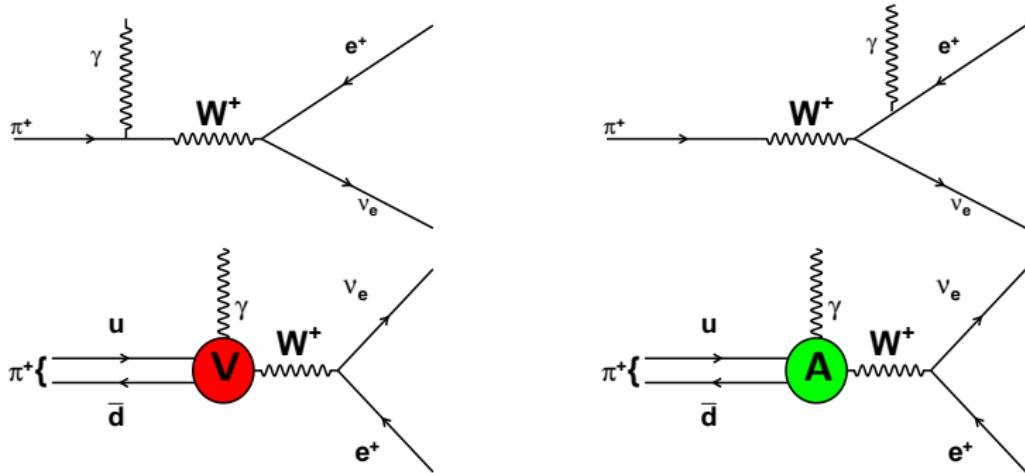
$$\chi_{2\text{peak}}^2 = \sum (\text{observed}_i - \text{predicted}_i)^2 = \sum \text{netto}_i^2$$

$$\chi_{3\text{peak}}^2 = \sum (\text{netto}_i - \text{muon}_i)^2$$

$$\begin{aligned}\Delta\chi^2 &= \sum_{i=0}^{1000} \underbrace{\left((\text{netto}_i - \text{muon}_i)^2 - \text{netto}_i^2 \right)}_{\chi_{3\text{ peak}}^2 - \chi_{2\text{ peak}}^2} / \sum_{i=0}^{1000} (\text{muon}_i)^2 \\ &= 1 - 2 \sum_{i=0}^{1000} \text{netto}_i \text{muon}_i / \sum_{i=0}^{1000} (\text{muon}_i)^2\end{aligned}$$



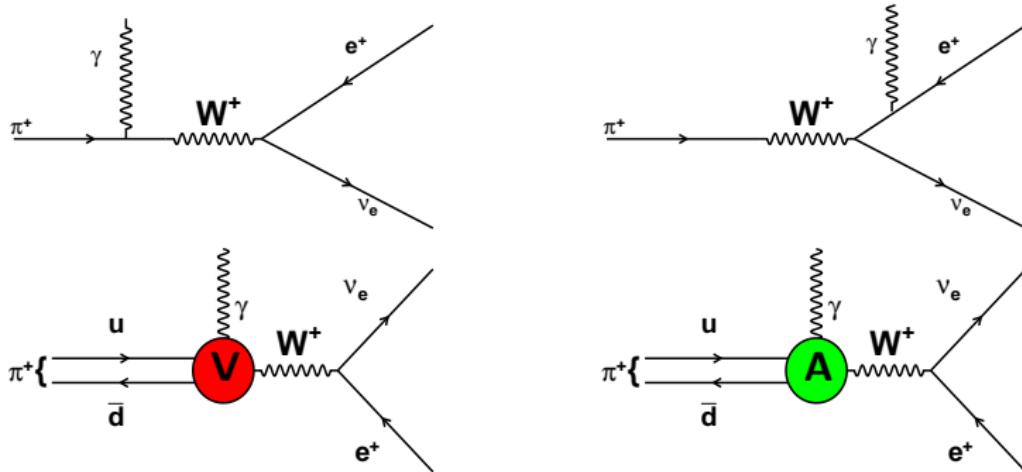
Physics of Radiative Decays



Physics of Radiative Decays

Inner Bremstrahlung (IB)

(Boring)



Structure Dependent (Not Boring!)



Physics and Math of Radiative Decays

$$\mathcal{M}(\pi^+ \rightarrow e^+ \nu_e \gamma) = \mathcal{M}_{IB} + \mathcal{M}_{SD}$$

Parameterizing $x = 2E_\gamma/m_\pi$ and $y = 2E_e/m_\pi$

$$\begin{aligned}\frac{\Gamma_{\pi e 2\gamma}}{dxdy} = & \frac{\alpha}{2\pi} \Gamma_{\pi e 2} \left\{ IB(x, y) + \left(\frac{m_\pi}{2f_\pi m_e} \right)^2 \right. \\ & \times \left[(F_V + F_A)^2 SD^+(x, y) + (F_V - F_A)^2 SD^-(x, y) \right] \\ & \left. + \left(\frac{m_\pi}{f_\pi} \right) [(F_V + F_A) S_{int}^+(x, y) + (F_V - F_A) S_{int}^-(x, y)] \right\}.\end{aligned}$$

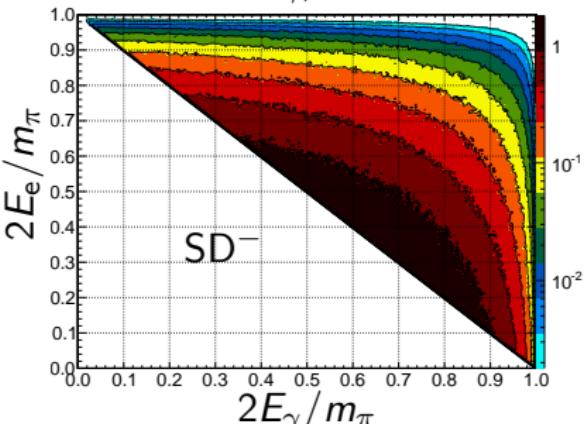
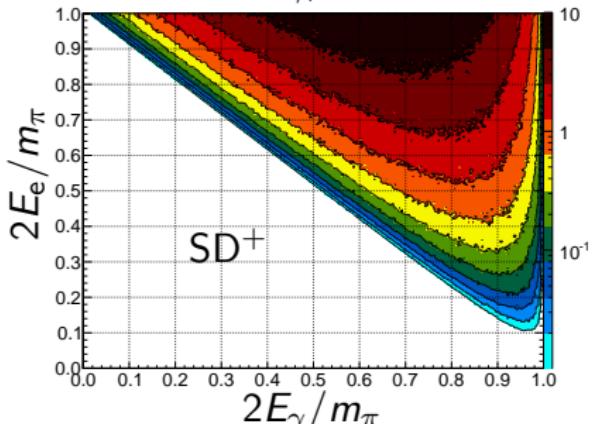
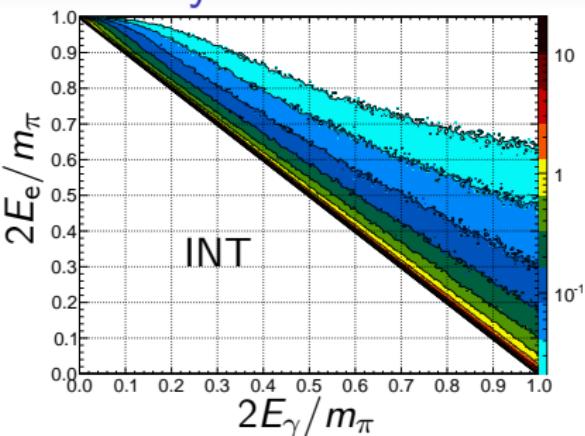
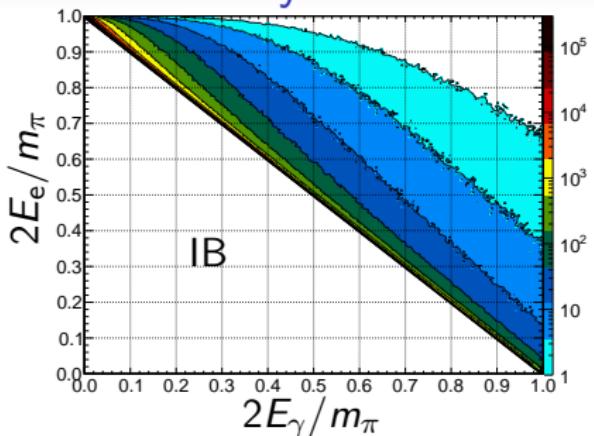
$$IB(x, y) = \frac{(1-y)[(1+(1-x)^2]}{x^2(x+y-1)}$$

$$SD^+(x, y) = (1-x)(x+y-1)^2, \quad SD^-(x, y) = (1-x)(1-y)^2$$

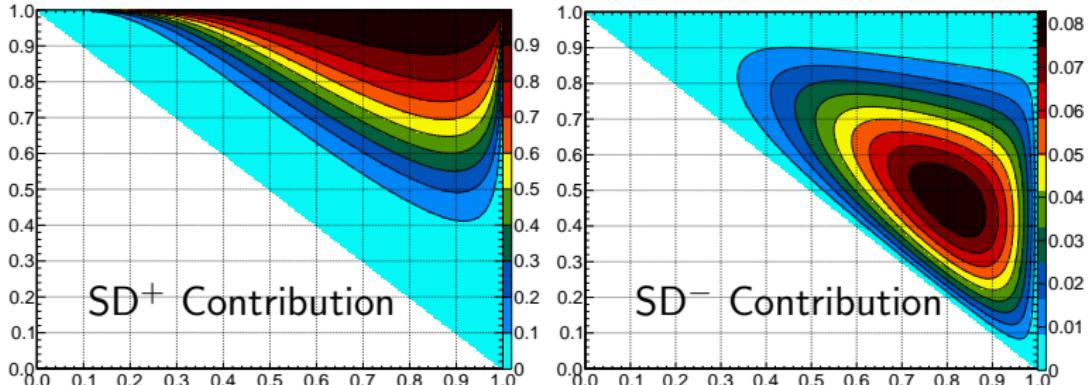
$$S_{int}^+(x, y) = -\frac{1}{x}(1-y)(1-x), \quad S_{int}^-(x, y) = \frac{1}{x^2}(1-y)(1-x + \frac{x^2}{x+y+1})$$



Physics of Radiative Decays in Pictures



Best Places for SD



SD^+ region consists of high energy e and γ 's.

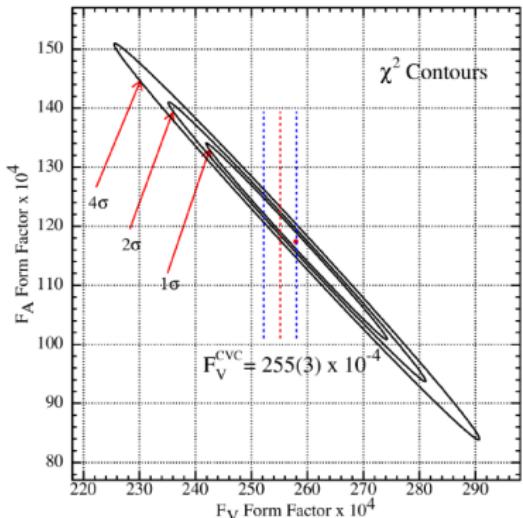
These high energy particle will have big opening angle between them

Large solid angle coverage required



Pibeta results for $\pi \rightarrow e\nu\gamma$

Pion FF values and precision improvement factors (pif) over previous work:



Observable	(pif)
$F_V = 0.0258(17)$	(8×)
$F_A = 0.0119(1)^{\text{exp}}_{(\text{F}_V^{\text{CVC}})}$	(16×)
$a = 0.10(6)^*$	(∞)
$-5.2 < 10^4 \cdot F_T < 4.0$	90 % c.l.
$B_{\pi e 2\gamma} = 73.86(54) \times 10^{-8}$	(17×)

* a ... q^2 dependence of F_V

† for ($E_\gamma > 10$ MeV, and $\theta_{e\gamma} > 40^\circ$)

[Bychkov et al., PRL 103, 051802 (2009)]

Tight constraint on SD⁺; not so tight on SD⁻!

