

Parity-Violating Electron Scattering as a Test of the Standard Model

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Blacksburg, Virginia, USA

14th Conference on the Intersections of Particle and Nuclear Physics

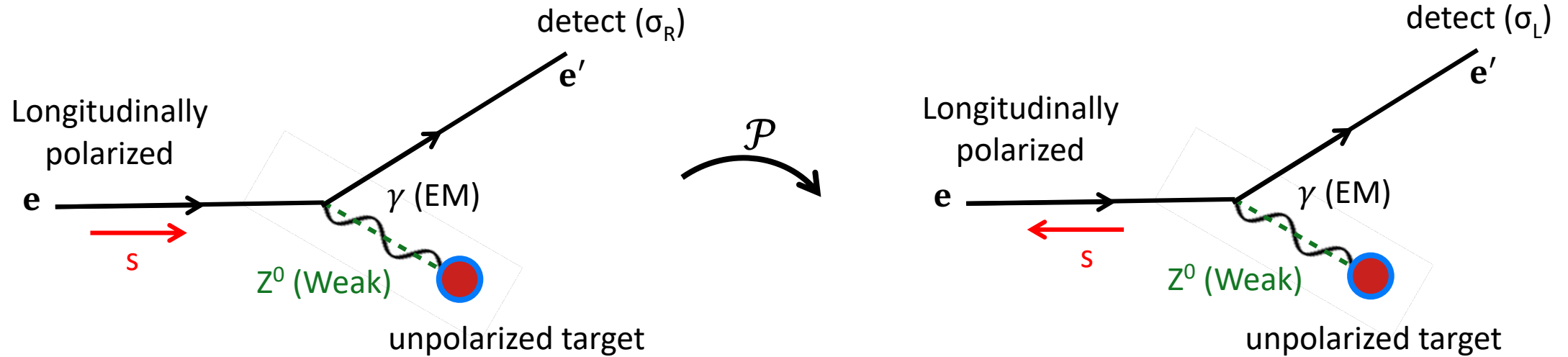


Outline

- Parity-violating electron scattering (PVeS) introduction
- History of PVeS experiments
- Electron scattering off electrons, protons, and quarks
 - Program to Search for New Neutral Current Interactions Beyond the Standard Model
 - Brief Review of Past Measurements
 - The Future: MOLLER, P2 and SoLID
- Summary and outlook

Parity-Violation in Electron Scattering

- Scattering of longitudinally polarized electrons from unpolarized targets.



- We change electron's helicity to mimic parity operation.
- Asymmetry (A_{PV}) of the detected rates between the beam's opposite helicity states.

$$A_{PV} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} \quad \text{where } \sigma \sim |\mathcal{M}_\gamma + \mathcal{M}_{Z^0}|^2$$

- At $Q^2 \ll (M_{Z^0})^2$, A_{PV} is dominated by the [interference between the weak and electromagnetic amplitudes](#).

$$A_{PV} \approx \frac{2\mathcal{M}_\gamma(\mathcal{M}_{Z^0})^*}{|\mathcal{M}_\gamma|^2} \sim 10^{-5} \cdot Q^2 \text{ to } 10^{-4} \cdot Q^2$$

PVeS Technique (SLAC E122 Experimental Blueprint)

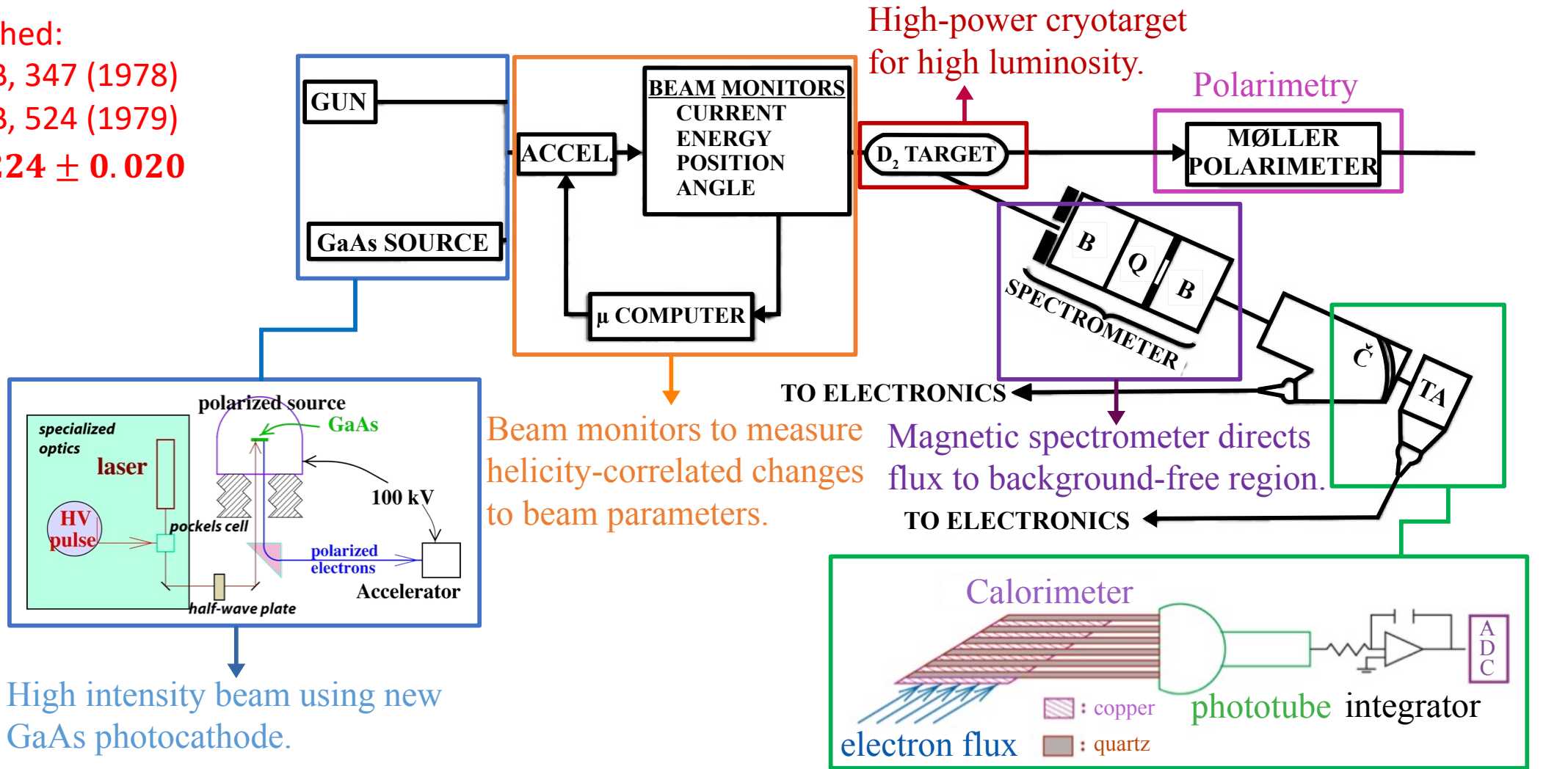
First observation of PV in weak neutral current

Published:

Phys. Lett. 77B, 347 (1978)

Phys. Lett. 84B, 524 (1979)

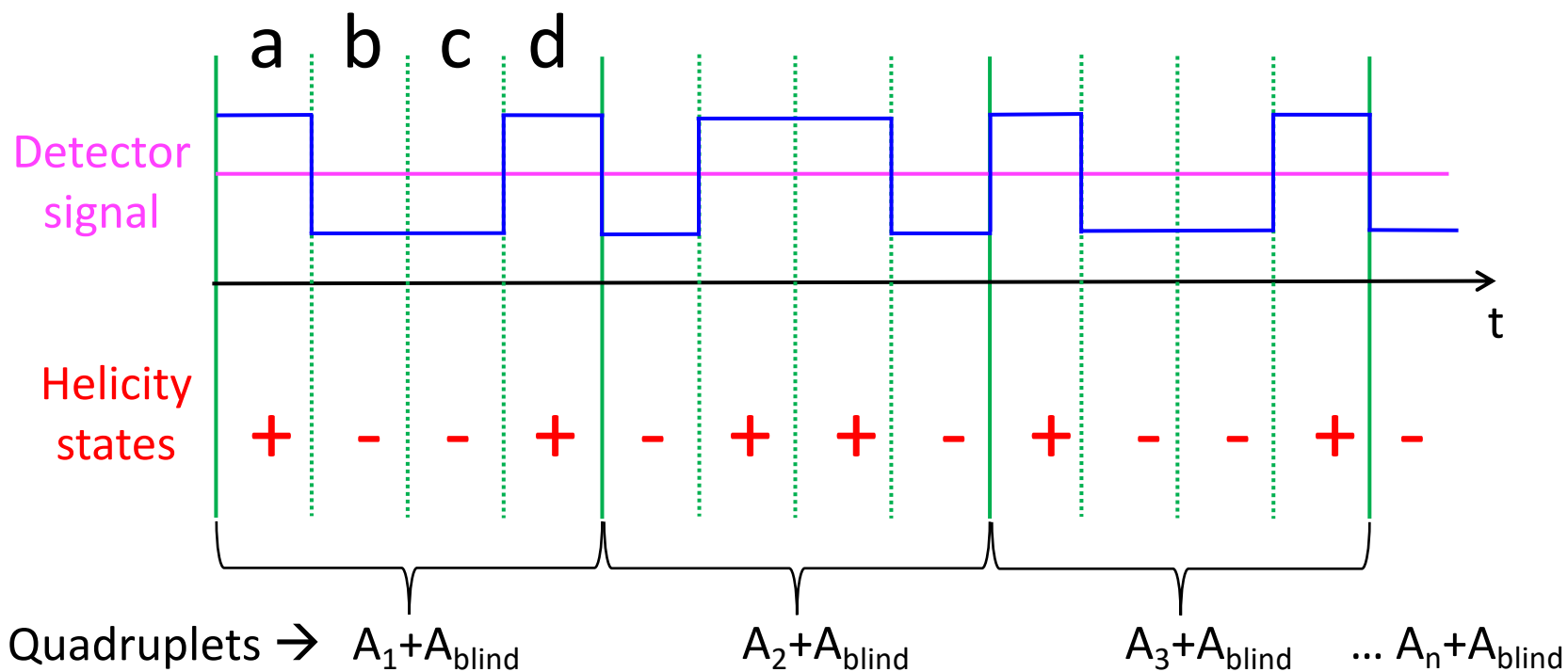
$$\sin^2 \theta_W = 0.224 \pm 0.020$$



High intensity beam using new GaAs photocathode.

Flux integration measures high rate without dead-time.

PVeS Technique Contd.



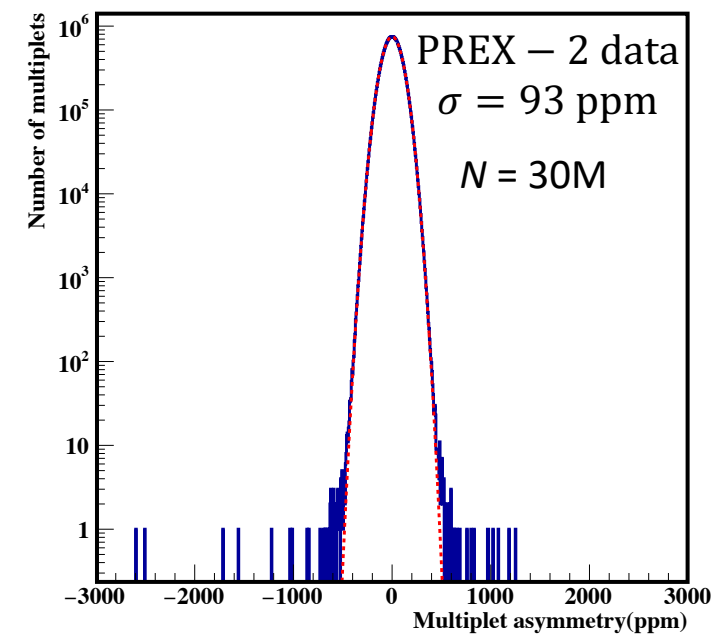
$$A_1 = \frac{(a + d) - (b + c)}{a + b + c + d}$$

Measure flux F for each helicity window

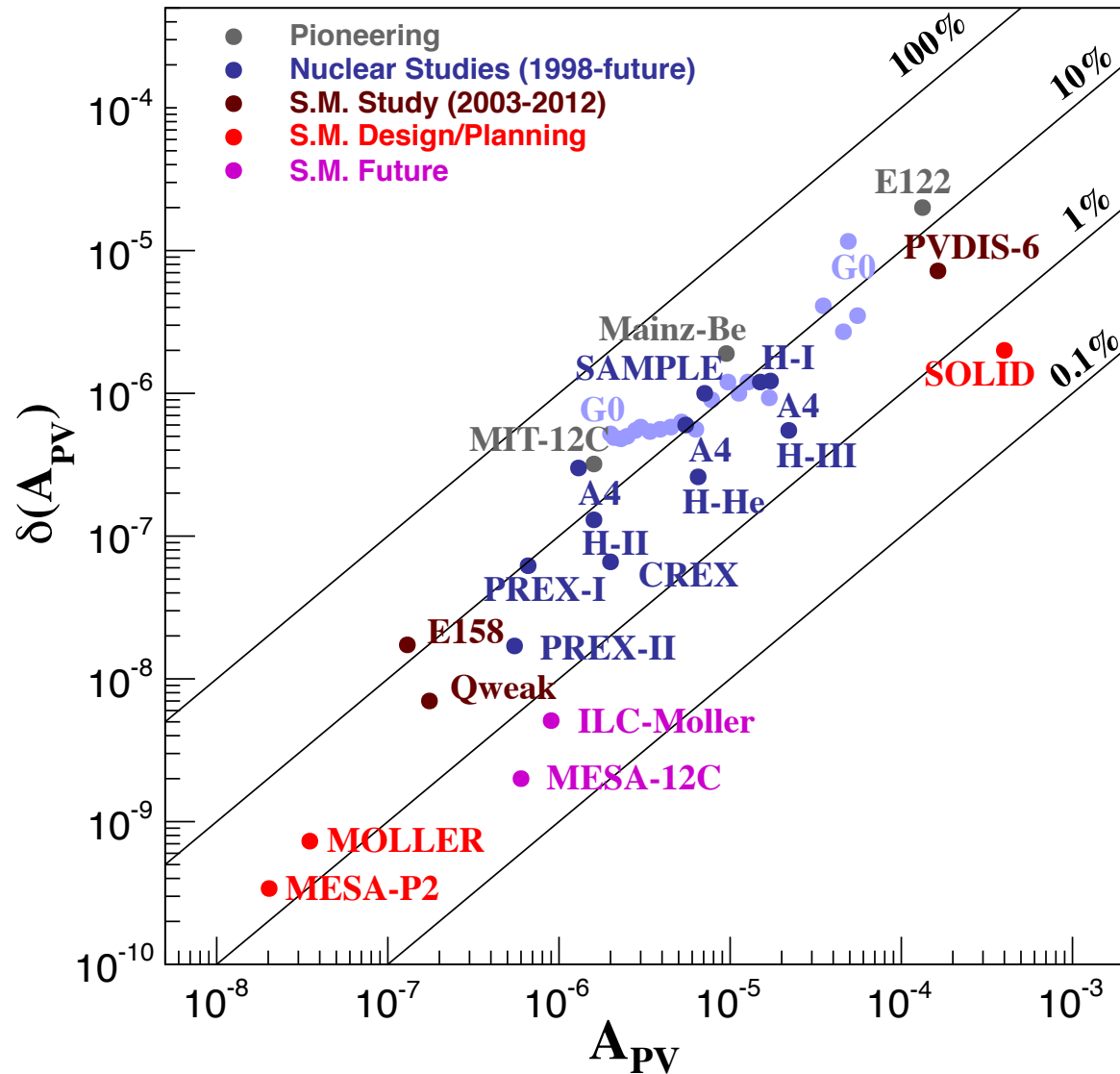
$$A_{\text{pair}} = \frac{F_R - F_L}{F_R + F_L}$$

For N window pairs: $A \pm \frac{\sigma}{\sqrt{N}}$

For MOLLER, $N = 30B$



Historical Perspective of PVeS



- E122 – 1st PVeS exp. (late 70's) at SLAC
- E158 – PV in Møller scattering at SLAC (2005)
- Significant improvement over time:
 - Photocathodes
 - Polarimetry
 - Cryotargets
 - Beam stability to nanometer level
 - Low noise electronics
 - Radiation-hard detectors

PVeS has become a precision tool!

- Beyond standard model searches
- Strange quark form factors
- Neutron skin of a heavy nucleus
- QCD structure of the nucleon

State-of-the-art:

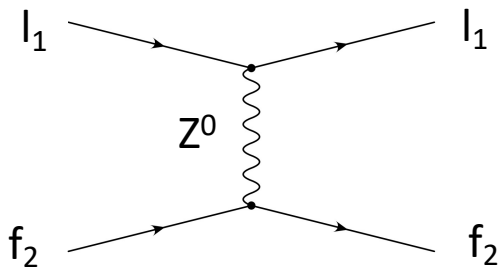
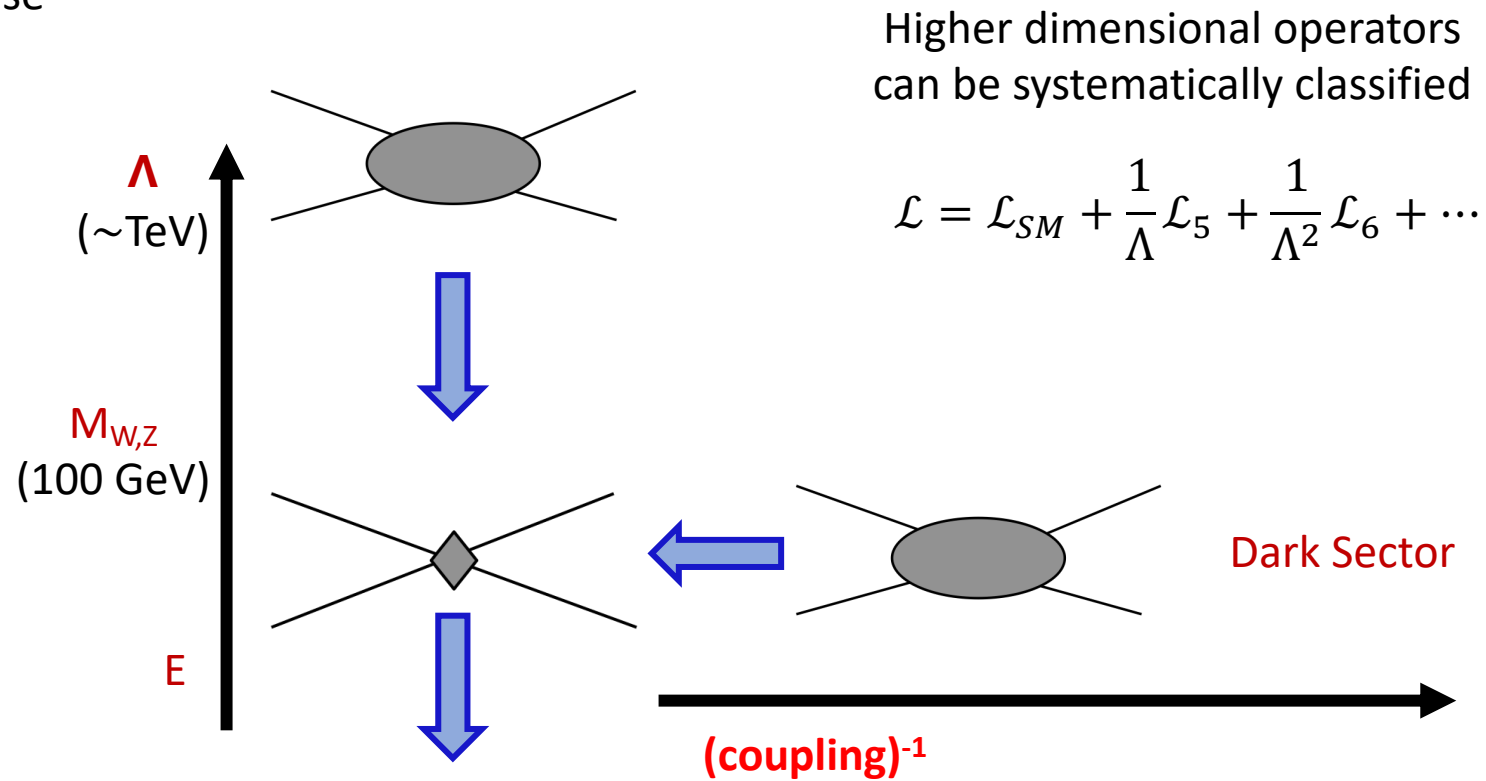
- Sub-part per billion statistical reach and systematic control
- Sub-1% normalization control

Modern Electroweak Physics

- Unraveling “New Dynamics” in the early universe
 - How did nuclear matter form and evolve?
- Nuclear Physics Initiatives:
 - Low Energy $\rightarrow Q^2 \ll M_Z^2$

courtesy
V. Cirigliano,
H. Maruyama,
M. Pospelov

High Energy Dynamics:



Leptonic and semileptonic weak neutral current interactions

Search for new flavor diagonal neutral currents
 Tiny yet measurable deviations from precisely calculable SM processes
 must reach $\Lambda \sim 10$ TeV

$$\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{\Lambda} \mathcal{L}_5 + \frac{1}{\Lambda^2} \mathcal{L}_6 + \dots$$

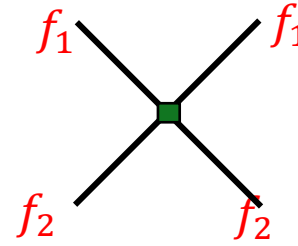
$$\frac{1}{\Lambda^2} \mathcal{L}_6$$

Weak Neutral Current Couplings

In GWS model, the weak neutral current $V - A$ couplings to the Z^0 are:

$$\begin{aligned}
 C_{1u} &= -\frac{1}{2} + \frac{4}{3} \sin^2 \theta_W \\
 C_{1d} &= \frac{1}{2} - \frac{2}{3} \sin^2 \theta_W \\
 C_{2u} &= -\frac{1}{2} + 2 \sin^2 \theta_W \\
 C_{2d} &= \frac{1}{2} - 2 \sin^2 \theta_W
 \end{aligned}$$

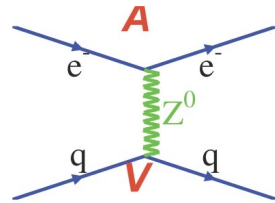
+ New Physics



$$\mathcal{L}_{f_1 f_2} = \sum_{i,j=L,R} \frac{(g_{ij}^{12})^2}{\Lambda_{ij}^2} \bar{f}_{1i} \gamma_\mu f_{1i} \bar{f}_{2j} \gamma_\mu f_{2j}$$

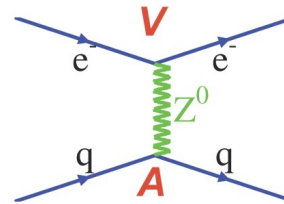
For $Q^2 \ll M_{Z^0}^2$, restrict to $e - q$ and $e - e$ four-fermion contact interactions:

$$\mathcal{L}^{PV} = \frac{G_F}{\sqrt{2}} \left[\bar{e} \gamma^\mu \gamma_5 e (C_{1u} \bar{u} \gamma_\mu u + C_{1d} \bar{d} \gamma_\mu d) + \bar{e} \gamma^\mu e (C_{2u} \bar{u} \gamma_\mu \gamma_5 u + C_{2d} \bar{d} \gamma_\mu \gamma_5 d) + C_{ee} \bar{e} \gamma^\mu \gamma_5 e (\bar{e} \gamma_\mu e) \right]$$



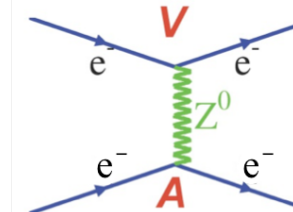
$$C_{1i} \equiv 2g_A^e g_V^i$$

quark vector: C_{1u}, C_{1d}



$$C_{2i} \equiv 2g_V^e g_A^i$$

quark axial-vector: C_{2u}, C_{2d}



$$C_{ee} \equiv 2g_V^e g_A^e$$

electron: C_{ee}

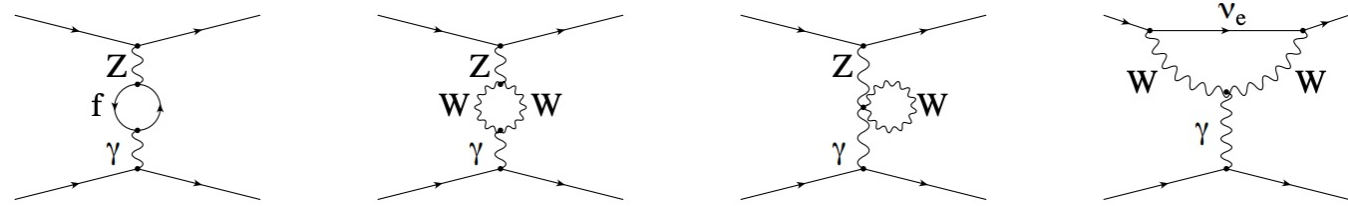
$$C_{1q} \propto (g_{RR}^{eq})^2 + (g_{RL}^{eq})^2 - (g_{LR}^{eq})^2 - (g_{LL}^{eq})^2 \rightarrow \text{PV Elastic e-N scattering, Atomic parity violation}$$

$$C_{2q} \propto (g_{RR}^{eq})^2 - (g_{RL}^{eq})^2 + (g_{LR}^{eq})^2 - (g_{LL}^{eq})^2 \rightarrow \text{PV deep inelastic scattering}$$

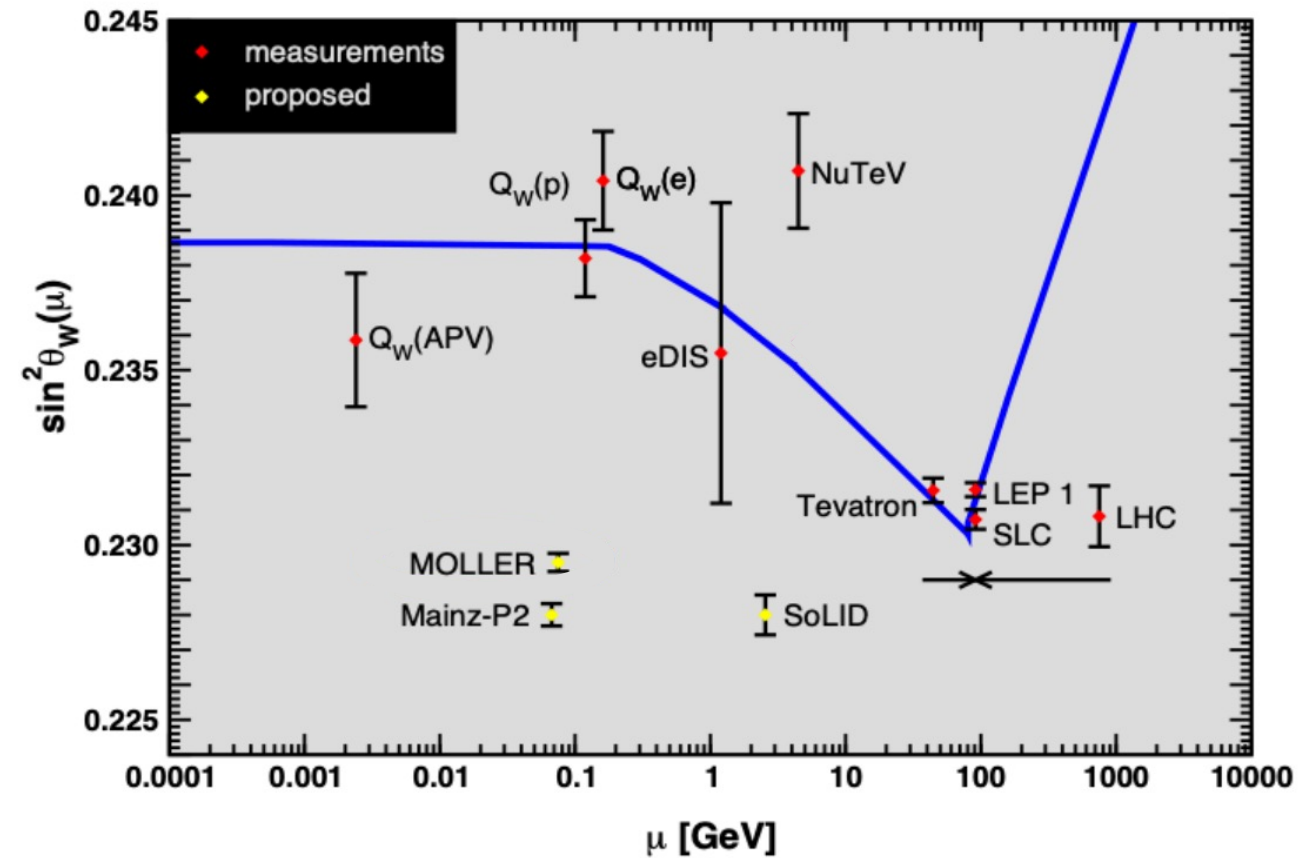
$$C_{ee} \propto (g_{RR}^{ee})^2 - (g_{LL}^{ee})^2 \rightarrow \text{PV Møller scattering}$$

Running of the Weak Mixing Angle $\sin^2 \theta_W$ – Standard Model Test

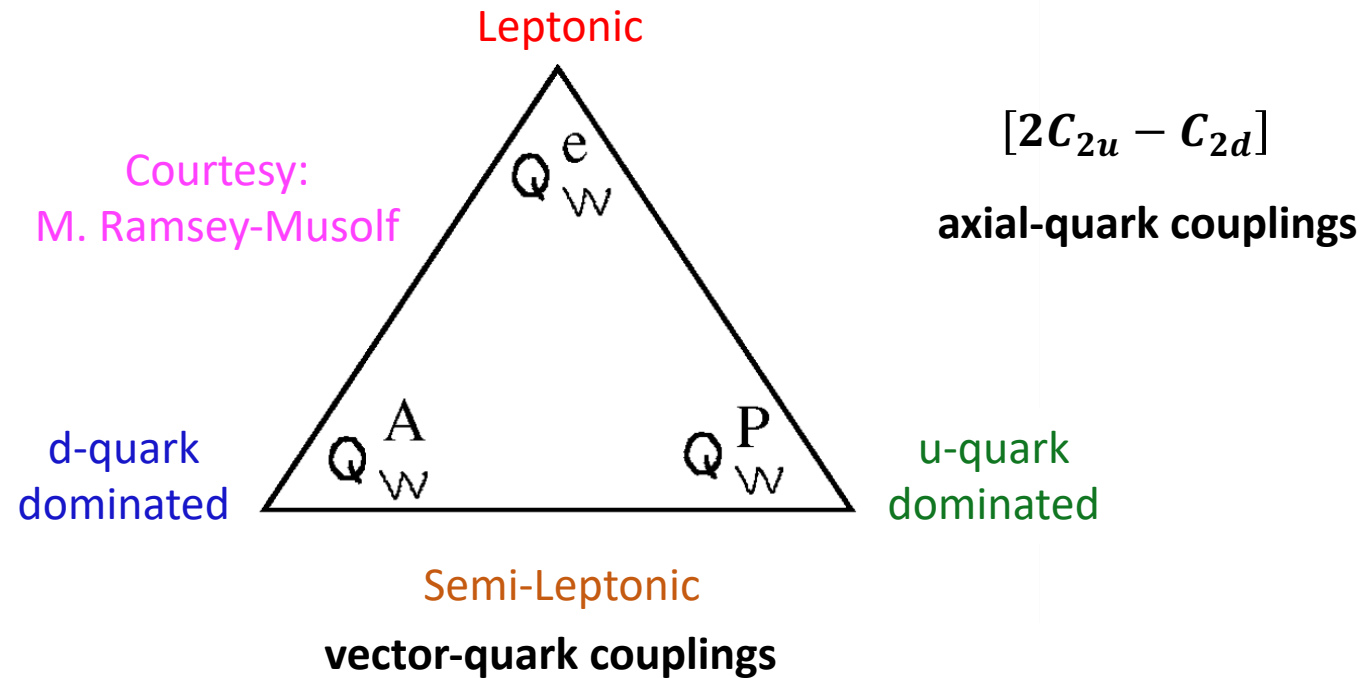
Electroweak radiative corrections cause the running of $\sin^2 \theta_W$



- Atomic Parity Violation (APV): ^{133}Cs
- Neutrino Deep Inelastic Scattering: NuTeV
- Parity-Violating Møller Scattering: E158 at SLAC
 - statistics limited; theory robust
 - next generation: MOLLER; factor of 5 improvement
- Parity-Violating e-p Scattering: Qweak
 - theory robust at low beam energy
 - next generation: P2; factor of 3 improvement
- Parity-Violating Deep Inelastic Scattering: PVDIS
 - theory robust for ^2H in valance quark region
 - next generation: SoLID; factor of 5 improvement



Low Energy Weak Neutral Current – Sensitivity to New Physics Models



- SUSY Loops → Q_W^e and Q_W^P : same absolute shift, smaller for others
- GUT Z' → High for $Q_W(C_s)$, Q_W^e (relative), smaller for others
- Leptophobic Z' → axial-quark couplings (C_2 's) only
- RPV SUSY → Different for all four in sign and magnitude
- Leptoquarks → semi-leptonic only; different sensitivities
- Lepton Number Violation → Q_W^e only

Fixed Target vs Collider Complementarity for Leptons

$$\mathcal{L}_{f_1 f_2} = \sum_{i,j=L,R} \frac{(g_{ij}^{12})^2}{\Lambda_{ij}^2} \bar{f}_{1i} \gamma_\mu f_{1i} \bar{f}_{2j} \gamma_\mu f_{2j}$$

Conventional Collider Contact Interaction Analysis: $|g_{RR}^2 - g_{LL}^2| = 4\pi$

Simultaneous fits to cross-sections and angular distributions

Model	η_{LL}^f	η_{RR}^f	η_{LR}^f	η_{RL}^f
LL^\pm	± 1	0	0	0
RR^\pm	0	± 1	0	0
LR^\pm	0	0	± 1	0
RL^\pm	0	0	0	± 1
VV^\pm	± 1	± 1	± 1	± 1
AA^\pm	± 1	± 1	∓ 1	∓ 1
VA^\pm	± 1	∓ 1	± 1	∓ 1

95% C.L.

LEP-200

$$\Lambda_{LL}^l \sim 12.8 \text{ TeV}$$

$$\Lambda_{RR}^l \sim 12.2 \text{ TeV}$$

$$\Lambda_{VV}^l \sim 22.2 \text{ TeV}$$

E158 Reach (actual limits asymmetric)

$$\Lambda_{LL}^{ee} \sim 12 \text{ TeV}$$

$$\Lambda_{RR-LL}^{ee} \sim 17 \text{ TeV}$$

MOLLER Reach

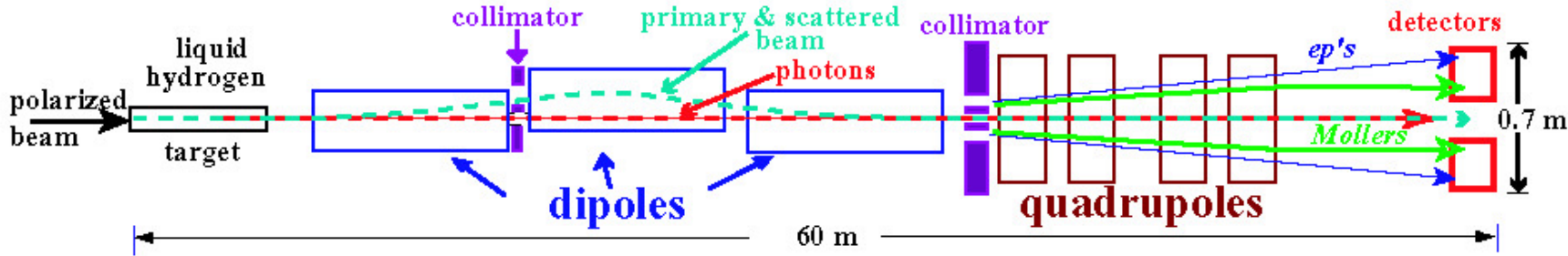
$$\Lambda_{LL}^{ee} \sim 27 \text{ TeV}$$

$$\Lambda_{RR-LL}^{ee} \sim 38 \text{ TeV}$$

LEP-200 insensitive

MOLLER is accessing discovery space that cannot be reached until the advent of a new lepton collider

E158 Experiment at SLAC: First Measurement of Q_W^e

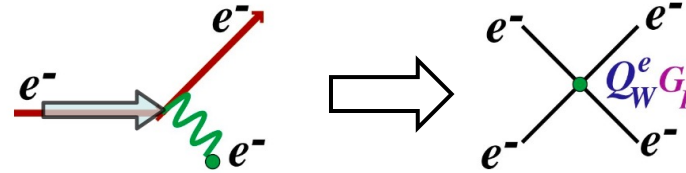


Measured at SLAC End Station A

Parameter	Value
E	48 GeV
θ	4 – 7 mrad
Q^2	$0.026 (\text{GeV}/c)^2$

Parity-Violating Møller scattering: $\vec{e} + e \rightarrow e + e$

$$A_{PV} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} = mE \frac{G_F}{\sqrt{2}\pi\alpha} \frac{4\sin^2\theta}{(3 + \cos^2\theta)^2} Q_W^e$$



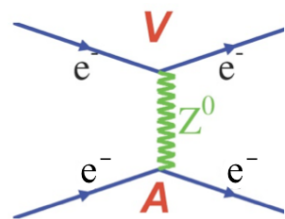
$$Q_W^e \equiv -2C_{ee} = -(1 - 4\sin^2\theta_W)$$

Published: PRL 95 081601 (2005)

$$A_{PV} = -131 \pm 14 (\text{stat.}) \pm 10 (\text{syst.}) \text{ ppb}$$

$$Q_W^e = -0.0369 \pm 0.0052$$

$$\sin^2\theta_W^{eff} = 0.2397 \pm 0.0010 (\text{stat.}) \pm 0.0008 (\text{syst.})$$



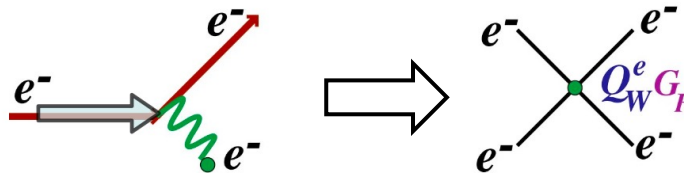
$$C_{ee} \equiv 2g_V^e g_A^e$$

electron: C_{ee}

MOLLER Experiment at JLab

- **MOLLER: Measurement Of Lepton Lepton Electroweak Reaction**
 - will have a factor of 5 improvement over E158 measurement

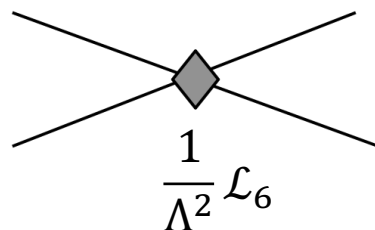
PV Møller scattering: $\vec{e} + e \rightarrow e + e$



$$A_{PV} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} = mE \frac{G_F}{\sqrt{2}\pi\alpha} \frac{4\sin^2\theta}{(3 + \cos^2\theta)^2} Q_W^e$$

$$Q_W^e = 1 - 4\sin^2\theta_W \approx 0.075$$

Parameter	Value
E	11 GeV
E'	2 – 9 GeV
θ_{CM}	60° – 90°
Target	125 cm long LH ₂
Max. Luminosity	2.4 × 10 ³⁹ cm ⁻² sec ⁻¹
Moller Rate @ 65 μA	134 GHz
Run Time	344 PAC-days
Polarization	≈ 90 %
$\langle A_{PV} \rangle$	33 ppb

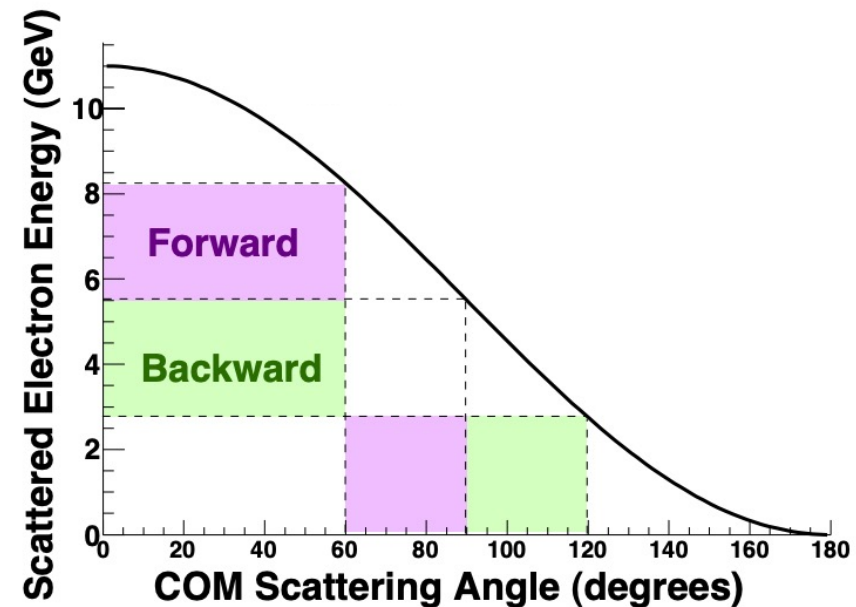
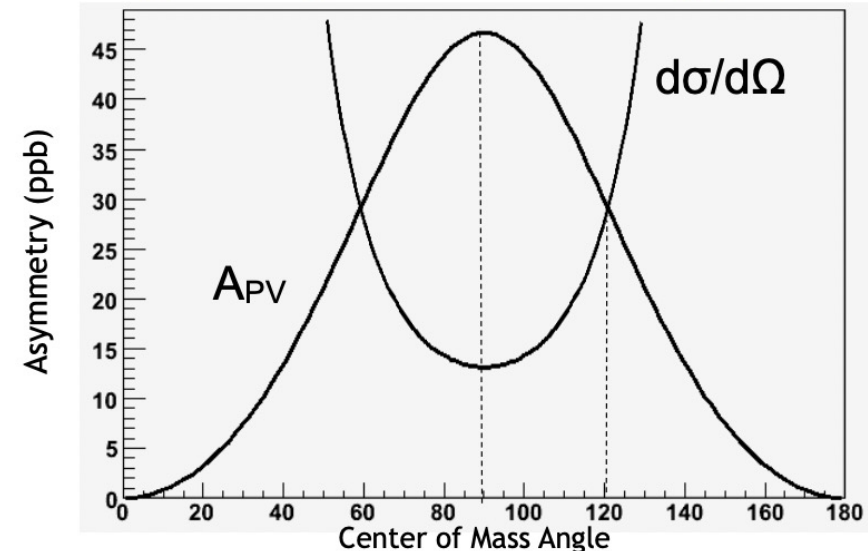


$$\mathcal{L}_{e_1 e_2} = \sum_{i,j=L,R} \frac{g_{ij}^2}{2\Lambda^2} \bar{e}_i \gamma_\mu e_i \bar{e}_j \gamma^\mu e_j$$

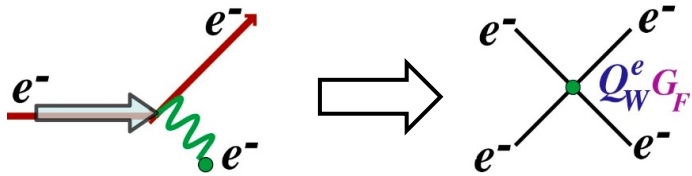
Sensitive up to:

$$\frac{\Lambda}{\sqrt{|g_{RR}^2 - g_{LL}^2|}} = 7.5 \text{ TeV}$$

Highest figure of merit at $\theta_{CM} = 90^\circ$



MOLLER Experiment at JLab

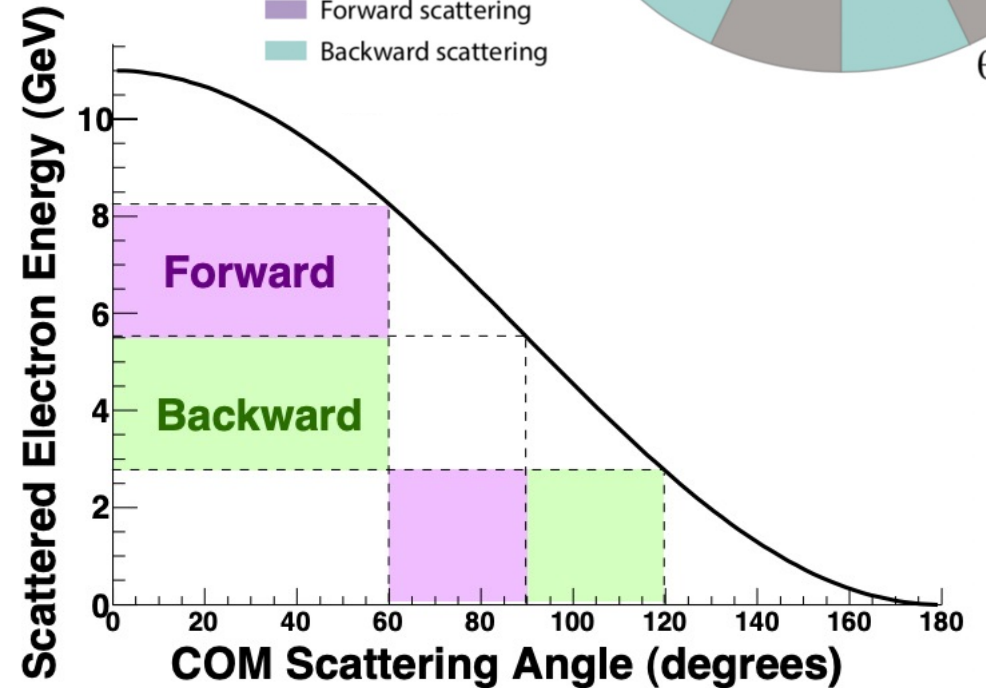
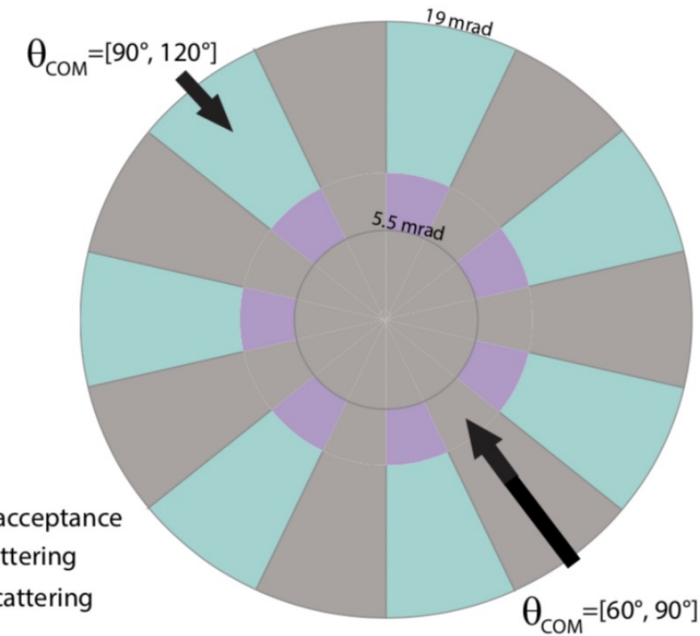
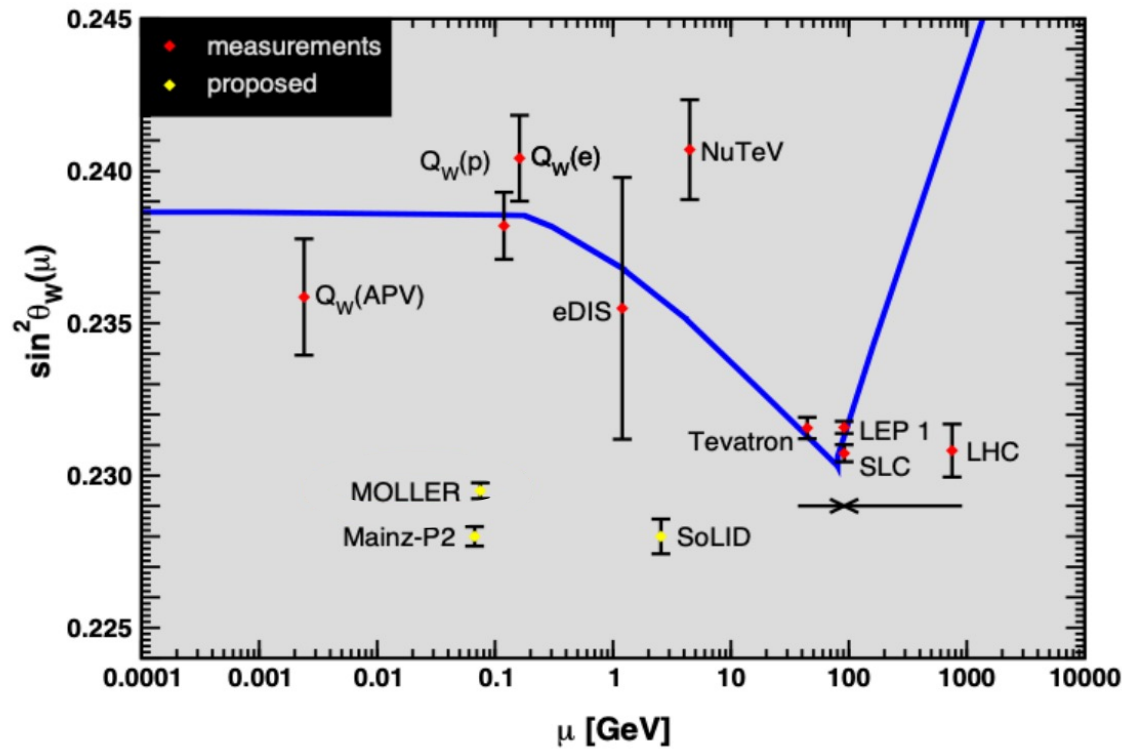


$$\mathcal{L}_{e_1 e_2} = \sum_{i,j=L,R} \frac{g_{ij}^2}{2\Lambda^2} \bar{e}_i \gamma_\mu e_i \bar{e}_j \gamma^\mu e_j$$

Sensitive up to: $\frac{\Lambda}{\sqrt{|g_{RR}^2 - g_{LL}^2|}} = 7.5 \text{ TeV}$

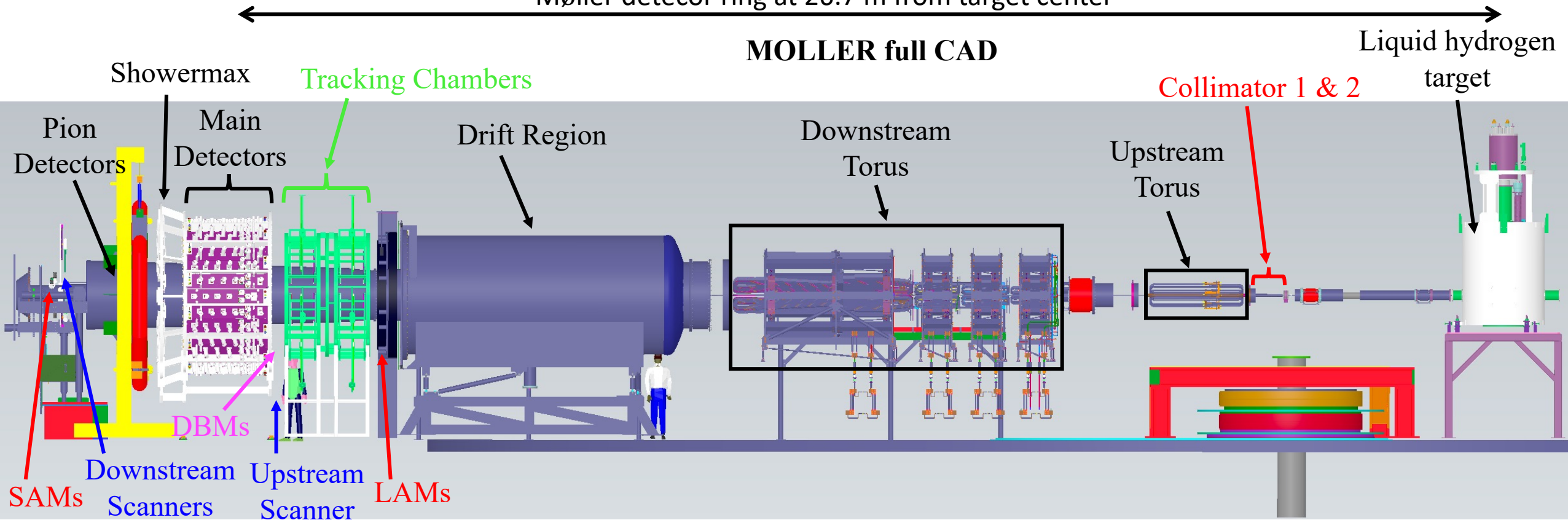
MOLLER precision:

$$\delta(\sin^2 \theta_W) = \pm 0.00023 \text{ (stat.)} \pm 0.00012 \text{ (syst.)} \Rightarrow 0.1 \%$$



MOLLER Equipment

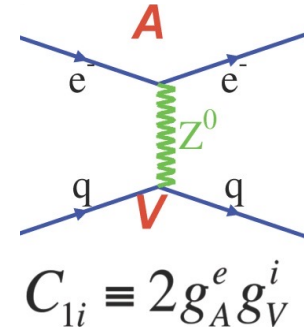
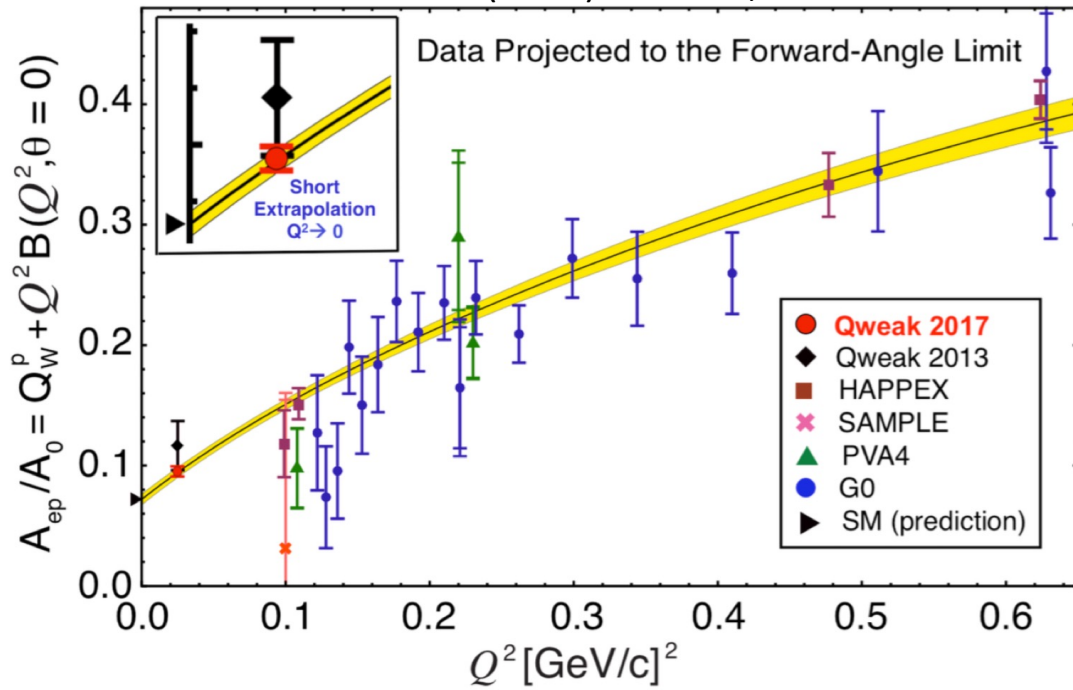
Møller detector ring at 26.7 m from target center



~ 48M\$ MIE by US DOE; also NSF, CFI funding
CD-1 granted in Dec 2020
CD-2 early in calendar year 2023
Construction: 2023 - 24

Qweak Experiment at JLab (First Measurement of Q_W^P) and AVP

Nature 557 (2018) no.7704, 207-211



Production Mode:

180 μ A, Integrating

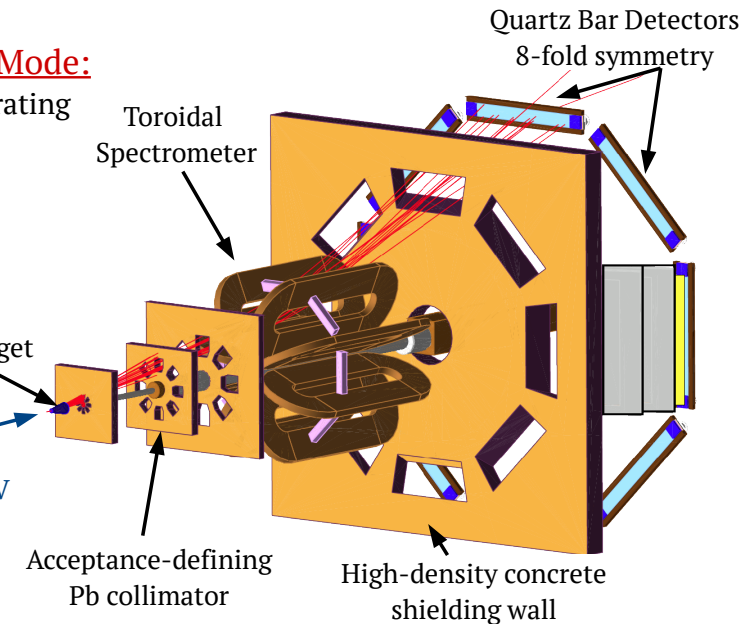
35 cm LH₂ target

e- beam

E = 1.16 GeV

I = 180 μ A

P = 88%



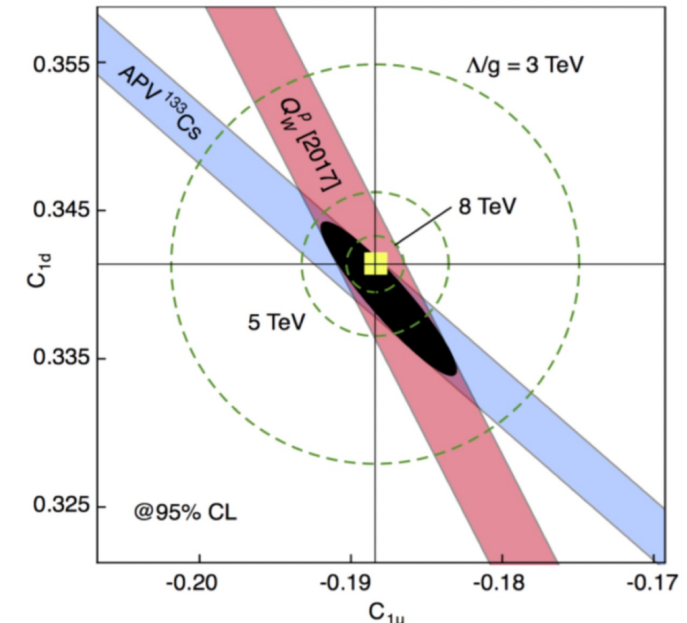
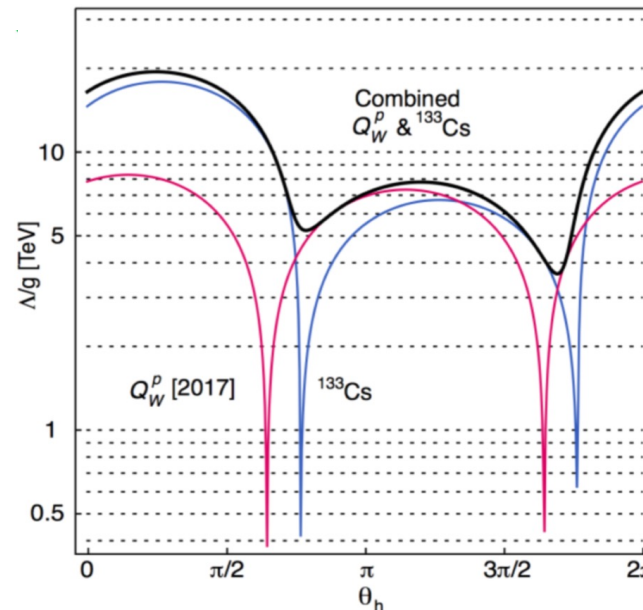
Parity-Violating e-p scattering: $\vec{e}^- + p \rightarrow e + p$

$$A_{PV}^{ep} = -226.5 \pm 7.3 \text{ (stat.)} \pm 5.8 \text{ (syst.) ppb}$$

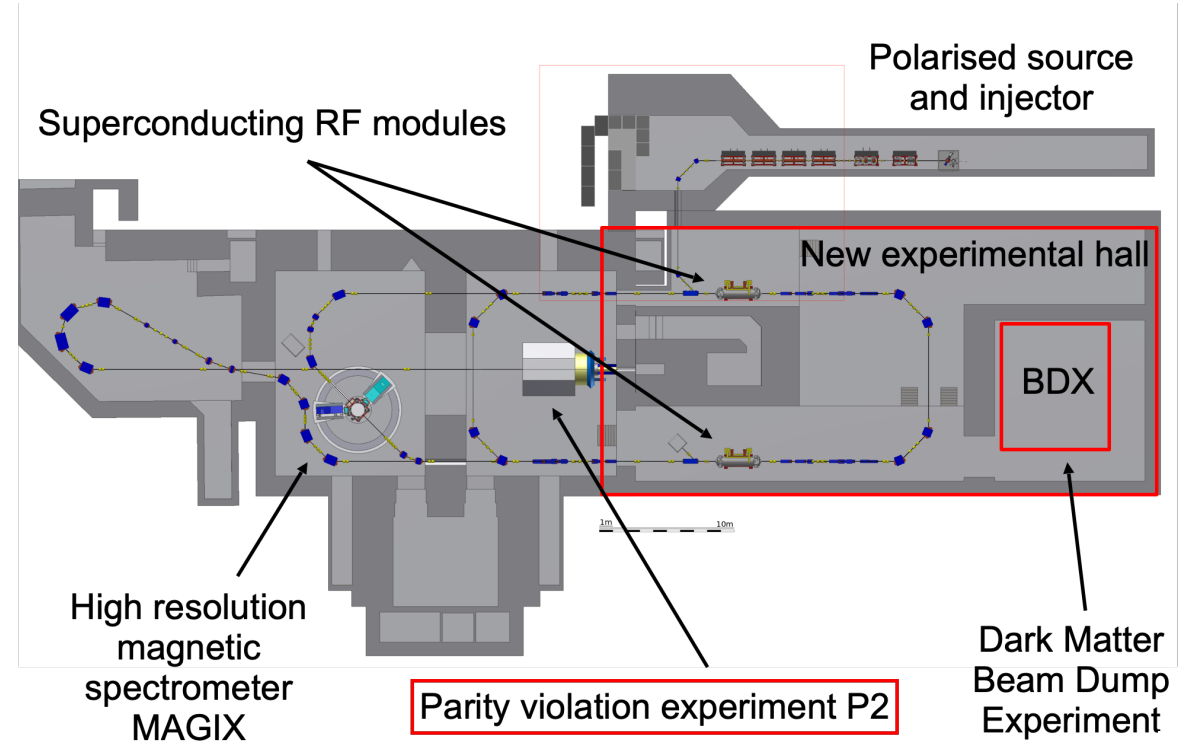
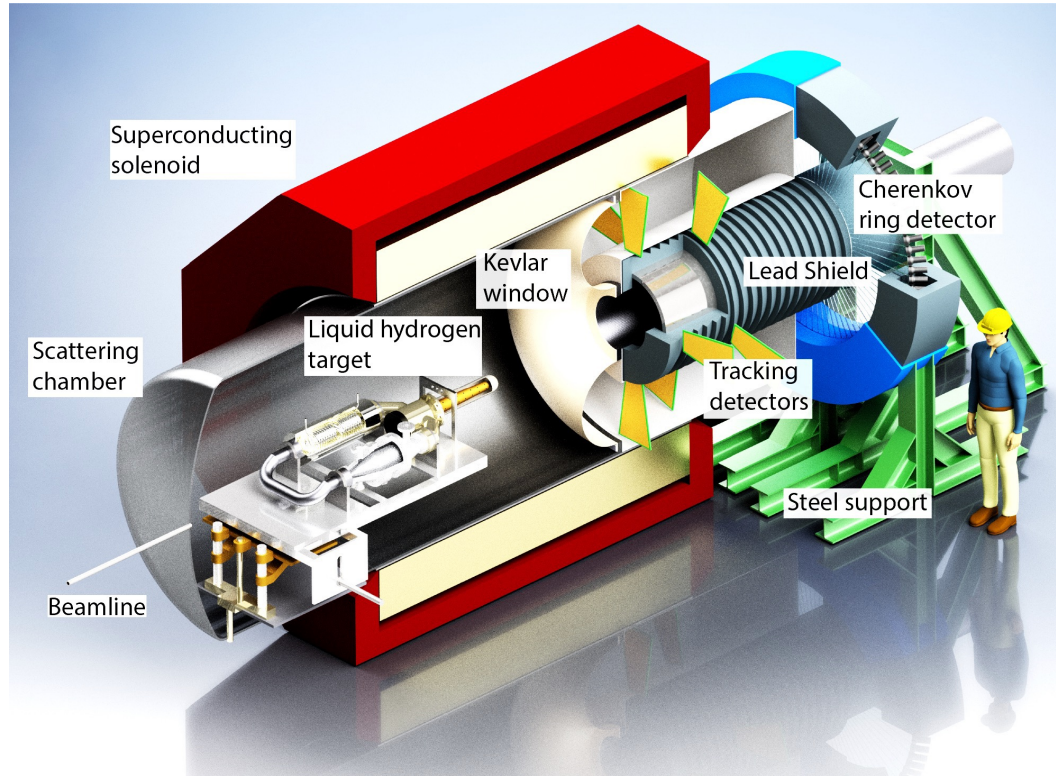
$$A_{PV}^{ep} = -\frac{G_F Q^2}{4\pi\alpha\sqrt{2}} [Q_W^P + Q^2 B(Q^2, \theta)]$$

$$Q_W^P = -2[2C_{1u} + C_{1d}] = 1 - 4\sin^2\theta_W = 0.0719 \pm 0.0045$$

$$\sin^2\theta_W = 0.2382 \pm 0.0011$$



P2 Experiment at MESA



Parity violating e-p elastic scattering at

$$Q^2 = 4.5 \times 10^{-3} \left(\frac{\text{GeV}}{c} \right)^2$$

Measures the weak charge of proton

$$A_{PV} = -24.03 \pm 0.50 \text{ (stat.)} \pm 0.29 \text{ (syst.) ppb}$$

$$\delta(Q_W^P) = 1.8\%$$

$$\delta(\sin^2 \theta_W) = 0.16\%$$

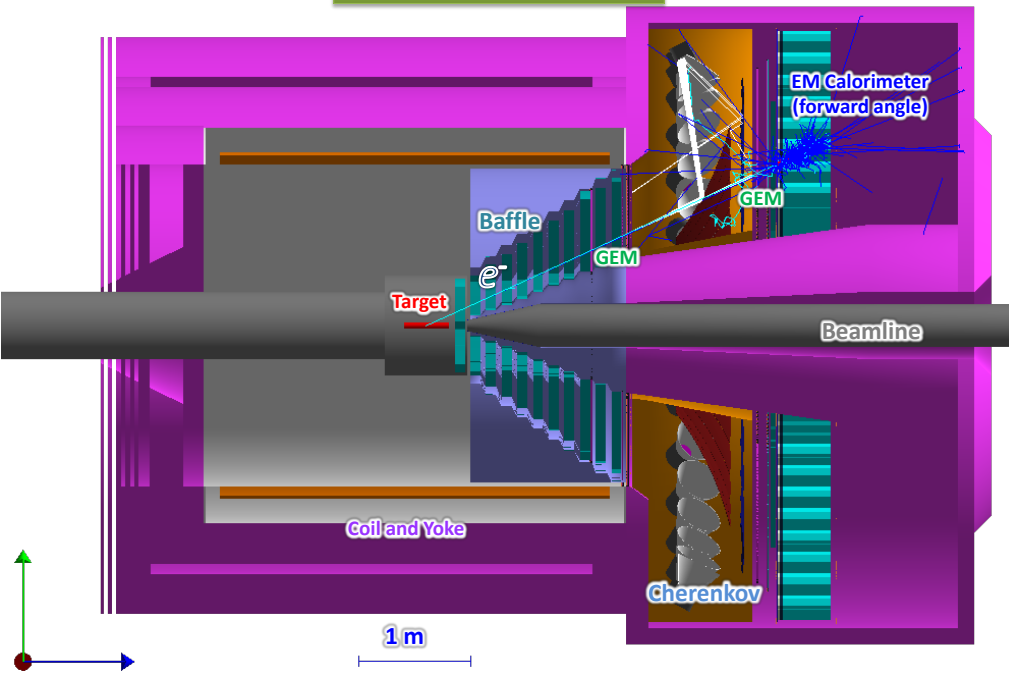
Construction 2021-23
Pilot experiments: 2024

Physics Program in 2025-30 with
proton, 12C and 208Pb targets

Most precise measurement of parity violating
e-p, e-C, and e-Pb scattering

SoLID (PVDIS) Experiment at JLab

SoLID (PVDIS)



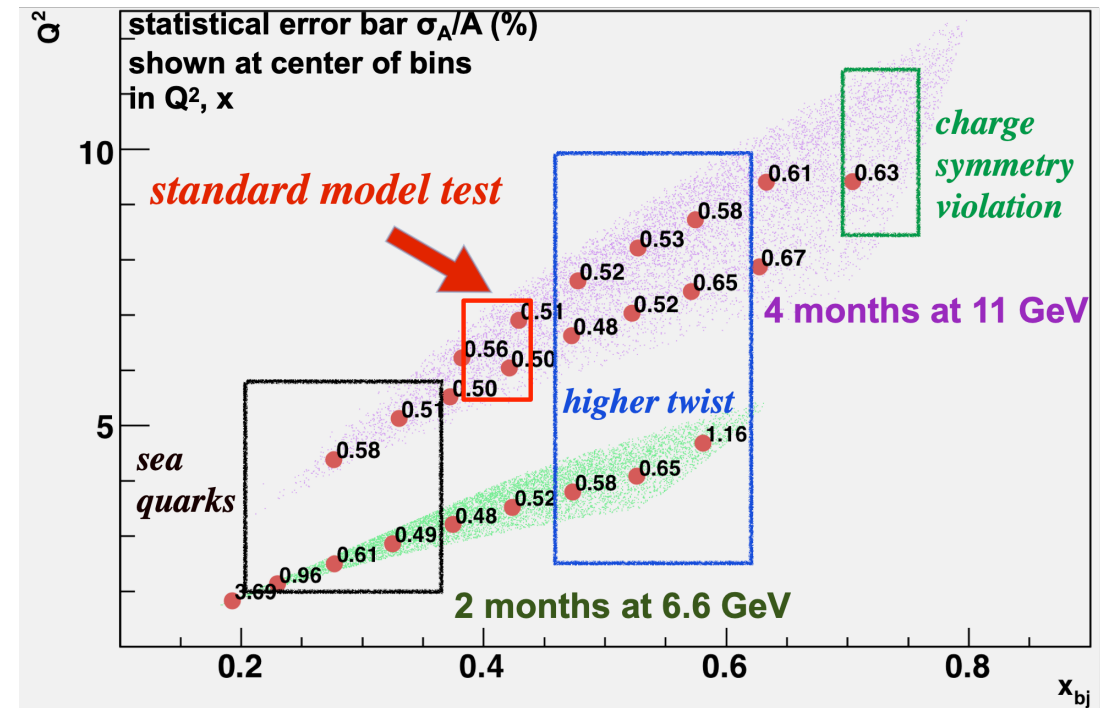
Requirements:

- High luminosity with $E > 10$ GeV
- Large scattering angles (for high x and y)
- Better than 1% errors for small bins
- x_{bj} range 0.20 – 0.75
- $W^2 > 4$ GeV²
- Q^2 range a factor of 2 for each x except for very high x
- Moderate running times

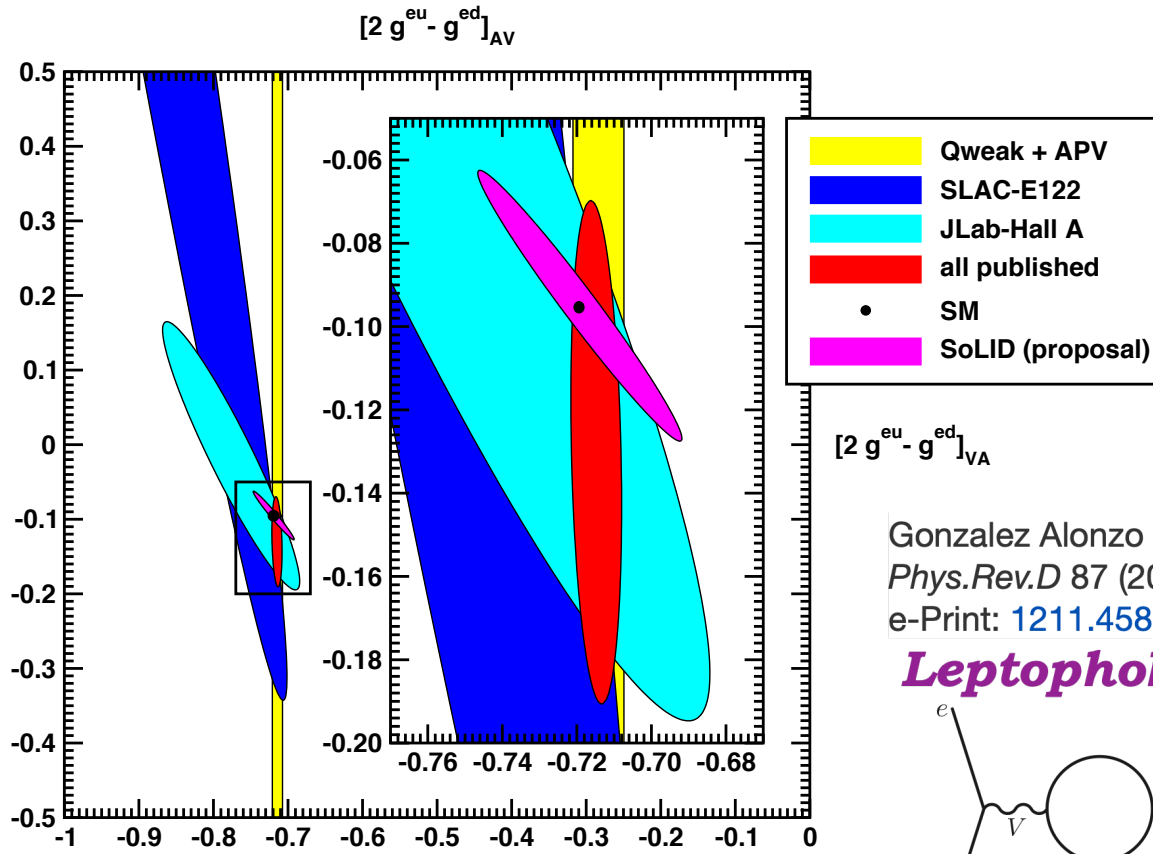
electron-deuteron parity-violating deep inelastic scattering

Strategy:

- sub-1% precision over broad kinematic range
- sensitive Standard Model test
- detailed study of hadronic structure contributions

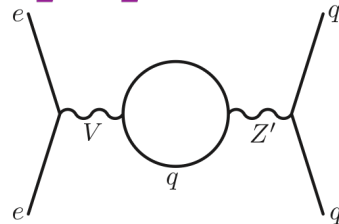


SoLID and P2: New Reach on e-q Couplings

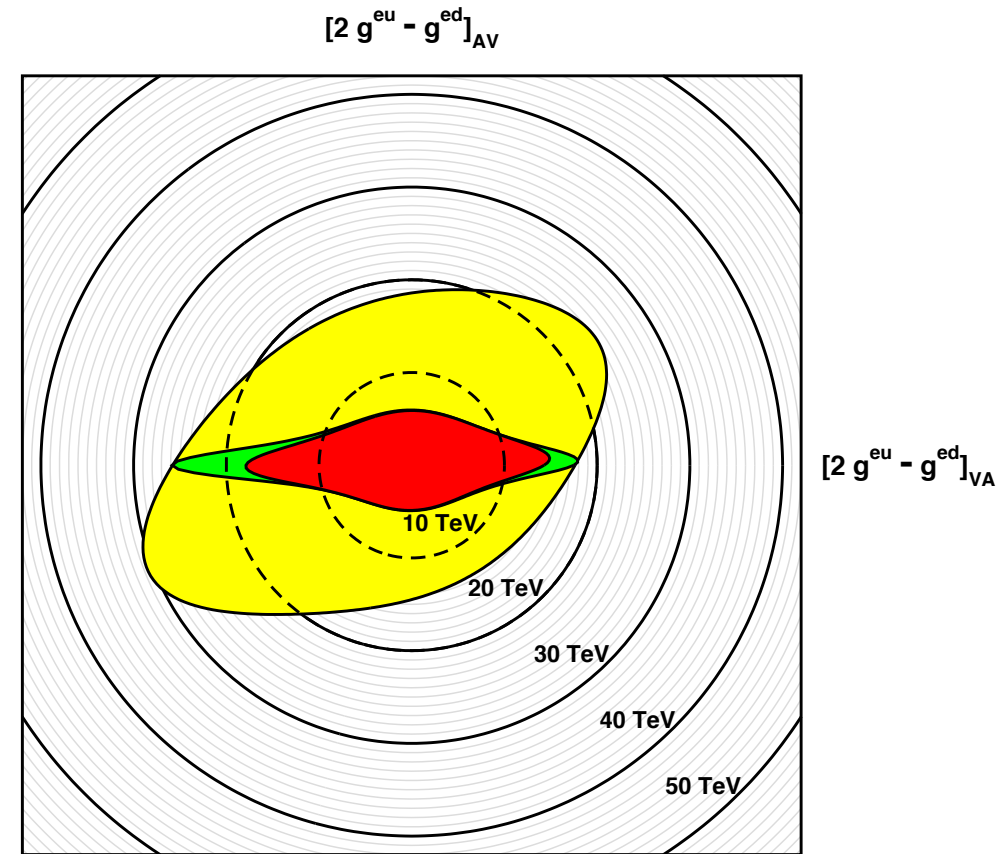


Gonzalez Alonzo and Ramsey-Musolf
Phys.Rev.D 87 (2013) 5, 055013
 e-Print: [1211.4581](https://arxiv.org/abs/1211.4581)

Leptophobic Z'



SOLID can improve sensitivity:
 100-200 GeV range



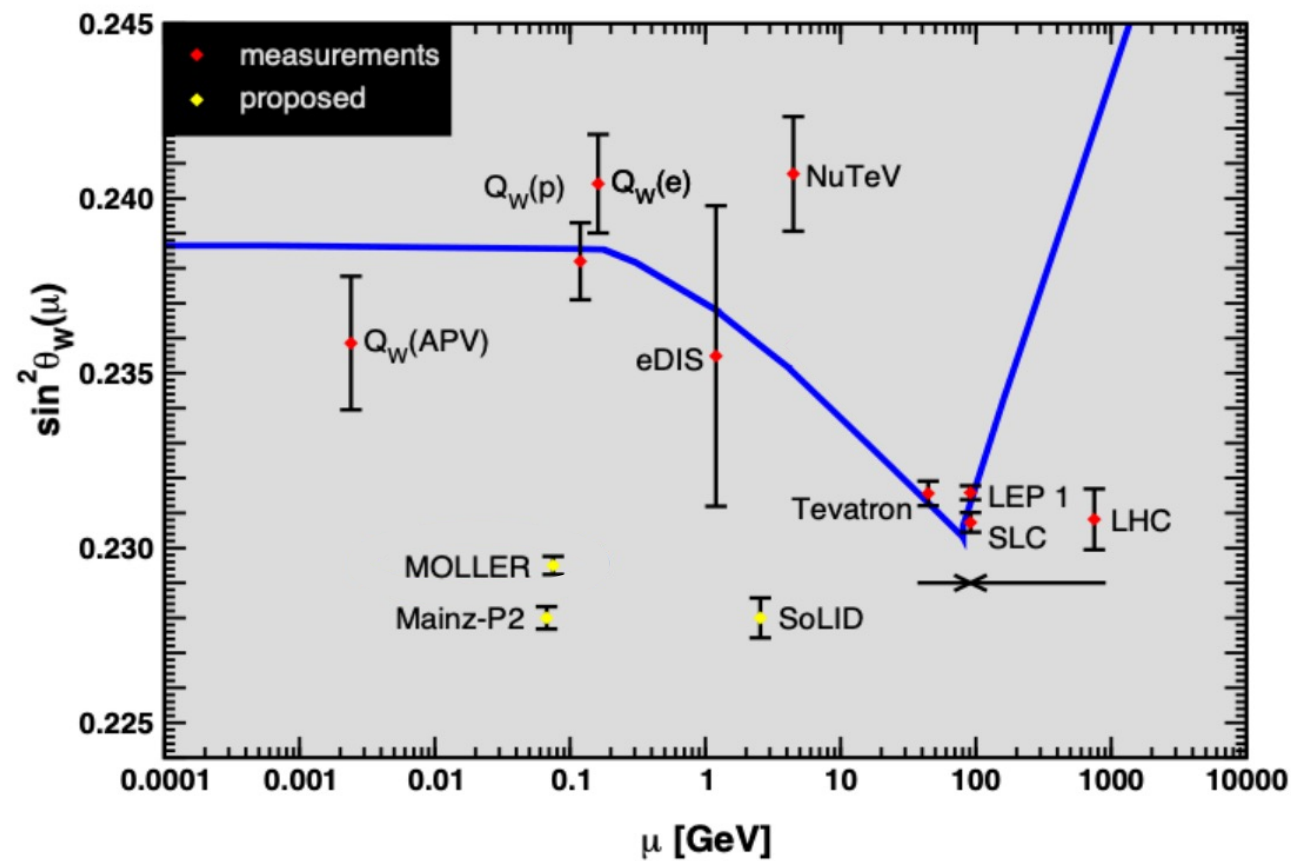
All data
 All data + P2
 All data + P2 + SoLID

Recent paper explores Z' sensitivity
 of P2 over a range of masses

B. Dev et al: *JHEP* 06 (2021) 039

Summary and Outlook

- **PVeS has become a precision tool for:**
 - Beyond standard model searches
 - Neutron skin of a heavy nucleus
 - QCD structure of the nucleon
- **Technical progress over time has enabled unprecedented precision**
- **Complementary to collider measurements**



Thank You



Low Energy Weak Neutral Current – Standard Model Test

$C_{1u}, C_{1d}, C_{ee} \rightarrow$ “weak charges”
neutral current analog to the
electric charge

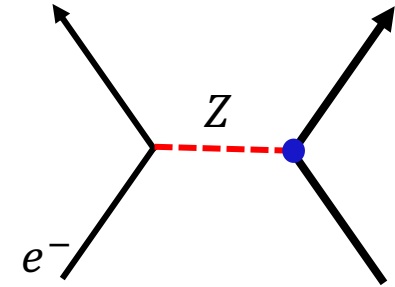
Electron’s weak charge:

$$Q_W^e = -2C_{ee} = -(1 - 4\sin^2\theta_W)$$

Parity-Violating Møller scattering:

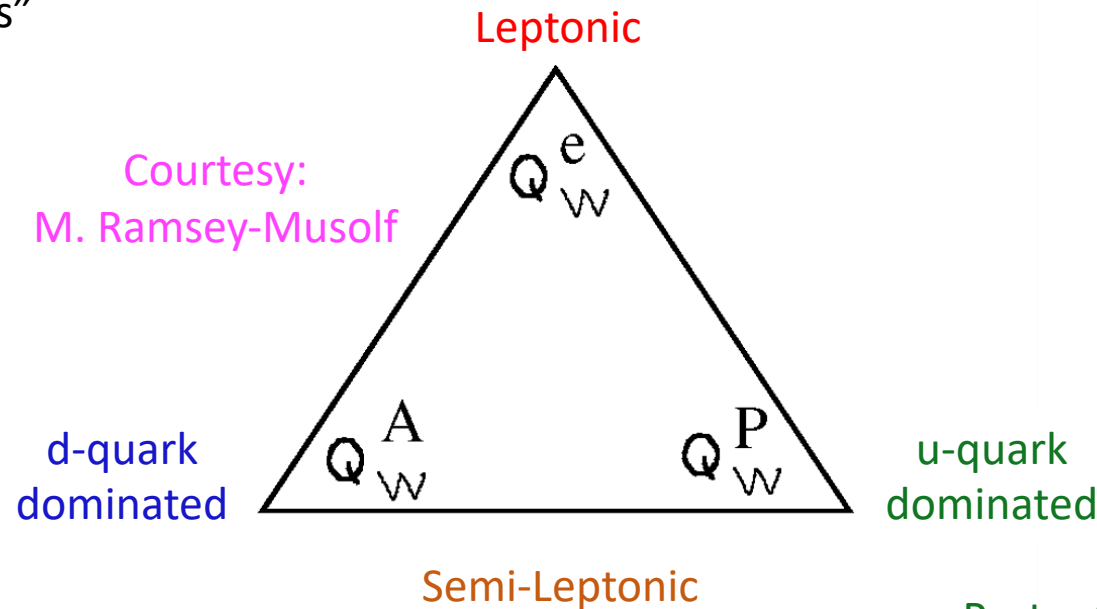
$$\vec{e}^- + e \rightarrow e + e$$

Published: SLAC E158 ~13% on Q_W^e



Q_W^e and Q_W^p are suppressed in SM:
increased sensitivity to “New Physics”
dynamics

Courtesy:
M. Ramsey-Musolf



Neutron’s weak charge:

$$Q_W^A(Z, N) \equiv -2[C_{1u}(2Z + N) + C_{1d}(Z + 2N)] \\ \approx Z(1 - 4\sin^2\theta_W) - N(1) \approx -N$$

Atomic parity violation (APV)

Published: ^{133}Cs ~0.6% on Q_W^A

Proton’s weak charge:

$$Q_W^p = -2[2C_{1u} + C_{1d}] = 1 - 4\sin^2\theta_W$$

Parity-violating elastic e-p scattering:

$$\vec{e}^- + p \rightarrow e + p$$

Published: Qweak ~6% on Q_W^p