

Theories of Neutrino Masses and Dark Matter

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Minimal Gauged $U(1)_{B-L}$ Model with Spontaneous R Parity Violation

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We study the minimal gauged $U(1)_{B-L}$ supersymmetric model and show that it provides an attractive theory for spontaneous R -parity violation. Both $U(1)_{B-L}$ and R parity are broken by the vacuum expectation value of the right-handed sneutrino (proportional to the soft supersymmetry masses), thereby linking the $B - L$ and soft SUSY scales. In this context we find a consistent mechanism for generating neutrino masses and a realistic mass spectrum, all in a supersymmetry standard model. We discuss the most general Z' gauge boson and R -parity violation.

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Three layers of neutrinos

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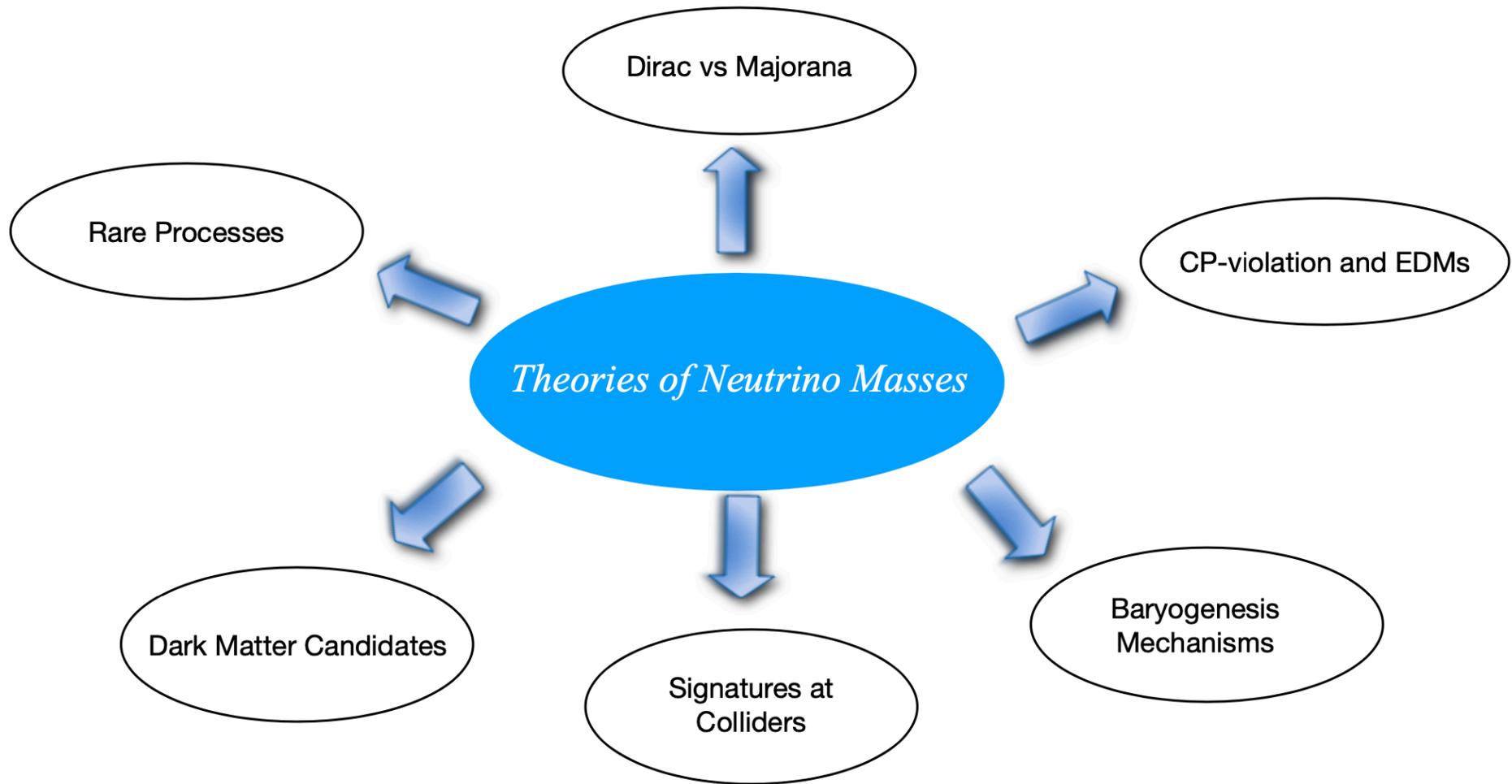
Abstract

In this Letter we point out that in a class of models for spontaneous R -parity breaking based on gauged $B - L$, the spectrum for neutrinos is quite peculiar. We find that those models generally predict three layers of neutrinos: one heavy sterile neutrino, two massive active neutrinos, and three nearly massless (one active and two sterile) neutrinos.

References

- *P. F. P.*, *Physical Review D* 110, 035018 (2024)
- H. Debnath, *P. F. P.*, *Physical Review D* 111, 075020 (2025)
- J. Butterworth, H. Debnath, J. Egan, *P. F. P.*, [arXiv:2505.06341](https://arxiv.org/abs/2505.06341)
- *P. F. P.*, M. B. Wise, *PRL and Phys.Rev.D* 88, 057703

Main Goal



Massive Neutrinos

- Majorana Fermions *(Lepton Number is broken by two units)*

$$\mathcal{L} \supset \frac{1}{2} \bar{\nu}_L^T C M_M \nu_L$$

- Dirac Fermions *(Lepton Number is conserved or broken but not effective Majorana masses)*

$$\mathcal{L} \supset M_D \bar{\nu}_L \nu_R$$

Majorana Neutrino Masses

$$\int \mathcal{L} \supset \frac{1}{2} \bar{\nu}_L^T C M_M \nu_L$$

Mechanisms:

- Type I Seesaw
- Type II Seesaw
- Type III Seesaw
- Zee's Model
- Colored Seesaw
- Witten's Model

...

...

Theories:

- B-L
- Left-Right Symmetry
- **Pati-Salam**
- GUTs
-

Canonical Seesaw

$$-\mathcal{L}_\nu = Y_\nu \bar{\ell}_L i\sigma_2 H^* \nu_R + \frac{1}{2} M_R \nu_R^T C \nu_R + h.c.$$



$$M_\nu = m_D M_R^{-1} m_D^T$$

if $m_D \sim 10^2$ GeV



$$M_R \lesssim 10^{14-15} \text{ GeV}$$

(Seesaw Scale)

What is the Seesaw Scale ?

Neutrino Masses:
“Standard Paradigm”

Quark-Lepton Unification

$$SU(4)_C \otimes SU(2)_L \otimes SU(2)_R \supset SO(10)$$

$$\begin{pmatrix} u_r & u_g & u_b & \nu \\ d_r & d_g & d_b & e \end{pmatrix}_L \quad \begin{pmatrix} u_r & u_g & u_b & N \\ d_r & d_g & d_b & e \end{pmatrix}_R$$



$$M_\nu = m_D^\nu M_R^{-1} (m_D^\nu)^T$$

$$m_D^\nu = m_U$$

$$M_R \lesssim 10^{14-15} \text{ GeV}$$

High Scale Seesaw

Low Scale Quark-Lepton Unification

$$SU(4)_C \otimes SU(2)_L \otimes U(1)_R$$

$$F_{QL} = \begin{pmatrix} u_r & u_g & u_b & \nu \\ d_r & d_g & d_b & e \end{pmatrix} \sim (\mathbf{4}, \mathbf{2}, 0),$$

$$F_u = (u_r^c \ u_g^c \ u_b^c \ \nu^c) \sim (\bar{\mathbf{4}}, \mathbf{1}, -1/2),$$

$$F_d = (d_r^c \ d_g^c \ d_b^c \ e^c) \sim (\bar{\mathbf{4}}, \mathbf{1}, 1/2).$$

Neutrino Masses

$$-\mathcal{L} \supset Y_5 F_u \chi S + \frac{1}{2} \mu S S + \text{h.c.},$$

$$S \sim (1, 1, 0)$$

$$\chi \sim (4, 1, 1/2)$$

$$(\nu \quad \nu^c \quad S) \begin{pmatrix} 0 & M_\nu^D & 0 \\ (M_\nu^D)^T & 0 & M_\chi^D \\ 0 & (M_\chi^D)^T & \mu \end{pmatrix} \begin{pmatrix} \nu \\ \nu^c \\ S \end{pmatrix},$$

Inverse Seesaw

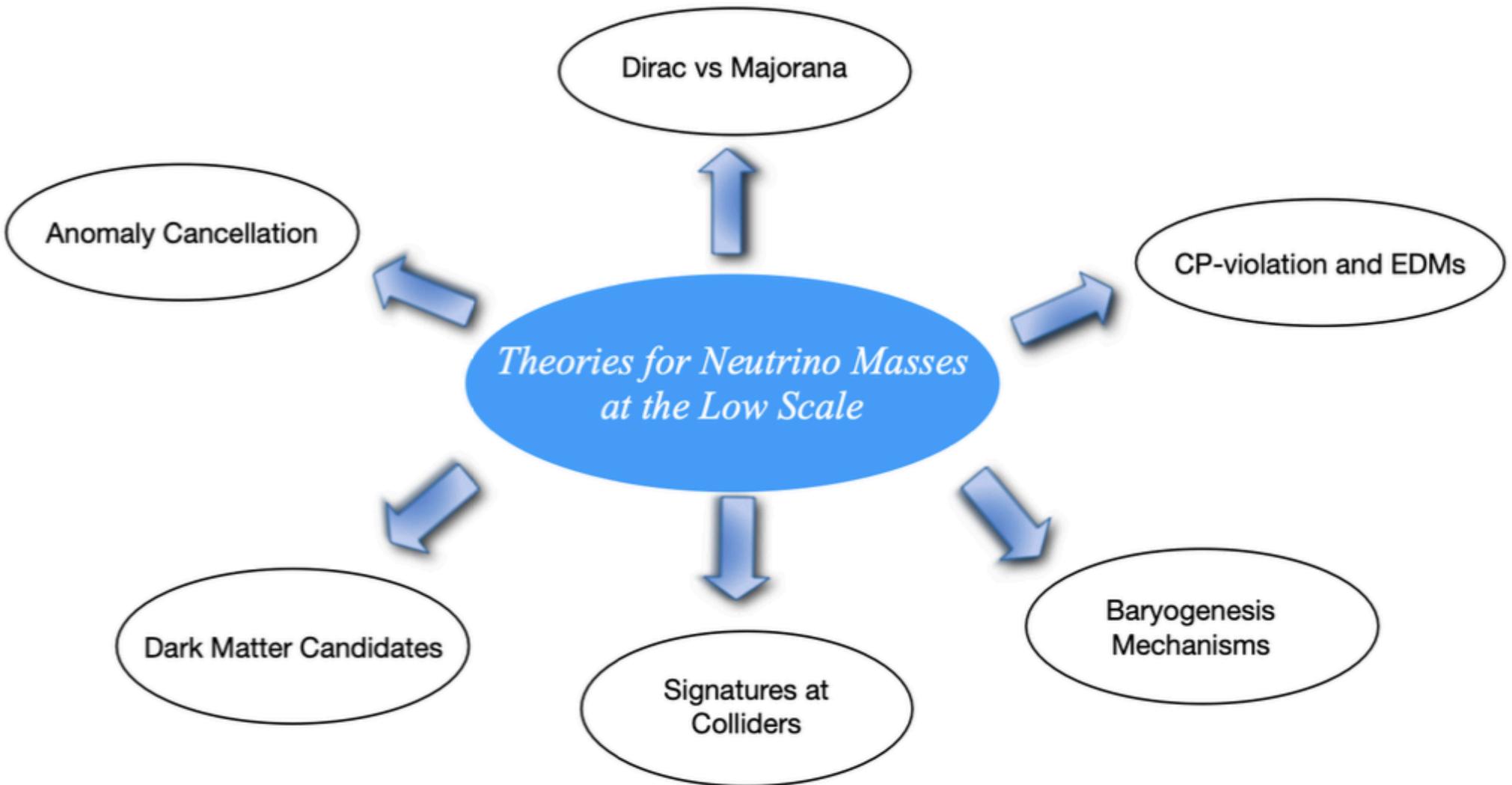


$$m_\nu \approx \mu \left(\frac{M_\nu^D}{M_\chi^D} \right)^2, \quad M_\chi^D \gg M_\nu^D \gg \mu,$$

$$M_{QL} \geq 10^3 \text{ TeV} \quad (K_L^0 \rightarrow e^\pm \mu^\mp)$$

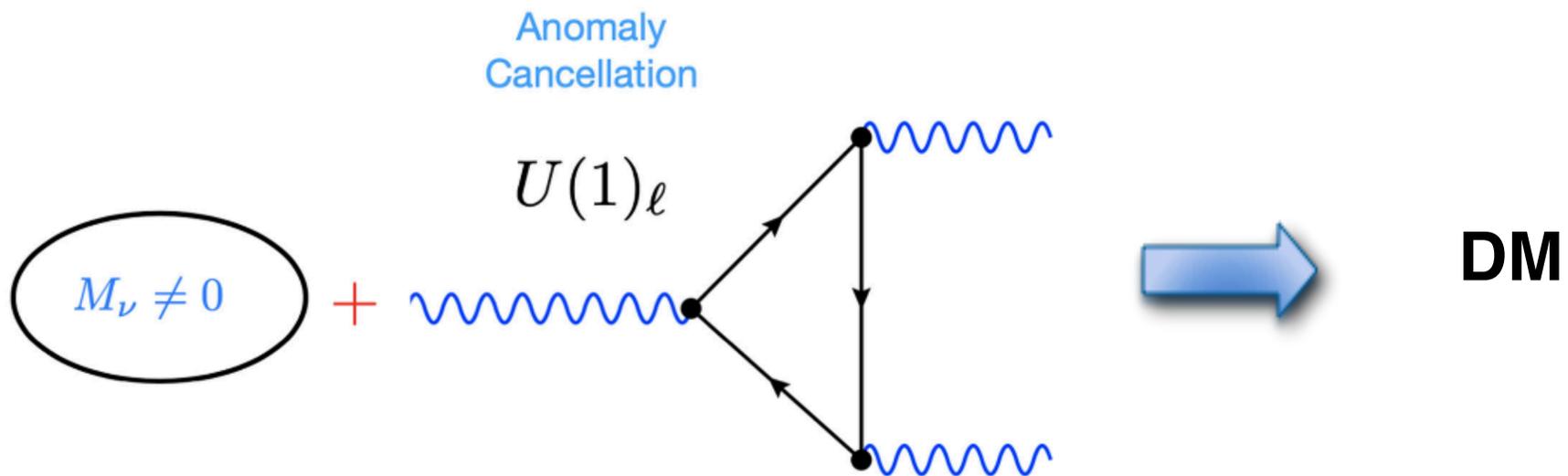
See also: [2308.07367](#), [2205.02235](#), [2203.07381](#), [2107.06895](#), [2104.11229](#)

Main Goal



*Theory of Neutrino Masses
at the Low Scale*

Lepton Number as Local Gauge Symmetry



$$\Omega_{DM} h^2 \leq 0.12$$



Low Scale Theory

Lepton Number as Local Gauge Symmetry

Anomaly Cancellation:

$$\ell_L \sim (\mathbf{2}, -1/2, 1) \quad \text{and} \quad e_R \sim (\mathbf{1}, -1, 1),$$

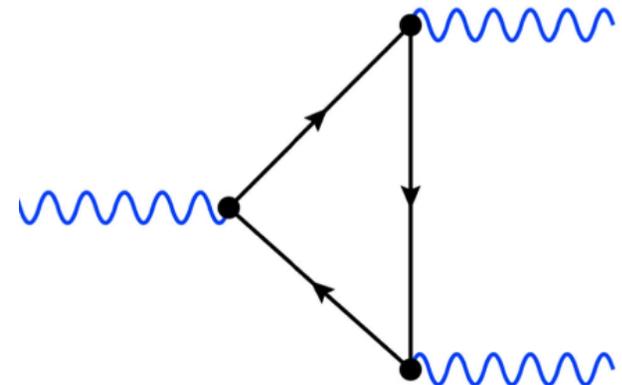
$$\mathcal{A}_1(SU(3)_C^2 U(1)_\ell) = 0,$$

$$\mathcal{A}_2(SU(2)_L^2 U(1)_\ell) = 3/2,$$

$$\mathcal{A}_3(U(1)_Y^2 U(1)_\ell) = -3/2,$$

$$\mathcal{A}_4(U(1)_Y U(1)_\ell^2) = 0,$$

$$\mathcal{A}_5(U(1)_\ell^3) = 3, \quad \text{and} \quad \mathcal{A}_6(U(1)_\ell) = 3.$$



Solutions:

- *Minimal Model*

P. F. P., Physical Review D 110, 035018 (2024)

- *Four representations*

P. F. P., S. Ohmer, H. H. Patel, Phys. Lett. B735, 283

- *Vector-like leptons*

P. F. P., M. B. Wise, JHEP1108, 068

M. Duerr, P. F. P., M. B. Wise, Phys. Rev. Lett. 110, 231801

Minimal Model

$$SU(3)_C \otimes SU(2)_L \otimes U(1)_Y \otimes U(1)_e.$$

$$\Psi_L \sim (\mathbf{1}, \mathbf{1}, -1, 3/4), \quad \Psi_R \sim (\mathbf{1}, \mathbf{1}, -1, -3/4),$$

$$\chi_L \sim (\mathbf{1}, \mathbf{1}, 0, 3/4), \quad \text{and} \quad \rho_L \sim (\mathbf{1}, \mathbf{3}, 0, -3/4).$$

$$\nu_R^i \sim (\mathbf{1}, \mathbf{1}, 0, 1),$$

Minimal number of fields to cancel all leptonic gauge anomalies

New Fermion Masses

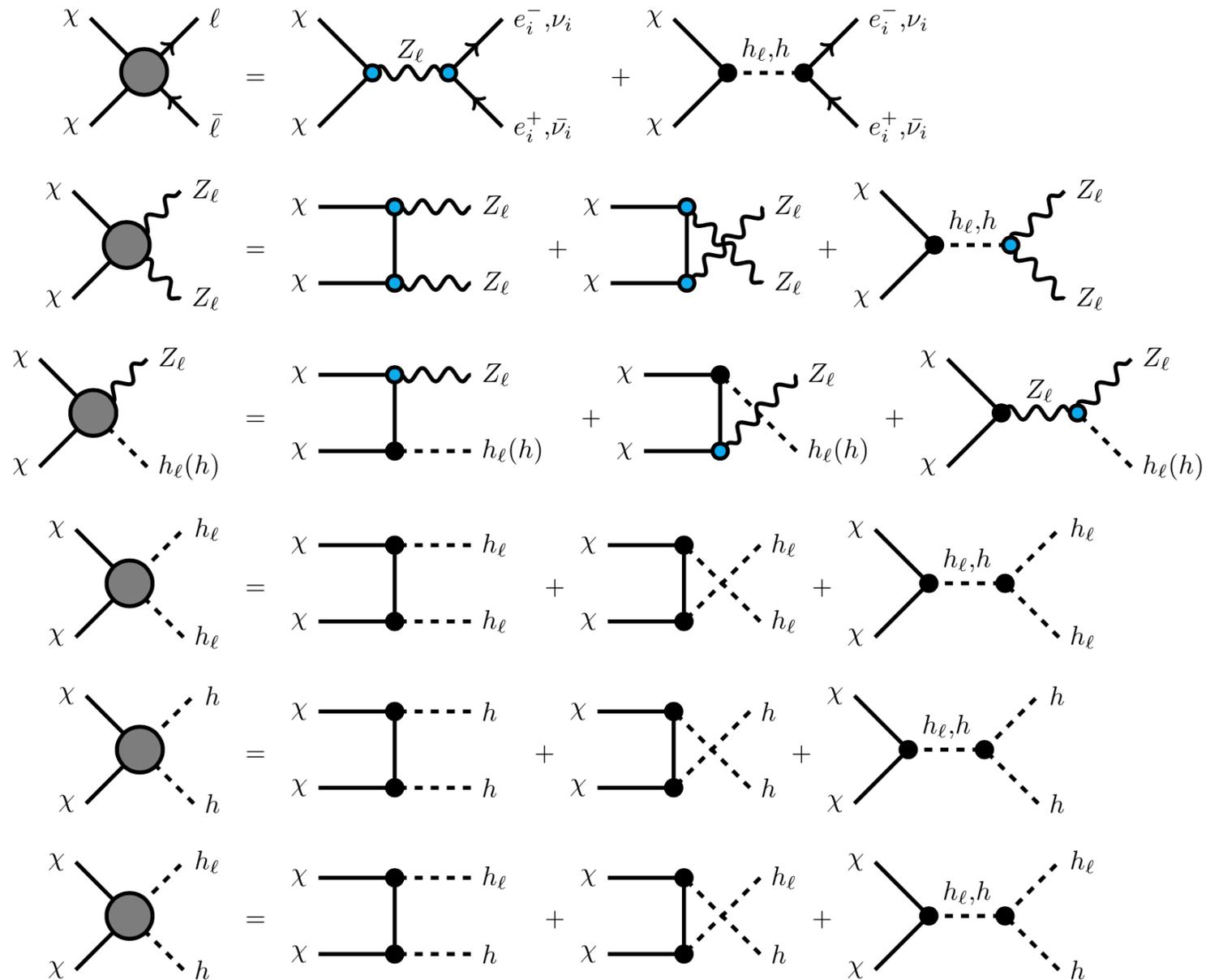
$$\rightarrow -\mathcal{L} \supset \lambda_\rho \text{Tr}(\rho_L^T C \rho_L) S + \lambda_\Psi \bar{\Psi}_L \Psi_R S + \lambda_\chi \chi_L^T C \chi_L S^* + \text{H.c.},$$

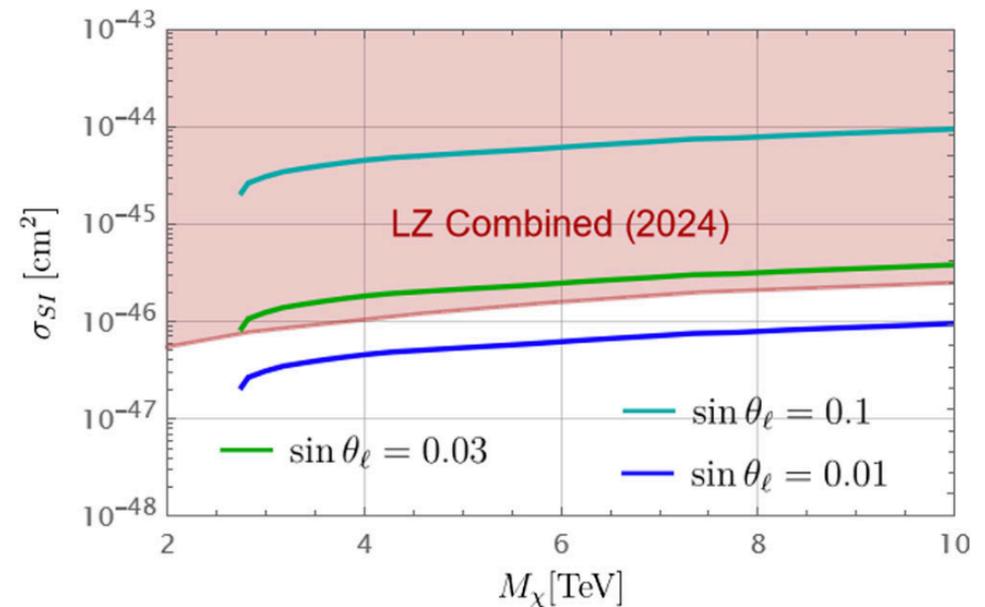
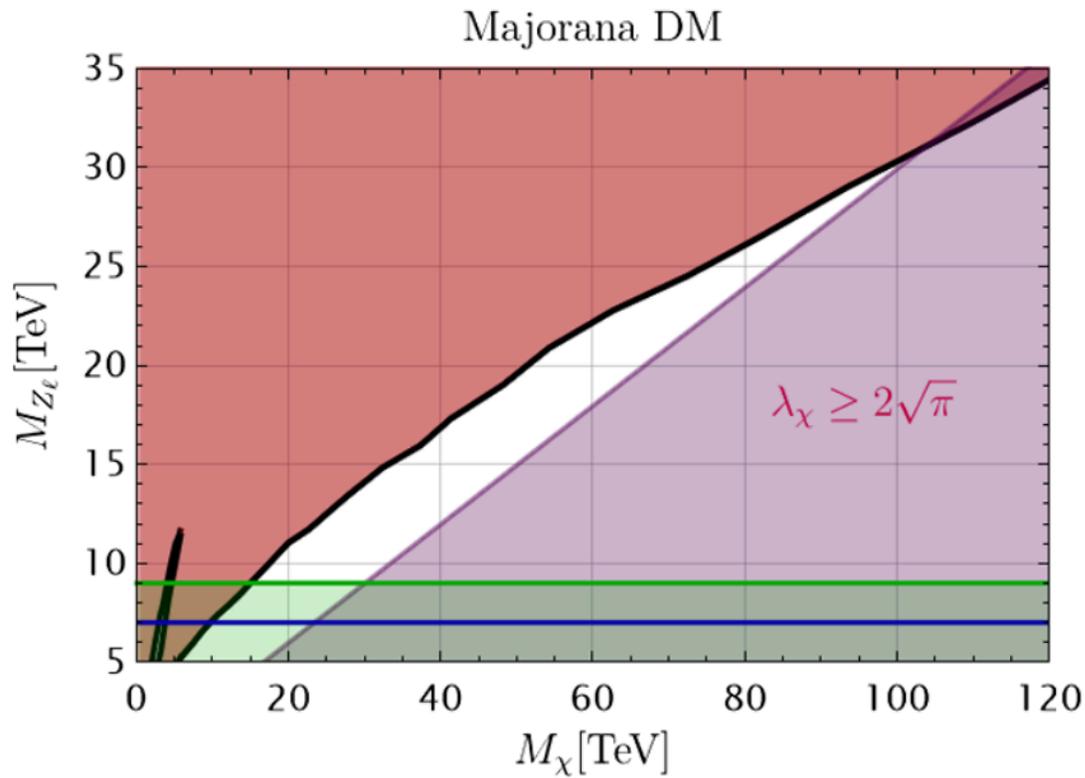
where $S \sim (1, 1, 0, 3/2)$.

$$\rightarrow -\mathcal{L} \supset Y_\nu \bar{\ell}_L i\sigma_2 H^* \nu_R + y_e \bar{\ell}_L H e_R + \text{H.c.}$$

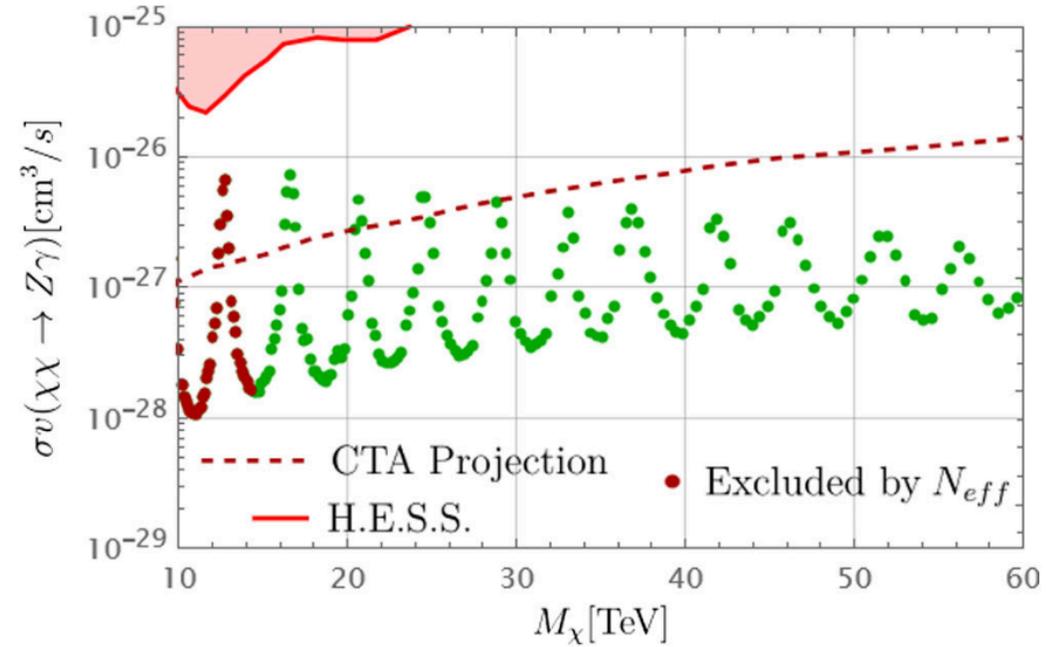
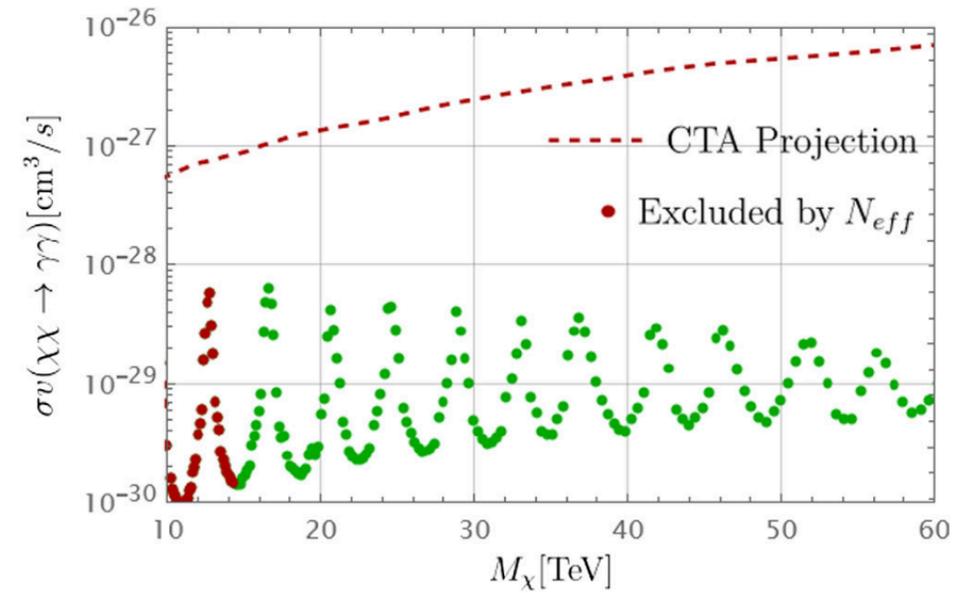
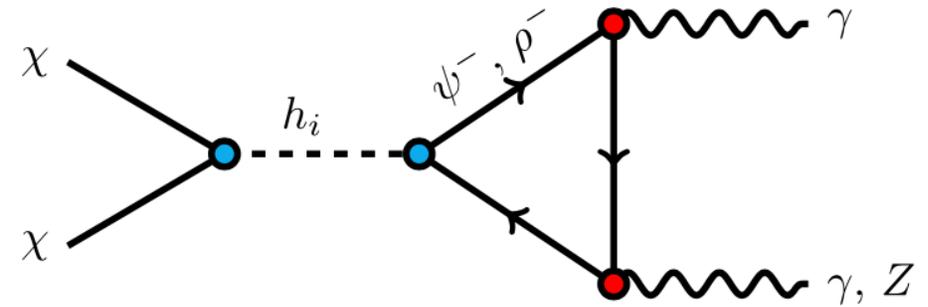
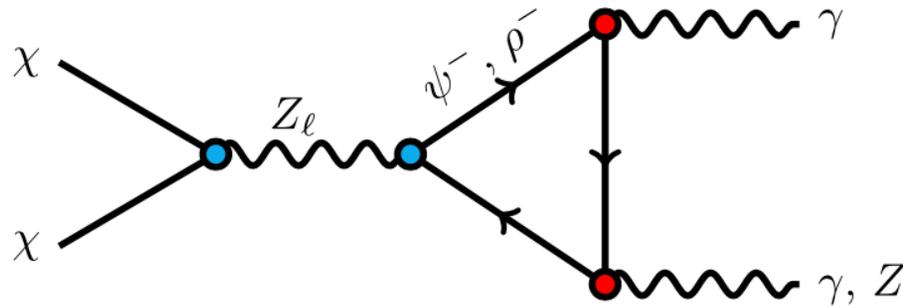
$$\mathcal{Z}_2: \Psi_L \rightarrow -\Psi_L, \quad \Psi_R \rightarrow -\Psi_R, \quad \rho_L \rightarrow -\rho_L, \quad \chi_L \rightarrow -\chi_L$$

Relic Density

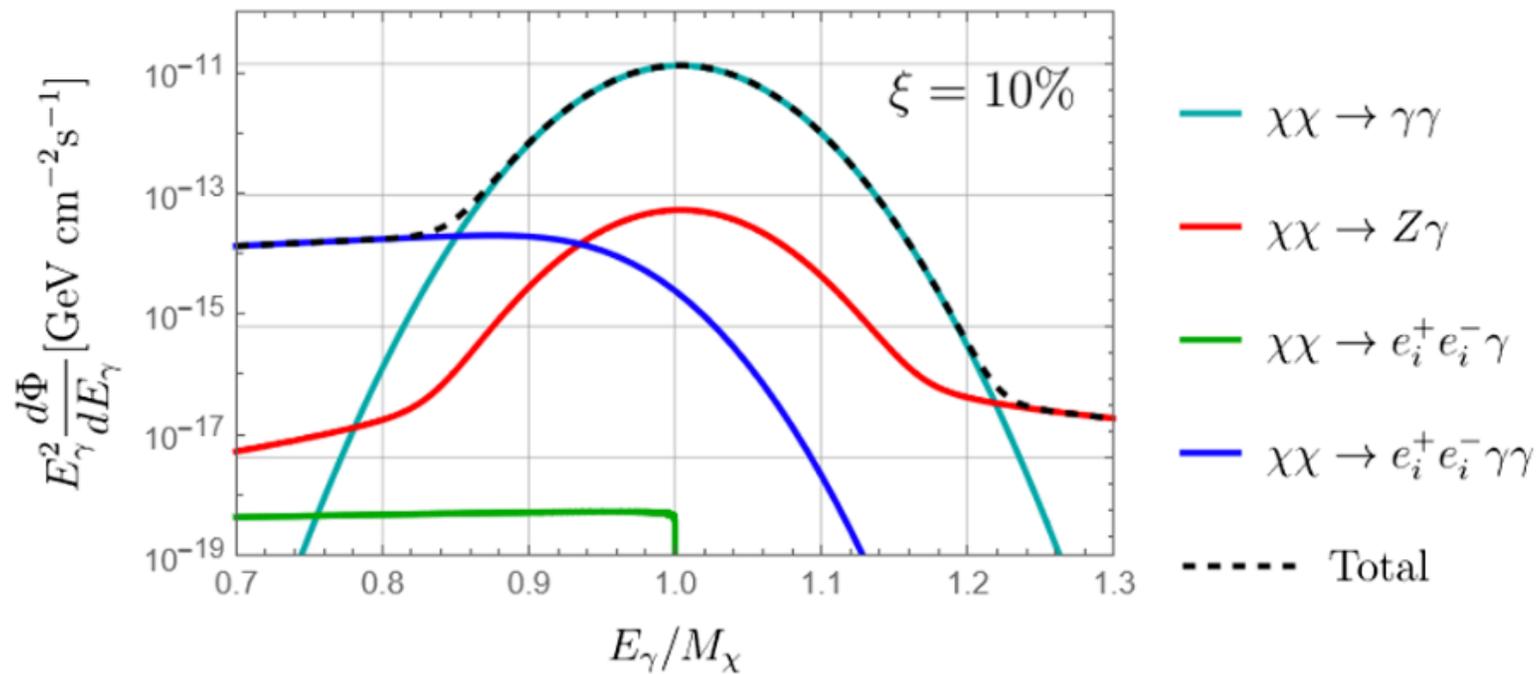




Indirect Detection



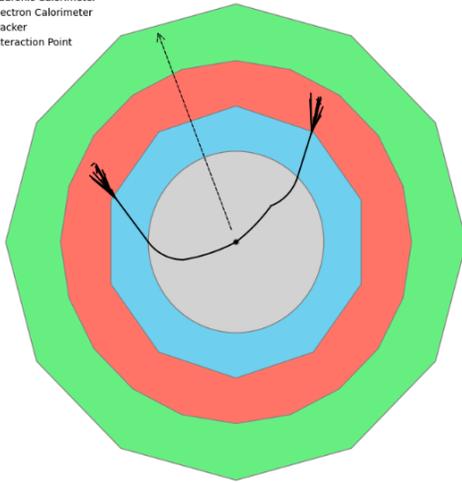
$$\begin{aligned} \frac{d\Phi_{\gamma\gamma}}{dE_\gamma} &= \frac{n_\gamma}{8\pi M_\chi^2} \frac{d(\sigma v_{\text{rel}}(\chi\chi \rightarrow \gamma\gamma))}{dE_\gamma} J_{\text{ann}} \\ &= \frac{n_\gamma(\sigma v_{\text{rel}}(\chi\chi \rightarrow \gamma\gamma))}{8\pi M_\chi^2} \frac{dN_{\gamma\gamma}}{dE_\gamma} J_{\text{ann}}. \end{aligned}$$



Collider Signatures

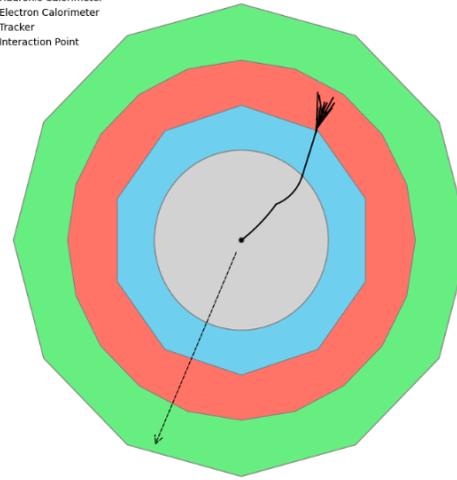
J. Butterworth, H. Debnath, J. Egan, [P. F. P.](#), [arXiv:2505.06341](#)

- Muon Spectrometer
- Hadronic Calorimeter
- Electron Calorimeter
- Tracker
- Interaction Point



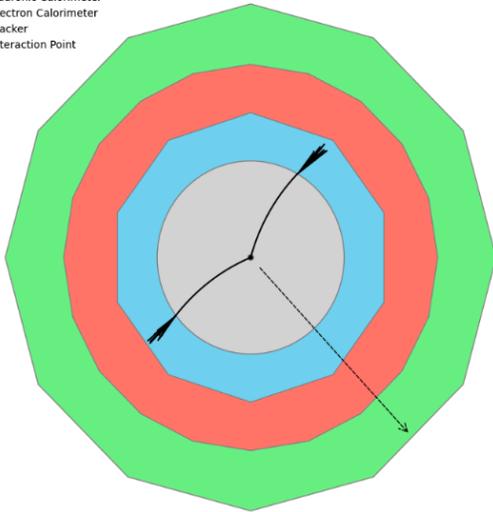
$$pp \rightarrow \rho^+ \rho^- \rightarrow \rho^0 \rho^0 \pi^+ \pi^-$$

- Muon Spectrometer
- Hadronic Calorimeter
- Electron Calorimeter
- Tracker
- Interaction Point



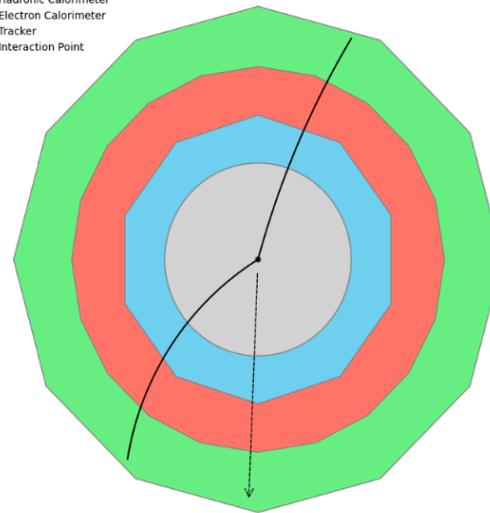
$$pp \rightarrow \rho^\pm \rho^0 \rightarrow \rho^0 \rho^0 \pi^\pm$$

- Muon Spectrometer
- Hadronic Calorimeter
- Electron Calorimeter
- Tracker
- Interaction Point



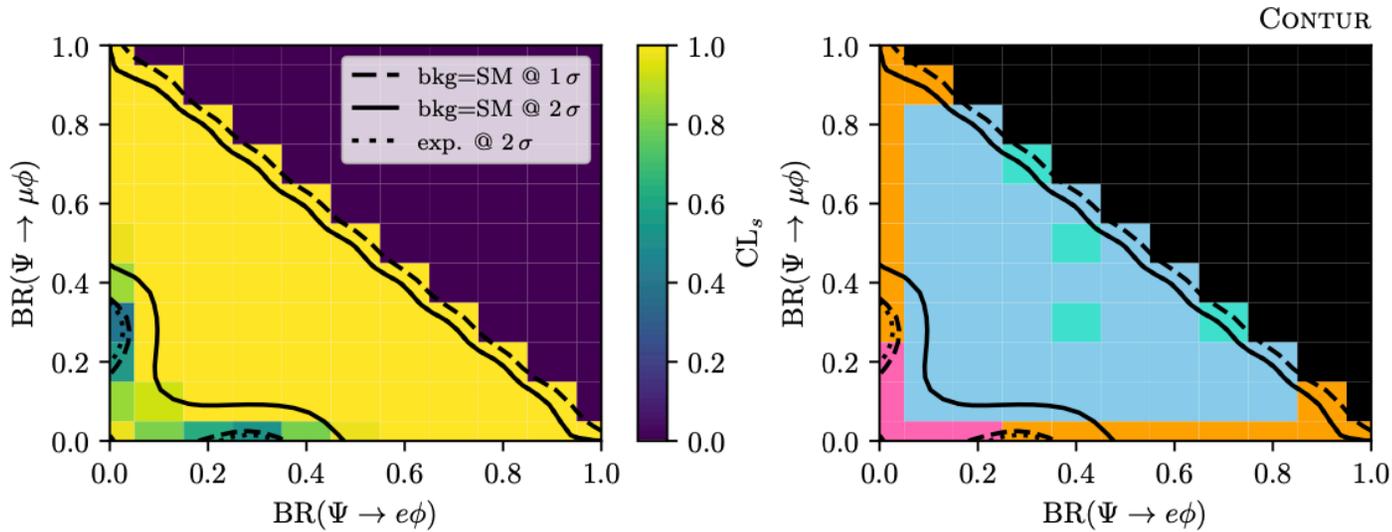
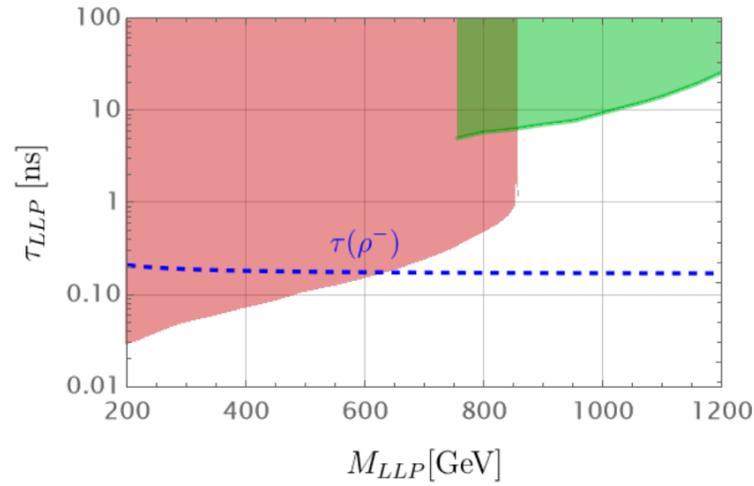
$$pp \rightarrow e^+ e^- E_T^{miss}$$

- Muon Spectrometer
- Hadronic Calorimeter
- Electron Calorimeter
- Tracker
- Interaction Point



$$pp \rightarrow \mu^+ \mu^- E_T^{miss}$$

Collider Signatures



$l^+l^- + \text{jet}$ [44]

$l_1l_2 + p_T^{\text{miss}}$ [45]

$l_1l_2 + p_T^{\text{miss}} + \text{jet}$ [46]

$\tau^+\tau^-$ [47]

Majorana Neutrinos

$$-\mathcal{L} \supset Y_\nu \bar{\ell}_L i\sigma_2 H^* \nu_R + \lambda_R \nu_R^T C \nu_R \phi + \text{H.c.}$$

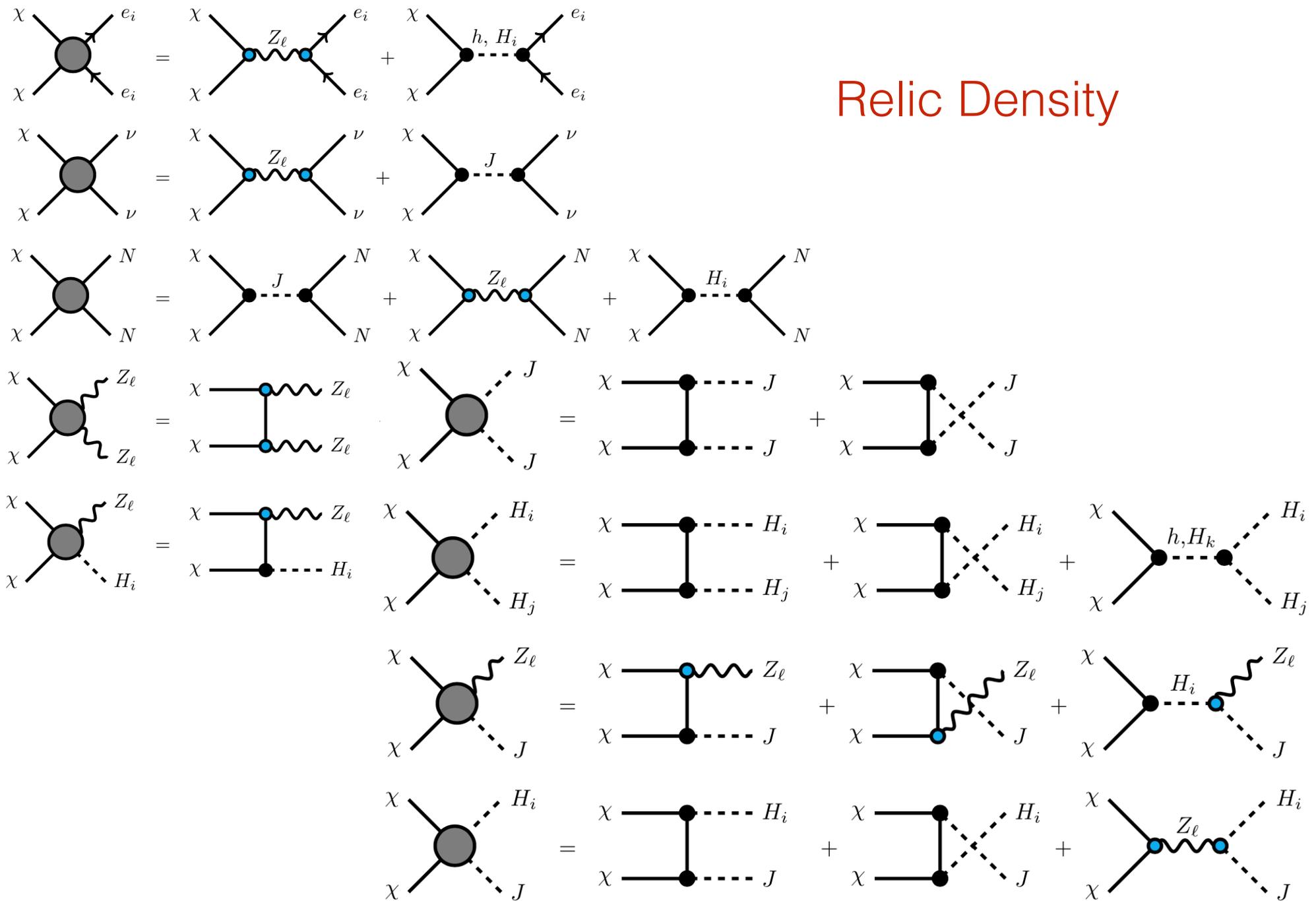


$$M_\nu = \frac{v_0^2}{2} Y_\nu M_N^{-1} Y_\nu^T,$$

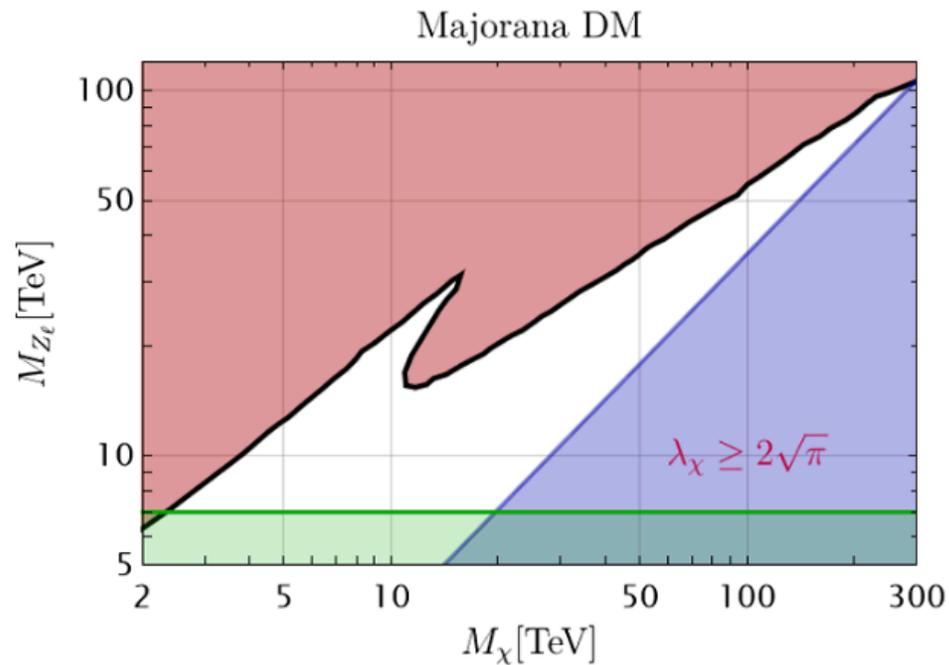


$$M_N = \sqrt{2} \lambda_R v_\phi = \frac{\lambda_R}{\sqrt{2}} \frac{M_{Z_\ell}}{g_\ell} \sin \beta.$$

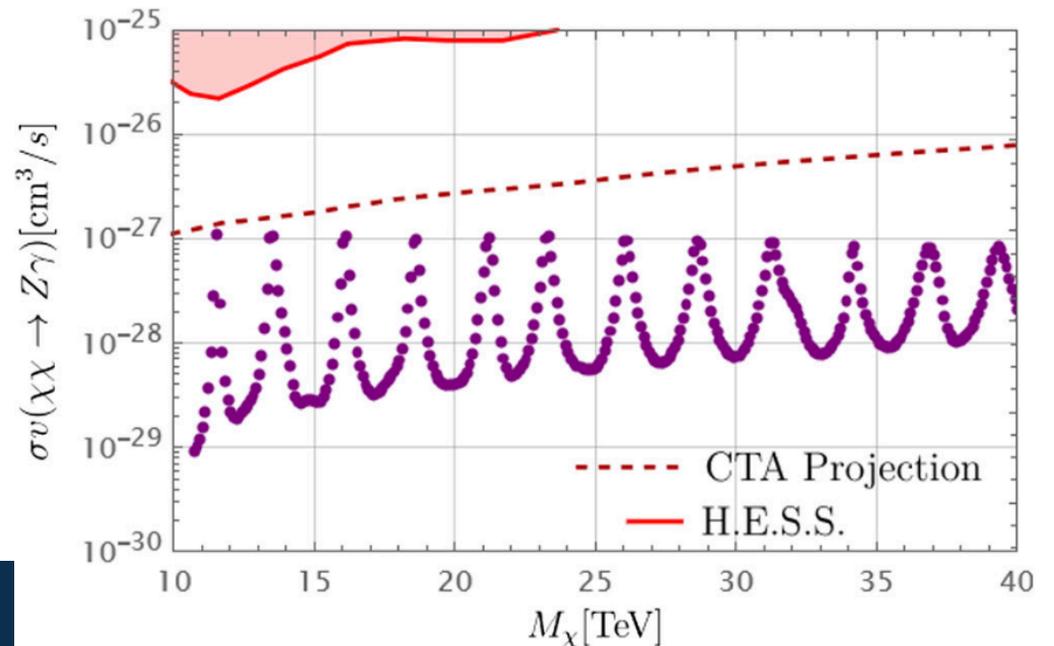
Relic Density



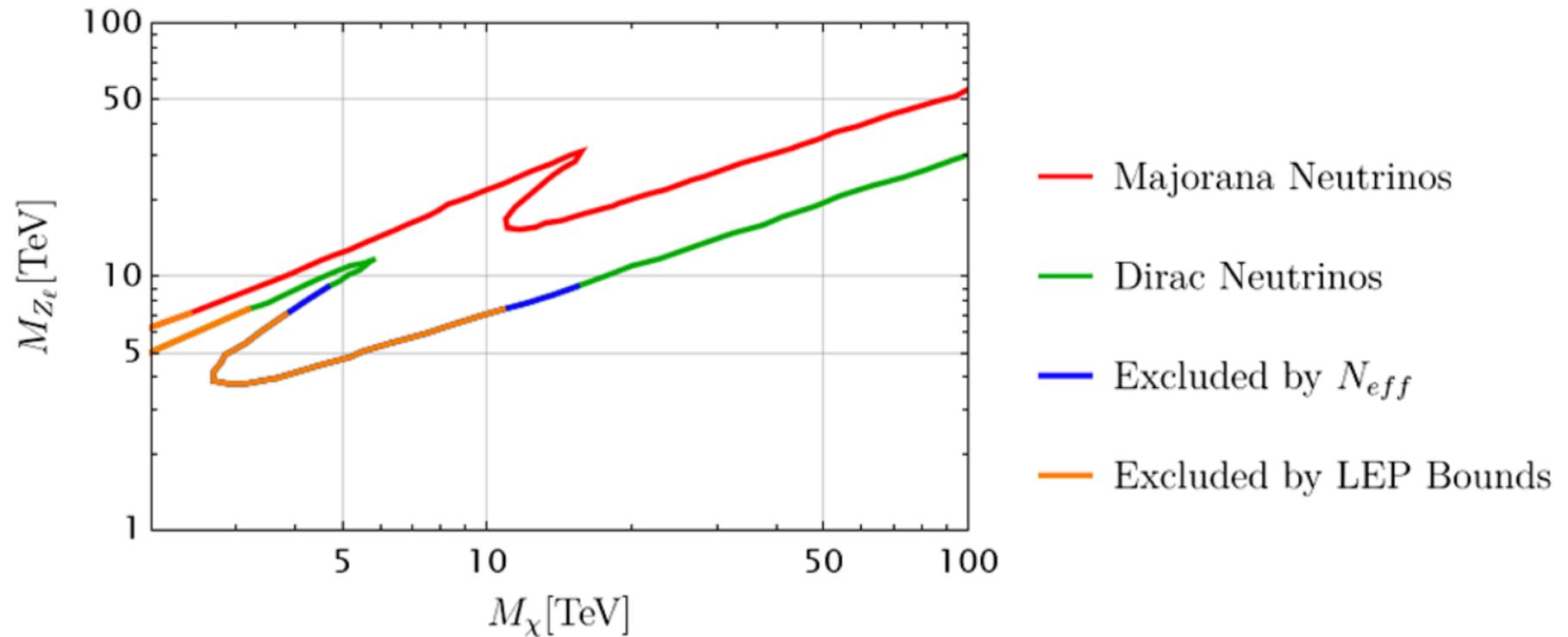
Majorana Neutrinos



- $g_\ell = 1$
- $\Omega_{DM} h^2 = 0.12$
- $\Omega_\chi h^2 > \Omega_{DM} h^2$
- $\lambda_\chi \geq 2\sqrt{\pi}$
- LEP Bound



Symmetry Breaking Scale: Dirac vs. Majorana



Summary

