# The electron's EDM in the decoupling limit of the aligned 2HDM

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#### CP violation (CPV)

• <u>Small set of parameters in</u> <u>the SM</u>: the SU(3)<sub>QCD</sub> phase (probed by nEDM), and one CPV phase in the Cabibbo-Kobayashi-Maskawa matrix



- Sakharov conditions: CPV is a required ingredient in order to generate dynamically the matter/anti-matter asymmetry of the visible Universe
- Many extensions of the SM introduce new sources of CPV, challenging this minimal picture

## Electric Dipole Moments (EDMs)

- EDMs probe CPV in the SM and beyond, both <u>gauge and matter</u> <u>field content and properties</u>
- Experimental accuracies are very high & SM contributions are highly suppressed (EDMs require at least three loops):

constrain New Physics (NP)

• Focus here on the **electron's** EDM: simpler description compared to the **neutron's** EDM, e.g., due to nonperturbative QCD dynamics



[from 1901.09966]

[Reviews: Pospelov, Ritz '05, Engel, Ramsey-M., van Kolck '13]

### Two Higgs Doublet Models (2HDMs)

would-be Goldstone bosons

• Two weak-isospin doublets  
with the same hypercharge;  
among the simplest extensions  
of the SM  
• 
$$\Phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2} \ G^+ \\ S_1 + v + i \ G^0 \end{pmatrix}$$
,  $\Phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2} \ H^+ \\ S_2 + i \ S_3 \end{pmatrix}$   
in the "Higgs basis"  
SU(2)xU(1)

- Scalar degrees of freedom: two CP-even scalars and one CP-odd pseudoscalar in total, plus +/- charged scalars; can play an important role in micro to macroscopic problems
- Rich phenomenology to be tested: EW physics, flavor physics, etc.
   In particular, new sources of CPV

#### The fermionic sector of 2HDMs

• Dim.-4 Yukawa couplings (in agreement with the local SM symmetries):

$$\mathcal{L}_{Y} = -\frac{\sqrt{2}}{v} \Big[ \overline{Q}'_{L} (M'_{d} \Phi_{1} + \frac{Y'_{d}}{\Psi_{2}}) d'_{R} + \overline{Q}'_{L} (M'_{u} \widetilde{\Phi}_{1} + \frac{Y'_{u}}{\Psi_{2}} \widetilde{\Phi}_{2}) u'_{R} + \overline{L}'_{L} (M'_{l} \Phi_{1} + \frac{Y'_{l}}{\Psi_{2}} \Phi_{2}) l'_{R} \Big] + \text{h.c.}$$
$$\widetilde{\Phi} = i\tau_{2} \Phi^{*} \qquad b \searrow_{H'} \swarrow^{s}$$

- To full generality: when diagonalizing fermion mass matrix M', <u>M'\*S<sub>1</sub> + Y'\*(S<sub>2</sub>+iS<sub>3</sub>)</u> is not diagonal; scalar-mediated flavor-changing neutral currents (FCNCs)
- SM FCNCs: GIM and CKM suppressed; various precisely measured |ΔF|=1 and |ΔF|=2 observables
- Strong constraints on *H*' mediator masses and couplings
   Various specific cases; assigning Z<sub>2</sub> quantum numbers constrains the Yukawa sector, thus avoiding FCNCs at the tree level

 $|\Delta B|=2$  meson mixing: used to extract SM-CPV



[Z<sub>2</sub>: Glashow, Weinberg '77]

### The Aligned 2HDM



• A different framework considers that the two sets of Yukawa couplings are proportional, or "aligned", thus avoiding FCNCs

 $Y_d = \varsigma_d M_d , \qquad Y_u = \varsigma_u^* M_u , \qquad Y_l = \varsigma_l M_l \qquad \begin{tabular}{c} \mbox{[Pich, Tuzón '09, \ + Jung '10]} \\ \end{tabular}$ 

- Radiative corrections, however, break this proportionality, but only by **small** amounts
- Freedom in Yukawa couplings w.r.t. SM parametrized by alignment parameters; couplings prop/ to masses
- Known Z<sub>2</sub>-symmetric versions are special cases, including Complex-2HDMs (i.e., CPV in the scalar potential after soft breaking of Z<sub>2</sub>)
- New sources of CPV w.r.t. Z<sub>2</sub>-symmetric 2HDMs & Complex-2HDMs

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#### Fermion-loop Barr-Zee in the A2HDM

 Novel contributions in the A2HDM: charged scalars have CPV couplings to fermions
 V: CKM matrix

• Dominant: **top-bottom**  $V_{tb}$ ; sub-dominant CKM contributions included since they involve large logarithms (thus use, e.g.,  $|V_{tb}|^2 + |V_{ts}|^2 + |V_{td}|^2 = 1$ )

#### => H<sup>±</sup>: CPV from alignment parameters only

• Other charged-scalar contributions are suppressed by quark masses and/or CKM matrix elements



[Bowser-C., Chang, Keung '97, Jung, Pich '13, Altmannshofer, Assi, Brod, Hamer, Julio, Uttayarat, Volkov '24]

#### Phenomenological effects

ectron'

 $|d_e^{exp}| < 4.1 \times 10^{-30} e \,\mathrm{cm} @ 90\% \,\mathrm{C.L.}$ [from 2212.11841]

- Black line: real alignment parameters
- Orange points: A2HDM, minus charged-current fermion-loop Barr-Zee contributions
- Blue points: A2HDM
- <u>Accidental cancellation</u> among contributions is possible

oenchmark

$$q_u$$
  $q_u$   $q_u$   $q_u$   $q_u$   $q_u$   $q_u$   $q_d$   $W^ e$   $(V^-)$   $(V$ 

Solution  

$$\begin{array}{l} \lambda_3 = 0.02 , \qquad \lambda_4 = 0.04 , \\ \lambda_7 = 0.03 , \qquad \operatorname{Re}(\lambda_5) = 0.05 , \\ \operatorname{Re}(\lambda_6) = -0.05 , \ \operatorname{Im}(\lambda_6) = 0.01 , \\ \alpha_3 = \pi/6 \ (\text{mixing } S_2 \ \text{and } S_3) \end{array}$$



#### The decoupling limit



- When the NP scale  $\Lambda >> EW$  scale  $\mu_{EW}$ : ignore the dynamics of the heavy new scalars at low energies
- The effects of the heavy dof's are encoded in couplings among the light dof's of the low-energy theory
- Wilson coefficients of dim.-6 SMEFT operators

 $X^3\,,\ X^2 H^2\,,\ \psi^2 H^3\,,\ \psi^2 X H\,,\ \psi^2 H^2 D\,,\ \psi^4$ 

X: field strength tensor, D: covariant derivative

[SMEFT: Hisano, Tsumura, Yang '12, Engel, Ramsey-M., van Kolck '13, Cirigliano, Dekens, de Vries, Mereghetti '16, + Chien '15, Cirigliano, Crivellin, Dekens, de Vries, Hoferichter, Mereghetti '19, ...; decoupling limit: Egana-U., Thomas '15, Crivellin, Ghezzi, Procura '16, Dermisek, Hermanek '24, ...]

## The A2HDM in the decoupling limit

- Logarithmic structure of contributions to the eEDM:
  - Log( $\Lambda/\mu_{EW}$ ): prop/ to the scalar potential parameter  $\lambda_6$  [no Log( $\Lambda/\mu_{EW}$ )<sup>2</sup>]
  - Log( $\Lambda/\mu_{EW}$ )<sup>2</sup>, Log( $\Lambda/\mu_{EW}$ ): accompanied by the top-quark mass<sup>2</sup>
  - Log( $\Lambda/\mu_{EW}$ ): accompanied by the **bottom**-quark mass<sup>2</sup> [no Log( $\Lambda/\mu_{EW}$ )<sup>2</sup>]
  - 2HDMs more general than A2HDM:  $Log(\Lambda/\mu_{EW})$  times **tau**-lepton mass<sup>2</sup>
- Use SMEFT to <u>understand the large logarithms in the A2HDM</u> in the decoupling limit
- $Log(\mu_{EW}/\mu_{Iow})^{\#}$  also present and numerically important, but beyond the scope of the current discussion (non-SMEFT operators)

[Davidson '16, Panico, Pomarol, Riembau '18, Altmannshofer, Gori, Hamer, Patel '20]



### Renormalization Group Equations

• Log in one-loop and two-loop computations:

 $\mu$ : renormalization scale; C: Wilson coefficients

1

$$\frac{d}{d\log\mu}C_i = \frac{1}{(4\pi)^2} \gamma_{ji}^{(1)} C_j \implies C_i(\mu) \simeq \frac{1}{(4\pi)^2} \gamma_{ji}^{(1)} \log\left(\frac{\mu}{\Lambda}\right) C_j(\Lambda) \qquad (C_i(\Lambda) = 0)$$

$$\frac{d}{d\log\mu}C_i = \frac{1}{(4\pi)^2} \gamma_{ji}^{(2)} C_i \implies C_i(\mu) \simeq \frac{1}{(4\pi)^2} \gamma_{ji}^{(2)} \log\left(\frac{\mu}{\Lambda}\right) C_i(\Lambda) \qquad (C_i(\Lambda) = 0)$$

$$\frac{a}{d\log\mu}C_i = \frac{1}{(4\pi)^4} \gamma_{ji}^{(2)} C_j \Rightarrow C_i(\mu) \simeq \frac{1}{(4\pi)^4} \gamma_{ji}^{(2)} \log\left(\frac{\mu}{\Lambda}\right) C_j(\Lambda) \quad \left(\gamma_{ji}^{(1)} = 0, \ C_i(\Lambda) = 0\right)$$

• Log<sup>2</sup> when there is a <u>chain</u> of operator mixing:

$$\frac{d}{d\log\mu}C_{C} = \frac{1}{(4\pi)^{2}} \gamma_{BC}^{(1)} C_{B}, \quad \frac{d}{d\log\mu}C_{B} = \frac{1}{(4\pi)^{2}} \gamma_{AB}^{(1)} C_{A}$$
$$\Rightarrow C_{C}(\mu) \simeq \frac{1}{2(4\pi)^{4}} \gamma_{AB}^{(1)} \gamma_{BC}^{(1)} \log^{2}\left(\frac{\mu}{\Lambda}\right) C_{A}(\Lambda) \qquad (C_{B}(\Lambda) = C_{C}(\Lambda) = 0)$$

γ: Anomalous Dimension Matrices (ADMs)

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## Four-fermion operator lequ(1): m<sup>2</sup>

- Chain of one-loop mixing [Jenkins, Manohar, Trott '13 '13, + Alonso '13]
- Single logarithm Log( $\Lambda/\mu_{EW}$ ): requires calculating one-loop finite contributions combined with one-loop ADM elements, and the ADM element at two loops
- 2HDMs more general than A2HDM: generation-dependent ( $\varsigma_u \neq \varsigma_c \neq \varsigma_t$ ) alignment parameters; include charm quark contributions



#### Four-fermion operator ledq: mb

- No one-loop mixing; nor chain of one-loop mixing [so no  $Log(\Lambda/\mu_{EW})^2$ ]
- ADM element only available in [Panico, Pomarol, Riembau '18]
- Independent calculation ongoing [Ferrando Solera, Jaeger, LVS] [talk later today at "Multicultural Greek"]
  - Treatment of  $y_5$ : in BMHV, need for finite renormalization to restore Ward identities  $\bigstar$
  - Extension to other dimension-6 four-fermion operators (e.g., to discuss nEDM; applications beyond 2HDMs)
- 2HDMs more general than A2HDM:  $m_{\tau^2}$  from lee'l' SMEFT operator  $(Im(\varsigma_e^*\varsigma_{\tau}) \neq 0)$



#### Illustrating the decoupling limit

- Black line: A2HDM
- Red line: only  $m_t^2 * Log(\Lambda/\mu_{EW})^2$
- Blue line: previously discussed SMEFT  $(\lambda_6, m_b^2)^*Log(\Lambda/\mu_{EW})$  contributions Blue band: vary the scale  $\Lambda$
- Decoupling limit: the larger the energy the closer the curves, i.e., logarithmic terms tend to dominate

$$\begin{array}{l} \lambda_3 = 0.02 \ , \qquad \lambda_4 = 0.04 \ , \\ \lambda_7 = 0.03 \ , \qquad \mathrm{Re}(\lambda_5) = 0.05 \ , \\ \mathrm{Re}(\lambda_6) = -0.05 \ , \ \mathrm{Im}(\lambda_6) = 0.01 \ , \\ \alpha_3 = \pi/6 \ (\mathrm{mixing} \ S_2 \ \mathrm{and} \ S_3) \end{array}$$



#### A2HDM vs. Z<sub>2</sub>-2HDMs

- Large logarithms prop/ to mt<sup>2</sup> and mb<sup>2</sup> absent in Z<sub>2</sub>-symmetric 2HDMs; large logarithms emerge from the mixing among SMEFT operators
- SMEFT contributions encode both heavy neutral and charged scalars charged H in a SU(2)xU(1) symmetric way;
  - EDMs in the decoupling limit in presence of  $Z_2$  symmetry => no contributions from four-fermion SMEFT operators, since no charged-scalar counterpart

neutral &

- Discussion holds only for CPV, which is the novelty in H<sup>±</sup> sector in the A2HDM
- Bottomline: the presence of the  $Z_2$  symmetry controls the basis of effective • operators needed in the description of EDMs => suppression mechanism in Z<sub>2</sub>-symmetric 2HDMs

#### Conclusions



- A2HDM: avoids FCNCs while introducing **new sources of CPV**
- Novel contribution from the charged Higgs w.r.t. Z<sub>2</sub>-2HDMs
- Discussing SMEFT/decoupling limit:
  - Anatomy of logarithmic contributions ( $\psi^2 H^3$  in back-up)
  - Cancellation mechanism: Z<sub>2</sub> symmetry suppresses large logarithms
- <u>Outlook</u> (see back-up): role of lepton-nucleon operators in the interpretation of experimental bounds on EDMs; nEDM

#### **BACK UP**



Cover: Jim Musil

### The Higgs particle

(Gauge couplings to fermions)

(Higgs self-interaction)

- Crucial piece to understand EW dynamics
- Up to the present accuracy, behaves as predicted by the SM

+  $\mathbf{Y}H\overline{\psi}\psi$  + h.c. (spectrum of quark masses, <u>CKM</u> matrix)

 $\mathcal{L}_{SM(NP)} \sim -\frac{1}{4} (F_{\mu\nu})^2 + i \bar{\psi} D \psi$ 

 $+ |D_{\mu}H|^2 - V(H)$ 

(short-range weak interactions)

 $- \left(+\sum_{d>4}rac{1}{\Lambda^{d-4}}
ight)$ 

[e.g., Brod, Haisch, Zupan '13]

• **Deviations** w.r.t. the SM can be probed in various ways, e.g., flavor conserving observables such as electron's EDM

In particular, due to the presence of a heavy NP sector compatible with the local SM symmetries

#### New Physics energy scale

Scalar potential in the Higgs-basis; CPV phases

$$V = \mu_1 \Phi_1^{\dagger} \Phi_1 + \mu_2 \Phi_2^{\dagger} \Phi_2 + \left[ \mu_3 \Phi_1^{\dagger} \Phi_2 + \text{h.c.} \right] + \frac{\lambda_1}{2} (\Phi_1^{\dagger} \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^{\dagger} \Phi_2)^2 + \lambda_3 (\Phi_1^{\dagger} \Phi_1) (\Phi_2^{\dagger} \Phi_2) + \lambda_4 (\Phi_1^{\dagger} \Phi_2) (\Phi_2^{\dagger} \Phi_1) + \left[ \left( \frac{\lambda_5}{2} \Phi_1^{\dagger} \Phi_2 + \lambda_6 \Phi_1^{\dagger} \Phi_1 + \lambda_7 \Phi_2^{\dagger} \Phi_2 \right) (\Phi_1^{\dagger} \Phi_2) + \text{h.c.} \right]$$

- The mass scale of the second doublet is not controlled by the EW scale, but by the dimensionful parameter  $\mu_2 \sim \Lambda$
- Current bounds on the A2HDM from a global fit analysis: Higgs strength, theoretical constraints, flavor observables, etc.

[CP conserving limit: Eberhardt, Martínez, Pich '20, Karan, Miralles, Pich '23, + Coutinho '24]

S <sub>1</sub> , S <sub>2</sub> mixing 68% C.L.)	$M_{H^\pm} \geq 390$ GeV (95%)	$M_H \ge 410 { m GeV}$ (99)	$M_H \ge 410  { m GeV}  (95\%)$		$M_A \ge 370  { m GeV}  (95\%)$	
	$\lambda_2: \ 3.2 \pm 1.9$	$\lambda_3$ : 5.9 $\pm$ 3.5	$\lambda_3$ : 5.9 $\pm$ 3.5		$\lambda_7:0.0\pm1.1$	
	$ ilde{lpha}$ : (0.05 $\pm$ 21.0) $\cdot$ 10 <sup>-3</sup>	$\varsigma_u$ : 0.006 ± 0.257	ς <sub>d</sub> : 0.12 =	± 4.12	$arsigma_\ell$ : $-0.39\pm11.69$	



#### Electron's EDM in 2HDMs

e

 $H_{j}$ 

- Contribution at one loop: prop/ to  $m_e^3/(4\pi)^2/\Lambda^2$
- <u>Barr-Zee diagrams</u>: two-loop effect scaling as  $m_e/(4\pi)^4/\Lambda^2$ ; avoids mass/chiral suppression at one loop



Red blobs: EW gauge bosons and scalar sector

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- EW sector in the loop: not gauge invariant by itself; combine with kite diagrams [e.g., Abe, Hisano, Kitahara, Tobioka '13, Altmannshofer, Gori, Hamer, Patel '20]
- Large logarithms  $Log(\Lambda/\mu_{low})^{\#}$  can be present

#### EDMs in SMEFT



- At tree level, only dipole operators  $\psi^2 XH$  contribute to EDMs
- At <u>one loop</u>, a few dimension-6 operators contribute via mixing (finite contributions also possible, but not logarithmic enhanced)

 $\psi^2 X H, X^3, X^2 H^2, Q^{(3)}_{\ell equ} = (\bar{\ell}^j \sigma_{\mu\nu} e) \epsilon_{jk} (\bar{q}^k \sigma^{\mu\nu} u)$ 

• At <u>two loops</u>, novel dimension-6 operators can contribute via mixing; their anomalous dimension matrix elements at one loop vanish

 $\psi^2 H^3$ ,  $Q^{(1)}_{\ell equ} = (\bar{\ell}^j e) \epsilon_{jk} (\bar{q}^k u)$ ,  $Q_{\ell edq} = (\bar{\ell} e) (\bar{d}q)$ ,  $Q'_{\ell e} = (\bar{\ell} e) (\bar{e}\ell)$ , ...

 Use SMEFT to <u>understand the large logarithms in the A2HDM in the</u> <u>decoupling limit</u>

#### Dim.-6 Yukawa operators $\psi^2 H^3$

- Mixing into dipoles absent at one loop
- Moreover, there is no chain of one-loop mixing [so no  $Log(\Lambda/\mu_{EW})^2$ ]
- ADM: calculated in [Altmannshofer, Gori, Hamer, Patel '20, Jaeger, Leslie, LVS '20] [global sign difference w.r.t. Panico, Pomarol, Riembau '18, Elias M., Ingoldby, Riembau '20]
- A2HDM: in the decoupling limit, a single parameter from the scalar potential  $d^{\text{SMEFT}} = a^2 3 = \text{Im}(\lambda^* \alpha) = (-\lambda^2)^2$



#### Outlook: lepton-gluonic operators

- Experimental bound: EDM & electron-nucleon interaction of coupling C<sub>s</sub>; it was assumed in this talk that C<sub>s</sub>=0: factor ~5 impact on the bound on [d<sub>e</sub>]!
- Semi-leptonic operators with heavy quarks lead to lepton-gluonic effective operators (dim.>6) at low-energies; need to include non-perturbative dynamics



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#### Outlook: neutron's EDM

- Further dimension-6 SMEFT operators, including chromo-magnetic dipole and Weinberg (chromo-EDM of gluons) operators า
- Color group factors and strong coupling constant can enhance their contributions
- ADM elements not yet available [Jaeger, LVS]

$$Q_{quqd}^{(1)} = (\bar{q}^{j}u)\epsilon_{jk}(\bar{q}^{k}d), \ Q_{qu}^{(1)'} = (\bar{q}u)(\bar{u}q), \ Q_{qd}^{(1)'} = (\bar{q}d)(\bar{d}q), \ \dots$$

#### Sym breaking at the quantum level

Single insertions of the BRST variation of the action

$$\int \mathrm{d}^{D} x \frac{\delta_{R} \Gamma \left[ X, K \right]}{\delta K_{n} \left( x \right)} \frac{\delta_{L} \Gamma \left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[ X, K \right]}{\delta X^{n} \left( x \right)} = \lim_{\mathbf{Q} \to 0} \int_{\mathbf{Q}} \frac{\left[$$

[cf. Quantum Action Principle; Martin, Sanchez-R. '00; Barnich, Brandt, Henneaux '00; Bélusca-M., Ilakovac, Madzor-B., Stoeckinger '20]

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 $\lim_{Q \to 0} \int d^{D}x \frac{\delta_{R} \Gamma \left[ X, K, Q \right]}{\delta Q \left( x \right)}$ true or trivial obstruction

Q: source for the **BRST transformation** of the sym.-breaking term  $i\bar{\xi}\partial\xi$ 

- This equation provides a unified framework for 'true anomalies' (e.g., chiral anomalies) and 'trivial anomalies'
- 'Trivial anomalies' can be removed with the addition of appropriate finite=non-evanescent, local counter terms