

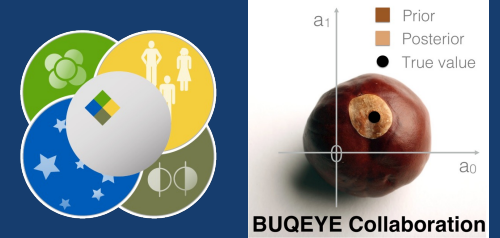
# Equation of State of Neutron-Rich Matter and Implications for Neutron Stars

OHIO  
UNIVERSITY

Christian Drischler

14th Conference on the Intersections of Particle and Nuclear Physics 2022

September 1, 2022



Ribbon-cutting ceremony  
May 2, 2022



See also Brad Sherrill's talk (Friday):  
*Status and Prospects with FRIB*



Facility for Rare Isotope Beams  
at Michigan State University

Samuel L. Stanley  
President of MSU

Jennifer M. Granholm  
Secretary of Energy



# Recent neutron star observations

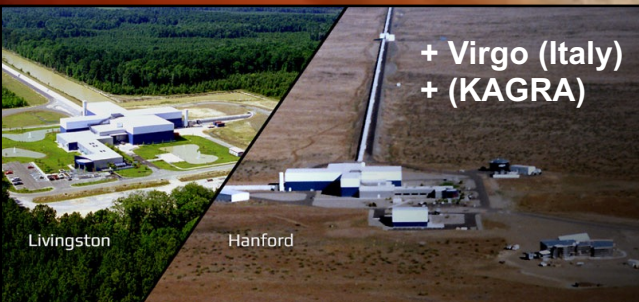
heaviest & fastest known  
galactic neutron star

$$M = 2.35 \pm 0.17 M_{\odot}$$

J0952-0607: Romani *et al.* (2022)

What is the maximum  
neutron star mass?

GW170817  
GRB170817A  
AT2017gfo



multi-messenger  
astronomy



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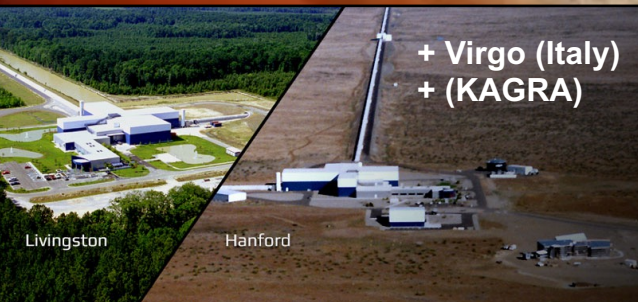
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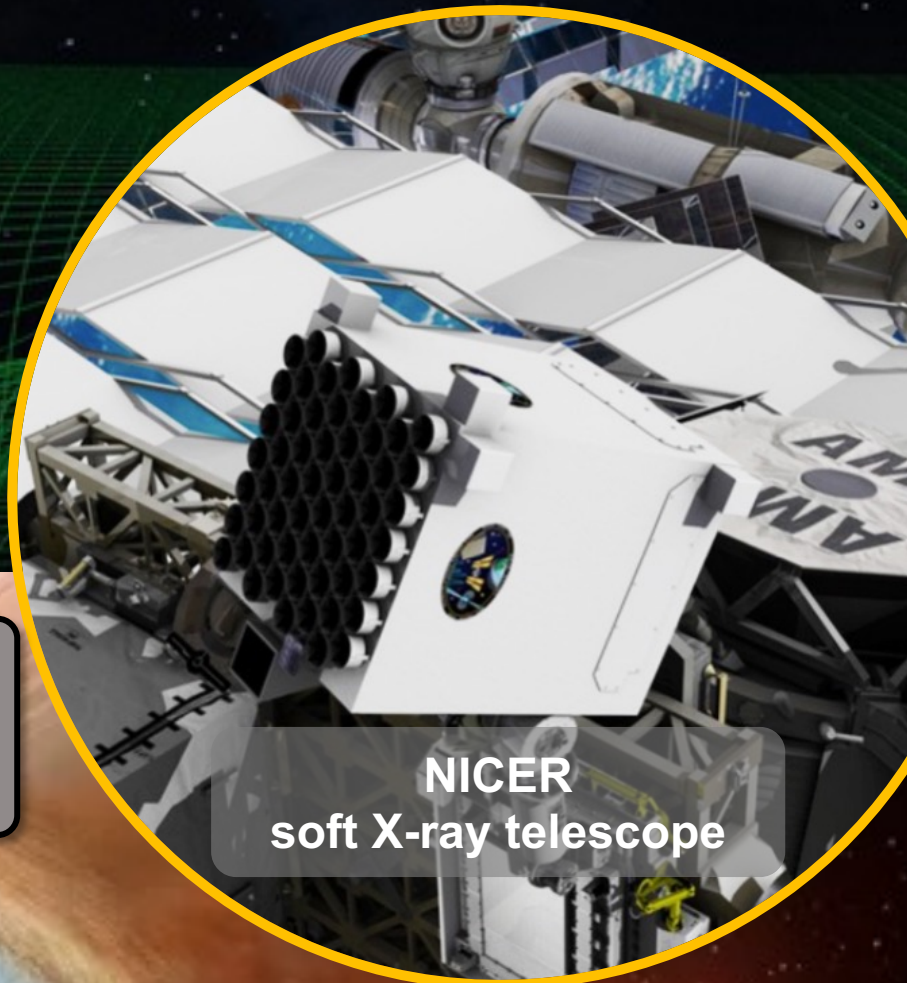
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See also Ben Margalit's talk (this session):  
*Mergers, kilonovae, and two-solar-mass neutron stars:  
What does astrophysics tell us about the nuclear EOS?*



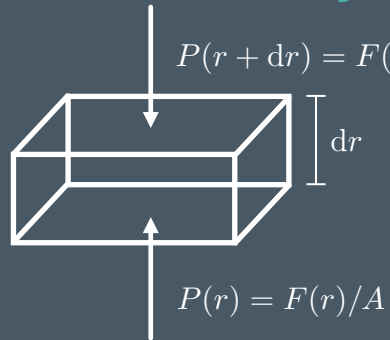
See also K. Chatzilioannou's talk (Saturday):  
*GWs from binary neutron stars and  
neutron star black-hole mergers*



multi-messenger  
astronomy

# Structure of cold neutron stars

hydrostatic equilibrium

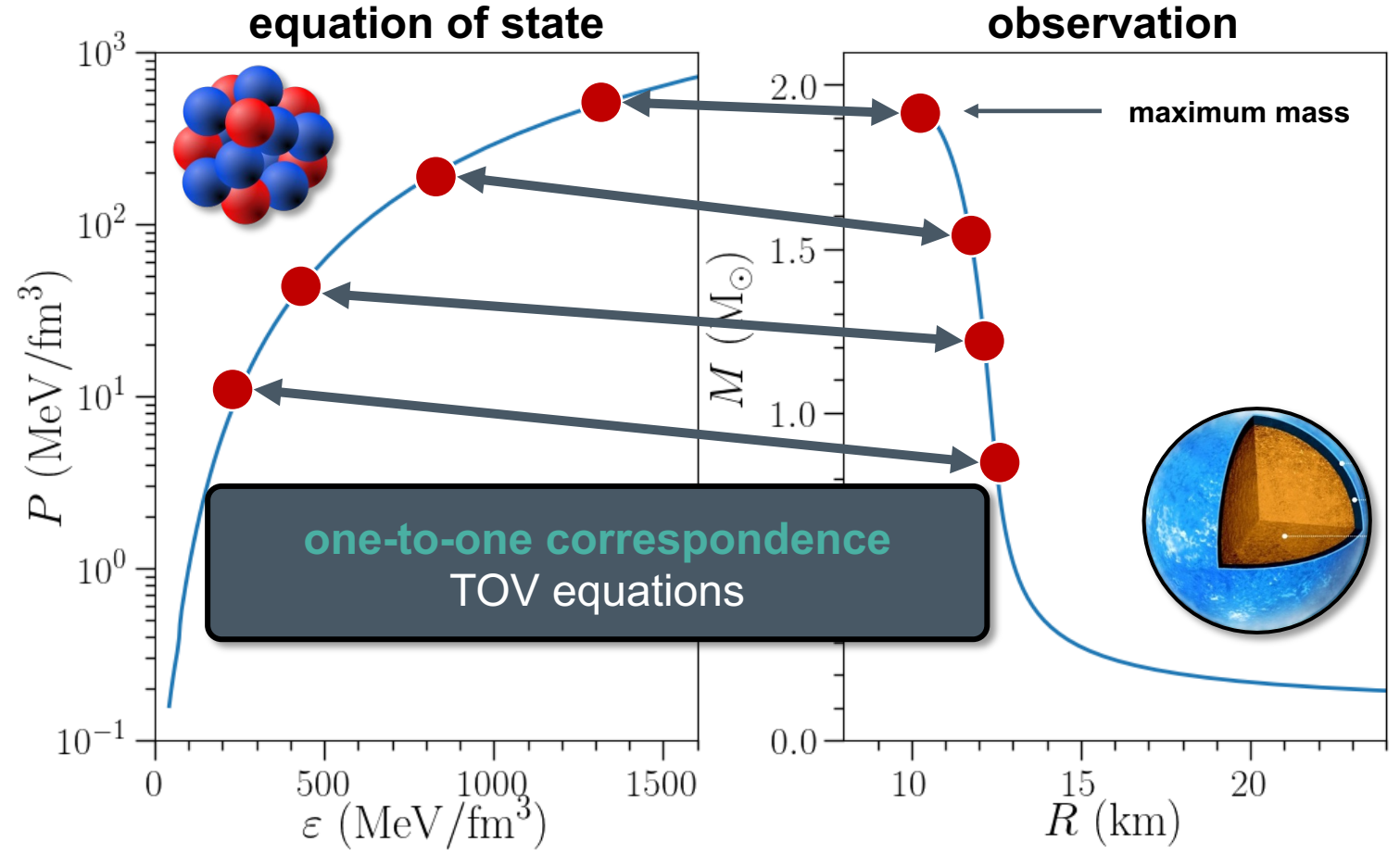
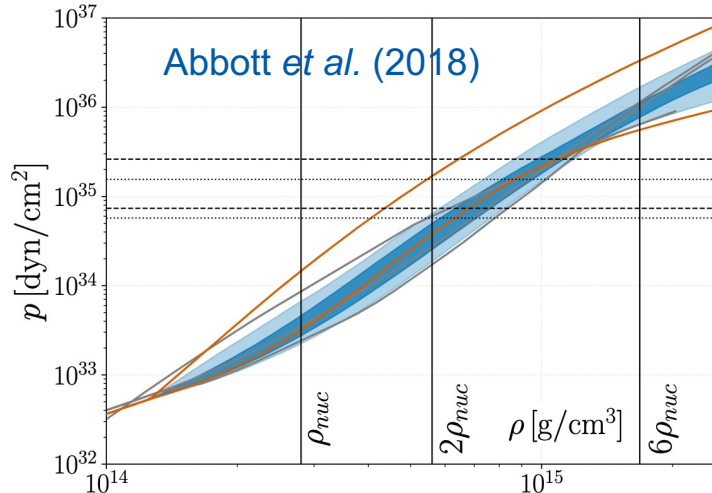


+

General Relativity

Tolman–Oppenheimer–Volkoff equation

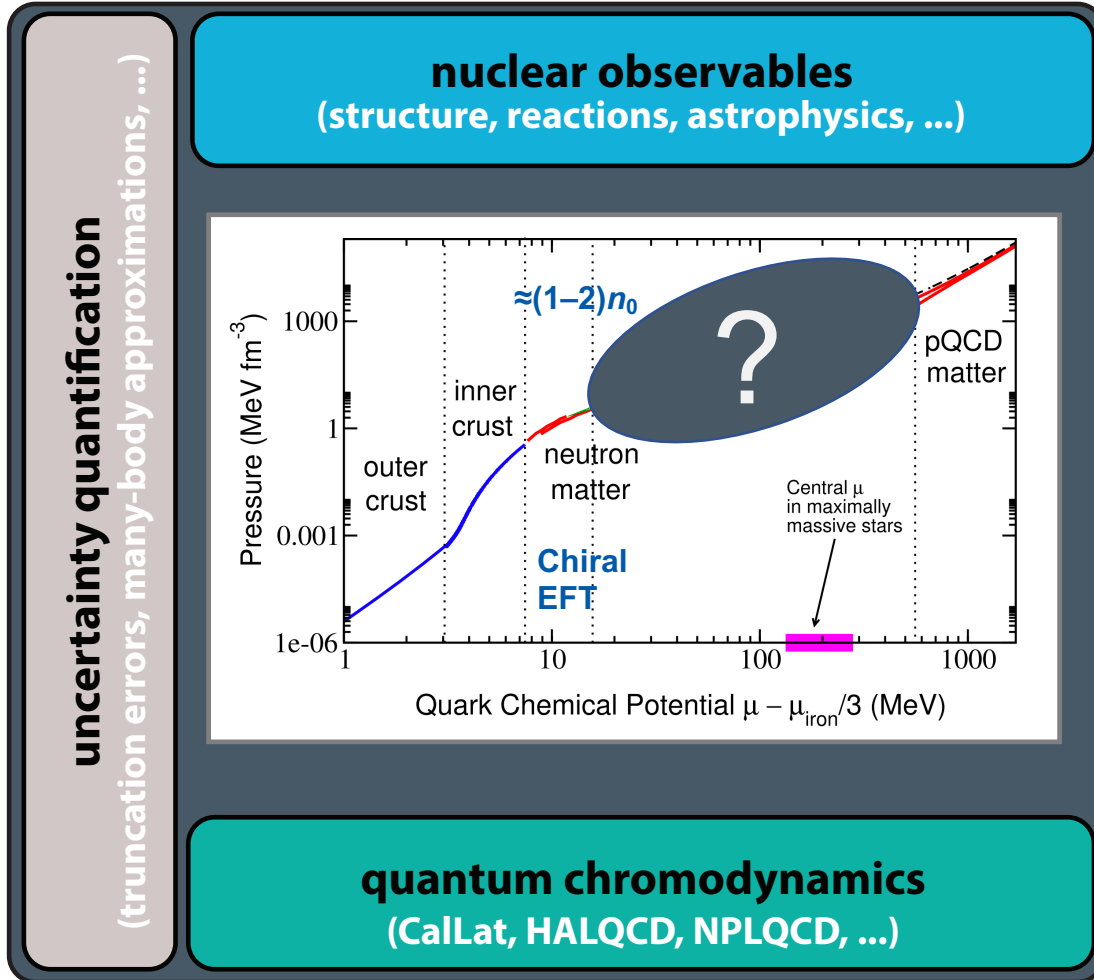
$$\frac{dP}{dr} = - \frac{(\varepsilon + P)(m + 4\pi r^3 P)}{r(r - 2m)} \quad \frac{dm}{dr} = 4\pi r^2 \varepsilon$$



Credit: A. Steiner

The general relativistic equation for hydrostatic equilibrium determines the neutron star structure



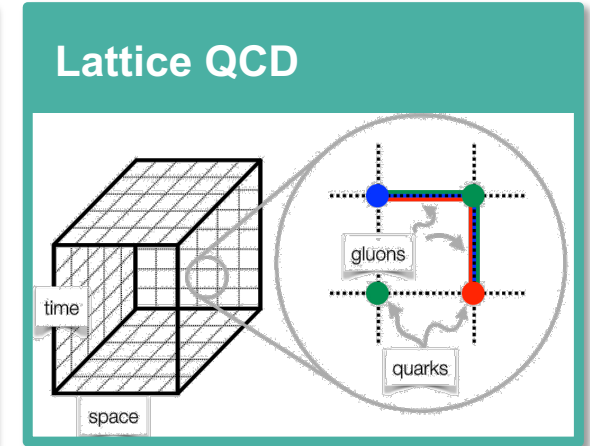
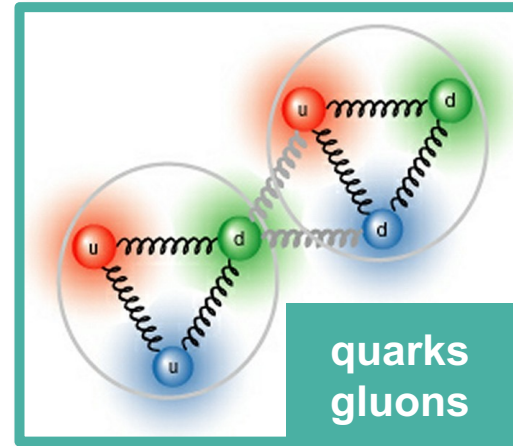


uncertainty quantification  
(truncation errors, many-body approximations, ...)

Here: nuclear equation of state (EOS)  
energy per particle (and derived quantities)

$$\frac{E}{A}(n, \delta, T)$$

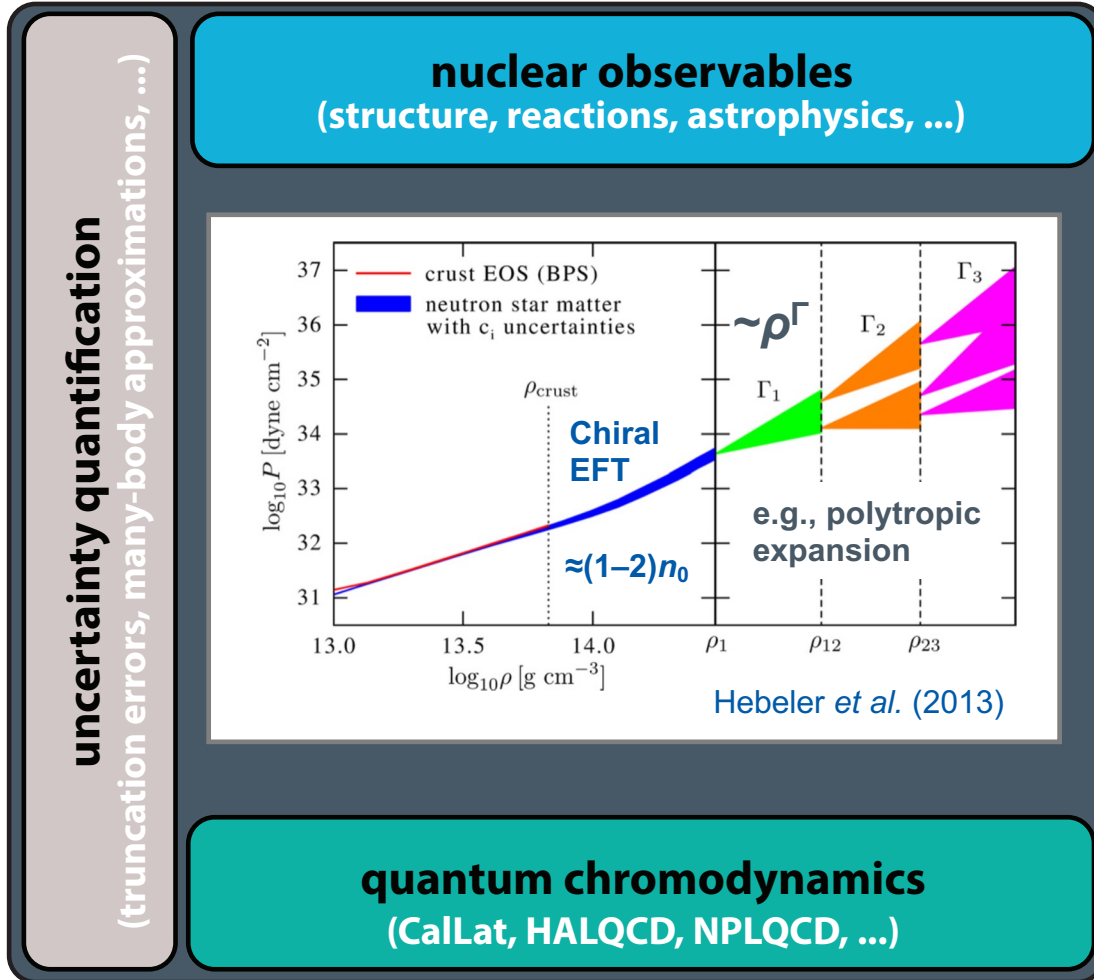
baryon density  $n$   
neutron excess  $\delta$   
temperature  $T (= 0)$



theory of strong interactions

QCD is nonperturbative at the low energies  
relevant for nuclear physics (cf. pQCD & LQCD)

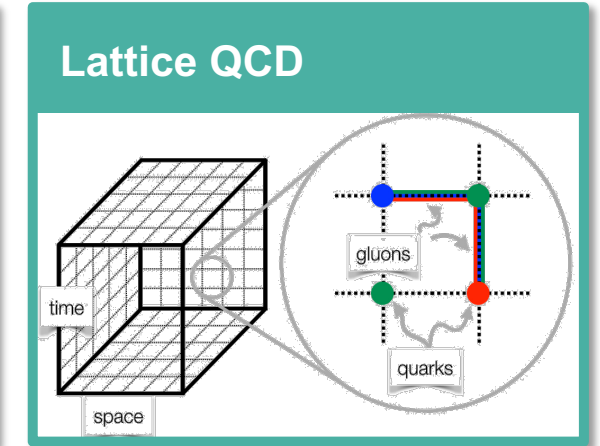
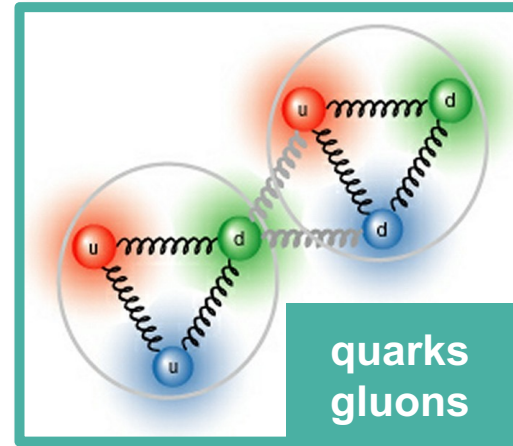




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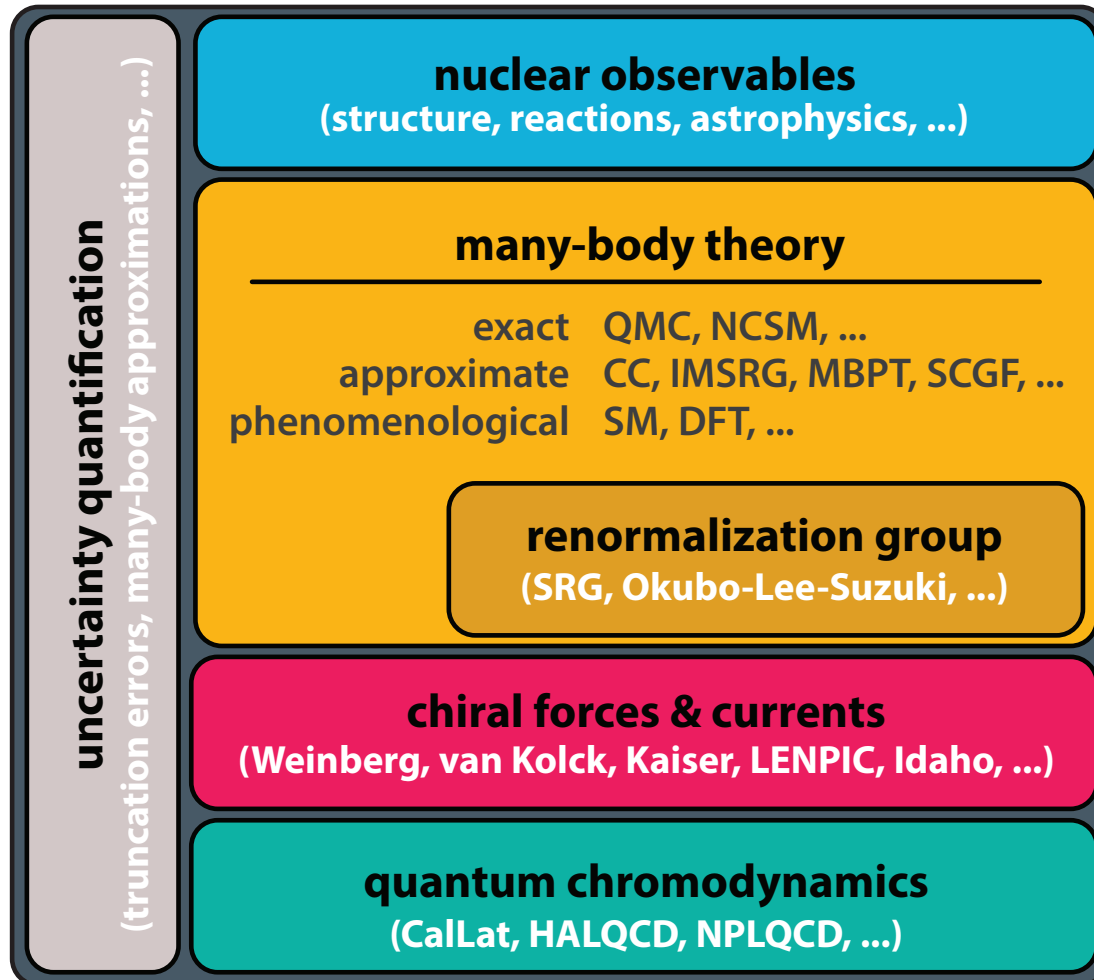
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### computational framework

solves the (many-body) Schrödinger equation  
requires a nuclear potential as input

### chiral effective field theory

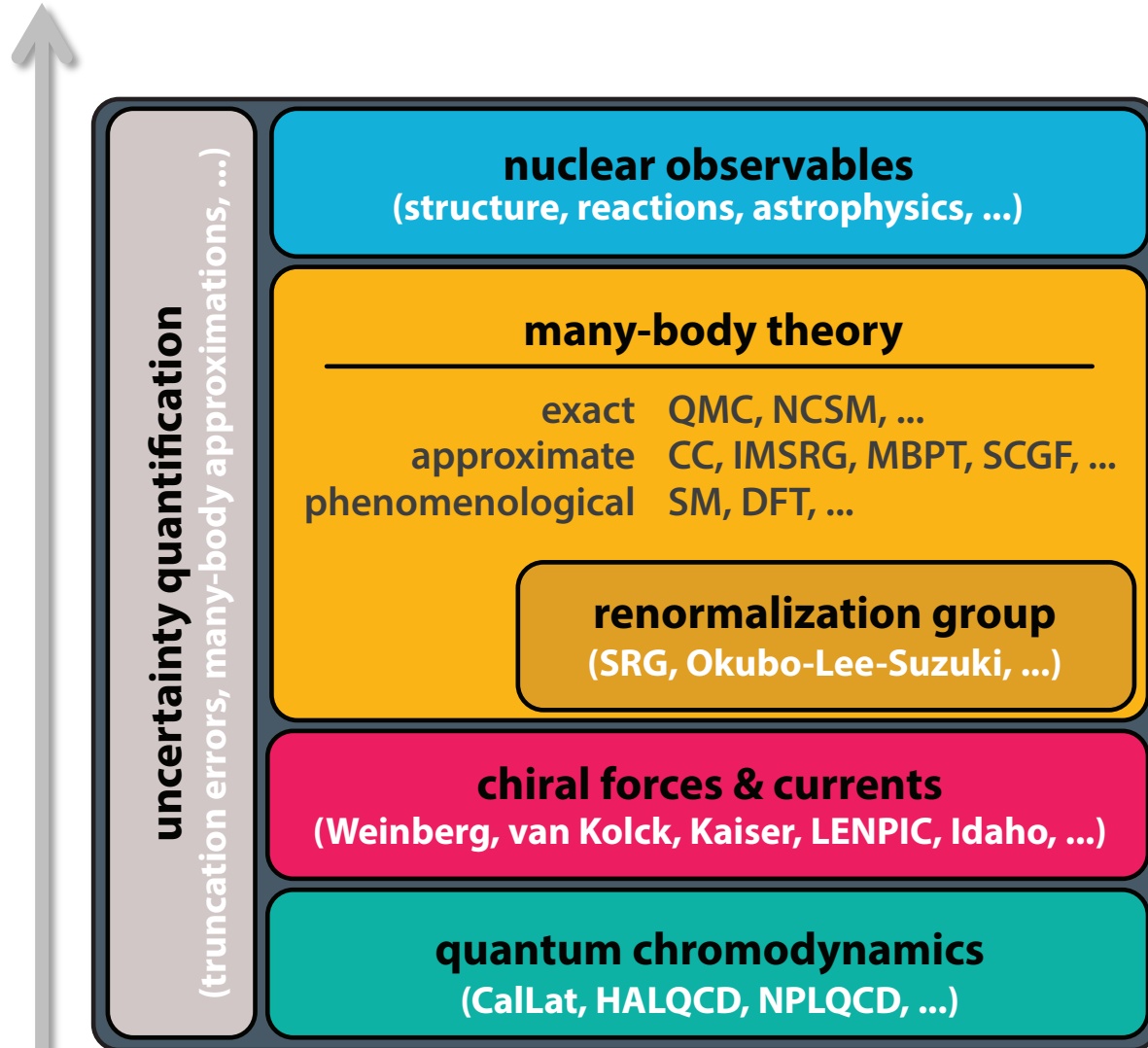
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**Recent highlight:** *Ab initio* predictions link the neutron skin  
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See also Heiko Hergert's slides:  
*A Status Update on  
Ab Initio Calculations in Nuclear Physics*

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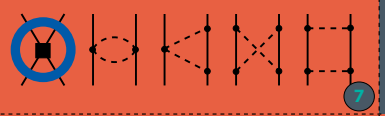

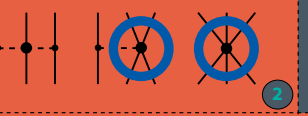


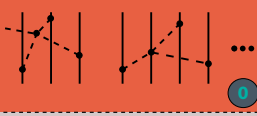
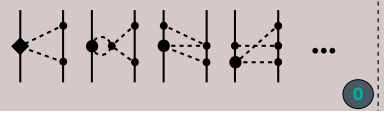
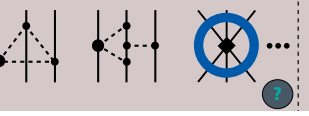
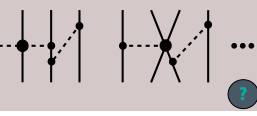
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# Rigorous UQ for nuclear matter



CD, Furnstahl, Melendez,  
Phillips, PRL 125, 202702

	NN forces	3N forces	4N forces
LO ( $Q^0$ )	 2	$Q = \max\left(\frac{p}{\Lambda_b}, \frac{m_\pi}{\Lambda_b}\right)$	
NLO ( $Q^2$ )	 7		
N <sup>2</sup> LO ( $Q^3$ )	 0	 2	
N <sup>3</sup> LO ( $Q^4$ )	 12	 0	 0
N <sup>4</sup> LO ( $Q^5$ )	 0	 7	 7

## Chiral Effective Field Theory (nucleons & pions)

dominant approach for deriving *microscopic* interactions consistent with the symmetries of *low-energy* QCD

three- and four-neutron forces predicted through N<sup>3</sup>LO

See also Evgeny Epelbaum's slides (LENPIC):  
*Chiral EFT for low-energy nuclear physics*

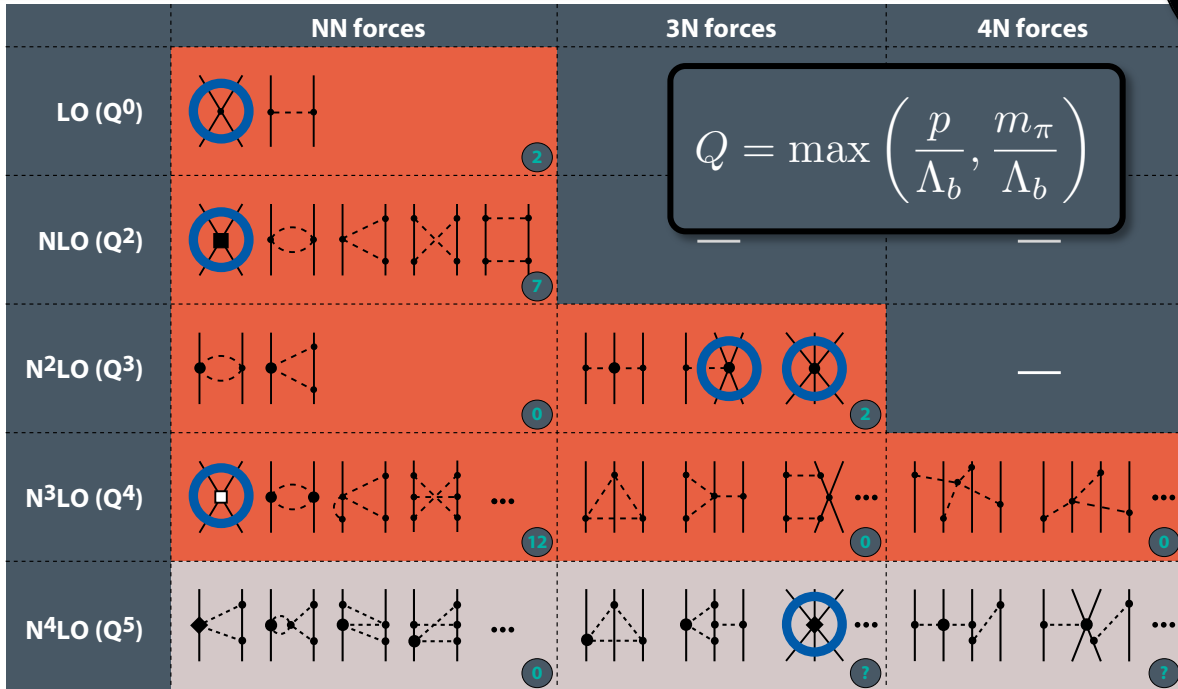
See also Maria Piarulli's slides:  
*Analyzing the nuclear interaction: challenges and new opportunities*



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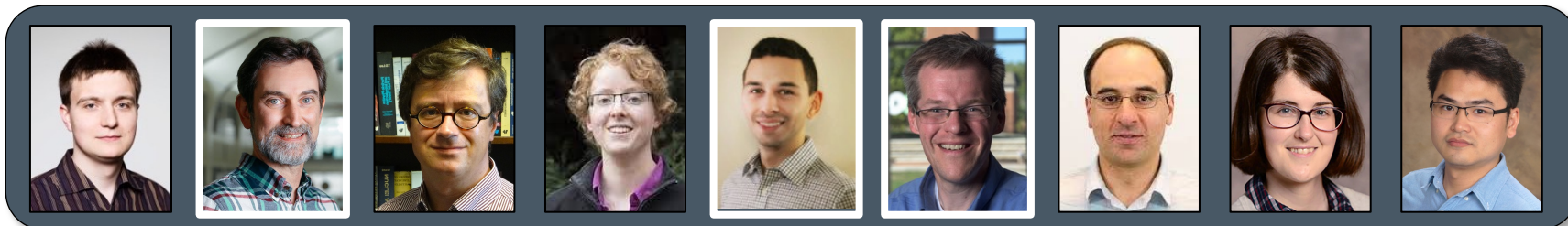
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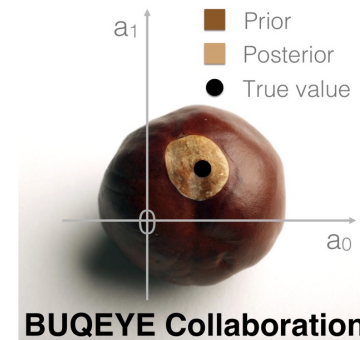
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enables **uncertainty quantification** (EFT truncation)

Bayesian methods are powerful tools for quantifying & propagating EFT uncertainties based on *falsifiable* model assumptions



Open-source software & tutorials (Jupyter): <https://buqeye.github.io>



**Bayesian  
Uncertainty  
Quantification:  
Errors for  
Your  
EFT**

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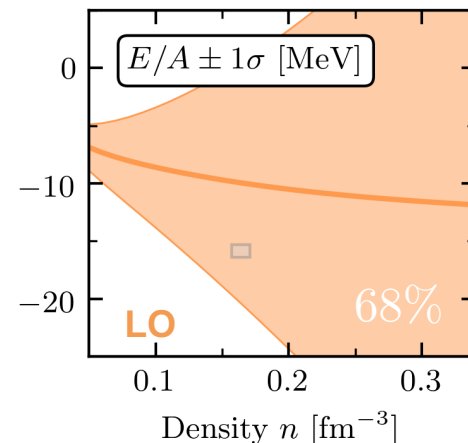
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### An example: symmetric matter

$$y = \frac{E}{A}, \quad k = 4 \quad (\text{N}^3\text{LO})$$

Uncertainty bands depict 68% credibility regions

$$y = y_k + \delta y_k$$

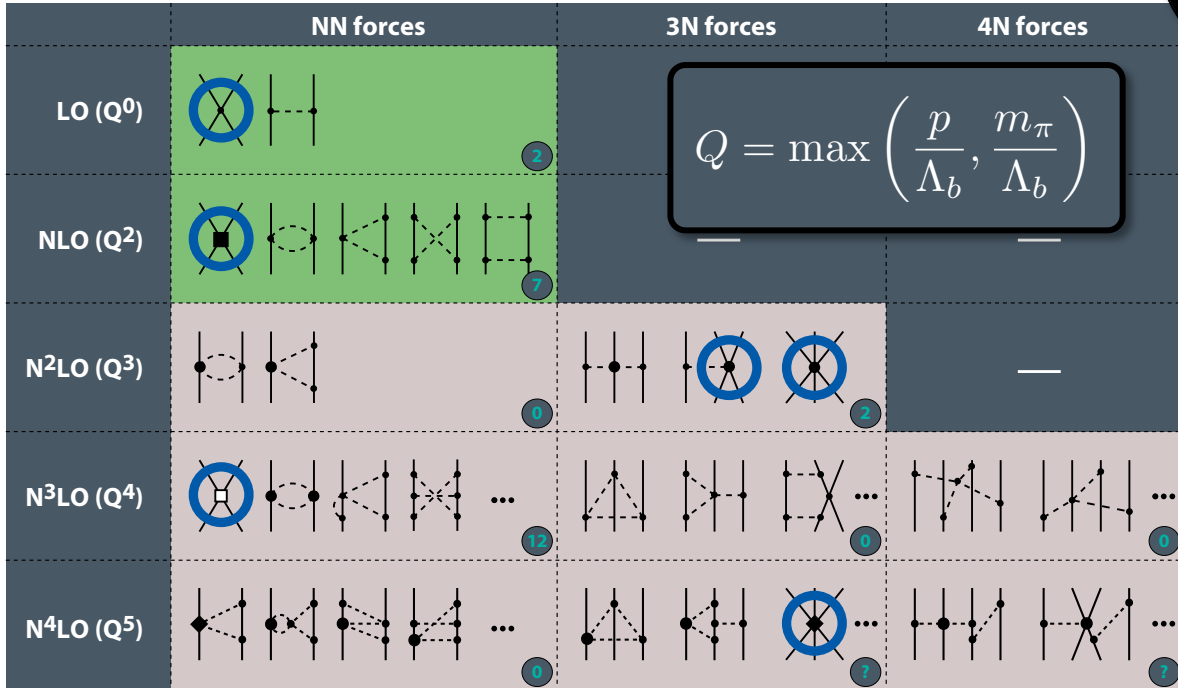




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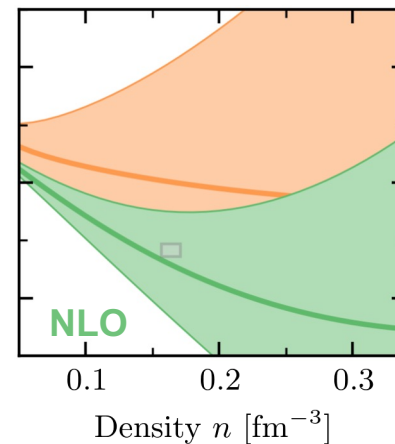
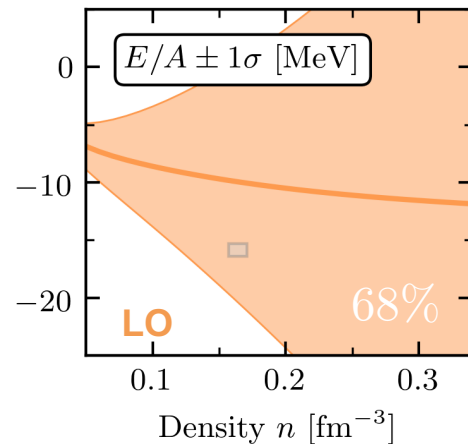
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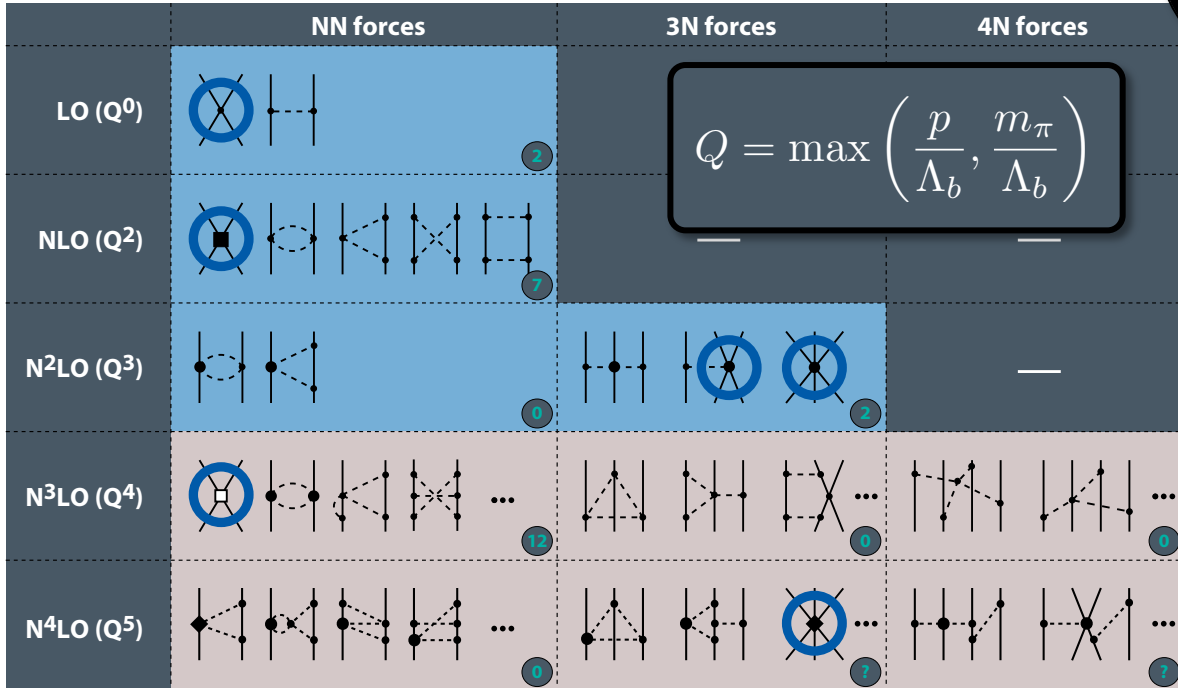
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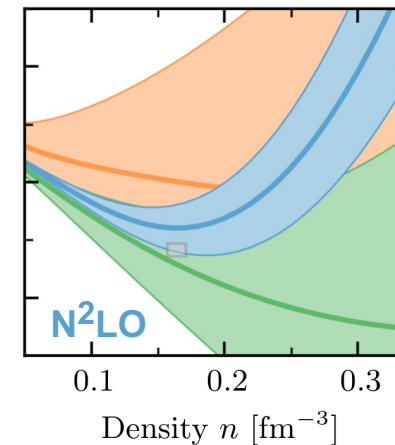
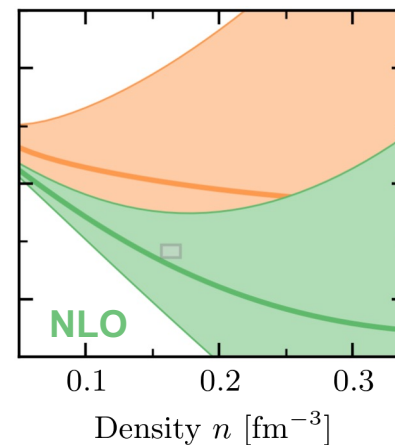
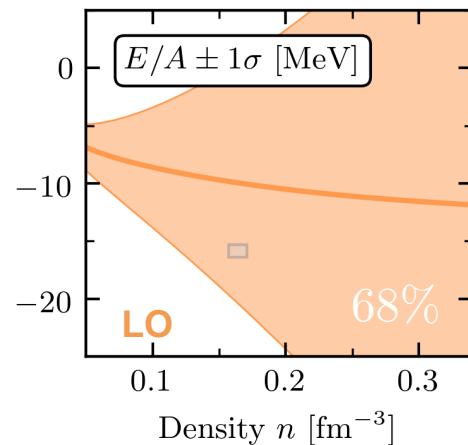
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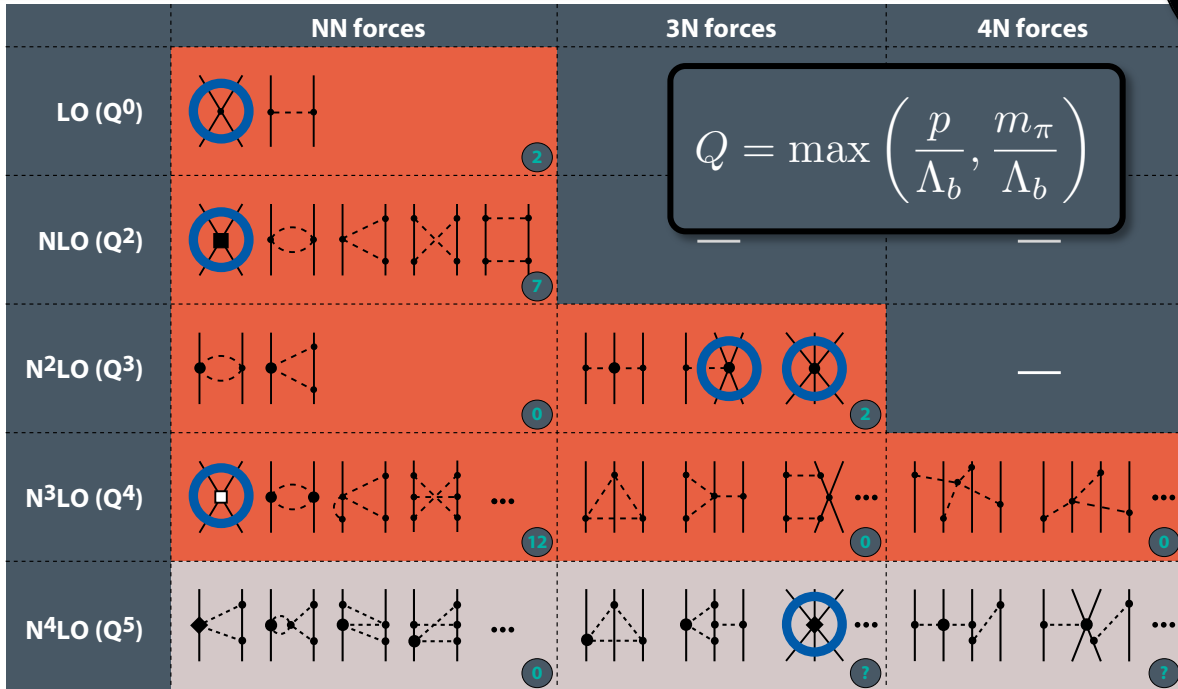




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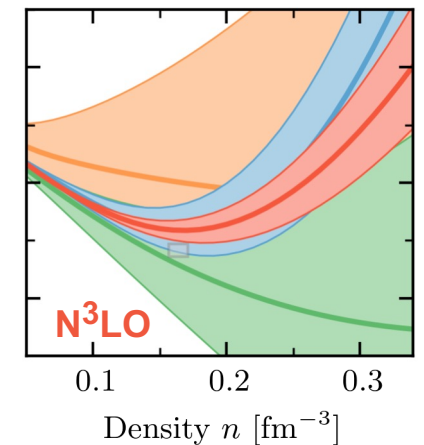
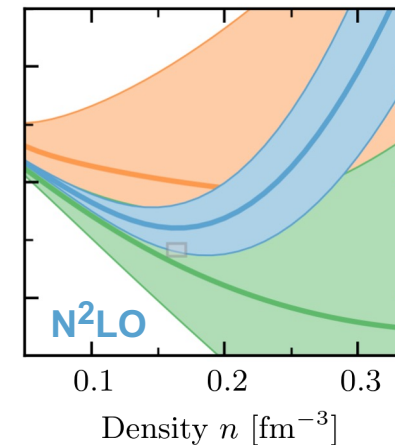
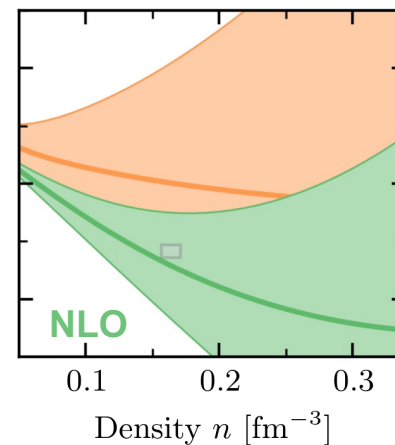
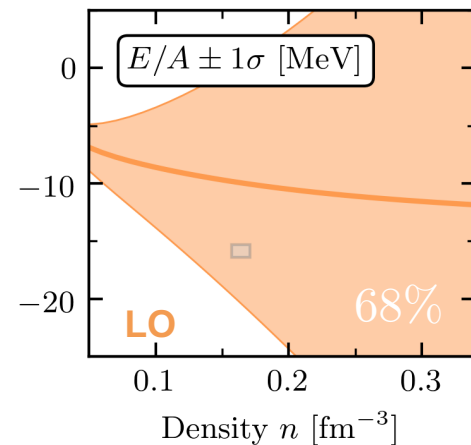
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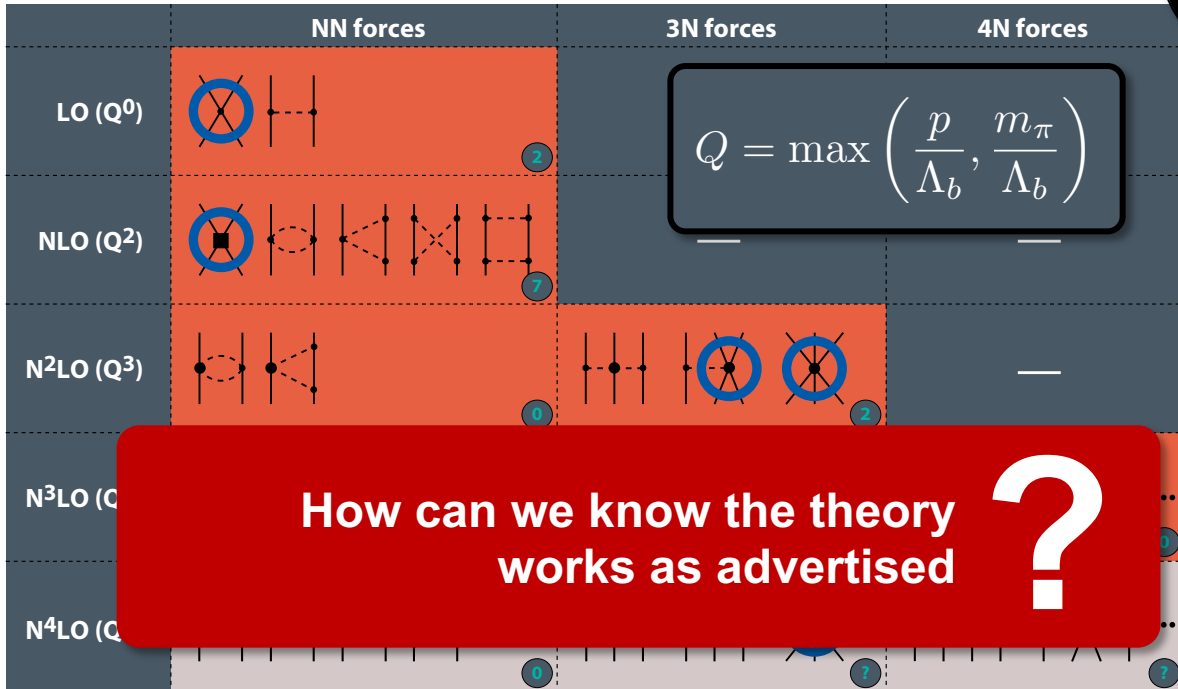
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How can we know the theory works as advertised

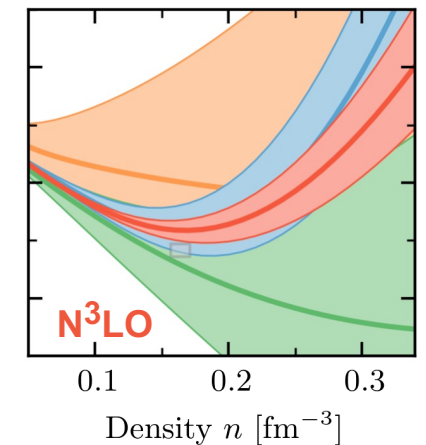
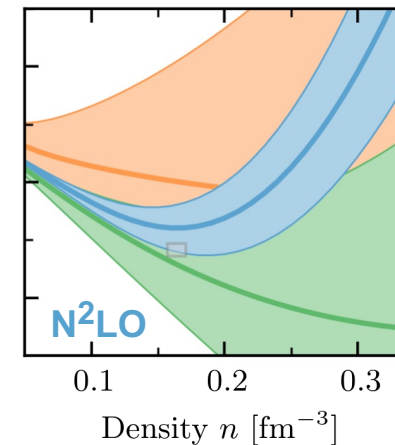
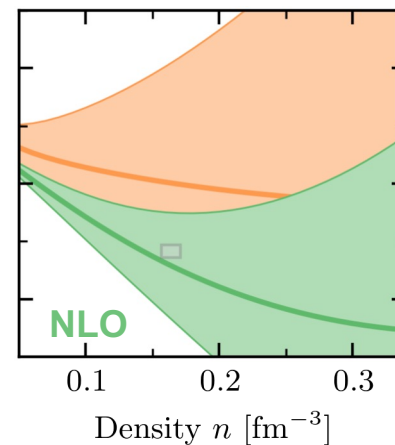
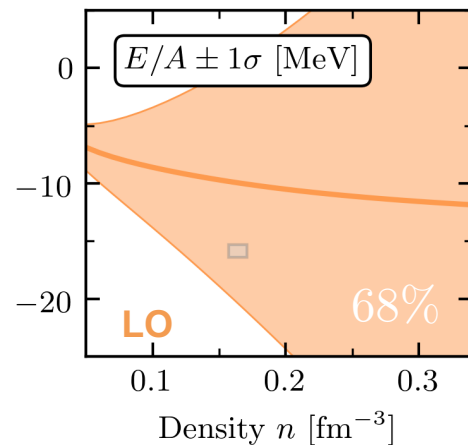


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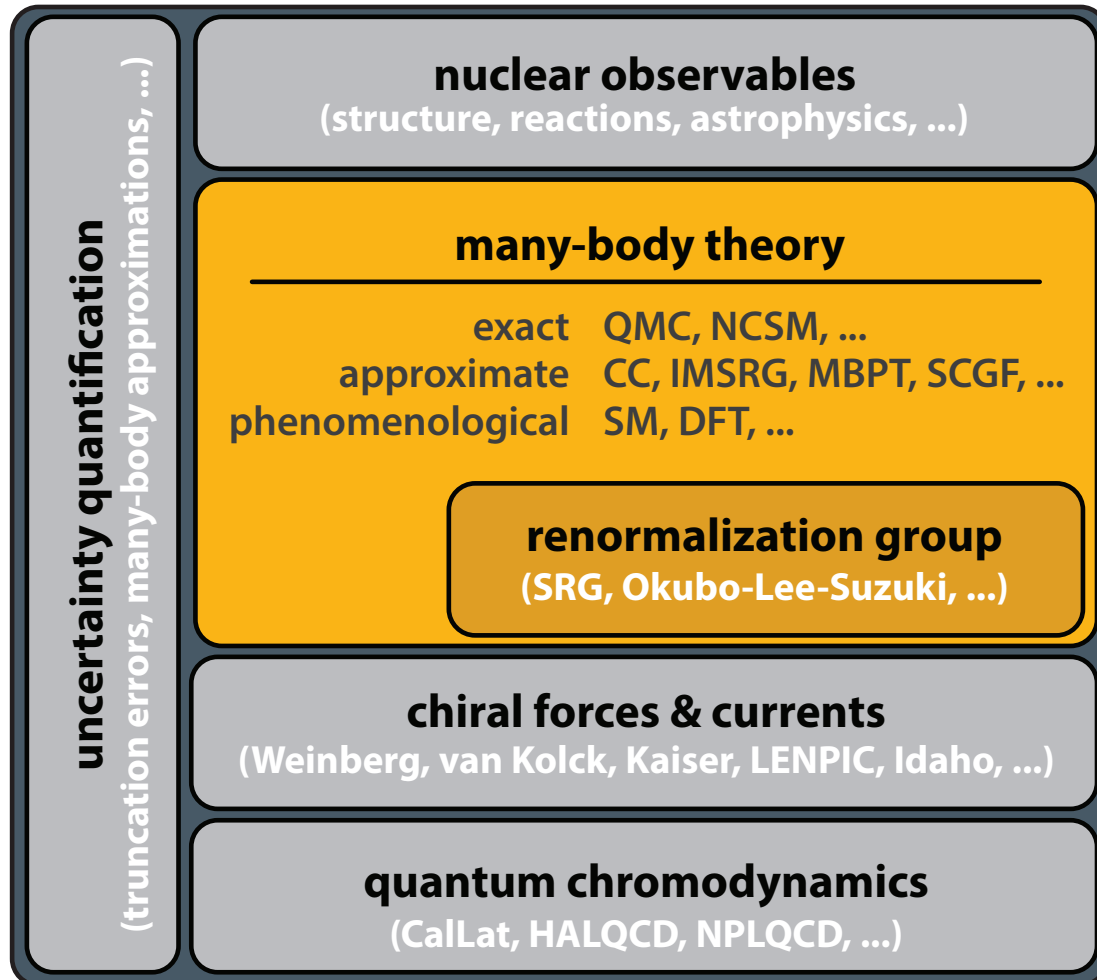
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CD & Bogner, Few Body Syst. **62**, 109

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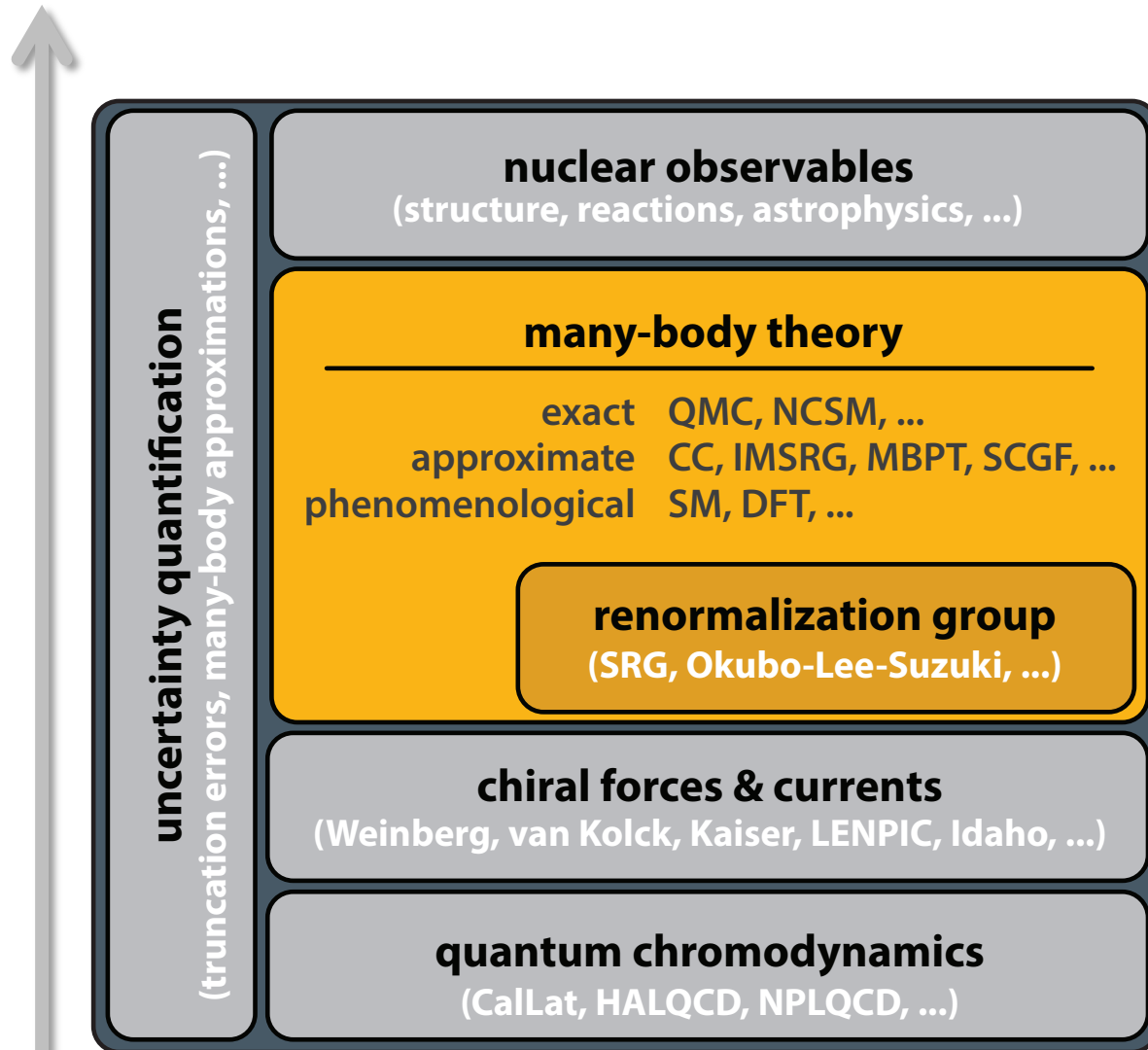
**Here: many-body perturbation theory (MBPT)**

computationally efficient method (HPC-friendly)  
allows to estimate many-body uncertainties

Widely applicable:

- ✓ **arbitrary proton fractions**
- ✓ finite temperature
- ✓ optical potentials, linear response, nuclei, ...

Other frameworks include **quantum Monte Carlo**,  
coupled cluster, and self-consistent Green's functions



CD & Bogner, Few Body Syst. 62, 109

Here: nuclear equation of state (EOS)

energy

See also Stefano Gandolfi's slides:  
*Recent QMC calculations of properties  
of nuclei & nuclear matter*

$A$

temperature  $T (= 0)$

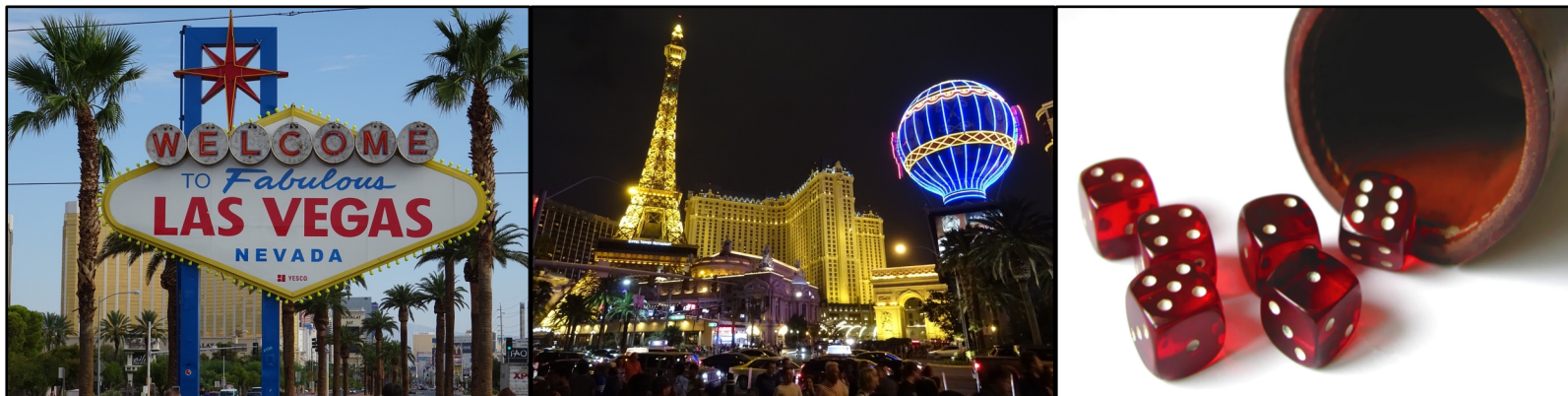
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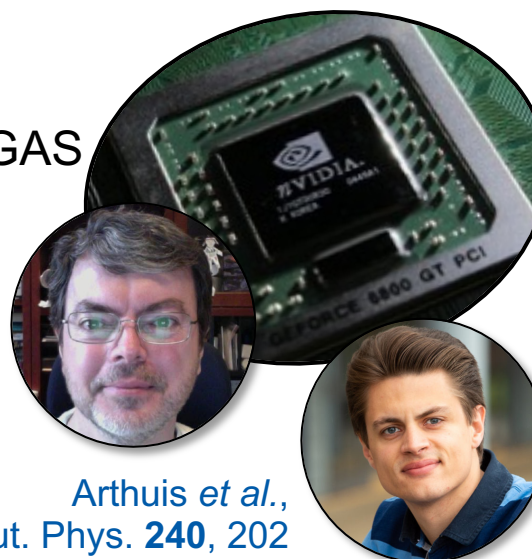
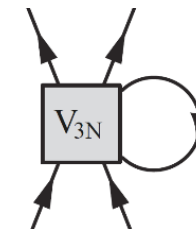
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## automated approach to MBPT for nuclear matter with NN, 3N, and 4N forces

- **implementation of arbitrary diagrams** has become **straightforward** (numerically exact)
- multi-dimensional momentum integrals: improved VEGAS
- GPU-accelerated normal ordering of **3N interactions**
- propagation of importance sampling distributions
- **controlled evaluation of 1000s of MBPT diagrams**



Arthuis *et al.*,  
Comput. Phys. **240**, 202

high-order MBPT  
calculations of the EOS

automated code  
generation

analytic expressions  
interaction & MBPT diagrams

automated diagram  
generation



The number of diagrams increases rapidly!

	<b>1</b>	<b>3</b>	<b>39</b>	<b>840</b>	<b>27 300</b>	<b>1 232 280</b>	<b>...</b>
$n =$	2	3	4	5	6	7	

Integer sequence A064732:

Number of labeled Hugenholtz diagrams with  $n$  nodes.

with automated diagram generation



automated approach  
to MBPT for nuclear matter

# MBPT: an HPC application

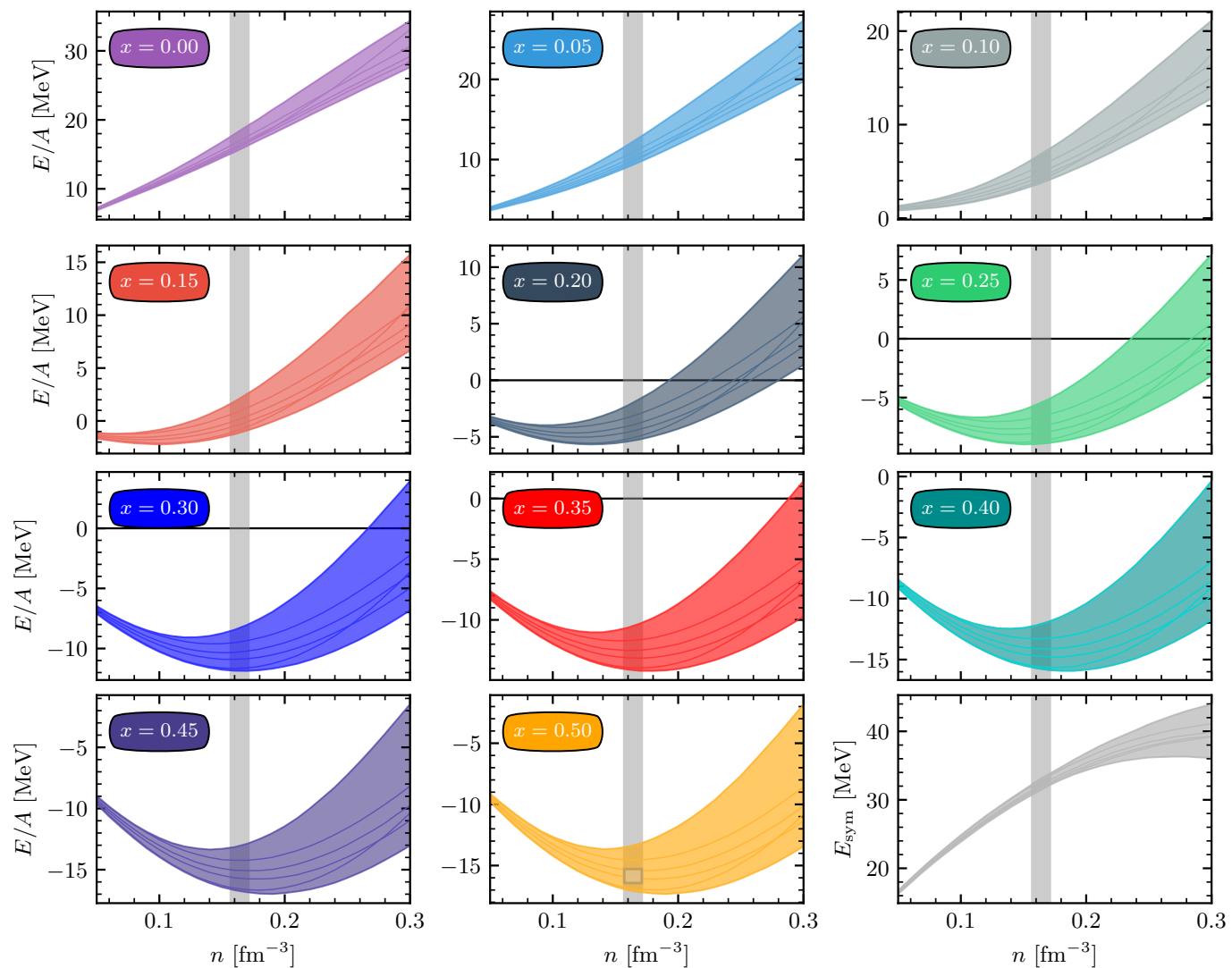
**#2 (U.S.)**

Summit @ Oak Ridge Leadership Computing Facility

202 752 CPU Cores  
27 648 Nvidia GPUs  
122.3 peta flops



# MBPT: an HPC application



Drischler, McElvain *et al.*, in prep.

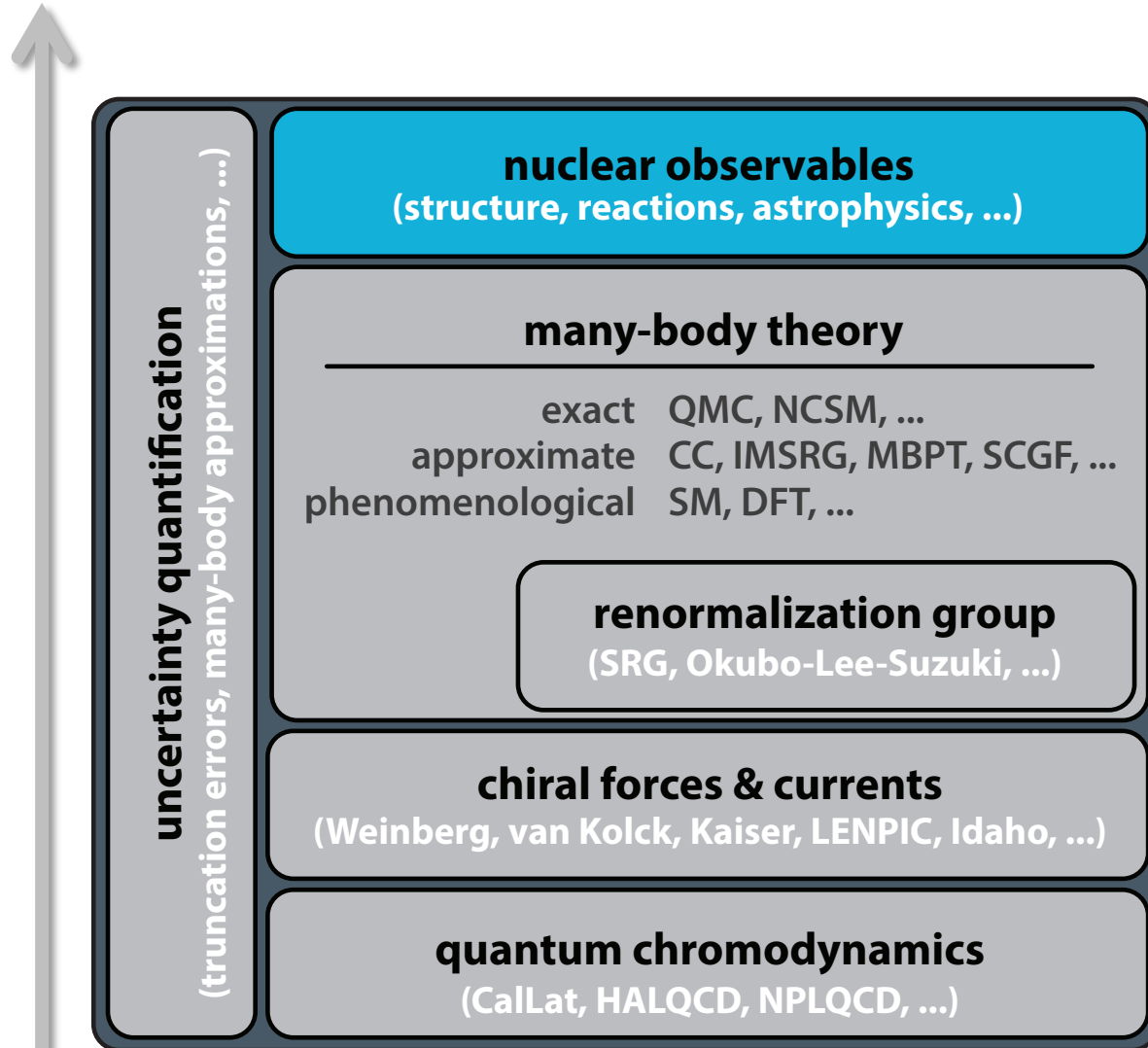
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**nuclear EOS with quantified uncertainties**  
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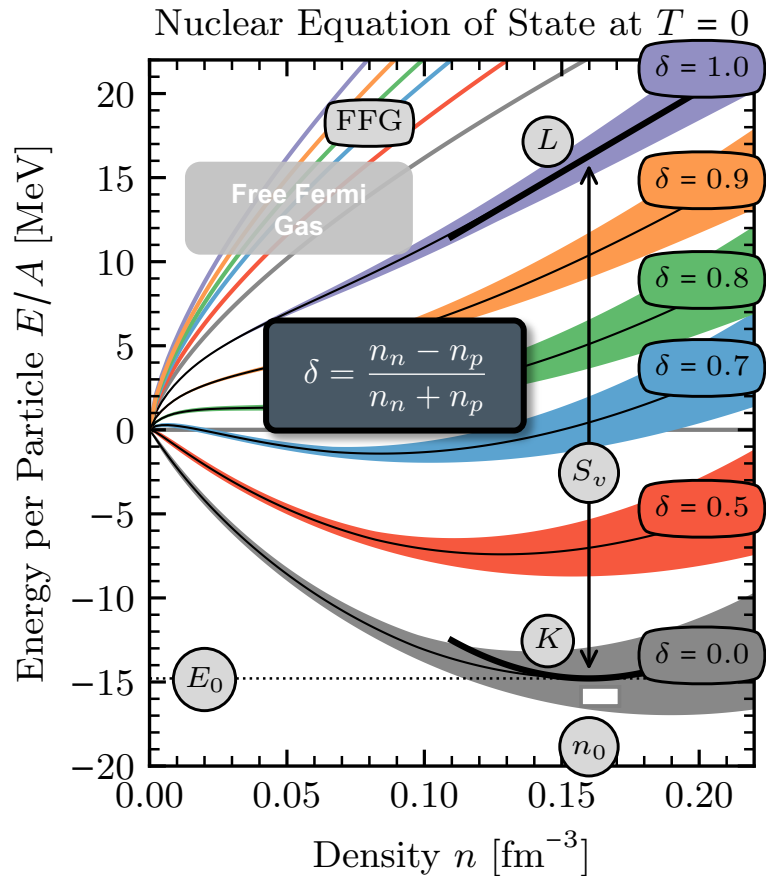
## Uncertainty quantification

robust estimates of theoretical uncertainties using Bayesian machine learning via Gaussian Processes  
uncertainties in EFT-based calculations due to:

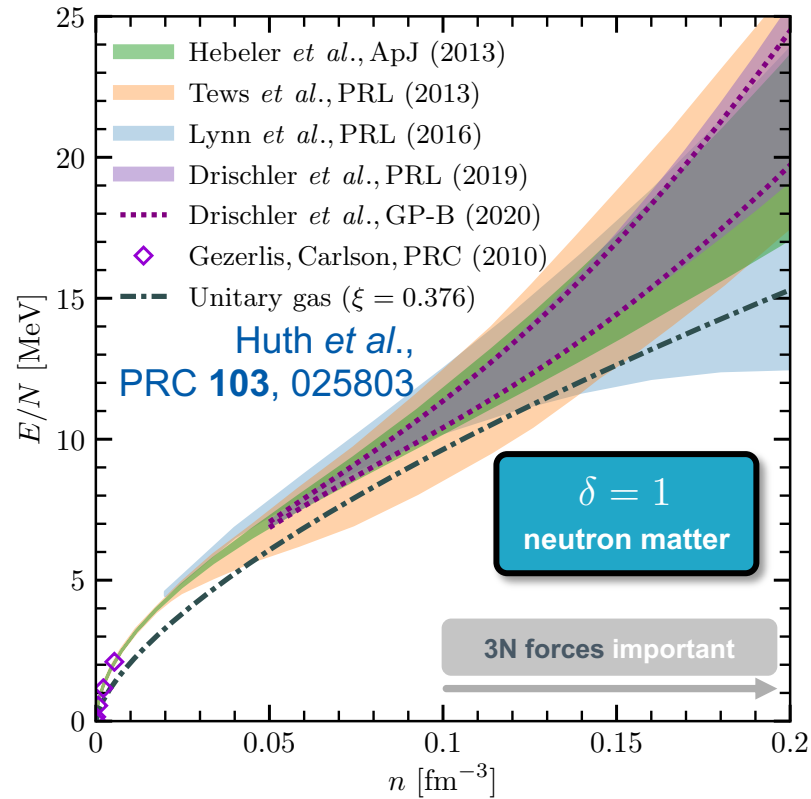
- truncating the EFT expansion
- applying many-body (and other) approximations
- fitting LECs to experimental data

First chiral potentials with uncertainties fully quantified and their applications:  
Wesolowski, Svensson *et al.*, PRC **104**, 064001  
Djärv, Ekstöm *et al.*, PRC **105**, 014005

# Neutron matter | saturation in symmetric matter

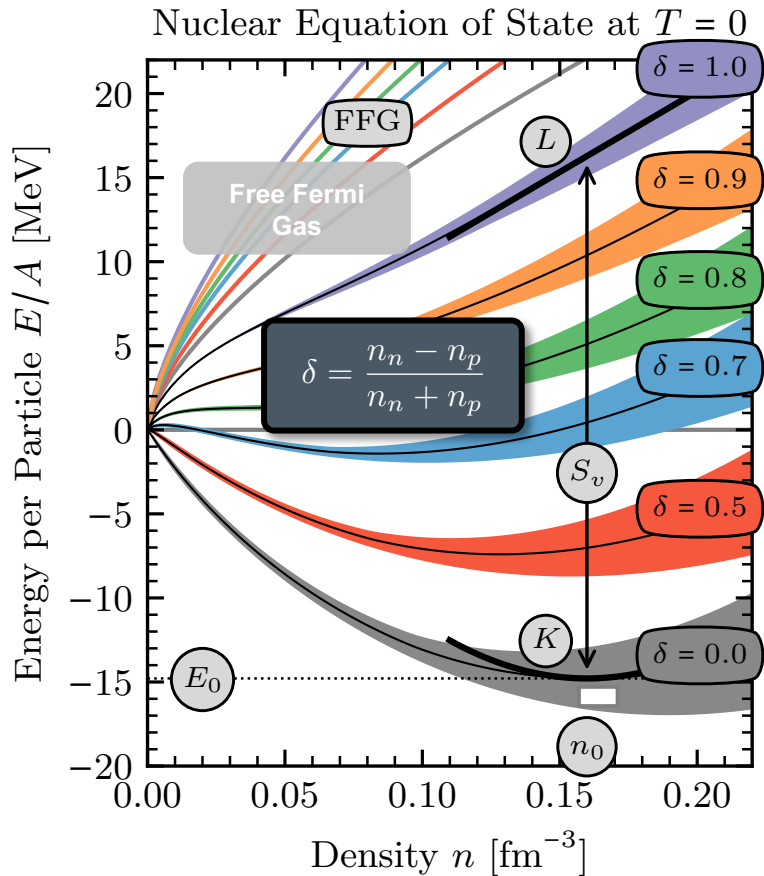


CD, Holt, and Wellenhofer, *Annu. Rev. Nucl. Part. Sci.* **71**, 403



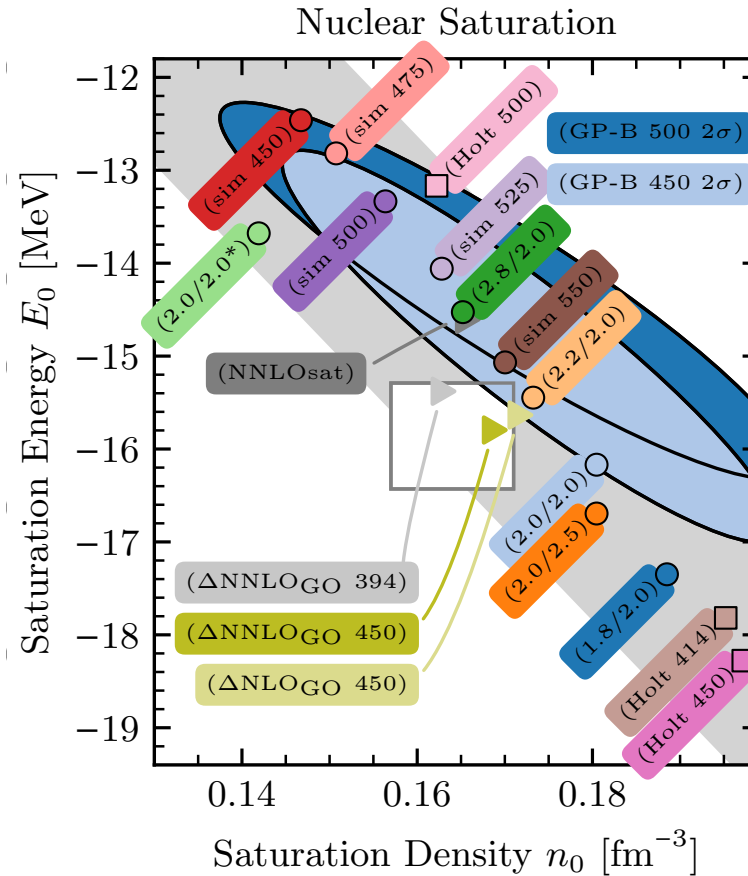
$$\left. \frac{d}{dn} \frac{E}{A}(n, 0) \right|_{n=n_0} = 0$$

# Neutron matter | saturation in symmetric matter



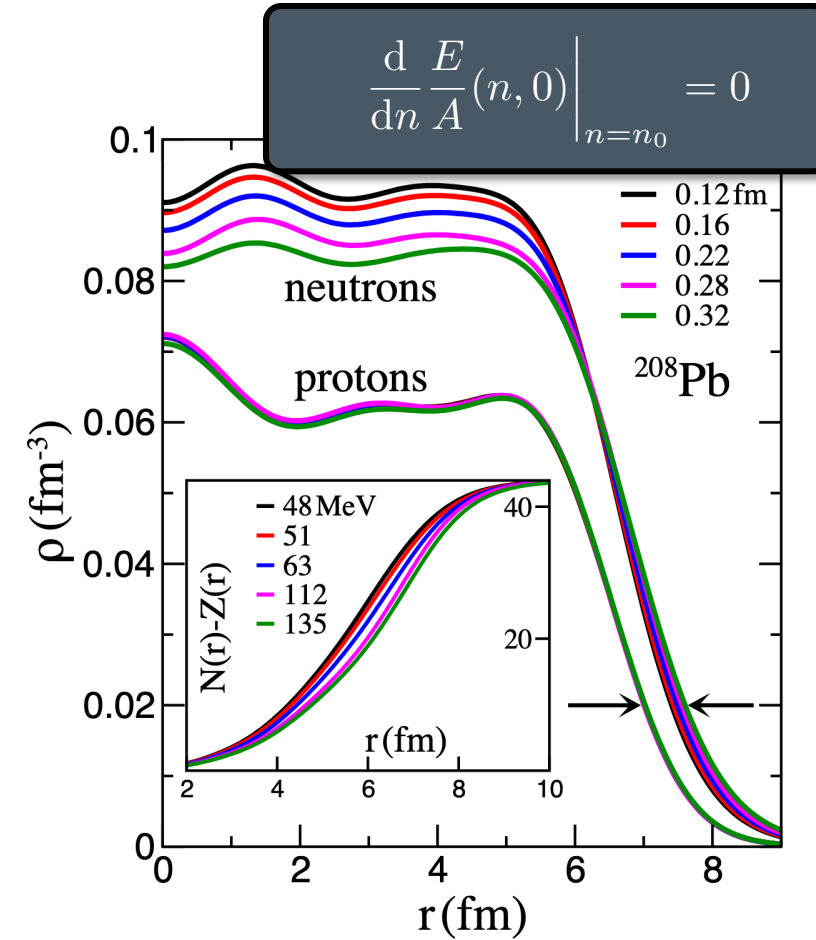
CD, Holt, and Wellenhofer, Annu. Rev. Nucl. Part. Sci. **71**, 403

saturation point: **fine-tuned cancellation** between the kinetic and interaction contributions (ideal testbed for chiral EFT)



**Coester band** overlaps with the empirical box (but limited meaning without errors)

Annotations: ( $\lambda / \Lambda_{3N}$ ) in  $\text{fm}^{-1}$  or ( $\Lambda$ ) in MeV

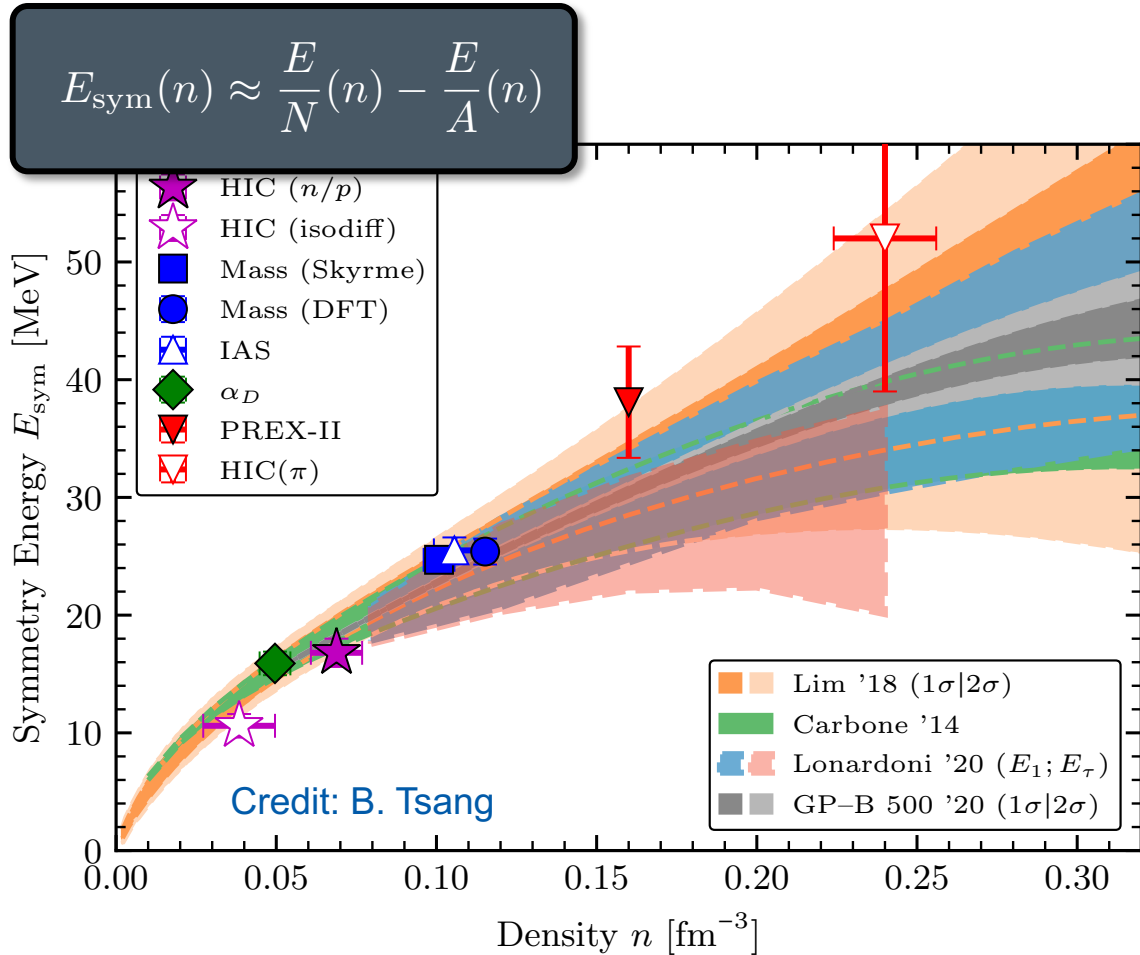


Piekarewicz & Fattoyev, Phys. Today **72**, 7

**needed:** improved predictions with novel NN+3N interactions and robust uncertainty quantification



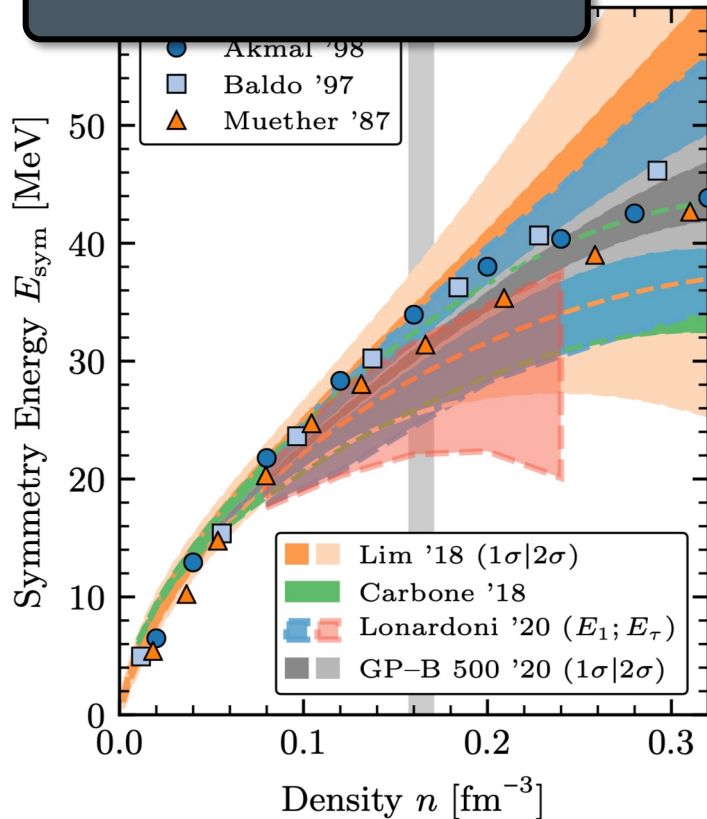
# Nuclear symmetry energy



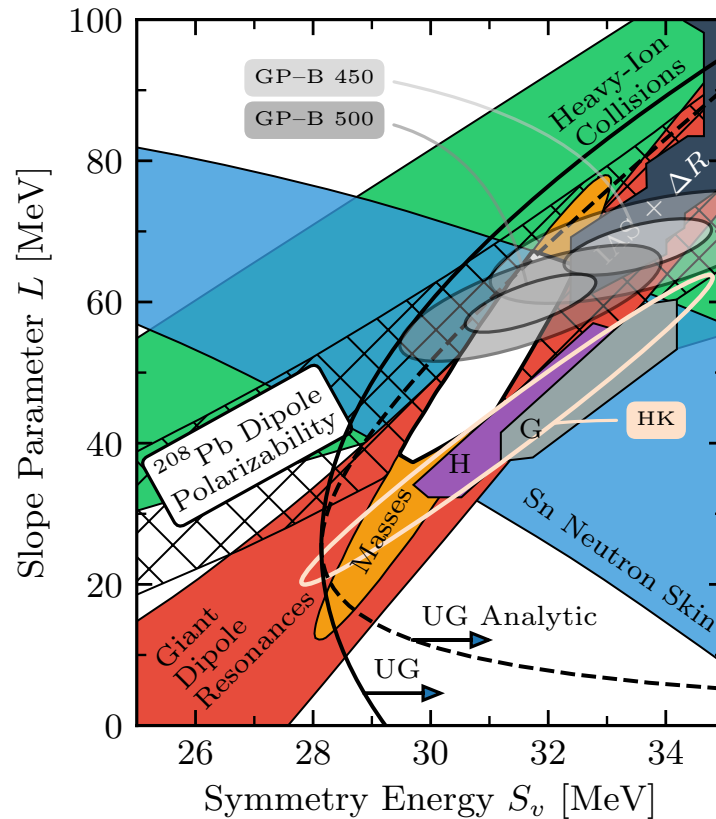
See also Betty Tsang's talk:  
*Symmetry Energy* (Saturday)

# Nuclear symmetry energy

$$E_{\text{sym}}(n) \approx \frac{E}{N}(n) - \frac{E}{A}(n)$$



excellent agreement with experiment



CD, Holt *et al.*, ARNPS 71, 403  
Lattimer & Lim, APJ 771, 51

**Correlations are important:**  
uncertainties can be smaller  
than one *might* naively think

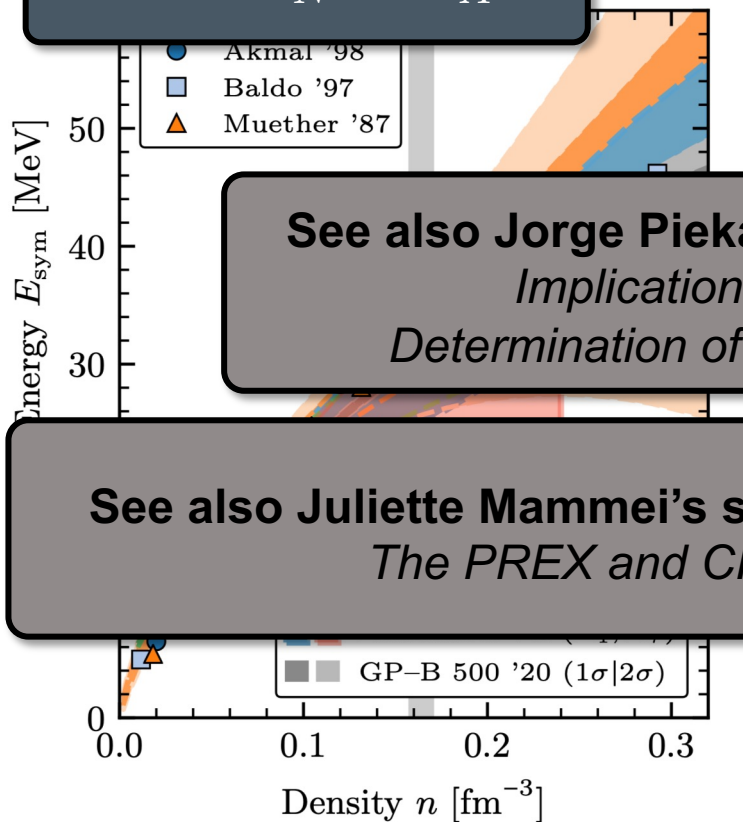
$$S_2(n) \equiv S_v + \frac{L}{3} \left( \frac{n - n_0}{n_0} \right) + \dots$$

$$\text{pr}(S_v, L | \mathcal{D}) = \int \text{pr}(S_v, L | \mathcal{D}, n_0) \text{pr}(n_0 | \mathcal{D}) dn_0$$

$$\text{pr}(n_0 | \mathcal{D}) \approx 0.17 \pm 0.01 \text{ fm}^{-3}$$

# Nuclear symmetry energy

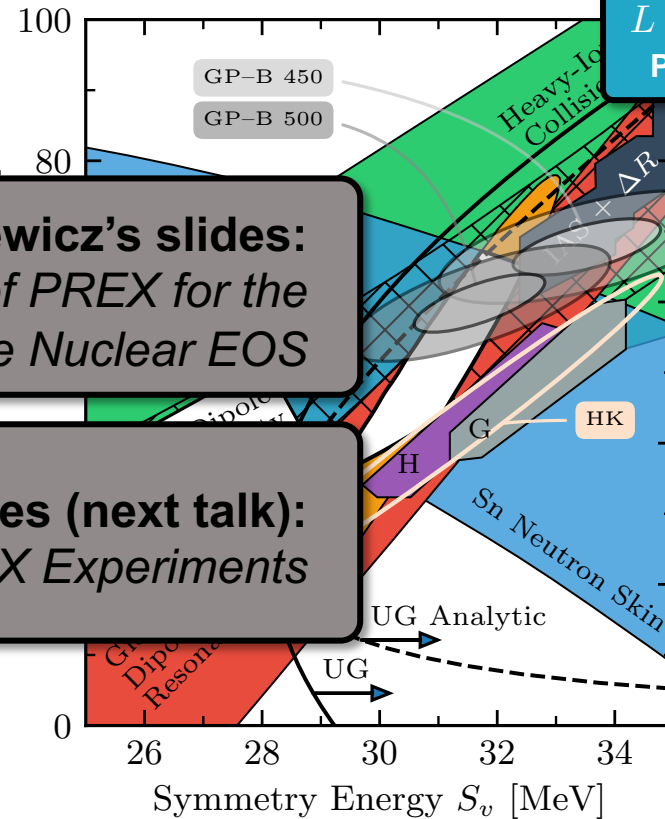
$$E_{\text{sym}}(n) \approx \frac{E}{N}(n) - \frac{E}{A}(n)$$



See also Jorge Piekarewicz's slides:  
*Implications of PREX for the Determination of the Nuclear EOS*

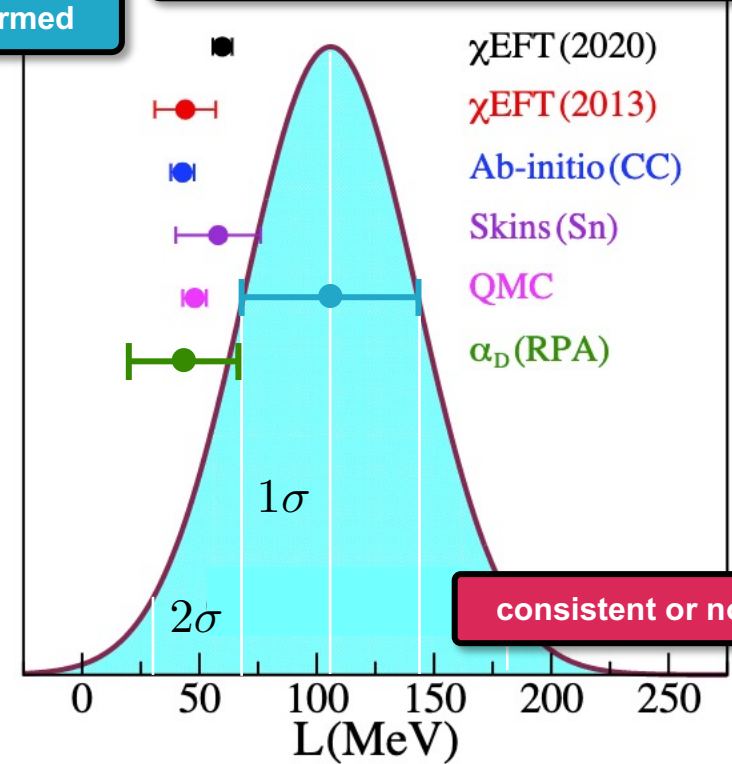
See also Juliette Mammei's slides (next talk):  
*The PREX and CREX Experiments*

excellent agreement with experiment



$L = 106 \pm 37 \text{ MeV}$   
PREX-II informed

$$S_2(n) \equiv S_v + \frac{L}{3} \left( \frac{n - n_0}{n_0} \right) + \dots$$



consistent or not?

CD, Holt *et al.*, ARNPS **71**, 403  
Lattimer & Lim, APJ **771**, 51

**Correlations are important:**  
uncertainties can be smaller than one *might* naively think

Reinhard *et al.*, PRL **127**, 232501  
Reed, Fattoyev *et al.*, PRL **126**, 172503  
Piekarewicz, PRC **104**, 024329

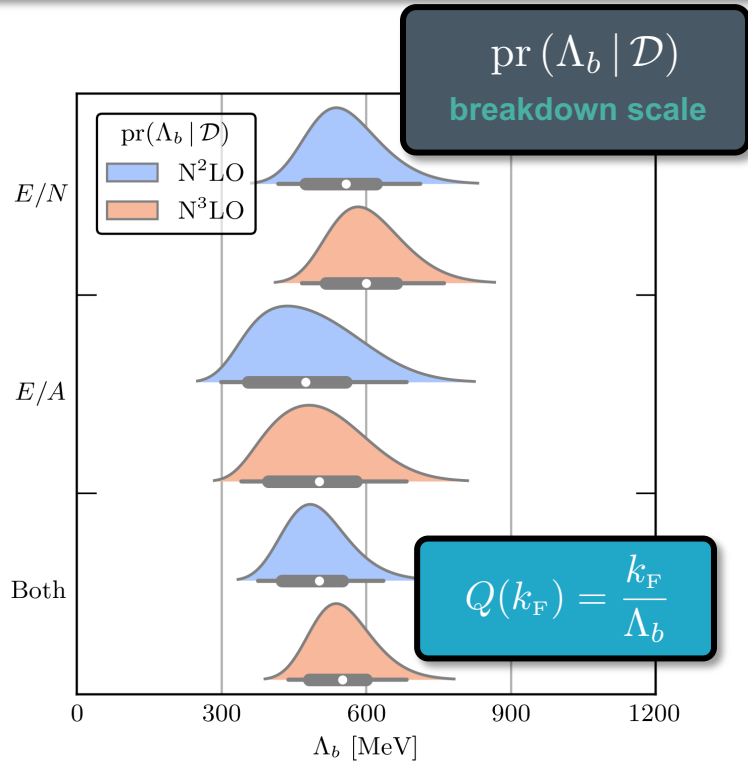
**“Tension” between PREX-II and different theoretical approaches at the ~68-95% level**

$$\text{pr}(S_v, L | \mathcal{D}) = \int \text{pr}(S_v, L | \mathcal{D}, n_0) \text{pr}(n_0 | \mathcal{D}) dn_0$$

$$\text{pr}(n_0 | \mathcal{D}) \approx 0.17 \pm 0.01 \text{ fm}^{-3}$$



# Exploring the limits of chiral EFT

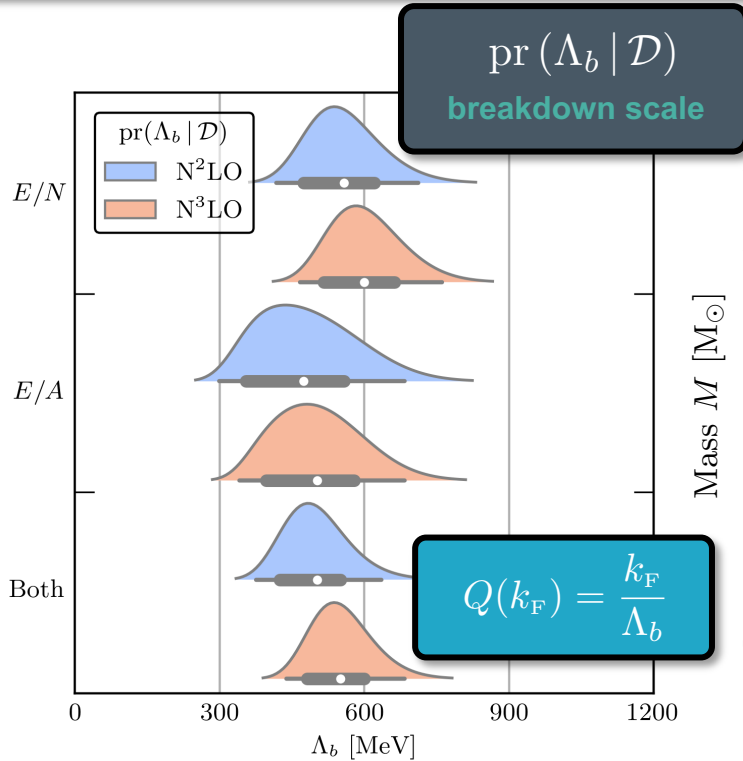


CD, Melendez *et al.*, PRC **102**, 054315

Bayesian inference of the  
in-medium breakdown scale

**But: at what *density* does  
chiral EFT break down?**

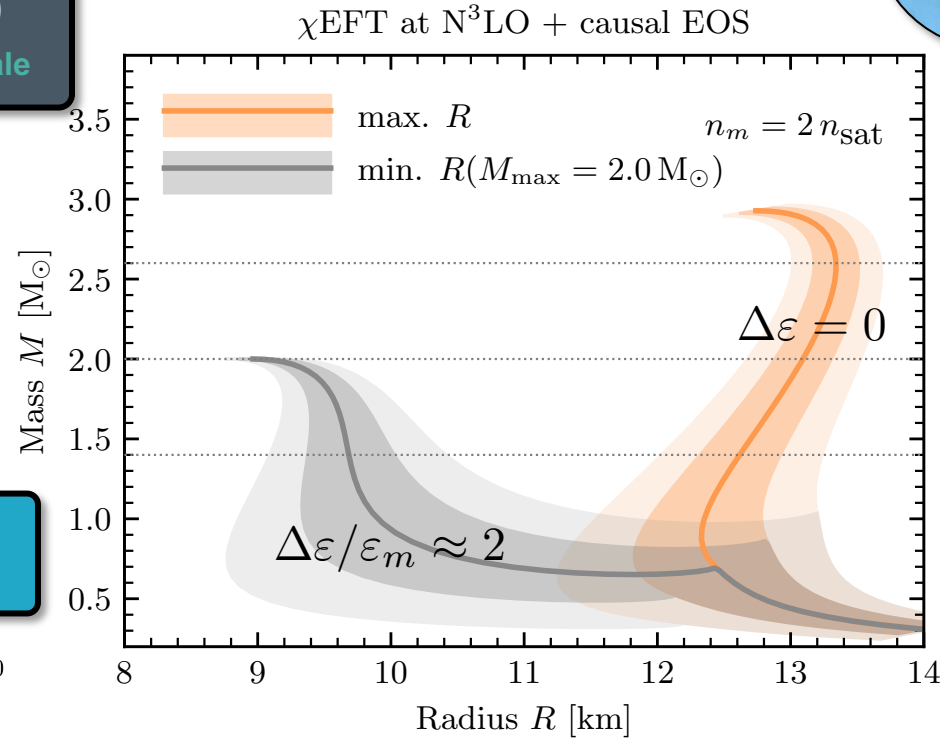
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CD, Melendez *et al.*, PRC **102**, 054315

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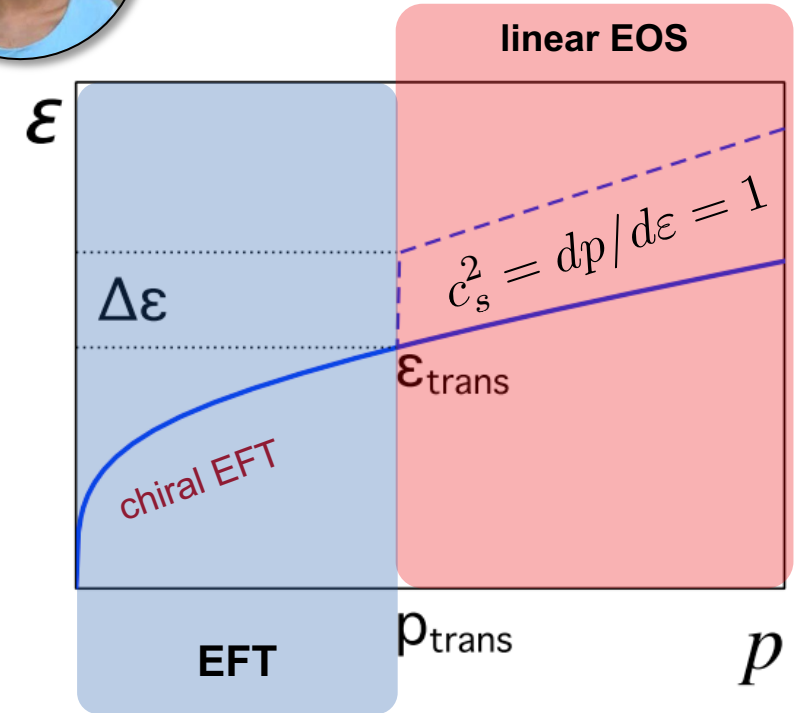


CD, Han, Lattimer *et al.*, PRC **103**, 045808  
CD, Han, and Reddy, PRC **105**, 035808

derived **bounds on the neutron star radius** (and sound speed) assuming chiral EFT is valid up to a given critical density (here:  $2n_0$ ) could already be challenged by NICER

$$R_{2.0} = (11.4 - 16.1) \text{ km}$$

Riley *et al.*, AJL **918**, L27  
Miller *et al.*, AJL **918**, L28



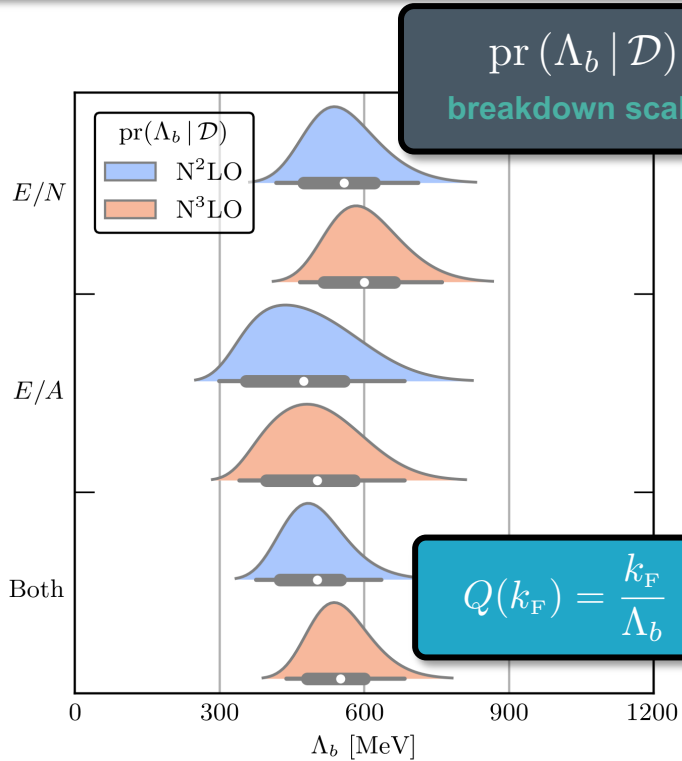
Han & Prakash, APJ **899**, 2  
Alford *et al.*, JPG: NPP **46**, 114001

extend EFT EOS at  $n_m$  to linear EoS with finite discontinuity (softening)

**continuous match sets upper bound**

use **lower limit on  $M_{\text{max}}$**  from observation to adjust  $\Delta\epsilon$  and constrain  $R_{\text{min}}$

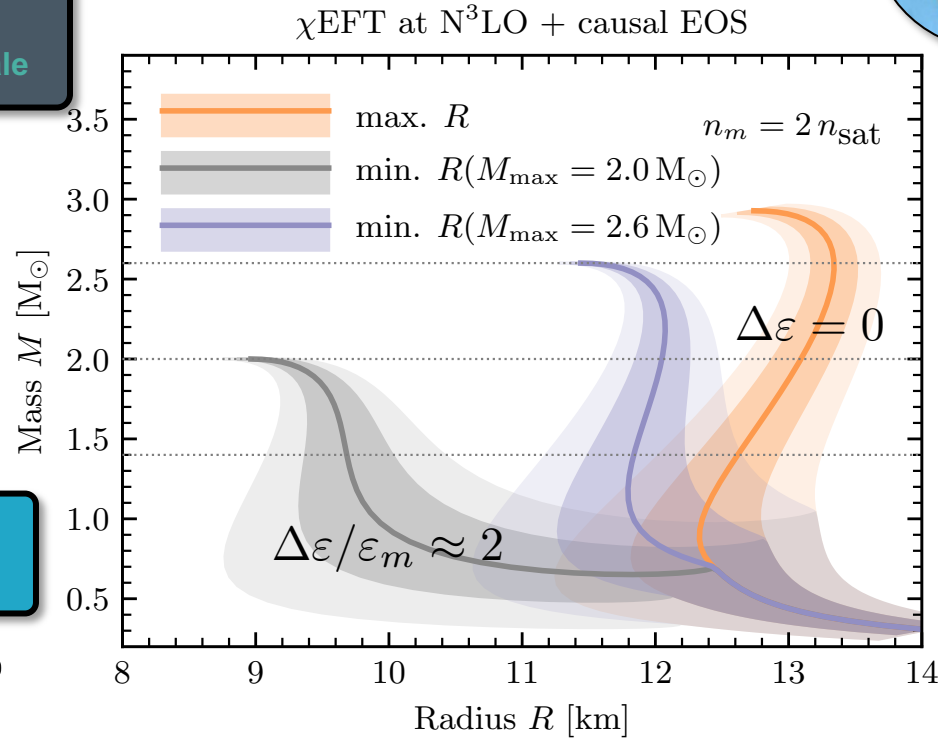
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CD, Melendez *et al.*, PRC **102**, 054315

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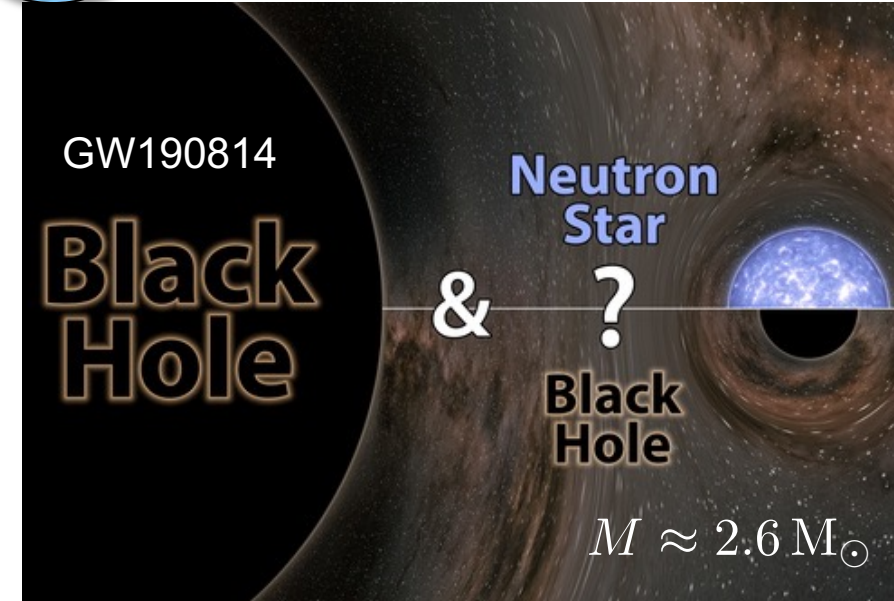


CD, Han, Lattimer *et al.*, PRC **103**, 045808  
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Alford *et al.*, JPG: NPP **46**, 114001

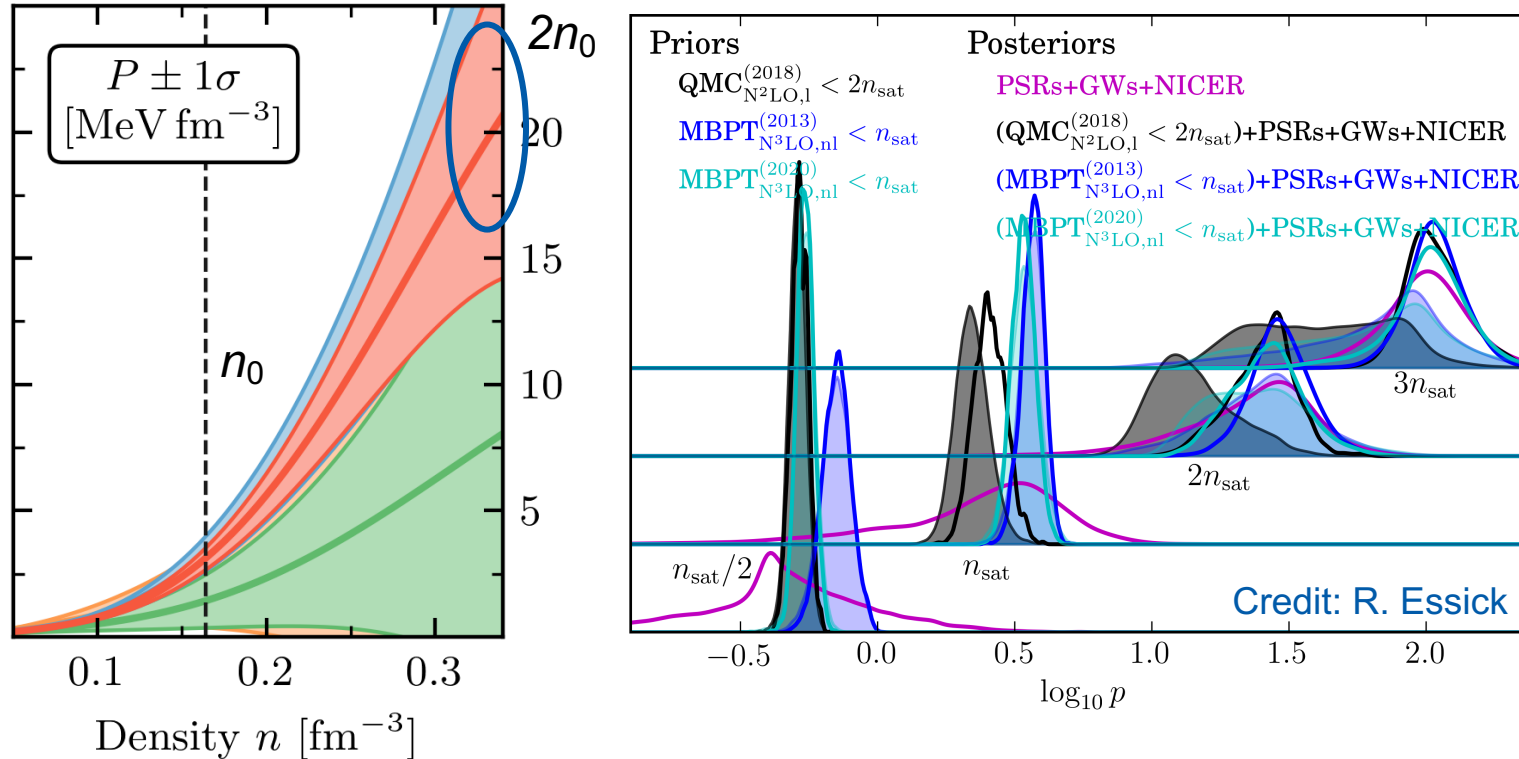
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# Direct astrophysical tests at supranuclear densities



CD, Furnstahl *et al.*, PRL **125**, 202702

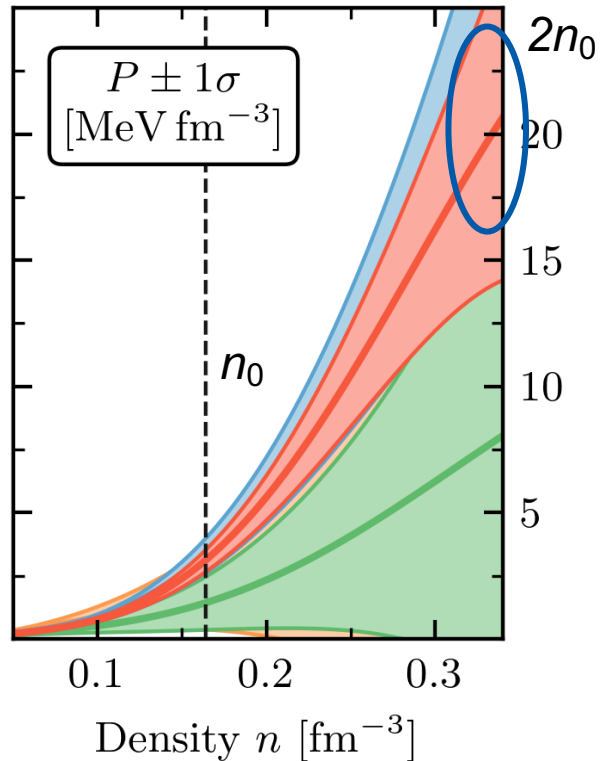
see also: Essick *et al.*, PRC **102**, 055803



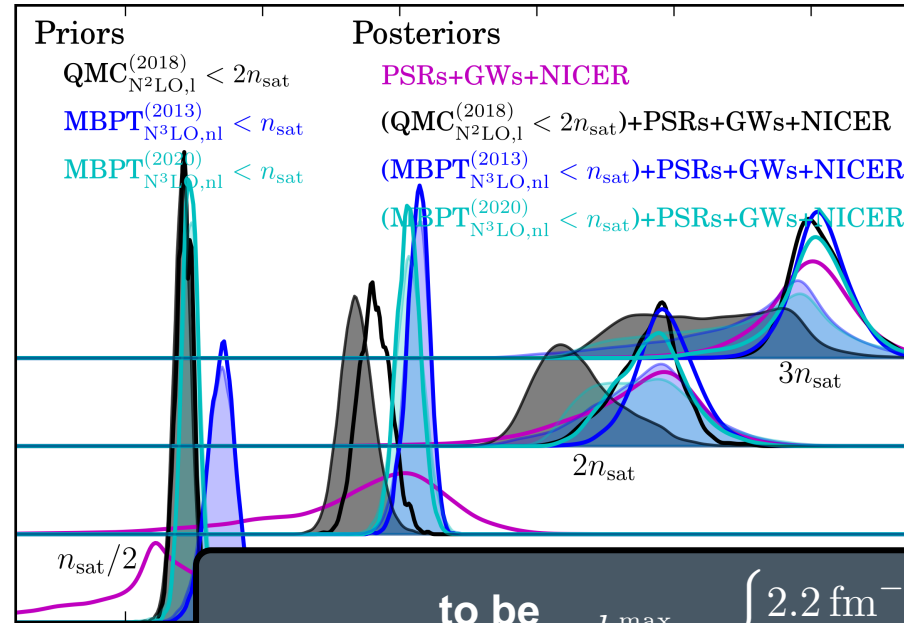
**Neutron star observations could be used for:**  
 Model checking & selection of chiral interactions  
 Constraints on coupling constants in nuclear forces

$$P(n = 0.32 \text{ fm}^{-3}) \approx \begin{cases} 20 \pm 6 \text{ MeV fm}^{-3} & \text{MBPT: nonlocal} \\ 15 \pm 5 \text{ MeV fm}^{-3} & \text{QMC: local } V_{E,1} \end{cases}$$

# Direct astrophysical tests at supranuclear densities



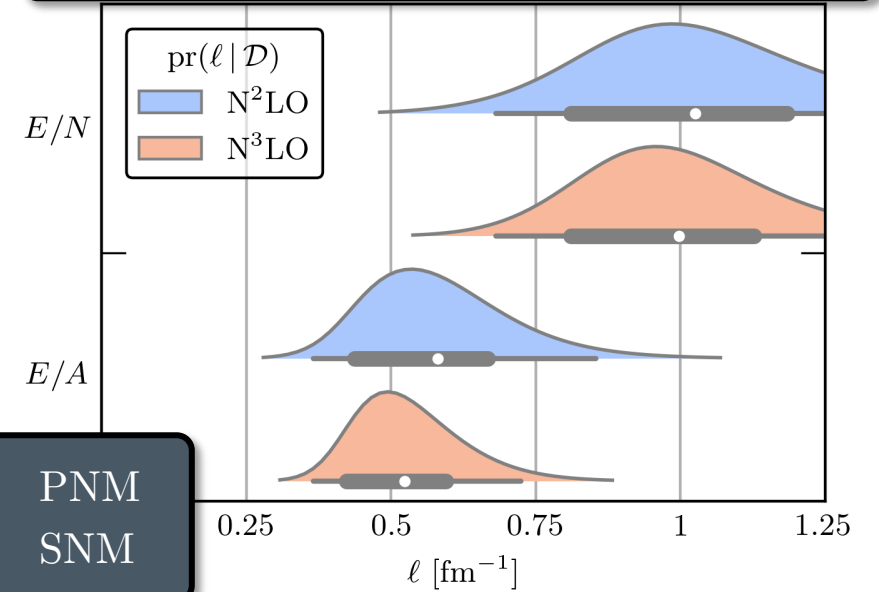
CD, Furnstahl *et al.*, PRL **125**, 202702



to be compared with  $k_F^{\max} = \begin{cases} 2.2 \text{ fm}^{-1} & \text{PNM} \\ 1.7 \text{ fm}^{-1} & \text{SNM} \end{cases}$

see also: Essick *et al.*, PRC **102**, 055803

How correlated is nuclear matter ?  $\text{pr}(\ell | \mathcal{D})$  correlation length



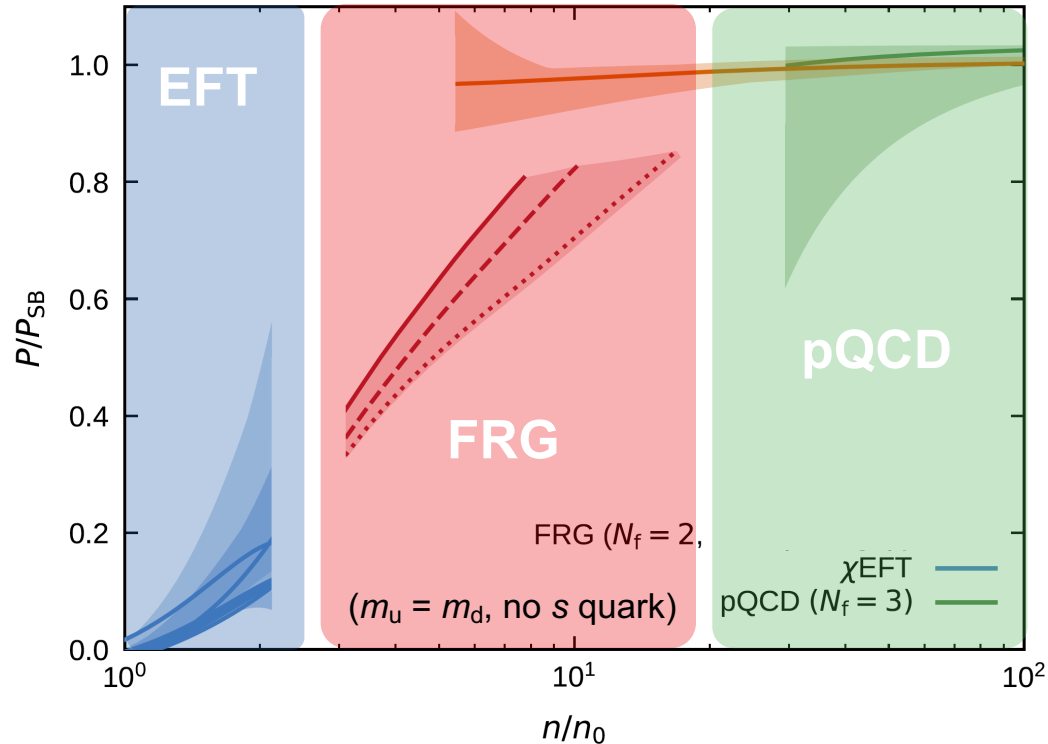
CD, Melendez *et al.*, PRC **102**, 054315



**Neutron star observations could be used for:**  
 Model checking & selection of chiral interactions  
 Constraints on coupling constants in nuclear forces

**EFT truncation error is highly correlated**

$$P(n = 0.32 \text{ fm}^{-3}) \approx \begin{cases} 20 \pm 6 \text{ MeV fm}^{-3} & \text{MBPT: nonlocal} \\ 15 \pm 5 \text{ MeV fm}^{-3} & \text{QMC: local } V_{E,1} \end{cases}$$

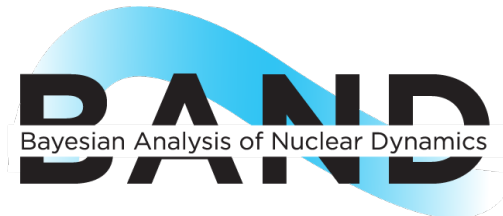


Leonhardt, Pospiech, Schallmo, Braun, CD,  
Hebeler, and Schwenk, PRL **125**, 142502

**Functional Renormalization Group** (based on QCD action):  
*ab initio* constraints at intermediate densities ( $\sim 3\text{--}10n_0$ )

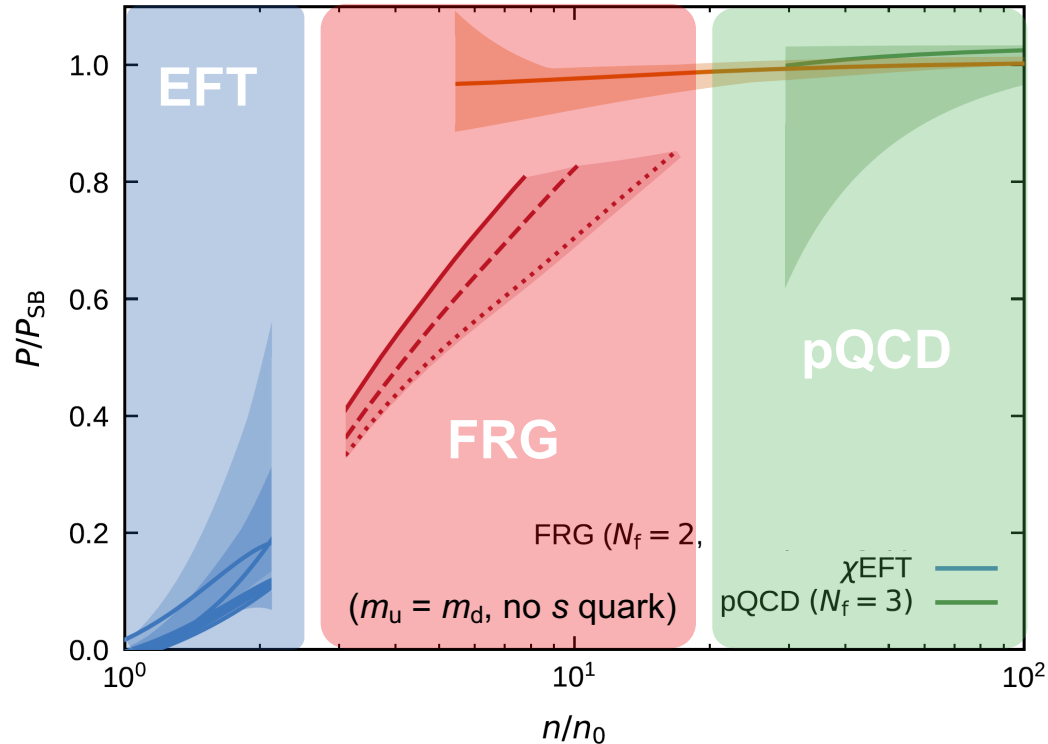
suggests that the different density regions can be  
straightforwardly combined

for neutron star matter, see: Braun & Schallmo; arXiv:2204.00358



**BAND Manifesto**,  
Phillips, Furnstahl, Heinz *et al.*,  
JGP: NP **48** 07200

# New predictions in SNM at intermediate densities

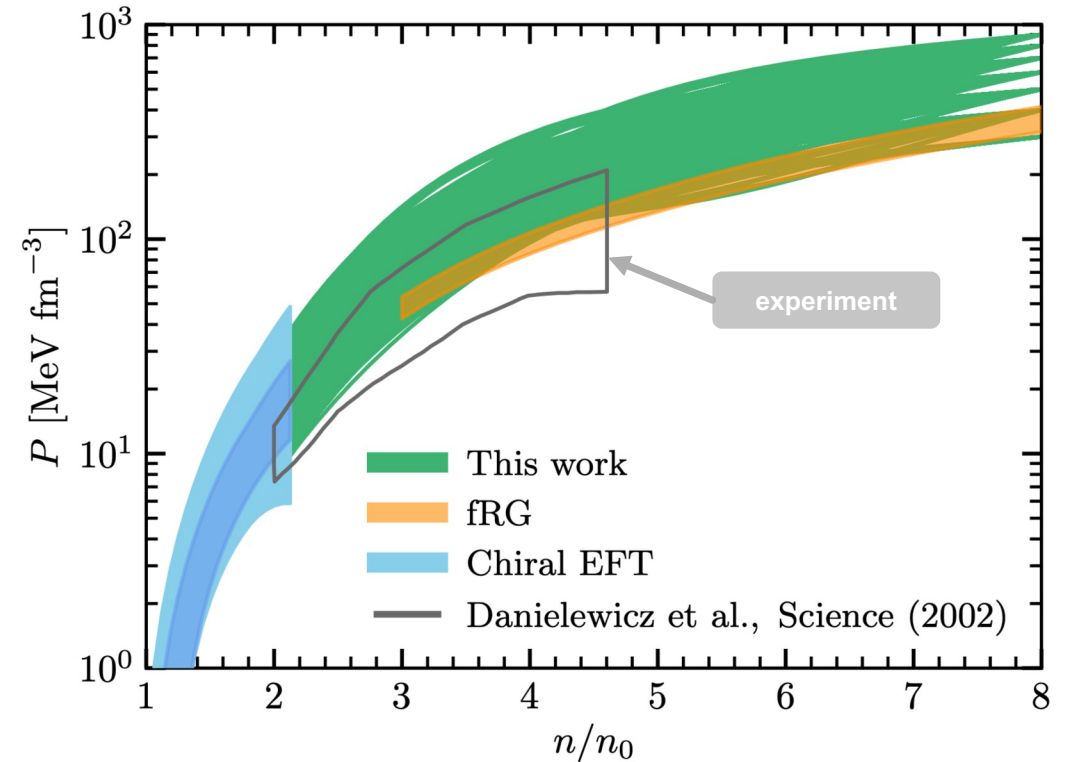


Leonhardt, Pospiech, Schallmo, Braun, CD, Hebeler, and Schwenk, PRL **125**, 142502

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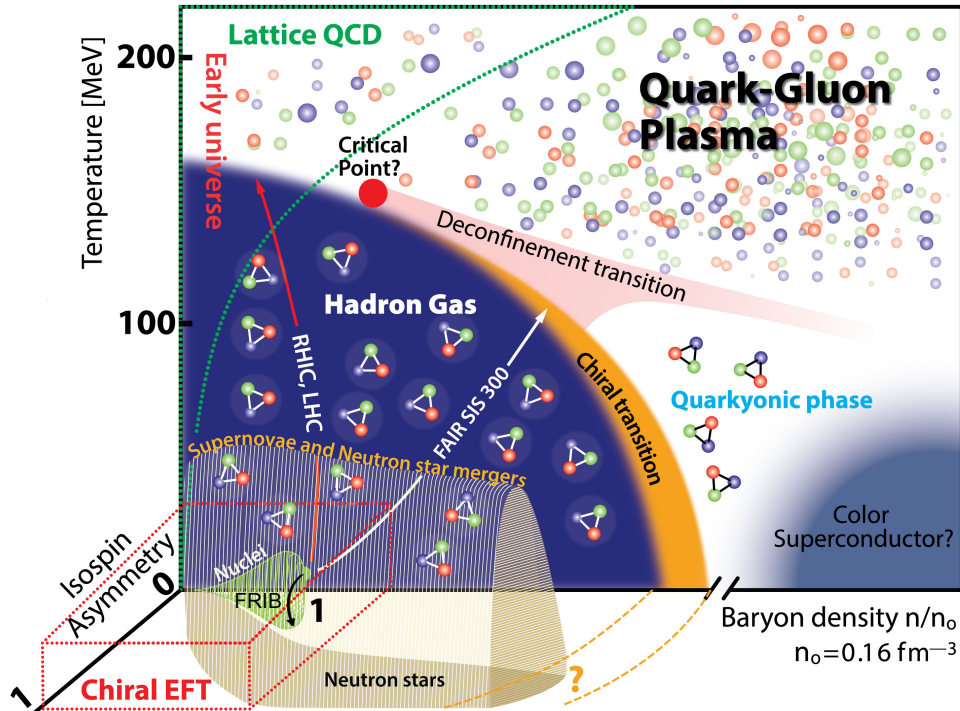
Huth, Wellenhofer, and Schwenk, PRC **103**, 025803

**remarkable consistency** between theory predictions, experiment, and astrophysics



**BAND Manifesto**,  
Phillips, Furnstahl, Heinz *et al.*,  
JGP: NP **48** 07200





## Chiral Effective Field Theory and the High-Density Nuclear Equation of State

Annual Review of Nuclear and Particle Science

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C. Drischler,<sup>1,2,3</sup> J.W. Holt,<sup>4</sup> and C. Wellenhofer<sup>5,6</sup>

<sup>1</sup>Department of Physics, University of California, Berkeley, California 94720, USA

<sup>2</sup>Nuclear Science Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA

<sup>3</sup>Facility for Rare Isotope Beams, Michigan State University, East Lansing, Michigan 48824, USA; email: [drischler@frib.msu.edu](mailto:drischler@frib.msu.edu)

<sup>4</sup>Cyclotron Institute and Department of Physics and Astronomy, Texas A&M University, College Station, Texas 77843, USA

<sup>5</sup>Institut für Kernphysik, Technische Universität Darmstadt, 64289 Darmstadt, Germany

<sup>6</sup>ExtreMe Matter Institute EMMI, GSI Helmholtzzentrum für Schwerionenforschung GmbH, 64291 Darmstadt, Germany

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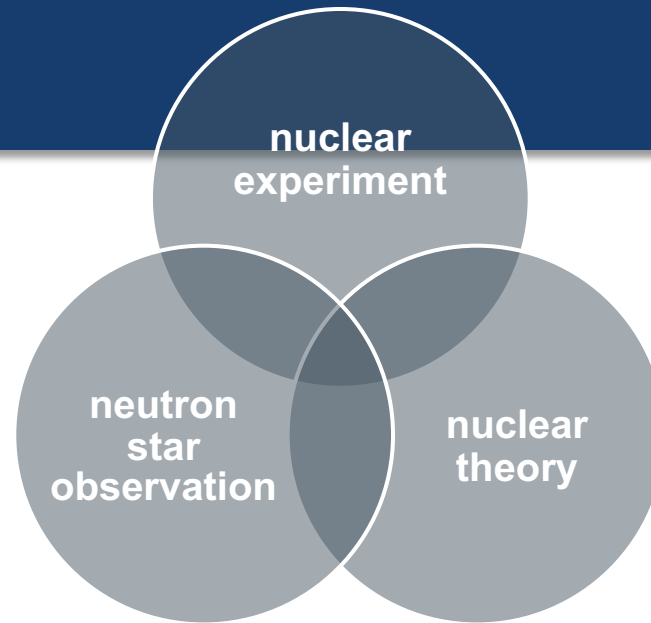
Chiral EFT | neutron stars | MBPT  
nuclear matter at zero and finite temperature  
Bayesian uncertainty quantification  
recent neutron star observations

see also in the same journal:

James Lattimer, *Annu. Rev. Nucl. Part. Sci.* **71**, 433

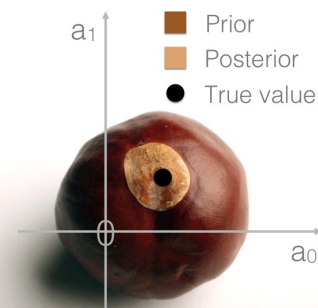
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multi-messenger  
nuclear precision  
FRIB } era



unique opportunity to obtain a **fundamental understanding** of strongly interacting matter, with great **potential for discoveries**

- 1 Upcoming observational (and experimental) campaigns will provide **stringent constraints** on the properties of neutron stars.
- 2 Chiral EFT enables **microscopic predictions** of nuclear matter (and nuclei) with **quantified uncertainties** to interpret these empirical constraints.
- 3 **Automated MBPT**: efficient EOS calculations across a wide range of densities, isospin asymmetries, and temperatures, as well as nuclear interactions.
- 4 Bayesian methods: powerful tools for quantifying & propagating **correlated uncertainties** in EFT-based calculations (*model checking* is important).



Many thanks to:

R. Furnstahl S. Han J. W. Holt J. Lattimer K. McElvain  
J. Melendez D. Phillips M. Prakash S. Reddy C. Wellenhofer T. Zhao