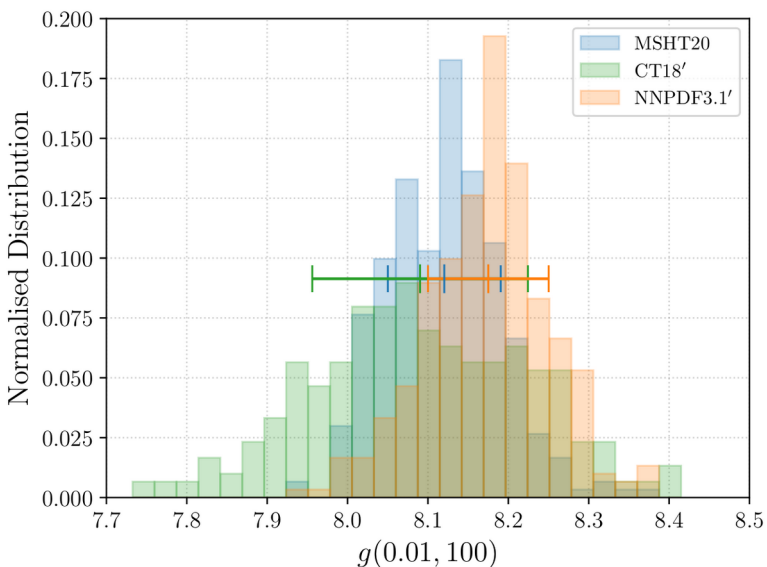
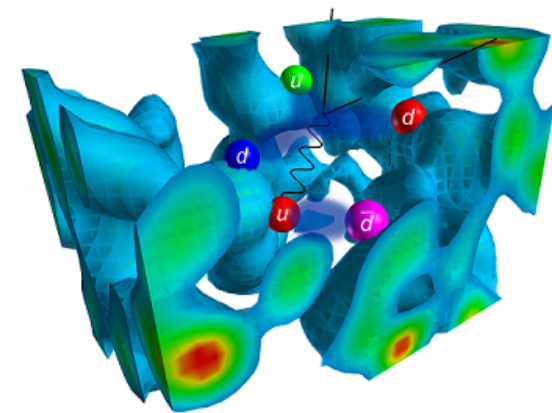
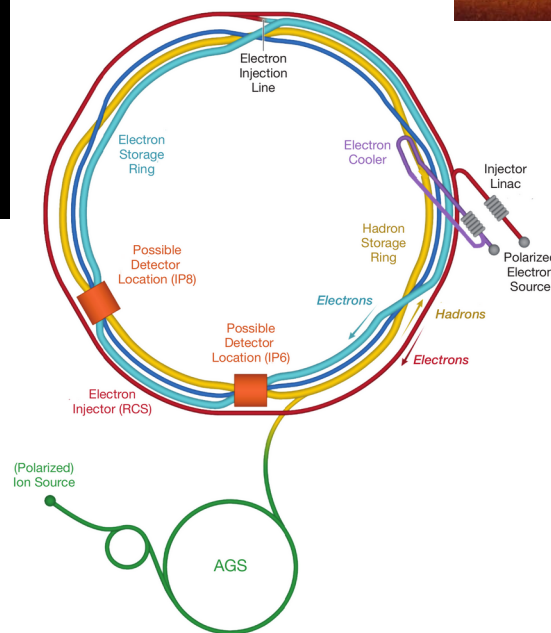
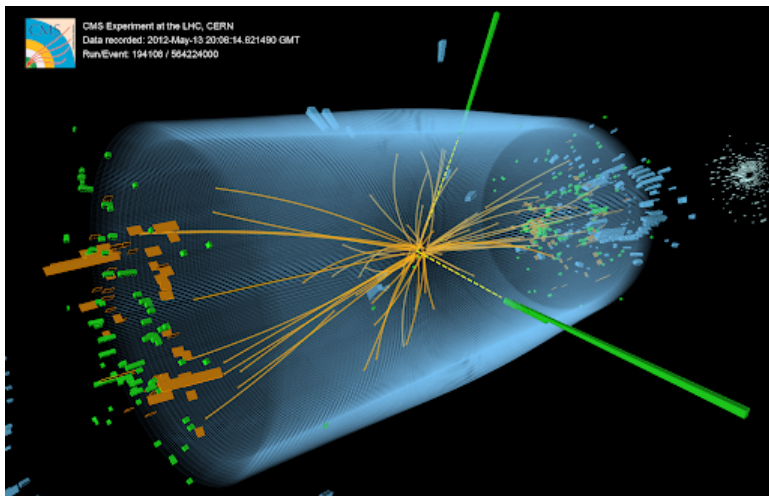


# PDFs from EIC, lattice QCD, and the LHC

Tim Hobbs – Fermilab, IIT

30<sup>th</sup> August 2022

“or, making data work for you”



# this talk: PDF activity key for 2 core needs in fundamental QCD

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## 1: LHC-based SM tests **limited by (incomplete) proton structure info**

Boughezal, ...

→ many **standard-candle HEP measurements PDF-limited**

Kaazde, Kotwal, ...

→ taming PDF dependence: knowledge of hard-to-access phase-space regions  
this talk: high  $x$

→ **PDF studies vital to nonpert. QCD**, mapping hadron structure

Metz, Sato, ...

## 2: parallel developments likely to impact both areas

Wagman, ...

→ lattice QCD: new opportunities to constrain inaccessible PDF behavior

→ EIC program, preparations have substantial PDF implications

Arratia, ...

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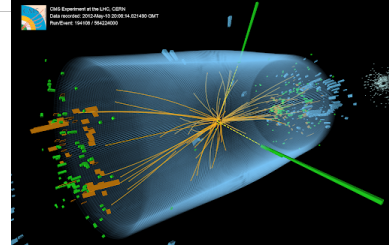
highlight through:

i current status of PDFs; ii lattice QCD possibilities

iii EIC projections; iv conclusion(s)

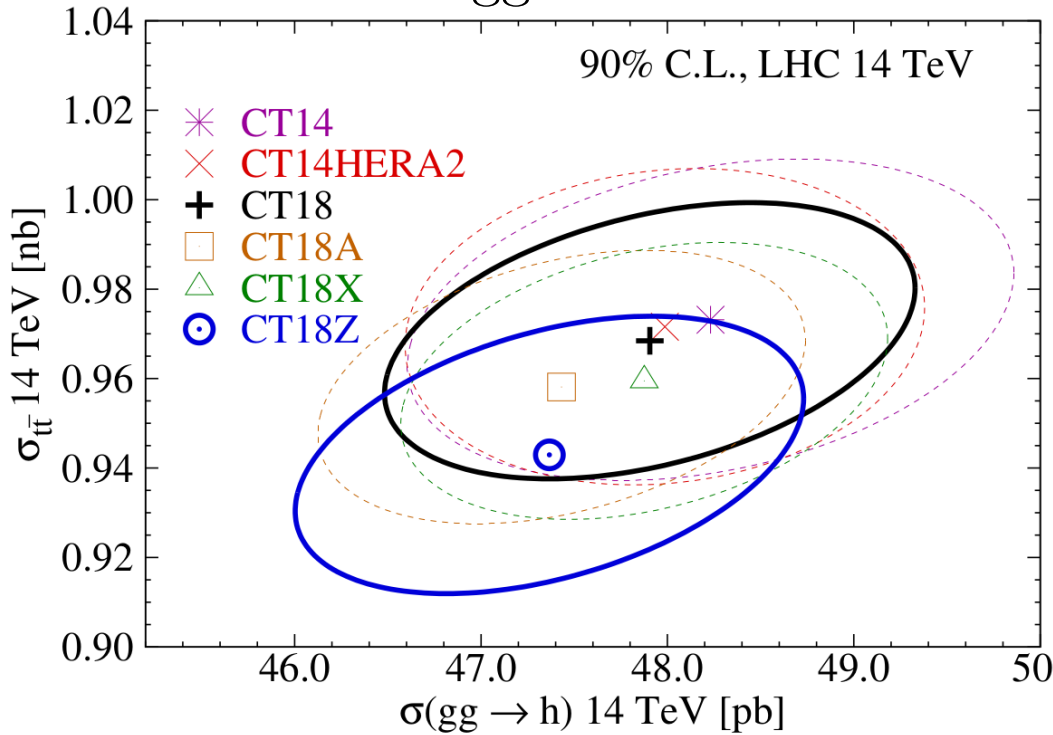
# i SM tests at LHC require high theory accuracy; precision

- from NNLO analyses, state-of-the-art predictions for fundamental LHC observables  $\rightarrow$  e.g., **total cross sections at 14 TeV**

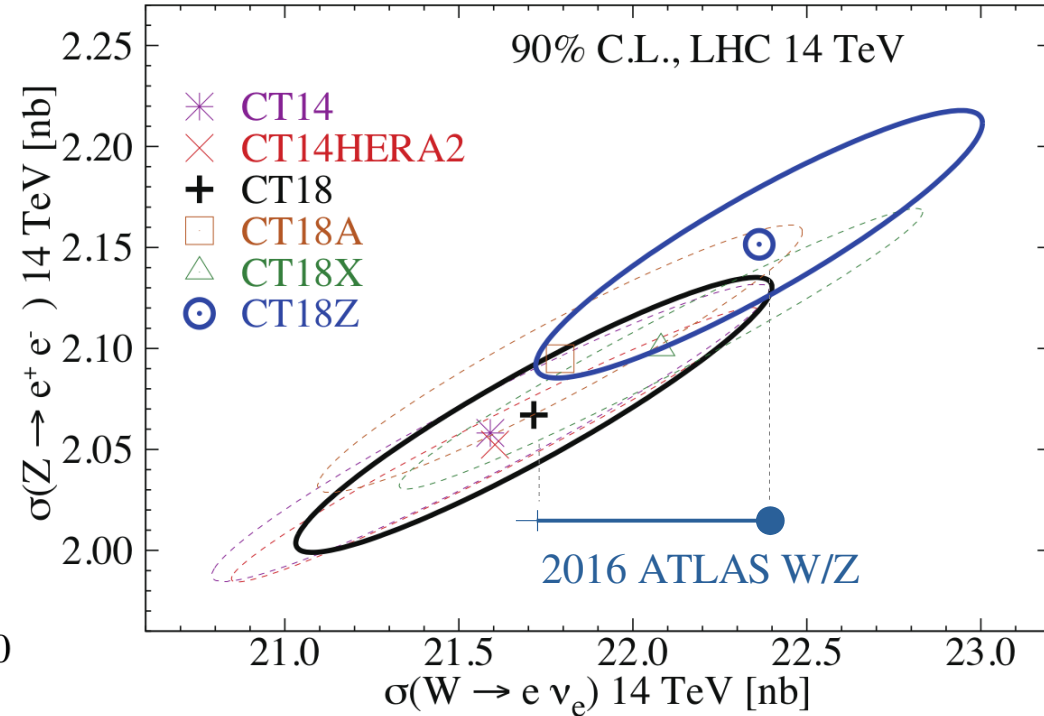


CT18 NNLO, PRD **103** (2021) 1.

### Higgs and $t\bar{t}$



### W and Z



Higgs, NNLO QCD: iHixs v1.3

$$\mu_R = \mu_F = m_t; m_{W,Z}; m_H$$

NNLO QCD: Vrap v0.9

$t\bar{t}$ , NNLO+NNLL: Top++ v2.0

- significant PDF-driven uncertainties; also, systematic effects: W cross sections sensitive to inclusion of 2016 7 TeV ATLAS inclusive W/Z data

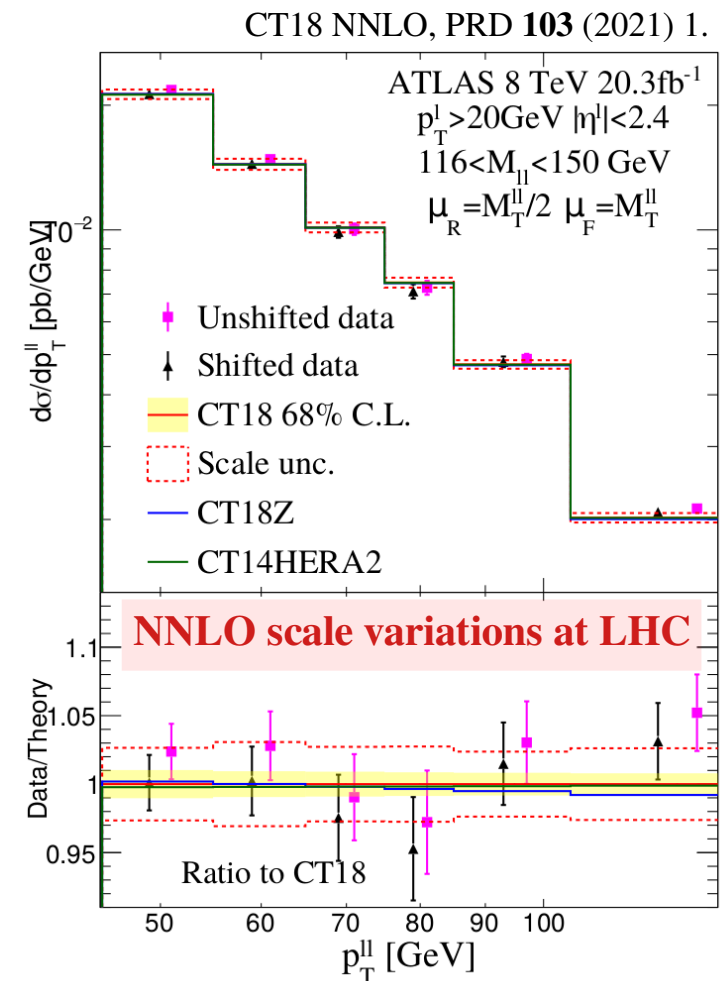
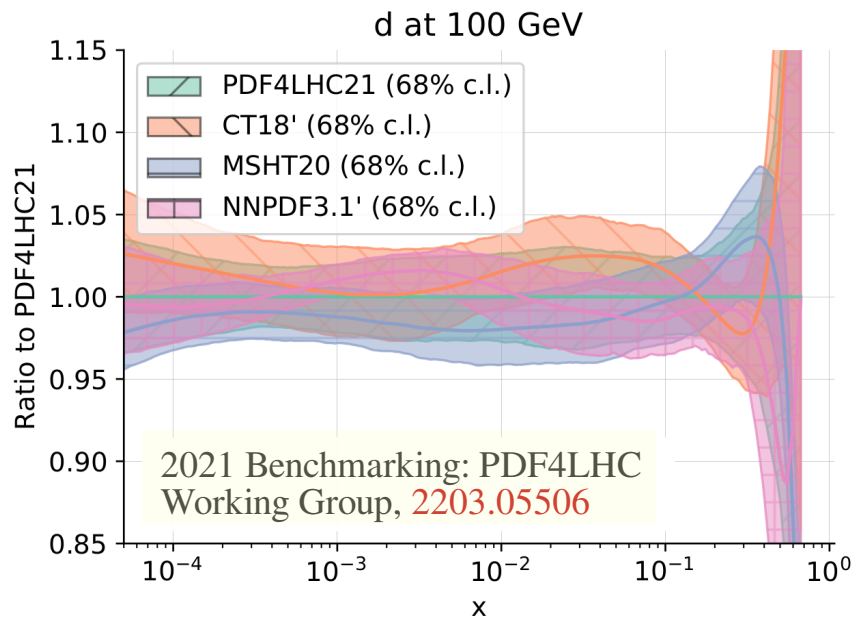
# PDFs critical to next-generation precision

Snowmass21, Amoroso et al.: [2203.13923](#)

→ driven by marriage of high-energy data; **latest theory**

modern standard: **NNLO**

$$\sigma(AB \rightarrow W/Z+X) = \sum_n \alpha_s^n \sum_{a,b} \int dx_a dx_b f_{a/A}(x_a, \mu^2) \times \hat{\sigma}_{ab \rightarrow W/Z+X}^{(n)}(\hat{s}, \mu^2) f_{b/B}(x_b, \mu^2)$$



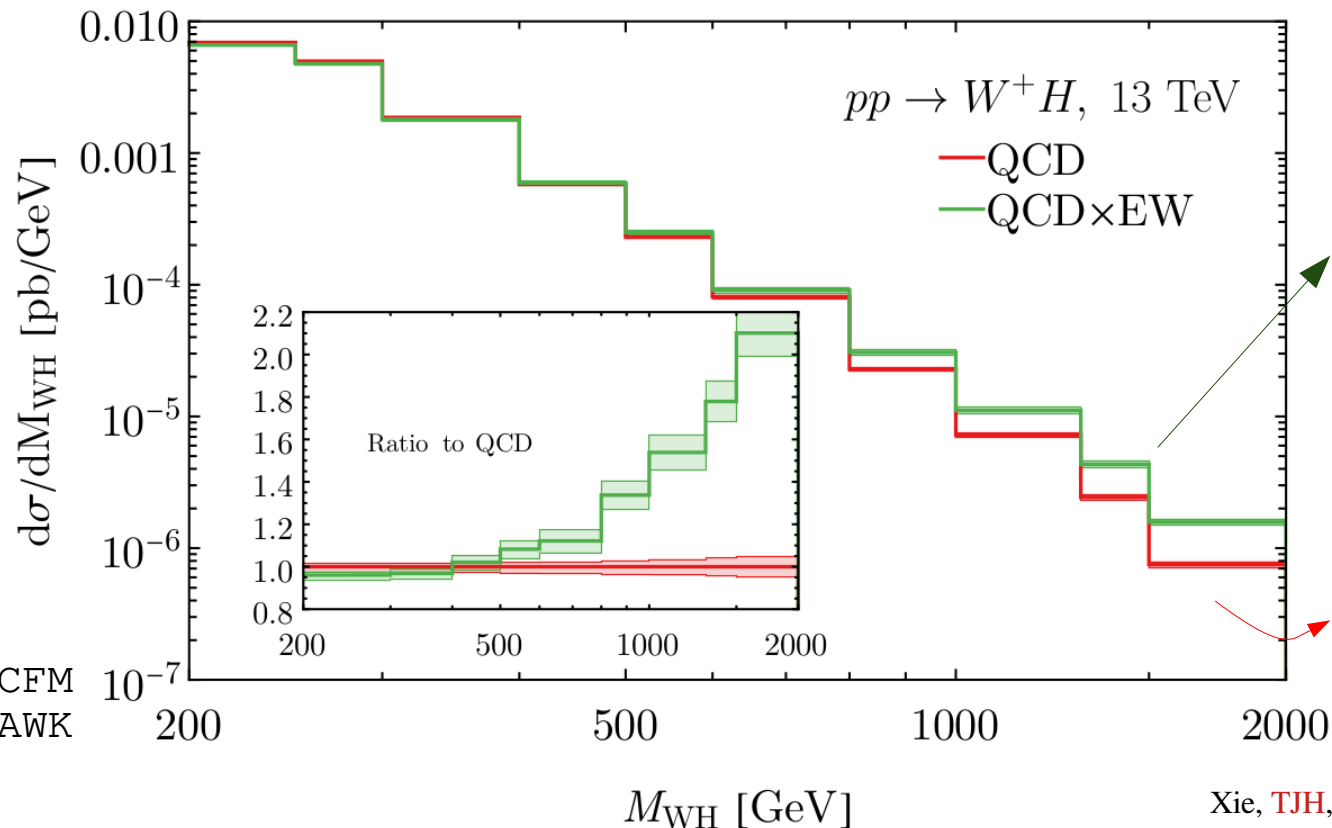
▪ periodic benchmarking (PDF4LHC21) valuable to cross-check treatment of data

→ intercompare theory choices; understand methodological dependence

i

# BSM searches in HEP also require EW theory accuracy

- non-standard physics may appear in tails of rapidity, inv. mass distributions
- important for high-energy LHC processes: *e.g.*, 13 TeV  $W+H$  production:



Xie, TJH, Hou, Schmidt, Yan, Yuan: PRD105 (2022) 5, 054006.

- TeV-scale NLO EW corrections dominated (60%) by single-photon (PDF) contributions

→ requires **delicate** treatment along with QCD perturbative effects

# i electroweak precision: photon, high- $x$ PDFs; nonpert. QCD

- at  $\mathcal{O}(\alpha_s^2)$  accuracy, EW corrections and explicit  $\gamma(x, \mu^2)$  needed

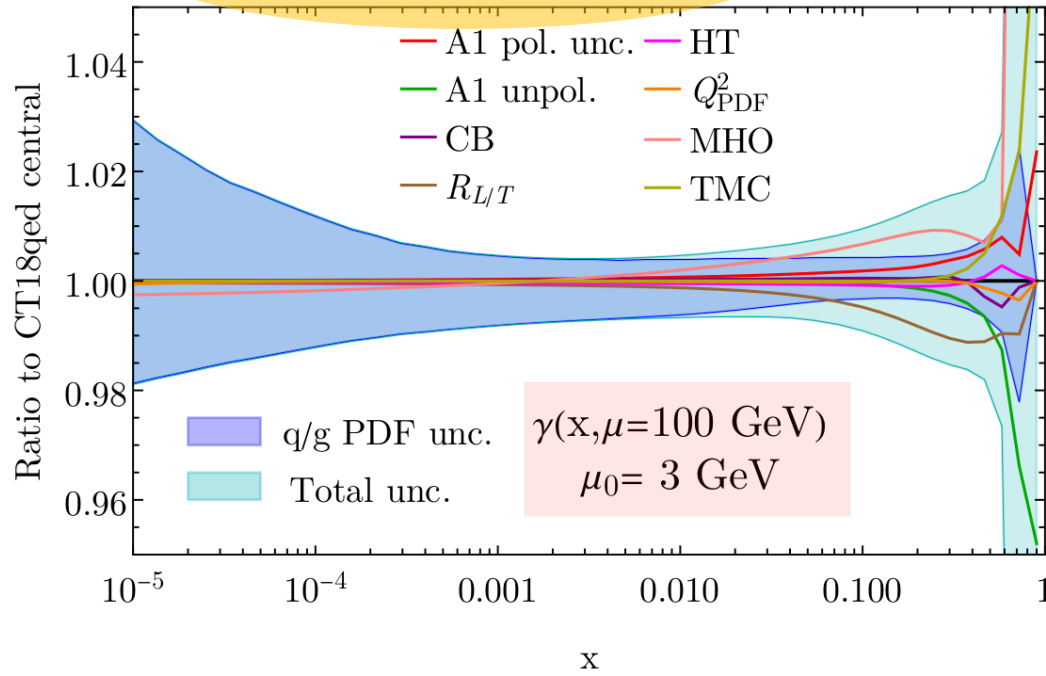
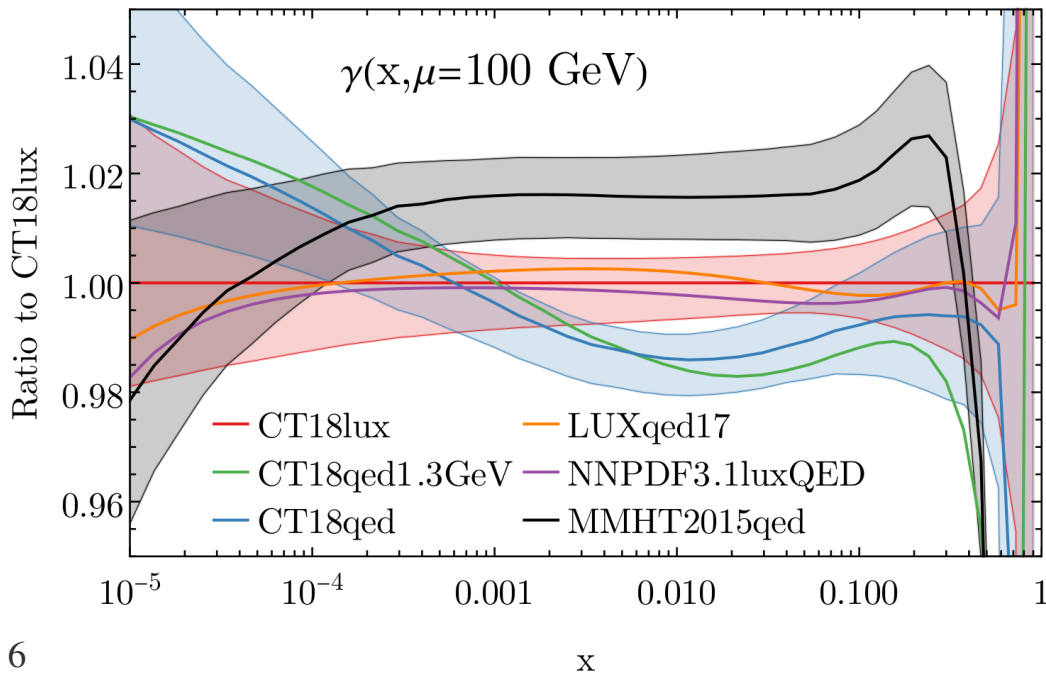
Xie, TJH, Hou, Schmidt, Yan, Yuan: PRD105 (2022) 5, 054006.

- following CT14QED, CT18QED now interfaces LUX formalism

$$x\gamma(x, \mu^2) = \frac{1}{2\pi\alpha(\mu^2)} \int_x^1 \frac{z}{z} \left\{ \int_{\frac{x^2 m_p^2}{1-z}}^{\frac{\mu^2}{1-z}} \frac{Q^2}{Q^2} \alpha_{\text{ph}}^2(-Q^2) \left[ \left( zp_{\gamma q}(z) + \frac{2x^2 m_p^2}{Q^2} \right) F_2(x/z, Q^2) - z^2 F_L(x/z, Q^2) \right] - \alpha^2(\mu^2) z^2 F_2(x/z, \mu^2) \right\} + \mathcal{O}(\alpha^2, \alpha\alpha_s)$$

- depends on nonperturbative inputs [kinematical cuts alone can't avoid this]

[large- $x$  physics...]



i

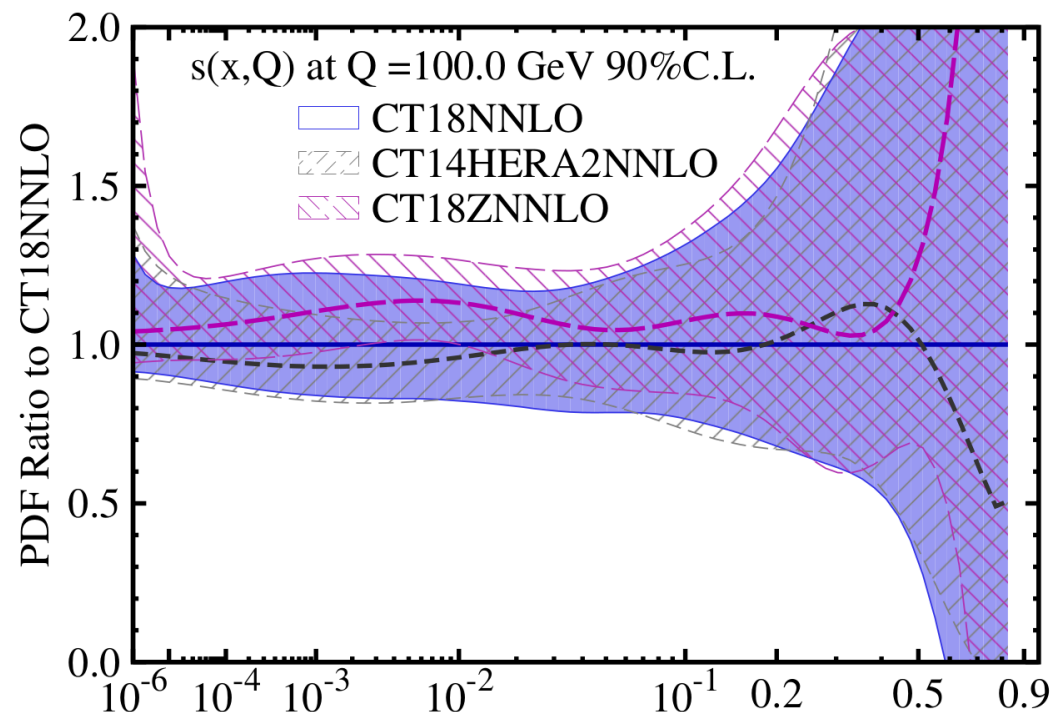
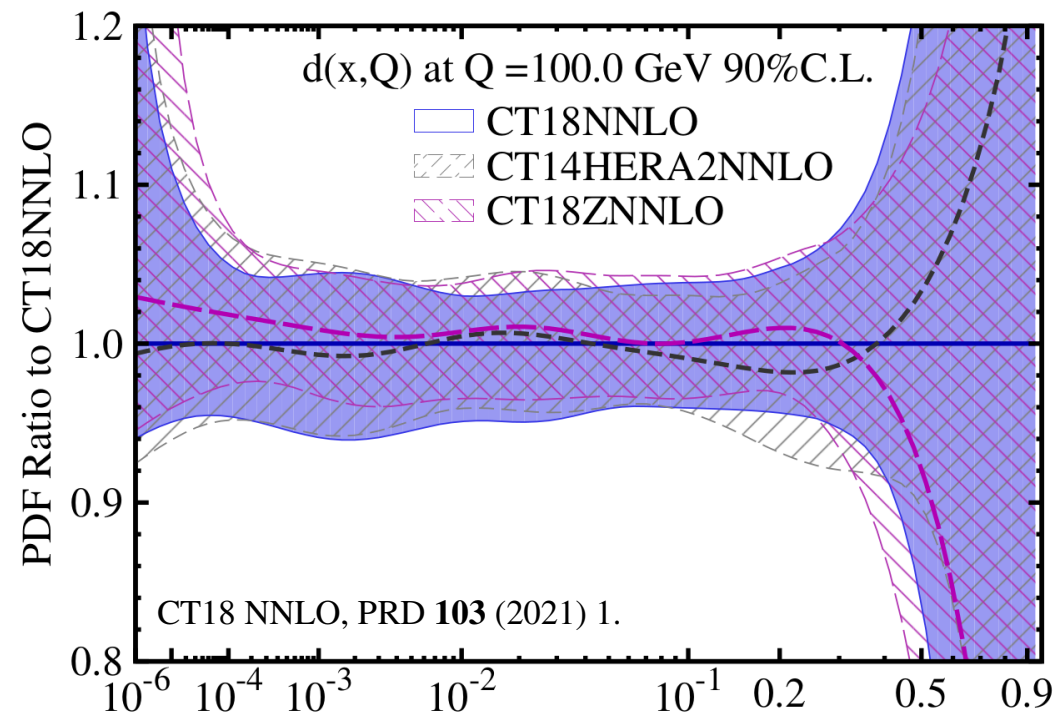
# high- $x$ PDFs remain dominated by large uncertainties

- PDF (Hessian) uncertainties enlarge dramatically in high- $x$  limit

→ limited data

→ extrapolation

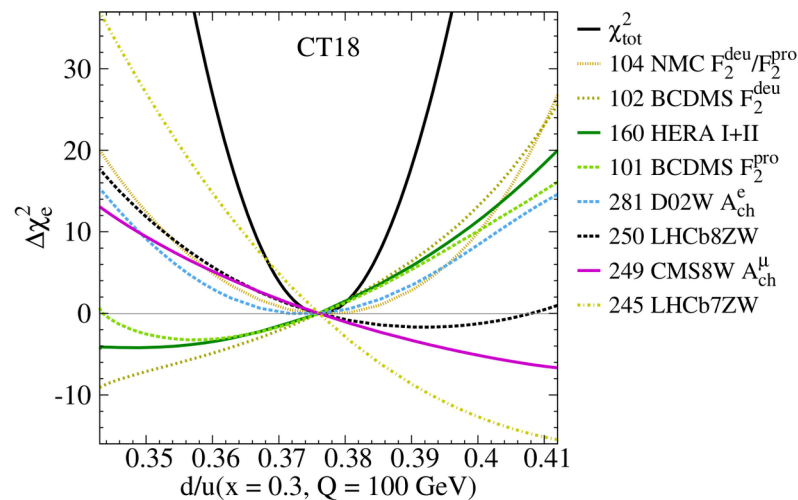
→ data tensions



- competing pulls of fitted data at high- $x$  also restrict precision; *e.g.*,

→ BCDMS,  $F_2^d$

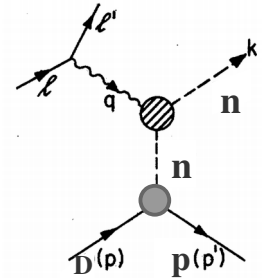
→ LHCb,  $W/Z$  7 TeV



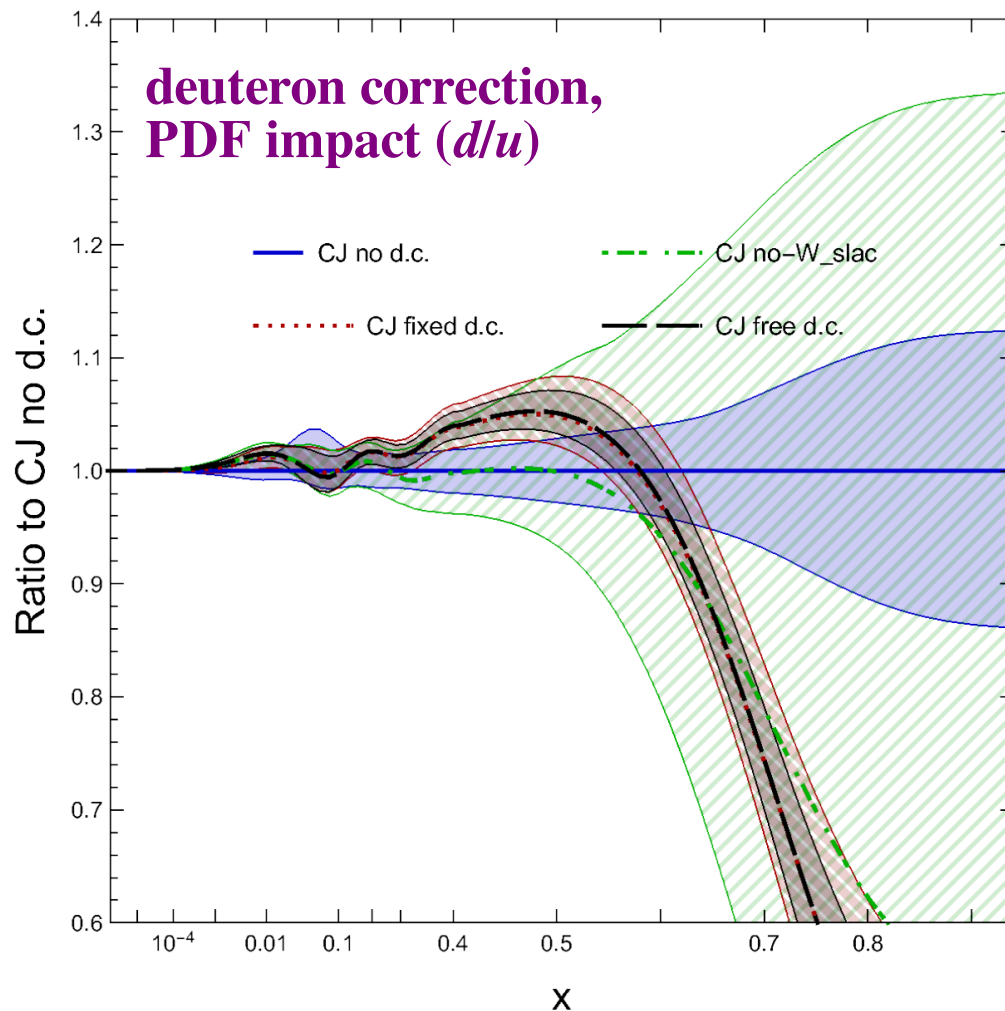
# nuclear corrections: high- $x$ PDFs and flavor separation

- $d$ -PDF information from deuteron scattering; nuclear corrections relevant

$$f^d(x, Q^2) = \int \frac{dz}{z} \int dp_N^2 \mathcal{S}^{N/d}(z, p_N^2) \tilde{f}^N(x/z, p_N^2, Q^2)$$



$d(x, Q)/u(x, Q)$  at  $Q=2.0$  GeV,  $T^2 = 10$



Accardi, TJH, Jing, Nadolsky: EPJC81 (2021) 7, 603.

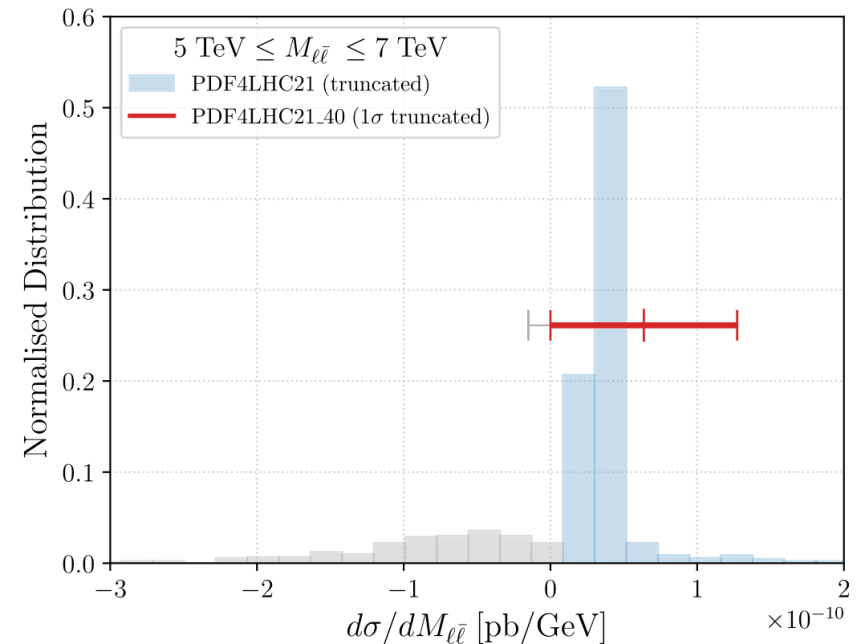
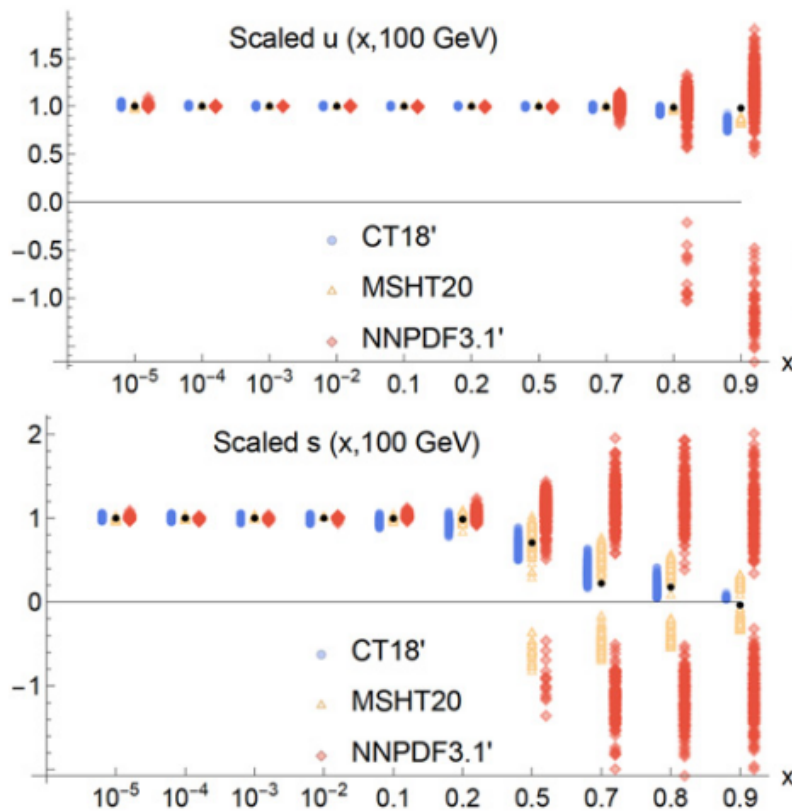
- corrections are generally ~percent-level, but can become larger, especially at high  $x$ 
  - also, PDF correlations with gluon, other flavors
- impacts LHC observables; necessary for high precision
- analogous situation for **heavy-nuclear effects** in  $\nu A$  scattering → main (inclusive) source of **strangeness** info.



- MC sampling of high- $x$  PDFs can sometimes produce irregularities

→ *e.g.*, positive-definiteness not always guaranteed for  $x \rightarrow 1$

→ can produce subtle but non-negligible phenomenological consequences:

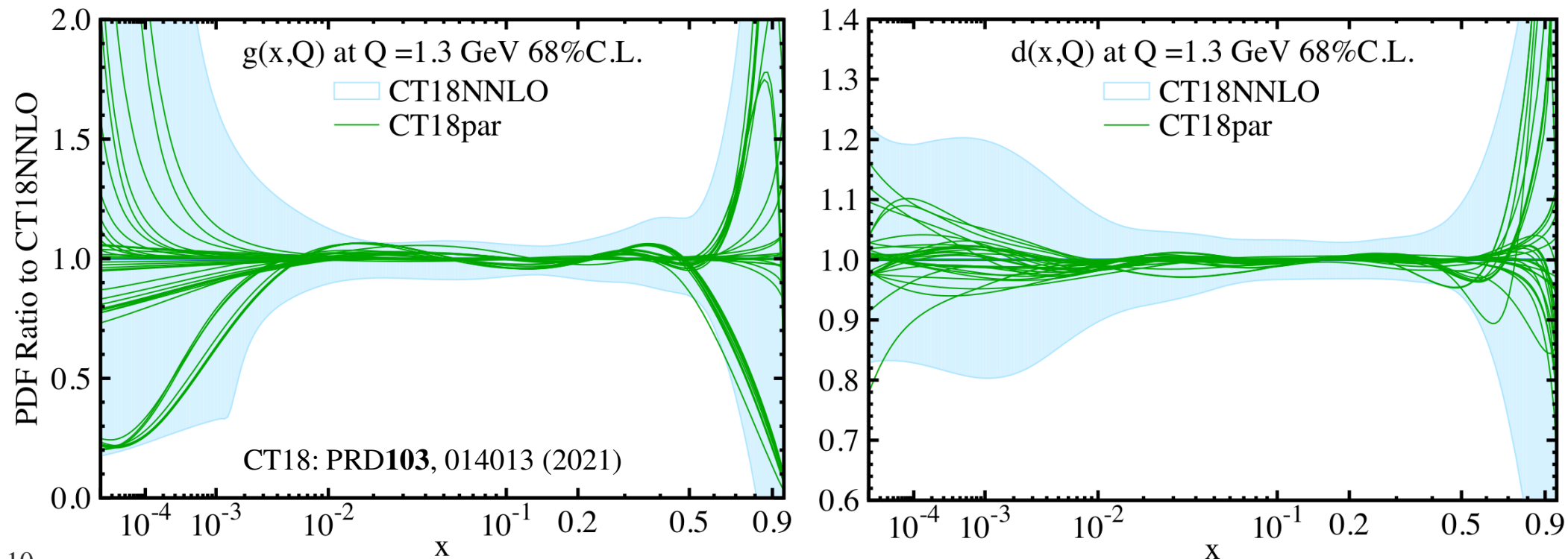


- strong need for high- $x$  sensitive data: JLab12 [24]; (HL-)EIC; FASER $\nu$

# PDF uncertainties: parametrization dependence

- initial PDFs still not generally calculable through rigorous QCD at  $Q = Q_0 = m_c$  (more on this shortly...)
  - subject to complex nonperturbative dynamics
  - practice agnosticism w.r.t. initial parametrization (some guidance from QCD, QCD-inspired models)
  - explore model uncertainty with many forms

parametrization uncertainties largest in extrapolated regions

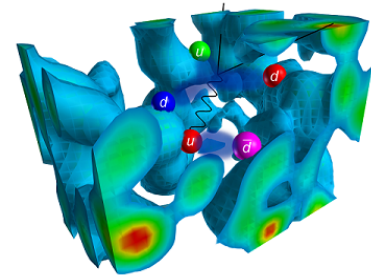


# but, what about *ab initio* QCD methods (lattice QCD)?

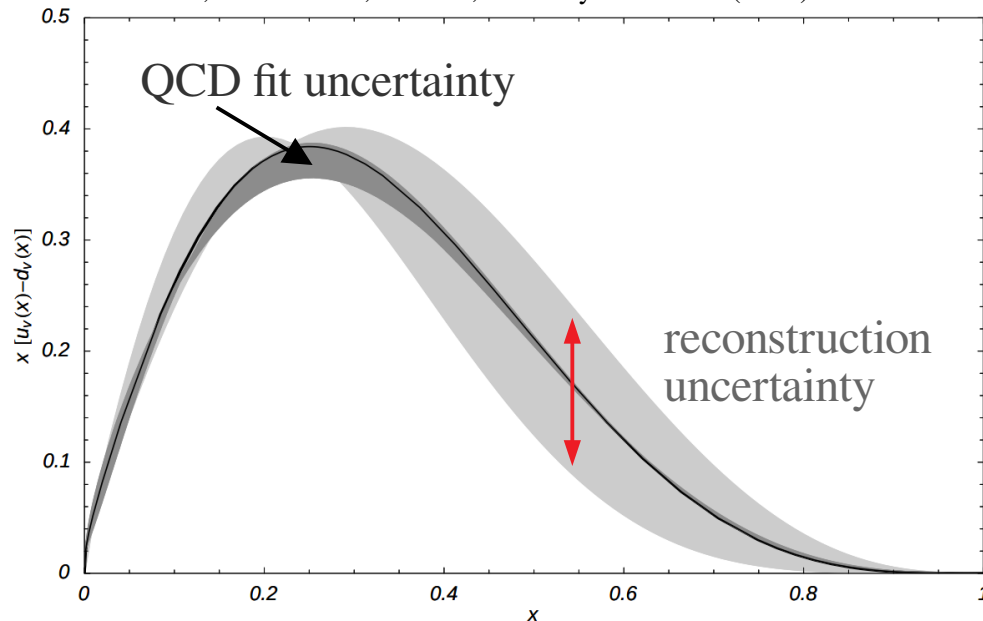
- PDF (Mellin) moments from lattice: **higher moments**  $\leftrightarrow$  **higher cov. derivatives**

$$\frac{1}{2} \sum_s \langle p, s | \mathcal{O}_{\{\mu_1, \dots, \mu_{n+1}\}}^q | p, s \rangle = 2v_q^{n+1} [p_{\mu_1} \cdots p_{\mu_{n+1}} - \text{traces}]$$

$$v_q^{n+1}(Q) = \int_0^1 dx x^n q(x, Q)$$



Detmold, Melnitchouk, Thomas, Mod.Phys.Lett. **A18** (2003) 2681.

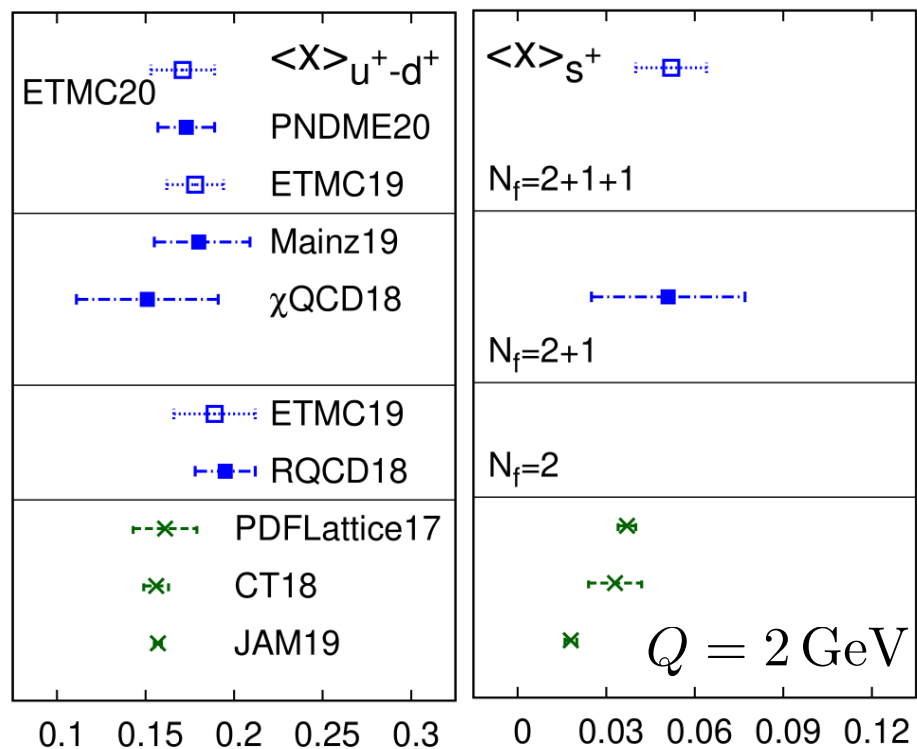


- higher moments sensitive to high- $x$  PDFs
- historically, efforts to reconstruct PDFs from lattice-calculable moments (large uncertainties)

more recently

- $\rightarrow$  technical advances: more (and better) Mellin moment determinations
- $\rightarrow$  formal advances: quasi- and pseudo-PDFs

Moment	Collaboration	Reference	$N_f$	DE	CE	FV	RE	ES	Value
$\langle x \rangle_{u^+ - d^+}$	ETMC 20	[235]	2+1+1	■	★	○	★	★	0.171(18)
	PNDME 20	[236]	2+1+1	★	★	★	★	★	0.173(14)(07)
	ETMC 19	[237]	2+1+1	■	★	○	★	★	0.178(16)
	Mainz 19	[238]	2+1	★	○	★	★	★	0.180(25)( $^{+14}_{-6}$ )
	$\chi$ QCD 18	[239]	2+1	○	★	○	★	★	0.151(28)(29)
	ETMC 19	[237]	2	■	★	○	★	★	0.189(23)
	RQCD 18	[240]	2	★	★	○	★	★	0.195(07)(15)
$\langle x \rangle_{s^+}$	ETMC 20	[235]	2+1+1	■	★	○	★	★	0.052(12)
	$\chi$ QCD 18	[239]	2+1	○	★	○	★	★	0.051(26)(5)



- depending on flavor, order – lattice moments have varying status (above, FLAG evaluations)
  - e.g., the first isovector moment has been computed by numerous groups
- systematic lattice effects are similarly widely varied
- lattice precision lags QCD fits, but **higher moments would be informative**
- also, novel lattice methods available →

quasi-PDFs allow access to  $x$  dependence

- boost-dependent **quasi-PDF** can be matched to light-front PDF, up to power-suppressed corrections

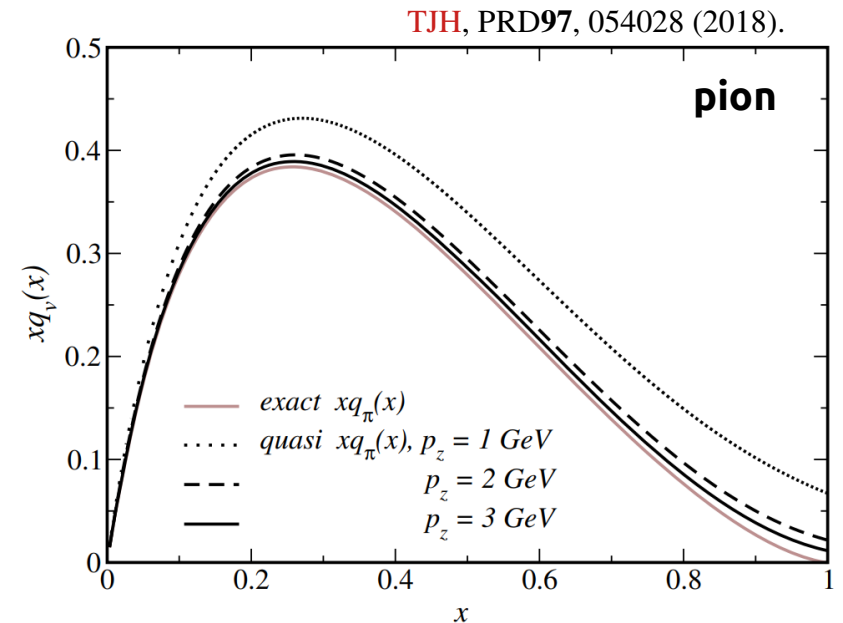
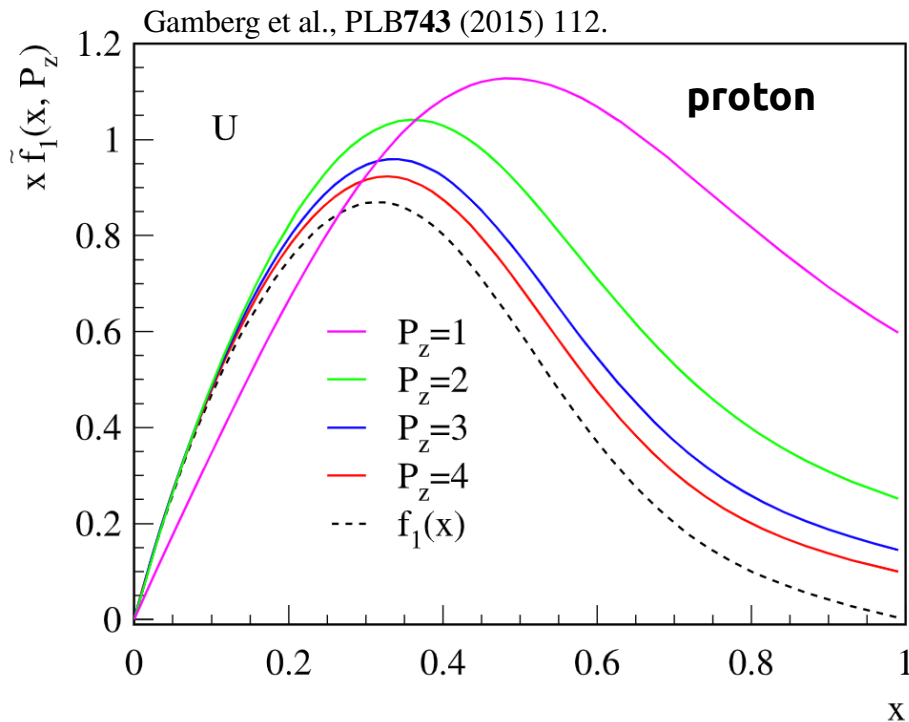
Ji, PRL**110**, 262002 (2013).

$$\sim \langle P | \bar{\psi} \gamma^{z,t} \psi | P \rangle$$

$$\sim \langle P | \bar{\psi} \gamma^+ \psi | P \rangle$$

$$\tilde{q}(x, P_z, \tilde{\mu}) = \int dy Z \left( \frac{x}{y}, \frac{\Lambda}{P_z}, \frac{\mu}{P_z} \right) q(y, \mu) + \mathcal{O} \left( \frac{\Lambda_{\text{QCD}}^2}{P_z^2}, \frac{M^2}{P_z^2} \right)$$

- yields  $x$ -dependent PDF information; limited by knowledge of **perturbative matching**,  $P_z$  dependence



model calculations: qPDFs converge to exact for  $P_z \rightarrow \infty$

- ultimately, the  $x$ - and  $P_z$  dependence of the qPDFs are informative of **hadronic wave functions**

ii

# lattice QCD output: basis for PDF-lattice synergy

there are (and will be) important synergies between PDF fitting and lattice QCD

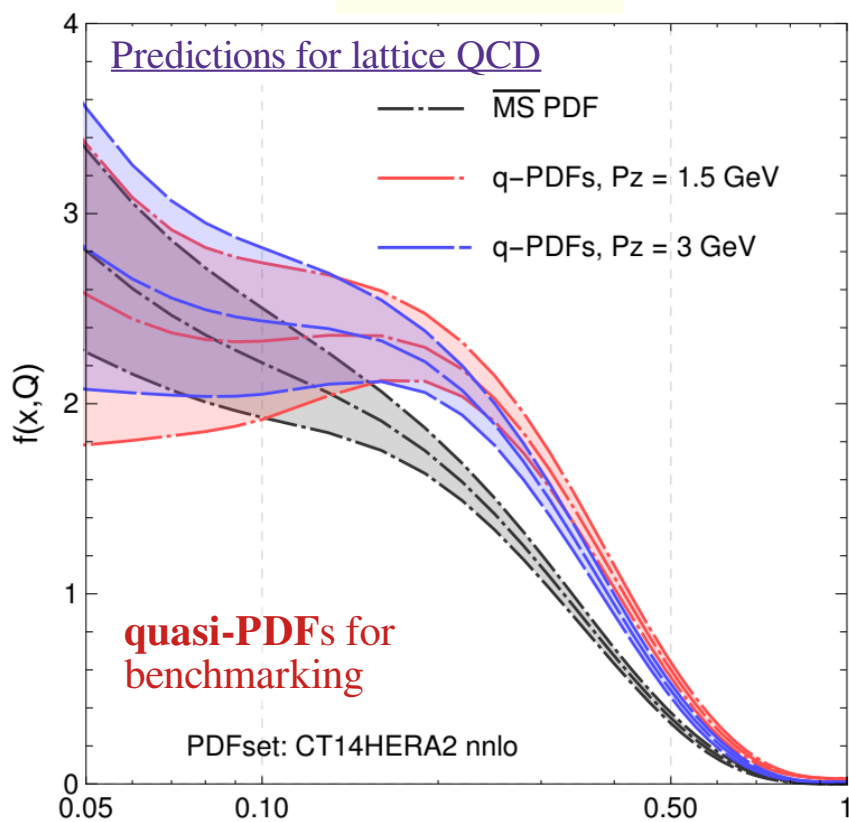
[overlaps with EIC; vDIS; LHC]

- PDF fits **benchmark** pQCD matching; lattice output can **constrain** QCD fits

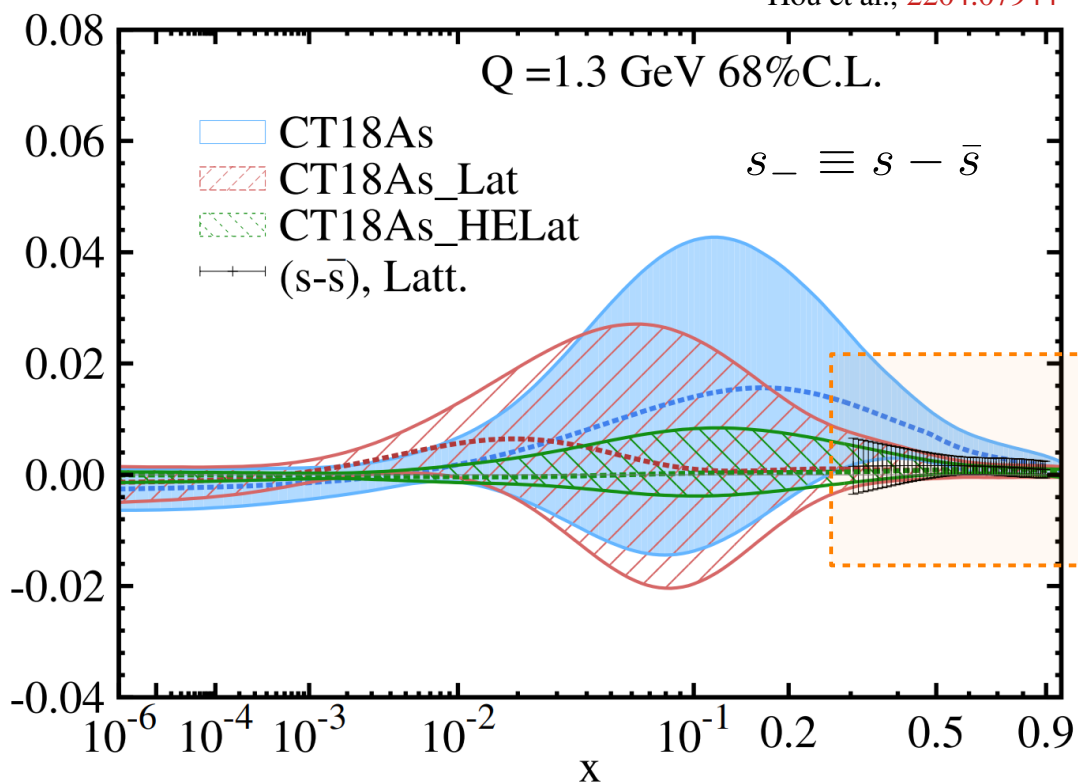
- lattice data can potentially inform high- $x$  behavior of quark sea

TJH, Wang, Nadolsky, Olness, PRD**100** (2019) 9, 094040.

u-d at  $\mu_F = 3\text{GeV}$



Hou et al., 2204.07944

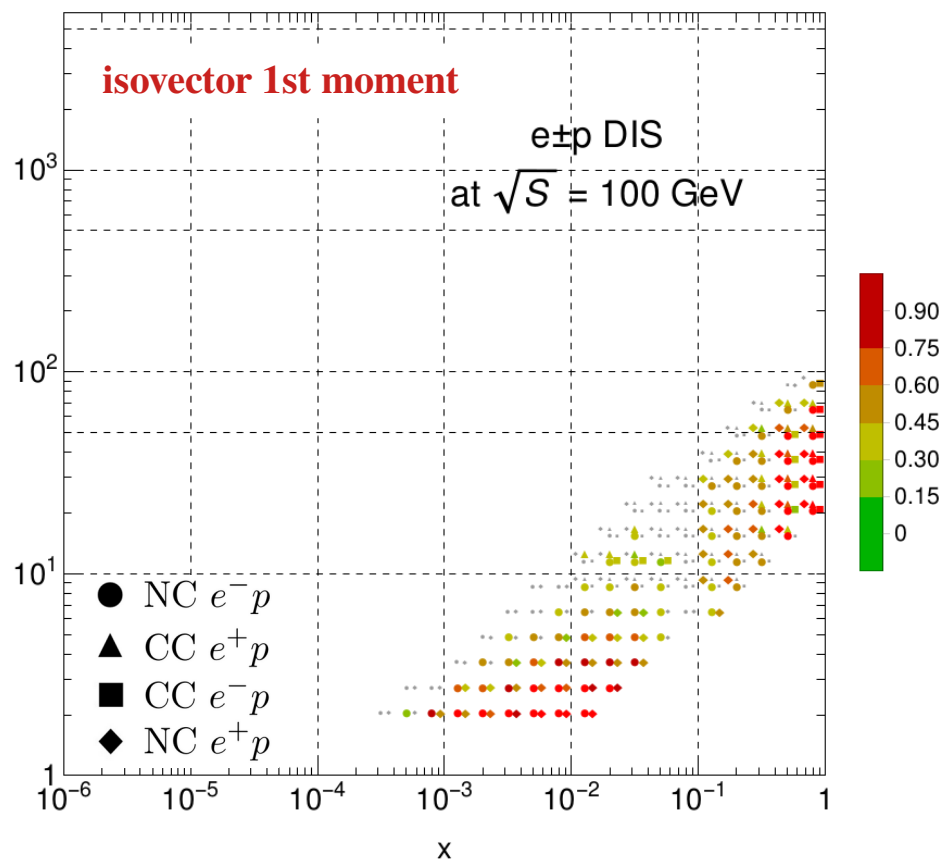


also: nuclear, spin-, transversity-, ..., PDFs

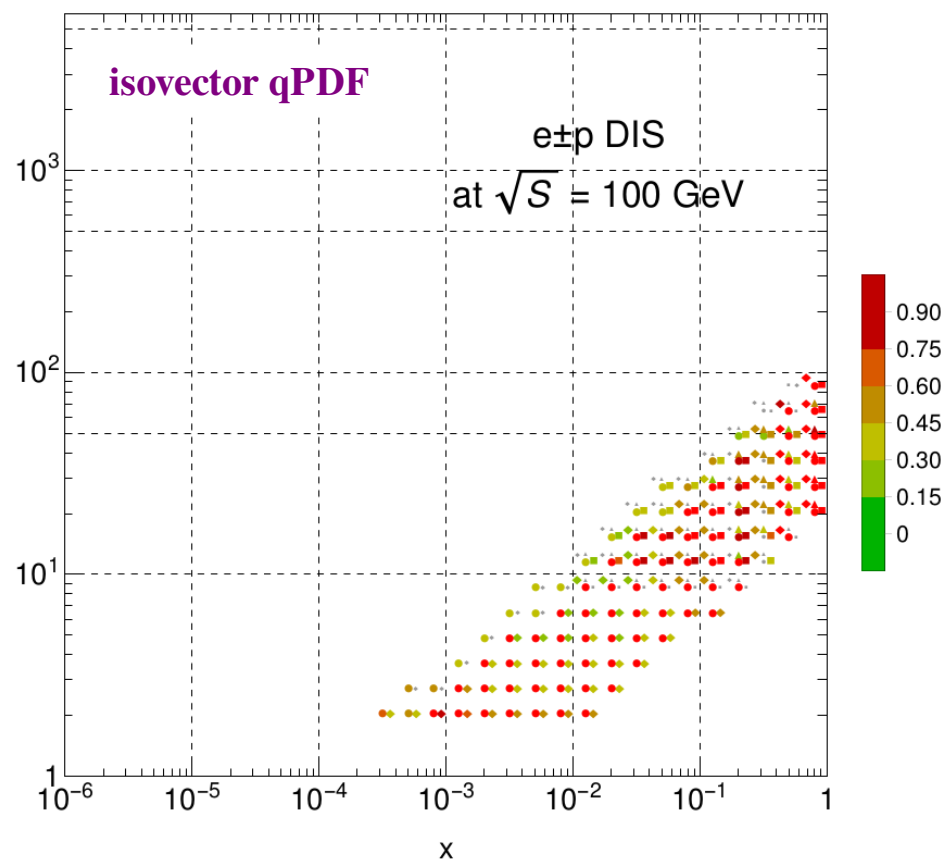
# EIC: sensitivity to high- $x$ ; driver of lattice benchmarks

- EIC inclusive DIS data would already have strong PDF sensitivity to many lattice observables; below, the isovector first moment (left) and analogous qPDF (right)

$|S_f|$  for  $\langle x^1 \rangle_{u^+ - d^+}$ , CT14HERA2



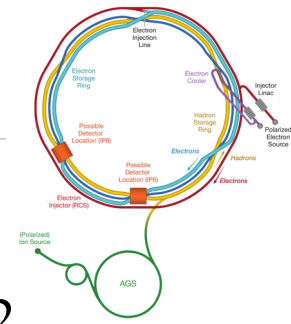
$|S_f|$  for  $[\tilde{u} - \tilde{d}](x=0.85, P_z=1.5\text{GeV})$ , CT14HERA2



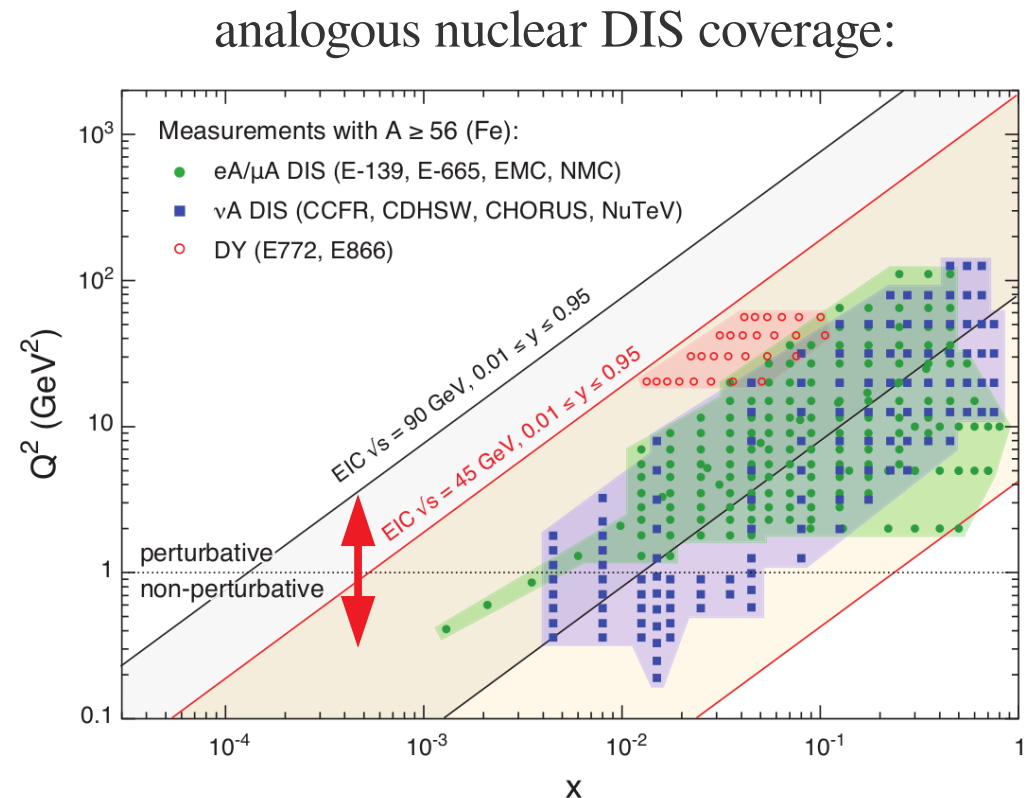
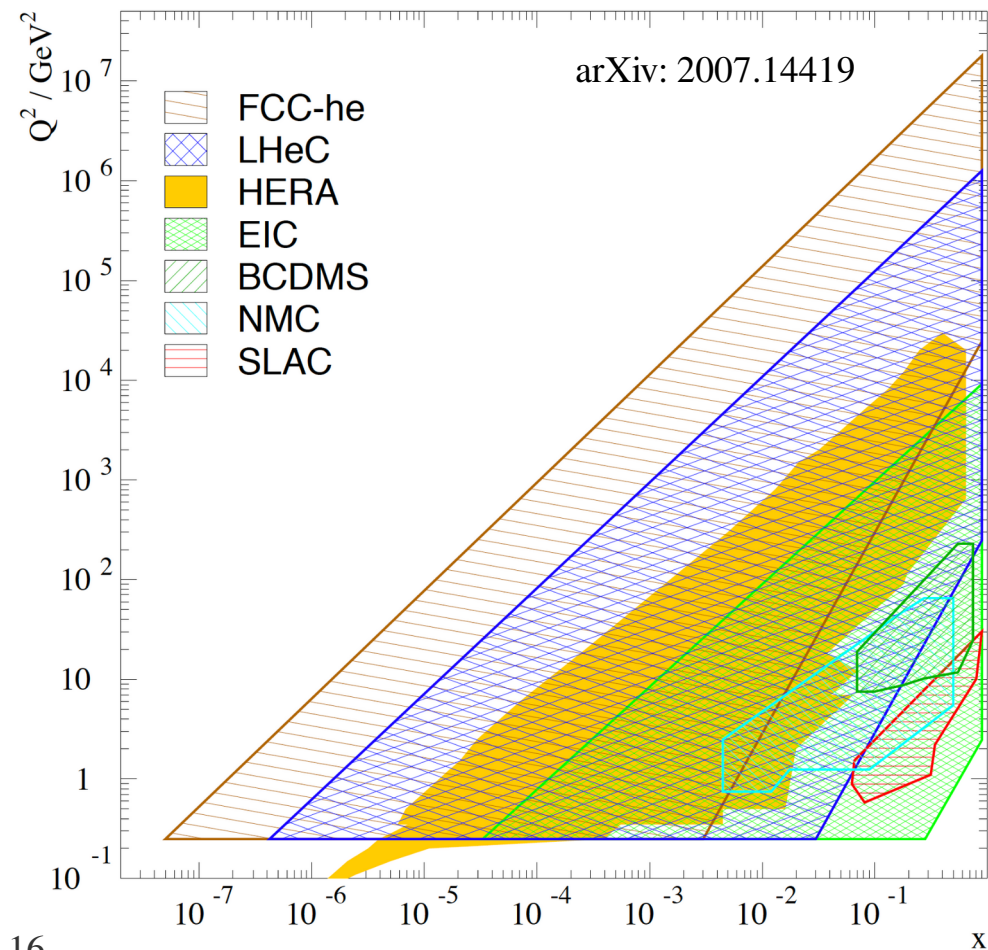
TJH, Wang, Nadolsky, Olness, PRD100 (2019) 9, 094040.

- sensitivity (indicated in red) from broad range of  $x$  and scale  $Q$ ; basis for reducing PDF uncertainties  $\rightarrow$  benchmarking lattice calculations  $\rightarrow$  further extrapolating to higher  $x$

# reach of the EIC program



- EIC explores unique region in  $[x, Q^2]$ ; machine for HEP-NP intersections
  - strong coverage of **quark-to-hadron transition** region between HERA, JLab12
- even higher luminosity would enhance EIC's coverage at periphery of nominal  $[x, Q^2]$  space
  - strengthen overlaps with other experiments; enable more scaling studies





# PDF impacts compared to high-value fixed-target DIS

ePump: Schmidt, Pumplin, and Yuan; PRD98 (2018) no.9, 094005.

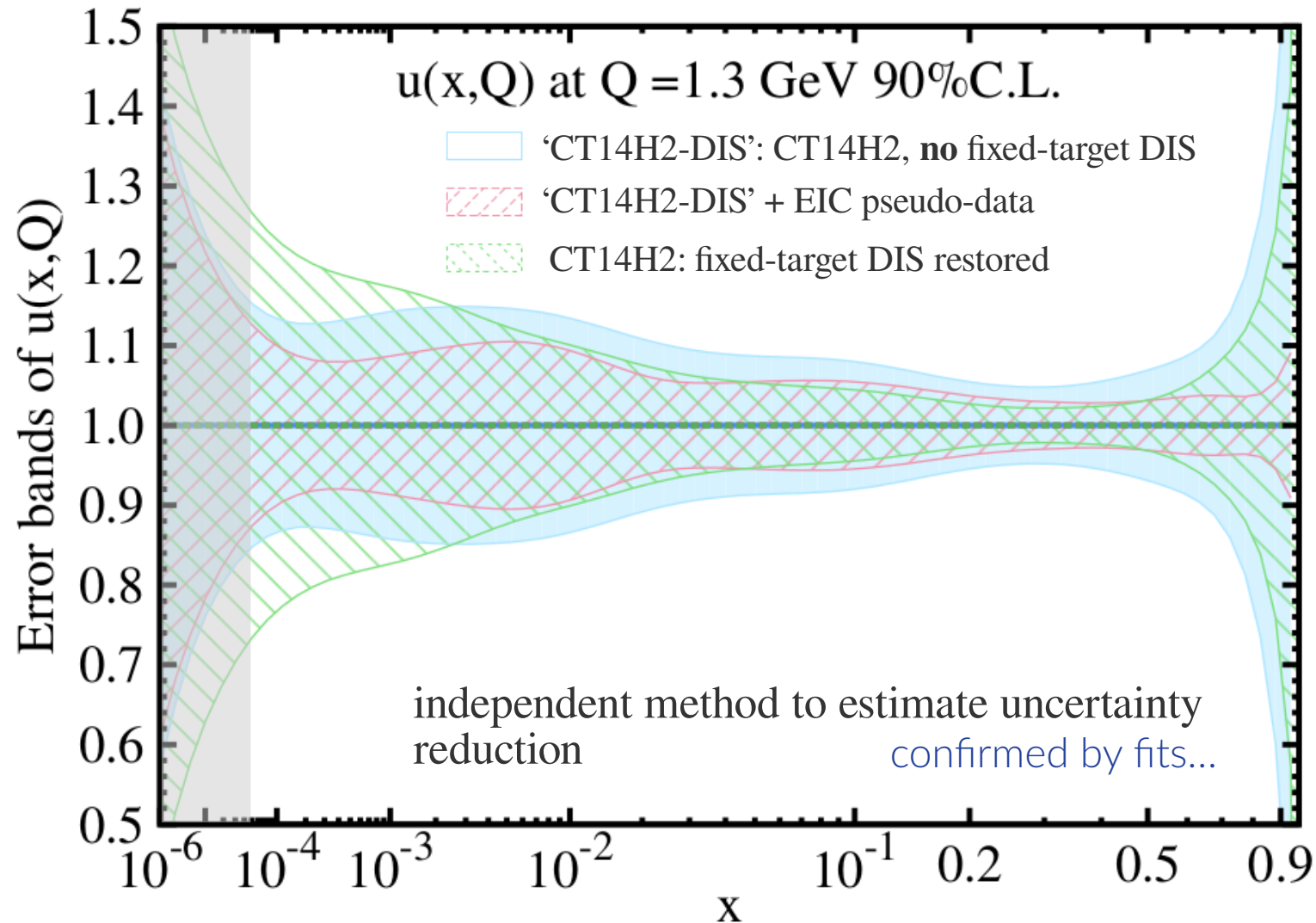


figure: S. Dulat

- **inclusive EIC may surpass total impact of fixed-target DIS in modern fits**

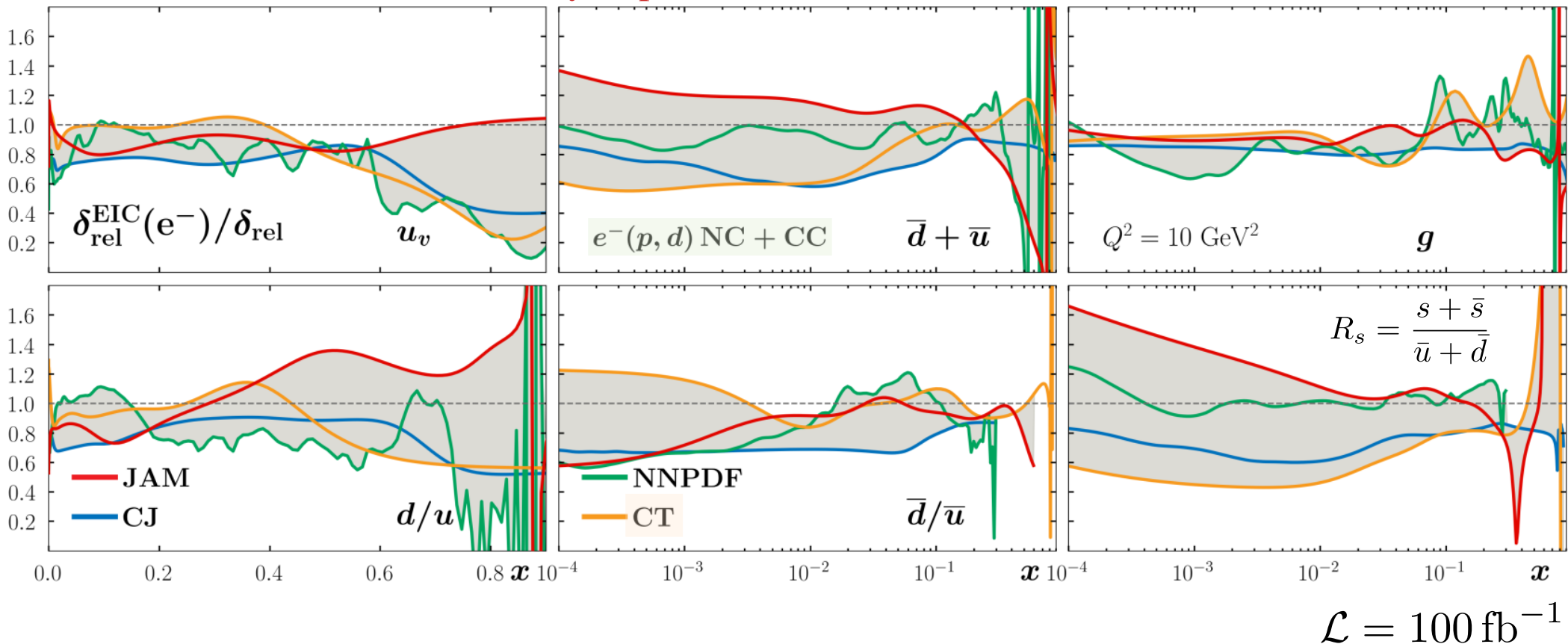
→ useful for negotiating among existing high-impact data; high lumi could extend further

- impact from simulated (optimistic) pseudodata; **estimated by various methods, groups**

EIC YR, 7.1.1

PDF uncertainty improvement

~1 year of [peak] data-taking



- broad impact, including on high- $x$   $u$ -,  $d$ -PDFs; probes of gluon, quark sea to low  $x$

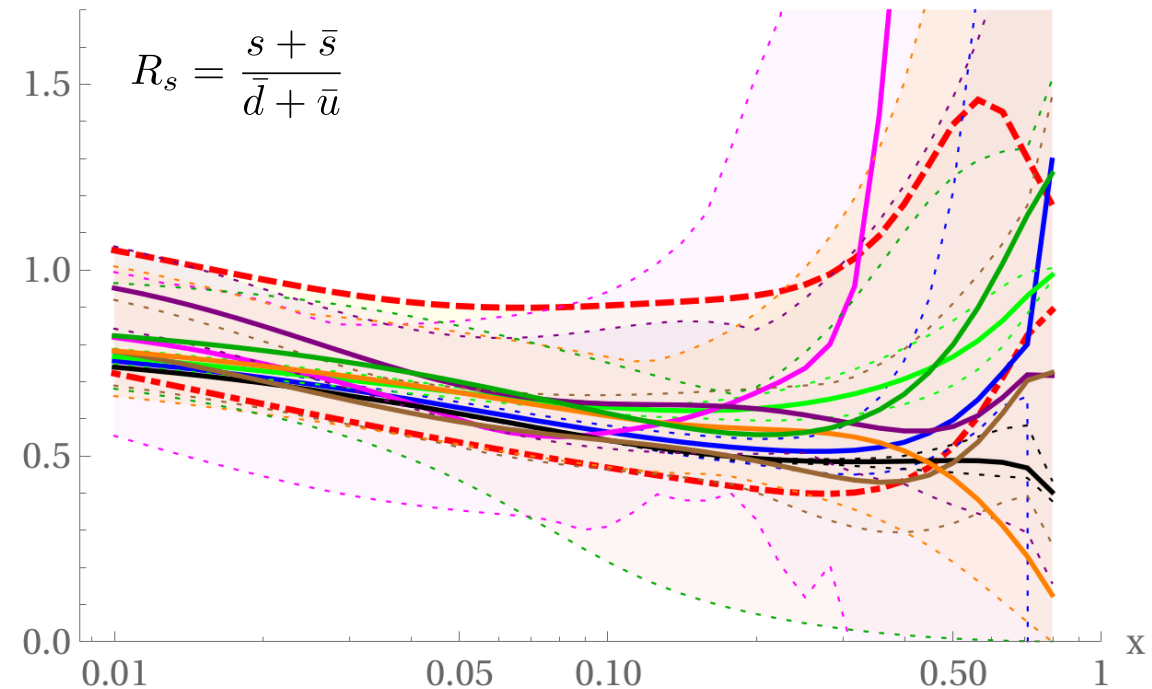
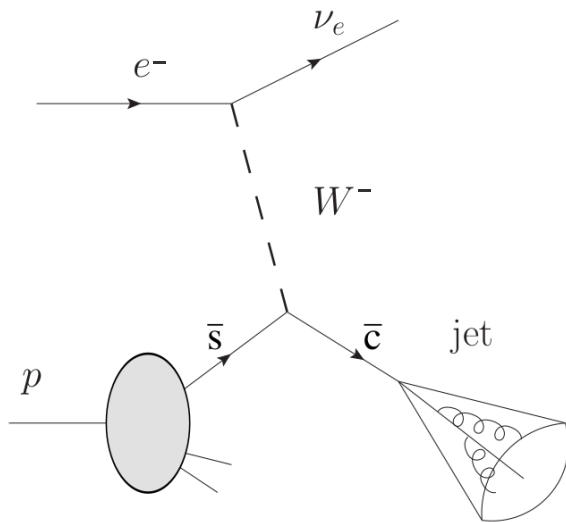
→ inclusive studies – indications of systematics limitations; **must also investigate**

- DIS jet production, including through charge-current interactions, provides further access to quark-level information

Arratia, Furlletova, TJH, Olness, Sekula; PRD **103** (2021) 7, 074023.

$R_s(x, Q)$   $Q=10$  GeV

100 fb<sup>-1</sup> CC DIS (10M simulated events),  
at 10x275 GeV ( $e^-$  on  $p$ );  $Q^2 > 100$  GeV<sup>2</sup>

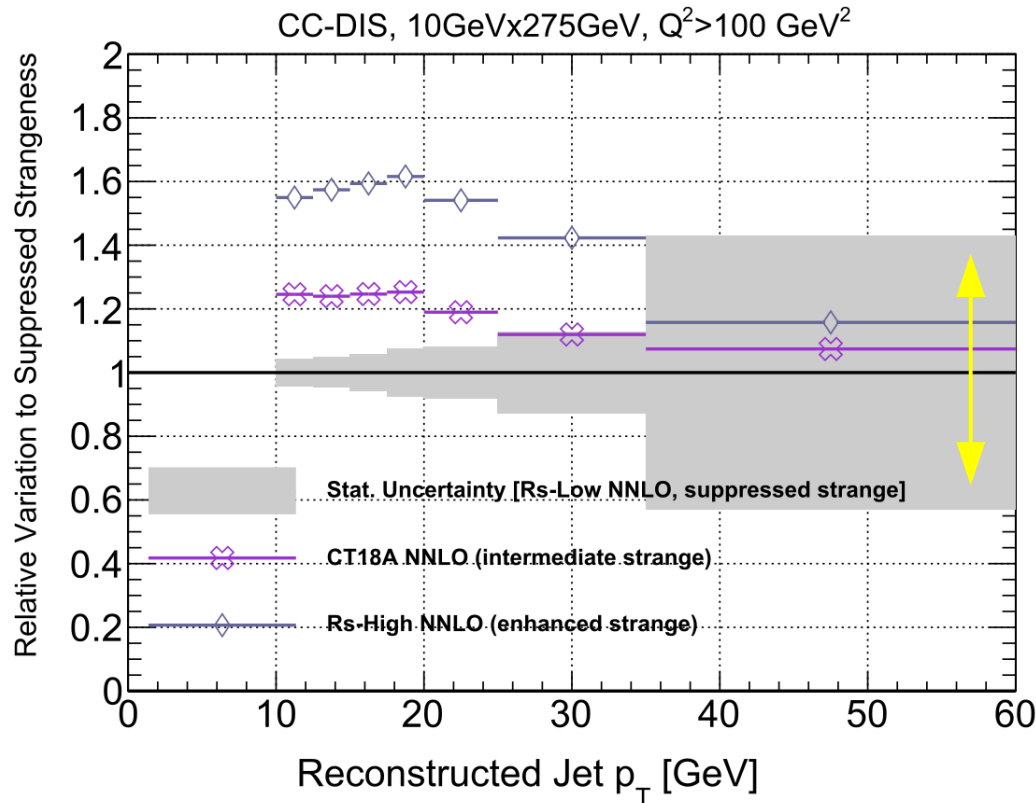


**final-state tagging provides lever arm for flavor separation (here, strangeness)**

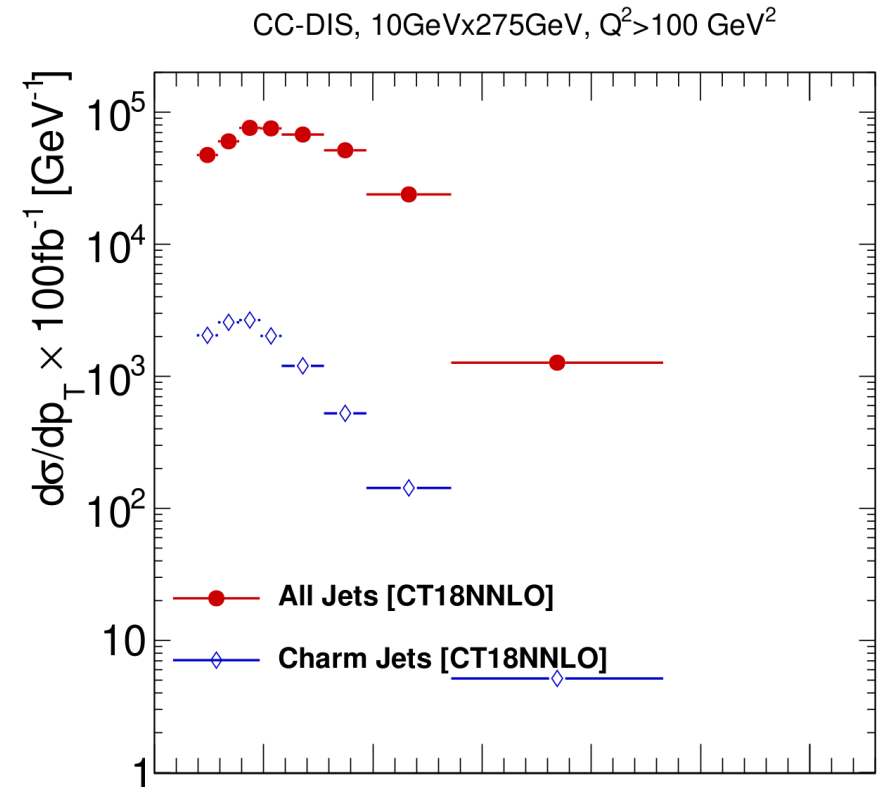
- n.b.: event generation, detector sim from PYTHIA8 + DELPHES; FASTJET reconstruction
  - analogous jet measurements might be extended to nonperturbative heavy flavor

# precision QCD through jet and heavy-flavor production

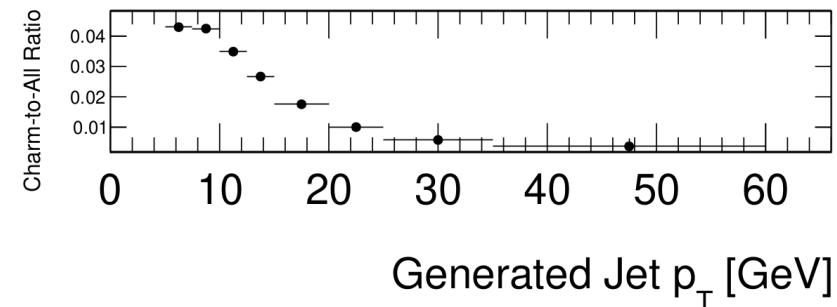
- challenging measurement: final-state flavor tagging; Jacquet-Blondel reconstruction



Arratia, Furlletova, TJH, Olness, Sekula; PRD **103** (2021) 7, 074023.



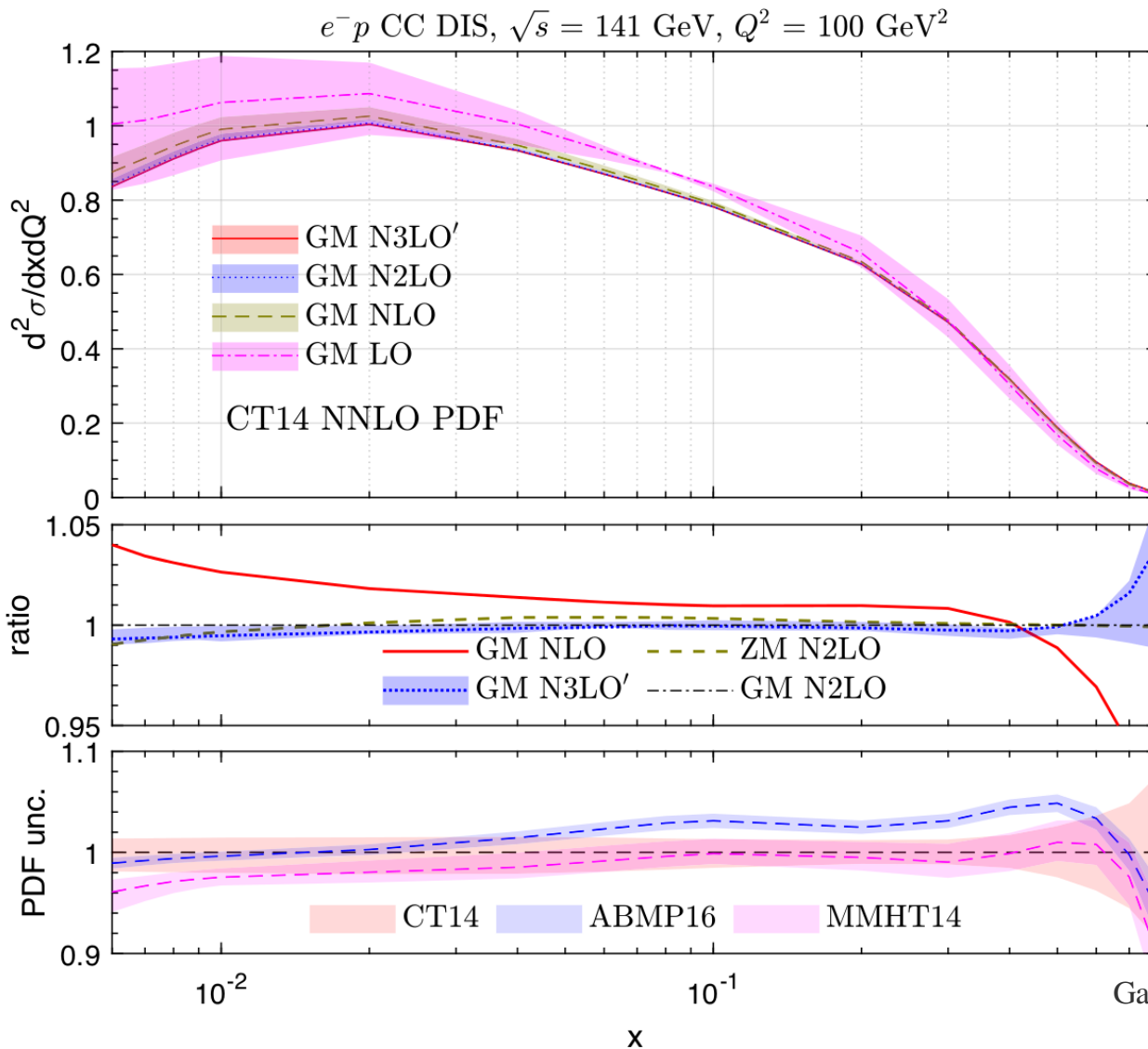
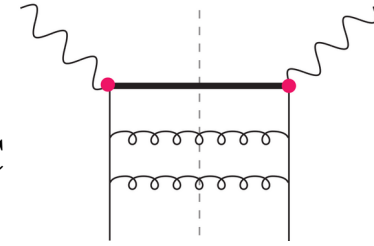
- charm production suppressed by  $>2$  orders of magnitude;  $p_T$  cross section steeply falling
- reduced  $\delta_{\text{stat}}$  could significantly enhance knowledge of  $p_T$  dependence



→ greater event rates may furnish enhanced discriminating power

# (CC) DIS at NNLO and beyond

- extracting PDF information from CC DIS requires robust theory accuracy
  - can compute NNLO, approximate N<sup>3</sup>LO corrections for highest energies at EIC



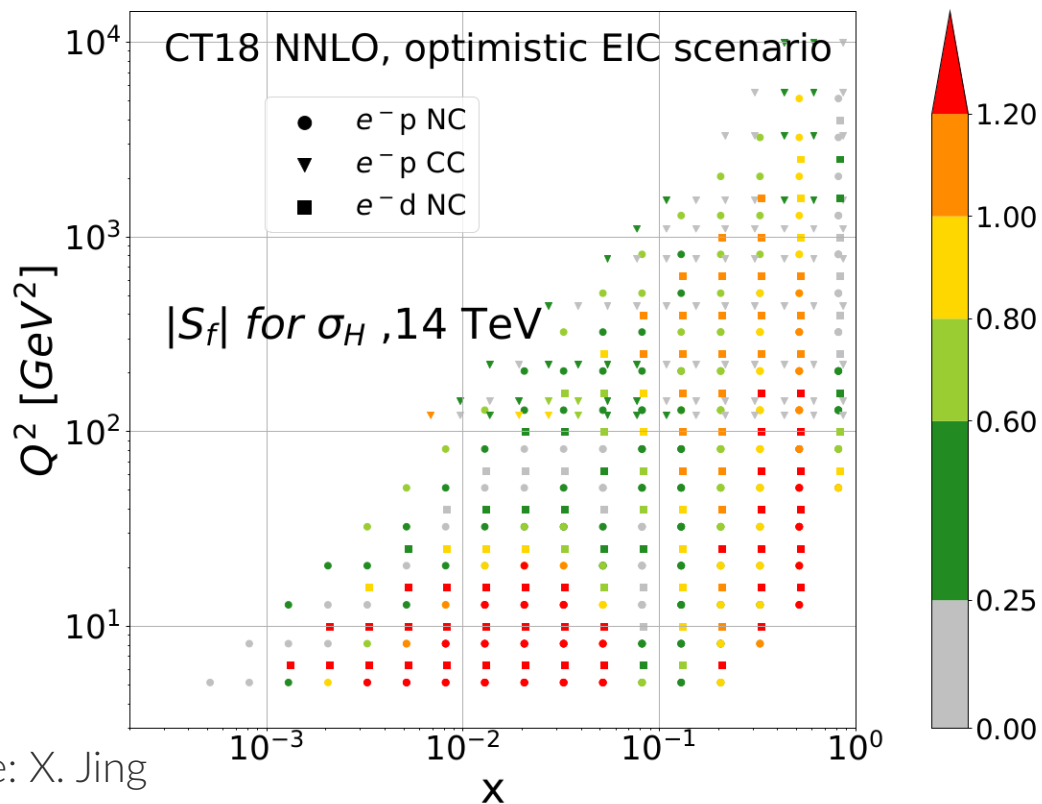
- strong perturbative convergence
  - for N<sup>3</sup>LO', scale variations generally contained to  $\lesssim 0.5 - 1\%$

- significantly smaller than PDF-driven uncertainties, which can be as large as  $\approx 2\%$

**vital ingredient in EIC PDF program**

- note improvements at high  $x$ : suggests possible synergy with high-luminosity measurements

iii

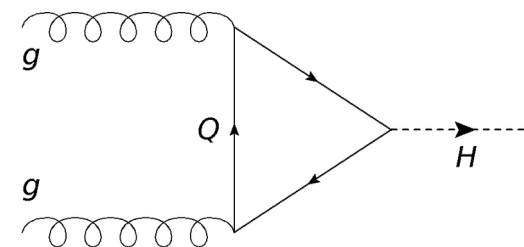
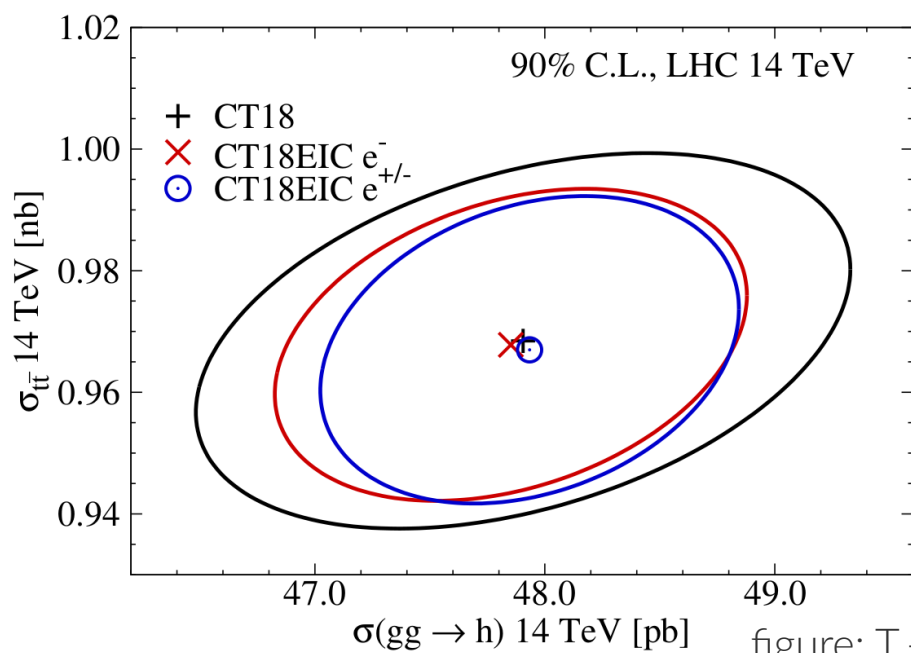


## precise EIC data impact high-energy predictions

example:

- PDF-driven improvement to **Higgs-production** cross section
- EIC impact on Higgs theory from broad region of the kinematical space it can access

figure: X. Jing



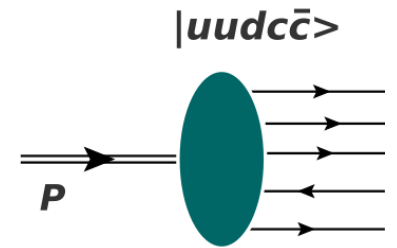
- impact closely tied to that of the integrated gluon PDF

→ similar impacts on EW observables

figure: T.-J. Hou

# coda: nonperturbative charm in the proton

- possible nonperturbative (‘intrinsic’) charm component of the nucleon long debated
- PDF valence-like *shape* predicted by various nonperturbative models
  - *normalization* has been challenging to determine

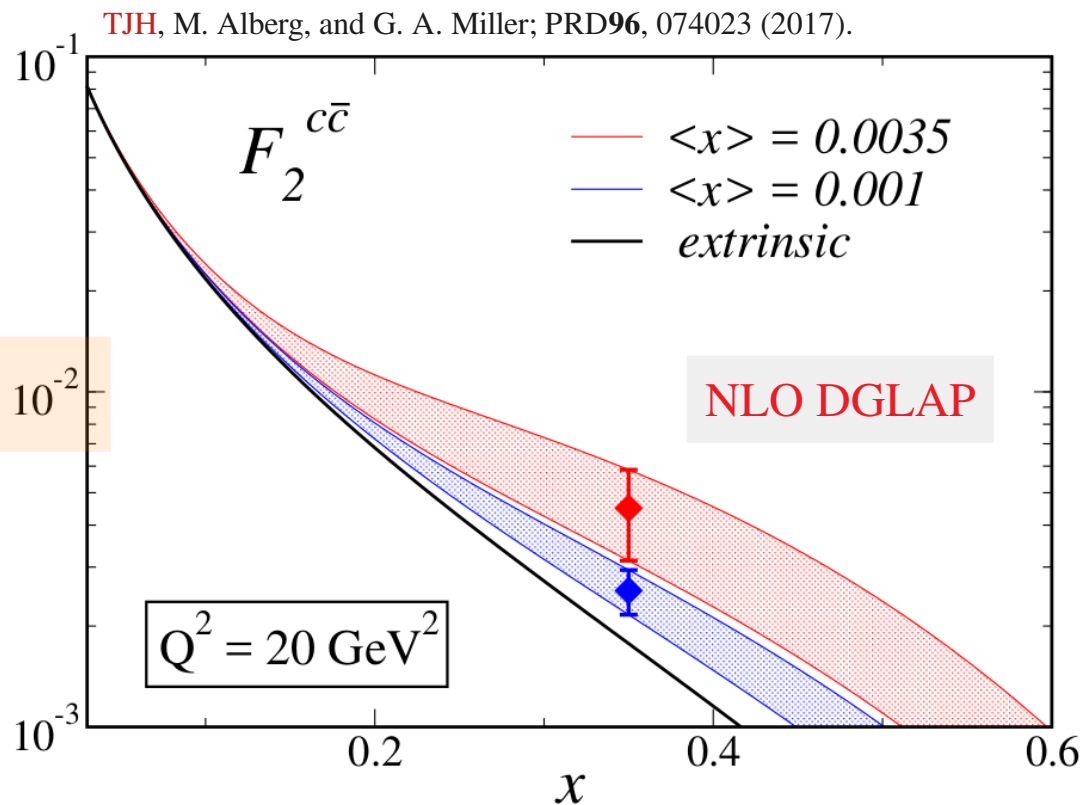


Brodsky et al.; PLB**93** (1980) 451.

TJH, Londergan, Melnitchouk; PRD**89** (2014) 7, 074008.

Nature 608 (2022) 7923, 483.

- recent NNPDF analysis claims evidence; nominal size,  $\langle x \rangle_{c^+}(Q = 1.51 \text{ GeV}) = [0.62 \pm 0.28]\%$



- other recent analyses, different conclusions:

→  $\langle x \rangle_{\text{IC}} < 0.1\%$  at  $5\sigma$

Jimenez-Delgado, TJH, Londergan, Melnitchouk; PRL**116** (2016).

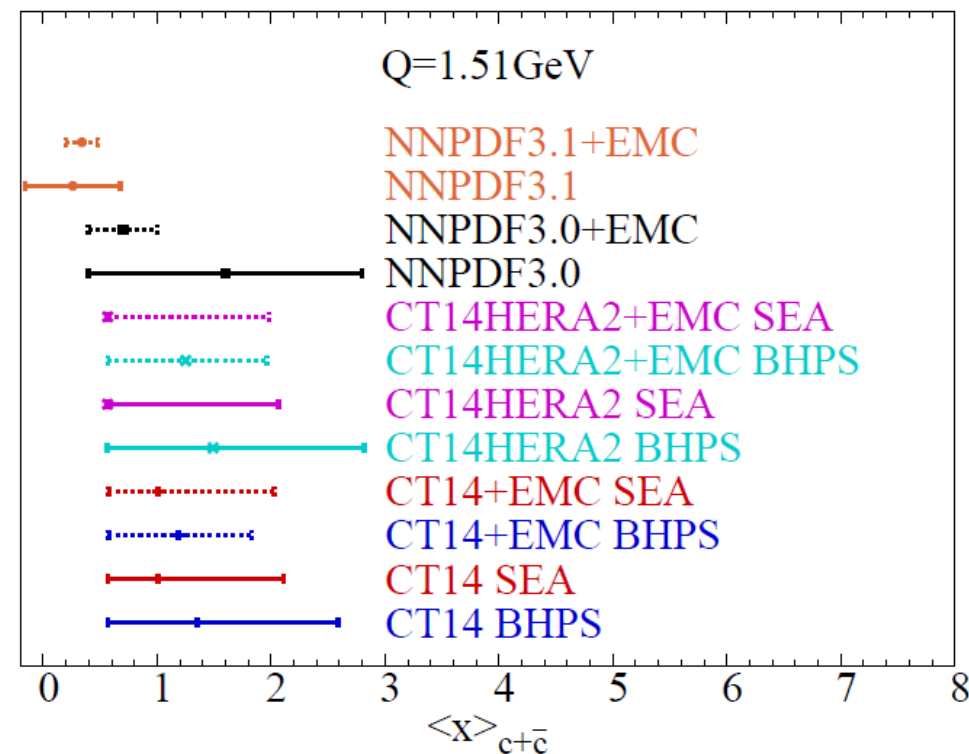
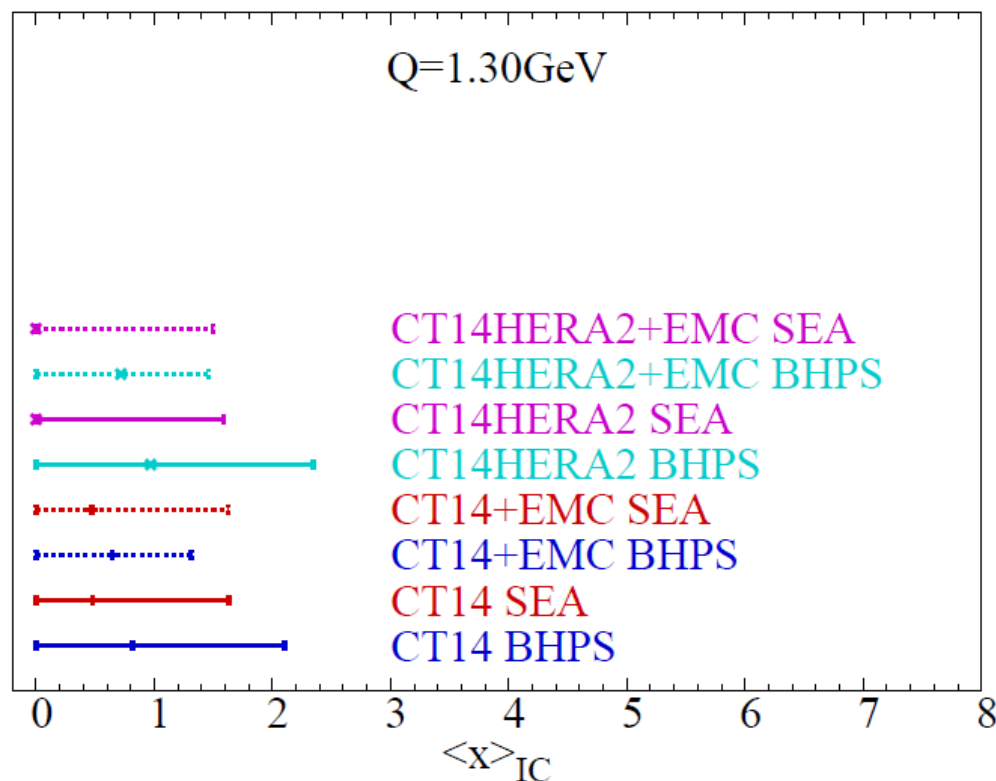
→  $\langle x \rangle_{\text{IC}} \lesssim 2\%$  CT14IC, Hou et al., JHEP **02** (2018) 059.

- subject remains unresolved!

→ ‘IC’ still lacks formal, universal def.

→ prime candidate for **EIC**; hard, but **lattice** might compute  $\langle x \rangle_{c^+}$

# Allowed momentum fractions

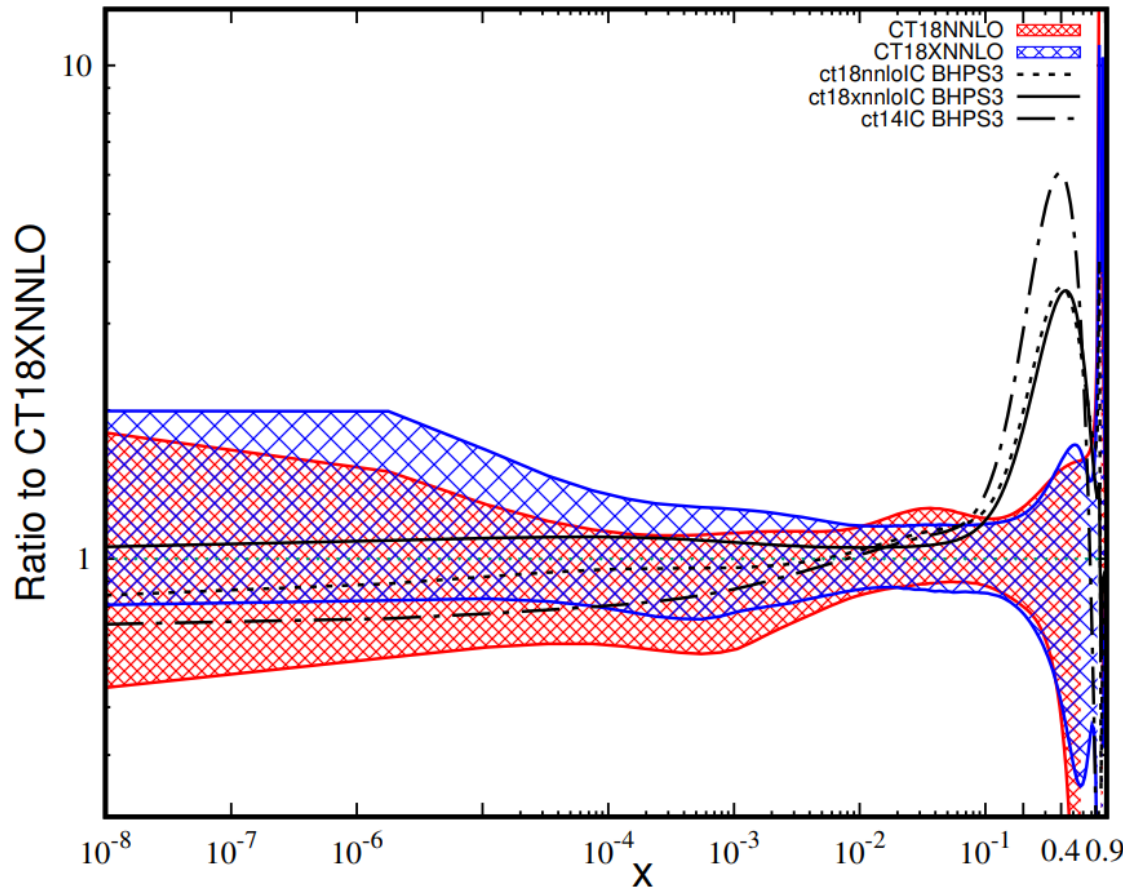


Sources of differences	CT14 IC	NNPDF3.x
order	NNLO only	NLO, NNLO
Settings	90% c.l., GeV	68% c.l., GeV
LHC 8 TeV	Under validation; mild tension with HERA DIS data	Included; strong effect despite a smallish data sample
1983 EMC data included?	Only as a cross check (unknown syst. effects in EMC data)	Optional, strong effect on the PDF error

- lattice information on momentum fraction would enlighten this landscape, along with EIC



Allowec



Forward Physics Facility  
whitepaper,

PR968 (2022); 2109.10905

- √ NNPDF3.1+EMC
- √ NNPDF3.1
- √ NNPDF3.0+EMC
- √ NNPDF3.0
- T14HERA2+EMC SEA
- T14HERA2+EMC BHPS
- T14HERA2 SEA
- T14HERA2 BHPS
- T14+EMC SEA
- T14+EMC BHPS
- T14 SEA
- T14 BHPS

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LHC 8 TeV	Under validation; mild tension with HERA DIS data	Included; strong effect despite a smallish data sample
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- lattice information on momentum fraction would enlighten this landscape, along with EIC

- **PDFs necessary for precision HEP measurements**
  - limit EW precision, sensitivity of collider-based BSM searches
  - active HEP program: higher theory accuracy; generator development
- **parallel developments from lattice, future EIC program will be instrumental**
  - lattice: challenging kinematics; flavor dependence; exotic matrix elements
  - EIC: comprehensive coverage of quark-hadron transition; QCD tests
  - must pioneer exciting synergies between QCD pheno./lattice

(this talk: mostly high- $x$ ; also opportunities at low  $x$ , high multiplicity)

- **all core to understanding (nonpert.) QCD; nuclear systems**
  - high- $x$ : flavor-symmetry breaking ( $\bar{d}/\bar{u}$ ); WF effects [ $d(x \approx 1)$ ]
  - nuclear PDFs: EIC data; few-body moments, qPDFs from lattice

future experiments central: JLab12 → EIC, HL-LHC, LBNF, ...

—— supplementary material ——

# high-interest SM quantities are precision-limited by PDFs

→ these include  $\sigma_H$ ,  $\sin^2 \theta_W$ ,  $m_W$ , ...

ATLAS, 1701.07240

for example:

Channel	$m_{W^+} - m_{W^-}$ [MeV]	Stat. Unc.	Muon Unc.	Elec. Unc.	Recoil Unc.	Bckg. Unc.	QCD Unc.	EW Unc.	PDF Unc.	Total Unc.
$W \rightarrow e\nu$	-29.7	17.5	0.0	4.9	0.9	5.4	0.5	0.0	24.1	30.7
$W \rightarrow \mu\nu$	-28.6	16.3	11.7	0.0	1.1	5.0	0.4	0.0	26.0	33.2
Combined	-29.2	12.8	3.3	4.1	1.0	4.5	0.4	0.0	23.9	28.0

→ the PDF uncertainty can be a/the dominant uncertainty!

→ frontier efforts at the HL-LHC aim for (sub)percent precision

→ **large cross-cutting effort spanning theory/expt to improve**

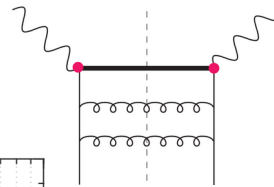
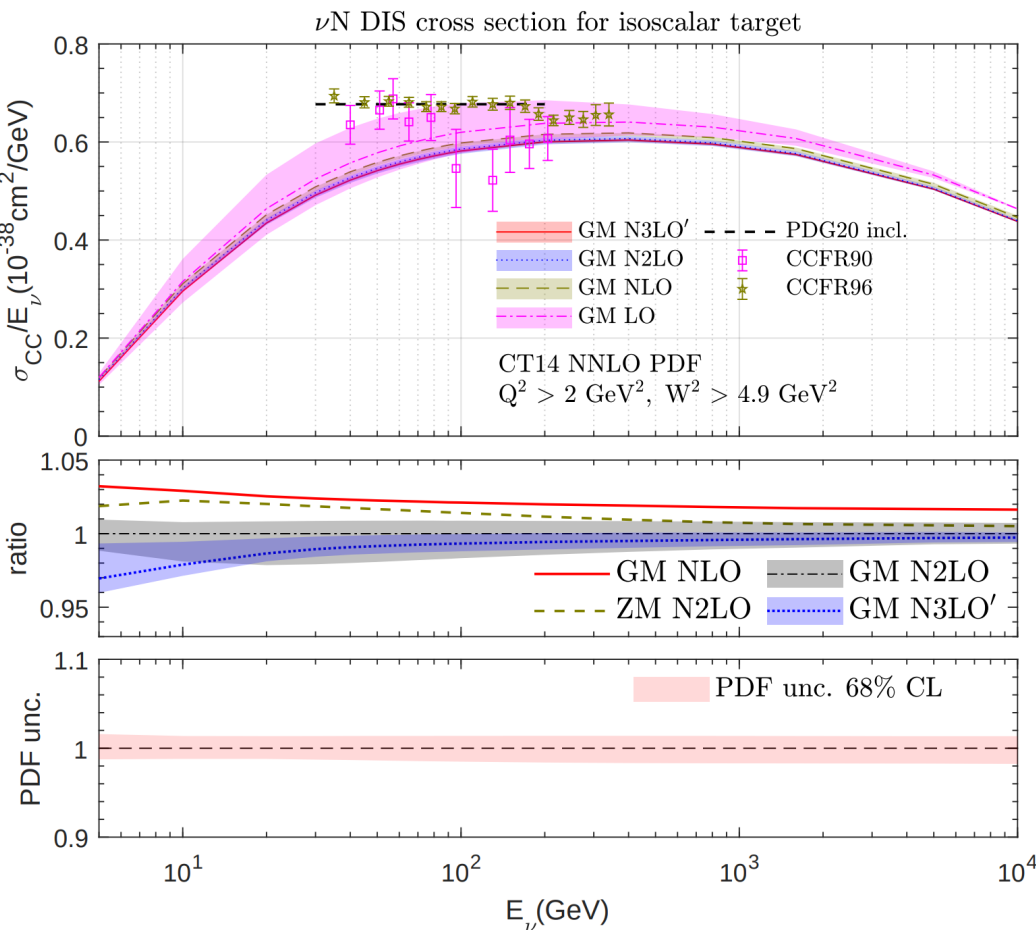
- heightened theory accuracy (HO, power corrections)
- novel measurements (EIC, LHC, vA)
- generator development

# theory ingredients → higher pQCD accuracy

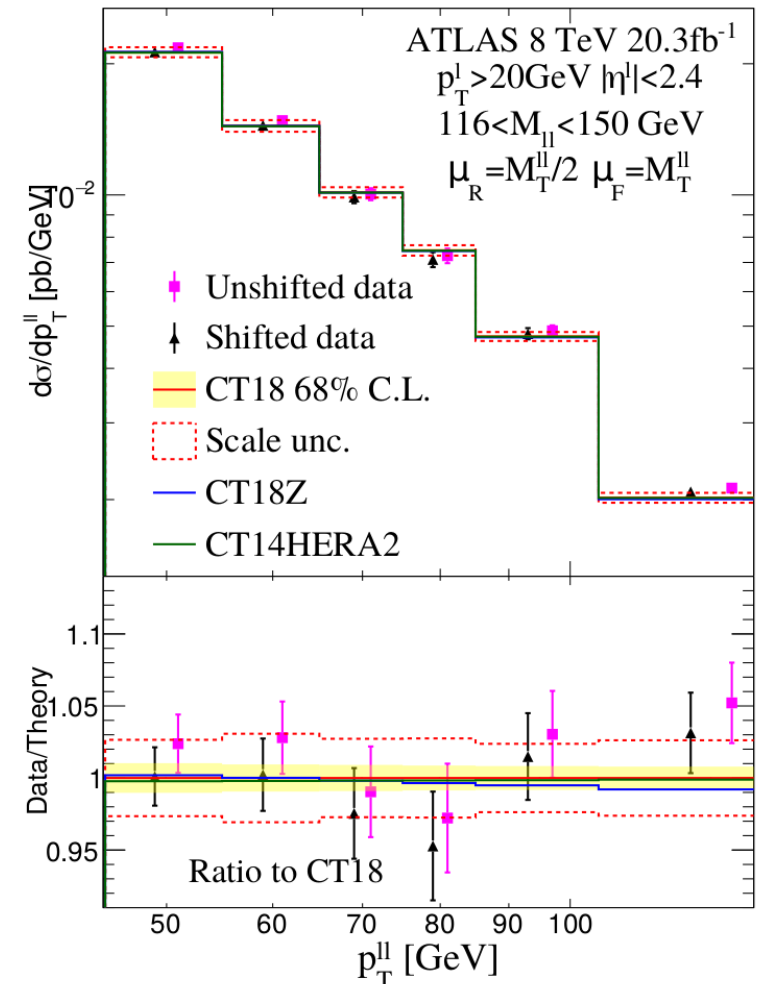
- current/future analyses involve interplay between pQCD & other dynamics
- NNLO+ necessary to stabilize scale uncertainties; especially over wide scales

## charge-current DIS

Gao, TJH, Nadolsky, Sun, Yuan: PRD105 (2022) 1, L011503



## NNLO scale variations at LHC



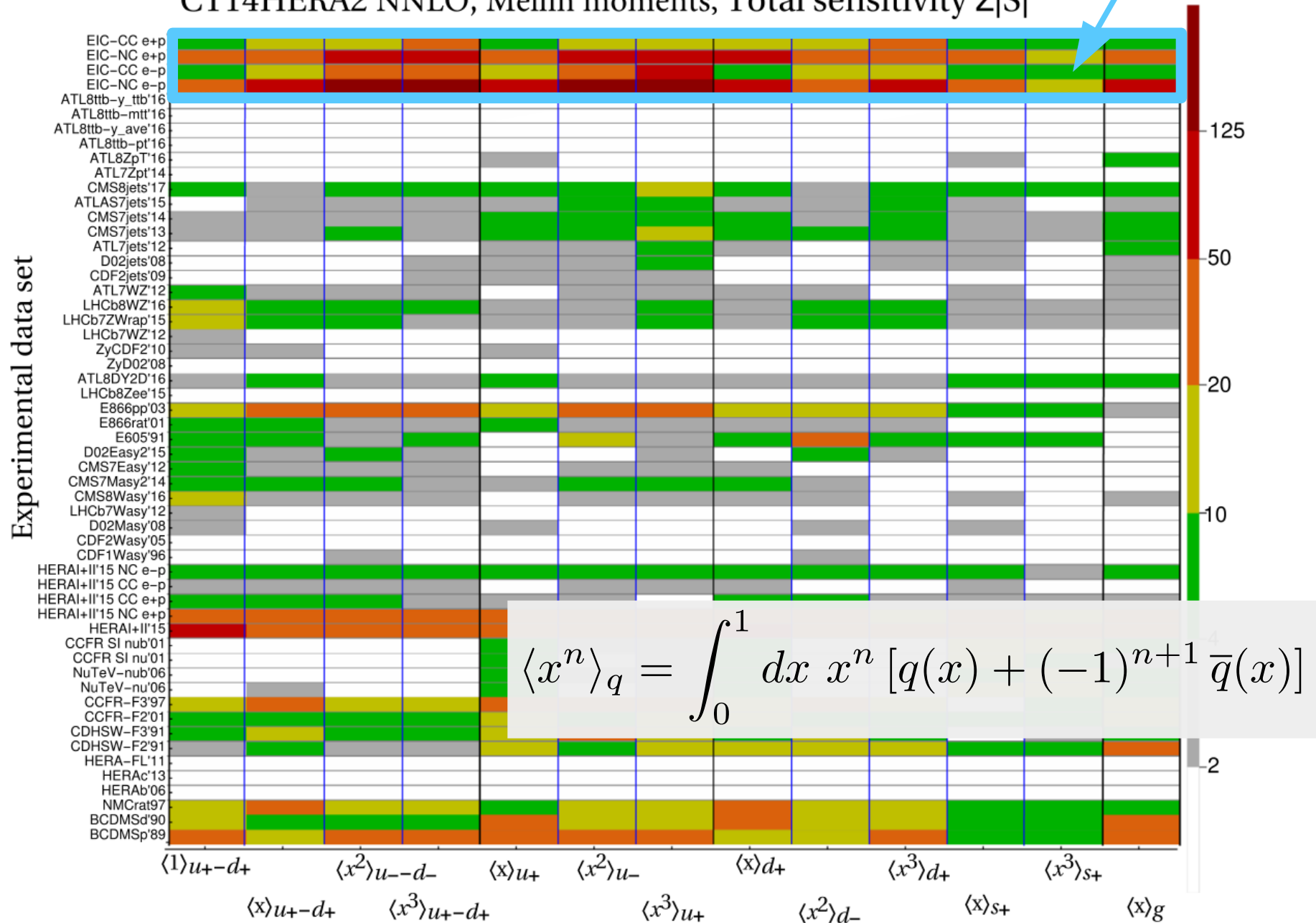
→ needed for DUNE, FASERν, EIC

# sensitivities can be aggregated for direct comparisons of exps

→ EIC strongly sensitive to PDF Mellin moments; lattice benchmarks

**EIC pseudodata**

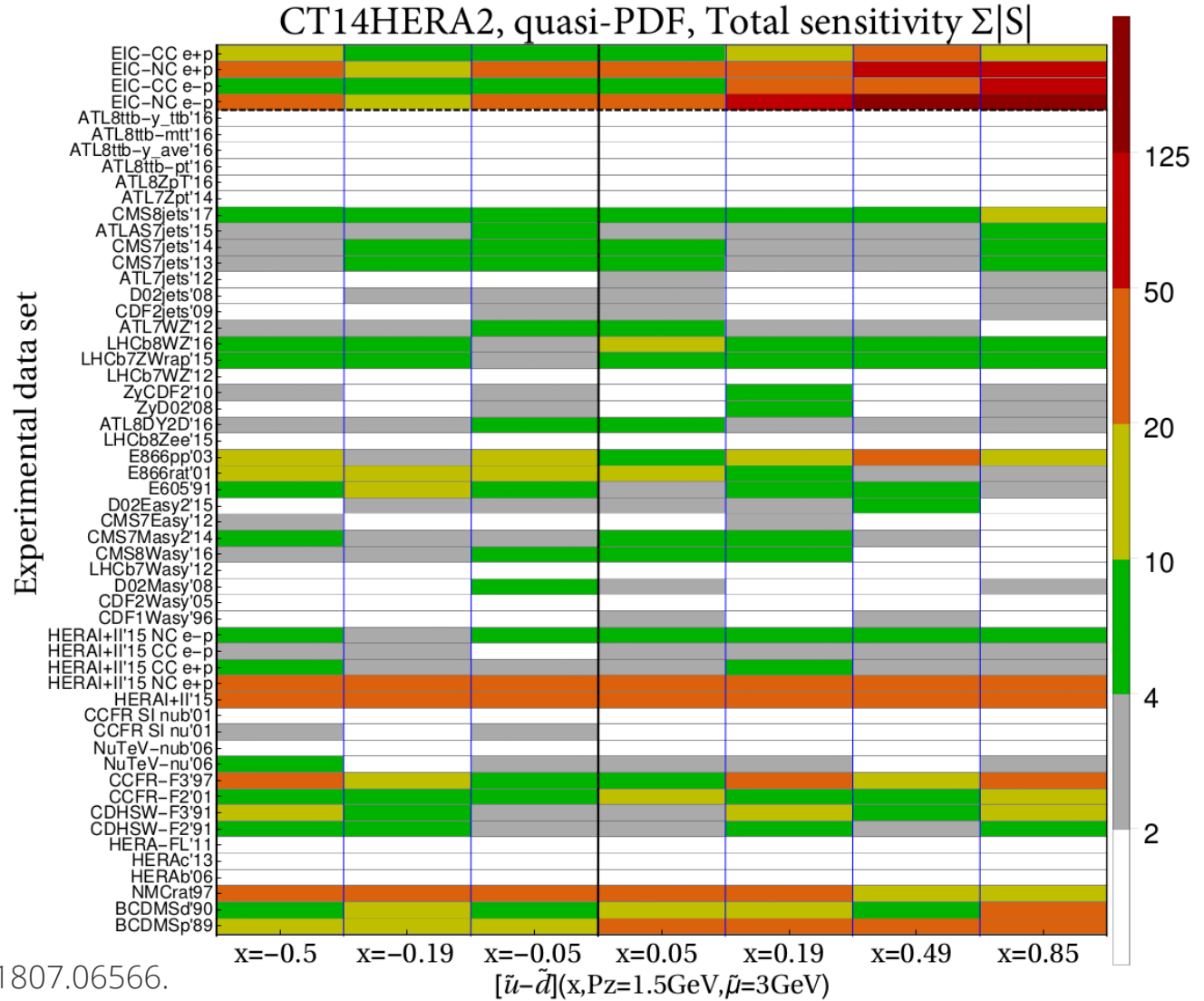
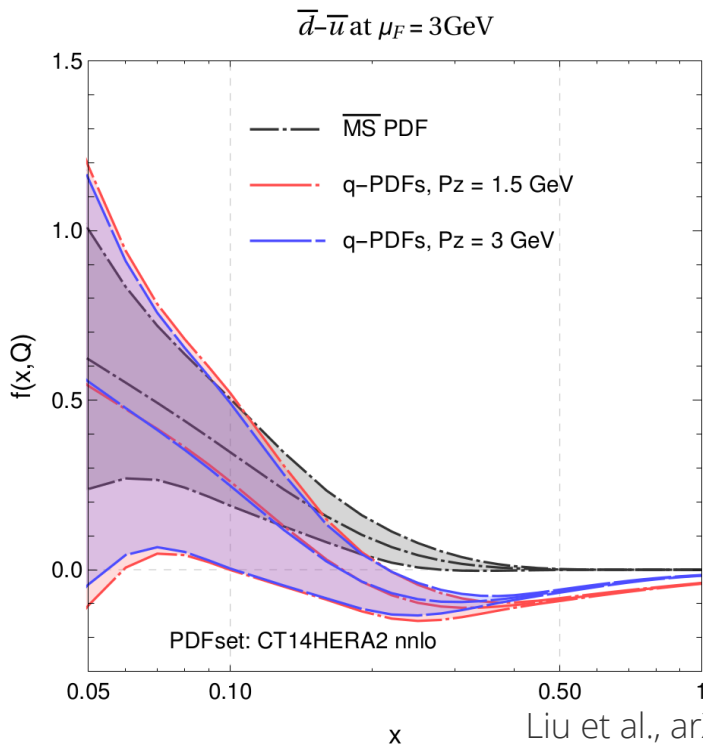
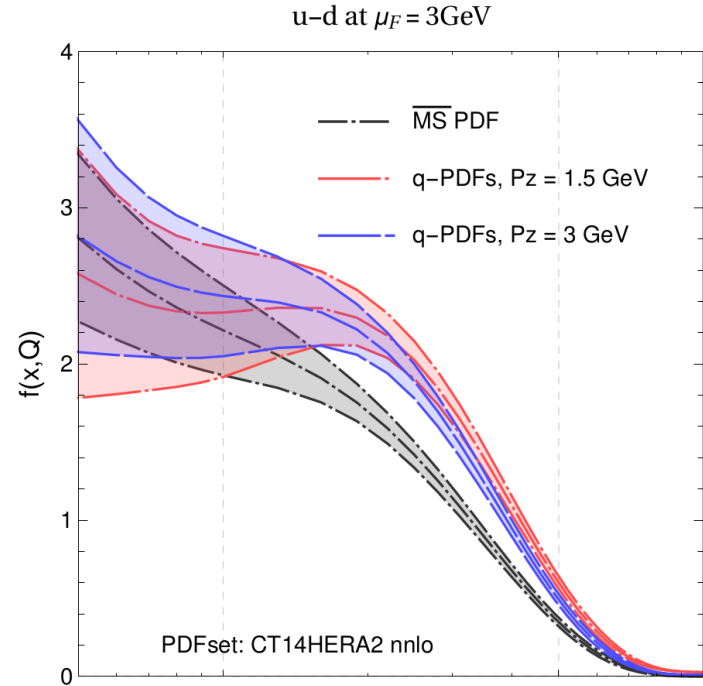
CT14HERA2 NNLO, Mellin moments, Total sensitivity  $\Sigma|S|$



# total sensitivity to matched quasi-PDFs

$$\bar{q}(x) = -q(-x) \rightarrow q(x) \equiv \begin{cases} u(x) - d(x), & x > 0 \\ \bar{d}(|x|) - \bar{u}(|x|), & x < 0 \end{cases}$$

$$P_z = 1.5 \text{ GeV}; \mu_F = 3 \text{ GeV}$$



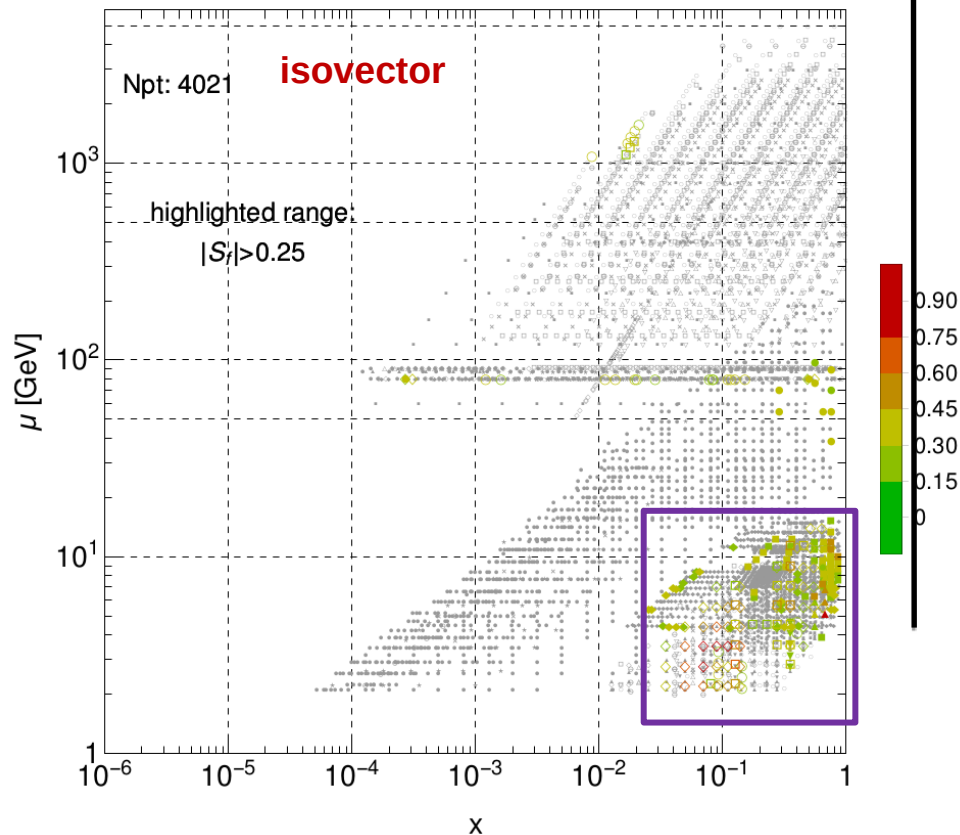
- Recovering PDFs from qPDFs requires the inversion of still-developing *matching relations*,

$$\tilde{q}(x, P_z, \tilde{\mu}) = \int dy Z \left( \frac{x}{y}, \frac{\Lambda}{P_z}, \frac{\mu}{P_z} \right) q(y, \mu) + \mathcal{O} \left( \frac{\Lambda^2}{P_z^2}, \frac{M^2}{P_z^2} \right)$$

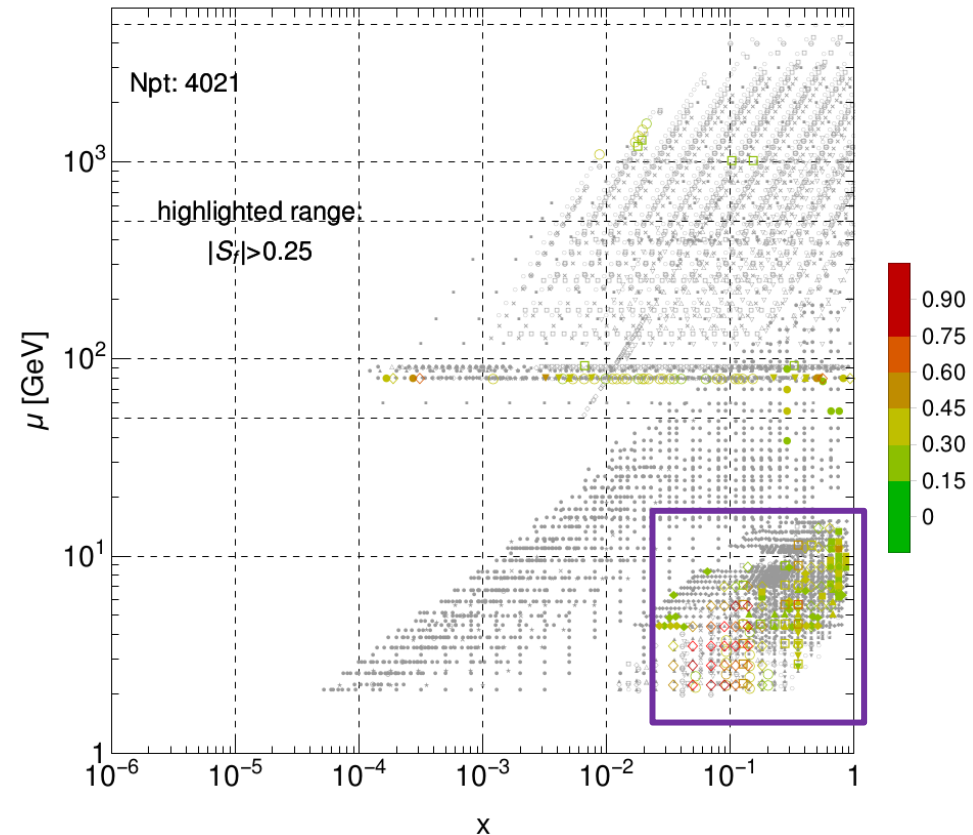
$\downarrow$   
qPDF
 $\downarrow$   
ordinary PDF

- The matching formalism depends crucially on the nucleon boost,  $P_z$ ; fixed-target DIS data at high  $x_i$  are mildly sensitive to this  $P_z$  dependence, and can aid theory developments in qPDFs:

$|S_f|$  for  $[\tilde{u}-\tilde{d}](x=0.85, P_z=1.5\text{GeV})$ , CT14HERA2

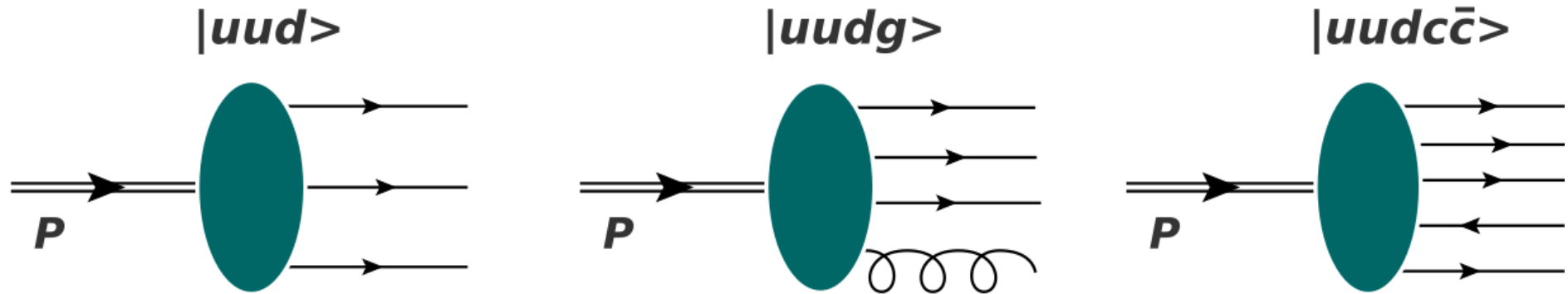


$|S_f|$  for  $[\tilde{u}-\tilde{d}](x=0.85, P_z=3\text{GeV})$ , CT14HERA2





BUT: nonperturbative QCD can generate a low-scale charm PDF



→ original models possessed *scalar* vertices...

- Brodsky et al. (1980): [intrinsic charm – ‘BHPS’ and other models](#)

$$P(p \rightarrow uudc\bar{c}) \sim \left[ M^2 - \sum_{i=1}^5 \frac{k_{\perp i}^2 + m_i^2}{x_i} \right]^{-2}$$

→ produces *intrinsic* PDF,  $c^{\text{IC}}(x) = \bar{c}^{\text{IC}}(x)$

Brodsky, Hoyer, Peterson, Sakai; Phys. Lett. B93 (1980) 451.

- Blümlein (2015):

$$\tau_{\text{life}} = \frac{1}{\sum_i E_i - E} = \frac{2P}{\left( \sum_{i=1}^5 \frac{k_{\perp i}^2 + m_i^2}{x_i} - M^2 \right)} \Big|_{\sum_j x_j = 1} \quad \text{vs.} \quad \tau_{\text{int}} = \frac{1}{q_0}$$

→ comparison constrains  $x - Q^2$  space over which IC is observable

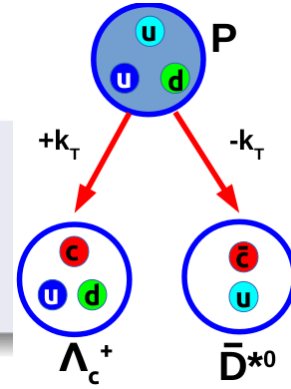
Blumlein; Phys. Lett. B753 (2016) 619.

# meson-baryon models (MBM)

- we implement a framework which *conserves spin/parity*

- nonperturbative mechanisms** are needed to break

$$c(x, Q^2 \leq m_c^2) = \bar{c}(x, Q^2 \leq m_c^2) = 0!$$

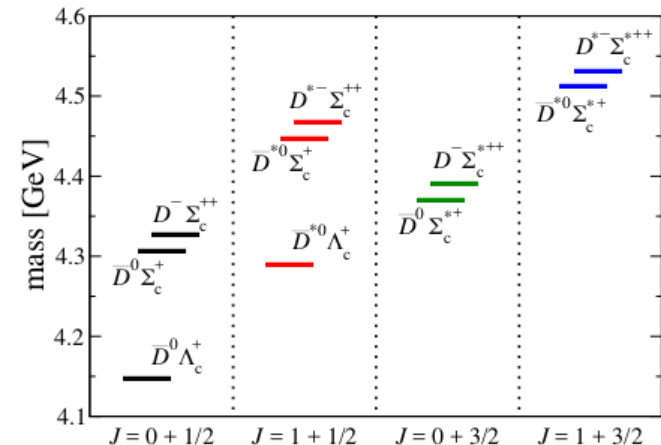


We build an **EFT** which connects IC to properties of the hadronic spectrum: [TJH, J. T. Londergan and W. Melnitchouk, Phys. Rev. D89, 074008 (2014).]

- $|N\rangle = \sqrt{Z_2} |N\rangle_0 + \sum_{M,B} \int dy \mathbf{f}_{MB}(\mathbf{y}) |M(y); B(1-y)\rangle$   
 $y = k^+ / P^+$ :  $k$  meson,  $P$  nucleon

$$c(x) = \sum_{B,M} \left[ \int_x^1 \frac{d\bar{y}}{\bar{y}} f_{BM}(\bar{y}) c_B\left(\frac{x}{\bar{y}}\right) \right]$$

- a similar *convolution* procedure may be used for  $\bar{c}(x) \dots$



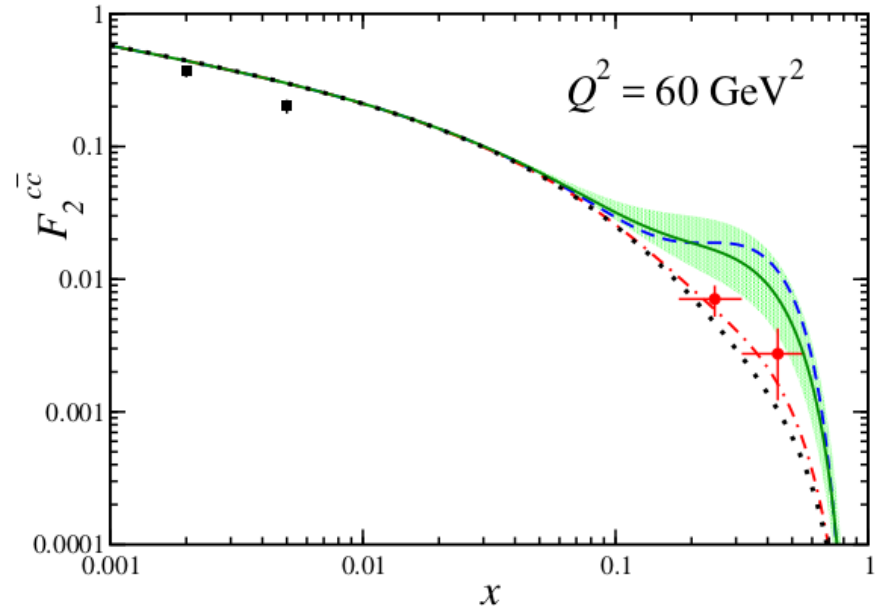
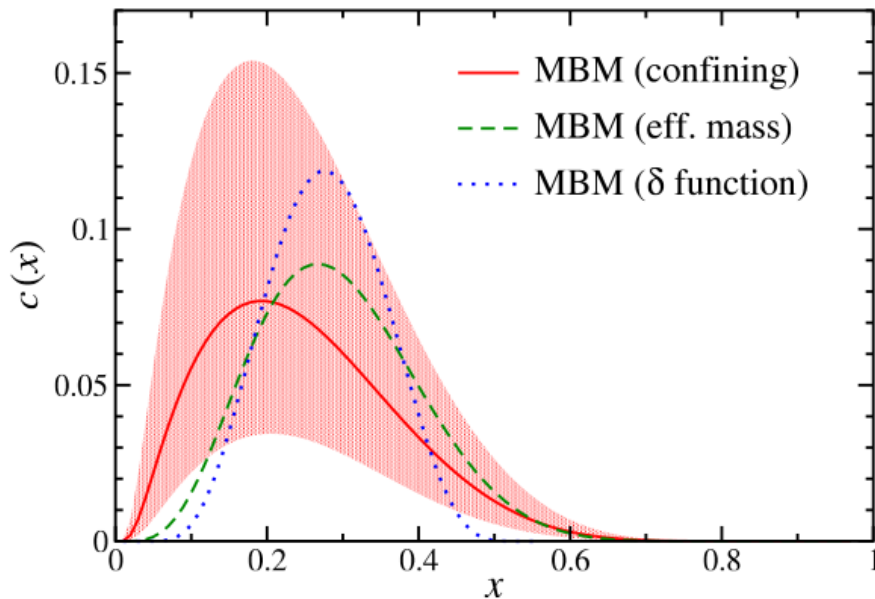
the resulting intrinsic charm depends on UV scales

- tune **universal** cutoff  $\Lambda = \hat{\Lambda}$  to fit **ISR**  $pp \rightarrow \Lambda_c X$  collider data

**multiplicities, momentum sum:**

$$\langle n \rangle_{MB}^{(\text{charm})} = 2.40\% \begin{matrix} +2.47 \\ -1.36 \end{matrix};$$

$$P_c := \langle x \rangle_{IC} = 1.34\% \begin{matrix} +1.35 \\ -0.75 \end{matrix}$$



$$F_2^{c\bar{c}}(x, Q^2) = \frac{4x}{9} [c(x, Q^2) + \bar{c}(x, Q^2)]$$

→ evolve to **EMC** scale,  $Q^2 = 60 \text{ GeV}^2$

low- $x$  H1/ZEUS data check *massless* **DGLAP** evolution

e.g., a 1<sup>st</sup> comprehensive fit including data on  $F_2^{c\bar{c}}$

P. Jimenez-Delgado, TJH, J. T. Londergan and W. Melnitchouk; PRL 114, no. 8, 082002 (2015).

26 sets:

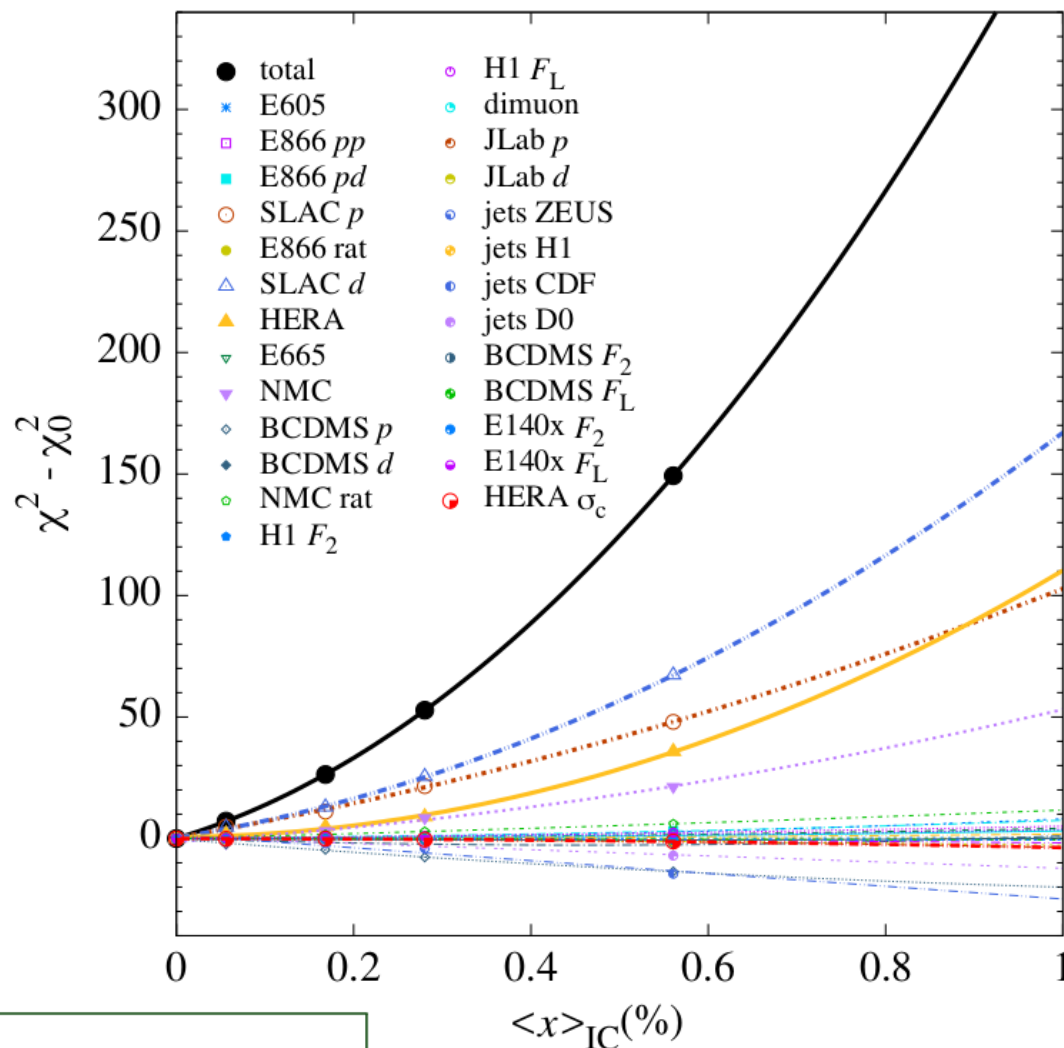
$$N_{dat} = 4296$$

$$Q^2 \geq 1 \text{ GeV}^2$$

$$W^2 \geq 3.5 \text{ GeV}^2$$



\*\* HTs, TMCs,  
smearing...



• constrain:

$$\langle x \rangle_{IC} = \int_0^1 dx x \cdot [c + \bar{c}](x)$$

... 'total IC momentum'

without the EMC data on  $F_2^{c\bar{c}}$

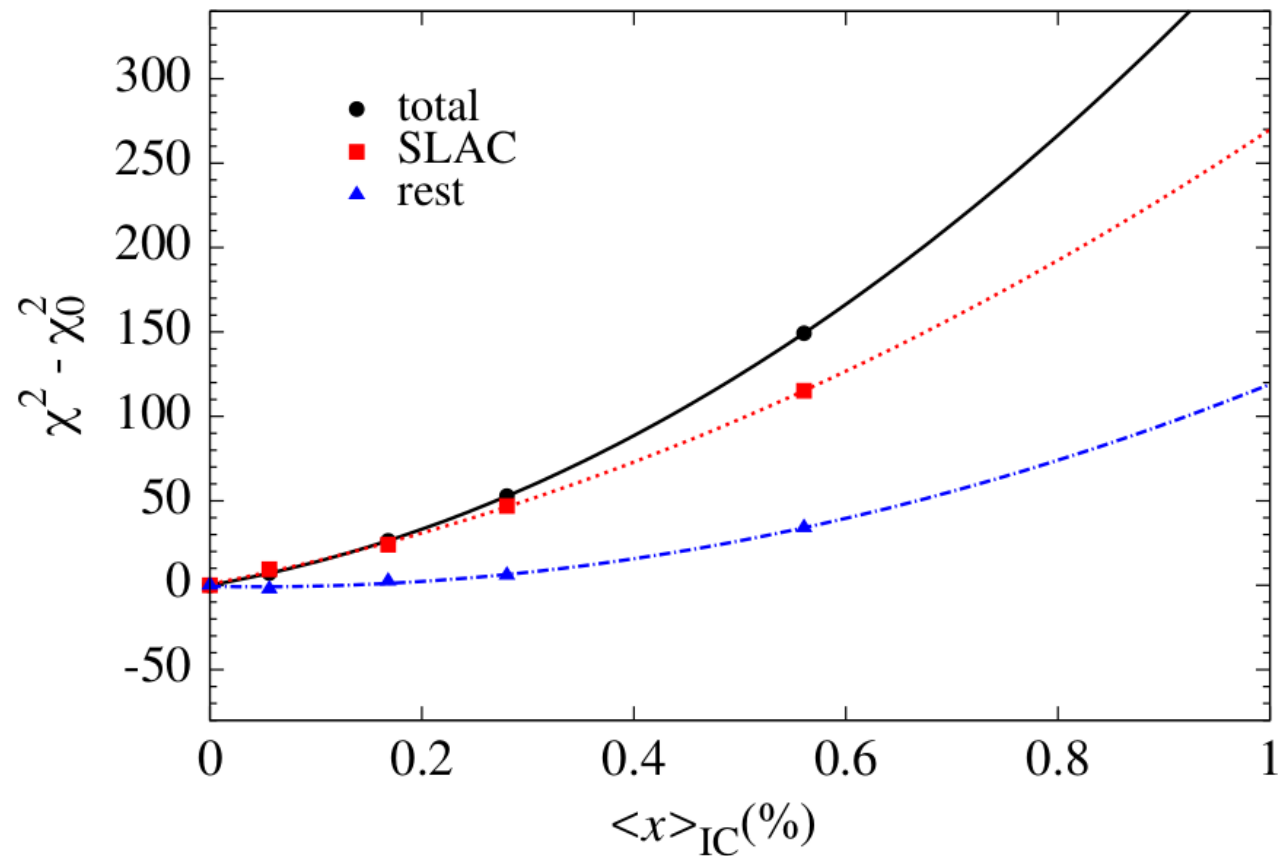
**IC is severely constrained via mom. sum rule via light-quark degrees of freedom**

SLAC *ep, ed* data!

$$\langle Q^2 \rangle \sim 15 \text{ GeV}^2$$

$$0.06 \leq x \leq 0.9$$

$$(\chi^2/N_{dat} \sim 1.25)$$



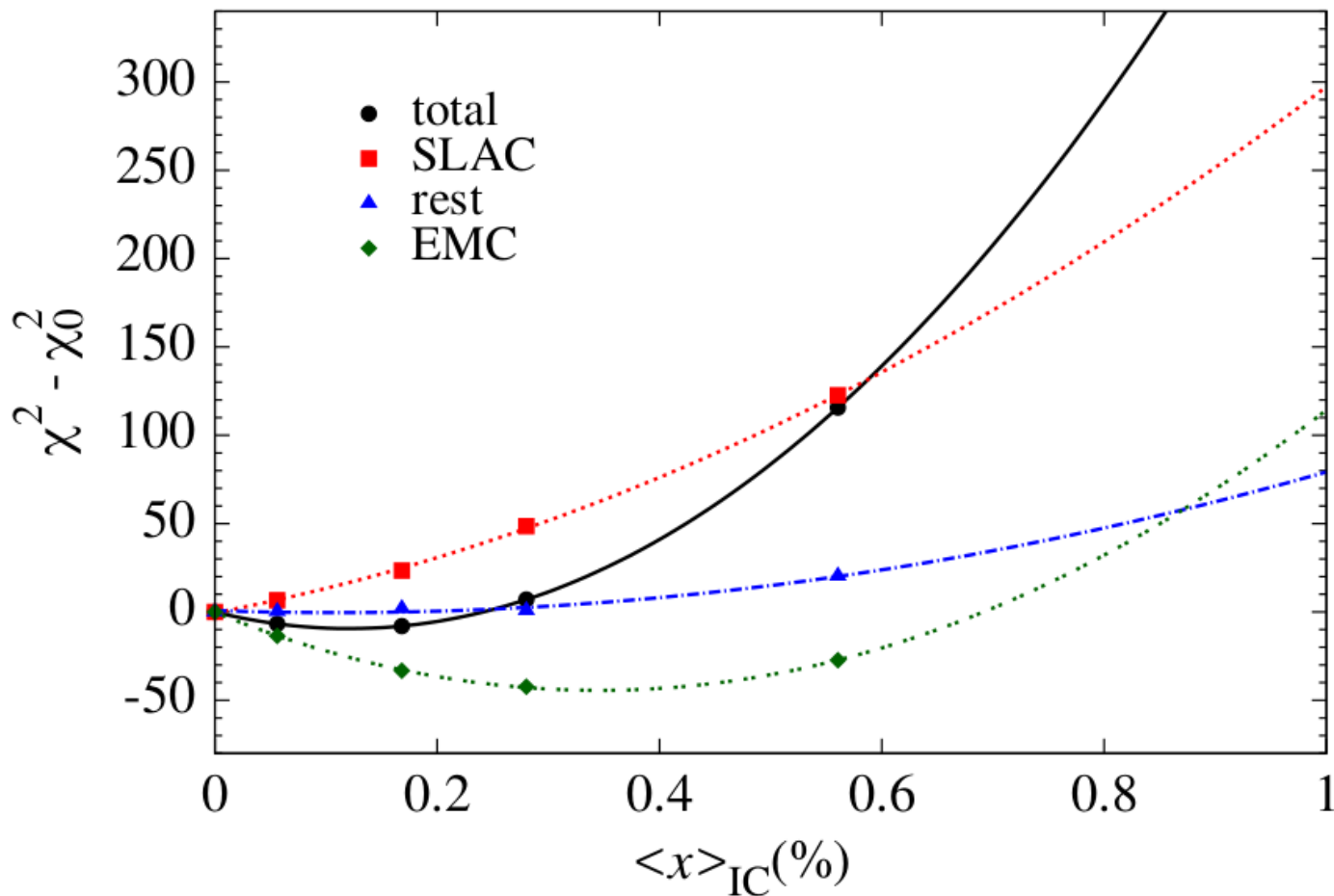
'SLAC + REST'  $\implies \langle x \rangle_{IC} < 0.1\%$ ; at  $5\sigma$  !

'REST' only  $\implies \langle x \rangle_{IC} < 0.1\%$ ; at  $1\sigma$

cf.  $\langle x \rangle_{IC} \lesssim 2\%$  CT14 fits with IC [Hou et al., arXiv:1707.00657]

N.B.: different tolerances:  $\Delta\chi^2 = 1$  vs.  $\Delta\chi_{CT}^2 = 100$

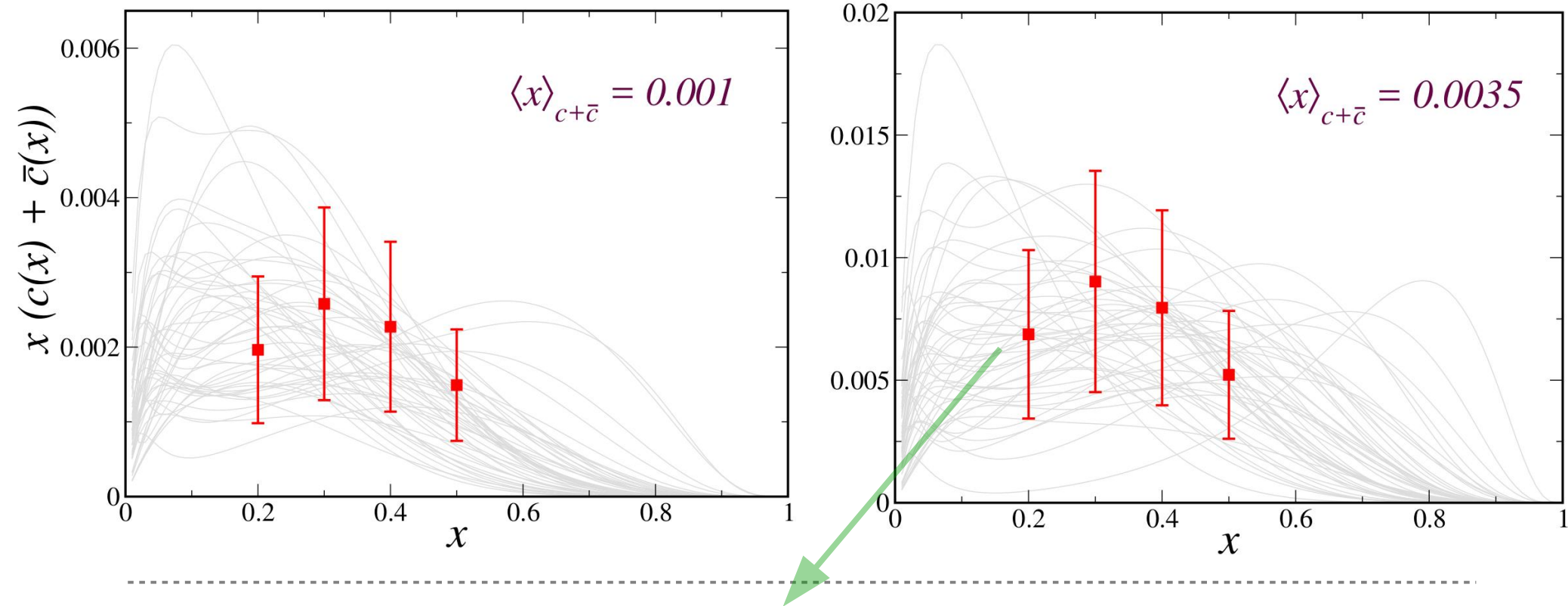
the EMC data prefer modest IC, but do not fit well...



EMC alone:  $\langle x \rangle_{IC} = 0.3 - 0.4\%$

+ **SLAC**/**REST**:  $\langle x \rangle_{IC} = 0.13 \pm 0.04\%$

...but  $F_2^{c\bar{c}}$  poorly fit —  $\chi^2 \sim 4.3$  per datum!

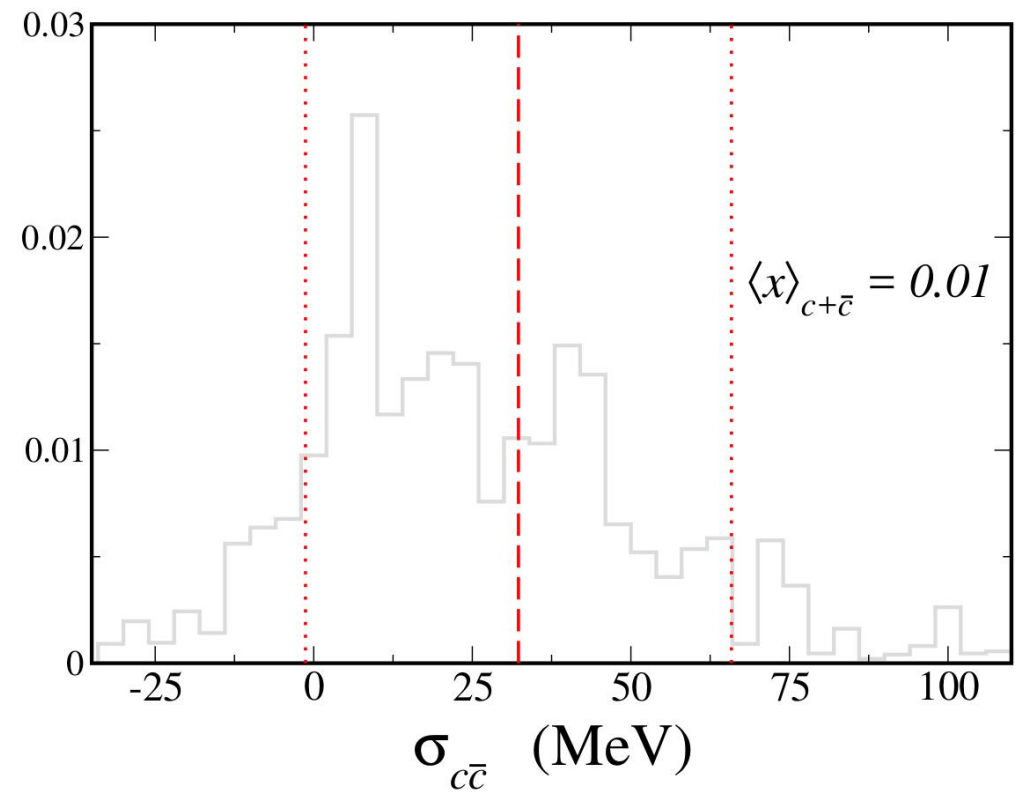
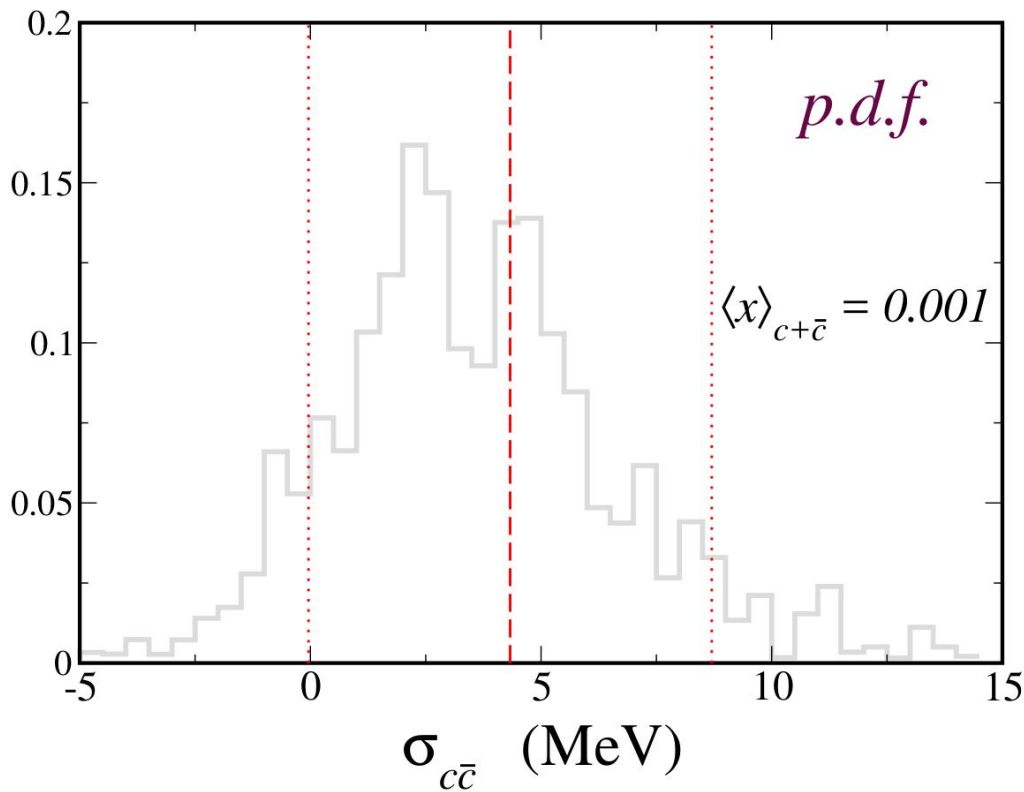


- we constrain the model with hypothetical **pseudo-data** (taken from the 'confining' MBM) of a given  $\langle x \rangle_{\text{IC}} \pm 50\%$

➔ (input data normalizations are inspired by the just-described global analysis)

$$\left\{ \begin{array}{ll} \langle x \rangle_{\text{IC}} = 0.001 & \text{[ upper limit tolerated by the full fit/dataset ]} \\ \langle x \rangle_{\text{IC}} = 0.0035 & \text{[ central value preferred by EMC data alone ]} \end{array} \right.$$

- rather than traditional  $\chi^2$  minimization, the model space is instead explored using **Bayesian methods**



---


$$\sigma_{c\bar{c}} = 4.3 \pm 4.4 \text{ MeV} \quad (\gamma = 3 \text{ interaction}) \quad \sigma_{c\bar{c}} = 32.3 \pm 33.6 \text{ MeV}$$

- we find better concordance cf. existing **lattice determinations**, for somewhat larger IC magnitudes; also, close correlation with the DIS sector -

$$\sigma_{c\bar{c}} = 94 (31) \text{ MeV} \quad (\chi\text{QCD}) \quad \vdots \quad = 67 (34) \text{ MeV} \quad (\text{MILC})$$

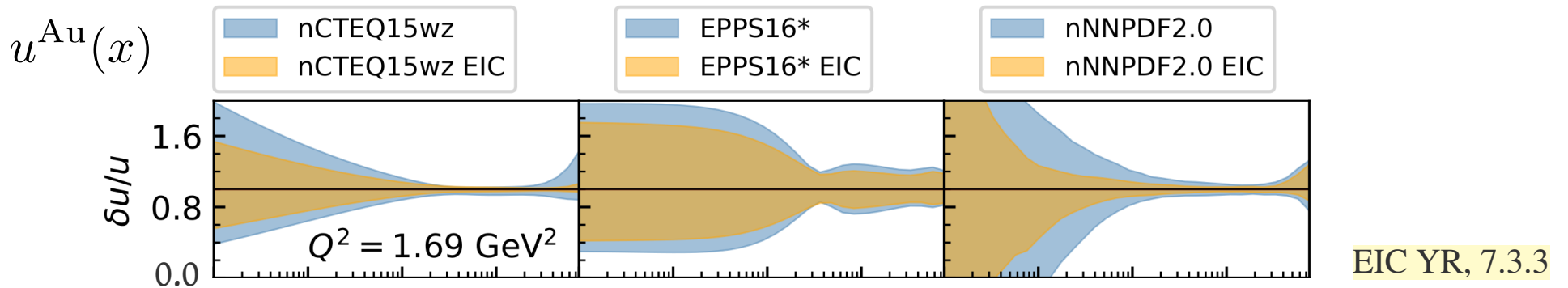
$${}^1\text{Abdel-Rehim et al., Phys. Rev. Lett. } \mathbf{116}, 252001 (2016). \quad \sigma_{c\bar{c}} = 79 (21) \binom{12}{8} \text{ MeV} \quad (\text{AR})^1$$

**bigger point:** lattice calculations can directly inform the IC PDF question

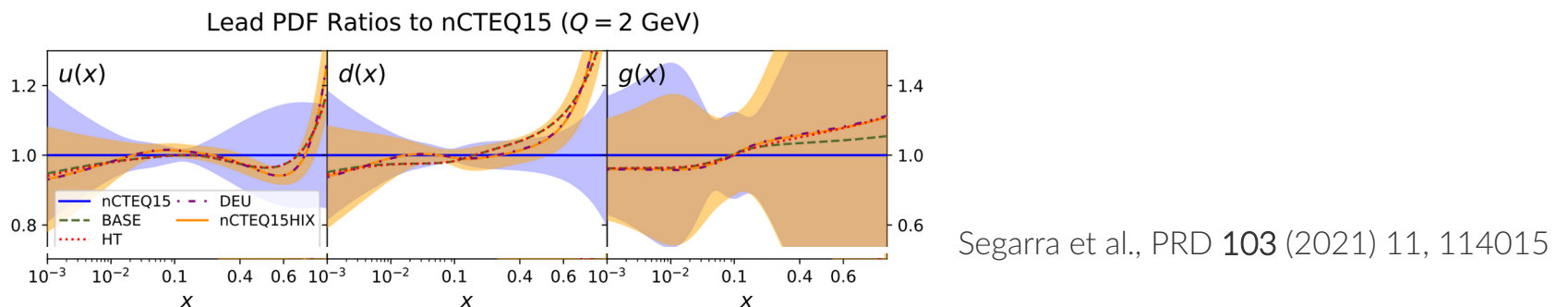


# understanding nuclear effects

→ EIC: measure only “clean” DIS from hadrons; but also explore nuclear medium!



▪ nPDFs can inform nuclear effects in free-nucleon studies and *vice versa*:

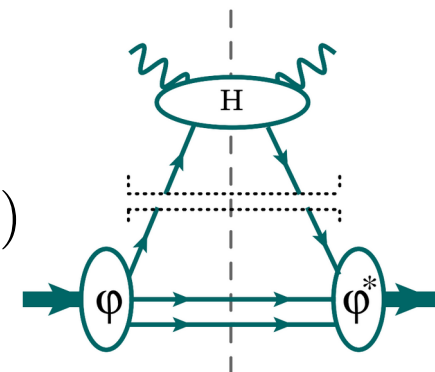


→ nuclear effects: jet production, hadronization; implications for AA, UPC programs

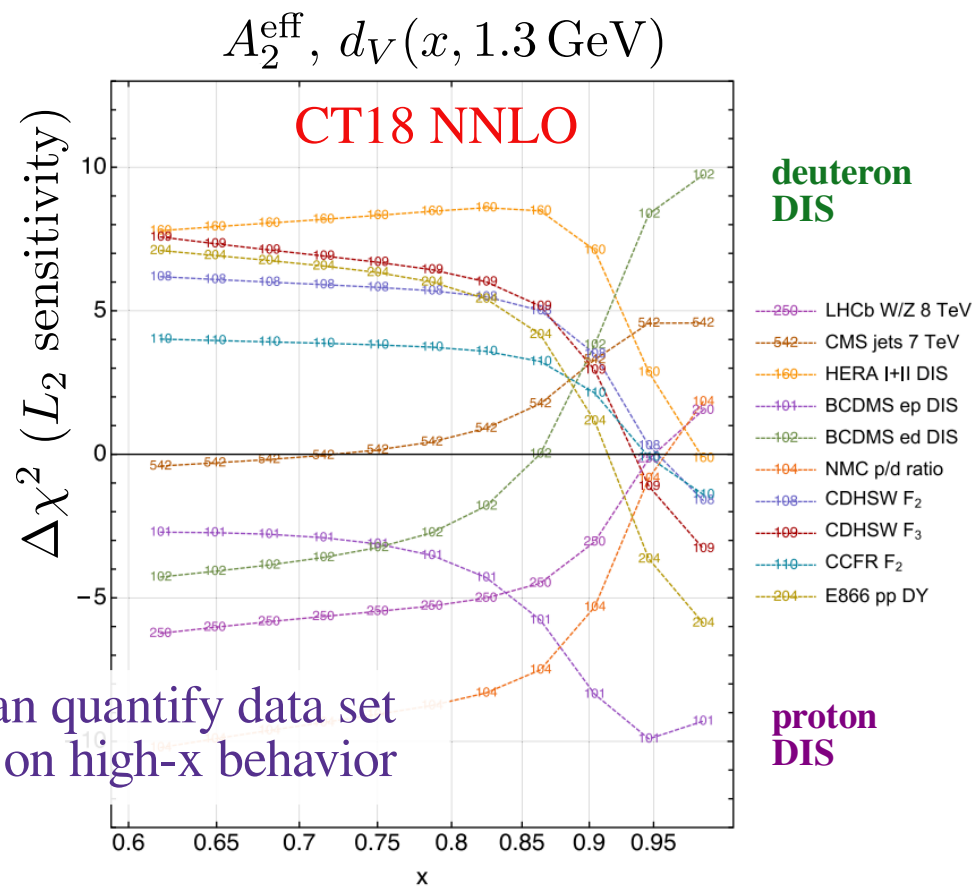
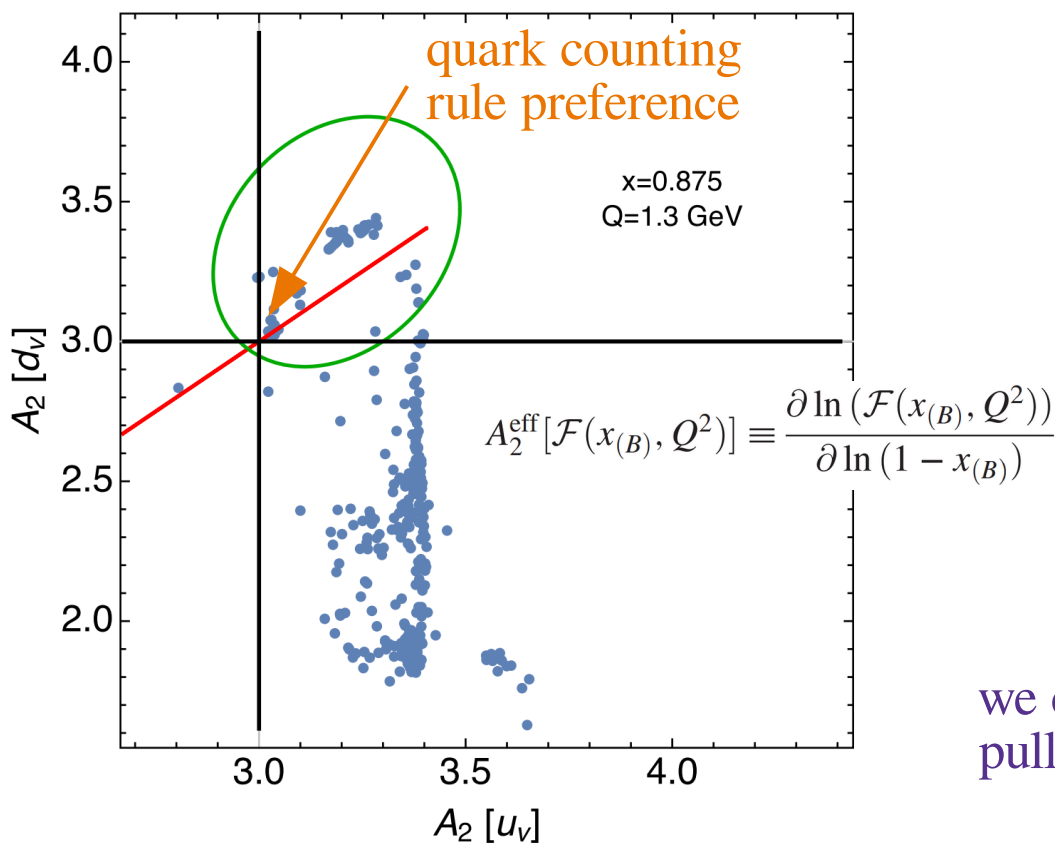
▪ nuclear  $A$  dependence requires copious data: **high luminosity essential**

# extracting high- $x$ dependence in PDF fits

- high- $x$  PDFs, ratios [e.g.,  $d/u$ ] connected to details of proton WF
- behavior at  $x \rightarrow 1$  an important nonpert. discriminator
- CT18, parametrize  $f_{a/A}(x, Q_0^2) = x^{A_{1,a}} (1-x)^{A_{2,a}} \times \Phi_a(x)$



Courtoy and Nadolsky, PRD103, 054029 (2021)



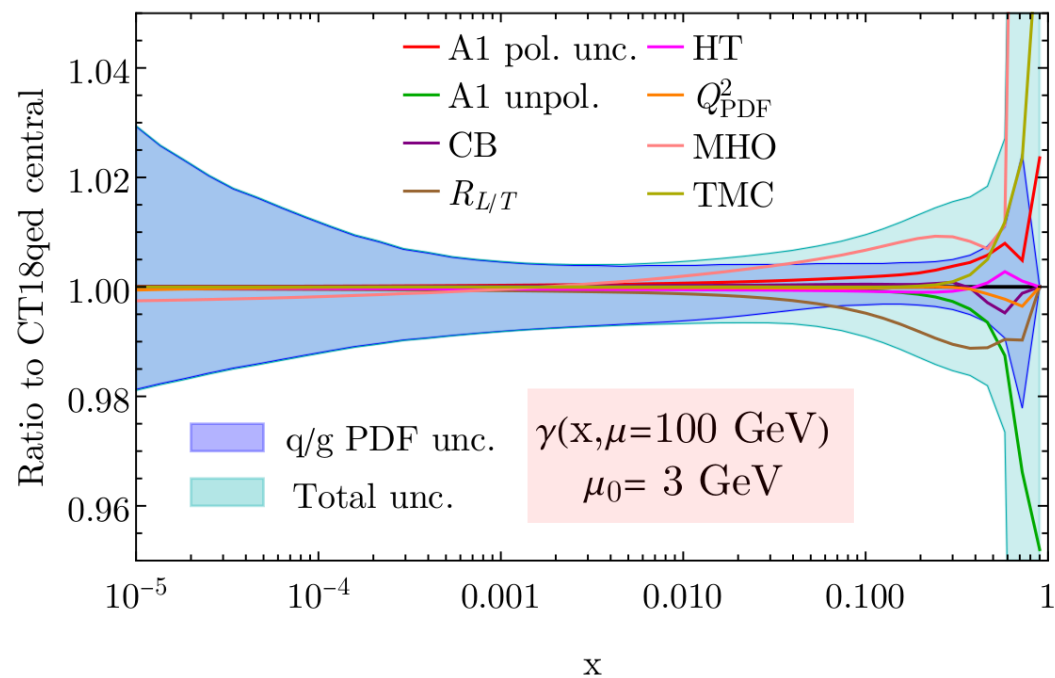
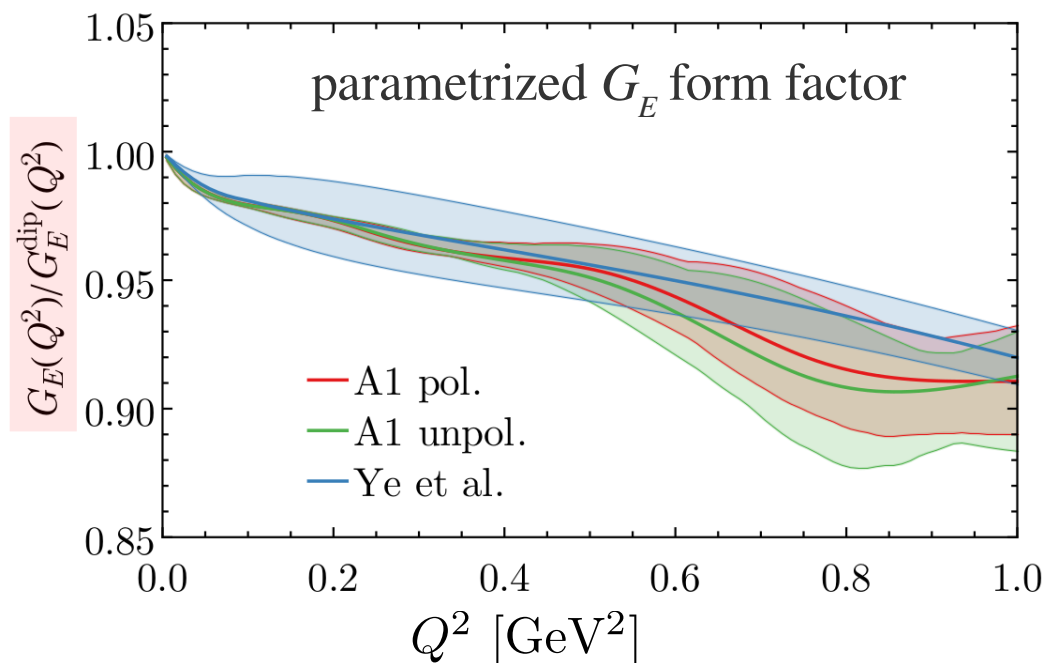
# electroweak precision: photon PDF

- depends on nonperturbative inputs [kinematical cuts alone can't avoid this]
- integrated proton SFs include contributions from low  $Q$ , moderate  $x$

$$x\gamma(x, \mu^2) = \frac{1}{2\pi\alpha(\mu^2)} \int_x^1 \frac{z}{z} \left\{ \int_{\frac{x^2 m_p^2}{1-z}}^{\frac{\mu^2}{1-z}} \frac{Q^2}{Q^2} \alpha_{\text{ph}}^2(-Q^2) \left[ \left( zp_{\gamma q}(z) + \frac{2x^2 m_p^2}{Q^2} \right) F_2(x/z, Q^2) - z^2 F_L(x/z, Q^2) \right] - \alpha^2(\mu^2) z^2 F_2(x/z, \mu^2) \right\} + \mathcal{O}(\alpha^2, \alpha\alpha_s)$$

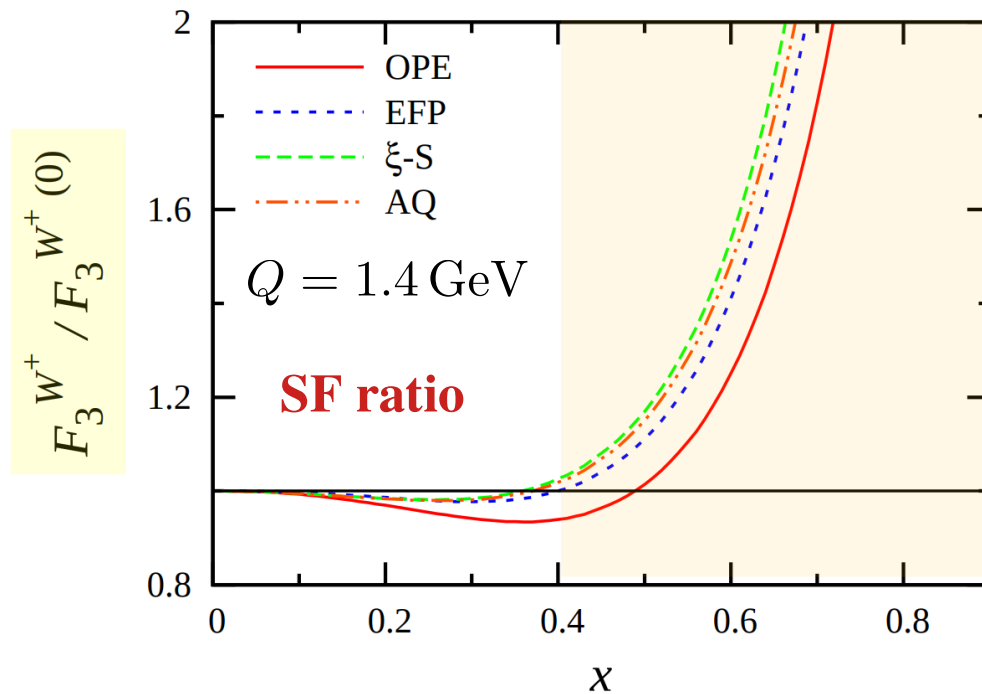
- dependence on Sachs EM form factors; twist-4, resonance prescriptions; ...

[AND quark-gluon PDFs, uncertainties] →



# higher luminosity: understand power-suppressed QCD corrections

- aside from higher-order corrections in  $\alpha_s$  : higher-twist, target-mass corrections



potentially large,  $\sim 1/Q^2$   
large- $x$  effects

crucial for precision in DIS

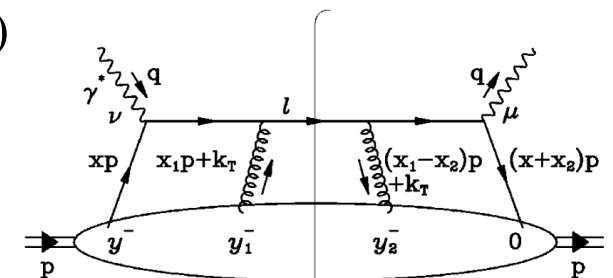
Brady, Accardi, TJH, Melnitchouk:  
PRD84 (2011) 9, 074008

- closely-related to **multi-parton interactions** at high energy:

(jet production in electron-nucleus vs. electron-nucleon DIS)

$$\Delta \langle p_T^2 \rangle \equiv \langle p_T^2 \rangle_{eA} - \langle p_T^2 \rangle_{ep} \quad (\text{jet } p_T \text{ broadening})$$

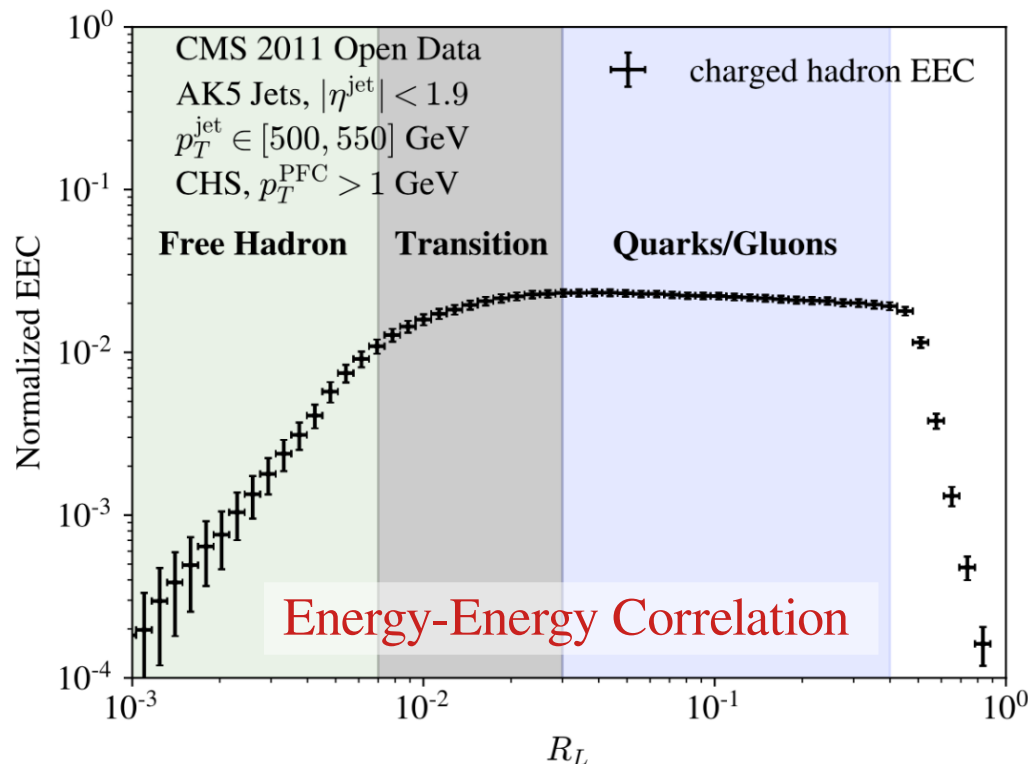
$$\langle p_T^2 \rangle = \int dp_T^2 p_T^2 \frac{d\sigma}{dx_B dQ^2 dp_T^2} / \frac{d\sigma}{dx_B dQ^2}$$



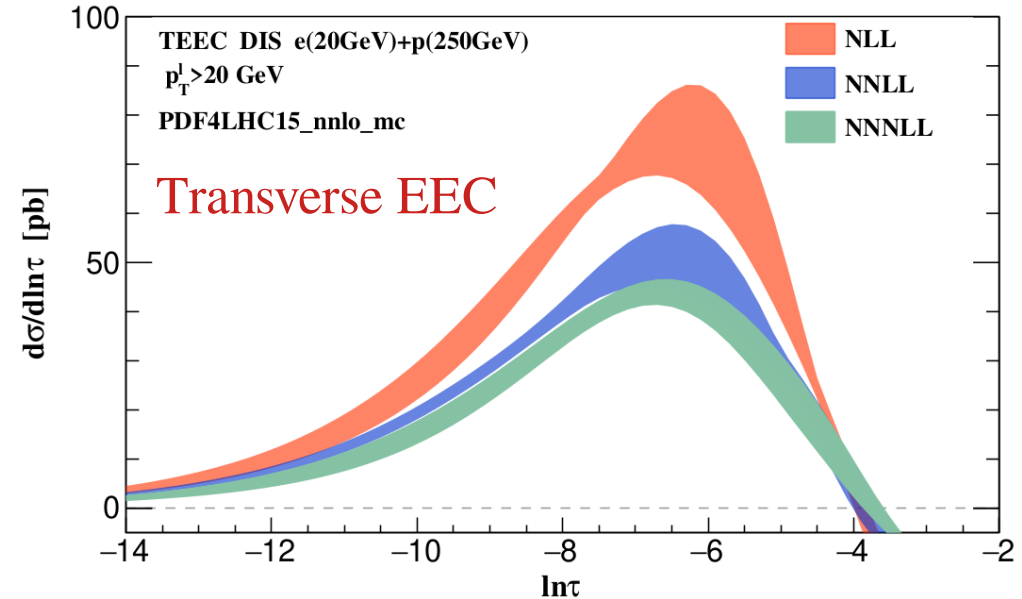
X. Guo, PRD58, 114033 (1998).

# sensitivity to possible ‘new’ QCD measurements

- strong interest in measurements connecting event-level observables to fundamental QCD
- e.g., QCD jets (various observables, constructions)
  - closely related to tests of QCD factorization
- event-shape measurements: energy correlation functions well-explored at LHC



→ explore scaling to EIC kinematics



→ further understanding of TMD physics

- higher luminosity significantly increases relevant cross sections

# EIC and SM inputs: $\alpha_s$

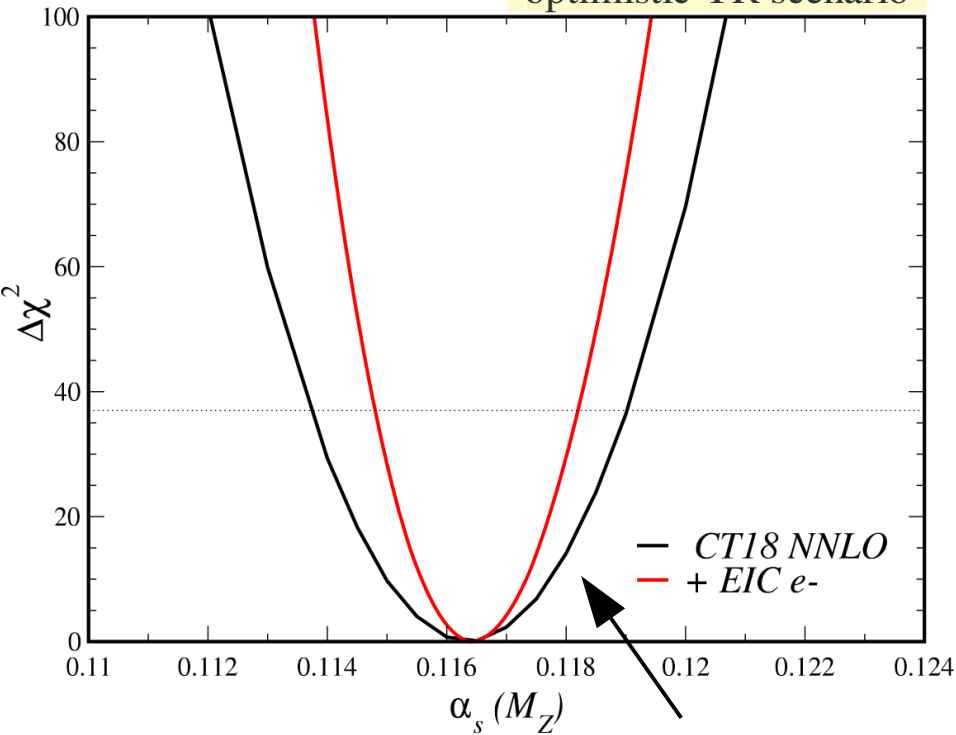
- part of moving toward N<sup>3</sup>LO PDFs, precise determinations needed for  $\alpha_s$

similar argument for  $m_Q$

from inclusive data alone

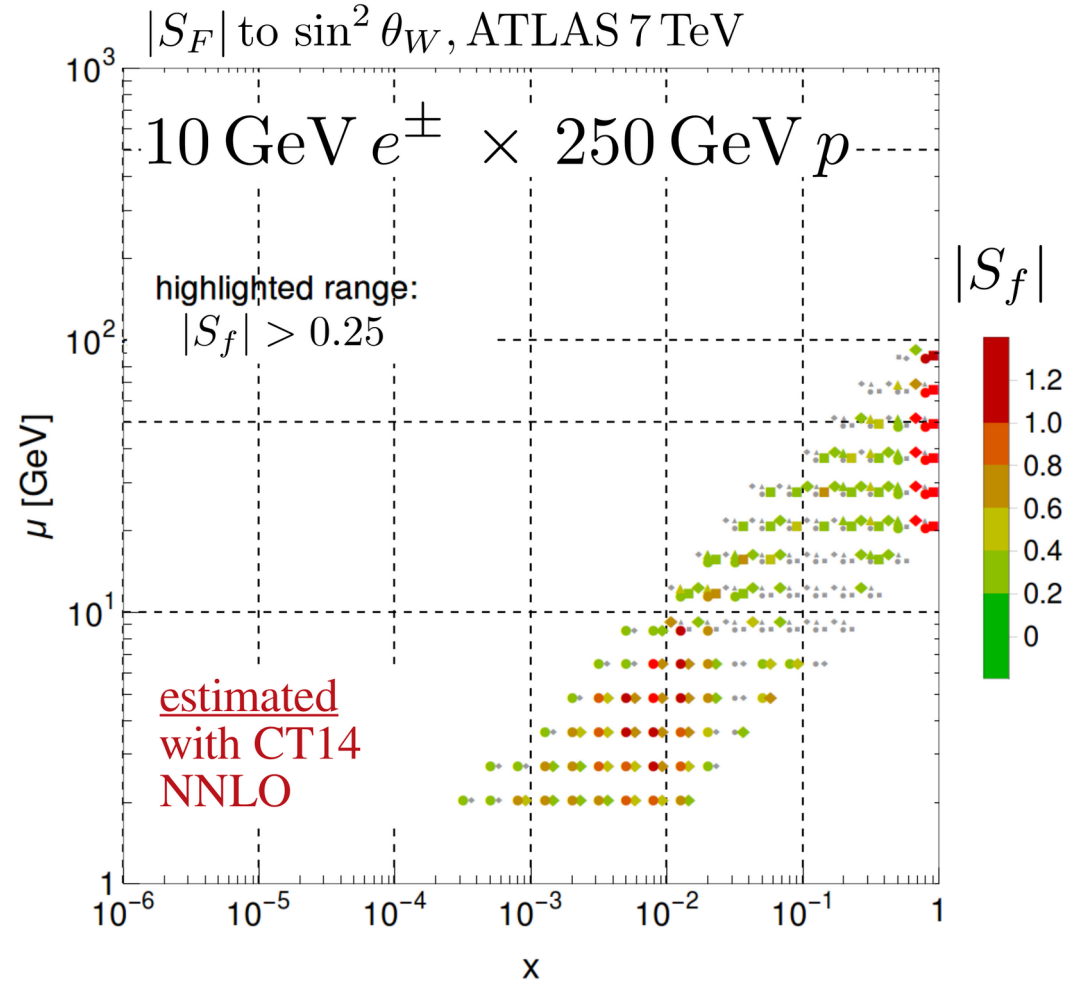
B.-T. Wang et al., PRD **98** (2018) 9.

“optimistic YR scenario”



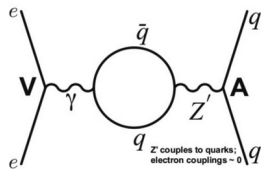
~40% reduction

- also: precise  $\alpha_s$  extractions based on global event shapes;  $N$ -jettiness,  $N$

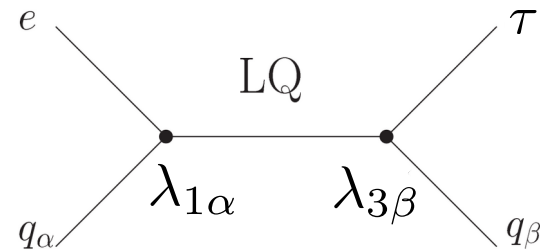


- robust PDF sensitivity to  $\sin^2 \theta_W$  from  $A_{FB}$

- potentially BSM-sensitive extractions of EW quark couplings,  $\sin^2 \theta_W$  through **parity violation**

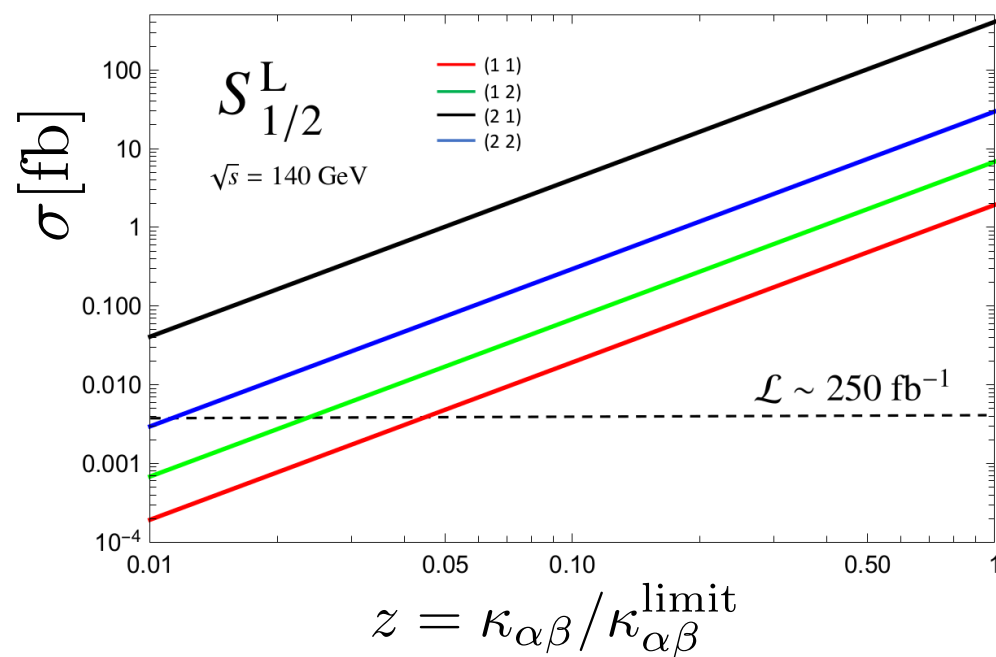
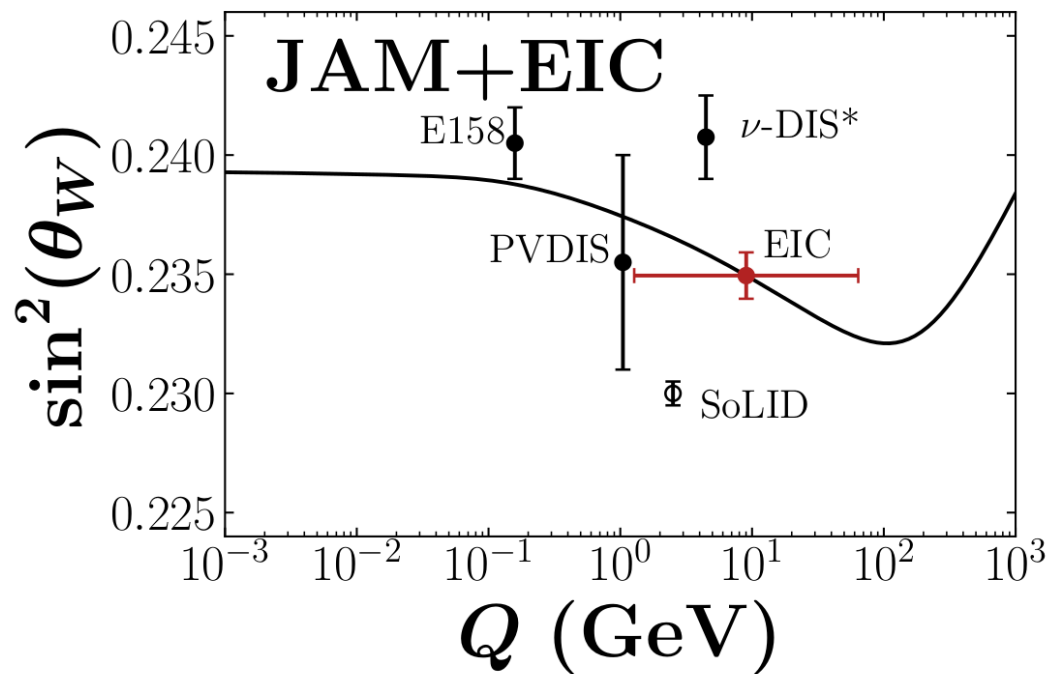


$$A_{PV}^e = \frac{d\sigma_L - d\sigma_R}{d\sigma_L + d\sigma_R}$$

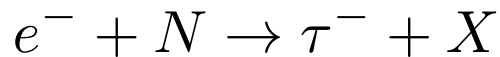


$$\kappa_{\alpha\beta} = \lambda_{1\alpha} \lambda_{3\beta} / M_{LQ}^2$$

EIC YR, 7.5.1



- more direct SM tests also possible: searches for charged-lepton flavor violation (CLFV)

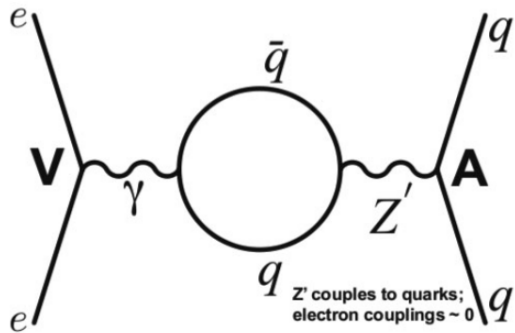


# the electroweak sector and **New Physics** searches at EIC

- if measured to sufficient precision, the quark-level electroweak couplings may be sensitive to an extended EW sector, e.g.,  $Z'$

$$\mathcal{L}^{\text{PV}} = \frac{G_F}{\sqrt{2}} \left[ \bar{e} \gamma^\mu \gamma_5 e \left( C_{1u} \bar{u} \gamma_\mu u + C_{1d} \bar{d} \gamma_\mu d \right) + \bar{e} \gamma^\mu e \left( C_{2u} \bar{u} \gamma_\mu \gamma_5 u + C_{2d} \bar{d} \gamma_\mu \gamma_5 d \right) \right]$$

$$C_{1u} = -\frac{1}{2} + \frac{4}{3} \sin^2 \theta_W$$



- a unique strength of an EIC is its combination of very high precision and **beam polarization**, which allows the observation of **parity-violating helicity asymmetries**:

$$A^{\text{PV}} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} \quad (\text{R/L : } e^- \text{ beam helicities})$$

selects  $\gamma$ - $Z$  interference diagrams!

TJH and Melnitchouk, PRD77, 114023 (2008).

$$A^{\text{PV}} = - \left( \frac{G_F Q^2}{4\sqrt{2}\pi\alpha} \right) (Y_1 a_1 + Y_3 a_3)$$

$$a_1 = \frac{2 \sum_q e_q C_{1q} (q + \bar{q})}{\sum_q e_q^2 (q + \bar{q})}$$

$$a_3 = \frac{2 \sum_q e_q C_{2q} (q - \bar{q})}{\sum_q e_q^2 (q + \bar{q})}$$



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→ with sufficient precision, an EIC (which will be statistics-limited in these measurements) can extract  $\sin^2 \theta_W$

- this measurement is potentially sensitive to the TeV-scale in a complementary fashion to energy-frontier searches!

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N.B.: extractions are dependent upon knowledge of the PDFs