

MASSIVE NEUTRINOS IN 2025

Concha Gonzalez-Garcia

(*YITP-Stony Brook & ICREA-University of Barcelona*)

Phenomenology Before and After the Standard Model

a symposium in honor of Vernon Barger

Madison, June 5, 2025



Solar experiments

- Chlorine total rate, 1 data point.
- Gallex & GNO total rates, 2 points.
- SAGE total rate, 1 data point.
- SK1 E and zenith spect, 44 points.
- SK2 E and D/N spect, 33 points.
- SK3 E and D/N spect, 42 points.
- SK4 2970-day E spectrum and D/N asym, 46 points.
- SNO combined analysis, 7 points.
- Borexino Ph-I 740.7-day low-E spect 33 points.
- Borexino Ph-I 246-day high-E spect ,6 points.
- Borexino Ph-II 1292-day low-E spect, 192 points.
- Borexino Ph-III 1433-day low-E spect, 120 points.

Reactor experiments

- KamLAND DS1,DS2&DS3 spectra with Daya-Bay fluxes 69 points
- DChooz FD/ND ratios with 1276-day (FD) and 587-day (ND) exposures , 26 points.
- Daya-Bay 3158-day EH1,EH2, EH3 spectra ,78 points.
- Reno 2908-day FD/ND ratios 45 points.

Atmospheric experiments

- IceCube/DeepCore 2019 3-year data.
- IceCube/DeepCore 2014 9,3-year data (χ^2 table provided)
- K I-V 484 kton-years(χ^2 table provided by SK)

Accelerator experiments

- MINOS 10.71×10^{20} pot ν_μ -disapp data, 39 points.
- MINOS 3.36×10^{20} pot $\bar{\nu}_\mu$ -disapp data , 14 points.
- MINOS 10.6×10^{20} pot ν_e -app data , 5 points.
- MINOS 3.3×10^{20} pot $\bar{\nu}_e$ -app data , 5 points.
- T2K 21.4×10^{20} pot ν_μ -disapp data, 28 points.
- T2K 21.4×10^{20} pot ν_e -app data, 9 points CCQE and 7 p
- T2K 16.3×10^{20} pot $\bar{\nu}_\mu$ -disapp, 19 points.
- T2K 16.3×10^{20} pot $\bar{\nu}_e$ -app, 9 points.
- NO ν A 26.6×10^{20} pot ν_μ -disapp data , 21 points.
- NO ν A 26.6×10^{20} pot ν_e -app data , 15 points.
- NO ν A 12.5×10^{20} pot $\bar{\nu}_\mu$ -disapp, 18 points.
- NO ν A 12.5×10^{20} pot $\bar{\nu}_e$ -app, 13 points.

The New Minimal Standard Model

- Minimal Extension to allow for LFV $\Rightarrow$ give Mass to the Neutrino

* With SM fields: Use ν_L^c is right-handed

$$\mathcal{L} - \mathcal{L}_{SM} = -\frac{1}{2} M_\nu \overline{\nu_L} \nu_L^c + h.c. \Rightarrow \begin{cases} L \text{ is violated} \Rightarrow \text{Majorana } \nu = \nu^c \\ SU(2)_L \text{ is violated} \Rightarrow \text{Effective LE} \end{cases}$$

* Introduce ν_R AND impose L conservation

$$\mathcal{L} - \mathcal{L}_{SM} = -M_D \overline{\nu_L} \nu_R - \frac{1}{2} \cancel{M_R} \overline{\nu_R} \nu_R^c + h.c. \Rightarrow \text{Dirac } \nu \neq \nu^c:$$

- Either way $\Rightarrow$ Mixing in charged current interactions of massive leptons

$$\frac{g}{\sqrt{2}} W_\mu^+ \sum_{ij} \left(U_{\text{LEP}}^{ij} \overline{\ell^i} \gamma^\mu L \nu^j + U_{\text{CKM}}^{ij} \overline{U^i} \gamma^\mu L D^j \right) + h.c.$$

The New Minimal Standard Model: ν flavour oscillations

- In vacuum:

$$P_{\alpha\beta} = \delta_{\alpha\beta} - 4 \sum_{j \neq i}^n \text{Re}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin^2 \left(\frac{\Delta_{ij}}{2} \right) + 2 \sum_{j \neq i} \text{Im}[U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*] \sin(\Delta_{ij})$$

$$\Delta_{ij} = (m_i^2 - m_j^2) \frac{L}{4E} \Rightarrow \text{No information on } \nu \text{ mass scale nor Majorana/Dirac}$$

- When osc between 2- ν dominates: $P_{\alpha \neq \beta} = \sin^2(2\theta) \sin^2 \left(\frac{\Delta m^2 L}{4E} \right)$
 $\Rightarrow$ No information on Mass Ordering ($\equiv \text{sign}(\Delta m^2)$) nor octant of θ nor CPV

The New Minimal Standard Model: ν flavour oscillations

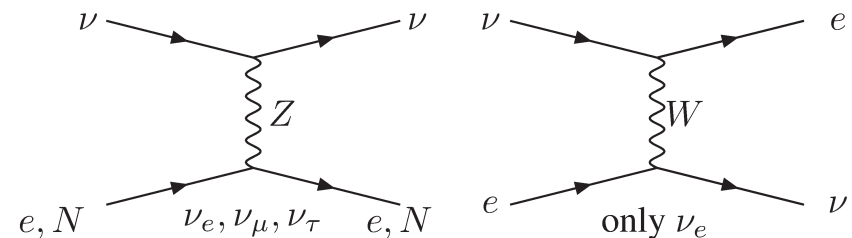
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- If ν cross matter regions (Sun, Earth...) it interacts coherently
 Different flavours have different interaction



- $\Rightarrow$ Effective potential in ν evolution: $V_e \neq V_{\mu,\tau} \Rightarrow \Delta V^{\nu_e} = -\Delta V^{\bar{\nu}_e} = \sqrt{2} G_F N_e$
- $\Rightarrow$ Modification of mixing angle and oscillation wavelength (MSW)
- $\Rightarrow$ For solar ν 's: Dependence on θ octant
- $\Rightarrow$ In LBL terrestrial experiment: Dependence on sign of Δm^2 and θ octant

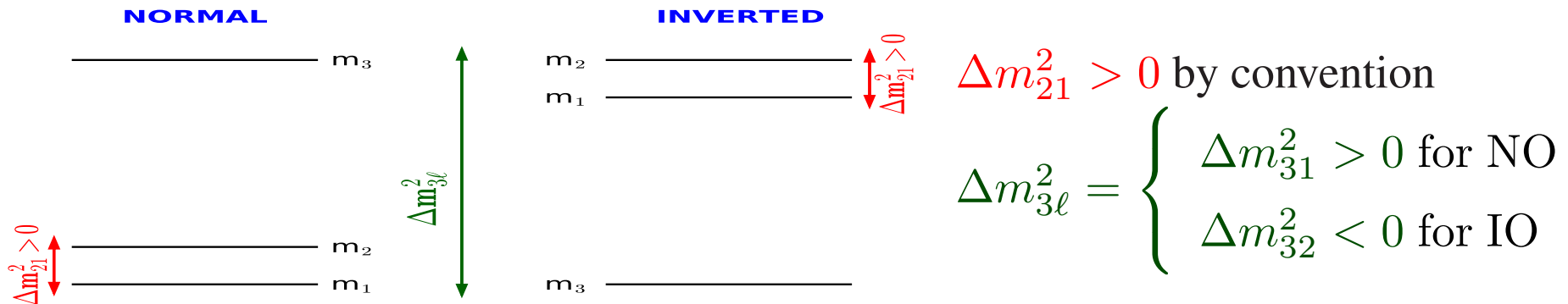
3ν Flavour Parameters

Concha Gonzalez-Garcia

- For 3 ν's : 3 Mixing angles + 1 Dirac Phase + 2 Majorana Phases

$$U_{\text{LEP}} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{i\delta_{\text{CP}}} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta_{\text{CP}}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{21} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} e^{i\phi_{21}} & 0 & 0 \\ 0 & e^{i\phi_{12}} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- Convention: $0 \leq \theta_{ij} \leq 90^\circ$ $0 \leq \delta \leq 360^\circ \Rightarrow 2$ Orderings



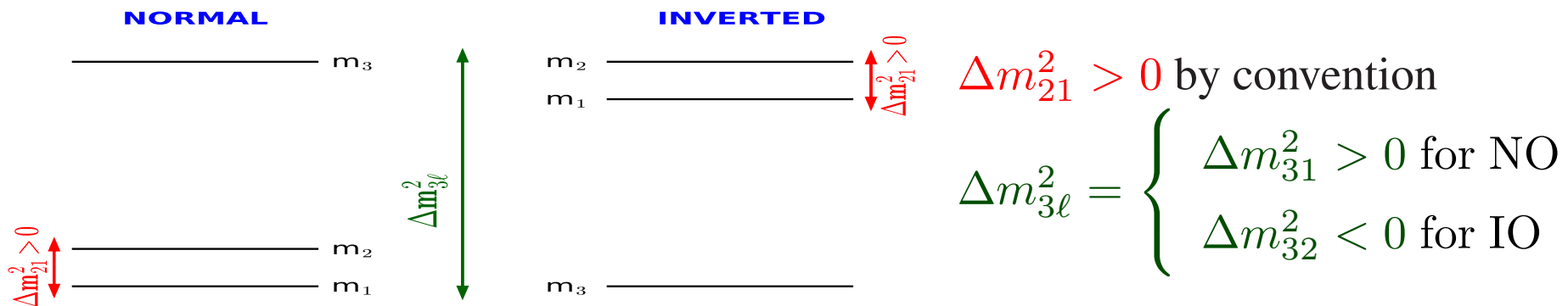
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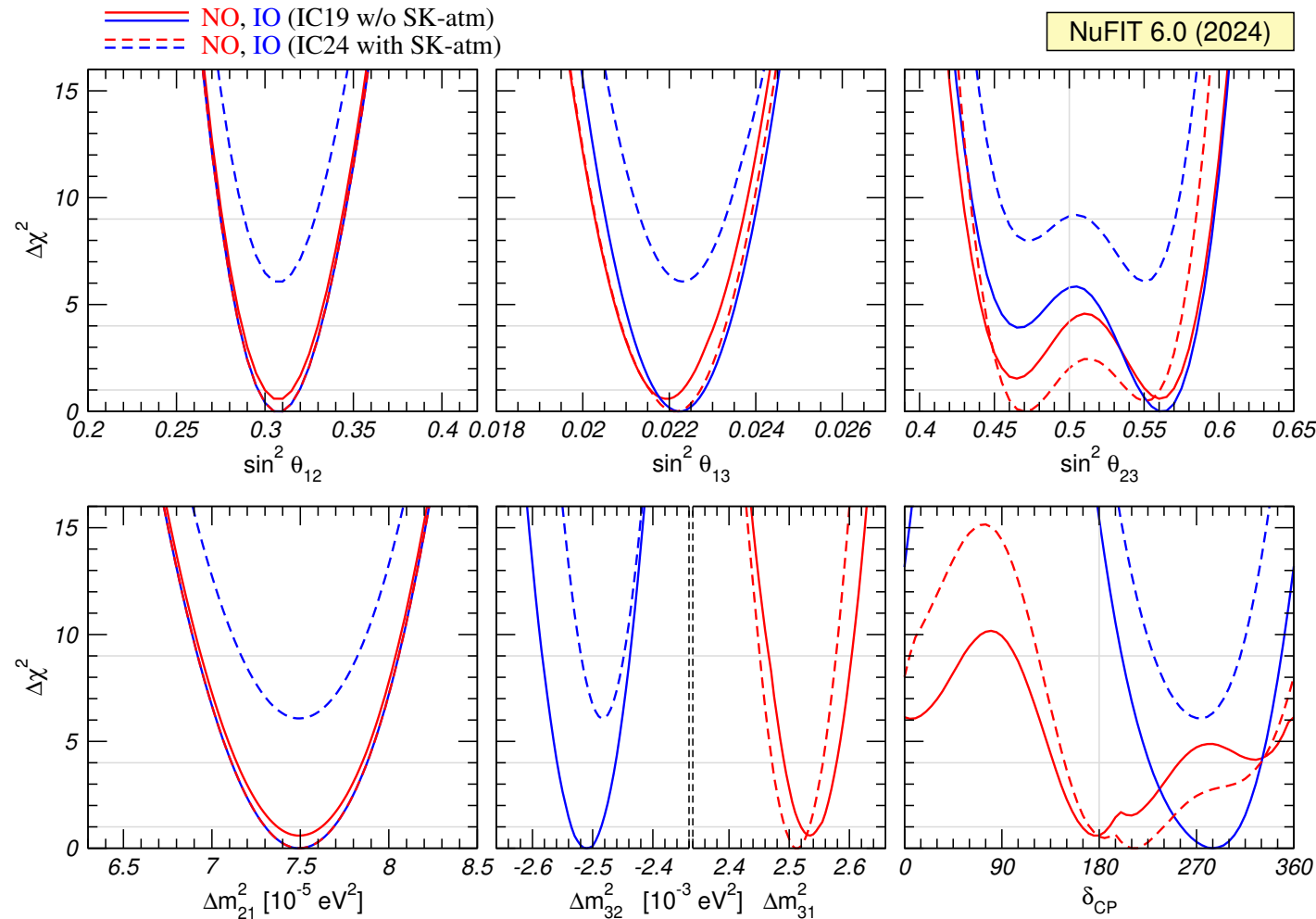
Experiment	Dominant	Important	Additional
Solar Experiments	θ_{12}	Δm_{21}^2	θ_{13}
Reactor LBL (KamLAND)	Δm_{21}^2	θ_{12}	θ_{13}
Reactor MBL (Daya Bay, Reno, D-Chooz)	$\theta_{13}, \Delta m_{3\ell}^2$		
Atmospheric Experiments (SK, IC)	θ_{23}	$\Delta m_{3\ell}^2$	$\theta_{13}, \delta_{\text{CP}}$
Acc LBL ν_μ Disapp (Minos, T2K, NOvA)	$\Delta m_{3\ell}^2, \theta_{23}$		
Acc LBL ν_e App (Minos, T2K, NOvA)	δ_{CP}	θ_{13}	$\theta_{23}, \Delta m_{3\ell}^2, \Delta m_{3\ell}^2$

Global 3 ν Flavour Parameters: Spring 2025

Global 6-parameter fit <http://www.nu-fit.org>

Esteban, Gonzalez-Garcia, Maltoni, Martinez, Pinheiro, Schwetz, 2410.05380

(In last years good agreement with results from Bari (2503.07752) and Valencia groups)

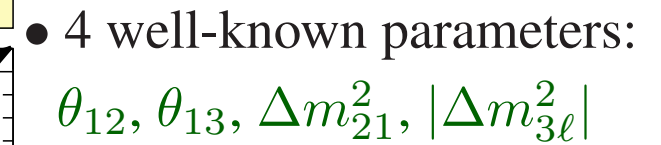


SK-atm $\equiv \chi^2$ table from SK1-5

IC24 $\equiv \chi^2$ table from Icecube
data from 2405.02163

IC19 $\equiv$ Our analysis of Icecube
data from 1902.07771

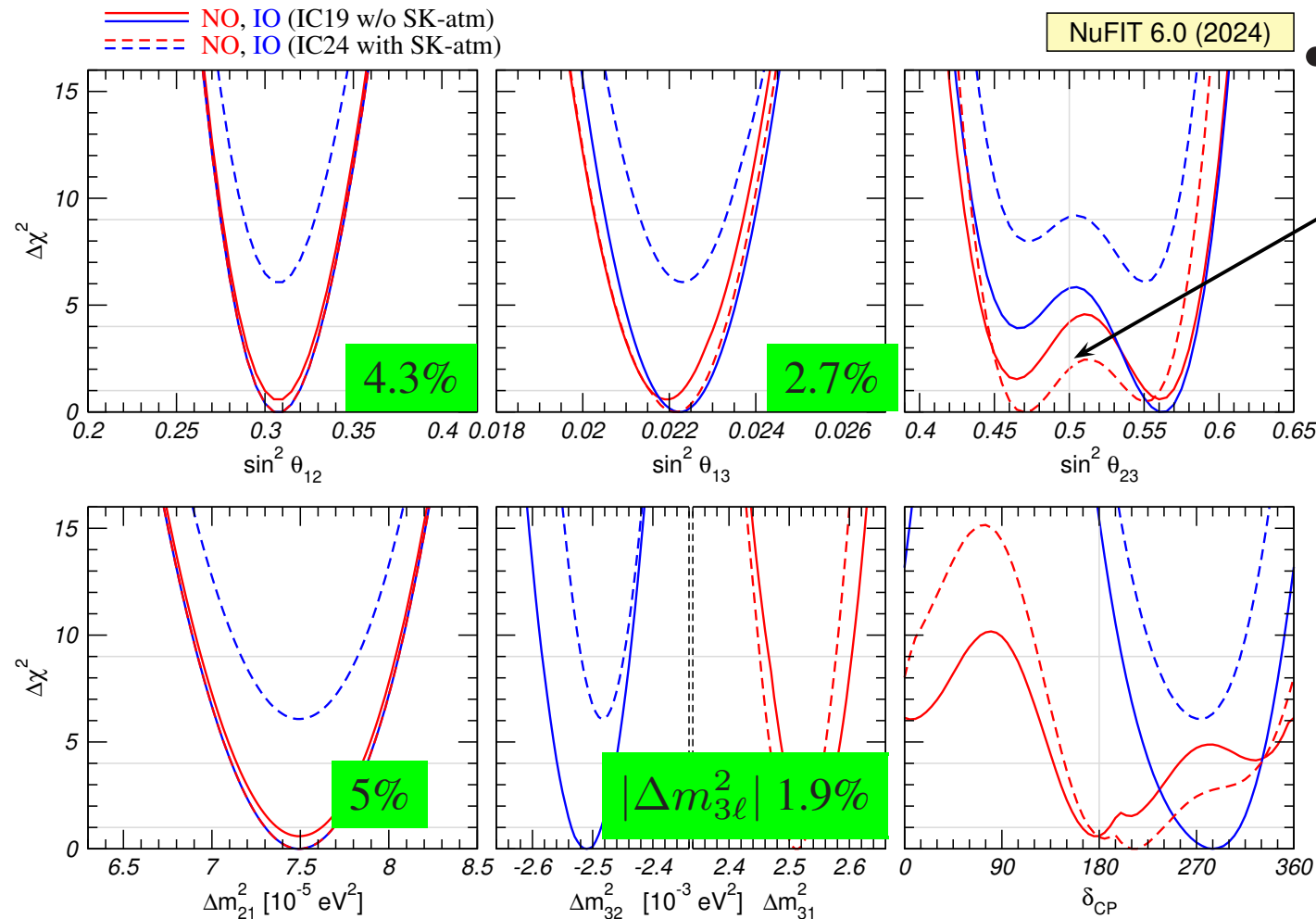
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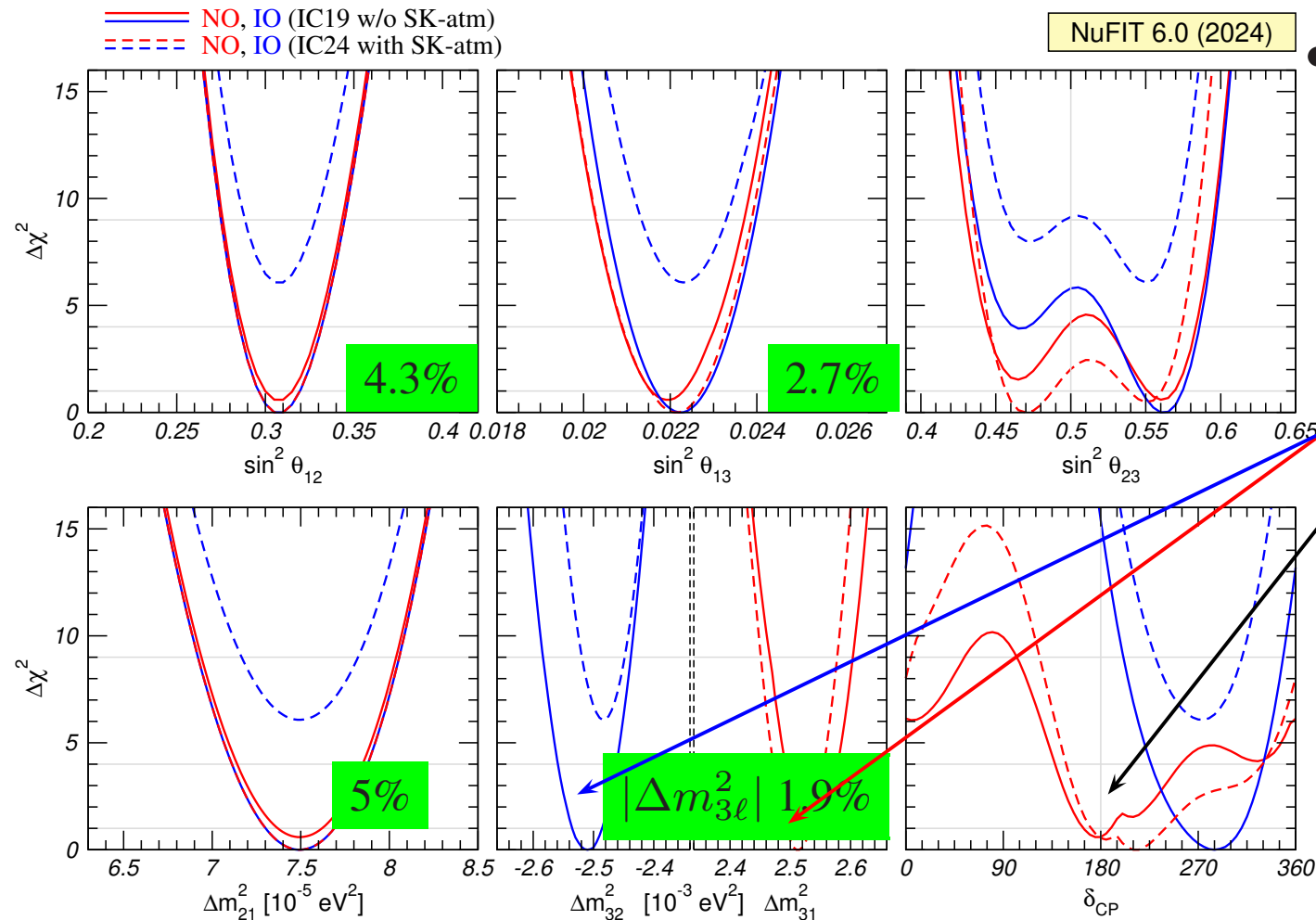
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• 4 well-known parameters:

$\theta_{12}, \theta_{13}, \Delta m_{21}^2, |\Delta m_{3\ell}^2|$

• θ_{23} : Least known angle

Maximal? Octant?

non-robust yet

• Ordering NO or IO?

CPV?:

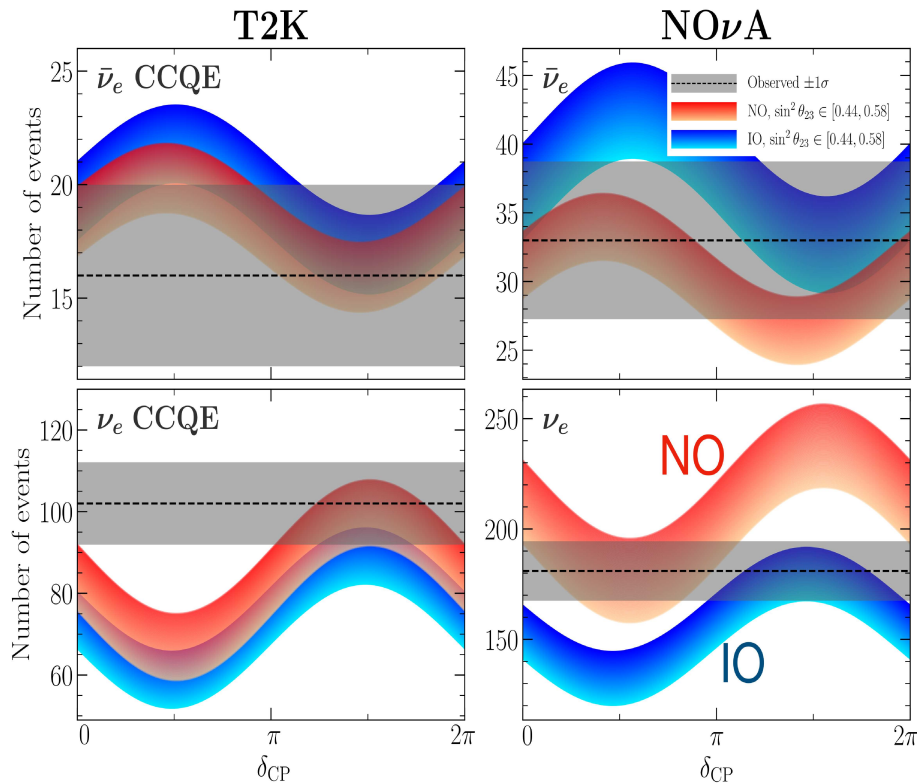
Mass Ordering (and CPV)

Concha Gonzalez-Garcia

- Dominant information in ν_e vs $\bar{\nu}_e$ appearance in LBL

$$P_{\mu e} \simeq s_{23}^2 \sin^2 2\theta_{13} \left(\frac{\Delta_{31}}{B_{\mp}} \right)^2 \sin^2 \left(\frac{B_{\mp} L}{2} \right) + \tilde{J} \frac{\Delta_{21}}{V_E} \frac{\Delta_{31}}{B_{\mp}} \sin \left(\frac{V_E L}{2} \right) \sin \left(\frac{B_{\mp} L}{2} \right) \cos \left(\frac{\Delta_{31} L}{2} \pm \delta_{CP} \right)$$

$$\Delta_{ij} = \frac{\Delta m_{ij}^2}{4E} \quad B_{\pm} = \Delta_{31} \pm V_E \quad \tilde{J} = c_{13} \sin^2 2\theta_{13} \sin^2 2\theta_{23} \sin^2 2\theta_{12}$$



$\Rightarrow$ Each T2K and NO ν A favour **NO**
 But some tension in value of δ_{CP} in **NO**

Mass Ordering (and CPV)

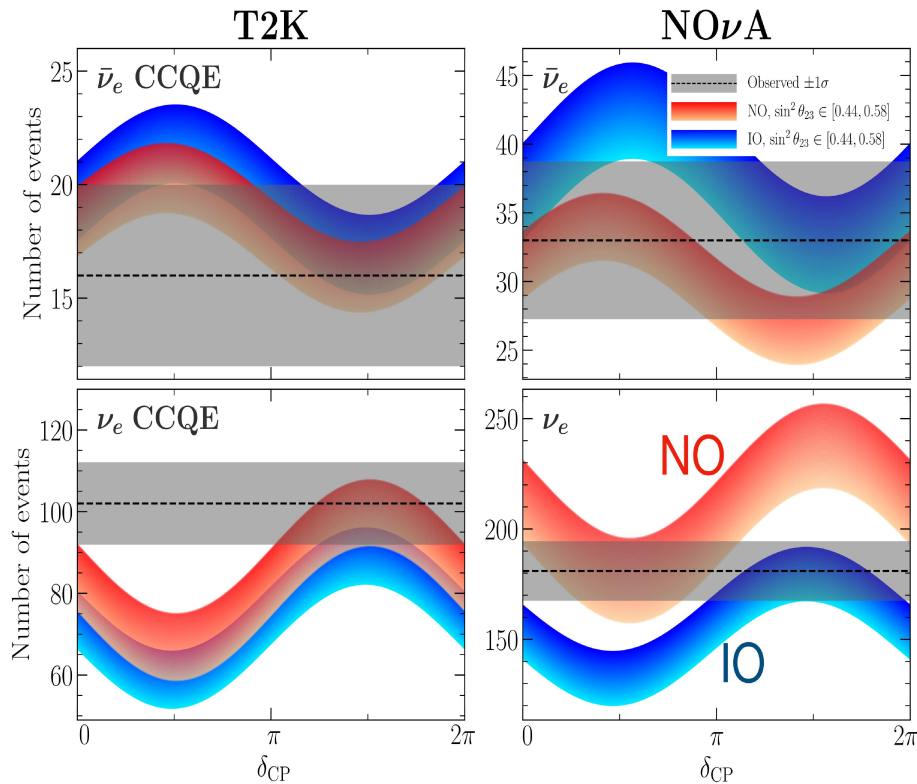
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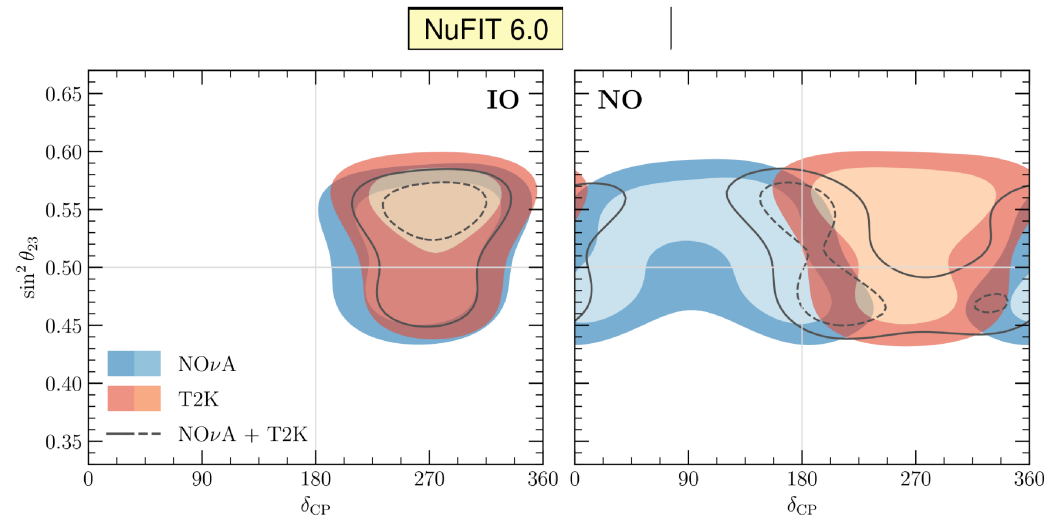
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$\Rightarrow$ **IO** best fit in LBL combination



$\Rightarrow$ Each T2K and NO ν A favour **NO**

But some tension in value of δ_{CP} in **NO**



Parameter goodness-of-fit (PG) test:

	normal ordering			inverted ordering		
	χ_{PG}^2/n	p-value	# σ	χ_{PG}^2/n	p-value	# σ
T2K vs NO ν A	7.9/3	0.047	2.0 σ	1.8/3	0.61	0.5 σ

No statistically significant incompatibility yet

- Dominant information in ν_e vs $\bar{\nu}_e$ appearance in LBL:

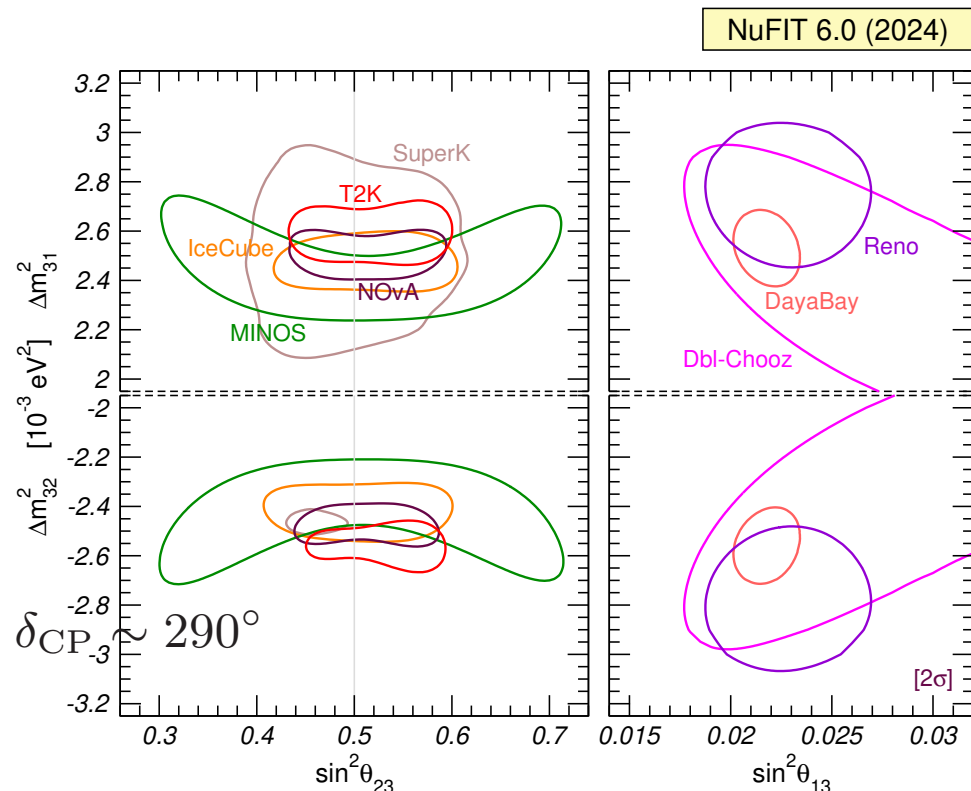
Each T2K and NO ν A favour **NO** but tension in value of δ_{CP} in **NO**

$\Rightarrow$ **IO** best fit in LBL combination $\Rightarrow$ b.f. $\delta_{CP} \sim 290^\circ$, CPC disfavoured at $\gtrsim 3.5\sigma$

- Additional information from ν_μ in LBL vs ν_e disappearance in MBL Reactors:

$$\Delta m_{\mu\mu}^2 \simeq \Delta m_{3l}^2 + \begin{matrix} c_{12}^2 \Delta m_{21}^2 & \text{NO} \\ s_{12}^2 \Delta m_{21}^2 & \text{IO} \end{matrix} + \dots$$

$$\Delta m_{ee}^2 \simeq \Delta m_{3l}^2 + \begin{matrix} s_{12}^2 \Delta m_{21}^2 & \text{NO} \\ c_{12}^2 \Delta m_{21}^2 & \text{IO} \end{matrix} \quad \text{Nunokawa, Parke, Zukanovich hep-ph/0503283}$$



$\Rightarrow$ Slightly better agreement in NO

$\Rightarrow$ LBL+Reac: NO and IO equally good

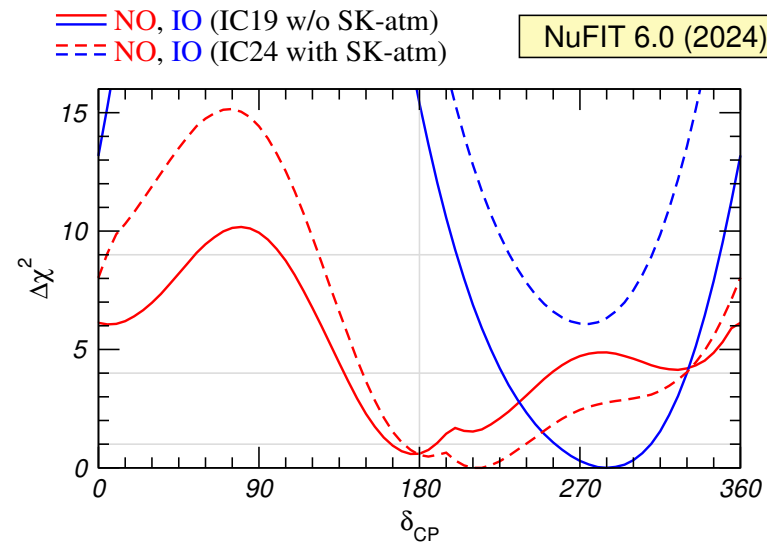
– NO: CPC $\delta_{CP} \sim 180^\circ$ allowed at $\lesssim 0.6\sigma$

– IO: CPC disfavoured at $\gtrsim 3.5\sigma$ b.f.

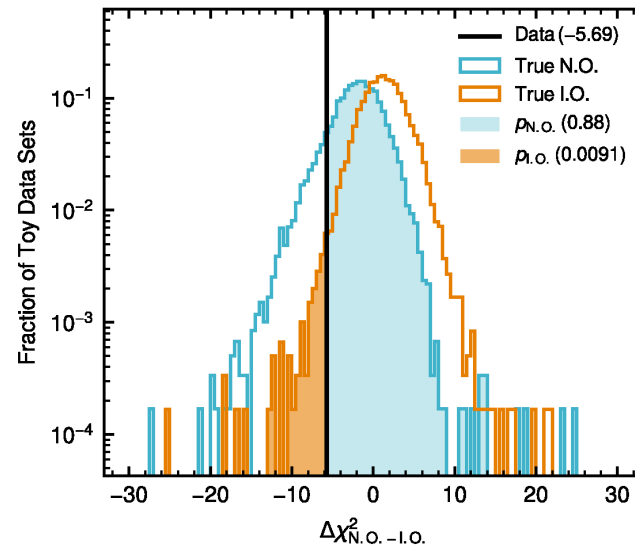
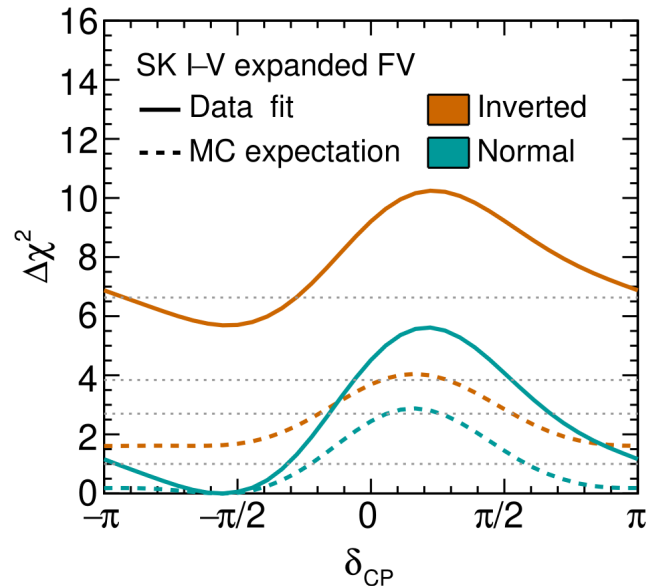
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 $\Rightarrow$ **IO** best fit in LBL combination $\Rightarrow$ b.f. $\delta_{CP} \sim 290^\circ$, CPC disfavoured at $\gtrsim 3.5\sigma$
- Additional information from ν_μ in LBL vs ν_e disappearance in MBL Reactors:
Slightly better agreement in **NO** $\Rightarrow$ LBL+Reac: **NO** and **IO** equally good $\Rightarrow$ **CPC OK**
- Additional information from SK-ATM $\Rightarrow$ favouring of **NO** $\Rightarrow$ **CPC** :
SK I-V 484 kton-years χ^2 table added $\Rightarrow \Delta\chi^2_{\text{IO-NO, with SK-atm}} \simeq 6$



- Dominant information in ν_e vs $\bar{\nu}_e$ appearance in LBL:
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SK I-V 484 kton-years χ^2 table added $\Rightarrow \Delta\chi^2_{\text{IO-NO, with SK-atm}} \simeq 6$
SK-atm result beyond expectation and not clearly compatible with any ordering



Flavour Parameters: leptons vs quarks

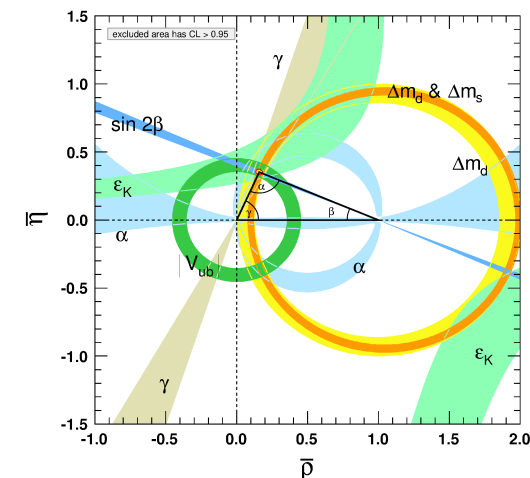
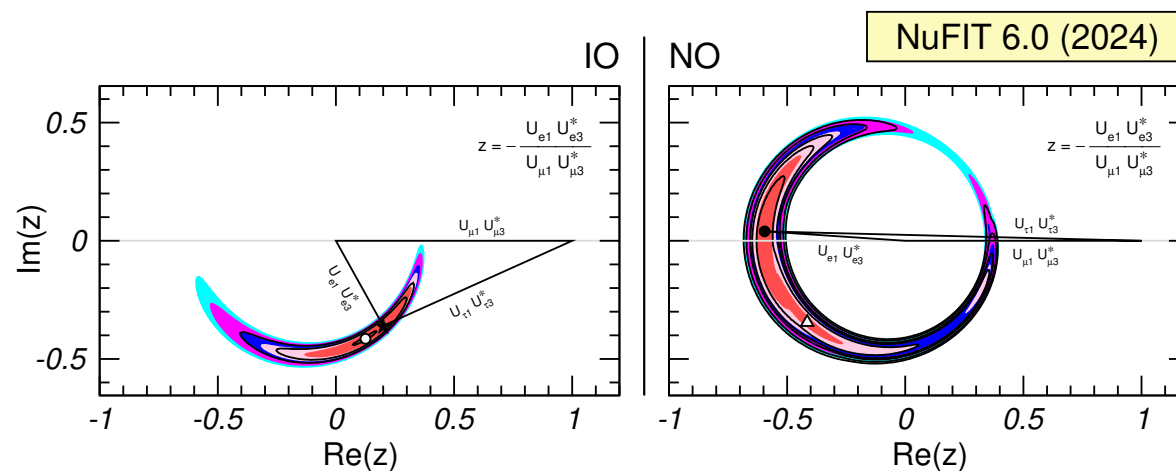
- Leptonic mixing matrix

$$|U|_{3\sigma} = \begin{pmatrix} 0.80 \rightarrow 0.85 & 0.51 \rightarrow 0.56 & 0.14 \rightarrow 0.16 \\ 0.23 \rightarrow 0.51 & 0.46 \rightarrow 0.69 & 0.63 \rightarrow 0.78 \\ 0.26 \rightarrow 0.53 & 0.47 \rightarrow 0.70 & 0.61 \rightarrow 0.76 \end{pmatrix}$$

- Very different and precision very far from:

$$|V|_{\text{CKM}} = \begin{pmatrix} 0.97427 \pm 0.00015 & 0.22534 \pm 0.0065 & (3.51 \pm 0.15) \times 10^{-3} \\ 0.2252 \pm 0.00065 & 0.97344 \pm 0.00016 & (41.2_{-5}^{+1.1}) \times 10^{-3} \\ (8.67_{-0.31}^{+0.29}) \times 10^{-3} & (40.4_{-0.5}^{+1.1}) \times 10^{-3} & 0.999146_{-0.000046}^{+0.000021} \end{pmatrix}$$

- CP violation



Early “Global Analysis”

- Barger, Whisnant, Cline, Phillips, PLB Jun 80

- De Rujula, Lusignoli, Maiani, Petcov, Petronzio, NPB May 80

Table 1
Experimental limits on neutrino oscillations and neutrino flux predictions

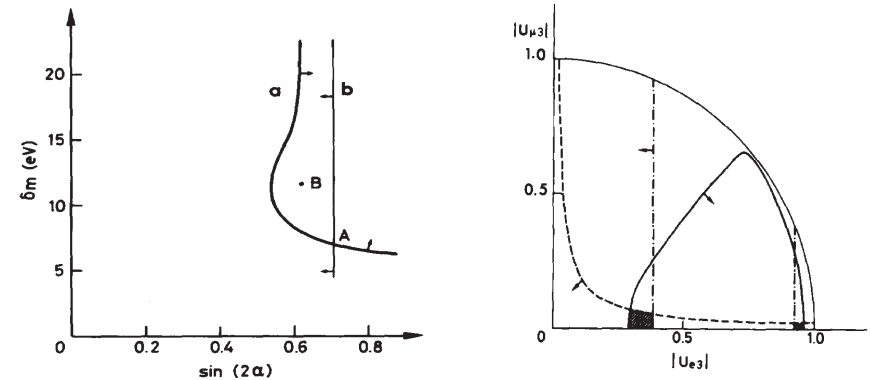
Observables	Source refs.	$\frac{L}{E} \text{ MeV}$	Present limit	Solution		
				A	B	C
$\langle P(\nu_e \rightarrow \nu_e) \rangle$	S [6]	10^{10}	$\geq 1/4, \lesssim 1/2$	0.41	0.33	0.41
$P(\bar{\nu}_e \rightarrow \bar{\nu}_e)$	R [3,4]	1-3	> 0.5	0.6-1.0	0.8-1.0	0.8 mean
	R a)	5-20		0.1-0.9	0.05-0.5	0.1-0.9
$P(\nu_e \rightarrow \nu_e)$	A	0.04	$> 0.85^e$	1.0	1.0	0.9
	M [12]	0.3	1.1 ± 0.4	0.95	1.0	0.8 mean
	M b)	1-3		0.6-1.0	0.8-1.0	0.8 mean
$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$	M [12]	0.3	< 0.04	10^{-4}	10^{-3}	10^{-3}
	M b)	3		0.03	0.11	0.03
$P(\nu_\mu \rightarrow \nu_e)/P(\nu_\mu \rightarrow \nu_\mu)$	A [10,11]	0.04	$< 10^{-3}$	10^{-6}	10^{-5}	10^{-4}
	A [18] c)	1-7		0-0.2	0-0.8	0-0.2
$P(\nu_e \rightarrow \nu_\tau)$	A d)	0.04	$< 0.2^e$	10^{-3}	10^{-5}	0.1
$P(\nu_\mu \rightarrow \nu_\tau)/P(\nu_\mu \rightarrow \nu_\mu)$	A [13]	0.04	$< 2.5 \times 10^{-2}$	10^{-5}	10^{-5}	10^{-3}
$\langle P(\nu_\mu \rightarrow \nu_\mu) \rangle$	D f)	10^2-10^3	~ 0.5	0.51	0.51	0.51
$\langle P(\nu_e \rightarrow \nu_\mu) \rangle$	D g)	10^3-10^5		0.48	0.44	0.48
$\langle P(\nu_e \rightarrow \nu_e) \rangle$	D g)	10^3-10^5		0.42	0.33	0.42
$P(\nu_e \rightarrow \nu_\mu)$	D g)	$10-10^2$		0.3-0.7	0.3-0.7	0.3-0.7
$P(\nu_e \rightarrow \nu_e)$	D g)	$10-10^2$		0.2-0.6	0.2-0.6	0.2-0.6

accommodates all known constraints is

δm_{13}^2	δm_{12}^2	θ_1	θ_2	θ_3	δ
Solution A: 1.0 eV^2 0.05 eV^2 45° 25° 30° 0° .					
Solution B: 0.15 eV^2 0.05 eV^2 55° 0° 45° 0°					
Solution C: 10 eV^2 0.05 eV^2 45° 25° 30° 0° .					

KM-like mixing convention

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} c_1 & s_1 c_3 & s_1 s_3 \\ -s_1 c_2 & c_1 c_2 c_3 + s_2 s_3 e^{i\delta} & c_1 c_2 s_3 - s_2 c_3 e^{i\delta} \\ -s_1 s_2 & c_1 s_2 c_3 - c_2 s_3 e^{i\delta} & c_1 s_2 s_3 + c_2 c_3 e^{i\delta} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix},$$



$$U = \begin{pmatrix} 0.65 & 0.65 & -0.38 \\ [-0.71 e^{i\delta} \mp |< 0.021|] & [0.71 e^{i\delta} \mp |< 0.02|] & \mp |< 0.06| \\ [0.27 \mp e^{i\delta} |< 0.04|] & [0.27 \pm e^{i\delta} |< 0.04|] & 0.92 \end{pmatrix}, \quad (6.2)$$

with mass differences in the ranges

$$10^{-5} \text{ eV} \lesssim \sqrt{|m_1^2 - m_2^2|} \lesssim 1 \text{ eV},$$

$$\sqrt{|m_3^2 - m_1^2|} \sim 10 \text{ eV}.$$

Early Reactor $\mathcal{O}(eV)$ “hints”

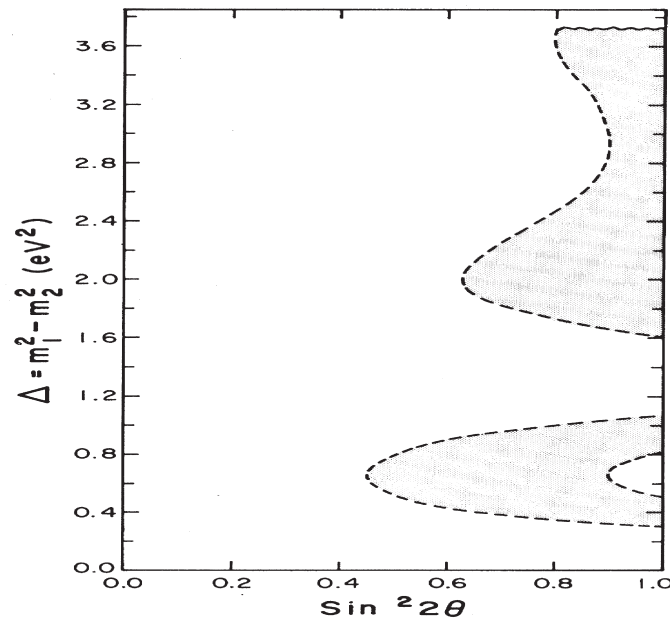
Concha Gonzalez-Garcia
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- Data from Savannah River Plant

Nezrick and Reines, PR Feb 66 $L=6$ m

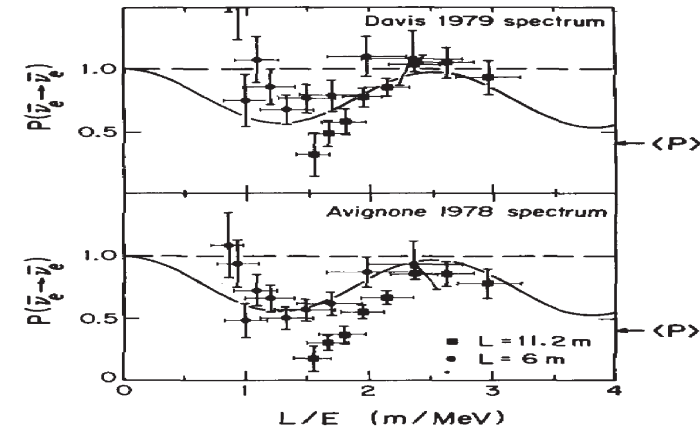
$$\frac{\bar{\sigma}_{\text{exp}}}{\bar{\sigma}_{\text{th}}} = 0.88 \pm 0.13$$

Reines, Sobel, Pasierb PRL Oct 80 $L=11.2$ m



- Early Pheno Analysis

Barger, Whisnant, Cline, Phillips, PLB Jun 80



- Even Flux Independent Analysis !!!

Silverman and Soni, PRL Feb 81

