

# Electroweak Precision Physics

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# Outline

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- **Introduction:**  
probes of the SM and beyond

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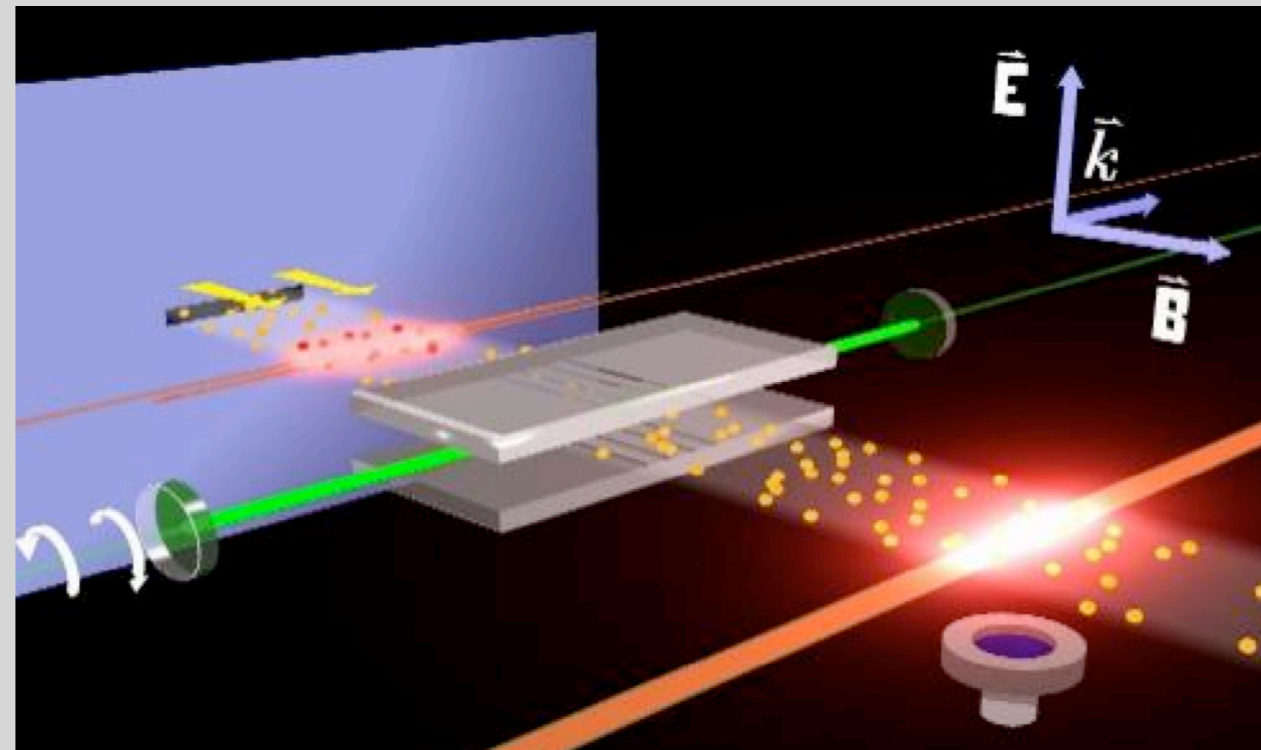
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probes of the SM and beyond
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Higgs boson mass
- **Physics beyond the SM:**  
 $Z'$  bosons and 4th fermion generation
- **Conclusions**

# Introduction

probes of the SM and beyond

# Low energy probes

- $\nu$ : scattering, oscillations, magnetic moments
- $e$ : polarization asymmetries,  $g-2$ , EDM
- $\mu$ : lifetime, decay parameters,  $g-2$ , LFV, EDM
- $\tau$ : lifetime, BRs, spectral functions, LFV
- atoms, ions, molecules, solids: PNC, EDMs
- muonic atoms, muonium: LFV





# Hadronic and nuclear probes

- **Mesons:** weak decays, mixings
- **$c\bar{c}$ ,  $b\bar{b}$ :** resonance parameters, production X-section
- **p:** lifetime, EDM
- **n:** lifetime, decay parameters, EDM,  $n$ - $\bar{n}$  oscillation
- **$^2\text{H}$ :** EDM
- **$^3\text{H}$ :** ordinary  $\beta$ -decay
- **nuclei ( $10 < A < 74$ ):** superallowed  $0^+ \rightarrow 0^+$   $\beta$ -decays
- **heavy nuclei:**  $\nu\beta\beta$ -decay

# High energy probes

- **t**: pair decays, single (EW) production X-section
- **W**: mass, width, BRs, anomalous gauge couplings
- **Z**: lineshape parameters, BRs, asymmetries
- **H**: collider searches



# SM global fit

## Higgs boson mass

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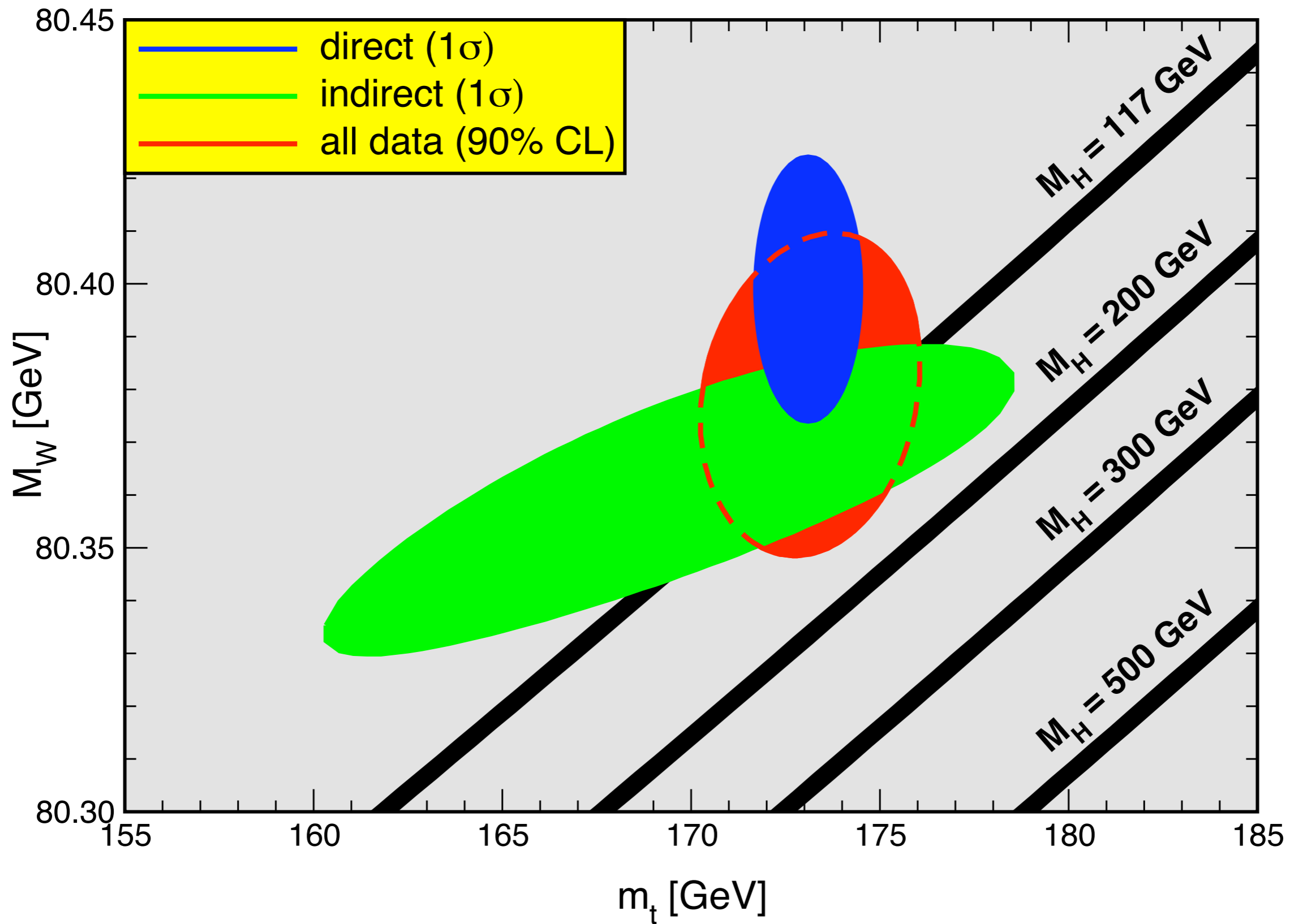
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- two equations, one unknown:  $M_H$  (in  $\bar{\rho}$ ,  $\Delta r$  &  $\Delta \bar{r}$ )

- there is independent  $M_H$ -dependence in  $\Gamma_Z$  & the low energy neutral current ( $\rho$ ) and the  $Zb\bar{b}$ -vertex



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$\chi^2/d.o.f.$	$48.0/45$ (35%)	muon $g-2$

# SM: Higgs boson mass

$58 \text{ GeV} < M_H < 146 \text{ GeV}$  (90% CL)

■ 5%

■ 90%

■ 5%

precision data



0

40

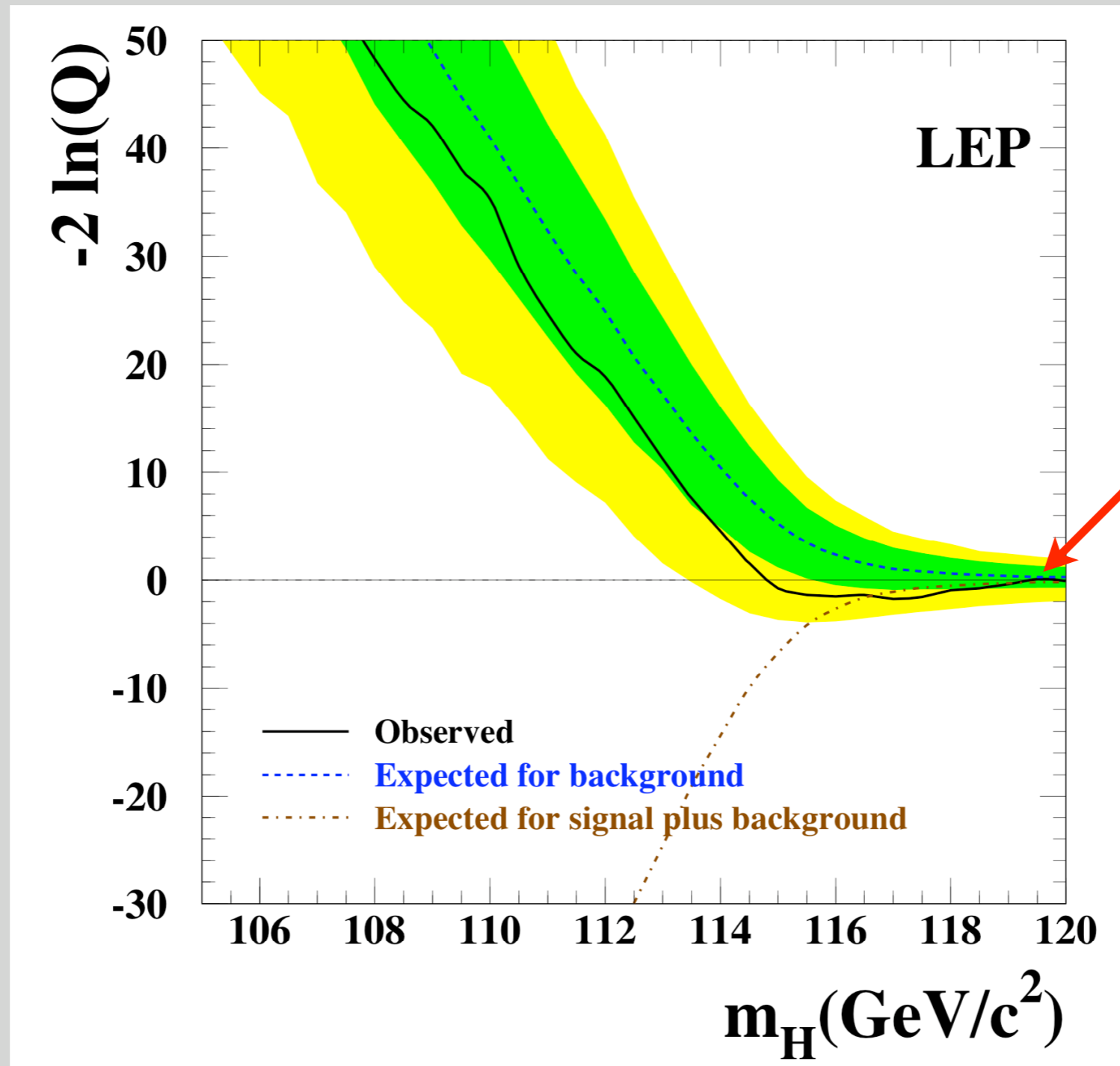
80

120

160

200

# LEP 2 Higgs searches



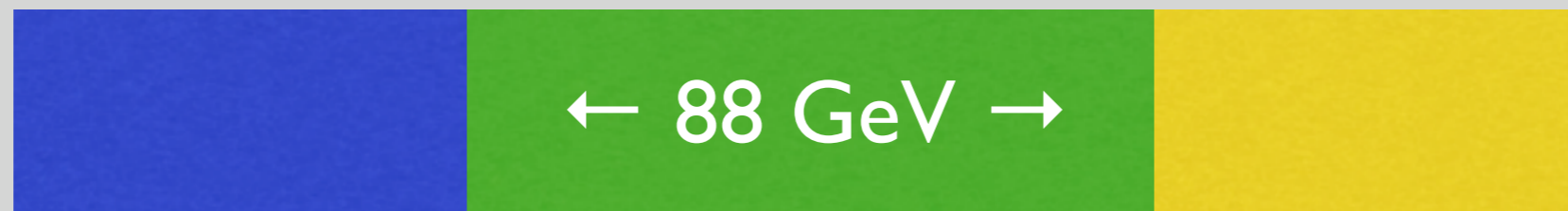
*Contribution to likelihood*

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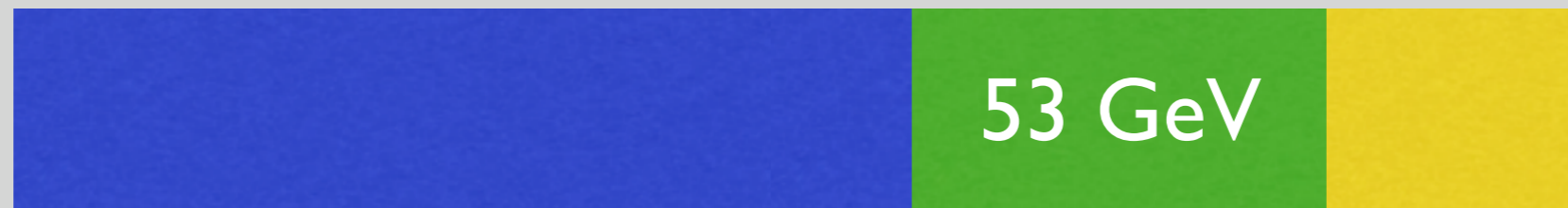
$115 \text{ GeV} < M_H < 168 \text{ GeV}$  (90% CL)

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precision data

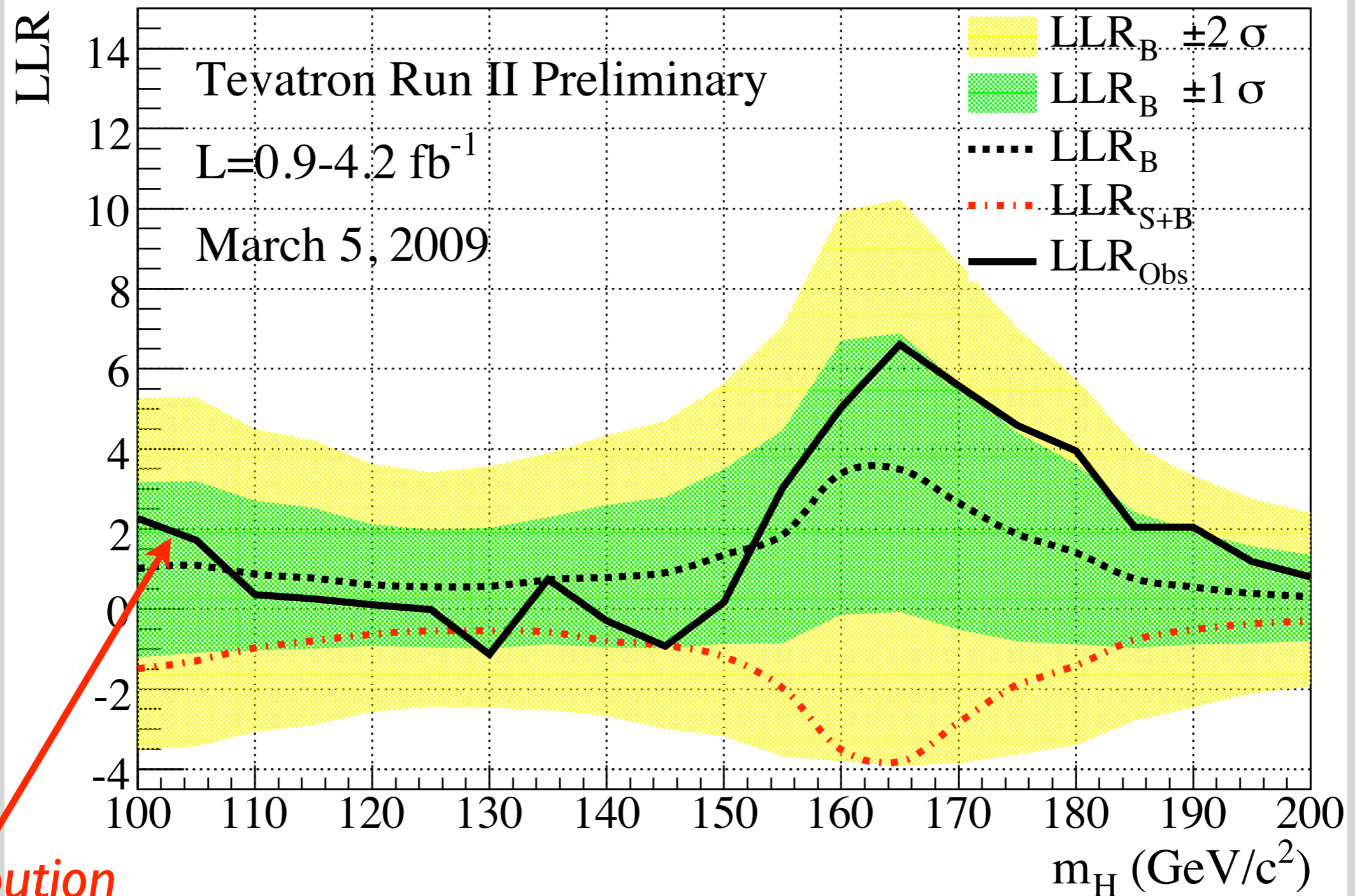


+ LEP 2



0      40      80      120      160      200

# Tevatron Higgs searches



Contribution  
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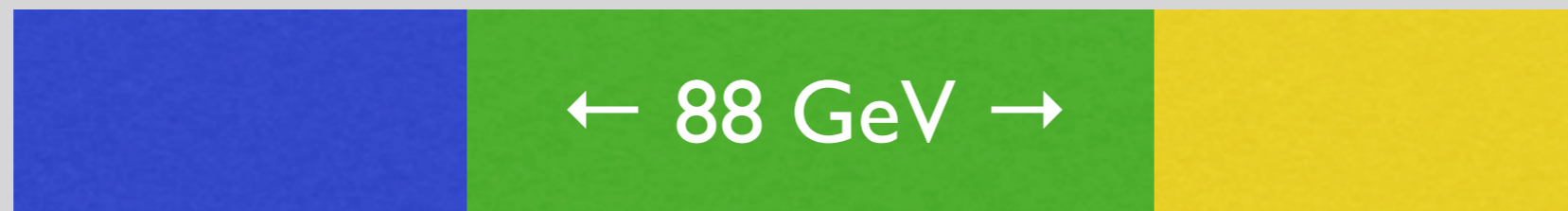


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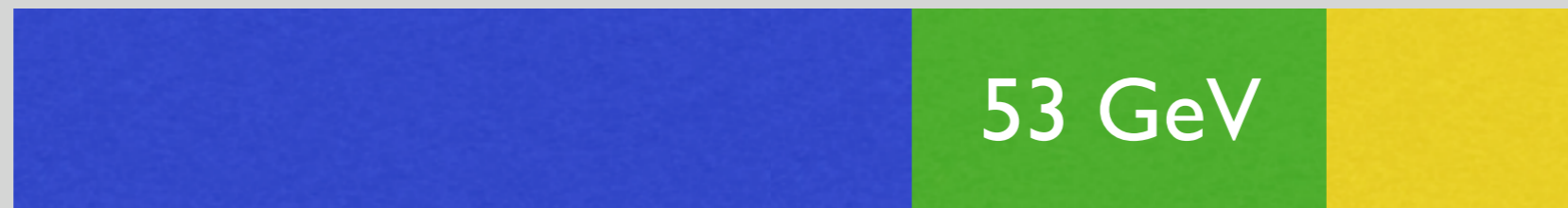
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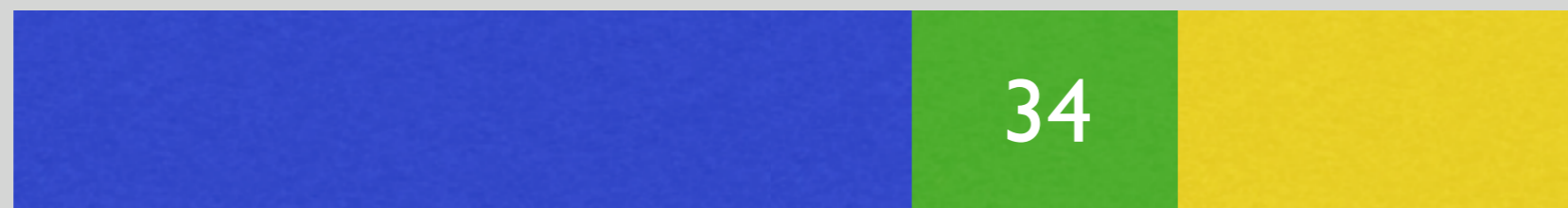
precision data



+ LEP 2



+ Tevatron



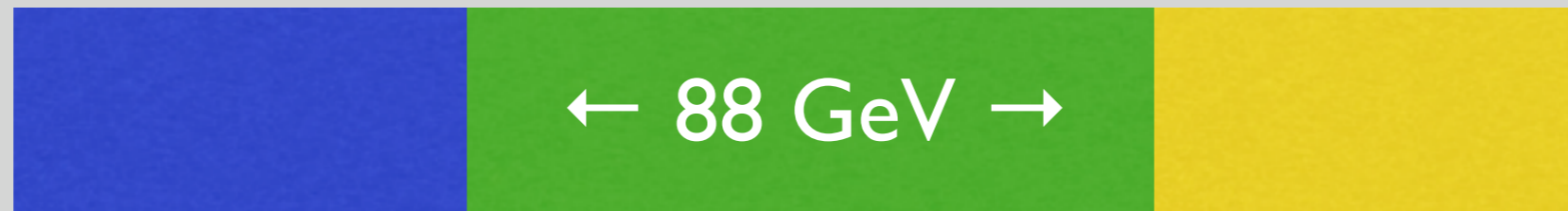
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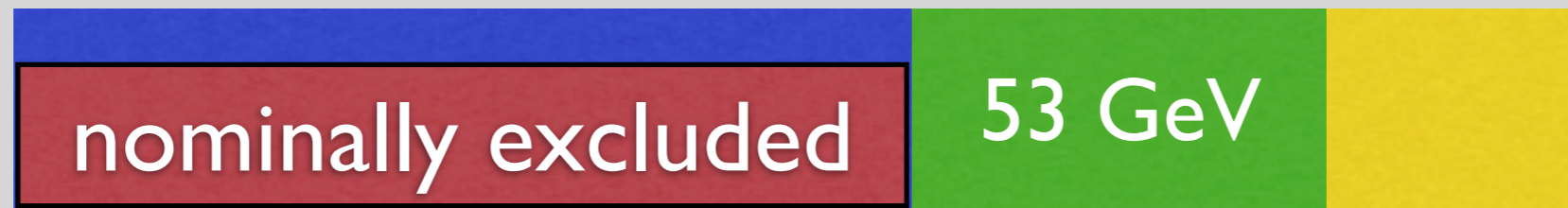
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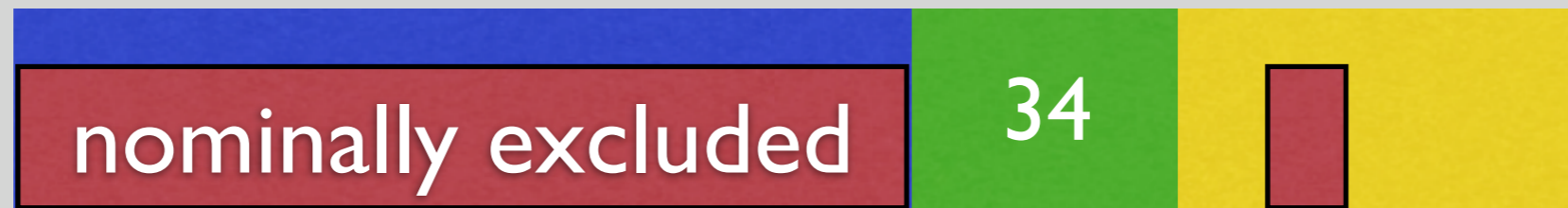
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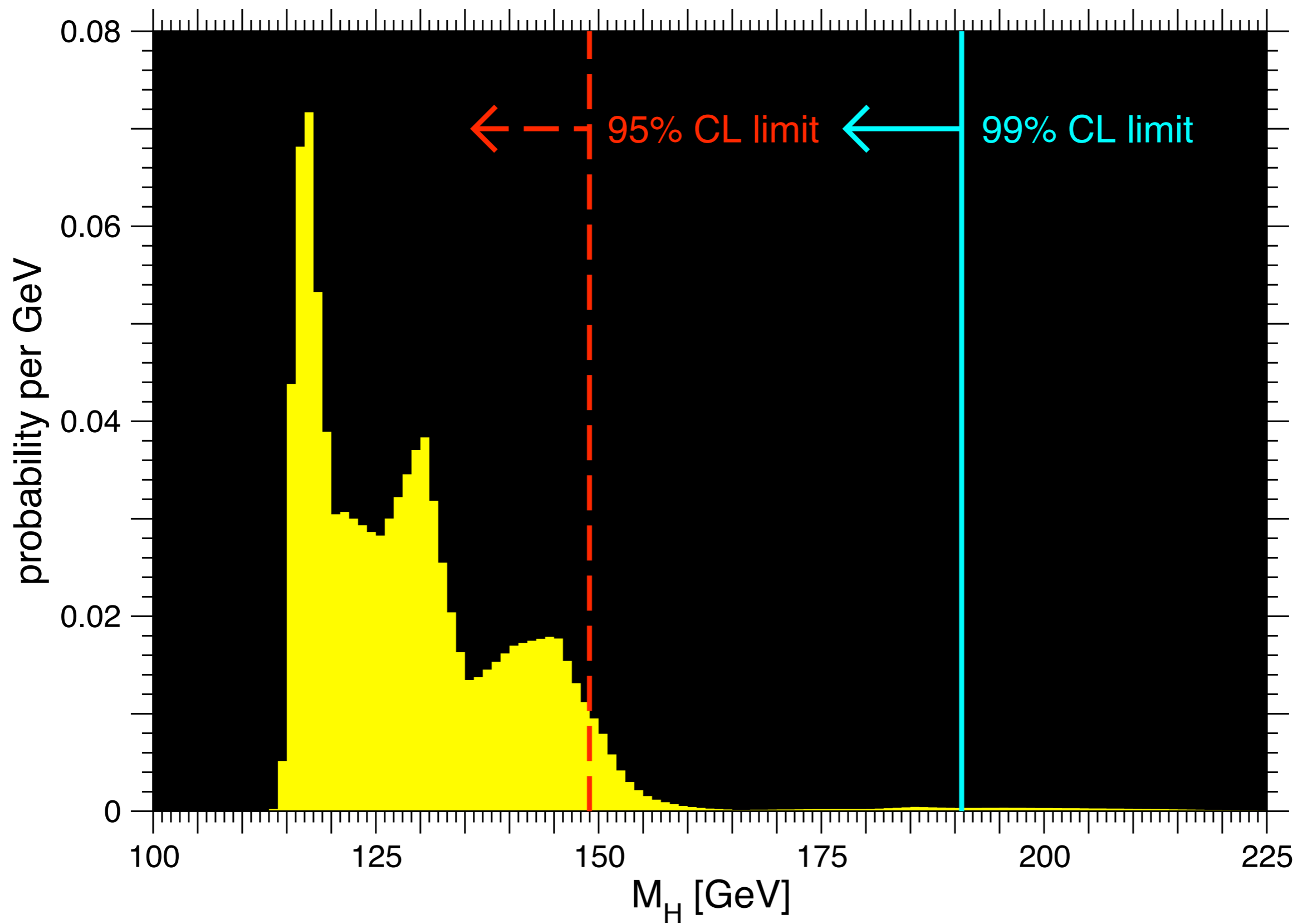
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# Physics beyond the SM

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- conversely: high energy data  $\Rightarrow \sin\theta \lesssim \mathcal{O}(10^{-3})$

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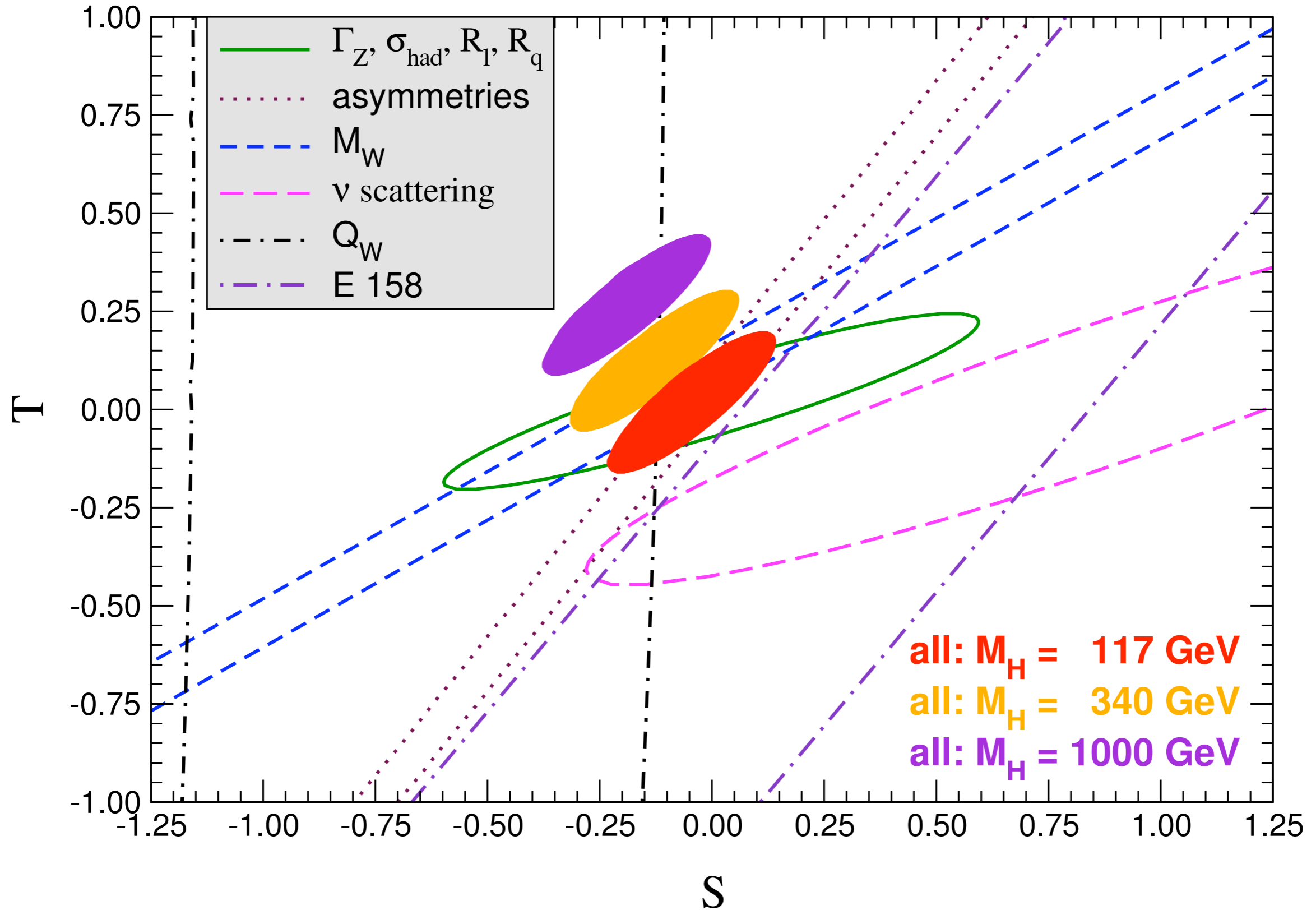
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- $\Rightarrow M_X \geq 0.89 \text{ TeV}$  (95% CL) ( $Z_\psi: q_L + q_R = 0$ )

# PDG 2008



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- $T$  parameter free:  $T = 0.21 \pm 0.04$  ( $M_H = 117$  GeV)  
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- Designer splittings ( $\Delta m \approx 50$  GeV) of doublets:  
(He, Polonsky, Su 2001; Bulanov et al. 2003;  
Novikov, Rozanov, Vysotsky 2009)  
( $m_{t'}, m_{\nu'}$ ) = (400, 100) GeV  $\Rightarrow S = 0.15, T = 0.19$   
(Kribs et al. 2007):  $\Delta\chi^2 = 2.8$  (marginal at **90% CL**)

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- $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 - 1 = 0.0000 \pm 0.0006$   
 $\propto e_L (e_L - q_L) \ln(M_{Z'}/M_W) / (M_{Z'}^2/M_W^2 - 1)$   
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from 1-loop  $W$ - $Z'$  box (Marciano, Sirlin 1987)
- $\Rightarrow M_X \geq 265 \text{ GeV}$  at 95% CL ( $\Delta\chi^2 \leq 3.84$ )  
(no constraint on  $Z_\psi$ , since  $e_L = q_L$ )

# Polarized Møller scattering



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- **SLAC E-158**:  $E = 45 \text{ \& } 48 \text{ GeV}$ ,  $P \approx 89 \pm 4 \%$   
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- **SM**:  $Q_w(e) = \rho (-1 + 4 \kappa \sin^2 \theta_w [\sqrt{Q^2}]) = -0.0472$

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(manifestly complementary to **Tevatron** and **LEP 2**)

# Polarized Møller scattering

- **SLAC E-158**:  $E = 45 \text{ \& } 48 \text{ GeV}$ ,  $P \simeq 89 \pm 4 \%$   
 $\Rightarrow Q^2 \simeq m E \simeq 0.026 \text{ GeV}^2$  (high energy, low  $Q^2$ )
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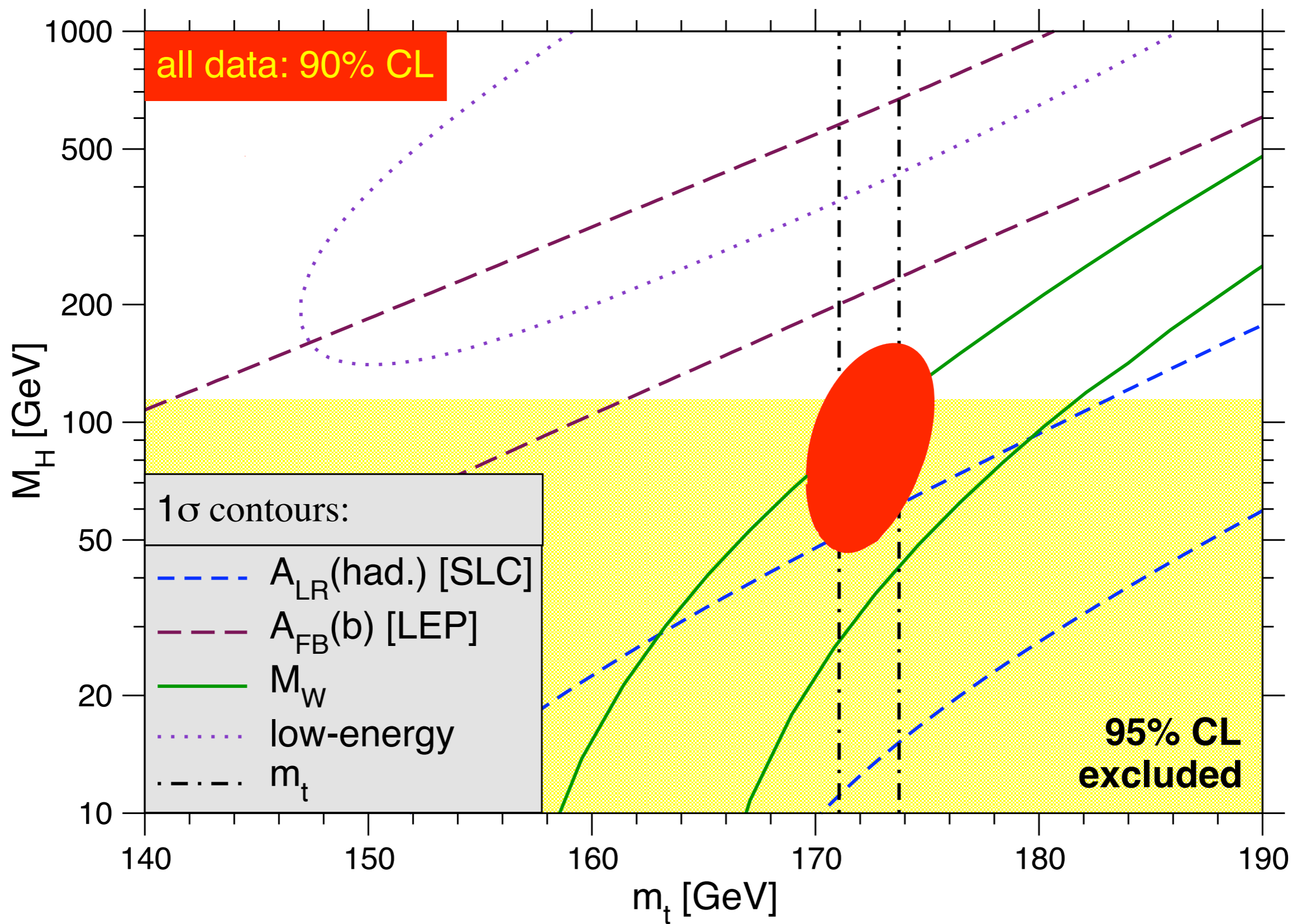
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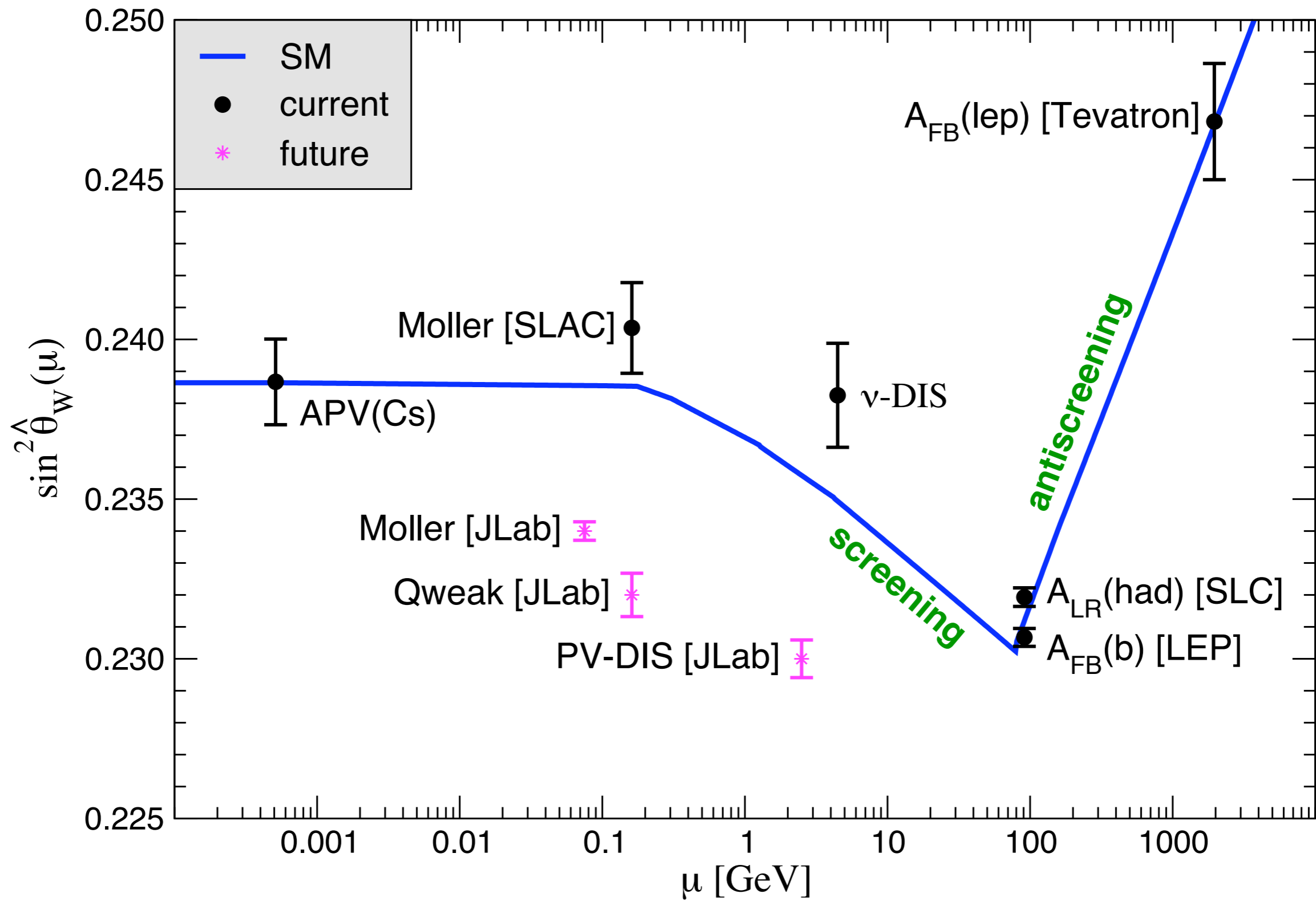
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- $e2ePV @ 12 \text{ GeV CEBAF}: \Delta Q_W(e) = \pm 0.0011 \Rightarrow$   
 $M_X \geq 1.07 \text{ TeV}$  or  $\Delta \sin^2\theta_W = \pm 0.00029$





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- absorb higher order QCD corrections into effective “**threshold masses**”,  $\bar{m}_q$ 
  - $\bar{m}_c$  and  $\bar{m}_b$ : from QCD sum rules (S resonances)
  - $\bar{m}_u$  and  $\bar{m}_d$  ( $E < 1.8 \text{ GeV}$ ): use dispersive result and approximate isospin symmetry,  $\bar{m}_u = \bar{m}_d$
  - $\bar{m}_s$ : difficult to determine independently of  $\bar{m}_d$

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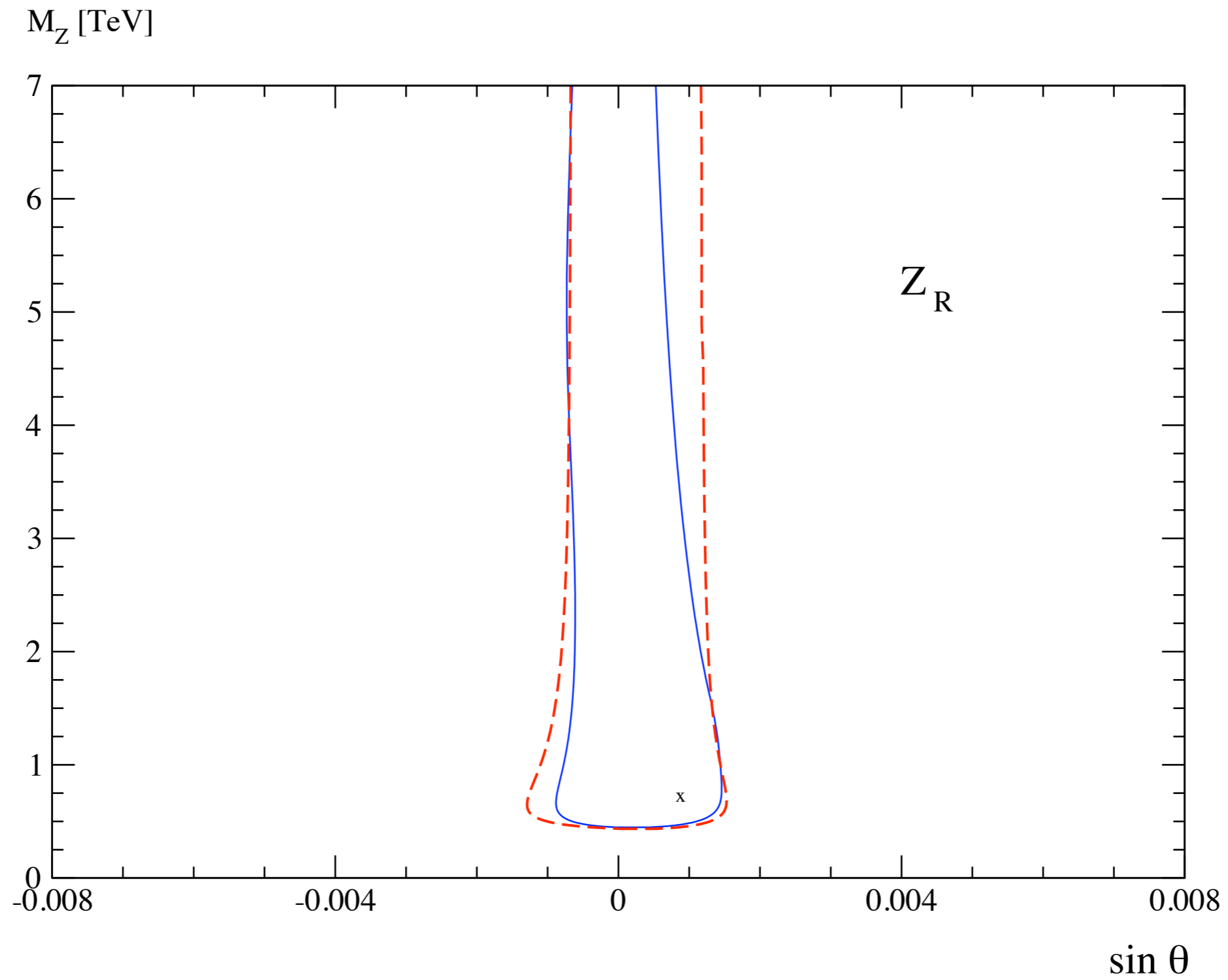
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**$0.46 \text{ TeV} < M_{Z'} < 29 \text{ TeV} \text{ (90\% CL)}$**

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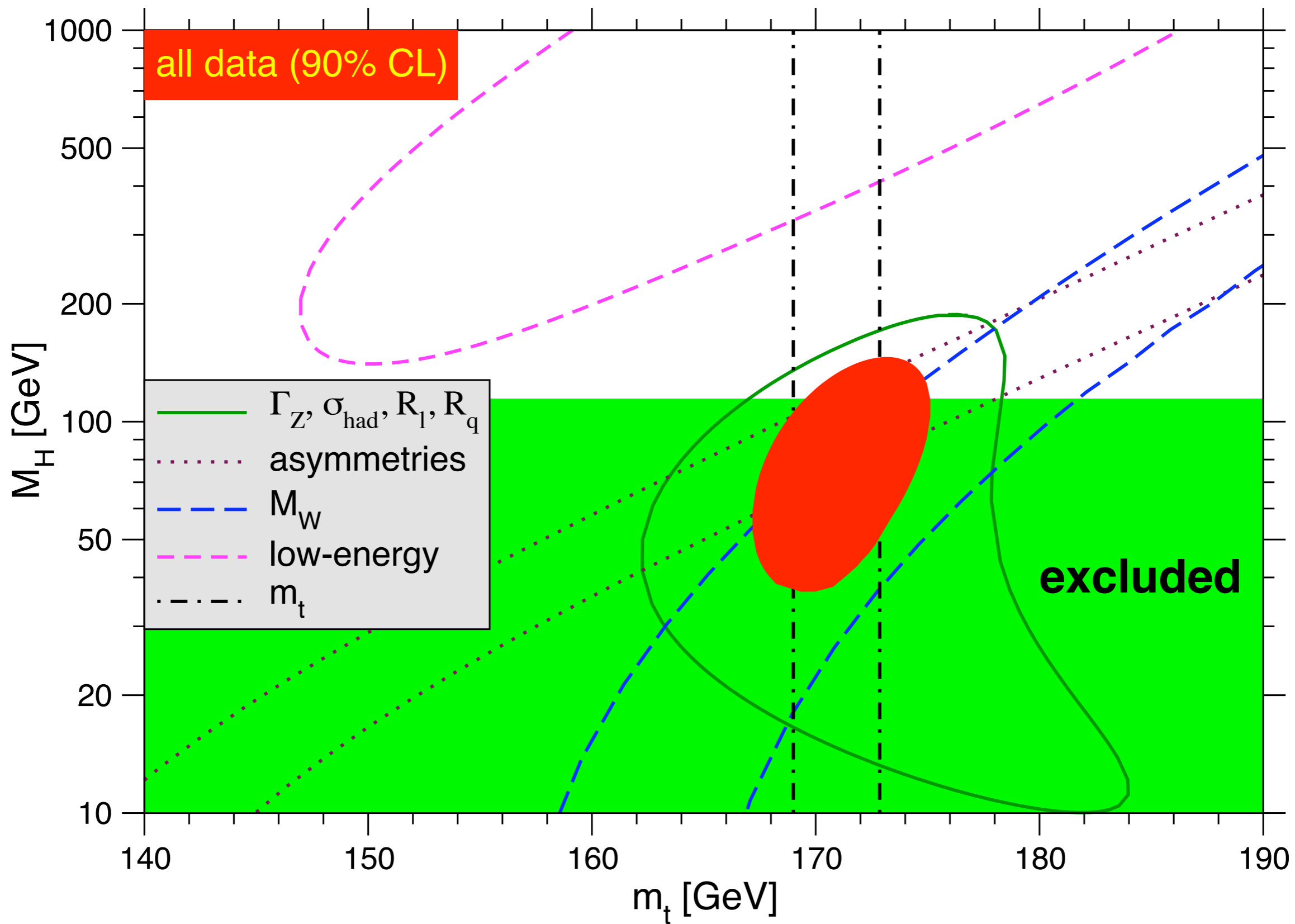
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- $2\sigma$  problems in CKM 1st row unitarity & APV disappeared entirely (4th family constraints somewhat weaker)

**Backup slides**



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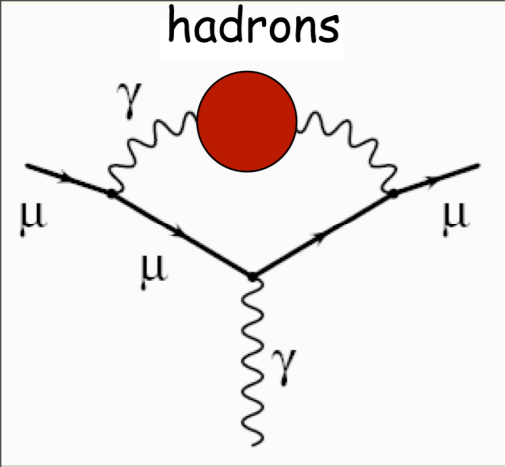
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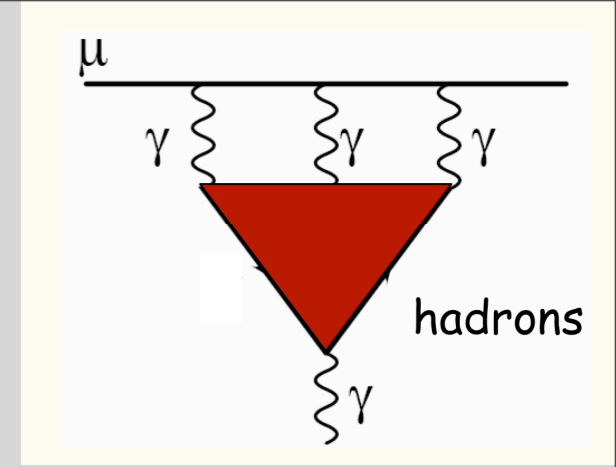


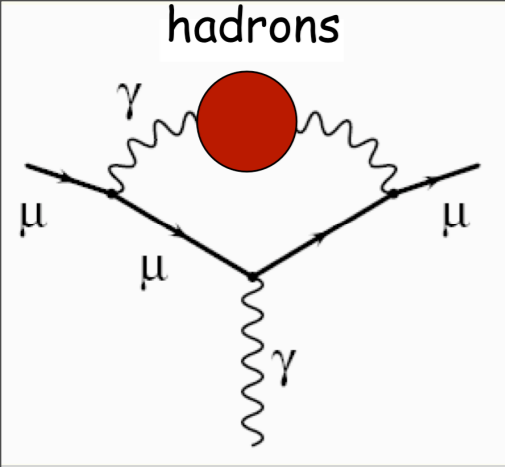
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- **nuclear effects**: different for NC and CC; 20% of effect, both signs possible (Brodsky, Schmidt, Yang)

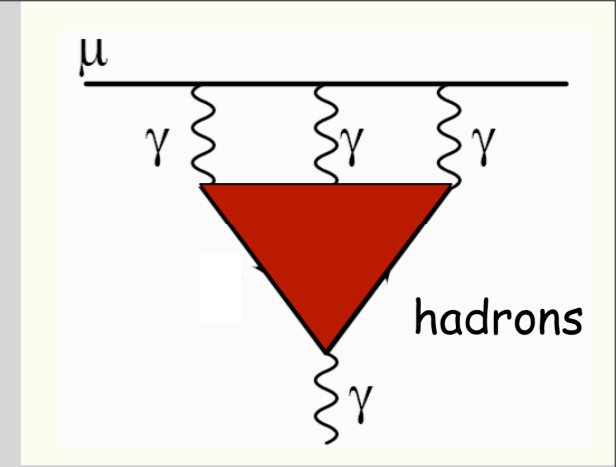


# Muon $g-2$ (BNL)

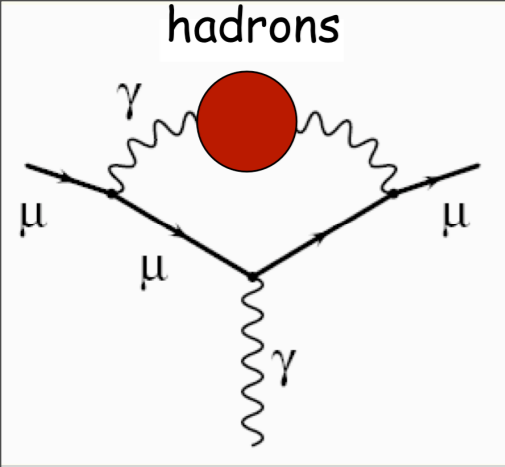




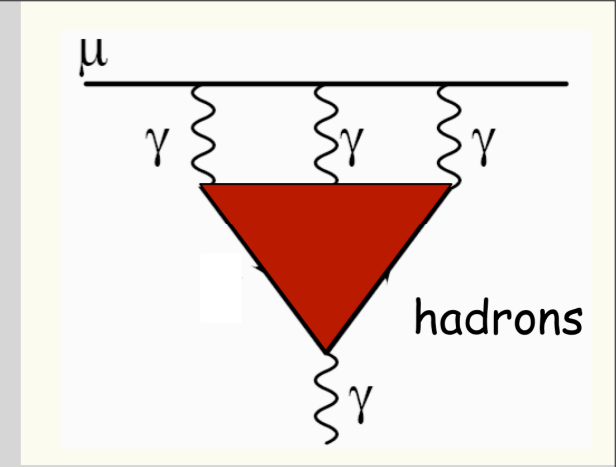
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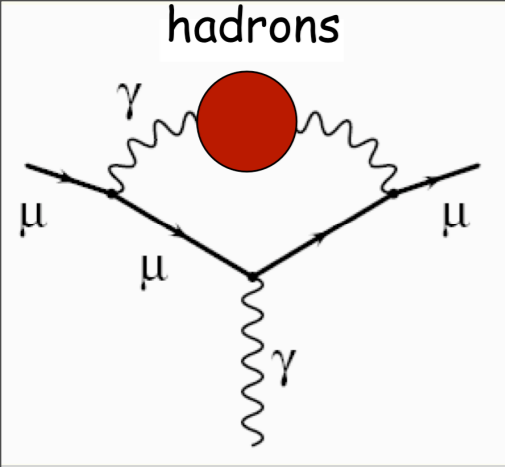
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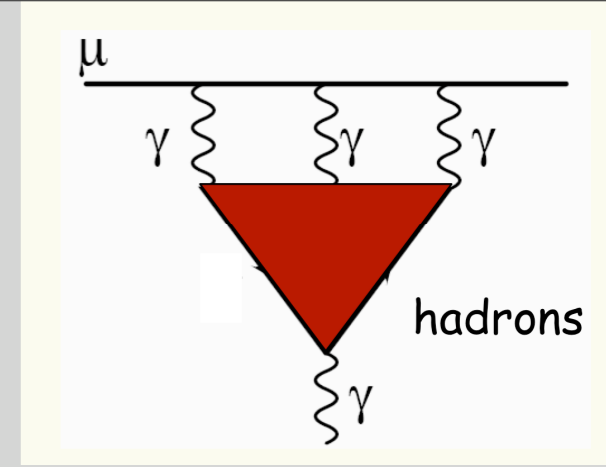
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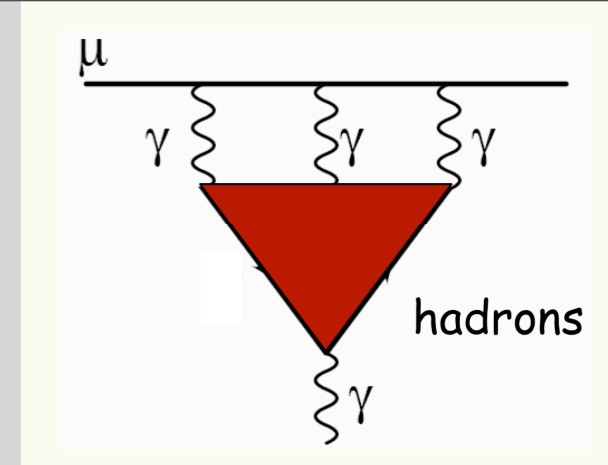
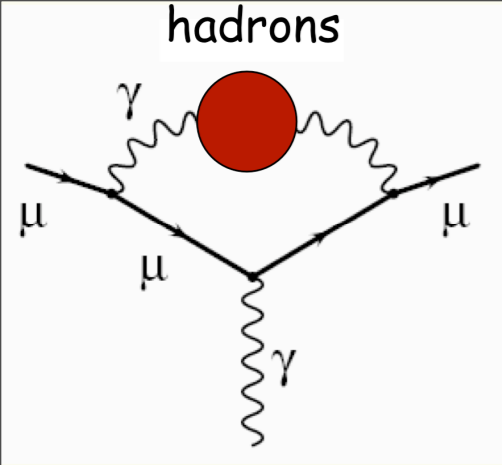
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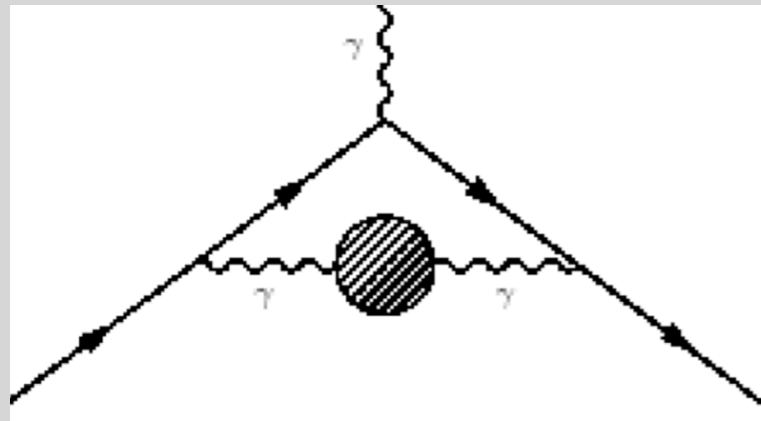
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- **2-loop vacuum polarization** (dispersion relation):  
 $\tau$  data inconsistent with  $e^+e^-$ : enhanced **CVC**?  
**CMD 2, SND, KLOE** inconsistent with **BaBar** (RR)  
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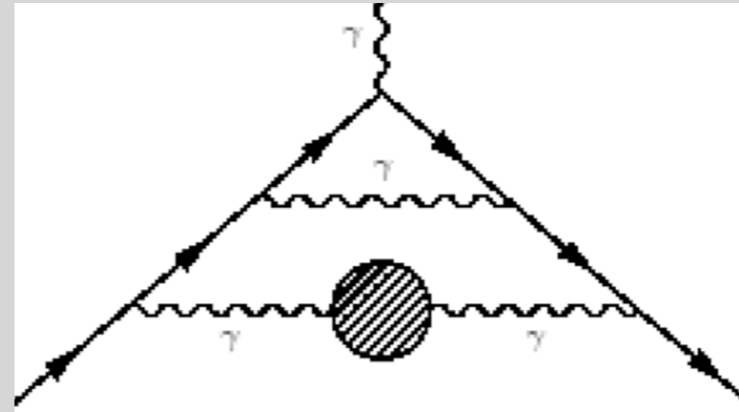
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- **3-loop  $\gamma \times \gamma$**  (**not** first principles calculations!):  
 $\pi^0 + \text{VMD}$ :  **$(1.16 \pm 0.40) \times 10^{-9}$**  (**Nyffeler 2009**)  
 free quarks:  **$< 1.59 \times 10^{-9}$**  (**Toledo, JE 2006**)

# $g-2$ : vacuum polarization



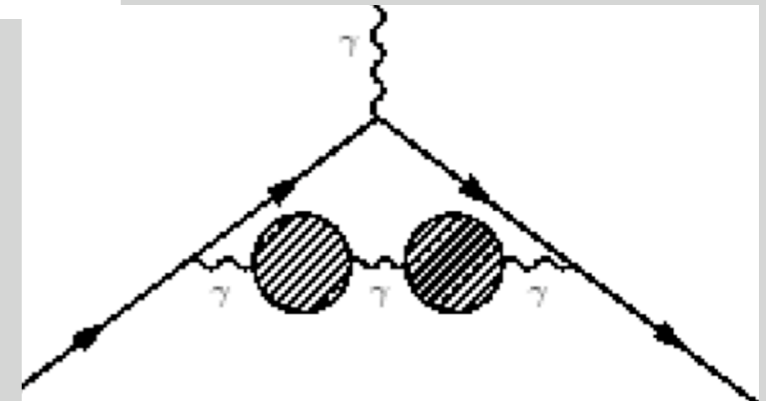
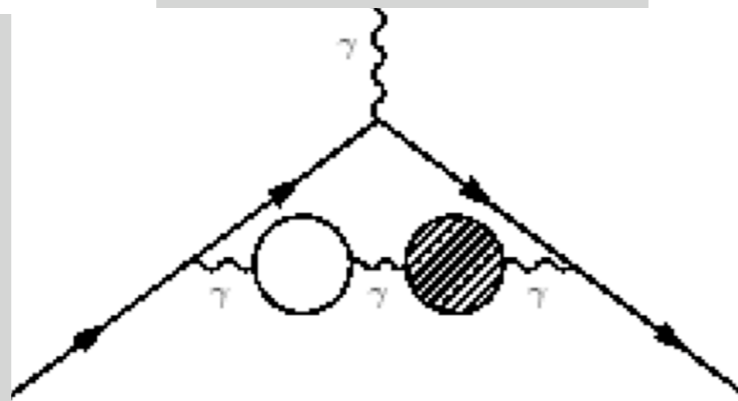
(1)

(2a)



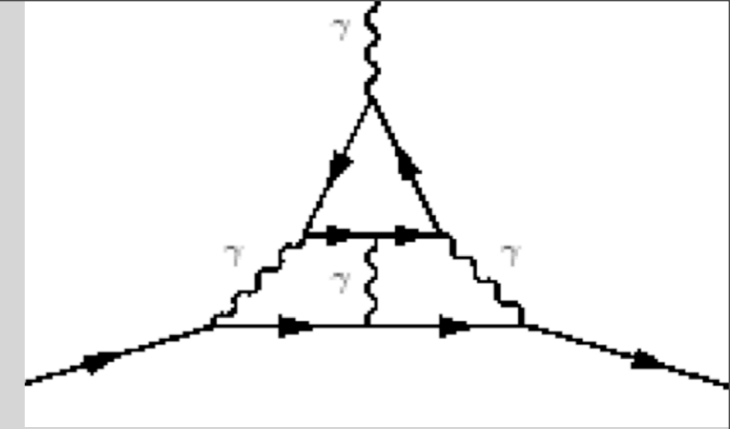
(2b)

(2c)



kernel	free quarks	data	deviation
$K^{(1)}$	+65.1	+70.3	8%
$K^{(2a)}$	-211.00	-182.00	14%
$K^{(2b)}$	+1.07	+0.99	7%
$K^{(2c)}$	+0.027	+0.028	4%

# $g-2$ : light $\times$ light



- **free quark estimate** (using quark masses for running  $\alpha$ )
- **exact** for infinitely heavy quarks (short distance ok)
- **overestimate** in chiral limit with  $m_\mu/m_\pi$  fixed (charged pointlike pions contribute negatively)
- **VMD**:  $(1.36 \pm 0.25) \times 10^{-9}$  (error: “rough guess”;  $\mu \sim 0.6$  GeV) **Melnikov, Vainshtein (2004)**
- **Toledo, JE (2006)**:

$$\text{free quarks} \begin{cases} (1.37_{+0.15}^{-0.27}) \times 10^{-9} \\ < 1.59 \times 10^{-9} (95\% \text{ CL}) \end{cases}$$