

The first results of the Muon g-2 experiment at Fermilab

Prof. Dr. Martin Fertl **CIPANP 2022** Orlando, FL, USA August 30th, 2022

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The magnetic moment of a charged lepton

Muon g-2: Status of theory vs. experiment before April 7th, 2021

The Muon g-2 experiment at FNAL

- The measurement principle
- The muon source
- The muon storage ring and its instrumentation

The data analysis chain

- The anomalous spin precession frequency and its corrections
- The precision magnetic field and its corrections

The current status of theory and experiment

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Outline



The magnetic moment of a charged lepton



This differs from (1) by the two extra terms

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Particle with magnetic dipole moment and spin

$$\overrightarrow{\mu} = g \frac{q}{2m} \overrightarrow{s}$$

$$\frac{eh}{c}(\sigma,\mathbf{H})+\frac{ieh}{c}\rho_1(\sigma,\mathbf{E})$$

in F. These two terms, when divided by the factor 2m, can be regarded as the additional potential energy of the electron due to its new degree of freedom. The electron will therefore behave as though it has a magnetic moment eh/2mc. σ and an electric moment $ieh/2mc \cdot \rho_1 \sigma$. This magnetic moment is just that assumed in the spinning electron model. The electric moment, being a pure imaginary, we should not expect to appear in the model. It is doubtful whether the electric moment has any physical meaning, since the Hamiltonian in (14) that we started from is real, and the imaginary part only appeared when we multiplied it up in an artificial way in order to make it resemble the Hamiltonian of previous theories.



SM contributions to the prediction of a_{μ}

A highest-precision prediction of the anomalous magnetic moment from within the SM is possible!



Figure: M. Tanabashi et al. (Particle Data Group), Phys. Rev. D98, 030001 (2018)

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$$a_{\mu} = a_{\text{QED}} + a_{\text{weak}} + a_{\text{had}}$$





2020 evaluation of the SM prediction of a_{μ}

QED ($O(\alpha^5)$, > 12000 digrams):

Electroweak:

LO hadronic vacuum polarization: NLO HVP: NNLO HVP:

LO hadronic light-by-light scattering: NLO hLbL scattering:

The largest uncertainty comes form hadronic physics contributions! Total SM prediction:

Numbers taken from "Muon g-2 Theory Initiative White Paper": Phys. Rept. 887 (2020) 1-166

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SM prediction meets the experiment

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Experiment (BNL E821):
$$a_{\mu}^{\text{BNL}} = 116592089 \pm 63 \text{ (540 ppb)}$$

Discrepancy: $\Delta a_{\mu} = a_{\mu}^{\exp} - a_{\mu}^{\text{SM}} = (279 \pm 76) \times$
Total SM2020 prediction: $a_{\mu}^{\text{SM}} = 116591810 \pm 43 \text{ (368 ppb)}$

3.7 σ deviation between SM2020 and BNL experiment!

Goal of the Muon g-2 experiment at Fermi National Laboratory Reduction of experimental uncertainty by a factor 4!

The two clocks of a free charged lepton

A *relativistic* charged lepton circulating in a homogenous magnetic field experiences two effects:

<u>Cyclotron motion</u>

Equilibrium between centrifugal and Lorentz force Coupling of magnetic moment and field

Cyclotron frequency

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Spin precession

Larmor frequency

$$\overrightarrow{\omega}_{\rm s} = -\left(\frac{g-2}{2} + \frac{1}{\gamma}\right)\frac{Qe}{m}\overrightarrow{B}$$

Anomalous spin precession frequency

$$\left(\frac{g-2}{2}\right)\frac{Qe}{m}\overrightarrow{B} = -a\frac{Qe}{m}\overrightarrow{B}$$

Clock frequency shifts for muons in motion

Evolution of muon's longitudinal polarization in a superposition of electric and magnetic fields

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Relativistically generated magnetic fields "electric field correction" "pitch correction" Reconstruction FNAL E989: $E \neq 0$ of complex beam suppressed at $\gamma = 29.3$ dynamics "magic momentum"

Extracting a_{μ} - the external ingredients

External measurements to anchor B and e to other high-precision measurements and calculations

$$a_{\mu} = \frac{\omega_{a}}{\tilde{B}'} \frac{m_{\mu}}{e} = \frac{\omega_{a}}{\tilde{\omega}_{p}'} \frac{\mu_{p}'(T_{r})}{\mu_{e}(H)} \frac{\mu_{e}(H)}{\mu_{e}(H)} \frac{m_{\mu}g_{e}}{m_{e}} \frac{g_{e}}{2}$$

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Total uncertainty from external quantities: 25 ppb

Measurement with $\frac{g_{\rm e}}{2}$ 0.28 ppt uncertainty Phys. Rev. A 83, 052122 (2011)

Extracting a_{μ} - our challenge

 $R' = \underbrace{\frac{\omega_{a}}{\tilde{\omega}_{p}'}}_{\mu} = \frac{f_{clock} \, \omega_{a}^{meas} \left(1 + C_{e} + C_{p} + C_{ml} + C_{pa}\right)}{\frac{\omega_{a}}{\tilde{\omega}_{p}'} \left(\frac{m_{\mu}}{f_{calib}} \left(\frac{M}{M} \left(\frac{x, \psi_{a}}{\omega_{p}} \phi\right)^{\mu_{p}'} \left(\frac{T_{r}}{p}\right) \mu_{e} \left(\frac{H}{M}\right) \left(\frac{m_{\mu}}{p} \frac{g_{e}}{g} B_{k} + B_{q}\right)}{\tilde{\omega}_{p}'} \left(\frac{M}{\tilde{\omega}_{p}'} \left(T_{r}\right) \mu_{e} \left(H\right) - \mu_{e}' \left(\frac{M}{m_{e}} \frac{g_{e}}{2} B_{k} + B_{q}\right)}{\tilde{\omega}_{p}'}\right)$

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Extracting a_{μ} - our tools

The statistics and the uncertainty table for Run 1

Dataset	Date	Field index n ESQ HV [kV]	Kicker HV [kV]	Number of positrons
1a	Apr 22, 2018 - Apr 25, 2018	0.108 18.3	130	0.9 x 10 ⁹
1b	Apr 26, 2018 - May 02, 2018	0.120 20.4	137	1.3 x 10 ⁹
1c	May 04, 2018 - May 12, 2018	0.120 20.4	132	2.0 x 10 ⁹
1d	Jun 06, 2018- Jun 29, 2018	0.108 18.3	125	4.0 x 10 ⁹

Quantity	Correction Terms	Uncertainty
	(ppb)	(ppb)
ω_a^m (statistical)	—	434
ω_a^m (systematic)	-	56
C_e	489	53
C_p	180	13
C_{ml}	-11	5
C_{pa}	-158	75
$f_{\text{calib}}\langle \omega_p(x, y, \phi) \times M(x, y, \phi) \rangle$		56
B_k	-27	37
B_q	-17	92
$\mu_{p}'(34.7^{\circ})/\mu_{e}$	-	10
m_{μ}/m_e	-	22
$g_e/2$	-	C
Total systematic		157
Total fundamental factors	-	25
Totals	544	462

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Uncertainty dominated by statistics!

The Fermilab muon campus

Figure courtesy: M. Convery

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A bright source of pulsed polarized muons is needed!

- 8 GeV p⁺ strike target, 120 ns bunch length
- 8 bunches spaced by 10 ms, second bunch train 200 ms later
- Pion production in the target:

$$p^+ + p^+ \to p^+ + n + \pi^+$$

Focus the "debris" into a momentum selective beam line

 ν_{μ} must be left-handed $\rightarrow \mu^+$ also left-handed!

- Figures: K.S. Khaw, PhD thesis, ETH Zürich, 2015

The muon g-2 experiment at Fermilab

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The superconducting magnet in MC1

Particles from delivery ring

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Magic momentum: $p_{\mu}^{\text{magic}} = 3.094 \,\text{GeV/c} \pm 0.5 \,\%$

The muon inflector magnet

Particles from delivery ring

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Superconducting inflector magnet cancels return B field in iron yoke to make muon travel straight!

Field free region

The fast kicker

The electrostatic quadrupoles

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Pulsed "electrostatic" quadrupoles

Vertical focusing and confinement of positive muon beam

Quasi-penning trap cover 43% of the ring

The positron calorimeter system

Wiggle plot basics and laser calibration system

Spin precession in muon rest frame

transforms to

above-energy-threshold count rate modulation in laboratory frame

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Dedicated laser calibration system to ensure energy calibration of calorimeter system

Extracting a_{μ} : the anomalous spin precession frequency

$$R' = \frac{\omega_{a}}{\omega_{p}'} = \frac{f_{clock}\omega_{a}^{meas}\left(1 + C_{e} + C_{p} + C_{ml} + C_{pa}\right)}{f_{calib}\left\langle M\left(x, y, \phi\right)\omega_{p}'\left(x, y, \phi\right)\right\rangle\left(1 + B_{k} + B_{q}\right)}$$

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Extract ω_{a}^{meas} from the wiggle plot

Separate analyses for Runs 1a-1d Histogram of decay e⁺ arrival times (wiggle plot)

3 independent event reconstruction schemes 11 different and independent analyses 6 independent groups

Complex beam dynamics encoded in wiggle plot M. Fertl - CIPANP 2022, August 30th 2022

Extensive systematic checks passed: \rightarrow "Software" unblinding to check consistency, hardware blinding still in place

Extracting a_{μ} : the muon beam dynamics corrections

$$R' = \frac{\omega_{a}}{\omega_{p}'} = \frac{f_{clock} \,\omega_{a}^{meas} \left(1 + C_{e} + C_{p} + C_{ml} + C_{pa}\right)}{f_{calib} \left\langle M\left(x, y, \phi\right) \,\omega_{p}'\left(x, y, \phi\right) \right\rangle \left(1 + B_{k} + B_{q}\right)}$$

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The straw tracker stations

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Determine e⁺ trajectory to decay position and extrapolate to find muon beam distribution! Input for beam dynamics simulations and magnetic field averaging

The long-known corrections: E-field and pitch correction

$$\frac{d}{dt}P_{\rm L} = \frac{d}{dt}\left(\hat{\beta}\cdot\vec{s}\right) = -\frac{e}{m}\vec{s_{\perp}}\cdot\left[a_{\mu}\hat{\beta}\times\vec{B} + \left(a_{\mu} - \frac{1}{\gamma^2 - 1}\right)\beta\vec{E}\right]$$

Pitch correction

Electrostatic focusing \rightarrow spin precession due to E_x and vertical harmonic motion in quadratic E field!

$$C_{\rm p} = \frac{n}{4R_0^2} \left\langle A^2 \right\rangle$$

Trackers measure vertical oscillation amplitude

Correction: 180 ppb, Uncertainty: 13 ppb

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Electric field correction

"Fast rotation analysis"

Run 1 muon distribution Muons were not centered!

$$C_e = -2n(1-n)\beta^2 \frac{\langle x_e^2 \rangle}{R_0^2}$$

Correction: 489 ppb, Uncertainty: 53 ppb

Phase acceptance correction

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$$N(t) \approx N_0 e^{-\lambda t} \left[1 + \int_{a} \cos \left(\omega_a t + \phi \right) \right]$$

The phase of the muon effects on stable, then:
$$\omega_a t + \phi_0 + \int_{a} t e^{-\lambda t} \left(\sum_{a=1}^{a} \cos \left((\omega_a + \phi')t + \phi_0 + e^{-\lambda t} \right) \right) = \cos \left((\omega_a + \phi')t + \phi_0 + e^{-\lambda t} \right)$$

The phase of the muon effects of the muon of the muon effects of the muon e

• The decay positrons encode a particular phase

- This phase depends on
 - Muon decay position
 - Decay positron energy

Extensive simulation campaign

• Not a problem if muon distribution is stable in time, but...

Phase acceptance correction: The voltage on the ESQs

Extracting a_{μ} : the magnetic field distribution and calibration

$$R' = \frac{\omega_{a}}{\omega_{p}'} = \frac{f_{clock} \,\omega_{a}^{meas} \left(1 + C_{e} + C_{p} + C_{ml} + C_{pa}\right)}{f_{calib} \left\langle M\left(x, y, \phi\right) \omega_{p}'\left(x, y, \phi\right) \right\rangle \left(1 + B_{k} + B_{q}\right)}$$

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The magnetic field calibration chain

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"The fixed probe array" "The calibration" "Plunging probe" to transfer 378 pulsed nuclear magnetic absolute calibration to trolley probes resonance probes measure 24/7 around µ beam PT1000 macor support aluminum shield 100.00 mm Serial inductor coi Base piece w RF coil support RF coil Outer crimp ring double crimp connection 254 mm Petroleum jelly volume Inner crimp ring Inner conductor of capacitor Parallel inductor coil Shatter Resistant

The precision magnetic field: spatial mapping

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A typical azimuthally averaged magnetic field map

For more details listen to

K.W. Hong Aug 30th, 2022, 3:30 PM Today!

Extracting a_{μ} : the muon weighted average magnetic field

$$R' = \frac{\omega_{a}}{\omega_{p}'} = \frac{f_{clock} \,\omega_{a}^{meas} \left(1 + C_{e} + C_{p} + C_{ml} + C_{pa}\right)}{f_{calib} \left(M\left(x, y, \phi\right) \,\omega_{p}'\left(x, y, \phi\right)\right) \left(1 + B_{k} + B_{q}\right)}$$

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The muon weighted average magnetic field

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Total uncertainty of convoluted field map: 56 ppb

 $R' = \frac{\omega_{a}}{\omega_{p}'} = \frac{f_{clock} \,\omega_{a}^{meas} \left(1 + C_{e} + C_{p} + C_{ml} + C_{pa}\right)}{f_{calib} \left\langle M\left(x, y, \phi\right) \,\omega_{p}'\left(x, y, \phi\right) \right\rangle \left(1 + B_{k} + B_{q}\right)}$

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Extracting a_{μ} : transients from ESQ

Transients from electrostatic quadrupoles (ESQ)

ESQ only static on the time scale of an muon beam bunch injection:

- Pulsing with high-voltage:
 - \rightarrow mechanical vibrations of electric conductors
 - \rightarrow perturbation of B field

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Extracting a_{μ} - our tools

$$(1 + C_{\rm e} + C_{\rm p} + C_{\rm ml} + C_{\rm pa})$$

$$\left(\omega_{p}^{\prime}(x,y,\phi) \right) \left(1 + B_{k} + B_{q} \right)$$

Muon beam dynamics

corrections

Spatial distribution of magnetic field

Transient magnetic fields

Calibration

All the analysis is available for you to look at in detail

PHYSICAL REVIEW ACCELERATORS AND BEAMS 24, 044002 (2021)

Beam dynamics corrections to the Run-1 measurement of the muon anomalous magnetic moment at Fermilab

PHYSICAL REVIEW D 103, 072002 (2021) T. Albahri, Featured in Physics **Editors' Suggestion** Measurement of the anomalous precession frequency of the muon in the Fermilab Muon g-2 Experiment PHYSICAL REVIEW A 103, 042208 (2021) T. Albahri, Featured in Physics

Magnetic-field measurement and analysis for the Muon g - 2 Experiment at Fermilab

T. Albahri,³⁹

PHYSICAL REVIEW LETTERS 126, 141801 (2021)

Editors' Suggestion

Featured in Physics

Measurement of the Positive Muon Anomalous Magnetic Moment to 0.46 ppm

B. Abi,⁴⁴ T. Albahri,³⁹ S. Al-Kilani,³⁶ D. Allspach,⁷ L. P. Alonzi,⁴⁸ A. Anastasi,^{11,a} A. Anisenkov,^{4,b} F. Azfar,⁴⁴ K. Badgley,⁷ S. Baeßler,^{47,e} I. Bailey,^{19,d} V. A. Baranov,¹⁷ E. Barlas-Yucel,³⁷ T. Barrett,⁶ E. Barzi,⁷ A. Basti,^{11,32} F. Bedeschi,¹¹ A. Behnke,²² M. Berz,²⁰ M. Bhattacharya,⁴³ H. P. Binney,⁴⁸ R. Bjorkquist,⁶ P. Bloom,²¹ J. Bono,⁷ E. Bottalico,^{11,32} T. Bowcock,³⁹ D. Boyden,²² G. Cantatore,^{13,34} R. M. Carey,² J. Carroll,³⁹ B. C. K. Casey,⁷ D. Cauz,^{35,8} S. Ceravolo,⁹ R. Chakraborty,³⁸ S. P. Chang,^{18,5} A. Chapelain,⁶ S. Chappa,⁷ S. Charity,⁷ R. Chislett,³⁶ J. Choi,⁵ Z. Chu,^{26,e} T. E. Chupp,⁴² M. E. Convery,⁷ A. Conway,⁴¹ G. Corradi,⁹ S. Corrodi,¹ L. Cotrozzi,^{11,32} J. D. Crnkovic,^{3,37,43} S. Dabagov,^{9,} P. M. De Lurgio,¹ P. T. Debevec,³⁷ S. Di Falco,¹¹ P. Di Meo,¹⁰ G. Di Sciascio,¹² R. Di Stefano,^{10,30} B. Drendel,⁷ A. Driutti,^{35,13,38} V. N. Duginov,¹⁷ M. Eads,²² N. Eggert,⁶ A. Epps,²² J. Esquivel,⁷ M. Farooq,⁴² R. Fatemi,³⁸ C. Ferrari,^{11,14} M. Fertl,^{48,16} A. Fiedler,²² A. T. Fienberg,⁴⁸ A. Fioretti,^{11,14} D. Flay,⁴¹ S. B. Foster,² H. Friedsam,⁷ E. Frlež,⁴⁷ N. S. Froemming,^{48,22} J. Fry,⁴⁷ C. Fu,^{26,e} C. Gabbanini,^{11,14} M. D. Galati,^{11,32} S. Ganguly,^{37,7} A. Garcia,⁴⁸ D. E. Gastler,² J. George,⁴¹ L. K. Gibbons,⁶ A. Gioiosa,^{29,11} K. L. Giovanetti,¹⁵ P. Girotti,^{11,32} W. Gohn,³⁸ T. Gorringe,³⁸ J. Grange,^{1,42} S. Grant,³⁶ F. Gray,²⁴ S. Haciomeroglu,⁵ D. Hahn,⁷ T. Halewood-Leagas,³⁹ D. Hampai,⁹ F. Han,³⁸ E. Hazen,² 44 A T H = 39.4 D W H = 648 C H = 164 36 A H = 39 7 H = 16 48 L H = 1

Beam dynamics

Muon spin precession

Magnetic field

The result

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The Muon g-2 collaboration

Domestic Universities

Boston Cornell Illinois James Madison Kentucky Massachusetts Michigan Michigan State Mississippi Northern Illinois Regis UT Austin Virginia Washington National Labs Argonne Brookhaven Fermilab

China Shanghai Jao Tong University United Kingdom Lancaster Liverpool University College London Italy Frascati Molise Naples Pisa Roma 2 Trieste Udine Germany JGU Mainz TU Dresden Russia JINR/Dubna Novosibirsk

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South Korea

CAPP/IBS KAIST

Result from combined Run 1 datasets

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 $a_{\mu}(BNL) = 0.00116592089(63) \rightarrow 540 \text{ ppb}$

 $a_{\mu}(FNAL, R1) = 0.00116592040(54) \rightarrow 463 \text{ ppb}$

Both experiments uncertainty dominated by statistics:

 $a_{\mu}(Exp) = 0.00116592061(41) \rightarrow 350 \text{ ppb}$

 $a_{\mu}(SM2020) = 0.00116591810(43) \rightarrow 350 \text{ ppb}$

4.2 σ discrepancy between experiment and community approved SM2020 prediction

BUT: the very recent results from IQCD for HVP reduce the tension!

A new era of a_{μ} comparisons

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Hadronic vacuum polarization: data-driven vs ab initio

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$$\Delta a_{\mu} = a_{\mu}^{\exp} - a_{\mu}^{SM} = (25.1 \pm 5.9) \times 10^{-10}$$

White paper, "Muon g-2 Theory Initiative"

R-ratio: $a_{\mu}^{\text{hvp, LO}} = (693.1 \pm 4.0) \cdot 10^{-10}$

[Aoyama et al., Physics Reports 887 (2020) and arXiv:2006.04822]

Hadronic vacuum polarization: data-driven vs ab initio

Intense scrutiny of the various contributions by several groups: window observables

This work: M.Ce et al, arXiv:2206.06582v1 ETMC 21: D. Giusti and S. Simula, arXiv:2111.15329 BMW 20: S. Borsanyi et al., arXiv:2002.12347

Fifth Plenary Workshop of the Muon g-2 <u>Theory Initiative</u> to "discuss recent progress on the theoretical calculations and prepare an update of the Standard Model prediction for Muon g-2" (starting 09/05/22)

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RBC/UKQCD 18: RBC, UKQCD collaboration, arXiv:1801.07224 Colangelo et al. 22, arXiv:2205.12963

Predictions are hard to make if they concern the future but, we...

- ... have vastly improved running conditions after Run 3: reduced systematic uncertainties!

- ... look forward to the update of the SM prediction!

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• ... have accumulated 19 x BNL raw statistics through Run 5. Run 6 with μ^+ to reduce systematic uncertainties

