

# The APEX Experiment; a dark matter search at Jefferson Lab Hall A

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of Glasgow

Jefferson Lab

Simple dark sector model: only introduces a single gauge boson.

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{\epsilon}{2} F^{\mu\nu} F'_{\mu\nu} + F'^{\mu\nu} F'_{\mu\nu} + m_{A'}^2 A'^{\mu} A'_{\mu}$$

This adds to the Standard Model Lagrangian,  $\mathcal{L}_{\text{SM}}$ :

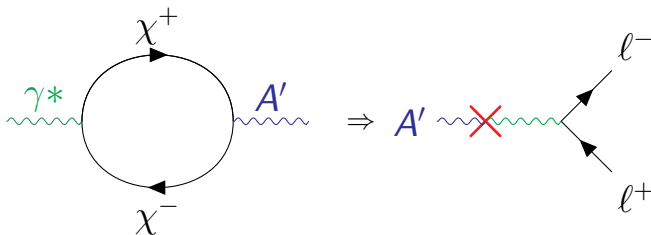
- A term analogous to the SM electromagnetic force.
- A term analogous to the massive weak bosons in the SM.
- A **kinematic mixing** term, which combines terms from the Standard Model and new dark sector.

## Kinematic mixing

Kinematic mixing parameter,  $\epsilon^2 = \frac{\alpha'}{\alpha_{\text{EM}}}$ , is one of the parameters measured by experiments.

# Kinematic mixing

*Kinematic mixing* refers to interactions crossing between the Standard Model and dark sector.



*(Visible Dark Photons)*

The new gauge boson ( $A'$ ) serves as a mediator of a 'hidden sector' which can kinematically mix with the SM photon.

- Holdom, Phys. Lett. B 166, 1986

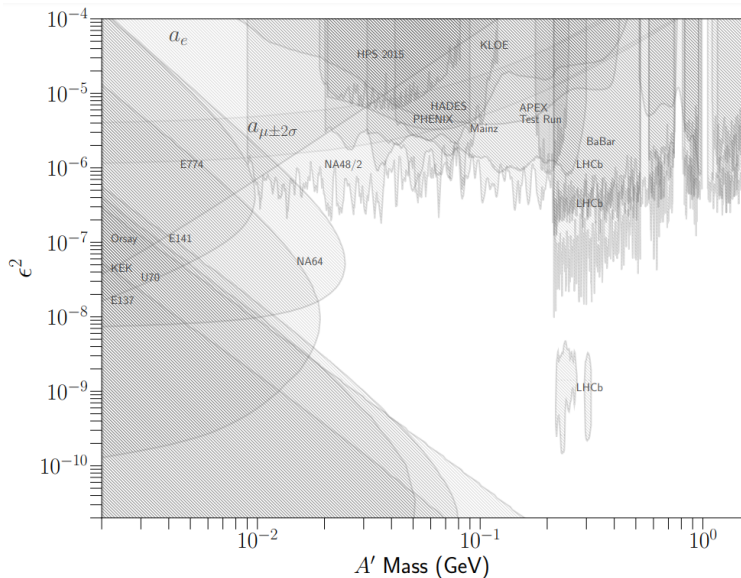
Depending on the mass and lifetimes of the  $A'$  and its potential dark matter companions,  $\chi$ , DM searches at colliders can look for

- a displaced vertex
- missing mass in the final state
- a bump in the background invariant mass spectrum

All of these are used by experiments past, current and future.

- APEX is a *bump hunt*.

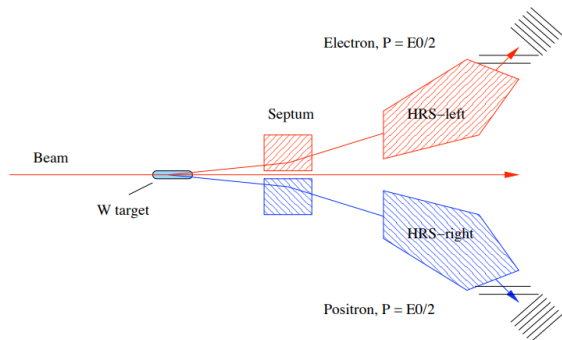
# Current status from published results



APEX was located in Hall A at Jefferson Lab, using a 2.138 GeV electron beam (provided by the CEBAF), incident on a tungsten target (10 foils for a total thickness of  $0.028 X_0$ ).

Invariant mass reconstructed from coincidence hits in two-arm High Resolution Spectrometer (HRS):  $e^-$  in LHRS and  $e^+$  in RHRS.

Each spectrometer was set to a central scattering angle of  $5^\circ$ , with an in-plane angular resolution of  $\sim 0.6$  mrad ( $\sim 1$  MeV invariant mass resolution).



HRS detector stack  
the same in both  
arms:

- 2 planes of scintillators, for timing
- VDC's, for tracking
- calorimeters and Cherenkov detectors, for PID

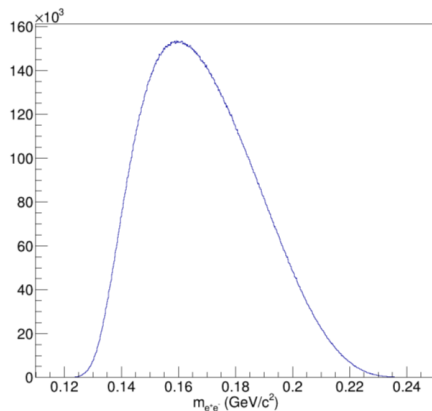
# Invariant mass spectrum

APEX reconstructed invariant mass of  $e^+e^-$  pairs, hitting the HRS arms in coincidence.

In 2010, a test run was taken for APEX, which recorded  $\sim 7.7 \times 10^5$  events; the full 2019 run recorded  $\sim 5.6 \times 10^7$   $e^+e^-$  pairs.

Blinded sample of full data set (10%) was used to fix the analysis procedure.

Once agreed upon, the data is unblinded for the final analysis.





# APEX Peak Search: Strategy/Outline

- **Discovery:** scan through final invariant mass spectrum and search for statistically significant peak (taking into account Look Elsewhere Effect).
  - Standard  $5\sigma$  for discovery.
- **Limit Setting:** set upper limits for number of signal events throughout mass spectrum, convert to limit in  $\epsilon^2$ .
- Fitting potential peak as Gaussian, over background (which can be modelled in different ways).

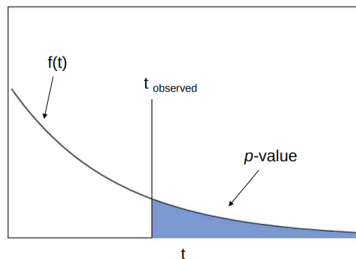
# APEX Peak Search: Discovery

- **Wilks' theorem:** under null hypothesis the log-likelihood ratio,  $t = -2 \ln(\lambda)$ , approaches the  $\chi^2$  distribution with degrees of freedom equal to parameters of interest ( $H_1 - H_0$ )
- Define test statistic,  $\tilde{q}_\mu$ , for discovery (with null hypothesis:  $\mu = 0 \implies \tilde{q}_0$ )

$$\lambda(\mu = 0) = \frac{L(\mu = 0, \hat{B}, \hat{a}_i)}{L(\hat{\mu}, \hat{B}, \hat{a}_i)}$$

$$p_\mu = \int_{\tilde{q}_{\mu, obs}}^{\infty} f(\tilde{q}_\mu | \mu) d\tilde{q}_\mu$$

$$\tilde{q}_0 = \begin{cases} -2 \ln(\lambda(0)) & \hat{\mu} > 0 \\ +2 \ln(\lambda(0)) & \hat{\mu} \leq 0 \end{cases}$$



- Take Look Elsewhere Effect (LEE) into account:  $p \Rightarrow p \frac{\text{mass range}}{\text{mass res}}$

# APEX Peak Search: Setting upper limit

- Start with value of  $\mu$  at each  $m$  and iterate potential  $\mu'$  until C.L. (Confidence Level) derived from  $\lambda$  reaches pre-set level (0.05) (similar to p-level test)

$\rightarrow \mu_{up}$

- Define 'median limit' as the median value of the signal upper limits from pseudo-experiments (used in 2010 analysis, only used as reference for current search)

$\rightarrow \mu_{median}$

- Translate Confidence Levels for number of signal events at different  $m_{A'}$ 's into limits on  $\alpha'/\alpha$
- Cross section from proposal of  $A'$  production to radiative trident cross section

$$\frac{d\sigma(A')}{d\sigma(\gamma^*)} = \left( \frac{3\pi\epsilon^2}{2N_{eff}\alpha} \right) \frac{m_{A'}}{\delta m}$$

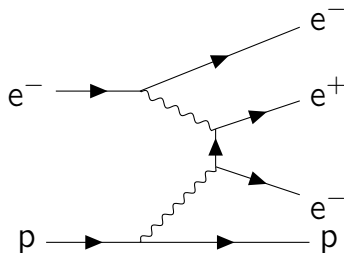
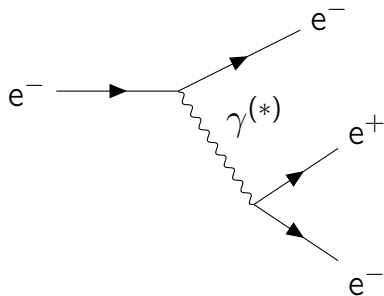
- Using the radiative fraction,  $f$ , to scale to full trident cross section, we can derive:

$$\epsilon^2 = \left( \frac{\alpha'}{\alpha_{fs}} \right)_{max} = \frac{1}{f} \frac{\mu_{up}}{(B/\delta m)} \frac{2N_{eff}\alpha}{3\pi m_{A'}}$$

# Radiative fraction

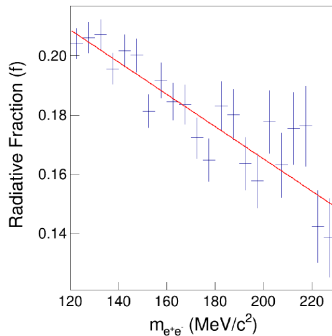
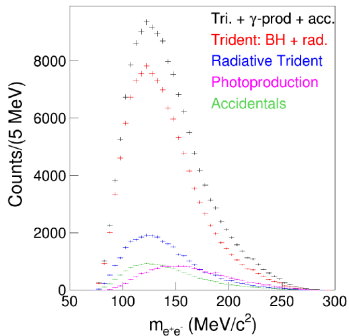
Primary backgrounds to the  $A'$  decay process include:

- Real  $e^+e^-$  photoproduction
- Radiative trident events
- Bethe-Heitler tridents



# Radiative fraction

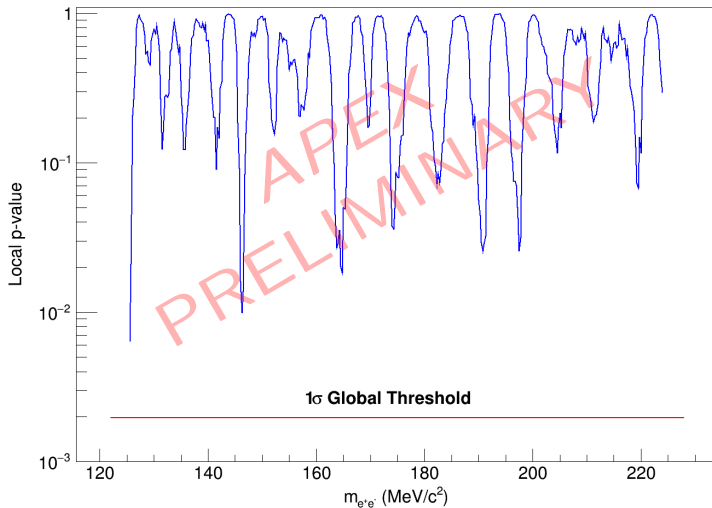
Radiative fraction,  $f$ , is the ratio of radiative trident events to the total background (as a function of invariant mass).



Trident and photoproduction BH counts are simulated using cross-sections calculated in MadGraph.

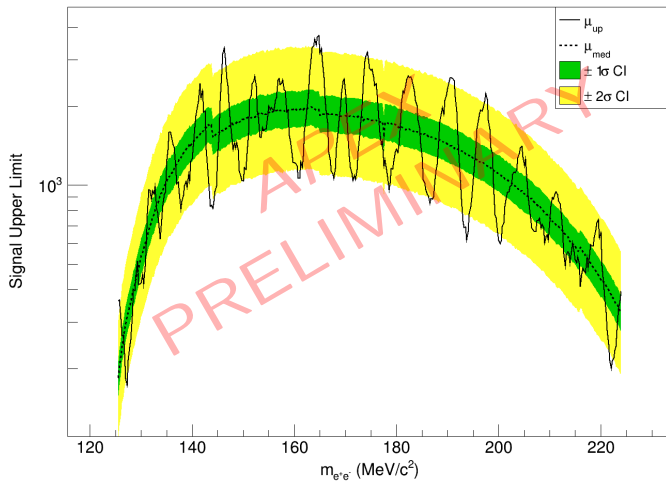
# APEX results: blinded data set

Analysis performed on blinded data set; shows *no significant signal*.



# APEX results: blinded data set

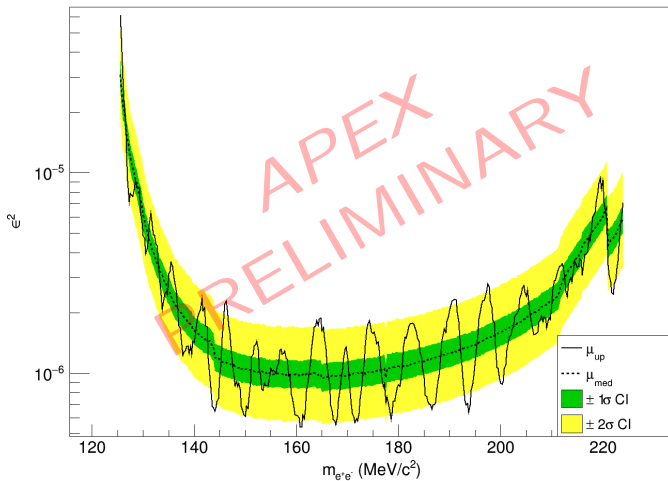
Analysis performed on blinded data set; looking at upper limits on signal counts, and 1 and 2 $\sigma$  confidence intervals.



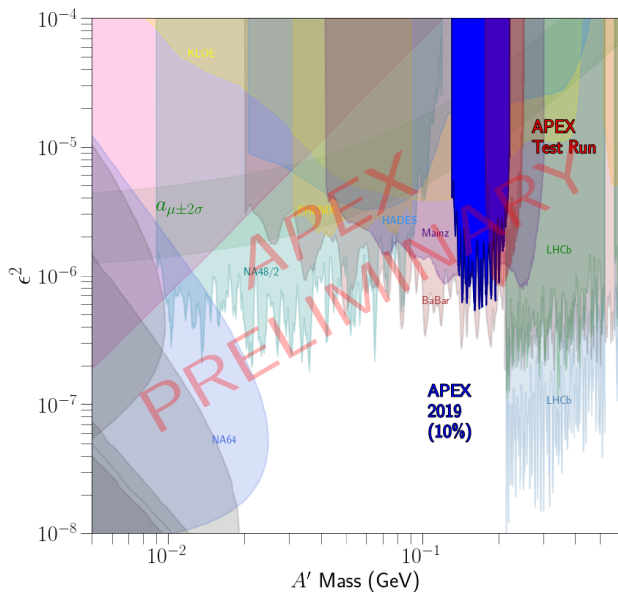


# APEX results: blinded data set

Analysis performed on blinded data set; looking at sensitivity covered by data.



# APEX results: blinded data set



- Systematic studies; inc. invariant mass resolution and choice of background function.
- Recovery of statistics from low efficiency runs.
- Run full peak search on unblinded 2019 data set.

Thank you for listening!  
Any questions?

# BACK UP SLIDES

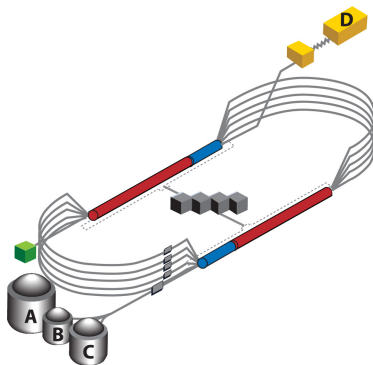
Consider that the dark photon,  $A'$ , has mass  $m_{A'}$ , and that the dark particles involved in kinematic mixing have mass  $m_\chi$ .

- If  $2m_e < m_{A'} < 2m_\chi$ , and the  $A'$  lifetime is small, use a **bump hunt**.
- If  $2m_e < m_{A'} < 2m_\chi$ , and the  $A'$  lifetime is non-negligible, search for a **displaced vertex**.
- If  $m_{A'} > 2m_\chi$ , or the  $A'$  lifetime is very large, look for **missing mass**.

# CEBAF at JLab

The **C**ontinuous **E**lectron **B**eam **A**ccelerator **F**acility at JLab.

- Continuous wave, 12 GeV electron beam
- Polarisable
- Delivers to 4 experimental halls, simultaneously



By default, the Hall A HRS pair has a minimum opening angle of  $25^\circ$ .

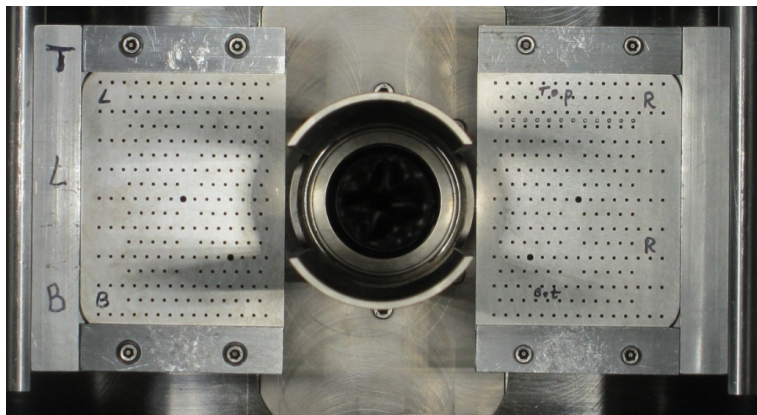
$A'$  production is focused at small angles; APEX employed a septum magnet to reach a central angle of  $5^\circ$  for each HRS arm.

APEX therefore requires a way to reconstruct the tracks in the HRS arms that is fine-tuned to this non-standard setup.



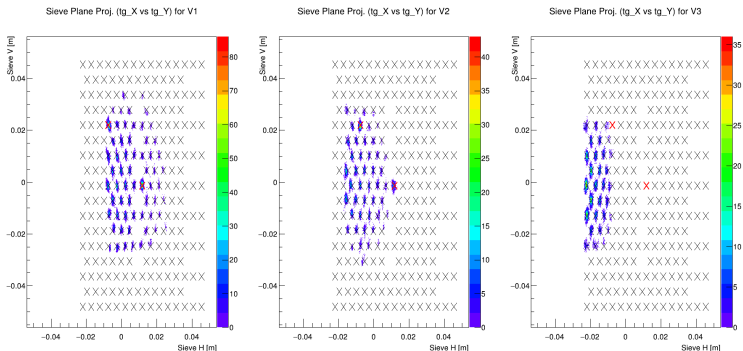
# APEX set-up; angular reconstruction

Sieve slits are placed in front of the septum. The reconstruction of the slit patterns off calibration targets can then be applied to data in the main run.



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# APEX Peak Search: Discovery

- Scan mass range testing different mass hypothesis with fixed mass range window centred at new mass hypothesis,  $m_{A'}$
- Form Profile Likelihood Ratio (PLR),  $\lambda(\mu)$ , from probability expression:

$$\lambda(\mu) = \frac{L(\mu, \hat{\hat{B}}, \hat{\hat{a}}_i)}{L(\hat{\mu}, \hat{B}, \hat{a}_i)}$$

- Where  $\mu$  is signal being tested ( $\#$  signal events),  $\hat{\hat{B}}$  is the background and  $\hat{\hat{a}}_i$  background parameters that maximise S (conditional Maximum Likelihood Estimators (MLEs))
- Denominator gives best fit of data: unconstrained MLEs

# Invariant Mass Resolution

$$\left(\frac{\delta_m}{m}\right)^2 = \left(\frac{\delta_p}{p}\right)^2 + 0.5 \times \left(\frac{\delta_\theta}{\theta}\right)^2$$

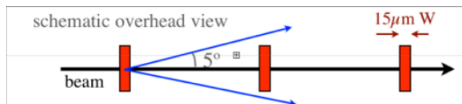
$$(\delta_\theta)^2 = (\delta_{\theta_{HRS}})^2 + (\delta_{\theta_{MS}})^2$$

$$\delta_p = 1 * 10^{-4} \Rightarrow \delta_\theta \text{ dominates}$$

$\delta_{\theta_{HRS}}$  is the HRS angular resolution contribution

$\delta_{\theta_{MS}}$  is the Multiple Scattering contribution

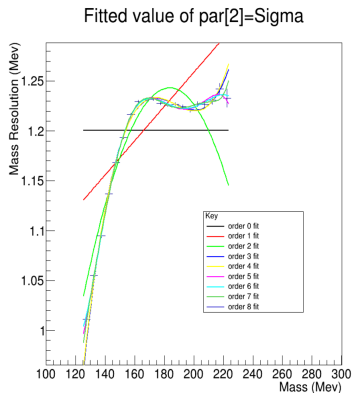
- $\delta_{\theta_{MS}}$  reduced by narrow targets (segmented):



- $(\delta_{\theta_{HRS}})$  is comprised of errors in track measurement in HRS and imperfections in optics reconstruction matrix.

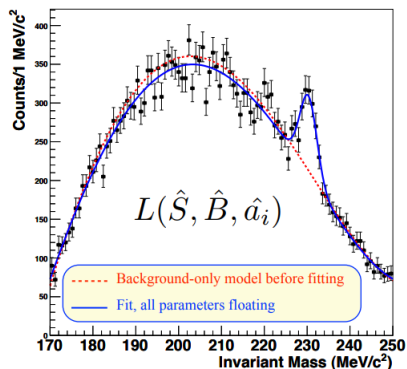
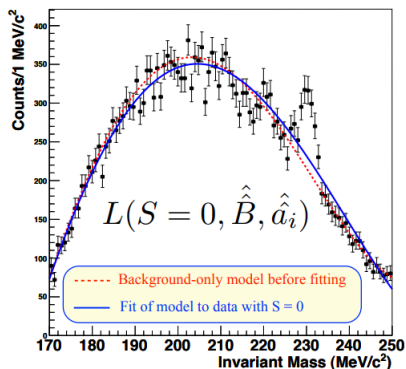
# Invariant Mass Resolution Function

- Need to obtain  $\delta m$  as function of  $m$ :  $\delta m = f(m)$
- Use angular resolutions (with multiple scattering) and momentum resolution to vary angles and momentum and calculate new mass ( $m'$ ), take difference with original mass,  $m$
- 5th order fit determined to be optimal to describe  $\delta m$



# APEX Peak Search: Discovery

$$\lambda(\mu = 0) = \frac{L(\mu = 0, \hat{\hat{B}}, \hat{\hat{a}}_i)}{L(\hat{\mu}, \hat{B}, \hat{a}_i)}$$



- (Plot from J. Beacham, with  $S = \mu$ )

# Fit logic: Look Elsewhere Effect (LEE)

- LEE: tested range of equally likely  $m_{A'}$  hypothesis, so should punish CL (the more  $m_{A'}$  hypotheses tested the more likely one is true by chance)
- crude version of correction to p values:

$$p \Rightarrow p \frac{\text{mass range}}{\text{mass res}}$$

$$\epsilon^2 = \left( \frac{\alpha'}{\alpha_{fs}} \right)_{max} = \frac{1}{f} \frac{\mu_{up}}{(B/\delta m)} \frac{2N_{eff}\alpha}{3\pi m_{A'}}$$

- $B/\delta m$  is the number of background events within a 1 MeV window around the tested mass.
- $\mu_{up}$  is the upper limit on the number of signal events, as defined by the confidence level.
- $N_{eff}$  is a scaling factor dependent on the mass of the  $A'$ :

$$N_{Eff} = \begin{cases} 1 & m_{A'} < 2m_{\mu} \\ 2 + R(m_{A'}) & m_{A'} \geq 2m_{\mu} \end{cases}$$

where  $R(m_{A'}) = \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$  is an energy-dependent term.