#### A Status Update on Ab Initio Calculations in Nuclear Physics

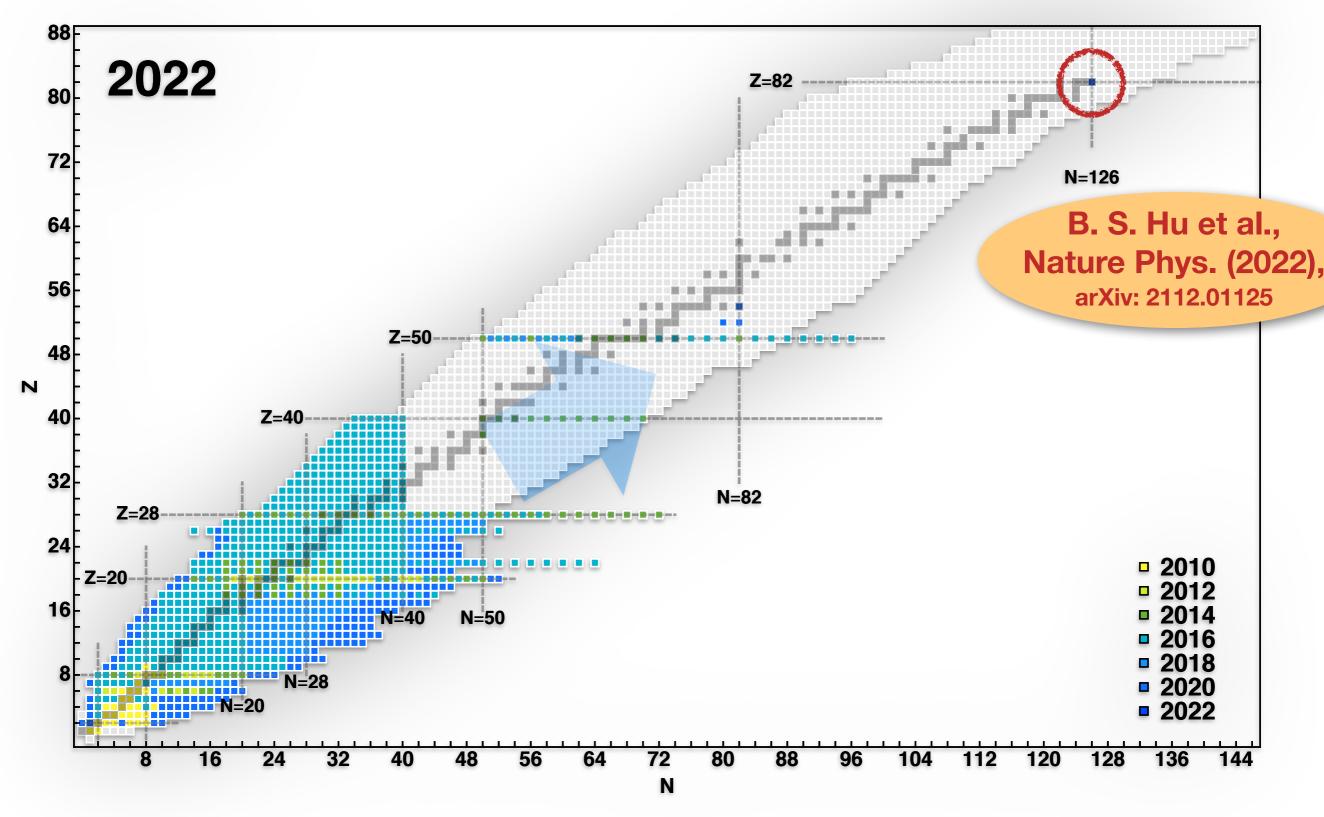
#### Heiko Hergert

Facility for Rare Isotope Beams & Department of Physics and Astronomy Michigan State University

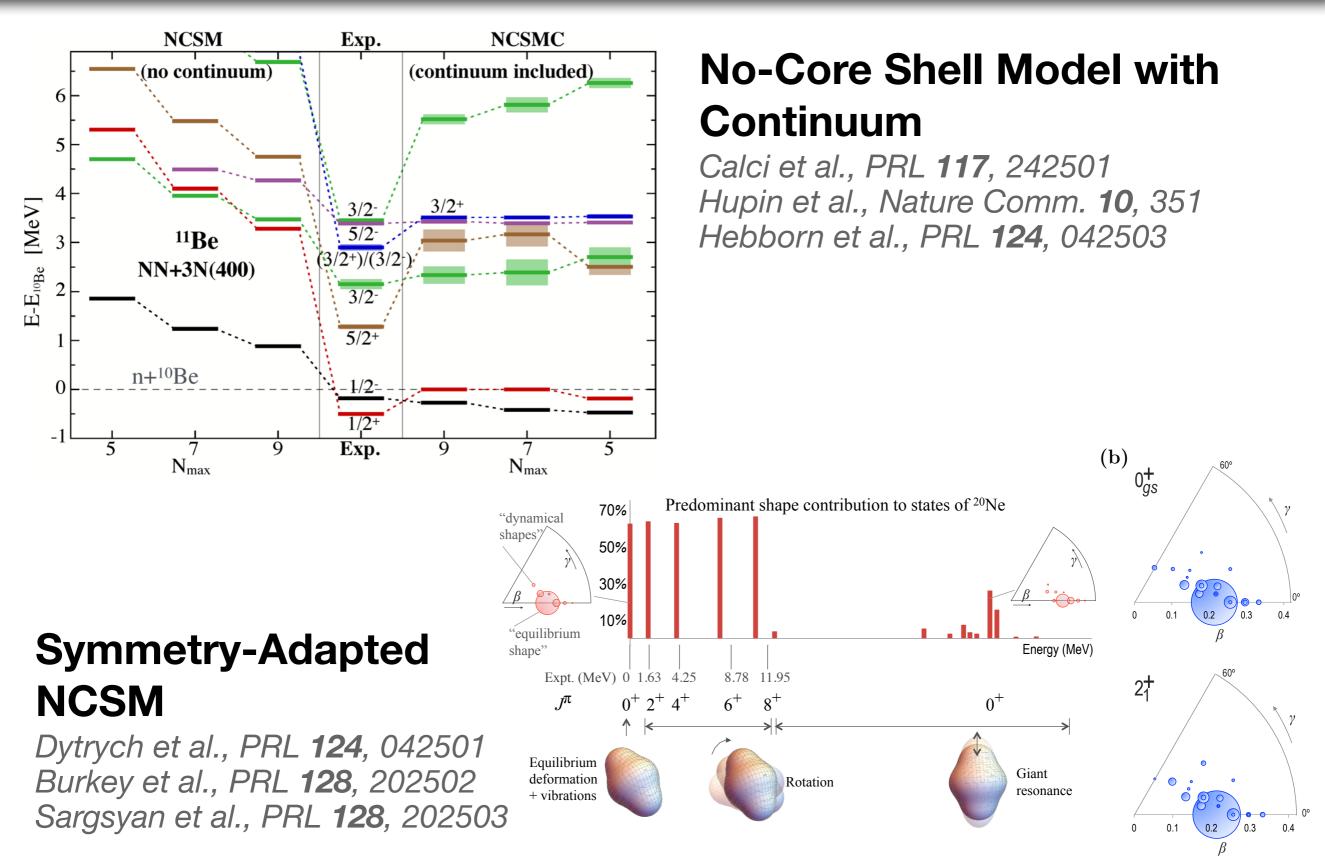




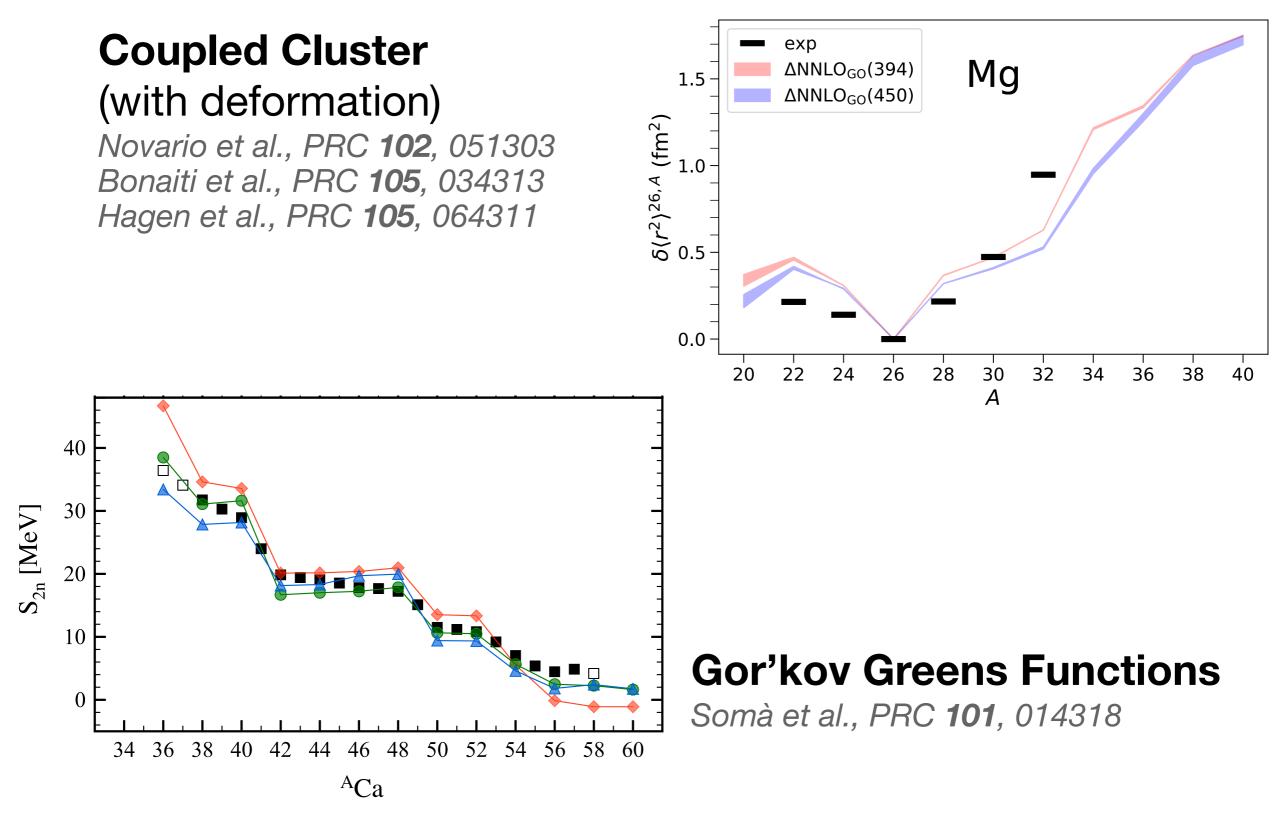
[cf. HH, Front. Phys. 8, 379 (2020)]





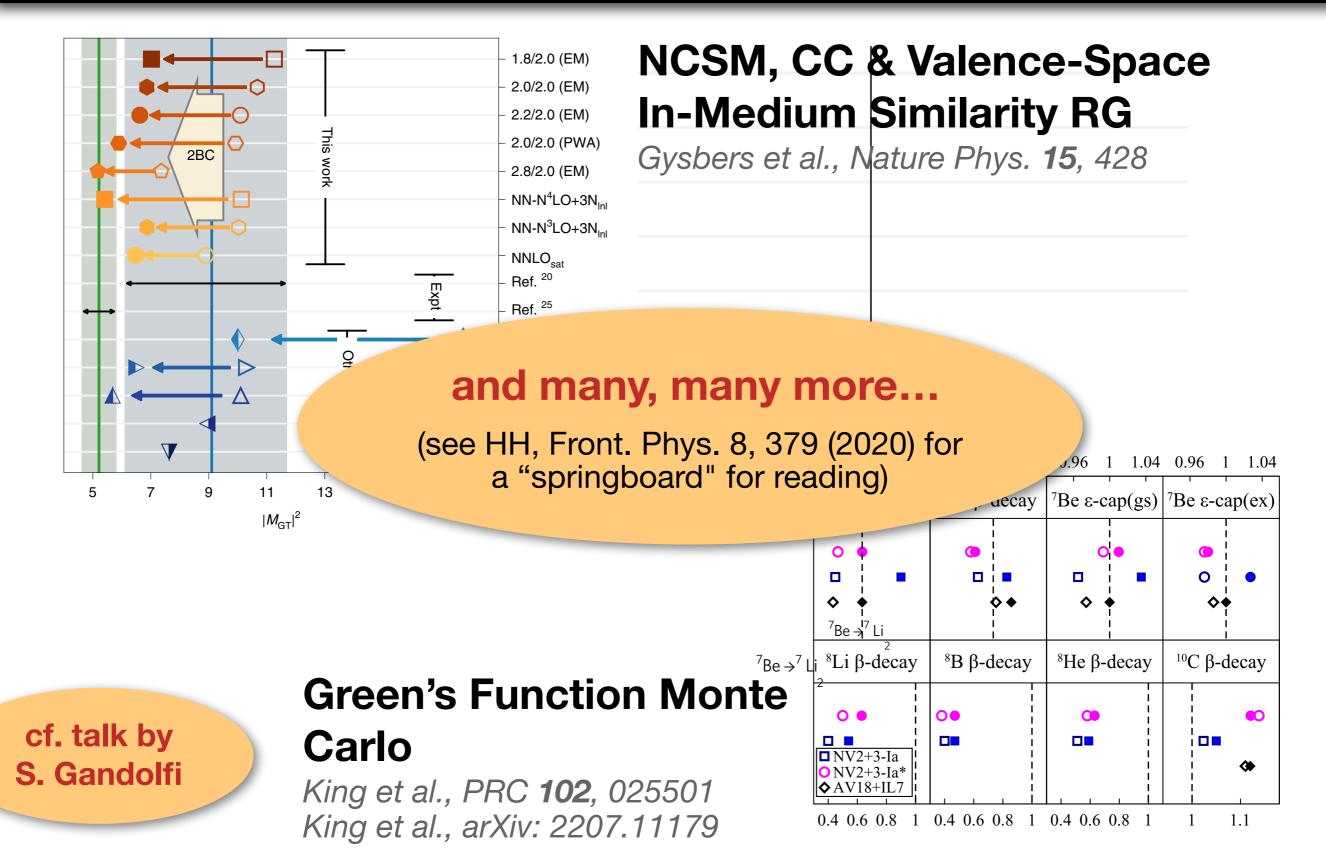






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#### (Multi-Reference) In-Medium Similarity Renormalization Group

HH, Phys. Scripta **92**, 023002 (2017)

HH, S. K. Bogner, T. D. Morris, A. Schwenk, and K. Tuskiyama, Phys. Rept. 621, 165 (2016)

HH, S. K. Bogner, T. Morris, S. Binder, A. Calci, J. Langhammer, R. Roth, Phys. Rev. C 90, 041302 (2014)

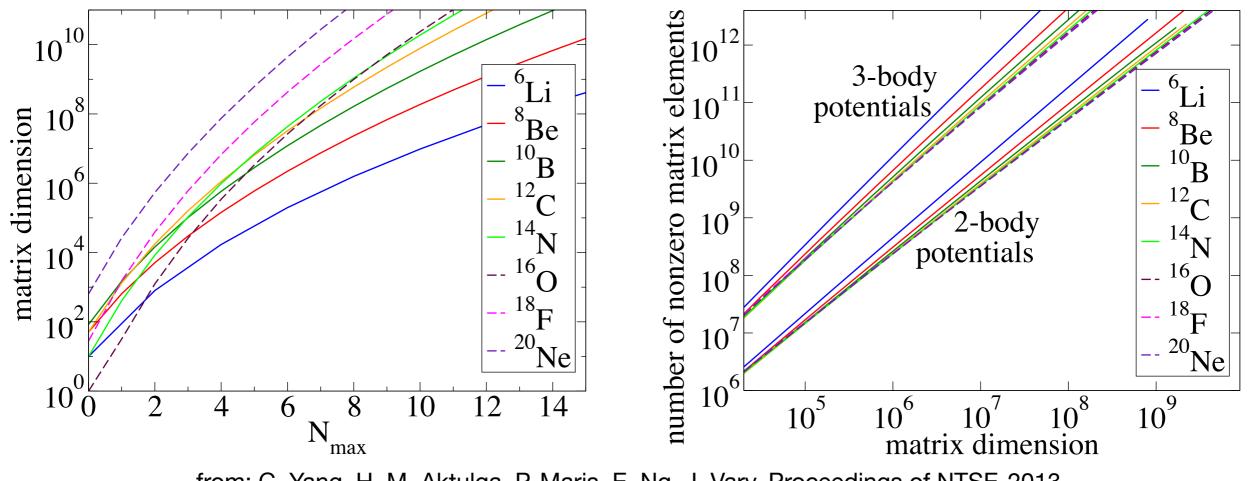
HH, S. Binder, A. Calci, J. Langhammer, and R. Roth, Phys. Rev. Lett 110, 242501 (2013)

K. Tsukiyama, S. K. Bogner, A. Schwenk, PRL 106, 222502 (2011)

S. K. Bogner, R. J. Furnstahl, and A. Schwenk, Prog. Part. Nucl. Phys. 65, 94

# Large-Scale Diagonalization

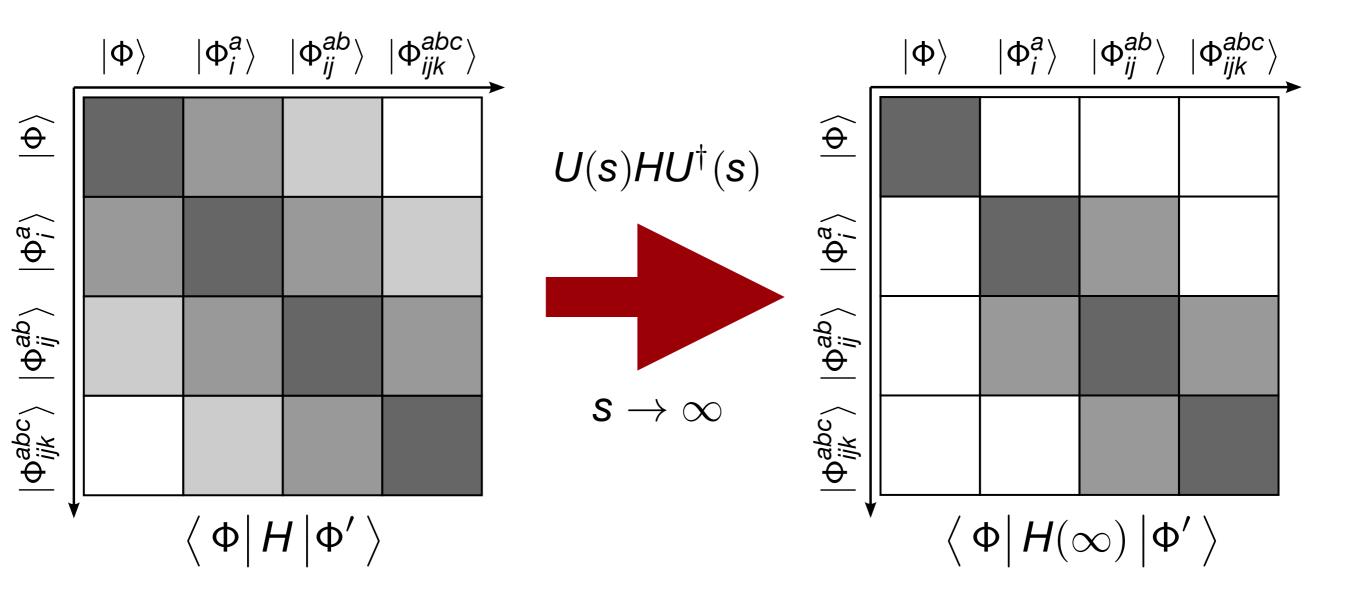




from: C. Yang, H. M. Aktulga, P. Maris, E. Ng, J. Vary, Proceedings of NTSE-2013

- basis-size "explosion": exponential growth
- importance truncation etc. cannot fully compensate this growth as A increases

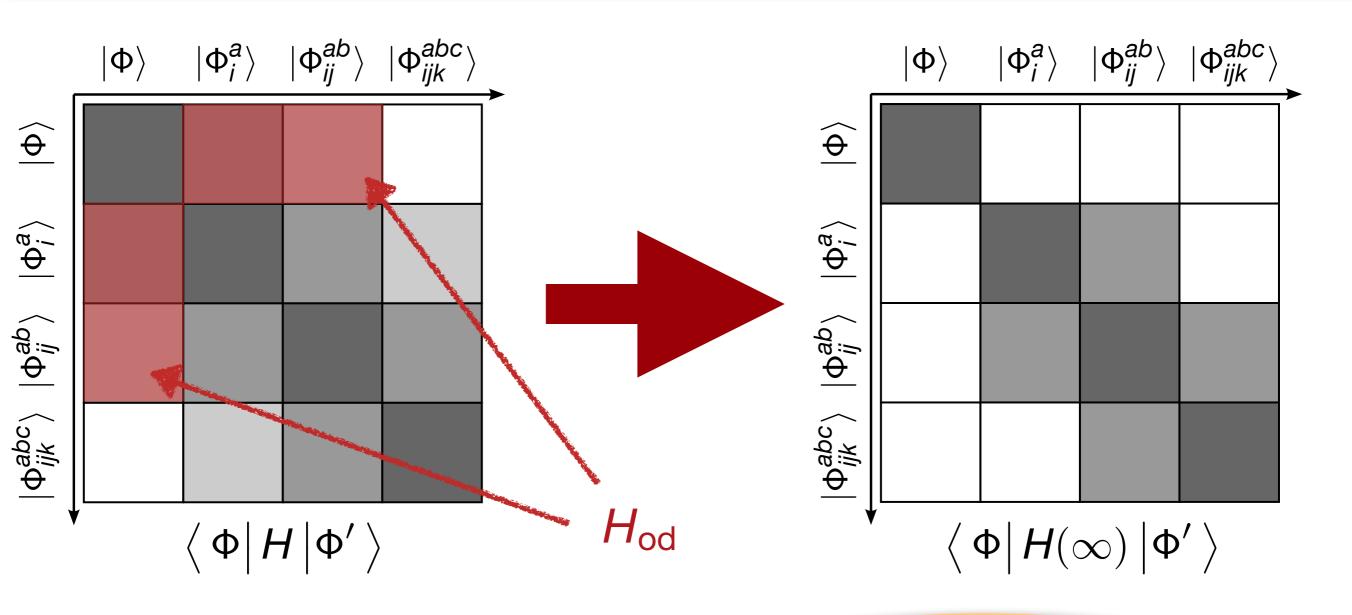
# Decoupling in A-Body Space



# **goal:** decouple reference state | $\Phi$ > from excitations

### Flow Equation



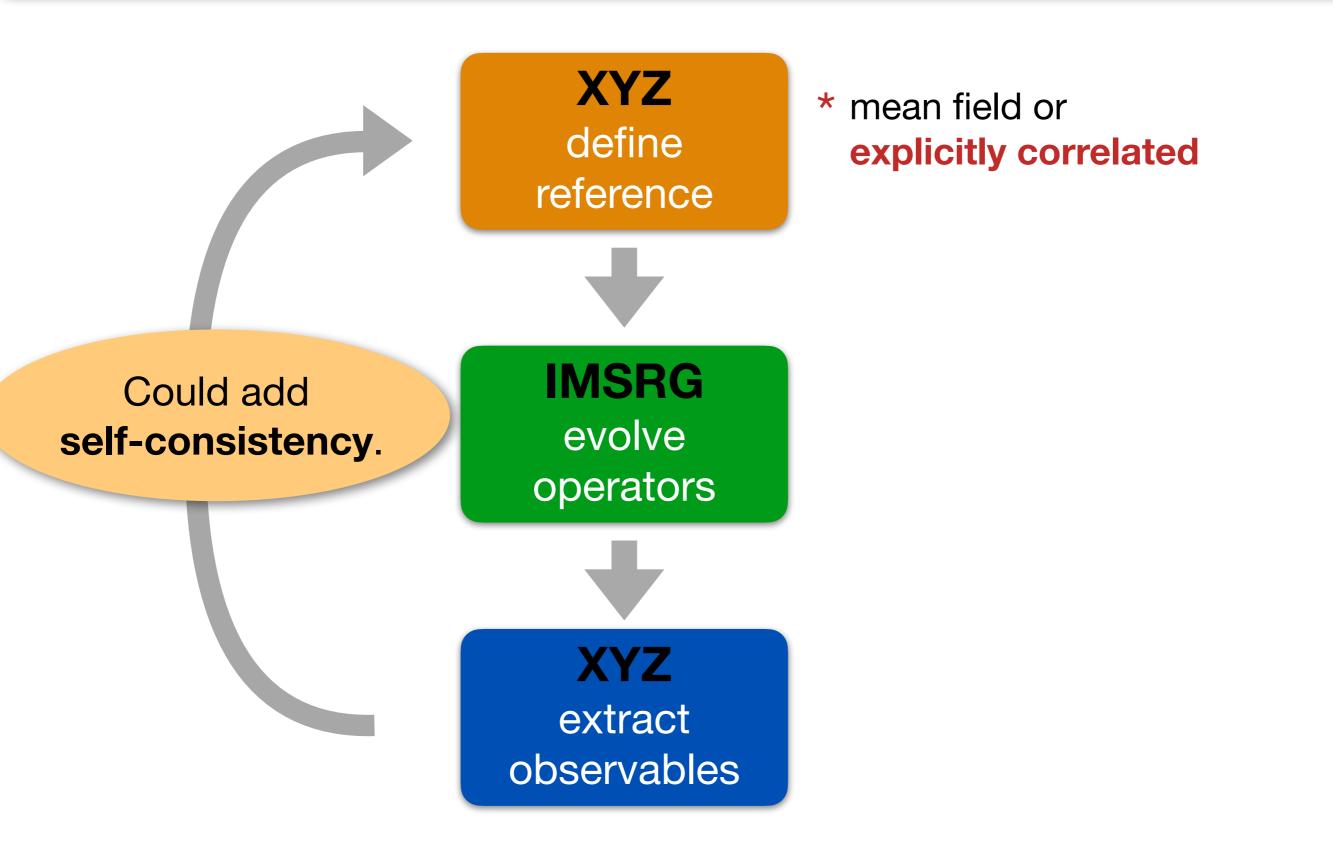


$$\frac{d}{ds}H(s) = [\eta(s), H(s)],$$

Operators truncated at two-body level matrix is never constructed explicitly!

#### **IMSRG-Improved Methods**





# **IMSRG-Improved Methods**

- IMSRG for closed and open-shell nuclei: IM-HF and **IM-PHFB** 
  - HH, Phys. Scripta, Phys. Scripta 92, 023002 (2017)
  - HH, S. K. Bogner, T. D. Morris, A. Schwenk, and K. Tuskiyama, Phys. Rept. 621, 165 (2016)
- Valence-Space IMSRG (VS-IMSRG)
  - S. R. Stroberg, HH, S. K. Bogner, J. D. Holt, Ann. Rev. Nucl. Part. Sci. **69**, 165
- In-Medium No Core Shell Model (IM-NCSM)
  - E. Gebrerufael, K. Vobig, HH, R. Roth, PRL 118, 152503

#### In-Medium Generator Coordinate Method (IM-GCM)

- J. M. Yao, J. Engel, L. J. Wang, C. F. Jiao, HH PRC 98, 054311 (2018)
- J. M. Yao et al., PRL 124, 232501 (2020)

IMSRG evolve operators

XYZ

reference







extract

observables

# Merging IMSRG and CI: Valence-Space IMSRG

**Review:** 

S. R. Stroberg, HH, S. K. Bogner, and J. D. Holt, Ann. Rev. Part. Nucl. Sci. 69, 165 (2019)

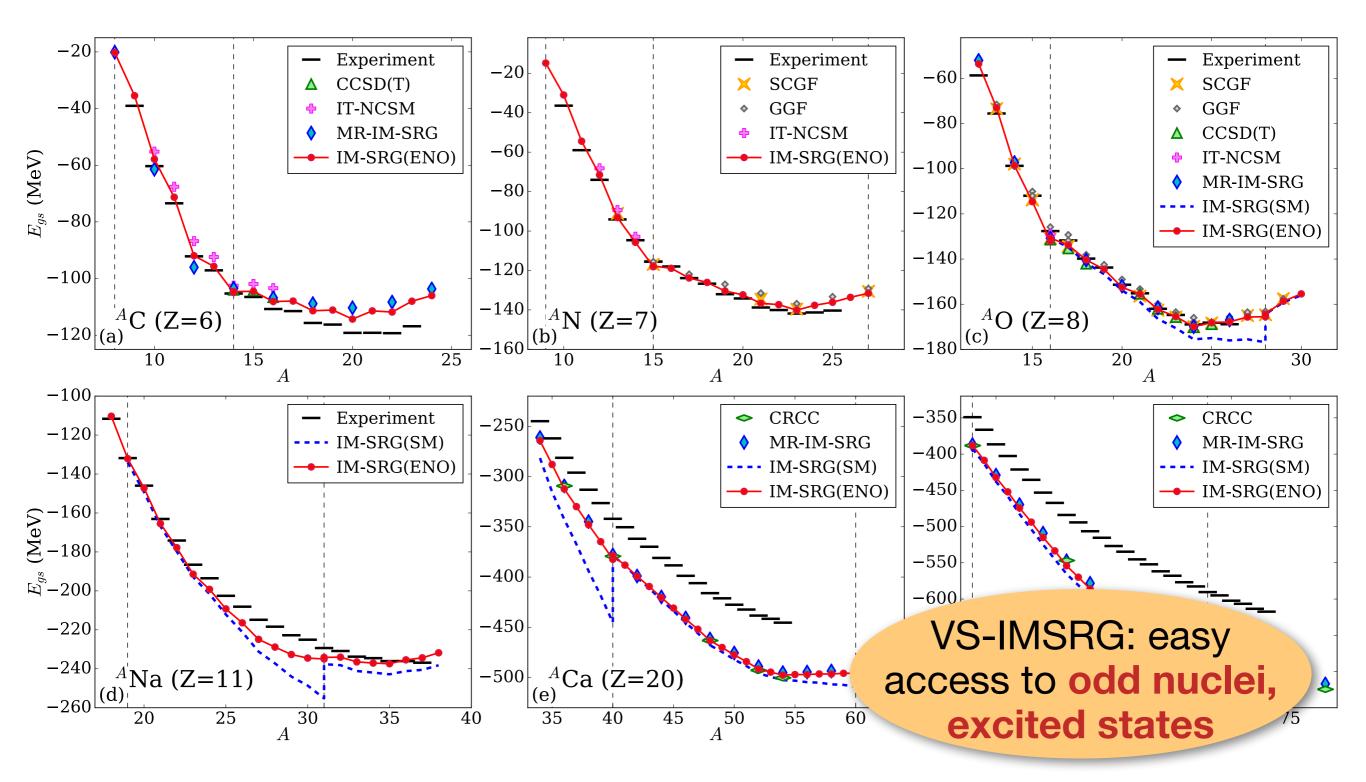
Full CI:

E. Gebrerufael, K. Vobig, HH, and R. Roth, Phys. Rev. Lett. 118, 152503 (2017)

#### **Ground-State Energies**



S. R. Stroberg, A. Calci, HH, J. D. Holt, S. K.Bogner, R. Roth, A. Schwenk, PRL **118**, 032502 (2017) S. R. Stroberg, HH, S. K. Bogner, J. D. Holt, Ann. Rev. Part. Nucl. Sci. **69**, 307 (2019)

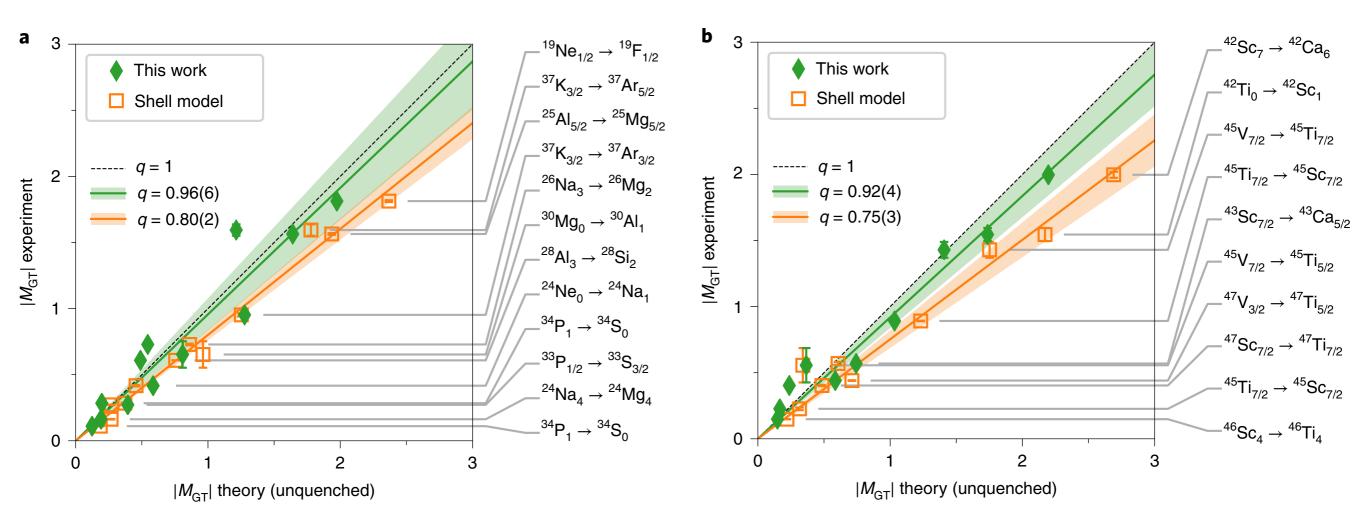


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# Quenching of Gamow-Teller Decays



P. Gysbers et al., Nature Physics 15, 428 (2019)

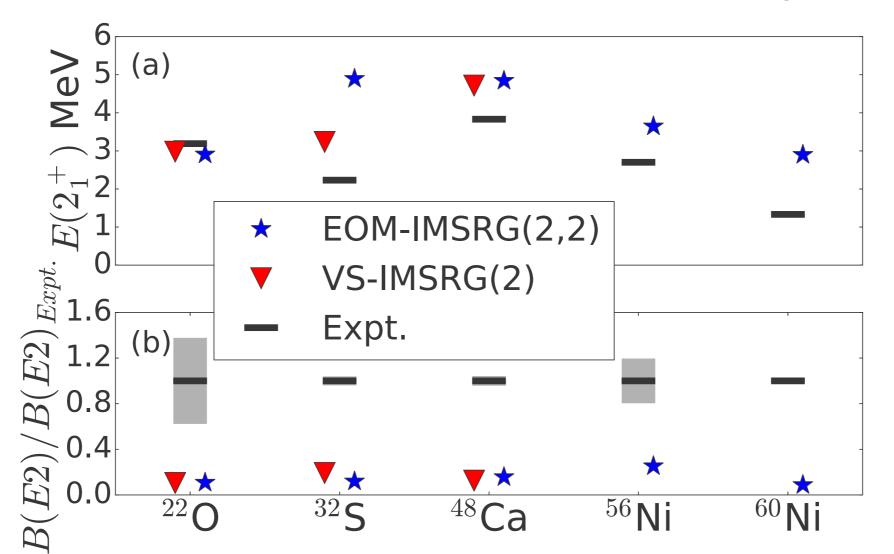


- empirical Shell model calculations require quenching factors of the weak axial-vector couling  $g_A$
- VS-IMSRG explains this through consistent renormalization of transition operator, incl. two-body currents

#### Transitions



N. M. Parzuchowski, S. R. Stroberg et al., PRC **96**, 034324 S. R. Stroberg, HH, S. K. Bogner, J. D. Holt, Ann. Rev. Part. Nucl. Sci. **69**, 307 (2019) S. R. Stroberg et al. PRC **105**, 034333 (2022)

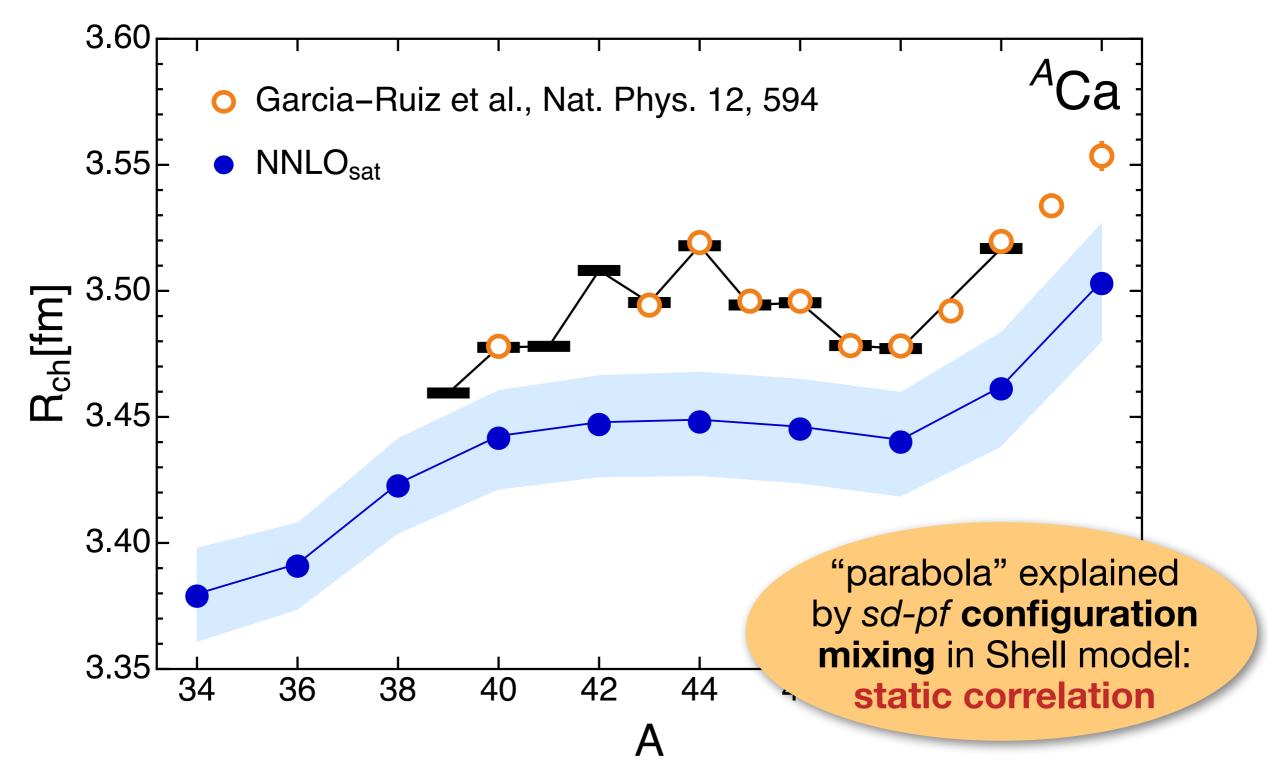


 B(E2) much too small: missing collectivity due to intermediate 3p3h, ... states that are truncated in IMSRG evolution (static correlation)

#### **Calcium Isotopes**



HH, Front. Phys. 8, 379 (2020)



# Capturing Collective Correlations: In-Medium Generator Coordinate Method

J. M. Yao, A. Belley, R. Wirth, T. Miyagi, C. G. Payne, S. R. Stroberg, HH, J. D. Holt, PRC **103**, 014315 (2021)

J. M. Yao, B. Bally, J. Engel, R. Wirth, T. R. Rodriguez, HH, PRL 124, 232501 (2020)

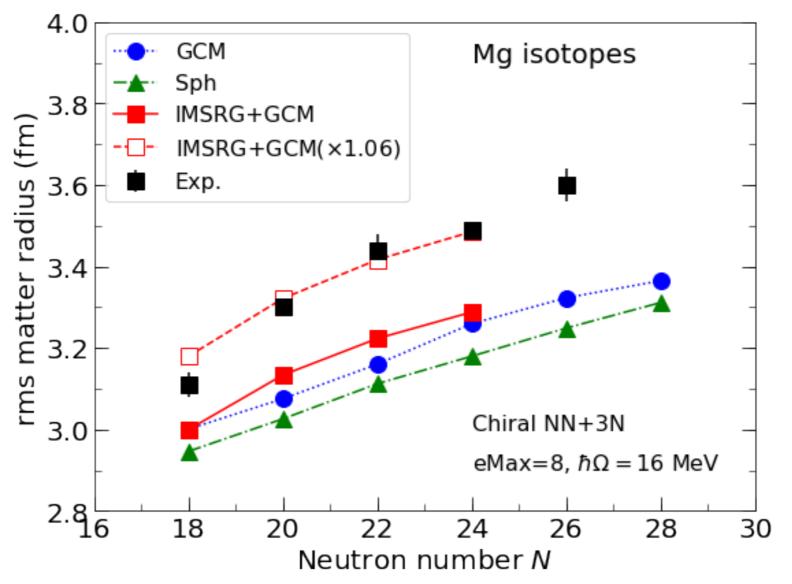
J. M. Yao, J. Engel, L. J. Wang, C. F. Jiao, H. H., PRC 98, 054311 (2018)

HH, J. M. Yao, T. D. Morris, N. M. Parzuchowski, S. K. Bogner and J. Engel, J. Phys. Conf. Ser. 1041, 012007 (2018)

# Magnesium Isotopes



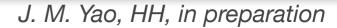
J. M. Yao, HH, in preparation

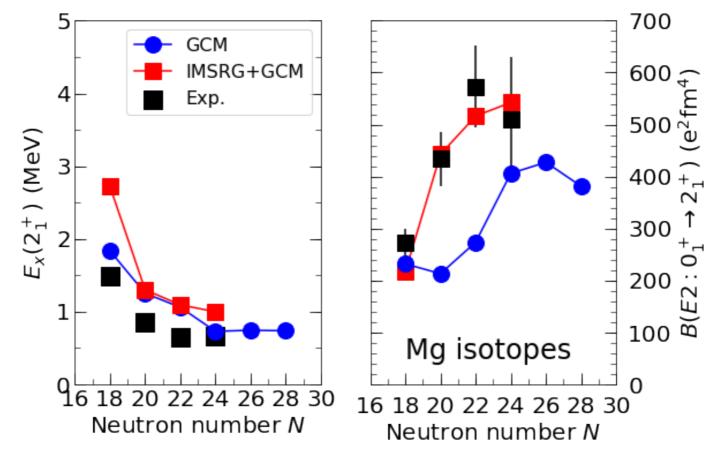


- note improvement of rms radius trend from IM-GCM
- global shifts (and/or rotation around "pivot") often associated with cutoff dependence of interactions

# Magnesium Isotopes





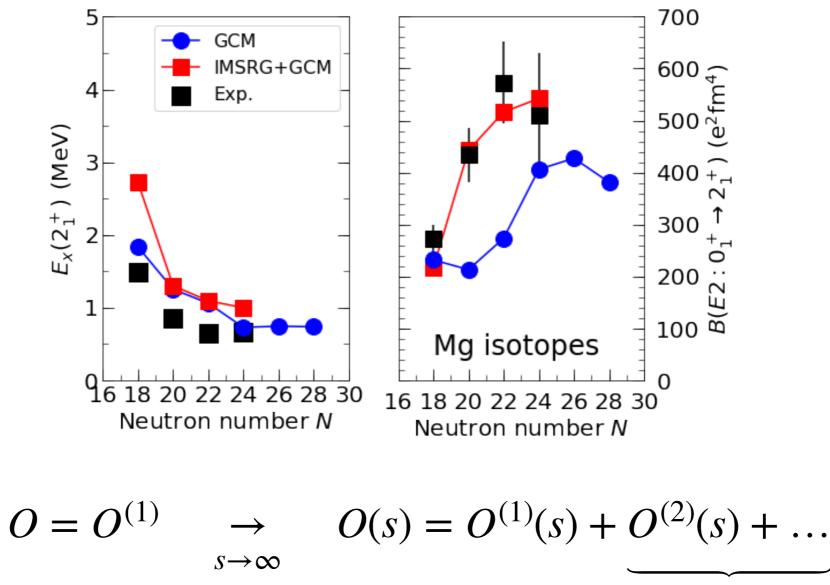


 much improved B(E2) values compared to standard GCM or VS-IMSRG calculations: IM-GCM captures dynamical and static correlations!

# Magnesium Isotopes







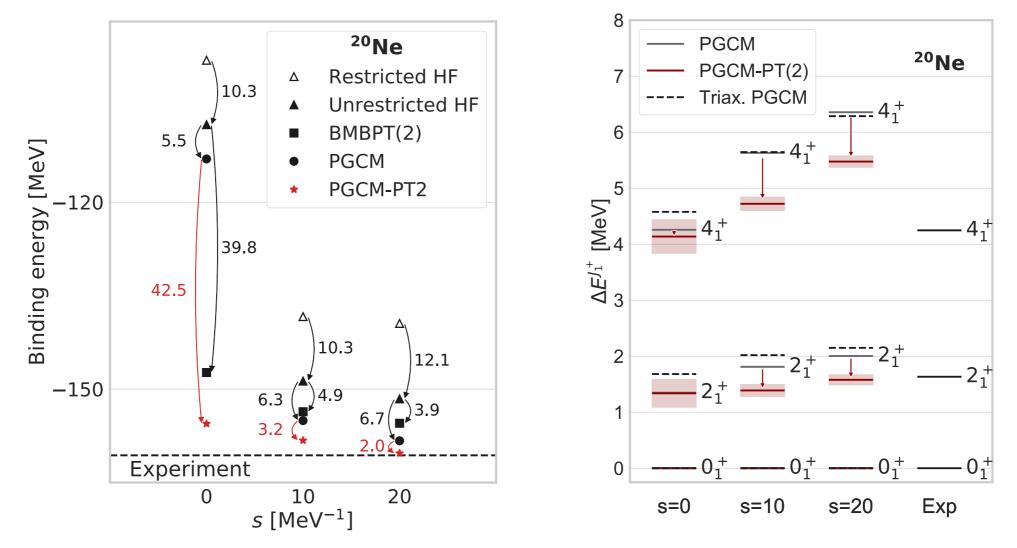
induced contributions

 induced 2B quadrupole operator is small (~5%), contrary to typical VS-IMSRG (~50%): GCM reference equips operator basis with better capability to capture collectivity

#### Perturbative Enhancement of IM-GCM



M. Frosini et al., EPJA 58, 64 (2022)

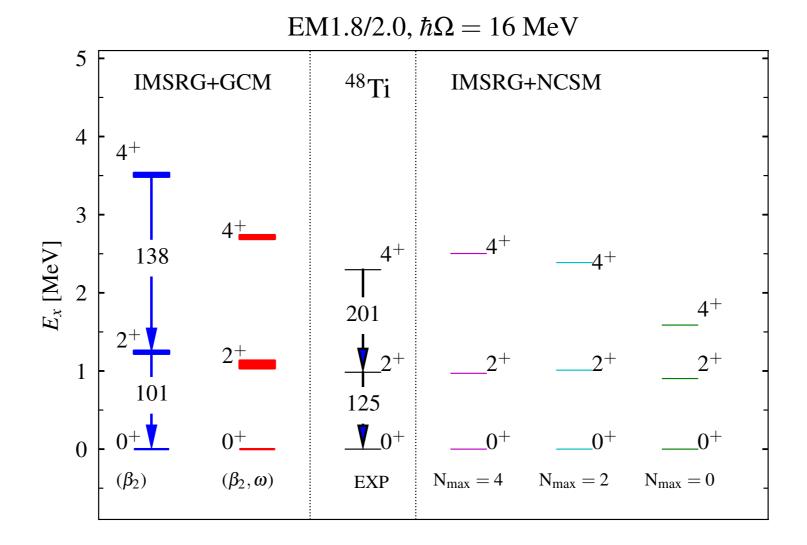


- s-dependence is a built-in diagnostic tool for IM-GCM (not available in phenomenological GCM)
  - if operator and wave function offer sufficient degrees of freedom, evolution of observables is unitary
- need richer references and/or IMSRG(3) for certain observables

# IM-GCM: $0\nu\beta\beta$ Decay of <sup>48</sup>Ca



J. M. Yao et al., PRL 124, 232501 (2020); HH, Front. Phys. 8, 379 (2020)

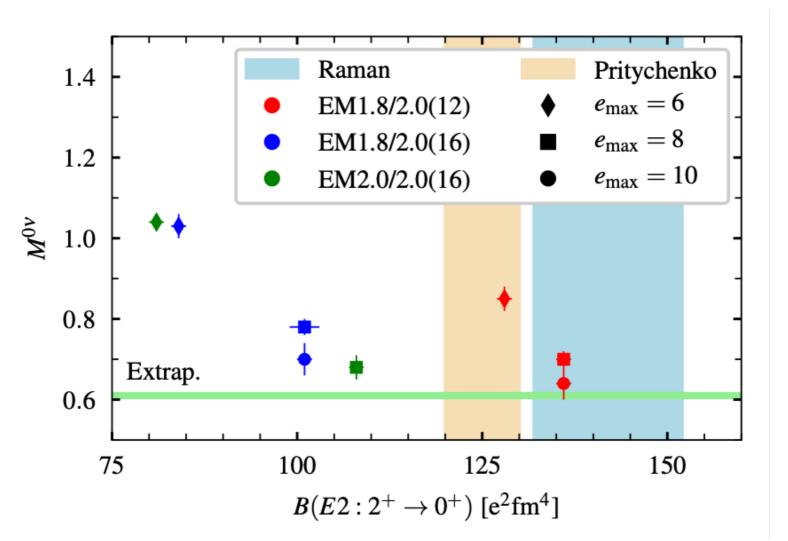


- richer GCM state through **cranking**
- consistency between IM-GCM and IM-NCSM

# 0 uetaeta Decay of <sup>48</sup>Ca



J. M. Yao et al., PRL 124, 232501 (2020); PRC 103, 014315 (2021)



- NME from different methods consistent for consistent interactions & transition operators (A. Belley et al., PRL 126, 042502, S. Novario story yet: improve IMSF
- interpretation and features differ from e only weak correlation between NME and

not the full story yet: improve IMSRG truncations, additional GCM correlations, include currents, ...

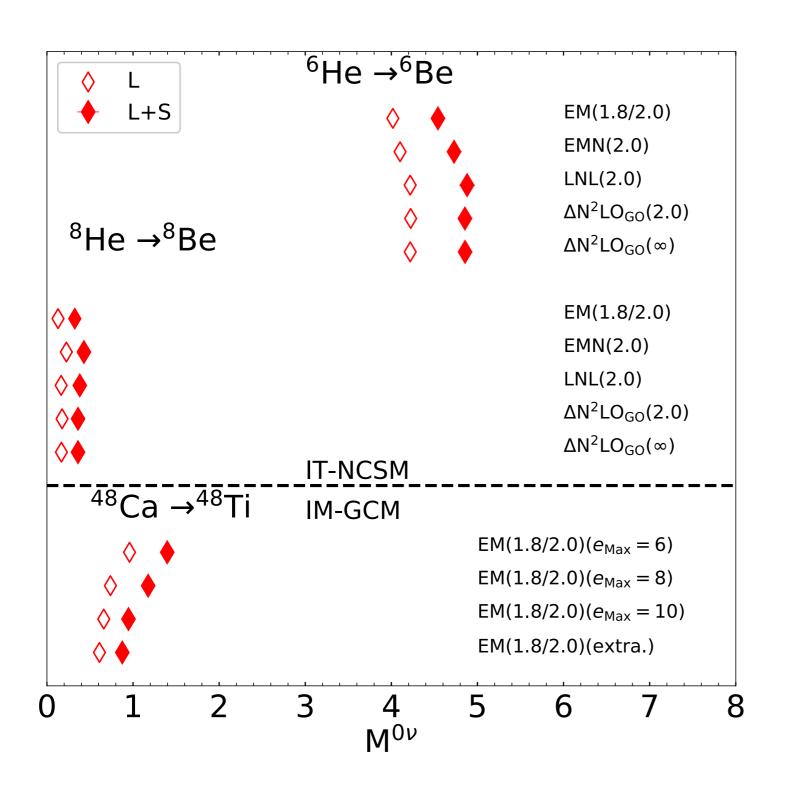
rug 31, 2022

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# Counterterm in $0\nu\beta\beta$ Operator



R. Wirth, J. M. Yao, H. Hergert, PRL 127, 242502 (2021)



- Cirigliano et al.: RG
   invariance of the DBD
   transition operator
   requires contact term
- Counter term yields robust enhancement
  - varied EFT orders, RG scales, interactions
- Next:
  - more interactions
  - inclusion of currents
  - LEC sensitivity / UQ

# Looking Ahead

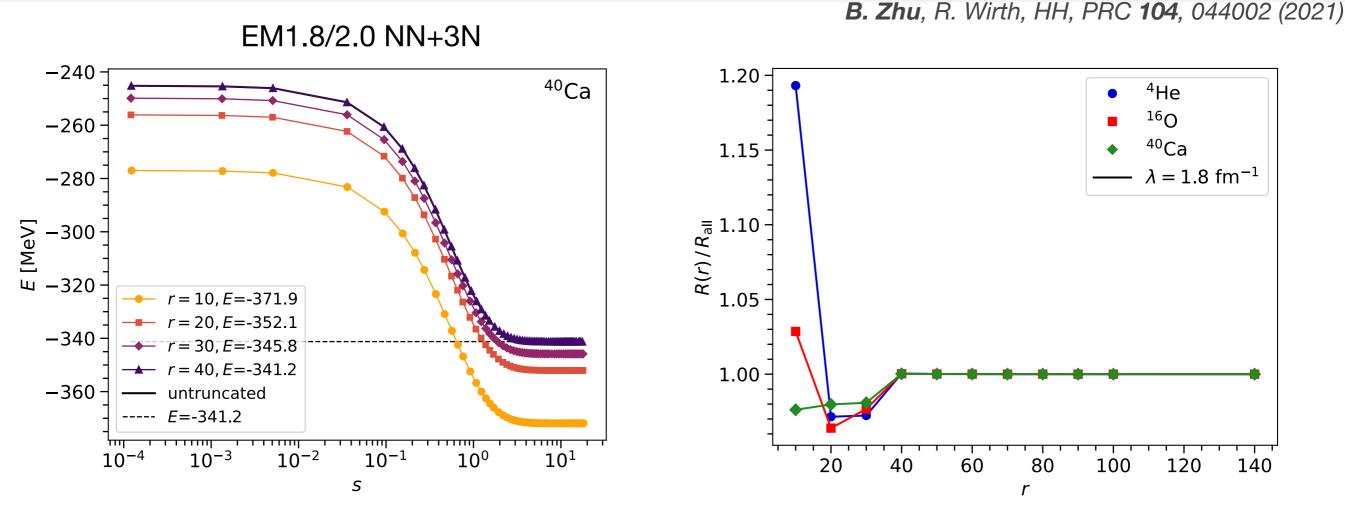
# (Some) Physics Goals



- Neutrinoless Double Beta Decay matrix elements for <sup>76</sup>Ge and other candidates
  - use VS-IMSRG for heavy lifting in parameter sensitivity analysis & UQ because IM-GCM is too costly
  - accelerate IMSRG & IM-GCM (GPUs, factorization, ...)
- increased precision for beta decays & Schiff moments
  - IM-GCM for odd nuclei
  - tackle nuclei for which large multi-shell valence-spaces make VS-IMSRG difficult or prohibitive
- Uncertainty Quantification / Sensitivity Analysis
  - need cheap surrogate models (emulators)

# Leveraging Low-Rank Structures

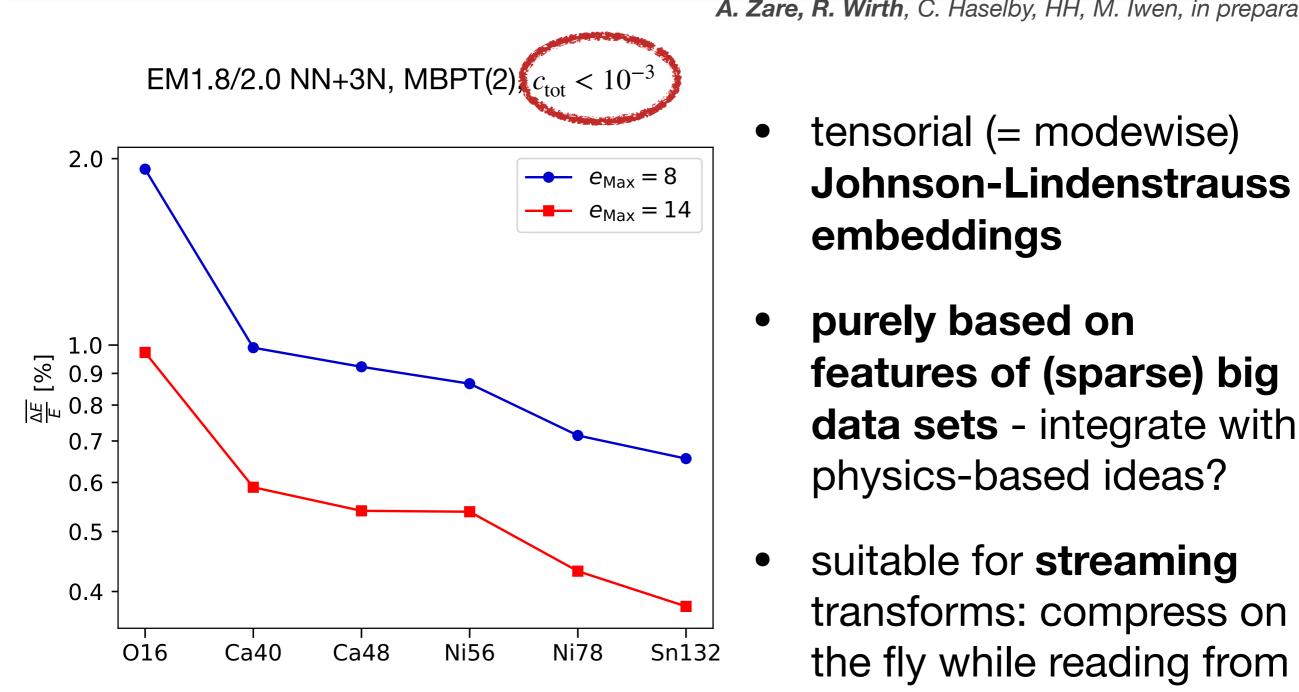




- principal component analysis of chiral interactions
  - free-space SRG effort and storage reduced by several orders of magnitude (but not a major bottleneck anyway)
  - no adverse affect on other (studied) observables
- next: 3N & leverage factorization in many-body calculation

#### **Compression with Random Projections**





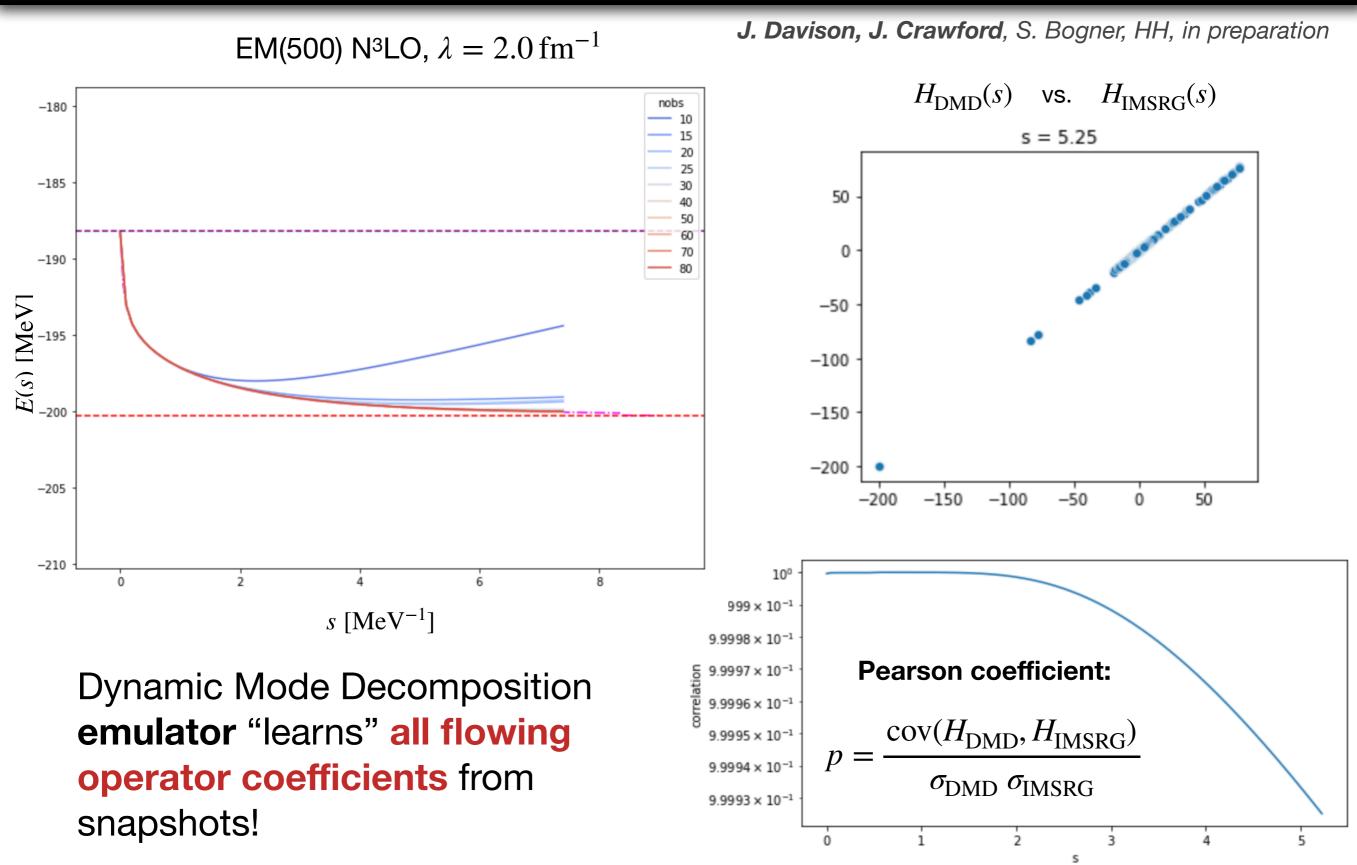
A. Zare, R. Wirth, C. Haselby, HH, M. Iwen, in preparation

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disk

# **Emulating IMSRG Flows**







- predictive ab initio theory with systematic uncertainties & convergence to exact result
- developing new capabilities: spectra, radii, transitions, clustering, bridge to dynamics /reactions...
- scalable techniques and codes: from day-to-day data analysis to leadership calculations

# Acknowledgments



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R. Roth, Ber Papakonstantinou, A. Gi

S. Binder, A. Calci, J. Langhammer<sup>Papenbrock</sup> UT Knoxville &

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- NSCL, Michigan State University R. Roth, T. Mongelli, T. Miyagi, A. Schwenk, A. Tichai TU Darmstadt

C. Haselby, M. Iwen, A. Zare CMSE, Michigan State University

K. Fossez Florida State University

A. Belley, J. D. Holt, P. Navrátil

inou, A. Gunther, S. Reinhardt, G. Hagen, G. Jansen, J. G. Lietz, T. D. Morris, T.

UT Knoxville & Oak Ridge National Laboratory

B. Bally, T. Duguet, M. Frosini, V. Somà CEA Saclay, France

R. J. Furnstahl The Ohio State University

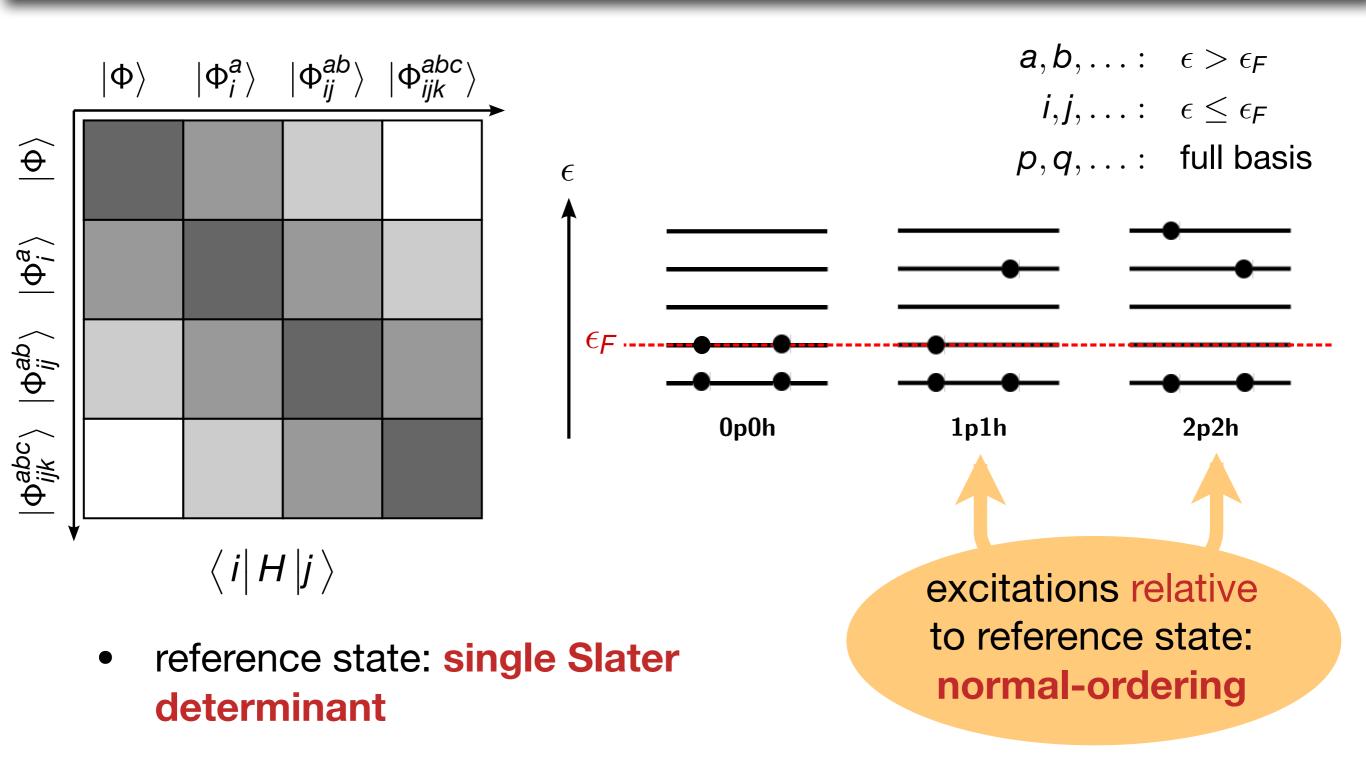
Grants: US Dept. of Energy, Office of Science, Office of Nuclear Physics DE-SC0017887 and DE-SC0018083 (SciDAC-4 NUCLEI Collaboration)



# Supplements

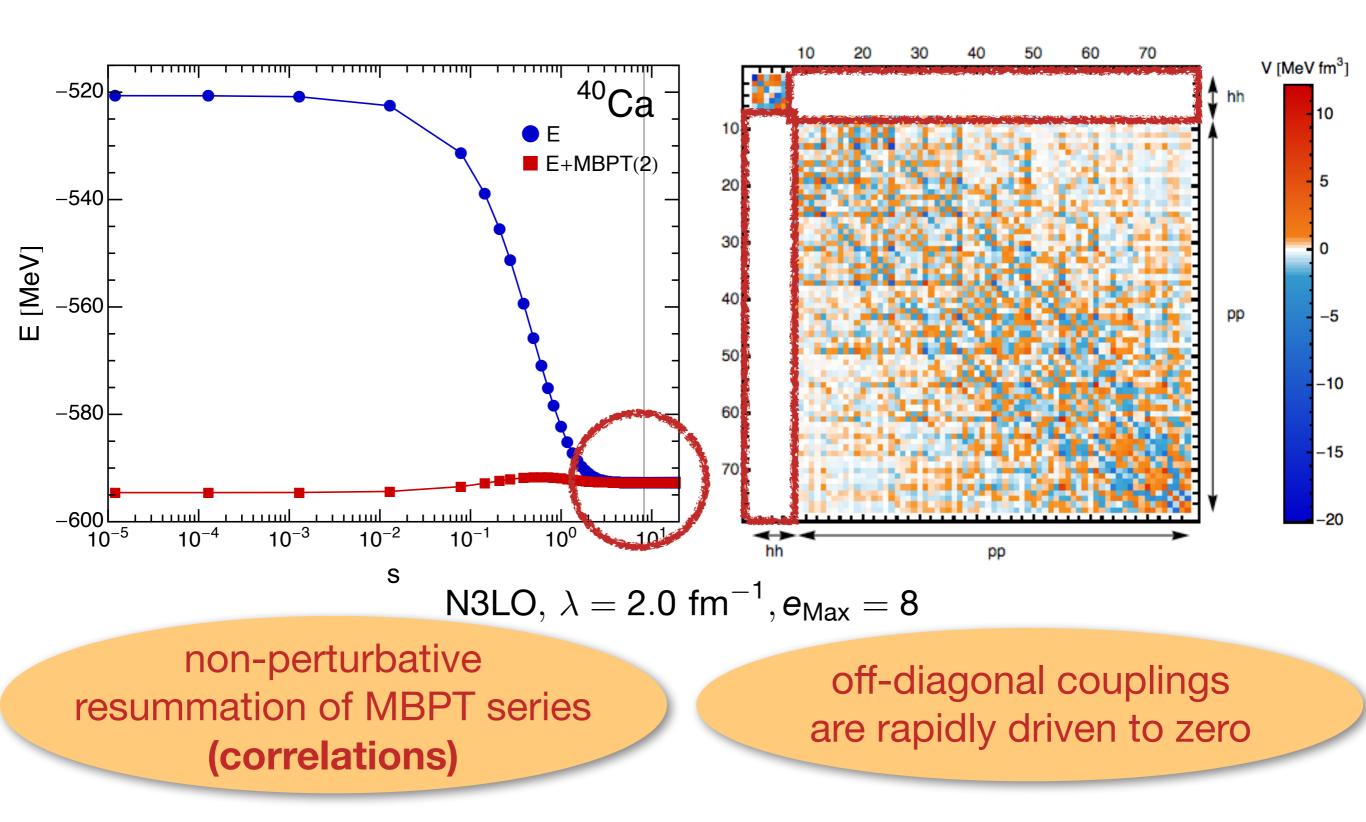
# Transforming the Hamiltonian





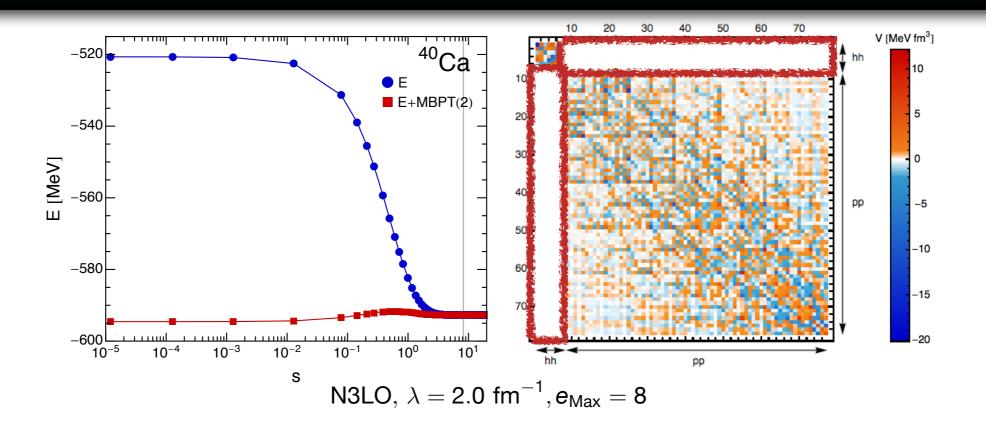
### Decoupling





# Decoupling





absorb correlations into RG-improved Hamiltonian

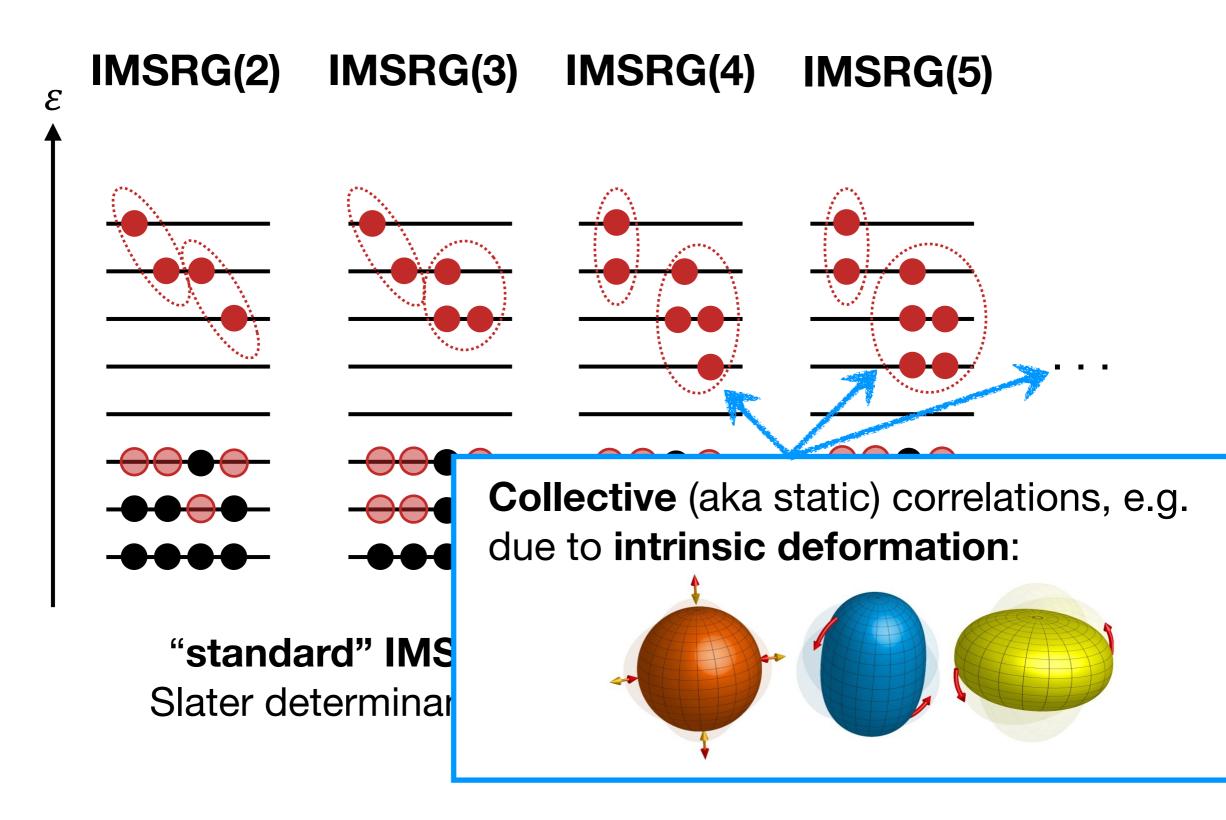
$$U(s)HU^{\dagger}(s)U(s)|\Psi_{n}\rangle = E_{n}U(s)|\Psi_{n}\rangle$$

 reference state is ansatz for transformed, less correlated eigenstate:

$$U(\mathbf{s}) \left| \Psi_n \right\rangle \stackrel{!}{=} \left| \Phi \right\rangle$$

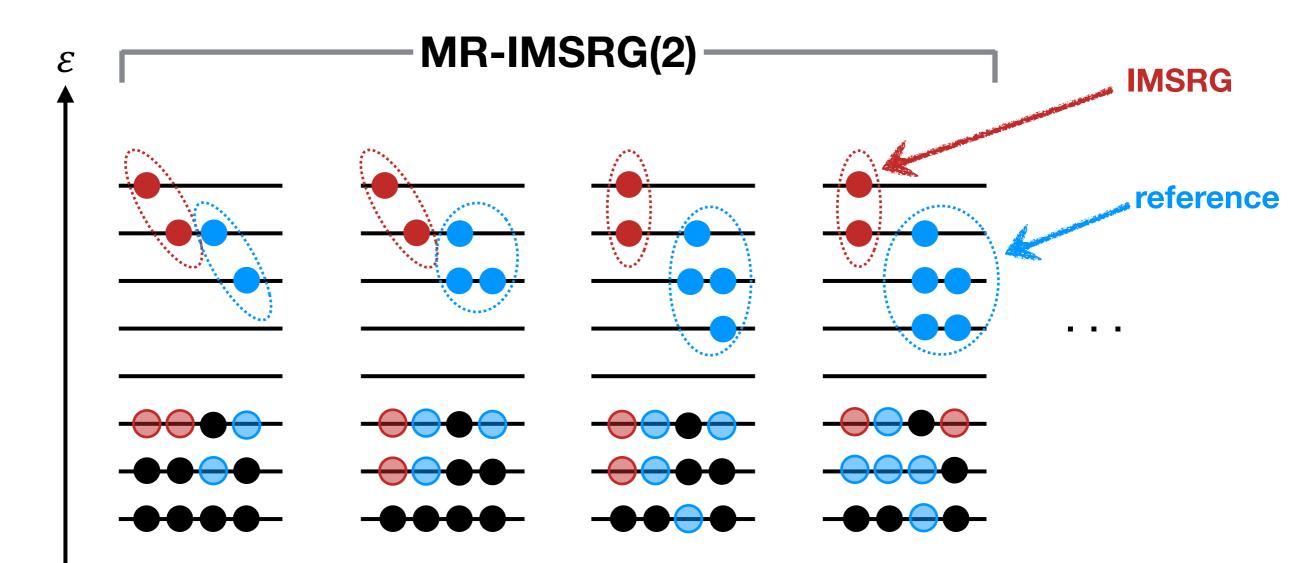
#### **Correlated Reference States**





#### **Correlated Reference States**

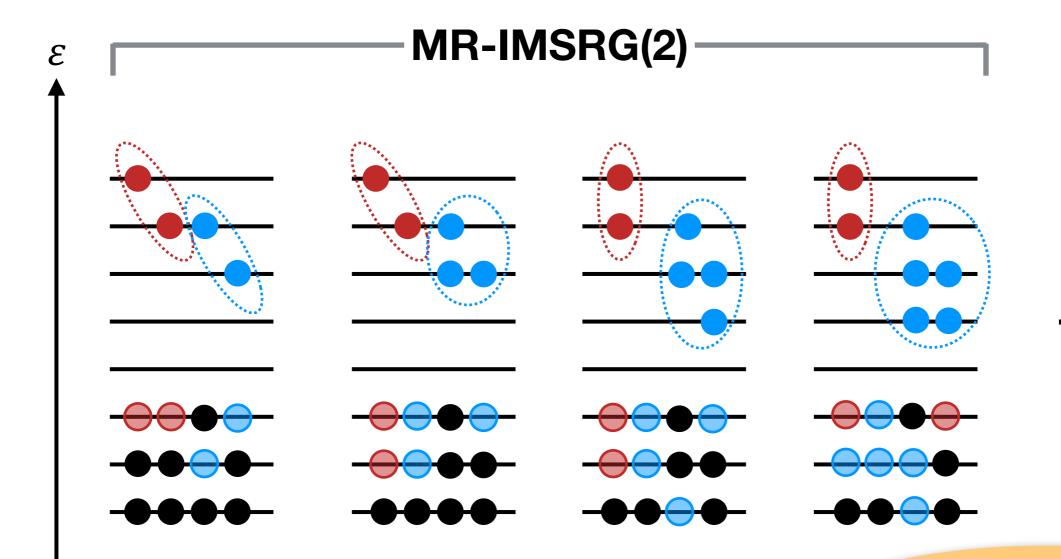




MR-IMSRG: build correlations on top of already correlated state (e.g., from a method that describes static correlation well)

#### **Correlated Reference States**

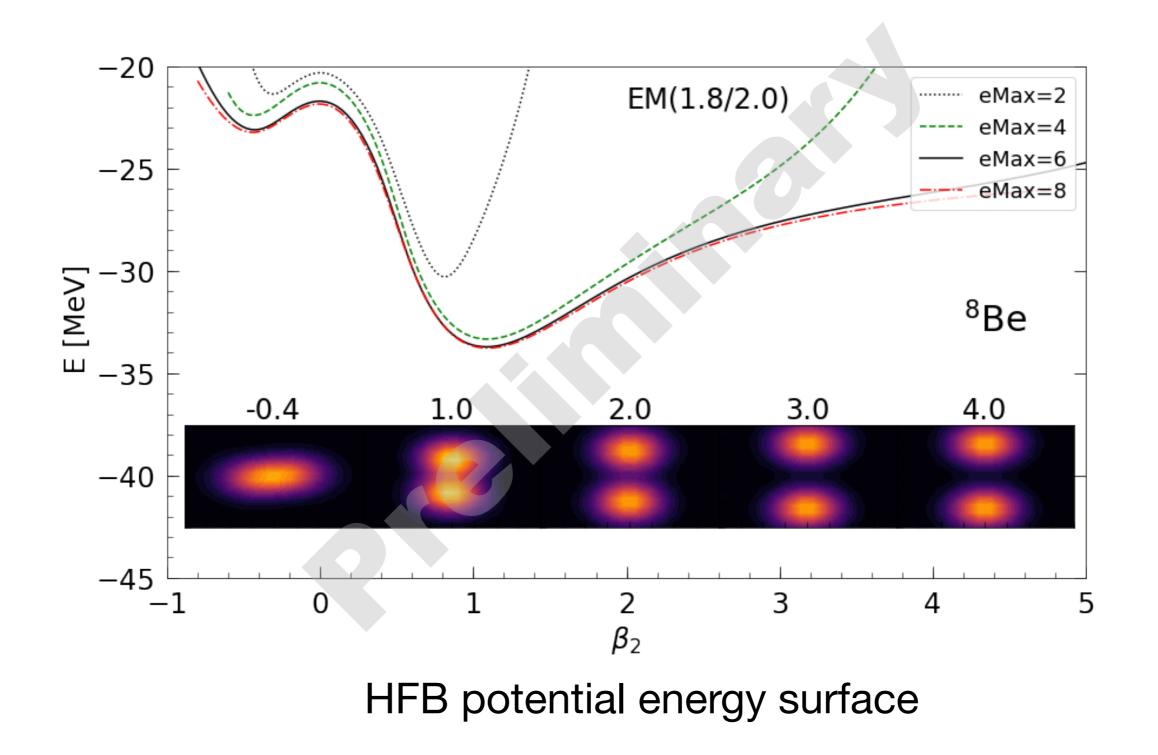




MR-IMSRG: build correlations already correlated state (e.g., fron describes static correlation. use generalized normal ordering with 2B,... densities

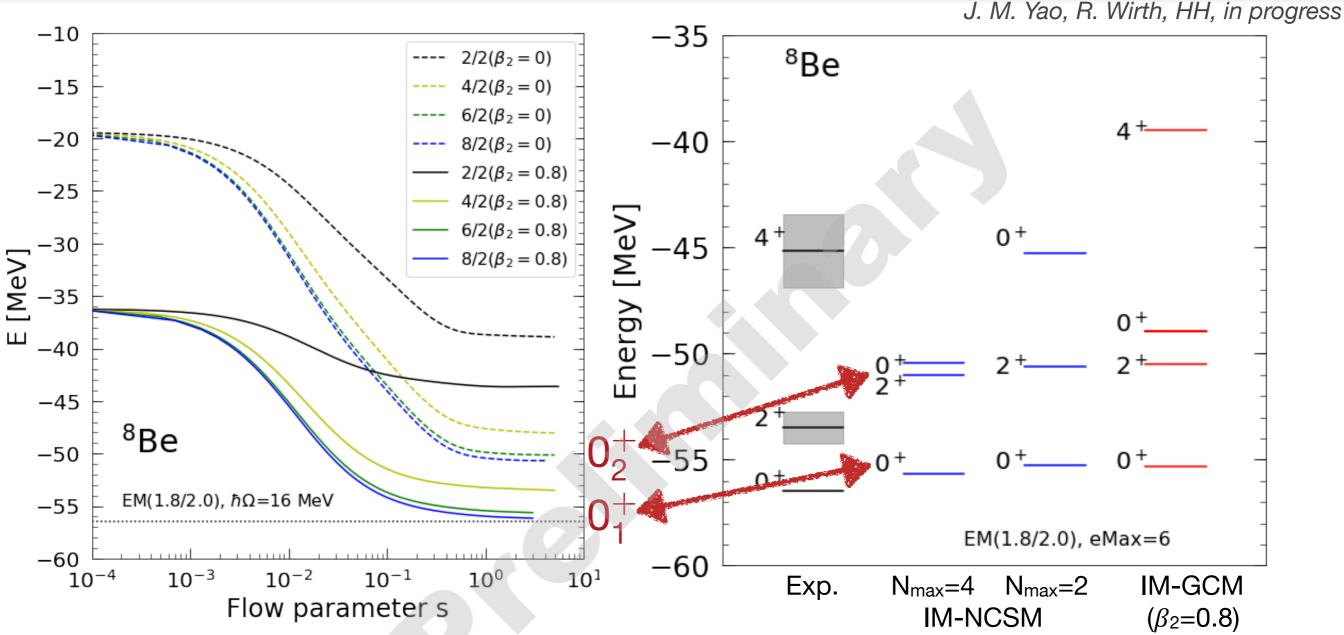


J. M. Yao, R. Wirth, HH, in progress



#### Cluster Structures: <sup>8</sup>Be



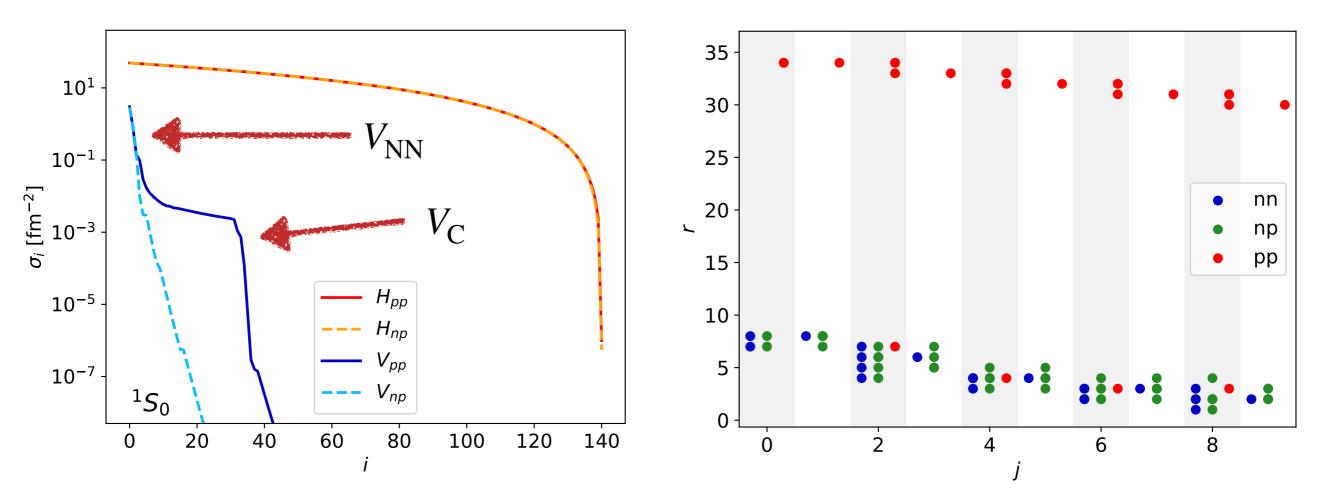


- Spherical and prolate references flow towards different 0+ states.
- Consistent with IM-NCSM:
  - prolate reference: ground state and excited 2+ state
  - spherical reference: first excited 0+

#### Factorized Interactions



B. Zhu, R. Wirth, HH, PRC 104, 044002 (2021)

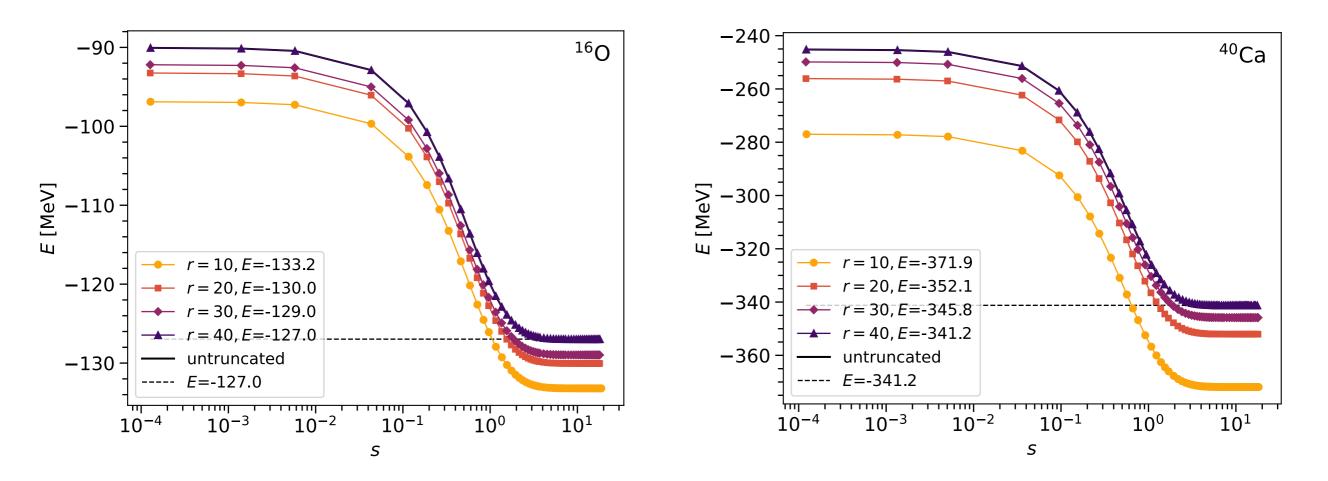


- O(10) operators, O(100) particles, but O(10<sup>8</sup>-10<sup>12</sup>) flow equations, basis dimension... there must be **redundancy**
- NN interaction: 5-10 SVD components (short range)
- Coulomb interaction: less well-behaved, but ~25-30 components sufficient (long range, no explicit scale)

#### Factorized Interactions



B. Zhu, R. Wirth, HH, PRC 104, 044002 (2021)

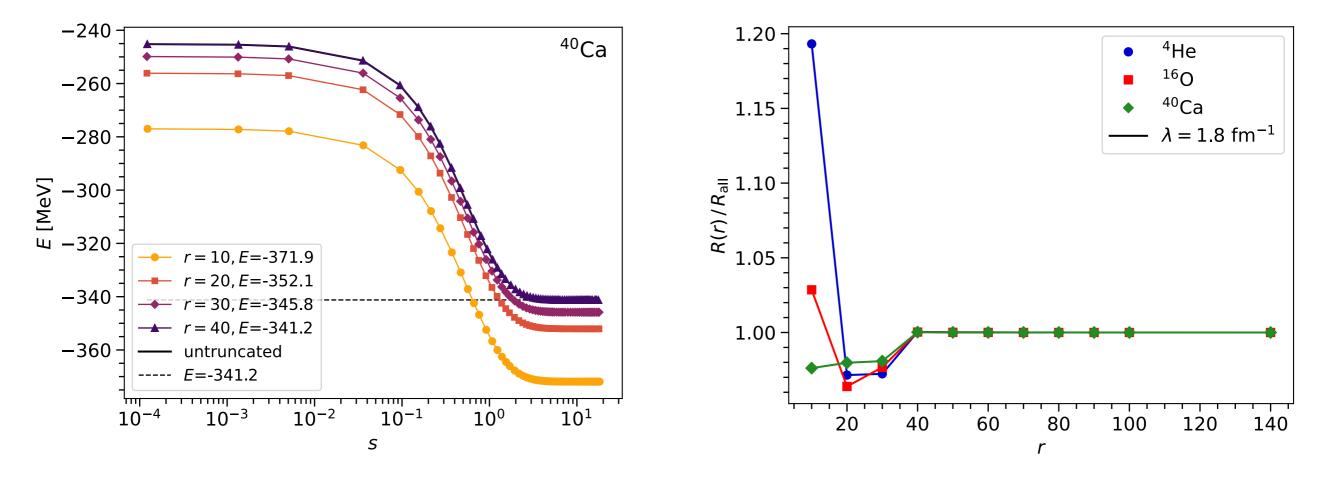


- NN interaction: free-space SRG evolution in component form (IMSRG not yet)
  - (3N interaction added to produce realistic binding / radii)
- free-space SRG effort and storage reduced by several orders of magnitude

#### Factorized Interactions



B. Zhu, R. Wirth, HH, PRC 104, 044002 (2021)



 implementing factorized SRG flow has no adverse affect on other observables / expectation values