

# Phenomenology

## Before & After the Higgs Boson

Phenomenology Before & After the Standard Model:  
a symposium in honor of Vernon Barger

June 5, 2025

Tao Han, University of Pittsburgh



Forty years ago, I took my first flight ride  
Beijing PEK → SFO → ORD → MSN  
a place I lived longer than any other places



# A Prime Time for HEP: The SSC Era

One of my 1<sup>st</sup> papers:



University of Wisconsin - Madison

MAD/PH/324  
January 1987

Improved Transverse-Mass Variable for  
Detecting Higgs-Boson Decays into  $Z$  Pairs

V. BARGER AND T. HAN

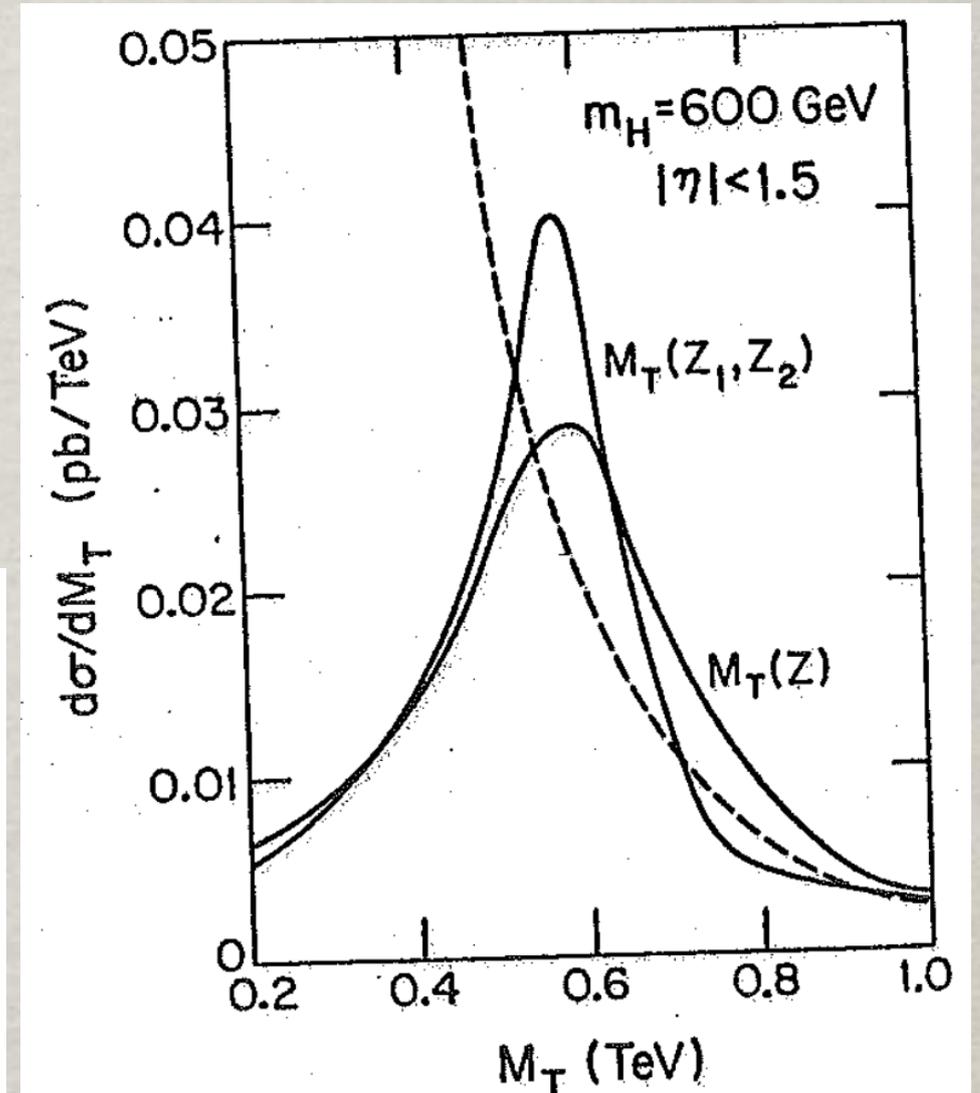
Physics Department, University of Wisconsin, Madison, Wisconsin 53706 USA

R. J. N. PHILLIPS

Rutherford Appleton Laboratory, Chilton, Didcot, Oxon, England

## ABSTRACT

A promising decay mode for detecting heavy Higgs bosons at a supercollider is  $H \rightarrow ZZ \rightarrow (\ell^+\ell^-)(\nu\bar{\nu})$ , with one  $Z$  detected by  $e^+e^-$  or  $\mu^+\mu^-$  decay and the other decaying to undetected neutrinos. Such events peak versus the transverse mass of the detected  $Z$ . We show there is an even sharper peak versus the two-body transverse mass, incorporating the missing transverse momentum carried by the second  $Z$ -boson.



$$M_T(Z) = 2(p_T^2 + M_Z^2)^{1/2}$$

$$[M_T(Z_1, Z_2)]^2 = \left[ (p_T^2 + M_Z^2)^{1/2} + (p_T^2 + M_Z^2)^{1/2} \right]^2$$

The “cluster transverse mass”  
was introduced

# From kinematics to dynamics



## RESCUING THE HEAVY HIGGS SIGNAL

V. BARGER and T. HAN

Physics Department, University of Wisconsin, Madison, WI 53706, USA

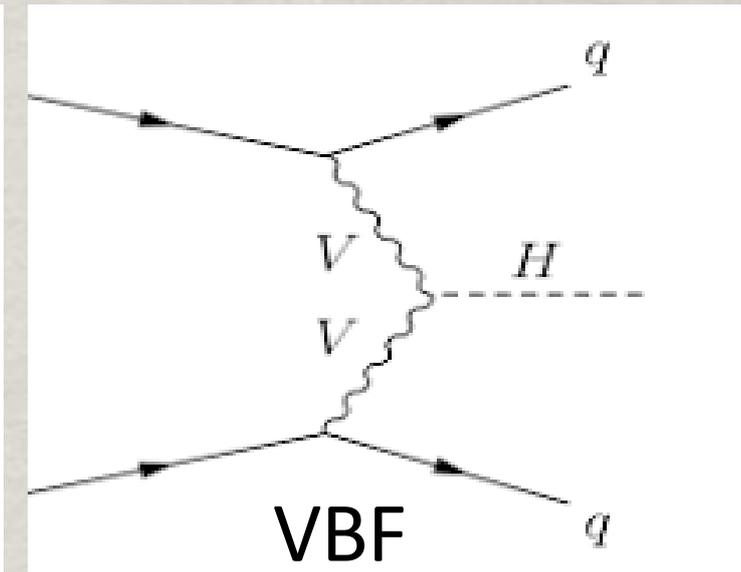
R. J. N. PHILLIPS

Rutherford Appleton Laboratory, Chilton, Didcot,

### ABSTRACT

If the Higgs scalar boson  $H^0$  has mass greater than 600 GeV have been foreseen in identifying it in  $pp$  collisions at the SSC. We show that the  $H^0 \rightarrow ZZ$  signal, with one  $Z \rightarrow \ell^+\ell^-$  and one  $Z \rightarrow \nu\bar{\nu}$  decay, can be separated from background by selecting events with  $\ell^+\ell^-$  at the  $Z$  mass plus large missing  $p_T$  plus two jets. This signal is enhanced by using an improved transverse-mass variable.

MAD/PH/368  
September 1987



“forward jet-tagging”

### Improving the Heavy Higgs Four Charged Lepton Signature

Vernon D. Barger (Wisconsin U., Madison), Tao Han (Wisconsin U., Madison), Phillips (Rutherford) (Dec, 1987)

Published in: *Phys.Lett.B* 206 (1988) 339-342

### Improving the Heavy Higgs Boson Two Charged Lepton - Two Neutrino Signal

Vernon D. Barger (Wisconsin U., Madison), Tao Han (Wisconsin U., Madison), R.J.N. Phillips (Rutherford) (1988)

Published in: *Phys.Rev.D* 37 (1988) 2005-2008

STANDARD MODEL HIGGS BOSON STUDIES  
FOR  
SUPERCOLLIDERS

by

TAO HAN

A thesis submitted in partial fulfillment of the  
requirements for the degree of

Doctor of Philosophy

(Physics)

at the

UNIVERSITY OF WISCONSIN-MADISON

1990

ACKNOWLEDGEMENTS

First of all, I would like to thank my advisor, Professor Vernon Barger, for his support and invaluable guidance throughout my graduate career. His extensive knowledge and experience were crucial to the progress made in my research. I am deeply indebted to him for making this thesis possible.

I would like to thank Dr. Roger J. N. Phillips for guidance and many collaborations; his keen insight and experience were crucial to the success of my research.

I am grateful to Drs. Ulrich Baur, Manuel Drees, Kaoru Hagiwara, Francis Halzen, JoAnne Hewett, Wai-Yee Keung, Duncan Morris, Martin Olsson, Tom Rizzo, Scott Willenbrock, and Dieter Zeppenfeld who have been always available for discussions and help. Many thanks also go to Linda Dolan, Bill Long, and Brenda Sprecher for technical assistance.

I also want to thank some of my fellow graduate students from whom I have been benefited: Drs. C. S. Kim, Jim Ohnemus, and H. Pi; as well as Gour Bhattacharya, Kingman Cheung, Bob Fletcher, Dan LaCourse, Y. B. Pan, and Alan Stange.



(~1989)

# More on the Transverse Mass: kinematics vs dynamics

## Heavy leptons at hadron supercolliders

V. Barger, T. Han, and J. Ohnemus

Show more

Phys. Rev. D 37, 1174 - Published 1 March, 1988

DOI: <https://doi.org/10.1103/PhysRevD.37.1174>

Am score 0

Citations 46

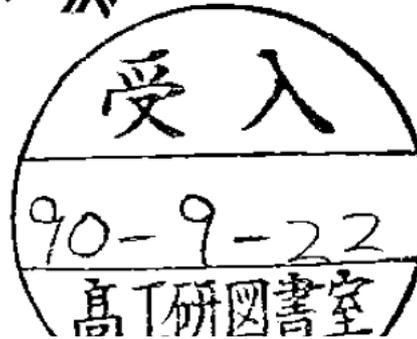
### Abstract

The production, decay, and detection of a fourth-generation charged heavy lepton  $L$  at hadron supercolliders is discussed for masses  $m_L > M_W$  and  $m_{\nu_L} \approx 0$ . The leptonic and hadronic signals for single  $L$  production and  $LL^-$  pair production are evaluated. In all channels examined, the heavy-lepton signal is smaller than backgrounds from single and pair production of  $W^\pm$  bosons. However, it may still be possible to detect a heavy lepton from its contribution to 4 jets events where the  $Z(\rightarrow \nu\bar{\nu}) + \text{jets}$  background may be determined from measurements of  $(Z \rightarrow l\bar{l}) + \text{jets}$  events.

$$M_T(l\bar{l}', \not{p}_T) = \left[ \left\{ p_T^2(l\bar{l}') + m^2(l\bar{l}') \right\}^{1/2} + |\not{p}_T| \right]^2 - |p_T(l\bar{l}') + \not{p}_T|^2$$

N. Glover, J. Ohnemus, S. Willenbrock: PDR 37 (1988) 3193: Higgs Boson Decay to One Real and One Virtual WW Boson

University of Wisconsin - Madison

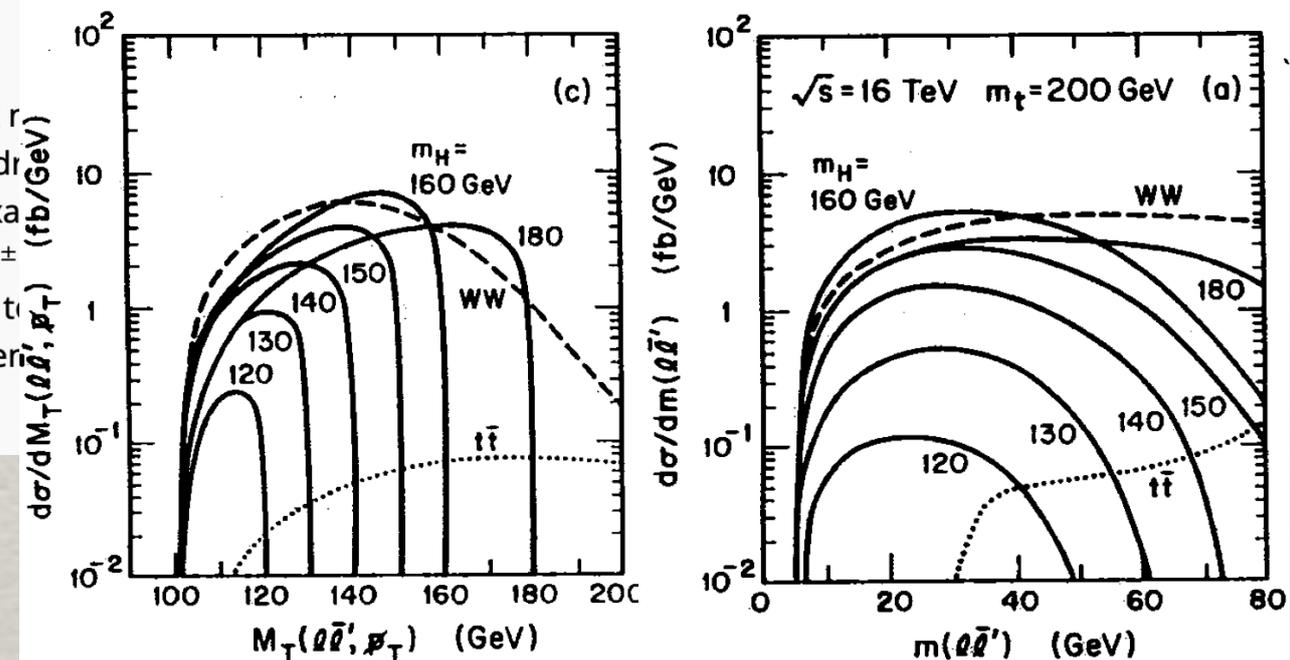


INTERMEDIATE MASS HIGGS BOSON  
AT HADRON SUPERCOLLIDERS

V. BARGER, G. BHATTACHARYA, T. HAN, AND B. A. KNieHL

Physics Department, University of Wisconsin, Madison, WI 53706, USA

MAD/PH/571  
August 1990



$M_T$  broad!  $M(l\bar{l}) \rightarrow$  spin correlation

# Forward-Jet Tagging & Central-jet Vetoing



University of Wisconsin - Madison

MAD/PH/556  
June 1990

## Strong $W^+W^+$ Scattering Signals at $pp$ Supercolliders

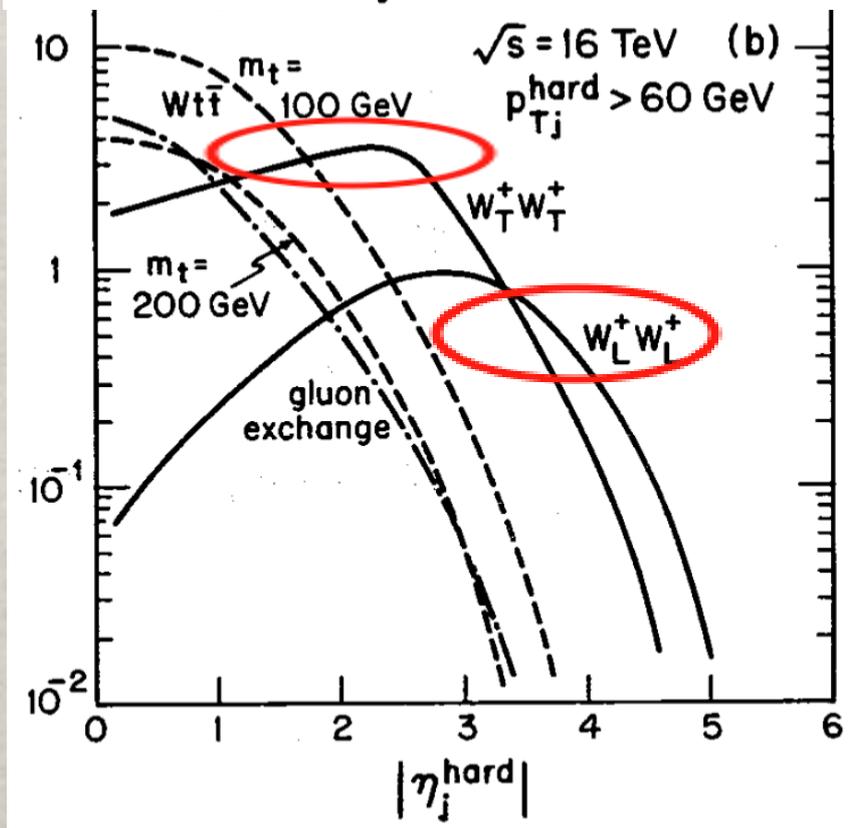
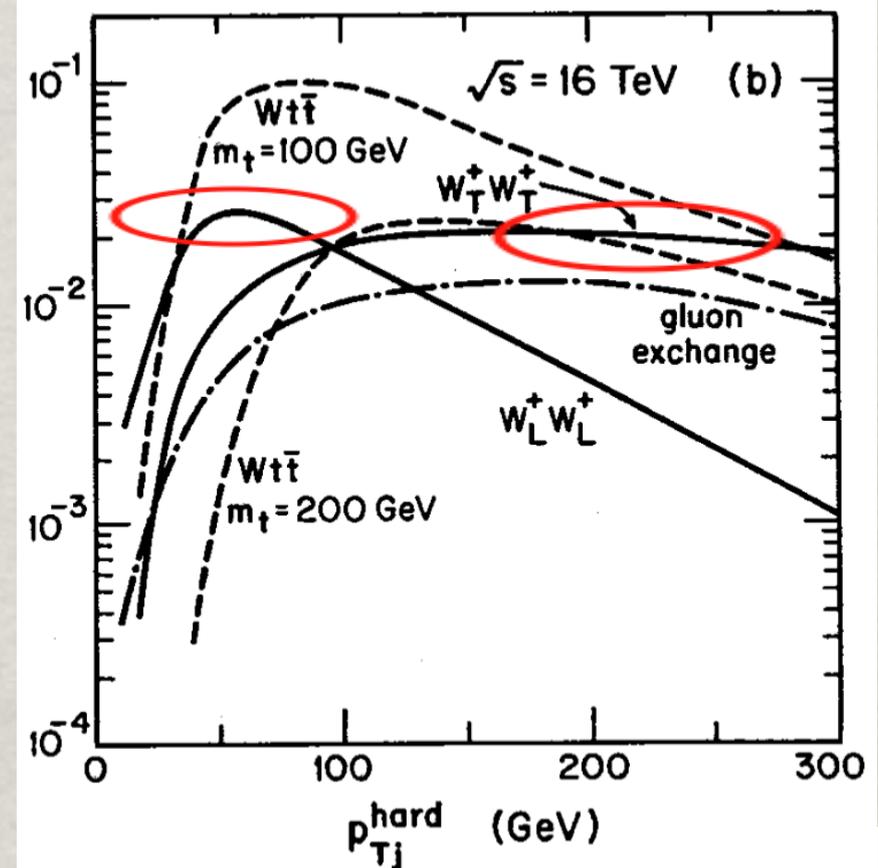
V. BARGER\*, KINGMAN CHEUNG\*, T. HAN\*, AND R. J. N. PHILLIPS†

\*Physics Department, University of Wisconsin, Madison, WI 53706

†Rutherford Appleton Laboratory, Chilton, Didcot, Oxon, England

### ABSTRACT

Like-sign  $W$  boson production has been proposed as a probe of possible strong scattering in the electroweak symmetry-breaking sector, that would enhance the production of longitudinally polarized gauge bosons. We evaluate the expected signals in the channel  $pp \rightarrow W^+W^+X$ ,  $W^+ \rightarrow \ell^+\nu$  at  $pp$  supercolliders, for several different theoretical models in which strong scattering occurs, using realistic acceptance cuts and comparing with standard model background contributions. We find that backgrounds are potentially a serious problem, especially those from electroweak production of transversely polarized  $W$  bosons. However, vetoing events with high  $p_T$  jets in the central region makes it possible to suppress all backgrounds at little cost to the signal. With an integrated luminosity of  $10 \text{ fb}^{-1}$  luminosity at the SSC or  $100 \text{ fb}^{-1}$  at the LHC and a dilepton efficiency of 50%, there could be 3 to 8 signal events, depending on the model, with about 3.5 (1.7) background events at the SSC and 8.5 (2.5) background events at the LHC for  $m_t = 100(200) \text{ GeV}$ .





University of Wisconsin - Madison



MAD/PH/638  
FERMILAB-PUB-91/76-T  
FSU-HEP-910404  
April 1991

A Comparative Study of the Benefits of Forward  
Jet Tagging in Heavy Higgs Production at the SSC

V. Barger,<sup>1</sup> Kingman Cheung,<sup>1</sup> T. Han,<sup>2</sup> J. Ohnemus,<sup>3</sup> D. Zeppenfeld<sup>1</sup>



**Fermi National Accelerator Laboratory**

Single Forward Jet-Tagging and Central Jet-Vetoing  
to Identify the Leptonic  $WW$  Decay Mode  
of a Heavy Higgs Boson

V. Barger,<sup>1</sup> Kingman Cheung,<sup>1</sup> T. Han,<sup>2</sup> D. Zeppenfeld<sup>1</sup>

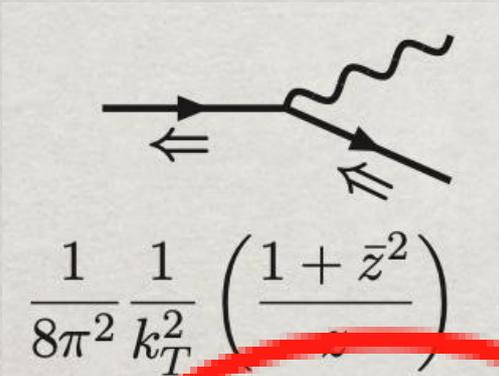
<sup>1</sup>*Department of Physics, University of Wisconsin, Madison, WI 53706*

<sup>2</sup>*Fermi National Accelerator Laboratory, P. O. Box 500, Batavia, IL 60510*

# EW Splitting: Kinematics & Dynamics

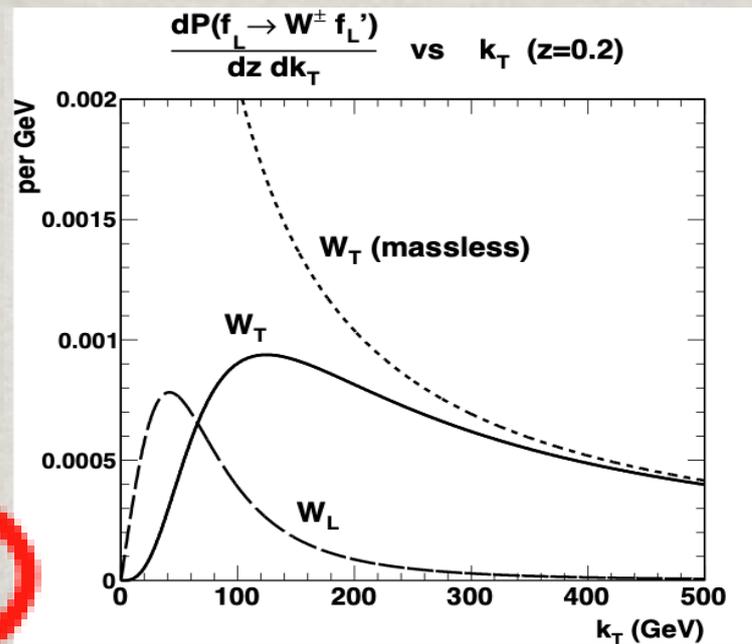
In the unbroken phase

$$f \rightarrow f V_T$$



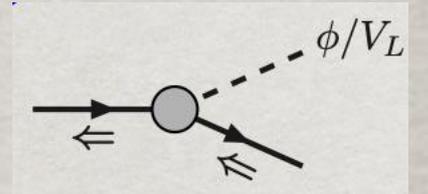
$$\frac{1}{8\pi^2} \frac{1}{k_T^2} \left( \frac{1 + \bar{z}^2}{x} \right)$$

$$P_{q \rightarrow q V_T} = (g_V^2 + g_A^2) \frac{\alpha_2}{2\pi} \frac{1 + (1-x)^2}{x} \ln \frac{Q^2}{\Lambda^2}$$



In the broken phase

$$f \rightarrow f V_L$$



$$\frac{v^2}{k_T^2} \frac{dk_T^2}{k_T^2} \sim \left(1 - \frac{v^2}{Q^2}\right)$$

$$P_{q \rightarrow q V_L} = (g_V^2 + g_A^2) \frac{\alpha_2}{\pi} \frac{1-x}{x}$$

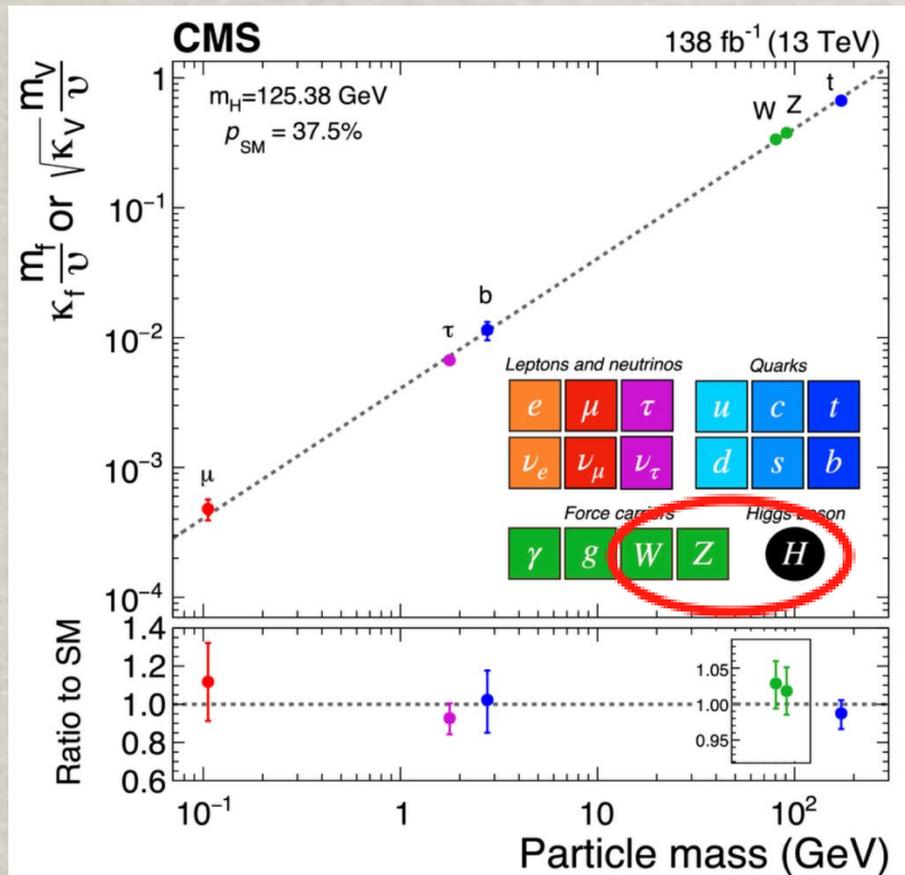
For a longitudinal vector:  $\epsilon(k)_L^\mu = \frac{E}{m_W} (\beta_W, \hat{k}) \approx \frac{k^\mu}{m_W} + O(M_W/E)$

trivial “scalarization”      EW symmetry breaking

- Broken phase  $\sim v^2 / Q^2 \rightarrow$  higher-twist effects like  $\Lambda_{\text{QCD}}^2 / Q^2$ .
- The PDFs for  $V_L$ :
  - no  $\log(Q^2/M^2) \rightarrow$  “Bjorken scaling” restoration
  - Goldstone Boson Equivalence Theorem violation!
- Kinematic basis “forward jet-tagging, central jet-vetoing”!

Ciafaloni et al., Hep-ph/0505047; J.M. Chen, TH & B. Tweedie, arXiv:1611.00788.

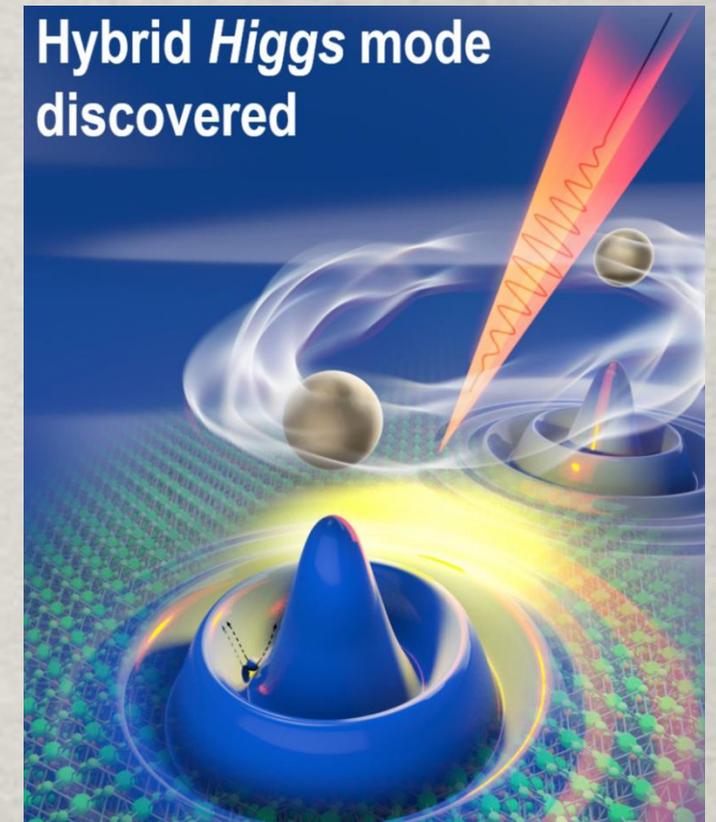
# Higgs on trial @ High Energies



$$\Phi = \begin{pmatrix} w_1 \\ w_2 \\ z \\ h \end{pmatrix}$$

or  $U = \exp\{i\omega^i \tau^i / v\}$

← CERN LHC  
 Laser @  $10^{12}$  Hz  
 (2021, Ames Lab) →



## EW Symmetry Restoration (EWSR)

$$\frac{v}{E} : \frac{v (250 \text{ GeV})}{10 \text{ TeV}} \approx \frac{\Lambda_{QCD} (300 \text{ MeV})}{10 \text{ GeV}} \quad v/E, m_t/E, M_W/E \rightarrow 0!$$

(i) the physics of the transverse gauge bosons ( $W_T^\pm, Z_T, \gamma$ ) and fermions is described by a massless theory in the unbroken phase;

(ii) the longitudinal gauge bosons ( $W_L^\pm, Z_L$ ) are scalarized as Goldstone bosons ( $\omega^\pm, \omega^0$ ), and join the Higgs boson to restore the unbroken  $O(4)$  symmetry ( $\omega^\pm, \omega^0, H$ ) in the Higgs sector.

parametrically:  $\delta = \frac{M_W}{2E_W}$

R. Capdevilla, TH, arXiv:2412.12336

# Test EWSR @ LHC / muon Collider

Huang, Lewis, Lane, Liu, arXiv:2009.09429; R. Capdevilla, TH, arXiv:2412.12336.

Massless gauge sector & Higgs sector:

$$r_{Z\gamma} = \frac{\sigma(WZ)}{\sigma(W\gamma)}, \quad r_{ZH} = \frac{\sigma(WZ)}{\sigma(WH)}$$

For  $\delta = M_W/2E \ll 1$ :

$$\frac{\sigma(W_T Z_T)}{\sigma(W_T \gamma)} \approx \frac{g_z^2 (g_-^{f_1})^2 + (g_-^{f_2})^2}{e^2 (Q_1^2 + Q_2^2)}$$

$$\sigma(W_L^\pm Z_L) \sim \sigma(W_L^\pm H),$$

or  $\sigma(\omega^\pm \omega^0) \sim \sigma(\omega^\pm H)$

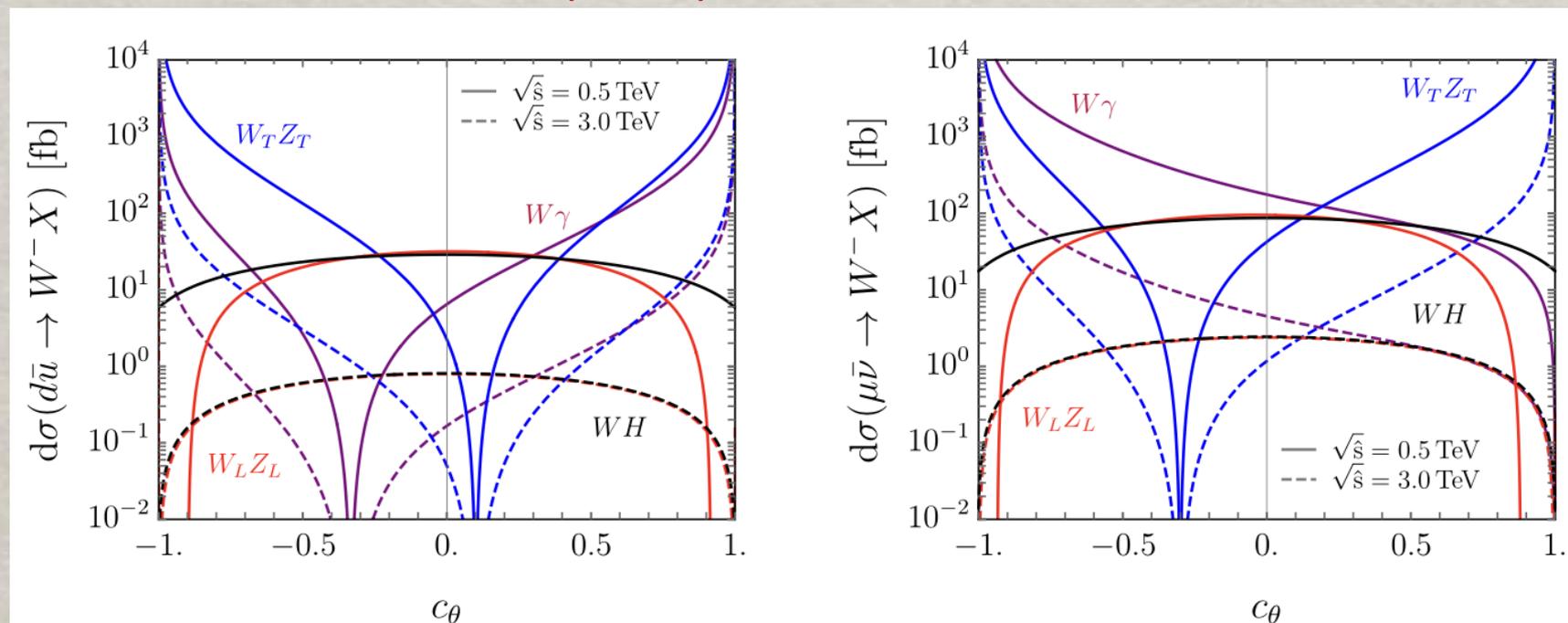
Utilizing the “Radiation Amplitude Zeros” (RAZs)

$$c_\theta^{W^- \gamma} = \frac{Q_d + Q_u}{Q_d - Q_u}$$

$$c_\theta^{W^- Z_T} = \frac{g_-^d + g_-^u}{g_-^d - g_-^u}$$

Mikaelian, Samuel PRL (1979)

U. Baur, TH, Jim Ohnemus, PRL (1994)



$$\delta \approx M_W/2 \text{ TeV} < 5\%$$

# What do we learn in testing EWSR?

“endlessly confirm the correctness of SM” ?!

- Carlo Rubia

SMEFT BSM

vs.

HEFT BSM

$$\varphi = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2}\phi^+ \\ v + H + i\phi^0 \end{pmatrix},$$

$$\mathcal{L}_{\text{SMEFT},\mu\phi} = - \sum_{n=1}^{\infty} \frac{c_{\varphi}^{(2n+4)}}{\Lambda^{2n}} (\varphi^\dagger \varphi)^{n+2}$$

$$U = e^{2i\phi^a T_a/v} \quad \text{with} \quad \phi^a T_a = \frac{1}{\sqrt{2}} \begin{pmatrix} \frac{\phi^0}{\sqrt{2}} & \phi^+ \\ \phi^- & -\frac{\phi^0}{\sqrt{2}} \end{pmatrix},$$

$$\mathcal{L}_{Uh} = \frac{v^2}{4} \text{tr}[D_\mu U^\dagger D^\mu U] F_U(H) + \frac{1}{2} \partial_\mu H \partial^\mu H - V(H)$$

weakly coupled (SUSY)

strongly coupled (composite)

new scale  $\sim \Lambda$

nearby scale  $\sim 4\pi v$

At the LHC: Higgs coupling SM-like  $\sim 10\%$

(light) Fermion Yukawa's wide open:

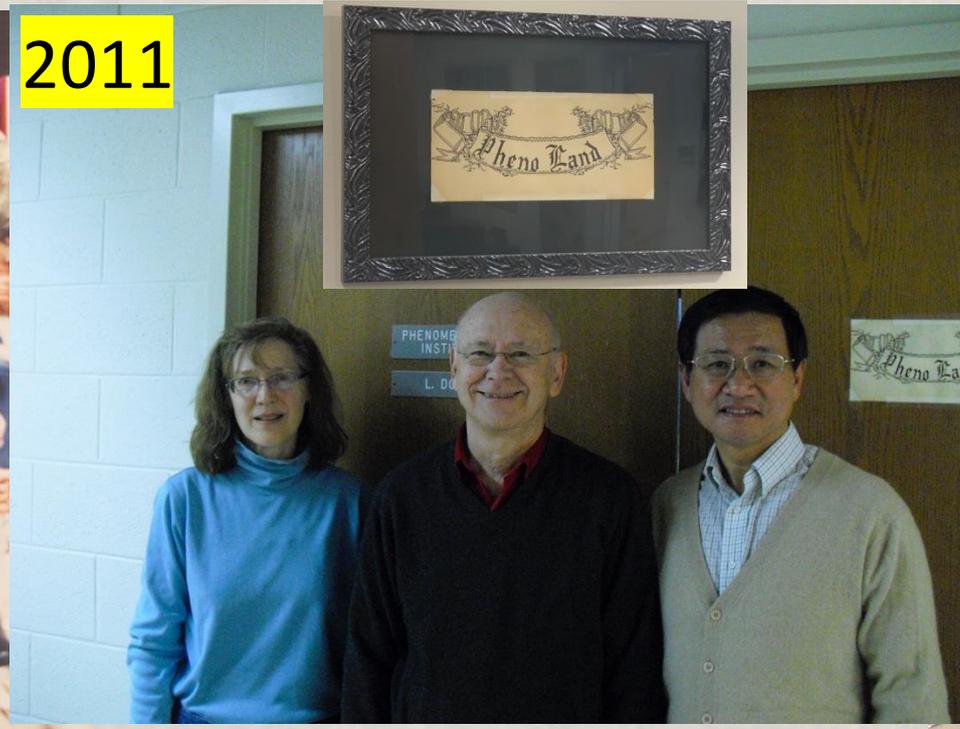
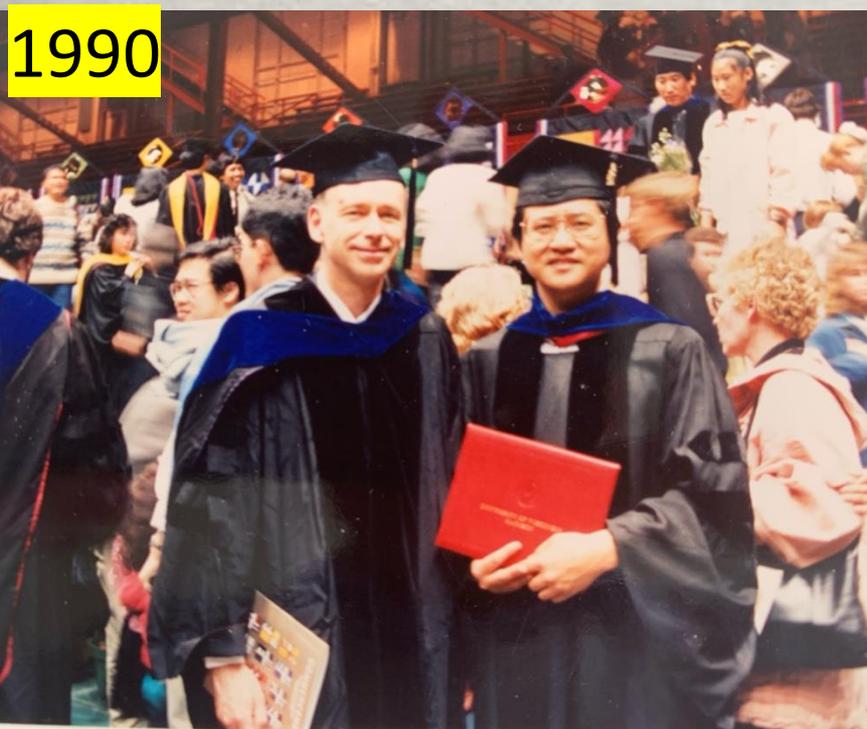
$$- \sum_{n=1}^{\infty} \frac{c_{l\varphi}^{(2n+4)}}{\Lambda^{2n}} (\varphi^\dagger \varphi)^n (\bar{l}_L \varphi \mu_R + \text{h.c.})$$

$$- \frac{v}{\sqrt{2}} [\bar{l}_L Y_\ell(H) U P_- \ell_R + \text{h.c.}]$$

$$Y_\ell(H) = \frac{\sqrt{2}m_\mu}{v} + \sum_{k \geq 1} y_{\ell,k} \left(\frac{H}{v}\right)^k$$

E. Celada, TH et al., arXiv:2312.13082

# Journey in phenomenology before & after the Higgs boson



**Congratulations Vernon  
for the 2021 APS Sakurai Prize!**

2021 Sakurai Prize Lecture

Vernon Barger

University of Wisconsin - Madison



# Pheno family tree

70 postdocs

40 PhD students

Name	Year	C
George Wojcik	2021-2024	C
Nicholas Orlofsky	2017-2020	C
Joshua Berger	2015-2018	P
Ran Lu	2013-2016	A
Jordi Salvado	2013-2015	P
Gabe Shaughnessy	2011-2014	S
Maïke Trenkel	2009-2011	R
Pavel Fileviez Perez	2010-2011	A
Sogee Spinner	2008-2011	S
Ian-Woo Kim	2007-2010	S
Tom McElmurry	2007-2010	S
Kathryn Zurek	2006-2008	A
Devin Walker	2006-2007	P
Patrick Huber	2006-2007	P
Hooman Davoudiasl	2004-2007	P
Heather Logan	2004-2006	F
Cheng-Wei Chiang	2002-2005	P
Lian-Tao Wang	2003-2004	P
Graham Kribs	2002-2004	P
Tilman Plehn	2000-2003	P
Carlo Oleari	1998-2002	P
Michal Brhlik	2000-2002	P
Stefan Hesselbach	2000-2001	S
Jaime Alvarez	2000-2001	T
Ren-Jie Zhang	1999-2000	P
Mauricio Magro	1998-2000	I
Toby Falk	1998-2000	P
Chung Kao	1997-2000	L
Gustavo Burdman	1996-2000	P
James Kelly	1996-1999	P
Laura Reina	1996-1998	A
Sean Fleming	1997-1998	P
James Amundson	1995-1997	P
Youichi Yamada	1994-1996	P
Erwin Mirkes	1995-1996	P
David Summers	1993-1995	P
Brian Wright	1993-1995	P
Maria Concepcion Gonzalez-Garcia	1992-1995	P
	1991-1994	P

Name	Year	Current Position
Michael Berger	1991-1994	Professor, University of Indiana
Mihiko Doncheski	1990-1993	Director of Academic Affairs, Penn State Mont Alto
Ted Allen	1992-1993	Professor, KEK
Gye (Tai) Park	1991-1997	Assoc. Professor, Hobart & William Smith
Roxanne Springer	1991-1992	Professor, Yonsei University
Enrique Zas	1990-1992	Professor, Duke University
Ulrich Baur	1990-1991	Deceased (formerly prof. at SLAC)
Berndt Kniehl	1989-1991	Professor, University of Bonn
Robert Foot	1989-1991	Deceased
Oscar Hernandez	1989-1990	Professor, University of Hamburg
JoAnne Hewett	1988-1991	Academic Staff, University of Melbourne
David B. Reiss	1988-1991	Professor, Marianopolis College
Duncan Morris	1988-1989	Professor, SLAC
Dieter Zeppenfeld	1987-1990	Consultant, Scientific Arts, Wolfram Sol.
Manuel Drees	1986-1989	Financial Industry (Canada/stock trading)
Kari Enqvist	1986-1988	Professor, University of Karlsruhe
Sumathi Rao	1986-1988	Professor, University of Bonn
Scott Willenbrock	1986-1987	Professor, Harish-Chandra Research Institute
Xerxes Tata	1986-1988	Professor, University of Illinois
Alexander Jourjine	1984-1986	Professor, University of Hawaii
Paul Stevenson	1984-1986	Professor, Tohoku University
M. Teresa Thomaz	1983-1984	MPI for Physics of Complex Systems, Dresden
Kaoru Hagiwara	1982-1983	Professor (emeritus), Rice University
J. L. Cortes	1981-1984	Professor, Univ. Federal Fluminense, Brazil
Cosmas Zachos	1981-1984	Professor, University of Zaragoza
Jacques Leveille	1981-1983	Professor, Argonne National Laboratory
David Scott	1979-1981	Professor, University of Kentucky
Benedikt Humpert	1978-1980	Lecturer, Cambridge University, Chem. Engineering
Julio Abad	1977-1978	Deceased (Formerly Professor, University of Zaragoza)
Dimitri Nanopoulos	1976-1978	Lecturer, Houston (geophysics)
Mark Singer	1976-1977	Swiss Business School, Zurich
Ronald McElhaney	1975-1977	Professor, Texas A&M University
Edward Osypowski	1973-1975	Boeing Advanced Technology
Chris Michael	1970-1971	Chief Technology Officer, Siebel Systems (Oracle)
Miguel Virasoro	1969-1969	Senior Lecturer (emeritus), University of Wisconsin, Marathon Co.
Keiji Kikkawa	1968-1970	Professor (emeritus), University of Liverpool
Paul Fishbane	1968-1969	Theoretical Physics
L. M. Simmons	1967-1969	Professor (emeritus), Kanagawa U., Dept. of Information Science
	1967-1969	Professor (emeritus), University of Virginia
	1967-1969	Co-founder, Santa Fe Center for Emergent Strategies and President, Aspen Center for Physics (1985-88)

Name	PhD	Advisor	Current Position
Stephen McKay	2024	Barger (w/ A. Barger)	Current student
Kairui Zhang	2014	Barger	Current student
Andrea Peterson	2013	Barger	Science Policy Analyst, FYI: Science Policy News, AIP
Tien-Tien Yu	2013	Barger	Associate Professor, University of Nebraska
Peisi Huang	2011	Barger	Associate Professor, University of Kansas
Brian Yenchao	2011	T. Han (w/ Barger)	Software Developer, Livefront
Ian Lewis	2010	Barger	Associate Professor, University of Kansas
Mat McCaskey	2010	Barger	Software engineer, Vantage Partners
Yu Gao	2010	Barger	Scientist, Beijing Institute of HEP
Gabe Shaughnessy	2007	Barger	Senior data scientist, Jungle Scout
Adam Tregre	2007	Barger	Actuarial analyst, QBE North America
Hye-Sung Lee	2005	Barger	Professor, Institute for Basic Science, Daejeon, Korea
Benjamin Wood	2002	Barger	Military systems analyst
Young-Jae Kim	2002	T. Han (w/Barger)	Scientific consultant, KhiMetrics
Danny Marfatia	2001	T. Han (w/Barger)	Professor, University of Hawaii
Tianjun Li	2000	L. Durand (w/ Barger)	Professor, UESTC, Chengdu
Hong Pi	1989	Balantekin (w/Barger)	Ocwen Financial Corporation
John Beacom	1997	Barger	Professor, The Ohio State University
Pedro Mercadante	1994	Barger	Assoc. Professor, U. Federal do ABC, Brazil
Paul Ohmann	1992	Barger	Professor, University of St. Thomas
Gour Bhattacharya	1992	Barger	Professor, Tsing Hua University
Kingman Cheung	1992	Barger	Assoc. Professor, Takii Govt. College, India
Alan Stange	1990	Barger	Professor, Tsing Hua University
Tao Han	1989	Barger	Financial analyst, Renaissance Technologies
William Putikka	1988	Barger	Professor, University of Pittsburgh
James Ohnemus	1987	Barger	Assoc. Professor, Ohio State U. at Mansfield
Howard Baer	1984	Barger	Senior Engineer (Sept 09), Cray Inc.
Kerry Whisnant	1982	Barger	Quantitative analyst, Iberdrola Renewables
Wai-Yee Keung	1980	Barger	Professor, University of Oklahoma
Thomas Gottschalk	1978	Barger	Professor (emeritus), UIC
Thomas Weiler	1976	Barger	Comp science, Caltech
John Luthé	1975	Barger	Deceased (Formerly Professor, Vanderbilt University)
Kevin Geer	1973	Barger	Assoc. Professor, Comp Sci and Engineering
Penny Estabrooks	1972	Barger	Mississippi State University
Peter Weiler	1971	Barger	Technical analyst, Santa Barbara
K.V.L. Sarma	1969	Barger	Professor (emeritus), Carleton University
			Computer specialist, UW-Madison (retired)
			Deceased (Formerly Professor, Tata Institute)

Vernon D. Barger  
 Emil Kazes  
 Marvin Goldberger  
 Enrico Fermi

**Back up slides**

# Radiation Amplitude Zeros (RAZs)

VOLUME 43, NUMBER 11

PHYSICAL REVIEW LETTERS

10 SEPTEMBER 1979

## Magnetic Moment of Weak Bosons Produced in $pp$ and $p\bar{p}$ Collisions

K. O. Mikaelian and M. A. Samuel

Physics Department, Oklahoma State University, Stillwater, Oklahoma 74074

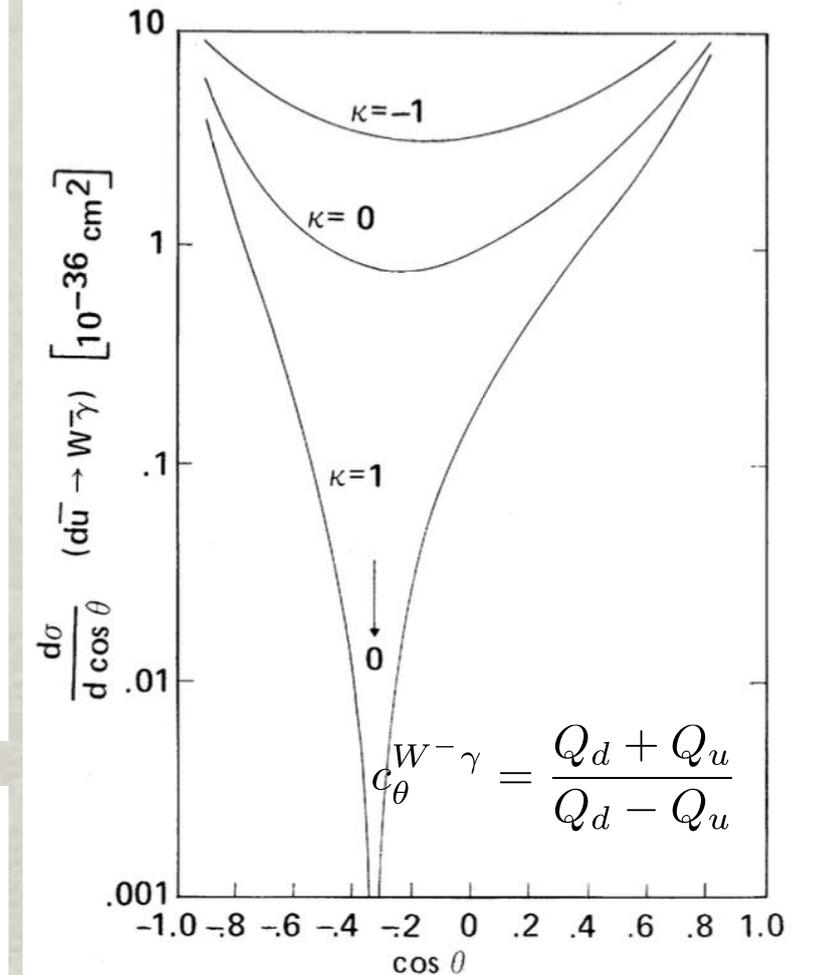
and

D. Sahdev

Physics Department, Case Western Reserve University, Cleveland, Ohio 44106

(Received 5 June 1979)

We suggest that the reactions  $pp \rightarrow W^\pm \gamma X$  and  $p\bar{p} \rightarrow W^\pm \gamma X$  are good candidates for measuring the magnetic moment parameter  $\kappa$  in  $\mu_W = (e/2M_W)(1+\kappa)$ . The angular distribution of the  $W$  bosons in  $p\bar{p} \rightarrow W^\pm \gamma X$  is particularly sensitive to this parameter. For the gauge-theory value of  $\kappa = 1$ , we have found a peculiar zero in  $d\sigma(d\bar{u} \rightarrow W^- \gamma)/d\cos\theta$  at  $\cos\theta = -\frac{1}{3}$ , the location of this zero depending on the quark charge through  $\cos\theta = -(1+2Q_d)$ . A similar zero occurs in  $d\sigma(u\bar{d} \rightarrow W^+ \gamma)/d\cos\theta$ . We can offer no explanation for this behavior.



VOLUME 72, NUMBER 25

PHYSICAL REVIEW LETTERS

20 JUNE 1994

## Amplitude Zeros in $W^\pm Z$ Production

U. Baur

Department of Physics, Florida State University, Tallahassee, Florida 32306

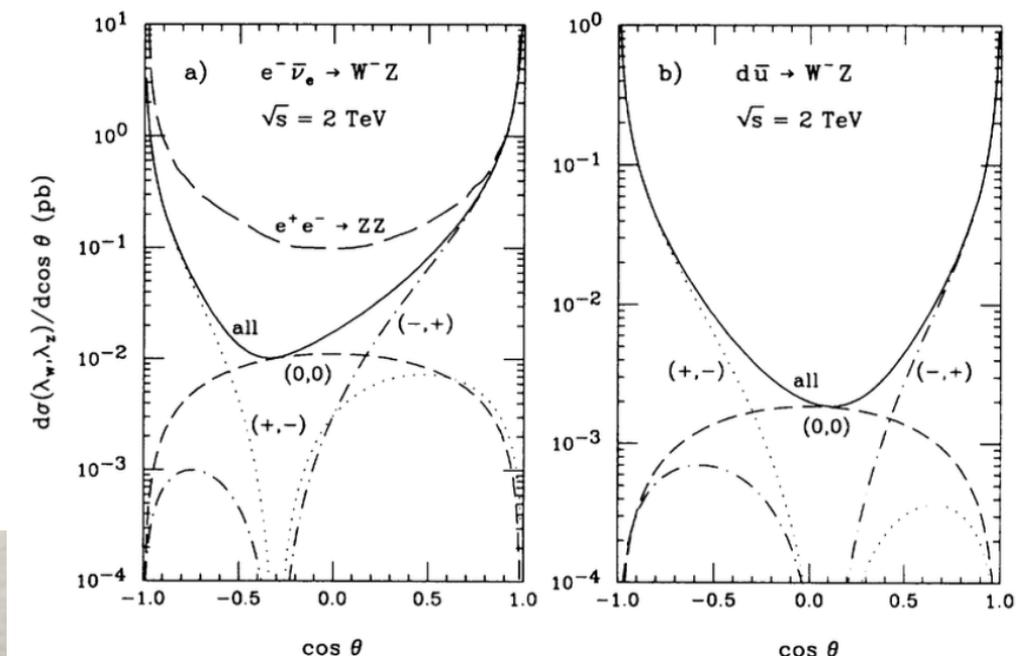
T. Han and J. Ohnemus

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(Received 9 March 1994)

We demonstrate that the standard model amplitude for  $f_1\bar{f}_2 \rightarrow W^\pm Z$  at the Born level exhibits an approximate zero located at  $\cos\theta = (g_-^{f_1} + g_-^{f_2}) / (g_-^{f_1} - g_-^{f_2})$  at high energies, where the  $g_-^{f_i}$  ( $i = 1, 2$ ) are the left-handed couplings of the  $Z$  boson to fermions and  $\theta$  is the center of mass scattering angle of the  $W$  boson. The approximate zero is the combined result of an exact zero in the dominant helicity amplitudes  $\mathcal{M}(\pm, \mp)$  and strong gauge cancellations in the remaining amplitudes. For non-standard  $WWZ$  couplings these cancellations no longer occur and the approximate amplitude zero is eliminated.

$$c_\theta^{W^- Z_T} = \frac{g_-^d + g_-^u}{g_-^d - g_-^u}$$



# Test EWSR @ LHC / muon Collider

Huang, Lewis, Lane, Liu, arXiv:2009.09429; R. Capdevilla, TH, arXiv:2412.12336.

Massless gauge sector & Higgs sector:

$$r_{Z\gamma} = \frac{\sigma(WZ)}{\sigma(W\gamma)}, \quad r_{ZH} = \frac{\sigma(WZ)}{\sigma(WH)}$$

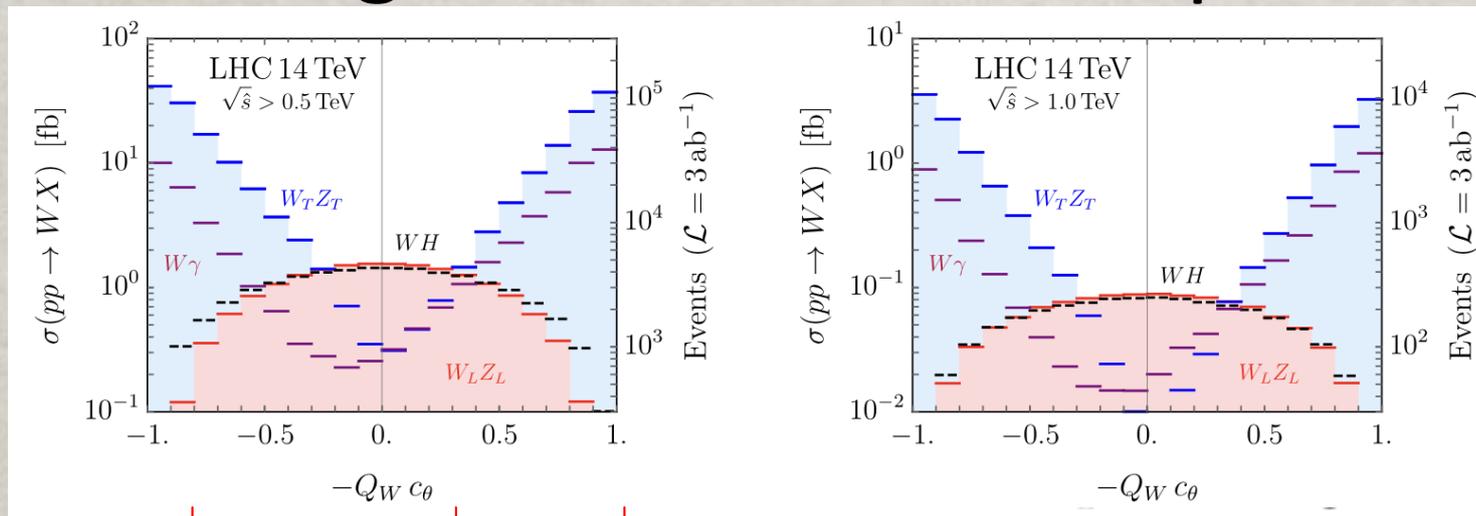
For  $\delta = M_W/2E \ll 1$ :

$$\frac{\sigma(W_T Z_T)}{\sigma(W_T \gamma)} \approx \frac{g_z^2 (g_-^{f_1})^2 + (g_-^{f_2})^2}{e^2 (Q_1^2 + Q_2^2)}$$

$$\sigma(W_L^\pm Z_L) \sim \sigma(W_L^\pm H),$$

or  $\sigma(\omega^\pm \omega^0) \sim \sigma(\omega^\pm H)$

Utilizing the “Radiation Amplitude Zeros” (RAZs)

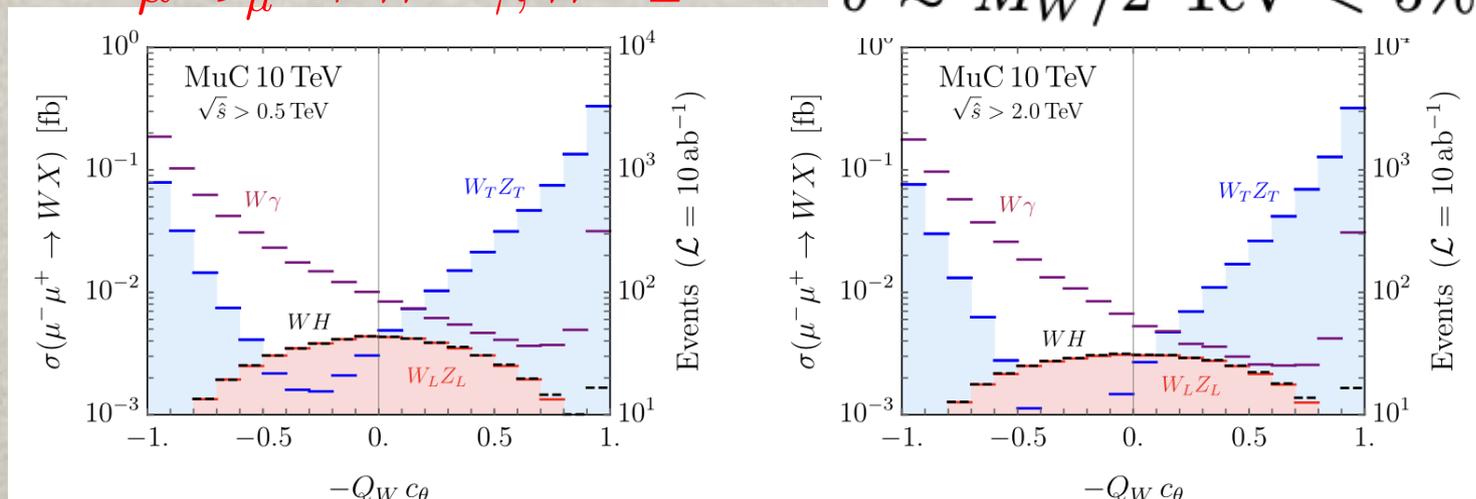


$$c_\theta^{W^- \gamma} = \frac{Q_d + Q_u}{Q_d - Q_u}$$

$$c_\theta^{W^- Z_T} = \frac{g_-^d + g_-^u}{g_-^d - g_-^u}$$

$\mu^\pm \nu_\mu \rightarrow W^\pm \gamma, W^\pm Z$

$\delta \approx M_W/2 \text{ TeV} < 5\%$



U. Baur, TH, Jim Ohnemus,  
PRL (1994)

$$\begin{aligned}
 f_1 \bar{f}_2 &\rightarrow W^\pm \gamma, \\
 f_1 \bar{f}_2 &\rightarrow W^\pm Z, \\
 f_1 \bar{f}_2 &\rightarrow W^\pm H.
 \end{aligned}$$

$$\begin{aligned}
 \mathcal{M}_{\pm\mp}^{W\gamma} &\approx -\frac{geV_{12}}{\sqrt{2}} \frac{(\lambda_w - c_\theta)}{s_\theta} \left[ Q_{(1-2)c_\theta} - Q_{(1+2)} \right], \\
 \mathcal{M}_{\pm\mp}^{WZ} &\approx \frac{gg_z V_{12}}{\sqrt{2}} \frac{(\lambda_w - c_\theta)}{s_\theta} \left[ g_-^{(1-2)} c_\theta - g_-^{(1+2)} \right], \\
 \mathcal{M}_{00}^{WZ} &\approx -\frac{g_z^2 V_{12}}{2\sqrt{2}} s_\theta g_-^{(1-2)} = \frac{g^2 V_{12}}{2\sqrt{2}} s_\theta, \\
 \mathcal{M}_0^{WH} &\approx \frac{g^2 V_{12}}{2\sqrt{2}} s_\theta,
 \end{aligned}$$

- Gauge sector: Radiation Amplitude Zeros (RAZs)

EM:  $c_\theta^{W^- \gamma} = \frac{Q_d + Q_u}{Q_d - Q_u}$  EW (transverse):  $c_\theta^{W^- Z_T} = \frac{g_-^d + g_-^u}{g_-^d - g_-^u}$

Mikaelian, Samuel (1979)

$$c_{\theta_0} = \begin{cases} -1/3 (\approx 0.1) & \text{for } d\bar{u} \rightarrow W_T^- \gamma (W_T^- Z_T), \\ 1 (\approx -0.3) & \text{for } \ell^- \bar{\nu} \rightarrow W_T^- \gamma (W_T^- Z_T), \end{cases}$$

U. Baur, TH, JO, (1994)

- Higgs scalar sector:  $\mathcal{M}^{W_L Z_L} (\delta \ll 1) \approx \mathcal{M}^{W_L h} (\delta \ll 1)$

