



Exclusive Reactions at COMPASS

CIPANP 2025

Madison, Wisconsin

June 10, 2025

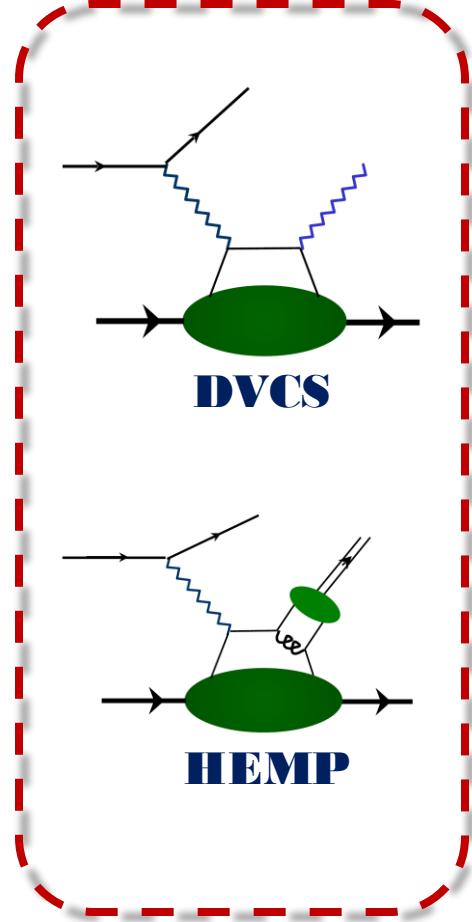
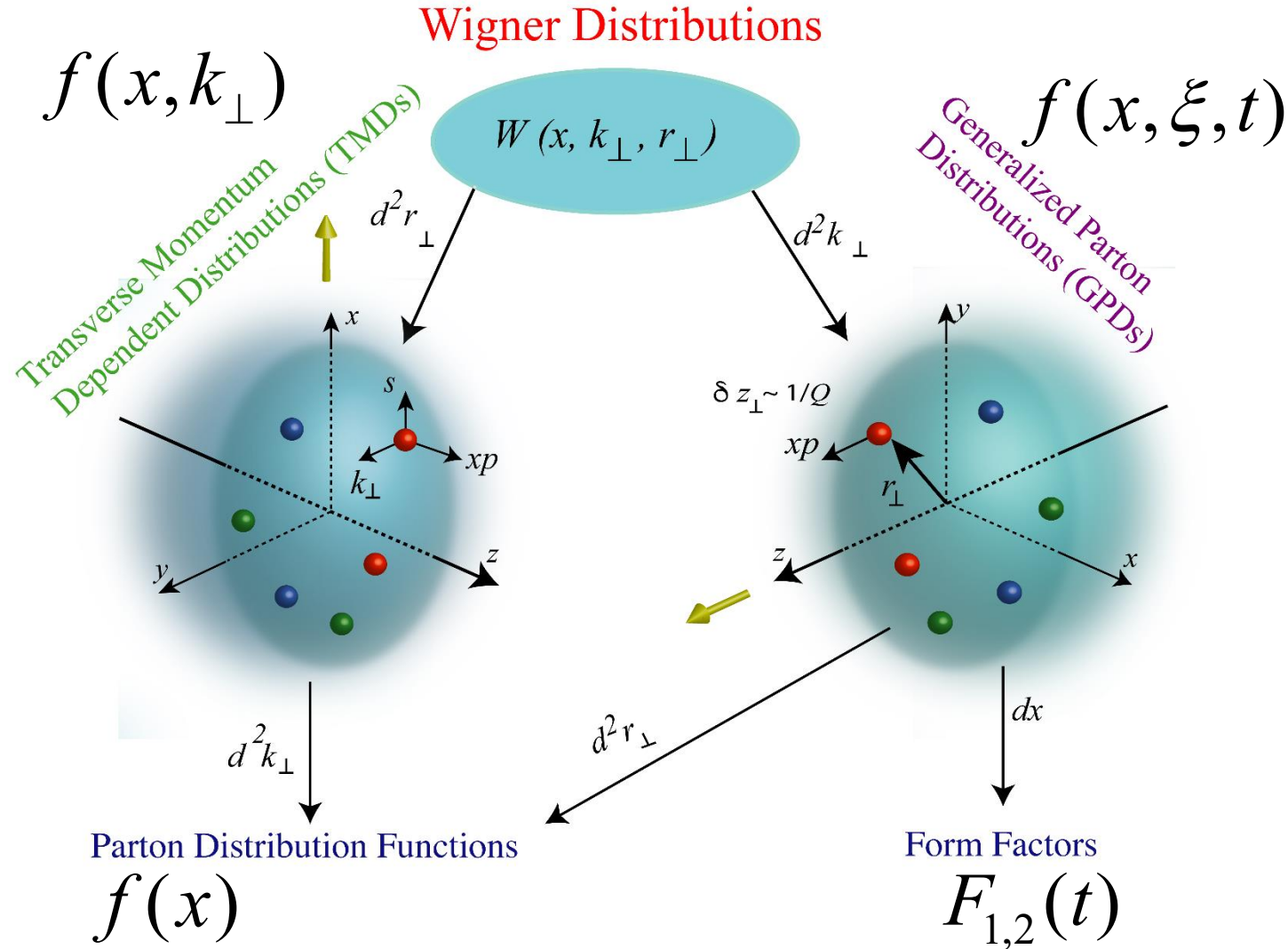
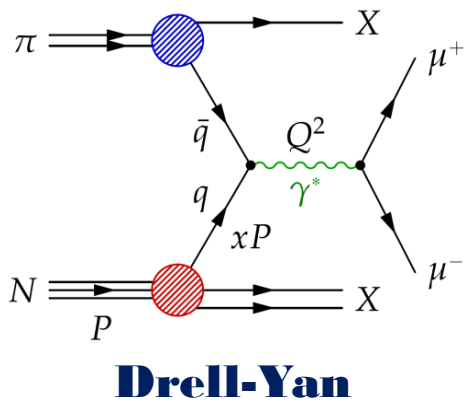
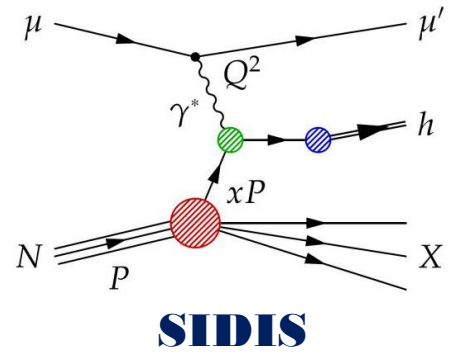
Po-Ju Lin

Department of Physics, National Central University

On behalf of the COMPASS Collaboration

Multi-dimensional Partonic Structures

<http://www.int.washington.edu/PROGRAMS/17-3/>



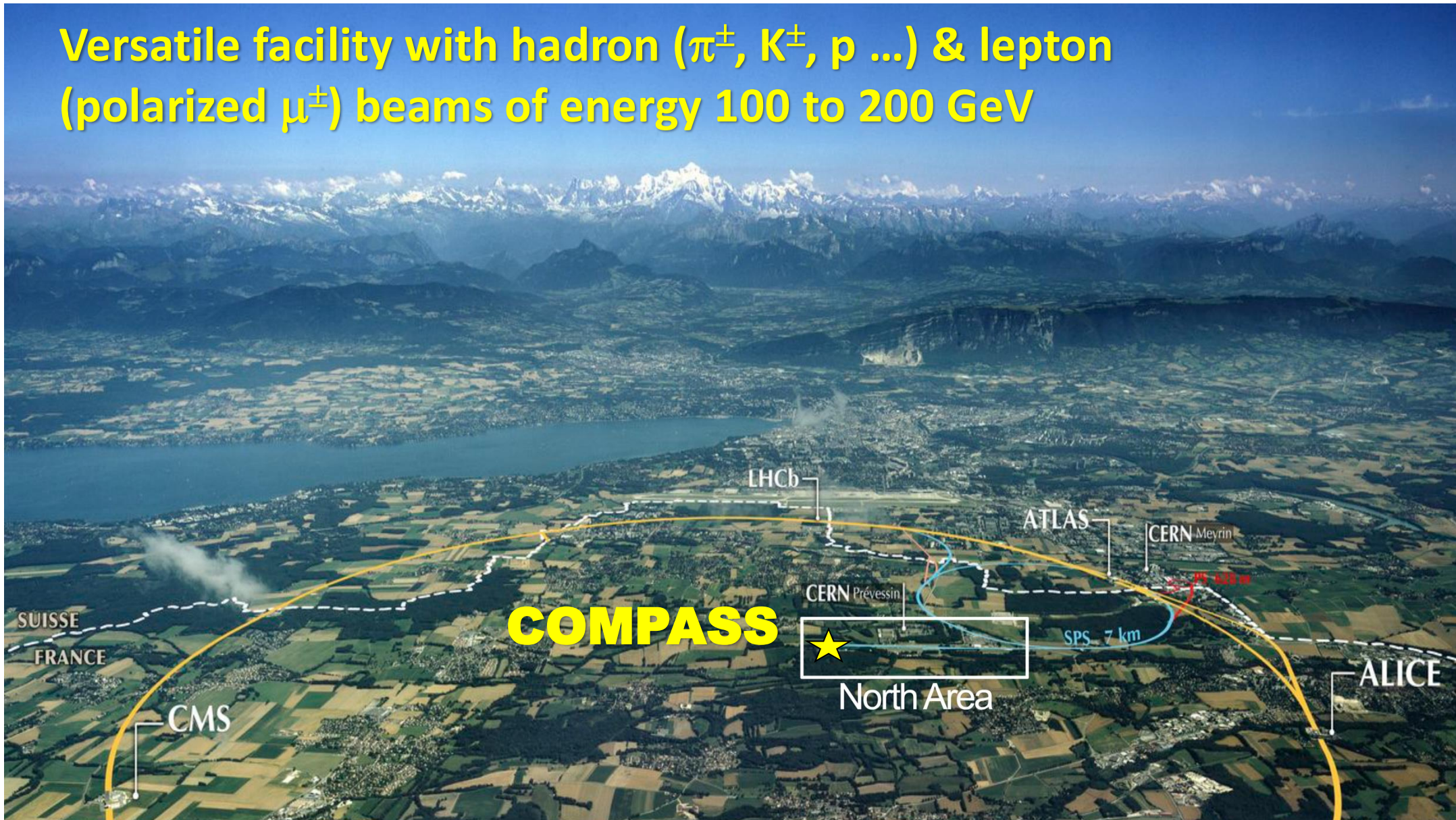
COMPASS investigates the multi-dimensional structure of nucleon via various processes

COMPASS Experiment

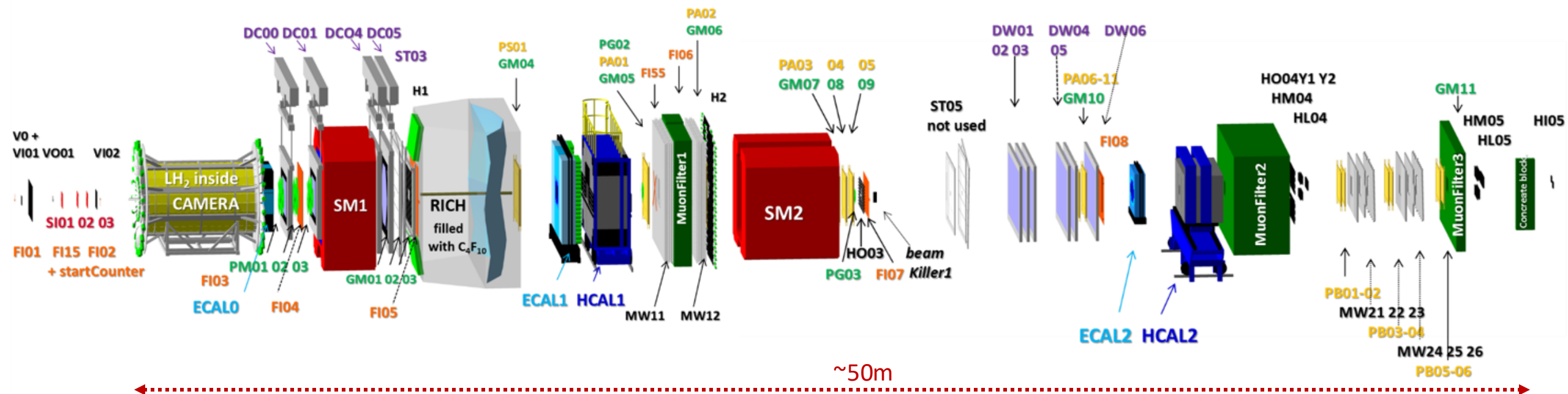


Versatile facility with hadron (π^\pm , K^\pm , p ...) & lepton (polarized μ^\pm) beams of energy 100 to 200 GeV

COmmon
Muon and
Proton
Apparatus for
Structure and
Spectroscopy



COMPASS Experimental Setup



- Primary beam – 400 GeV p from SPS
 - Impinging on Be production target
- 190 GeV secondary hadron beams
 - h^- beam: 97% π^- , 2% K^- , 1% p
 - h^+ beam: 75% π^+ , 24% p , 1% K^+
- 160 GeV tertiary muon beams
 - μ^\pm longitudinally polarized

Large-acceptance forward spectrometer

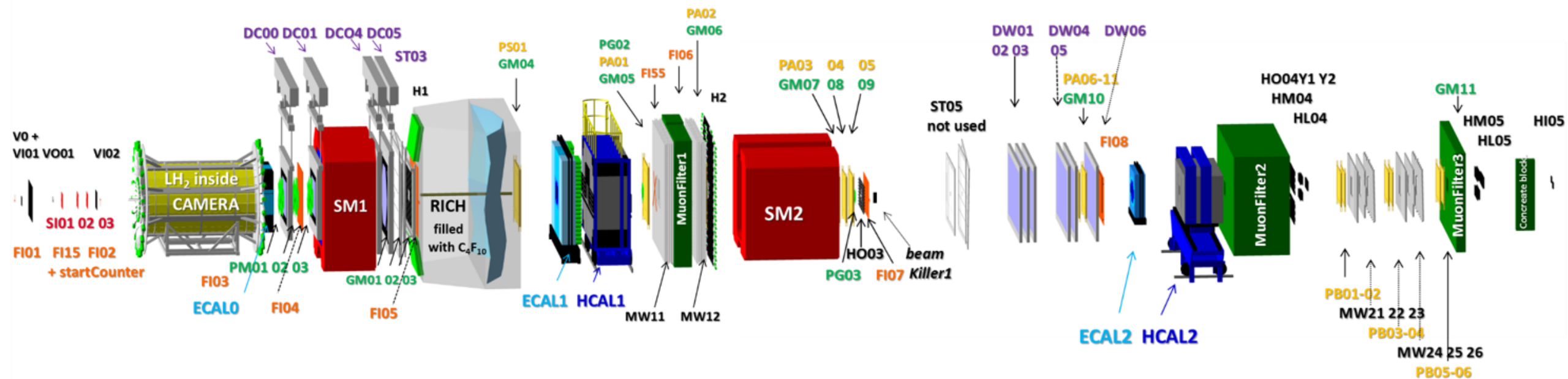
- Precise tracking (350 planes)
SciFi, Silicon, MicroMegas, GEM, MWPC, DC, straw
- PID – CEDARs, RICH, calorimeters, Muon Walls

Various targets:

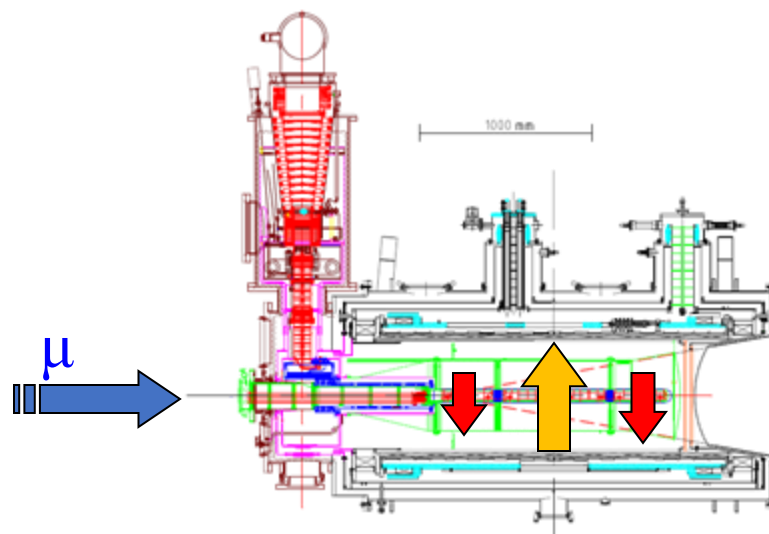
- Polarized solid-state NH_3 or ^6LiD
- Liquid H_2
- Solid-state nuclear targets

❖ NIM A 577 (2007) & NIM A 779 (2015) 69

COMPASS Experimental Setup

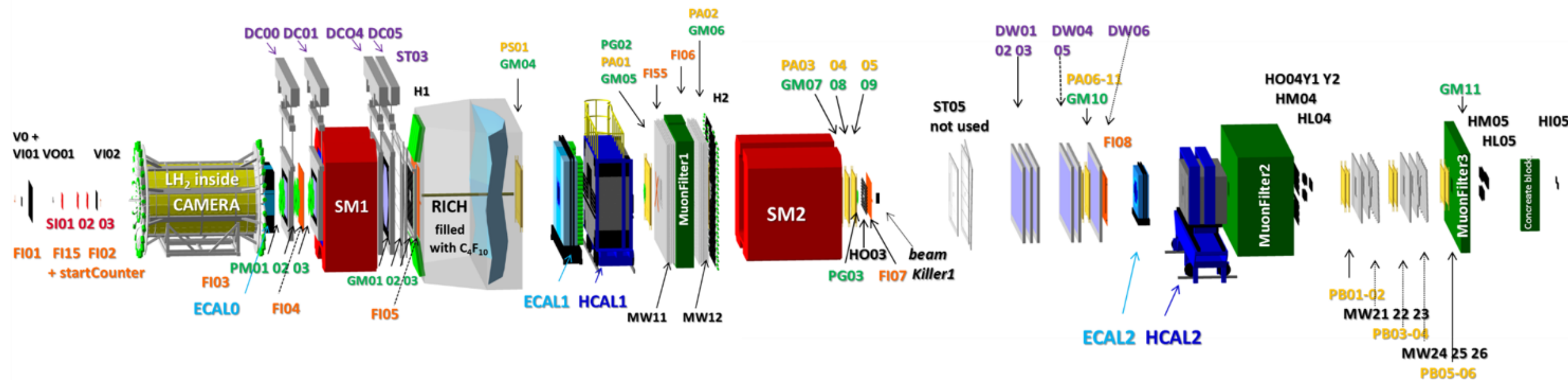


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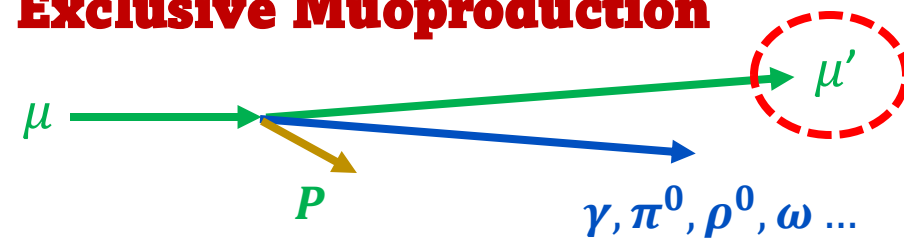
- In early GPD studies, transversely polarized target was used.
- Polarization reversal by magnetic field rotation
- 2.5m unpolarized LH₂ target used in GPD dedicated runs

COMPASS Setup for Exclusive Processes

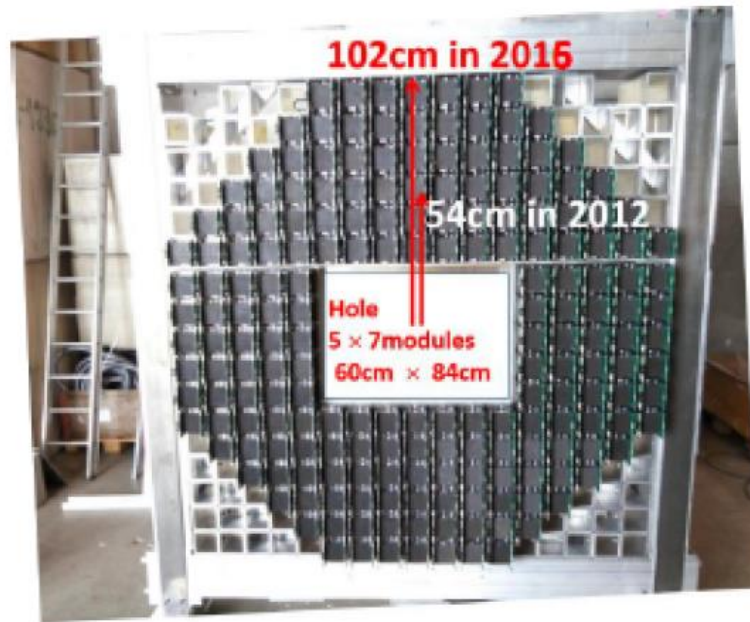
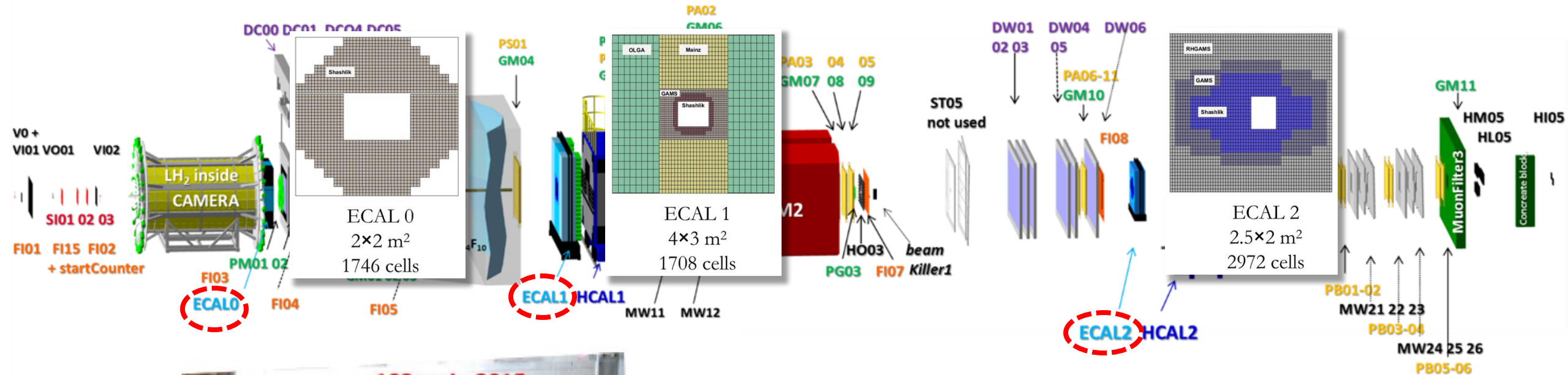


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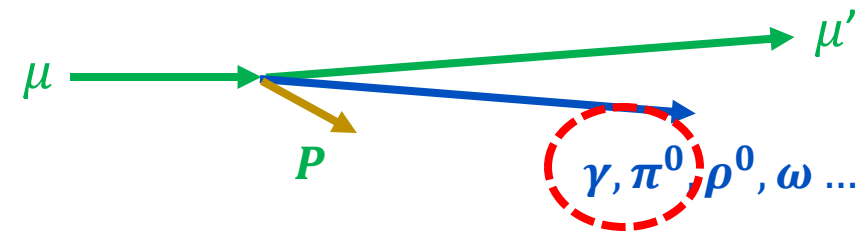
Exclusive Muoproduction



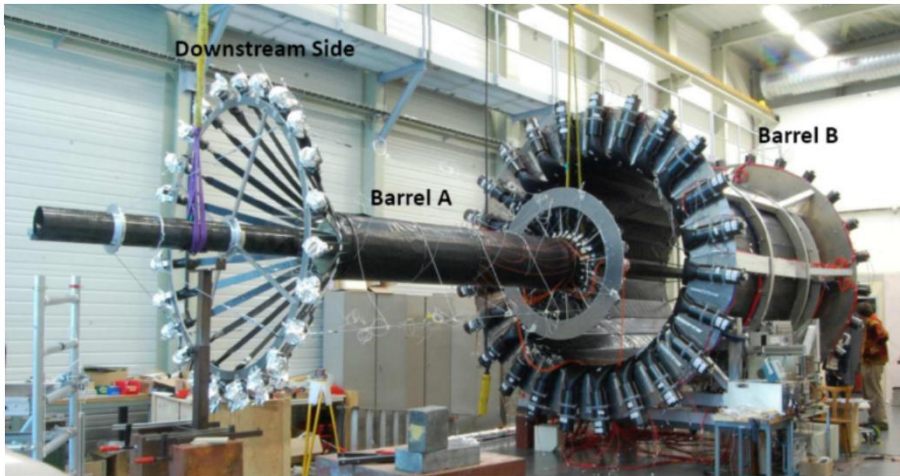
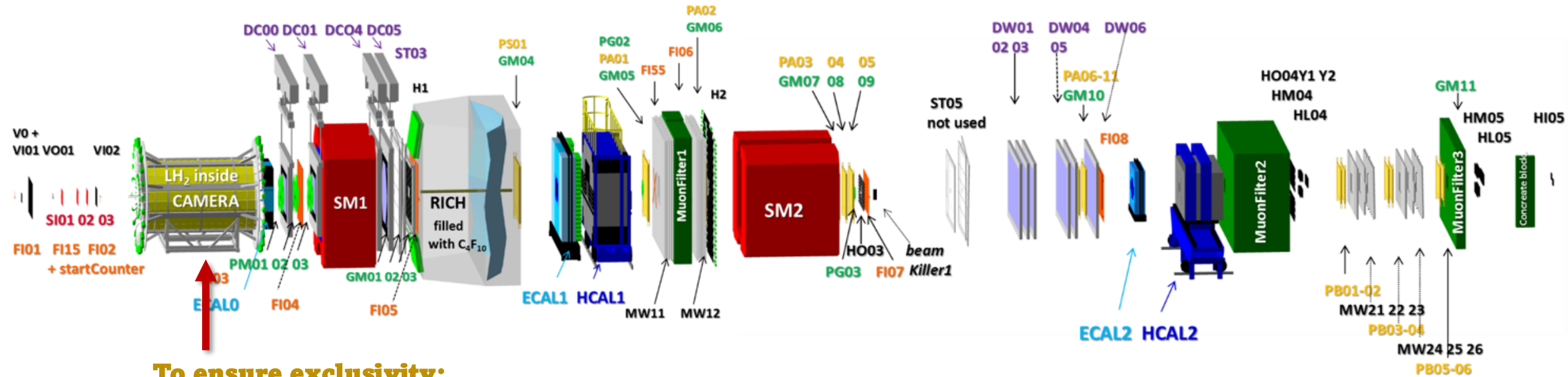
COMPASS Setup for Exclusive Processes



Exclusive Muoproduction

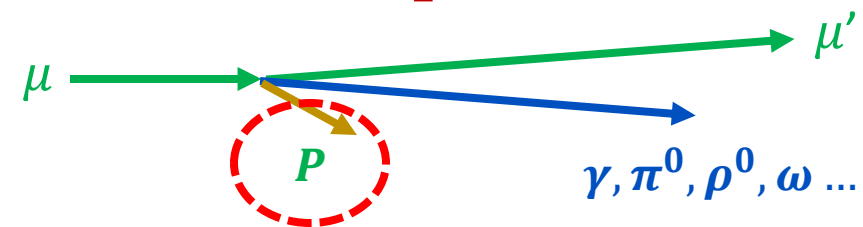


COMPASS Setup for Exclusive Processes



CAMERA recoil proton detector

Exclusive Muoproduction



COMPASS Experiment



2002-2022 COMPASS data taking

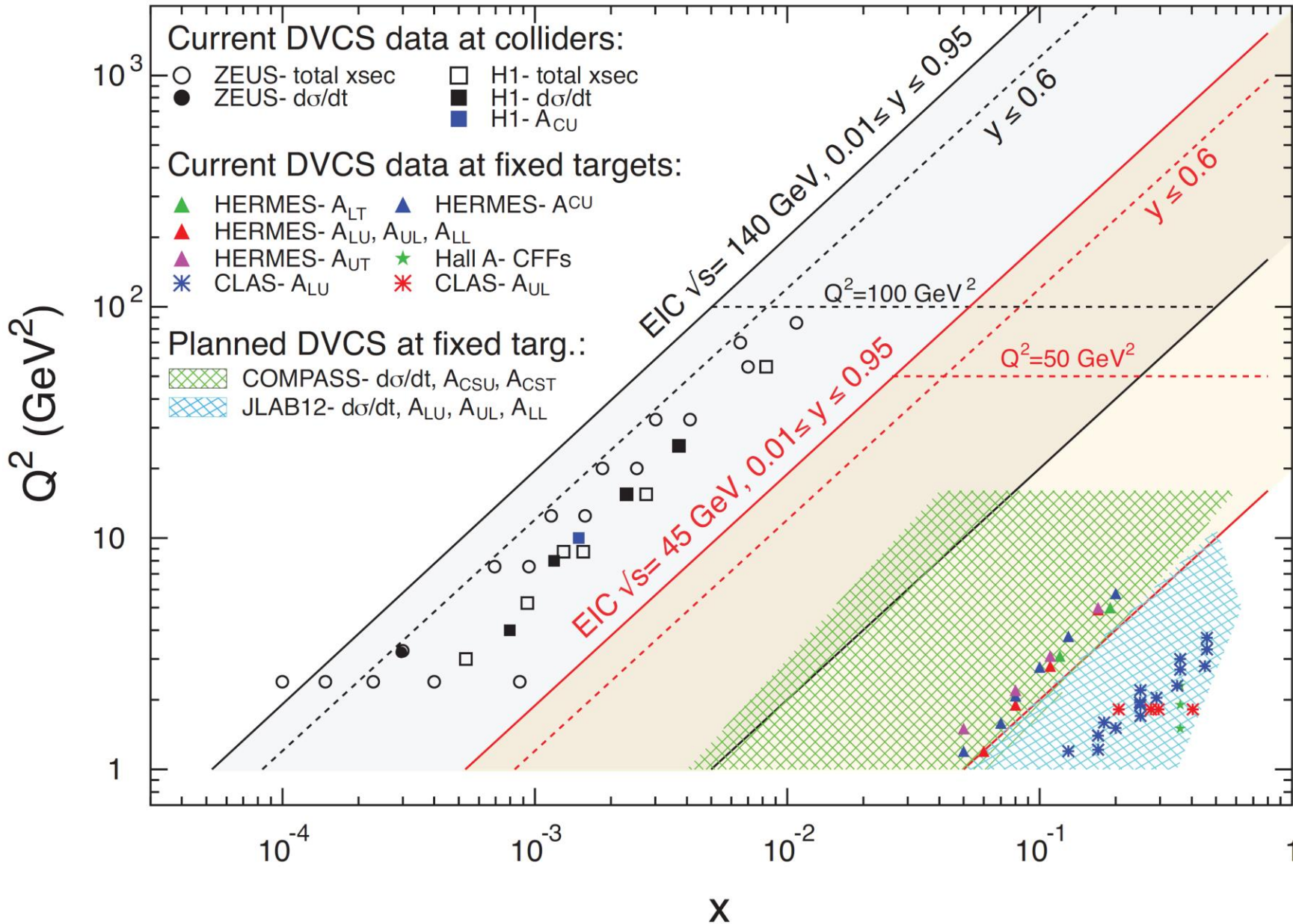
2002-2004	DIS & SIDIS, μ^+ - d , 160 GeV, L & T polarized target
2005	<i>CERN accelerator shutdown, increase of COMPASS acceptance</i>
2006	DIS & SIDIS, μ^+ - d , 160 GeV, L polarized target
2007	DIS & SIDIS, μ^+ - p , 160 GeV, L & T polarized target
2008-2009	Hadron spectroscopy & Primakoff reaction, $\pi/K/p$ beam
2010	SIDIS, μ^+ - p , 160 GeV, T polarized target
2011	DIS & SIDIS, μ^+ - p , 200 GeV, L polarized target
2012	Primakoff reaction, $\pi/K/p$ beam
2012 pilot run	DVCS/HEMP/SIDIS, μ^+ & μ^- - p , 160 GeV, unpolarized target
2013	<i>CERN accelerator shutdown, LS1</i>
2014-2015	Drell-Yan, π^- - p , T polarized target
2016-2017	DVCS/HEMP/SIDIS, μ^+ & μ^- - p , 160 GeV, unpolarized target
2018	Drell-Yan, π^- - p , T polarized target
2019-2020	<i>CERN accelerator shutdown, LS2</i>
2021-2022	SIDIS, μ^+ - d , 160 GeV, T polarized target

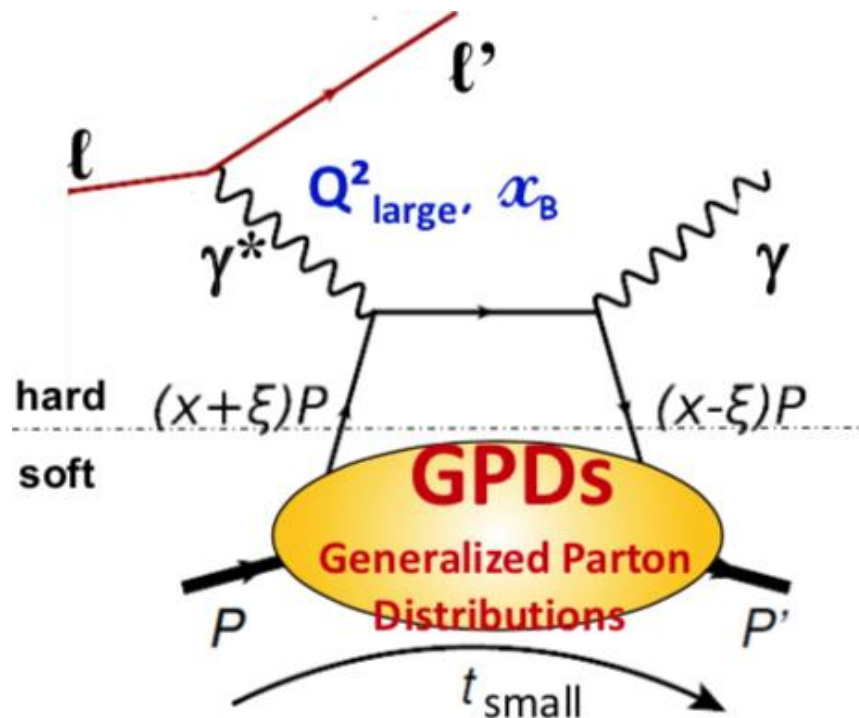
Study hadron structure with complementary tools:

➤ **COMPASS holds the record for the longest-running CERN experiment**

- 2012 pilot run with 4-week data taking
- 2016-17 dedicated run. 2 x 6 months.

Landscape – Global Programs of DVCS



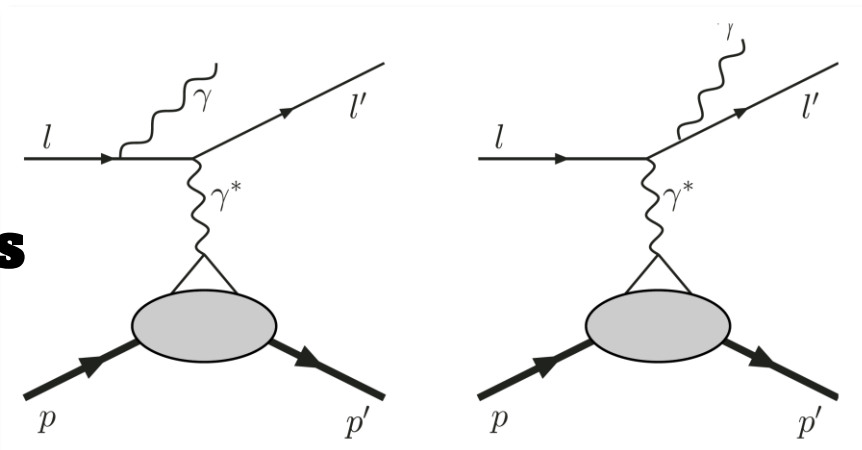


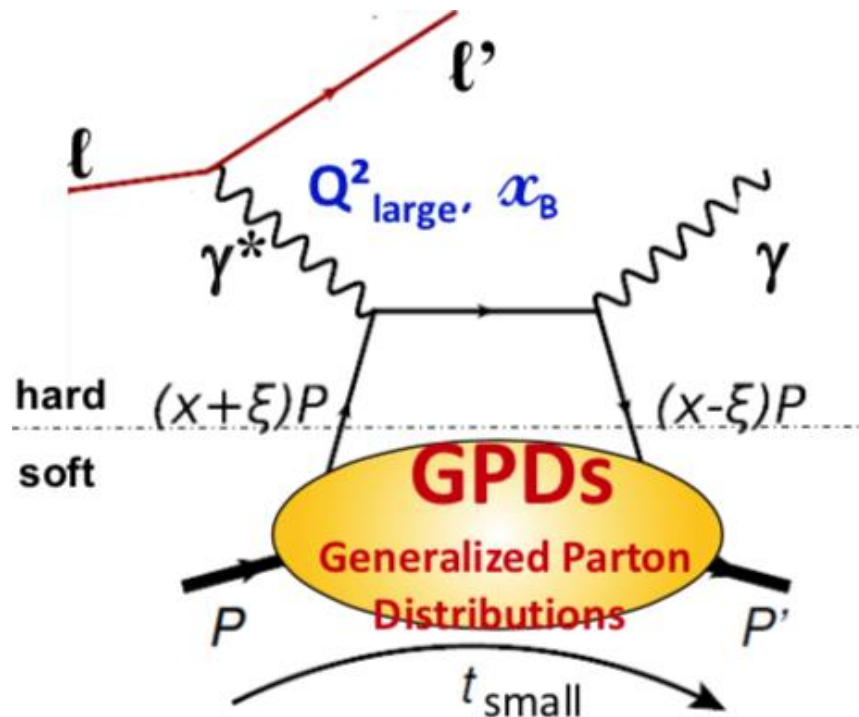
$$\text{DVCS: } l + p \rightarrow l' + p' + \gamma$$

- As the golden channel to access GPDs, DVCS has been the workhorse for GPD Extraction.
- Its interference with the well-understood Bethe-Heitler process gives access to more info.

- The GPDs depend on the following variables:
 - x : average longitudinal momentum frac.
 - ξ : longitudinal momentum diff.
 - t : four momentum transfer
(correlated to b_{\perp} via Fourier transform)
 - Q^2 : virtuality of γ^*

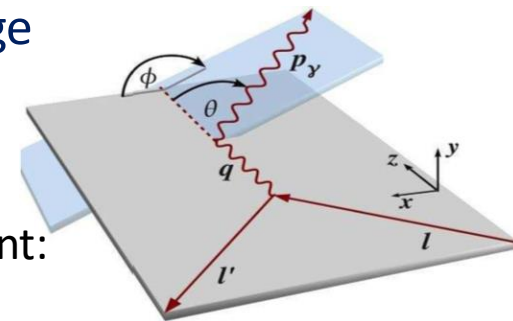
**BH
Process**





DVCS: $l + p \rightarrow l' + p' + \gamma$

- With LH₂ target and small x_B coverage
→ focuses on H at COMPASS



- The variables measured in the experiment:
 $E_\ell, Q^2, x_{Bj} \sim 2\xi/(1+\xi),$
 t (or $\theta_{\gamma^*\gamma}$) and ϕ ($\ell\ell'$ plane/ $\gamma\gamma^*$ plane)

$\text{CFE} \rightarrow \mathcal{H}(\xi, t) = \int_{-1}^{+1} dx \frac{\mathbf{H}(x, \xi, t)}{x - \xi + i\epsilon} + \dots$
 $\text{GPD} \rightarrow \mathbf{H}(x, \xi, t)$

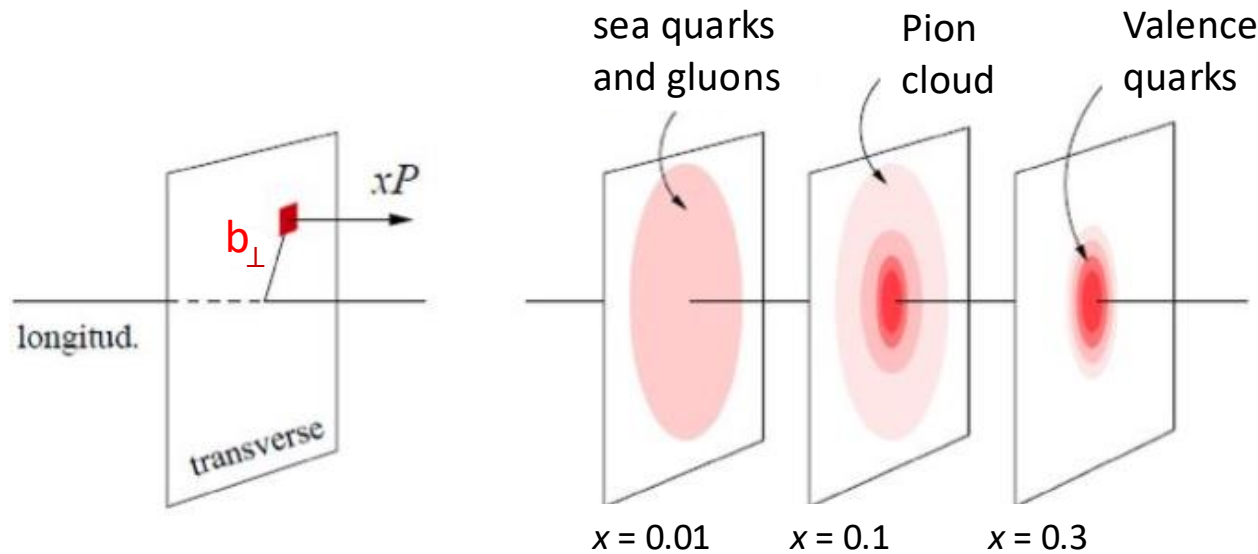
$\mathcal{H}(\xi, t) = \mathcal{P} \int_{-1}^{+1} dx \frac{\mathbf{H}(x, \xi, t)}{x - \xi} - i\pi \mathbf{H}(x = \pm \xi, \xi, t) + \dots$

REAL part: $\mathcal{P} \int_{-1}^{+1} dx \frac{\mathbf{H}(x, \xi, t)}{x - \xi}$
 Imaginary part: $-i\pi \mathbf{H}(x = \pm \xi, \xi, t)$

$$\Re \mathcal{H}(\xi, t) = \mathcal{P} \int dx \frac{\text{Im } \mathcal{H}(x, t)}{x - \xi} + \Delta(t)$$

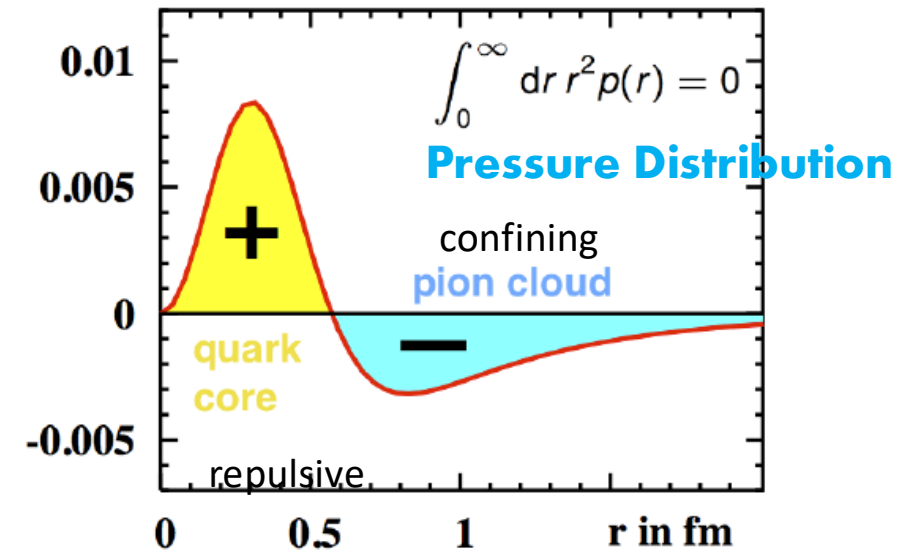
Transverse Imaging and Pressure Distribution

Mapping in the transverse plane



M. Polyakov, P. Schweitzer, *Int.J.Mod.Phys. A33* (2018)

$r^2 p(r)$ in GeV fm^{-1}



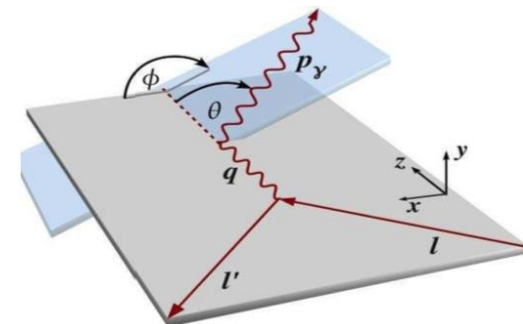
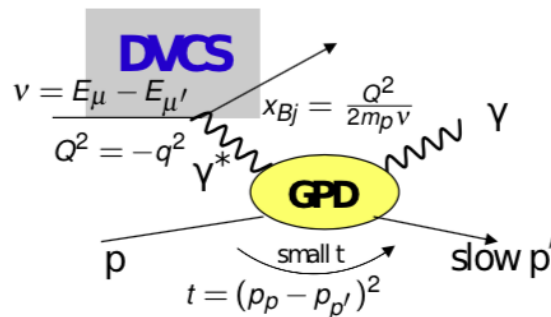
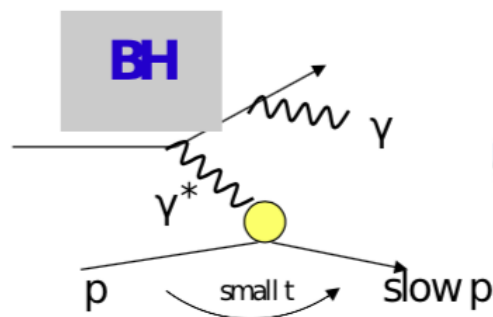
$\text{CFF} \rightarrow \mathcal{H}(\xi, t) = \int_{-1}^{+1} dx \frac{\mathbf{H}(x, \xi, t)}{x - \xi + i\epsilon} + \dots$
 $\text{GPD} \rightarrow \mathcal{H}(x, \xi, t) = \mathcal{P} \int_{-1}^{+1} dx \frac{\mathbf{H}(x, \xi, t)}{x - \xi} - i\pi \mathbf{H}(x = \pm \xi, \xi, t) + \dots$

$\text{REAL part} \rightarrow \mathcal{R}e \mathcal{H}(\xi, t) = \mathcal{P} \int dx \frac{\text{Im } \mathcal{H}(x, t)}{x - \xi} + \Delta(t)$

$\text{Imaginary part} \rightarrow \text{FT of } \mathcal{H}(x, \xi=0, t)$

$\text{D-term} \rightarrow d_1(t)$

Azimuthal Dependence of BH & DVCS



$$\frac{d^4\sigma(\ell p \rightarrow \ell p \gamma)}{dx_B dQ^2 d|t| d\phi} = \underset{\text{Well known}}{d\sigma^{BH}} + \left(d\sigma_{unpol}^{DVCS} + P_\ell d\sigma_{pol}^{DVCS} \right) + (e_\ell \text{Re } I + e_\ell P_\ell \text{Im } I)$$

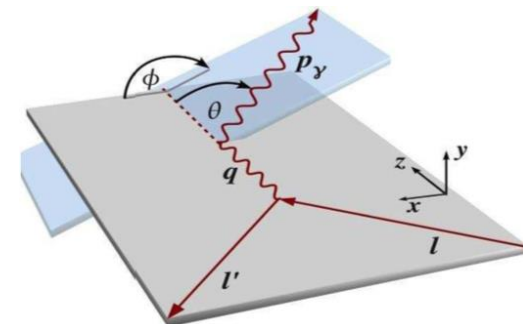
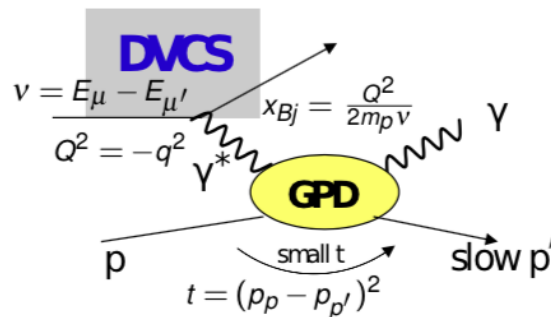
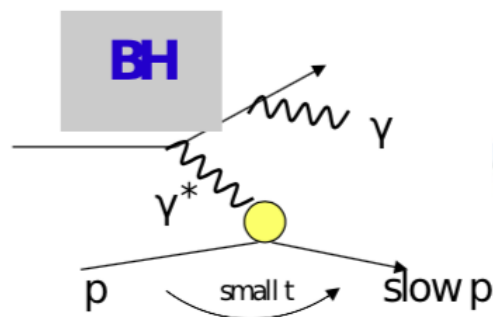
Beam Charge-spin difference & sum

$$\mathcal{D}_{CS,u}(\phi) \equiv d\sigma(\mu^{+\leftarrow}) - d\sigma(\mu^{-\rightarrow})$$

$$\mathcal{S}_{CS,u}(\phi) \equiv d\sigma(\mu^{+\leftarrow}) + d\sigma(\mu^{-\rightarrow})$$

$$\begin{aligned} d\sigma^{BH} &\propto c_0^{BH} + c_1^{BH} \cos \phi + c_2^{BH} \cos 2\phi \\ d\sigma_{unpol}^{DVCS} &\propto c_0^{DVCS} + c_1^{DVCS} \cos \phi + c_2^{DVCS} \cos 2\phi \\ d\sigma_{pol}^{DVCS} &\propto s_1^{DVCS} \sin \phi \\ \text{Re } I &\propto c_0^I + c_1^I \cos \phi + c_2^I \cos 2\phi + c_3^I \cos 3\phi \\ \text{Im } I &\propto s_1^I \sin \phi + s_2^I \sin 2\phi \end{aligned}$$

Azimuthal Dependence of BH & DVCS



$$\frac{d^4\sigma(\ell p \rightarrow \ell p \gamma)}{dx_B dQ^2 d|t| d\phi} = \underset{\text{Well known}}{d\sigma^{BH}} + \left(d\sigma_{unpol}^{DVCS} + P_\ell d\sigma_{pol}^{DVCS} \right) + (e_\ell \text{Re } I + e_\ell P_\ell \text{Im } I)$$

Beam Charge-spin difference & sum

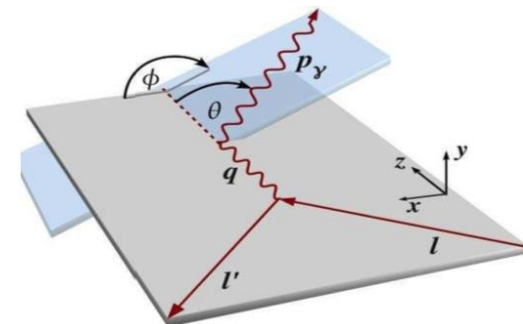
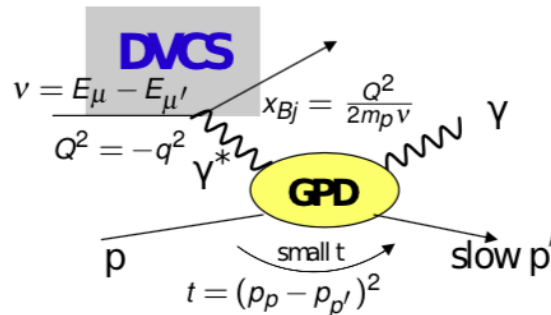
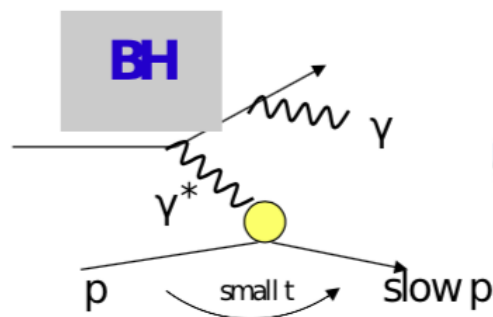
$$\mathcal{D}_{CS,u}(\phi) \equiv d\sigma(\mu^{+\leftarrow}) - d\sigma(\mu^{-\rightarrow})$$

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$$\mathcal{D}_{CS,u}(\phi)$$

Azimuthal Dependence of BH & DVCS



$$\frac{d^4\sigma(\ell p \rightarrow \ell p \gamma)}{dx_B dQ^2 d|t| d\phi} = \underset{\text{Well known}}{d\sigma^{BH}} + \left(d\sigma_{unpol}^{DVCS} + P_\ell d\sigma_{pol}^{DVCS} \right) + (e_\ell \text{Re } I + e_\ell P_\ell \text{Im } I)$$

Beam Charge-spin difference & sum

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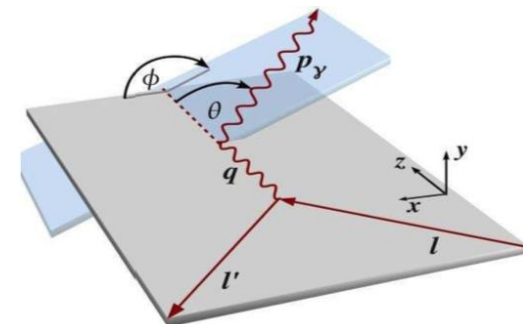
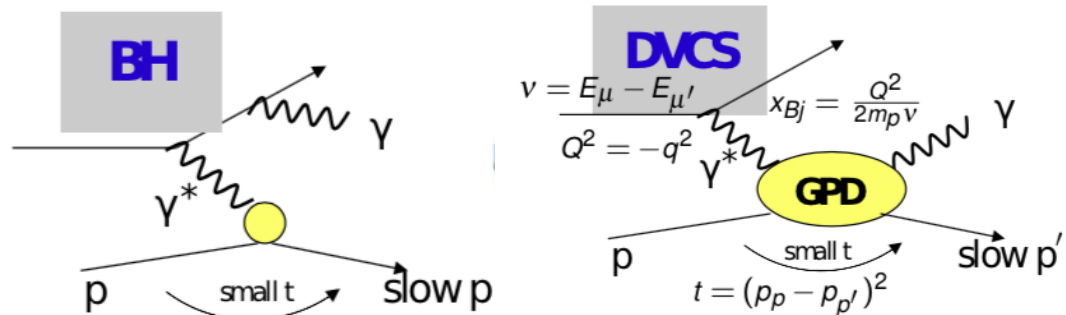
$$\text{Re } I \propto c_0^I + c_1^I \cos \phi + c_2^I \cos 2\phi + c_3^I \cos 3\phi$$

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$\mathcal{S}_{CS,u}(\phi)$

$\mathcal{S}_{CS,u}(\phi)$

Azimuthal Dependence of BH & DVCS



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Beam Charge-spin difference & sum

$$\mathcal{D}_{CS,u}(\phi) \equiv d\sigma(\mu^{+\leftarrow}) - d\sigma(\mu^{-\rightarrow}) \Rightarrow \underline{C_1^I \propto \text{Re } \mathcal{F}}$$

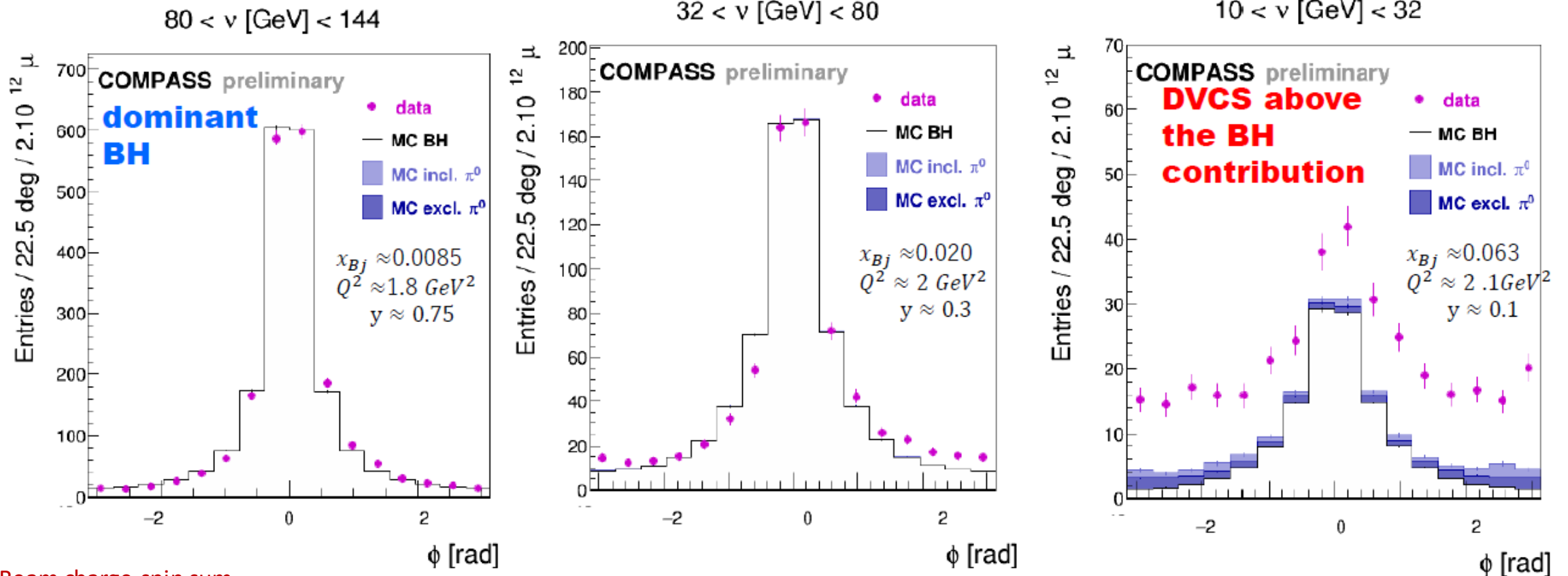
More challenging

$$\mathcal{S}_{CS,u}(\phi) \equiv d\sigma(\mu^{+\leftarrow}) + d\sigma(\mu^{-\rightarrow}) \Rightarrow \underline{C_0^{DVCS} \propto (\text{Im } \mathcal{H})^2} \text{ and } \underline{S_1^I \propto \text{Im } \mathcal{F}}$$

Easier to measure

$$\mathcal{F} = F_1 \mathcal{H} + \xi(F_1 + F_2) \mathcal{H} + t/4m^2 F_2 \mathcal{E} \xrightarrow[\text{Small } x_B \text{ at COMPASS}]{\text{Proton Target}} F_1 \mathcal{H} \quad \text{Compton Form factor linked to GPD } \mathcal{H}$$

COMPASS 2016 Preliminary Results



➤ Beam charge-spin sum

$$\begin{aligned}
 S_{CS,u}(\phi) &\equiv d\sigma(\mu^{+\leftarrow}) + d\sigma(\mu^{-\rightarrow}) = 2[d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + \text{Im } I] \\
 &= 2[d\sigma^{BH} + c_0^{DVCS} + c_1^{DVCS} \cos \phi + c_2^{DVCS} \cos 2\phi + s_1^I \sin \phi + s_2^I \sin 2\phi]
 \end{aligned}$$

$$c_0^{DVCS} \underset{\text{small } x_{Bj}}{\propto} 4(\mathcal{H}\mathcal{H}^* + \tilde{\mathcal{H}}\tilde{\mathcal{H}}^*) + \frac{t}{M^2} \mathcal{E}\mathcal{E}^* \underset{\text{model dependent}}{\rightarrow} 4 (\text{Im } \mathcal{H})^2$$

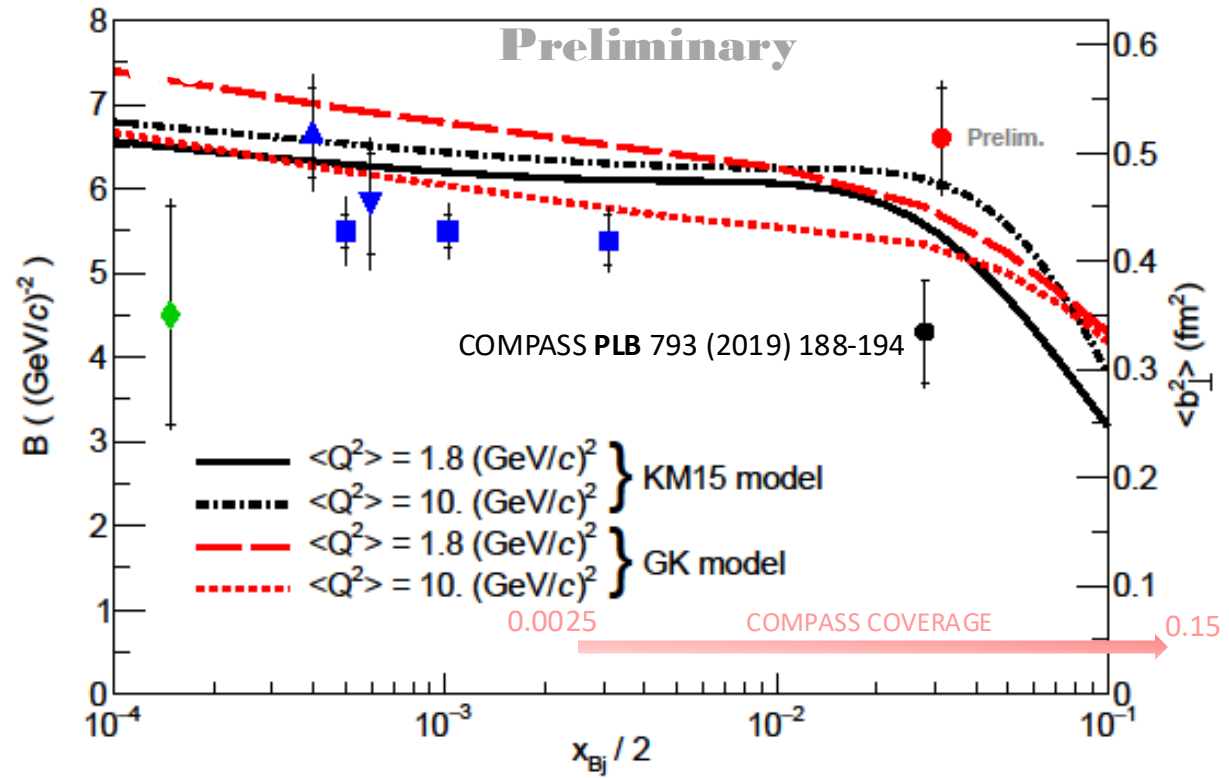
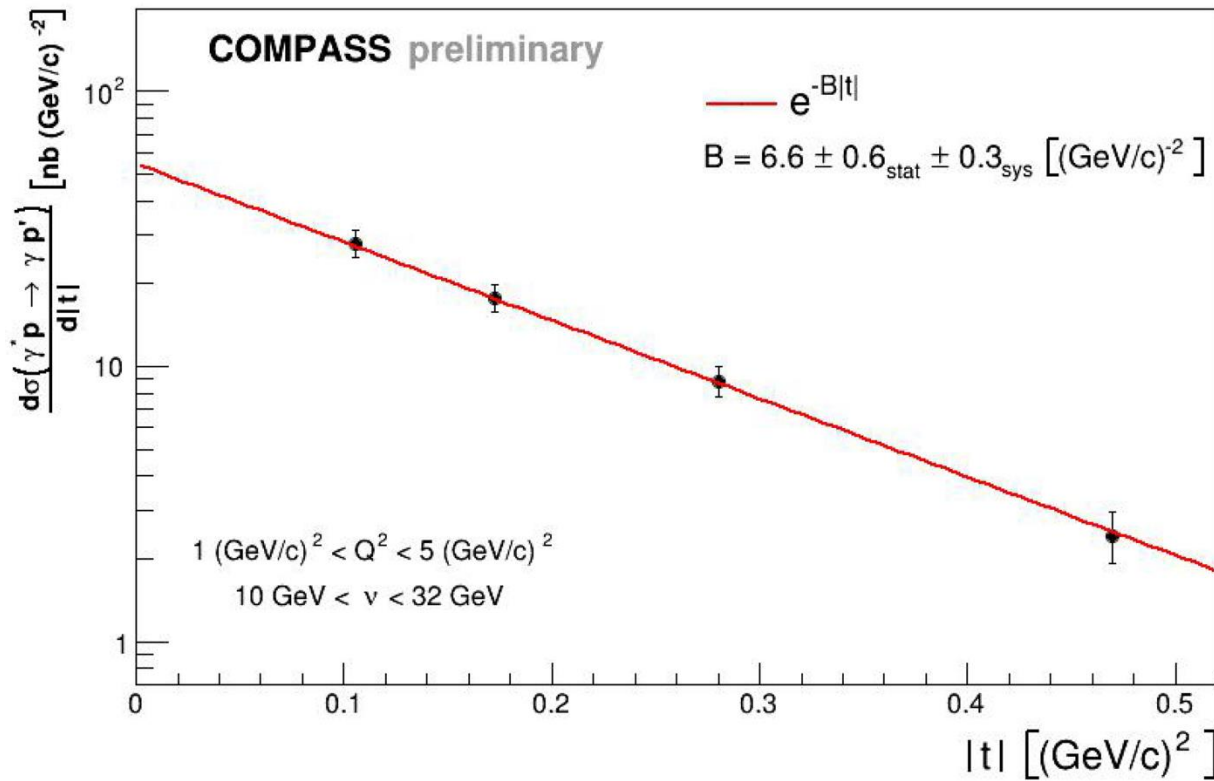
Transverse extension of partons – 2016 data



$$d\sigma^{DVCS}/d|t| \propto e^{-B|t|}$$

$$\langle r_{\perp}^2(x_B) \rangle \approx 2B(x_B) \quad \text{At small } x_B$$

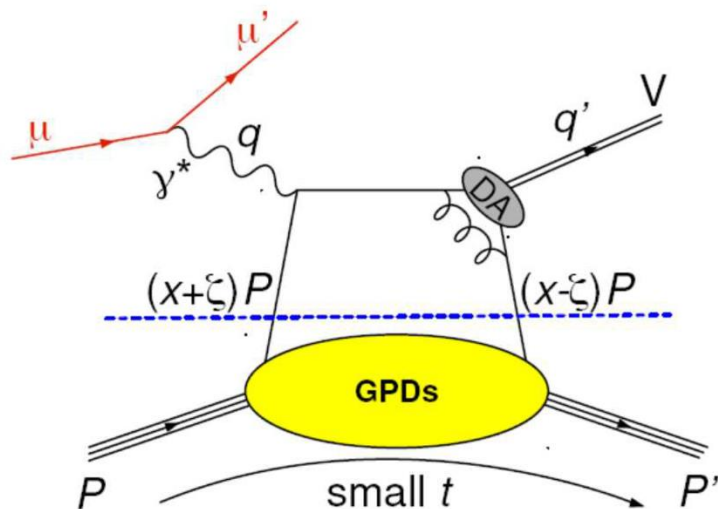
- COMPASS: $\langle Q^2 \rangle = 1.8 \text{ (GeV/c)}^2$
- ◆ ZEUS: $\langle Q^2 \rangle = 3.2 \text{ (GeV/c)}^2$
- ▲ H1: $\langle Q^2 \rangle = 4.0 \text{ (GeV/c)}^2$
- ▼ H1: $\langle Q^2 \rangle = 8.0 \text{ (GeV/c)}^2$
- H1: $\langle Q^2 \rangle = 10. \text{ (GeV/c)}^2$



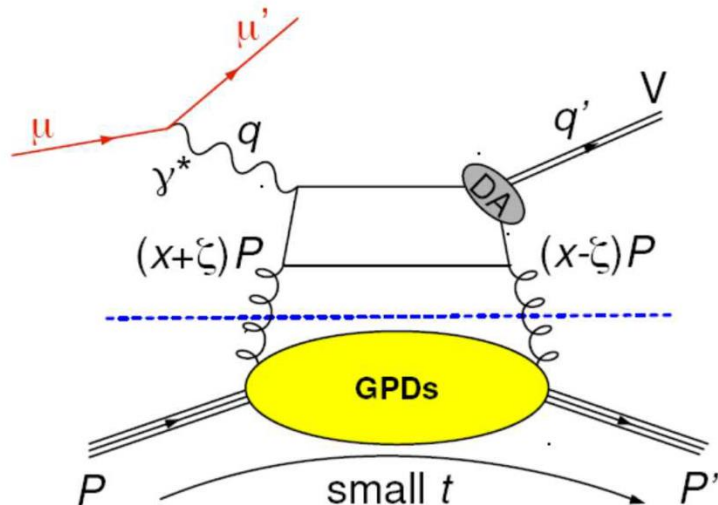
➤ The transverse-size evolution as a function of x_{Bj} → Expect at least 3 x_{Bj} bins from 2016-17 data

GPDs in Hard Exclusive Meson Production

quark contribution



gluon contribution



4 chiral-even GPDs: helicity of parton unchanged

$$\mathbf{H}^q(x, \xi, t) \quad \mathbf{E}^q(x, \xi, t) \quad \rightarrow \text{Vector Meson}$$

$$\tilde{\mathbf{H}}^q(x, \xi, t) \quad \tilde{\mathbf{E}}^q(x, \xi, t) \quad \rightarrow \text{Pseudo-Scalar Meson}$$

+ 4 chiral-odd (transversity) GPDs: helicity of parton changed
(not possible in DVCS)

$$\begin{aligned} \mathbf{H}_T^q(x, \xi, t) & \quad \mathbf{E}_T^q(x, \xi, t) \\ \tilde{\mathbf{H}}_T^q(x, \xi, t) & \quad \tilde{\mathbf{E}}_T^q(x, \xi, t) \end{aligned} \quad \bar{\mathbf{E}}_T^q = 2 \tilde{\mathbf{H}}_T^q + \mathbf{E}_T^q$$

- Ability to probe the chiral-odd GPDs.
- Universality of GPDs, quark flavor filter
- In addition to nuclear structure, provide insights into reaction mechanism.
- Additional non-perturbative term from meson wave function.

Exclusive π^0 Production on Unpolarized Proton



$\mu p \rightarrow \mu \pi^0 p$

$$\frac{d^2\sigma}{dt d\phi_\pi} = \frac{1}{2\pi} \left[\left(\frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right) + \epsilon \cos 2\phi_\pi \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_\pi \frac{d\sigma_{LT}}{dt} \right]$$

ϵ : degree of longitudinal polarization

$$\frac{d\sigma_L}{dt} = \frac{4\pi\alpha}{k'} \frac{1}{Q^6} \left\{ (1 - \xi^2) |\langle \tilde{H} \rangle|^2 - 2\xi^2 \text{Re} [\langle \tilde{H} \rangle^* \langle \tilde{E} \rangle] - \frac{t'}{4m^2} \xi^2 |\langle \tilde{E} \rangle|^2 \right\}$$

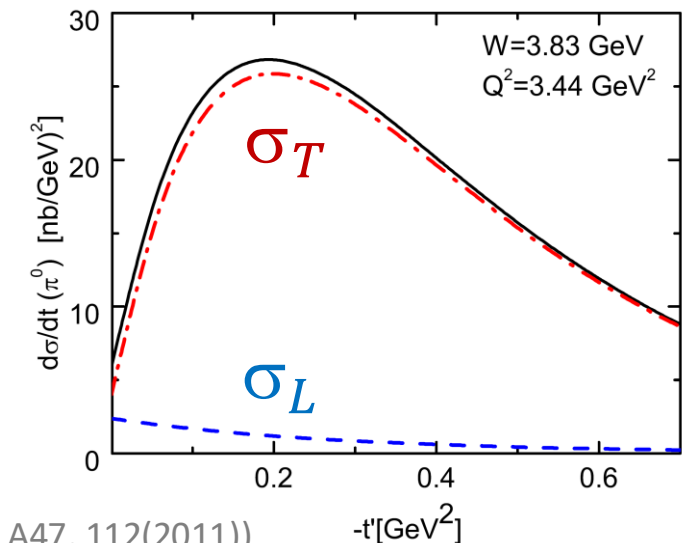
Leading twist expected be dominant
But measured as \approx only a few % of $\frac{d\sigma_T}{dt}$

The other contributions arise from coupling between chiral-odd (quark helicity flip) GPDs to the **twist-3** pion amplitude

$$\frac{d\sigma_T}{dt} = \frac{4\pi\alpha}{2k'} \frac{\mu_\pi^2}{Q^8} \left[(1 - \xi^2) |\langle H_T \rangle|^2 - \frac{t'}{8m^2} |\langle \bar{E}_T \rangle|^2 \right]$$

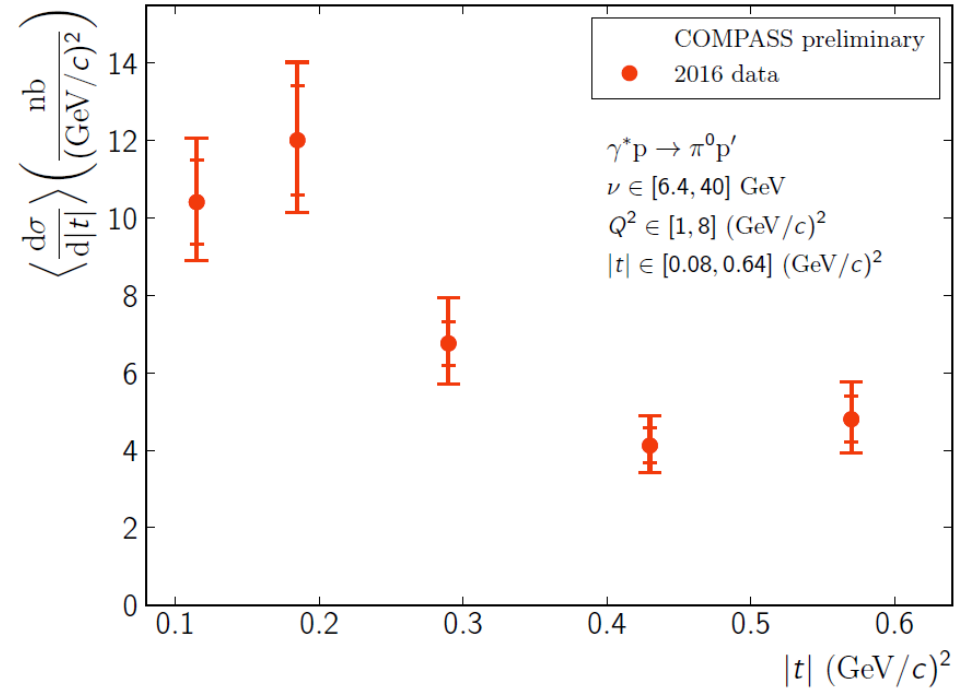
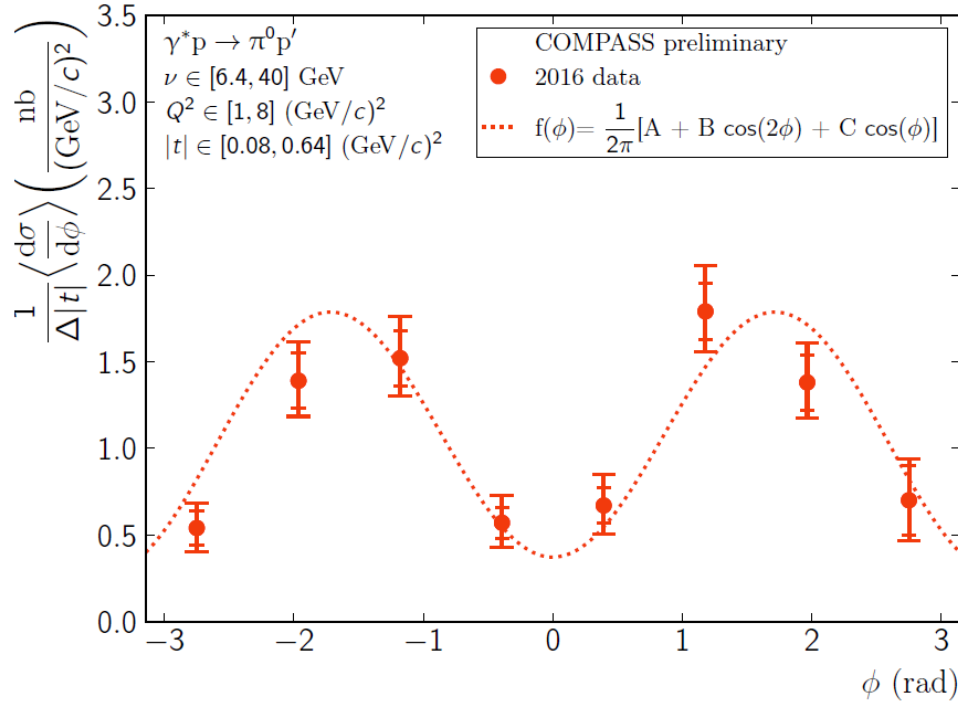
$$\frac{\sigma_{LT}}{dt} = \frac{4\pi\alpha}{\sqrt{2}k'} \frac{\mu_\pi}{Q^7} \xi \sqrt{1 - \xi^2} \frac{\sqrt{-t'}}{2m} \text{Re} [\langle H_T \rangle^* \langle \tilde{E} \rangle]$$

$$\frac{\sigma_{TT}}{dt} = \frac{4\pi\alpha}{k'} \frac{\mu_\pi^2}{Q^8} \frac{t'}{16m^2} |\langle \bar{E}_T \rangle|^2$$



New 2016 Exclusive π^0 Prod. on Unpolarized Proton

➤ Kinematic domain: $\nu \in [6.4, 40]$ GeV and $Q^2 \in [1, 8]$ GeV^2/c^2 , $\langle x_B \rangle = 0.134$



$\mu p \rightarrow \mu \pi^0 p$

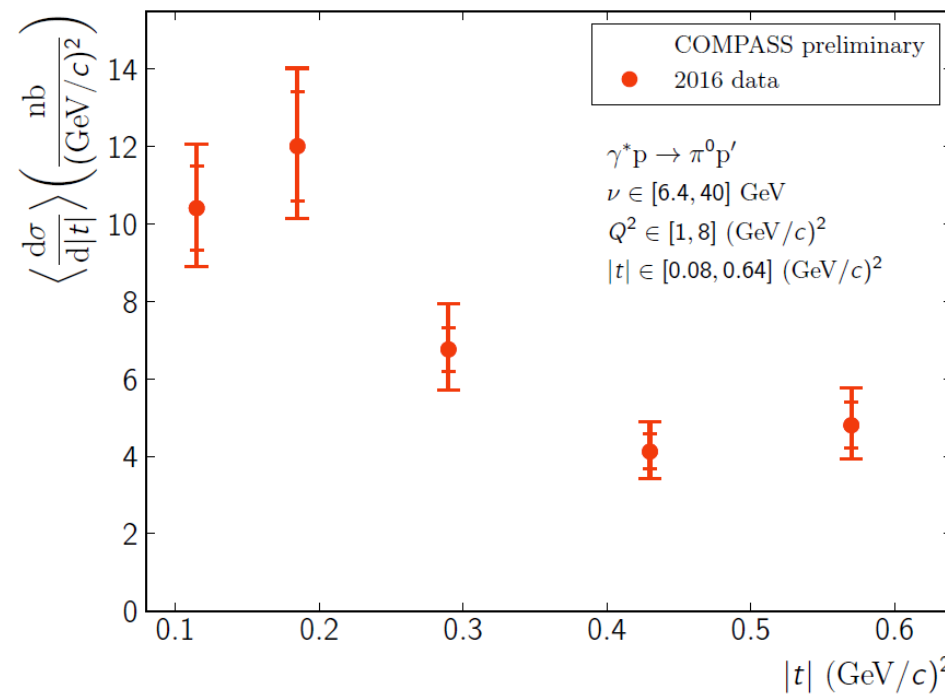
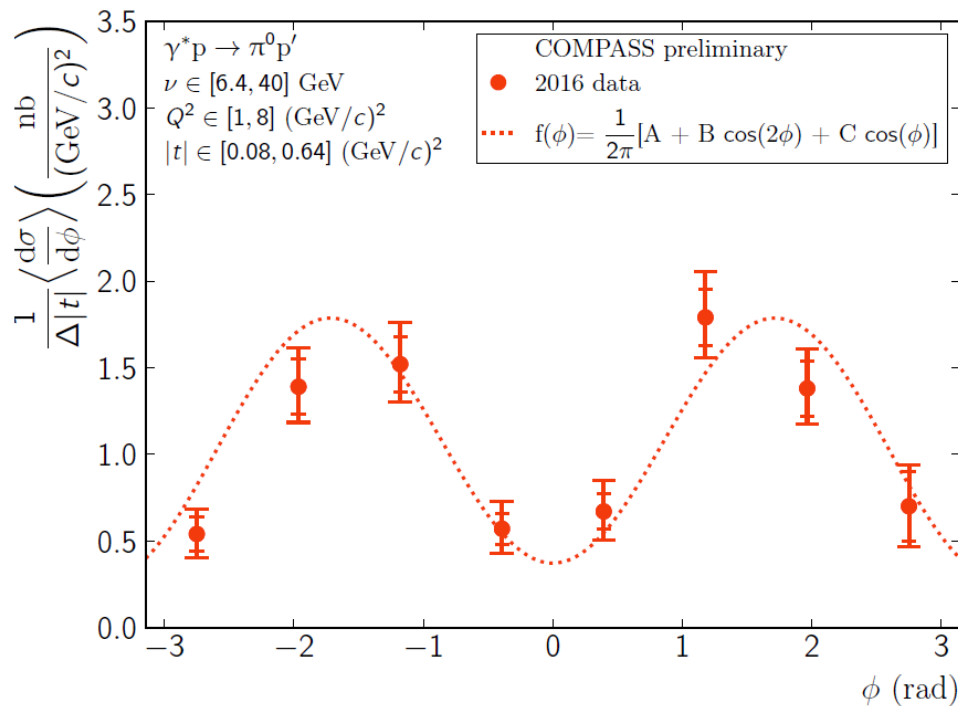
$$\frac{d^2\sigma}{dt d\phi_\pi} = \frac{1}{2\pi} \left[\left(\frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right) + \epsilon \cos 2\phi_\pi \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_\pi \frac{d\sigma_{LT}}{dt} \right]$$

Chiral-odd GPDs

New 2016 Exclusive π^0 Prod. on Unpolarized Proton



- Kinematic domain: $\nu \in [6.4, 40]$ GeV and $Q^2 \in [1, 8]$ GeV^2/c^2 , $\langle x_B \rangle = 0.134$



$$\left\langle \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right\rangle = \left(6.6 \pm 0.3_{\text{stat}}^{+0.9}_{-0.8} \Big|_{\text{sys}} \right) \frac{\text{nb}}{(\text{GeV}/c)^2}$$

$$\left\langle \frac{d\sigma_{TT}}{dt} \right\rangle = \left(-4.6 \pm 0.5_{\text{stat}}^{+0.3}_{-0.3} \Big|_{\text{sys}} \right) \frac{\text{nb}}{(\text{GeV}/c)^2}$$

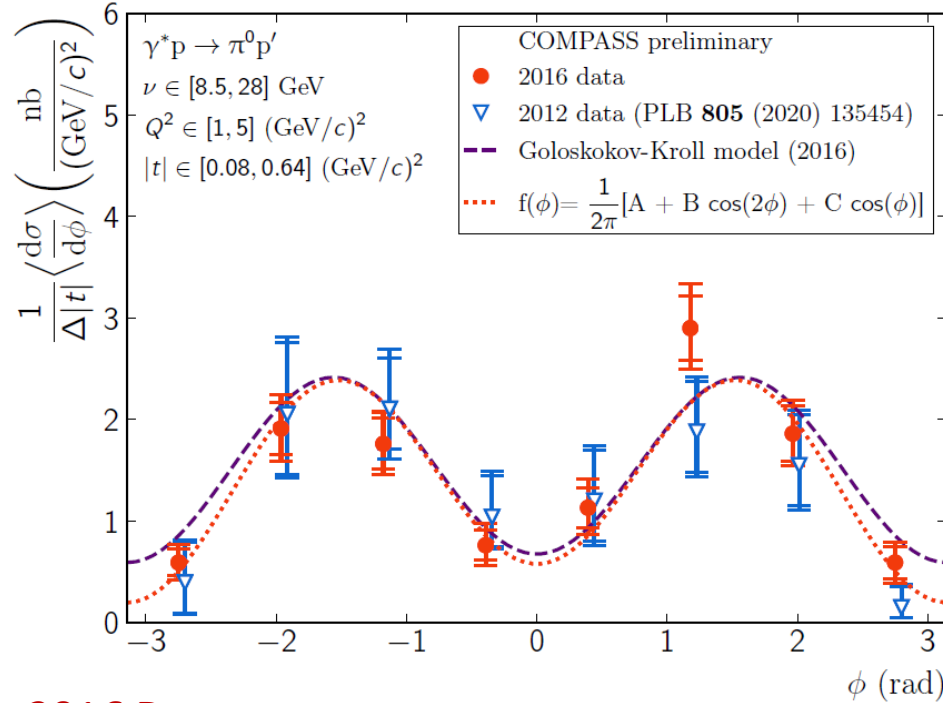
$$\left\langle \frac{d\sigma_{LT}}{dt} \right\rangle = \left(0.2 \pm 0.2_{\text{stat}}^{+0.2}_{-0.2} \Big|_{\text{sys}} \right) \frac{\text{nb}}{(\text{GeV}/c)^2}$$

$$\langle \epsilon \rangle = 0.997$$

- Cross section extracted in a larger (ν, Q^2) domain, compared with the 2012 result. (COMPASS, **PLB** 805 (2020) 135454)
- Comparable $|\sigma_{TT}|$ and $\sigma_T + \epsilon\sigma_L$

2012-16 Exclusive π^0 Prod. Comparison

➤ Kinematic domain: $\nu \in [8.5, 28]$ GeV and $Q^2 \in [1, 5]$ GeV^2/c^2 , $\langle x_B \rangle = 0.10$



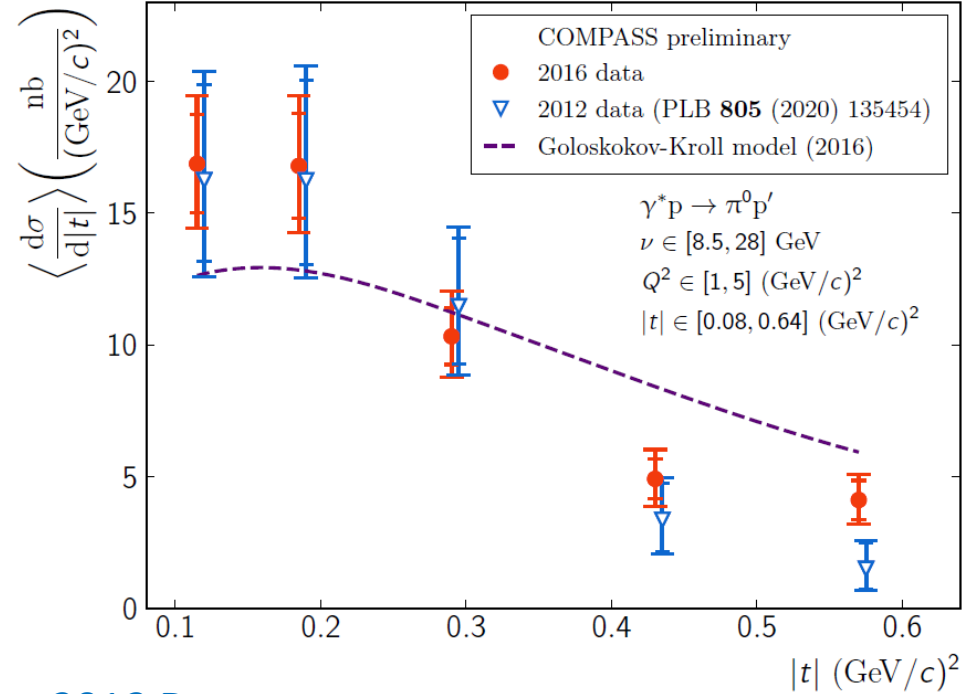
2016 Data:

$$\left\langle \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right\rangle = \left(8.7 \pm 0.5_{\text{stat}}^{+1.0}_{-1.0} \Big|_{\text{sys}} \right) \frac{\text{nb}}{(\text{GeV}/c)^2}$$

$$\left\langle \frac{d\sigma_{TT}}{dt} \right\rangle = \left(-6.3 \pm 0.8_{\text{stat}}^{+0.4}_{-0.5} \Big|_{\text{sys}} \right) \frac{\text{nb}}{(\text{GeV}/c)^2}$$

$$\left\langle \frac{d\sigma_{LT}}{dt} \right\rangle = \left(0.6 \pm 0.3_{\text{stat}}^{+0.3}_{-0.3} \Big|_{\text{sys}} \right) \frac{\text{nb}}{(\text{GeV}/c)^2}$$

$$\langle \epsilon \rangle = 0.996$$



2012 Data:

$$\left\langle \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right\rangle = \left(8.1 \pm 0.9_{\text{stat}}^{+1.1}_{-1.0} \Big|_{\text{sys}} \right) \frac{\text{nb}}{(\text{GeV}/c)^2}$$

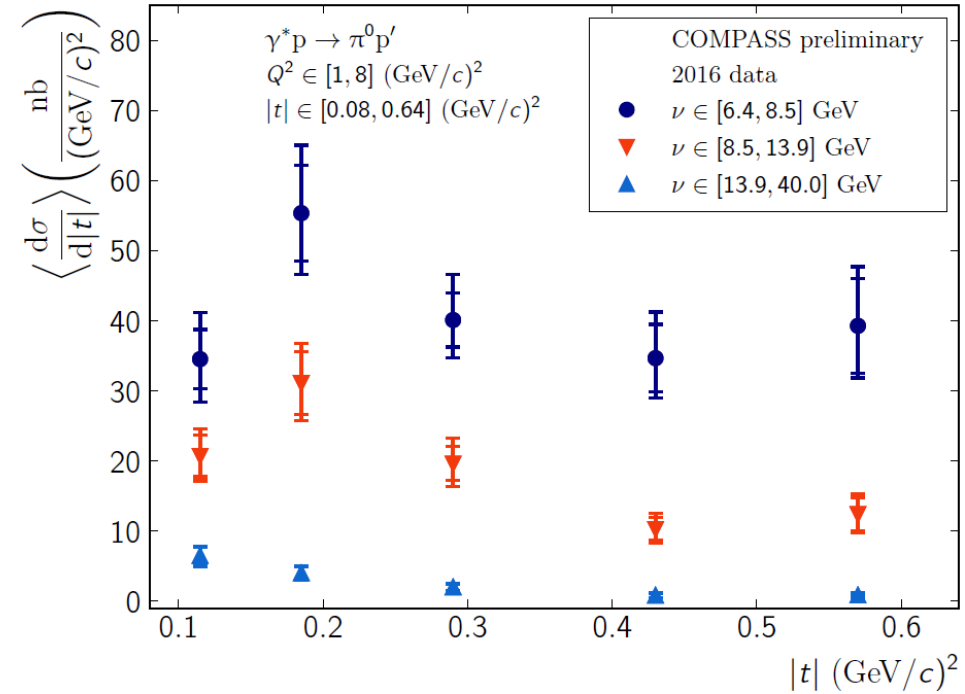
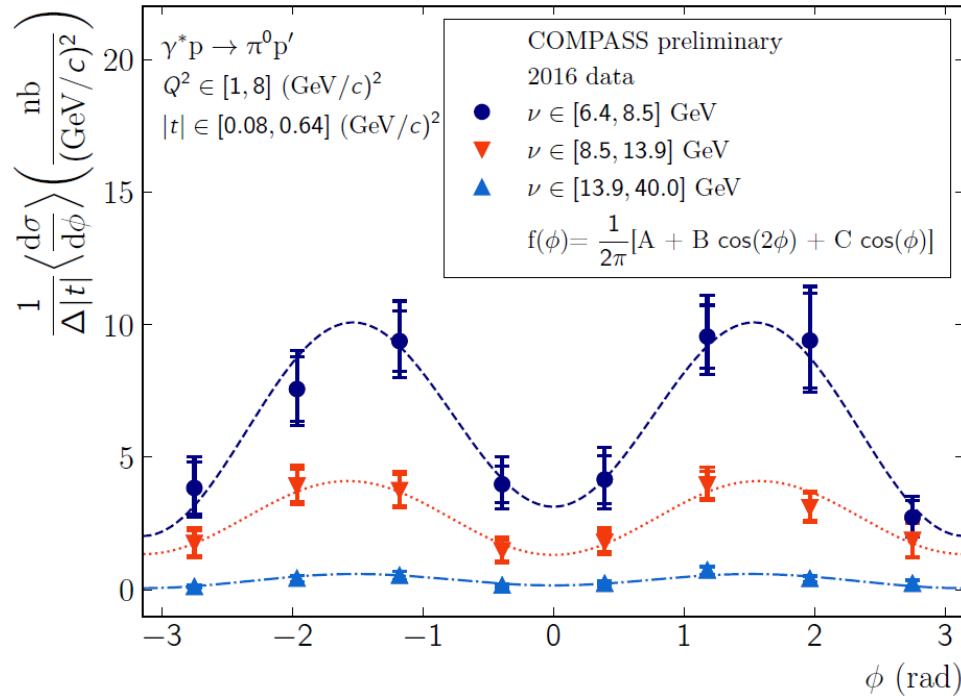
$$\left\langle \frac{d\sigma_{TT}}{dt} \right\rangle = \left(-6.0 \pm 1.3_{\text{stat}}^{+0.7}_{-0.7} \Big|_{\text{sys}} \right) \frac{\text{nb}}{(\text{GeV}/c)^2}$$

$$\left\langle \frac{d\sigma_{LT}}{dt} \right\rangle = \left(1.4 \pm 0.5_{\text{stat}}^{+0.3}_{-0.2} \Big|_{\text{sys}} \right) \frac{\text{nb}}{(\text{GeV}/c)^2}$$

$$\langle \epsilon \rangle = 0.996$$

New 2016 Exclusive π^0 Cross-section Evolution with ν

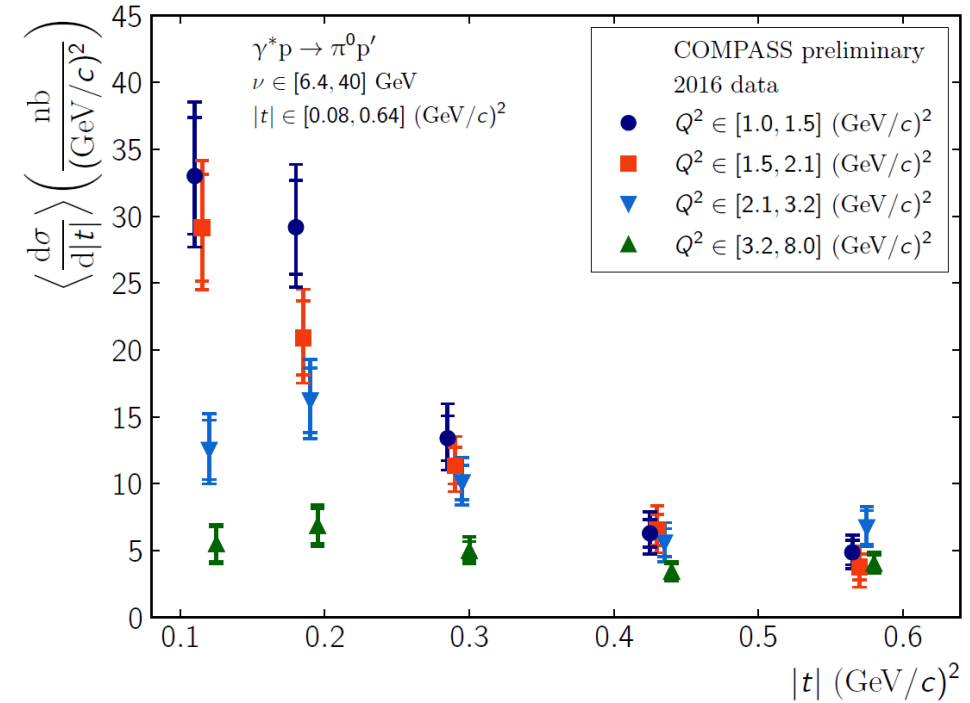
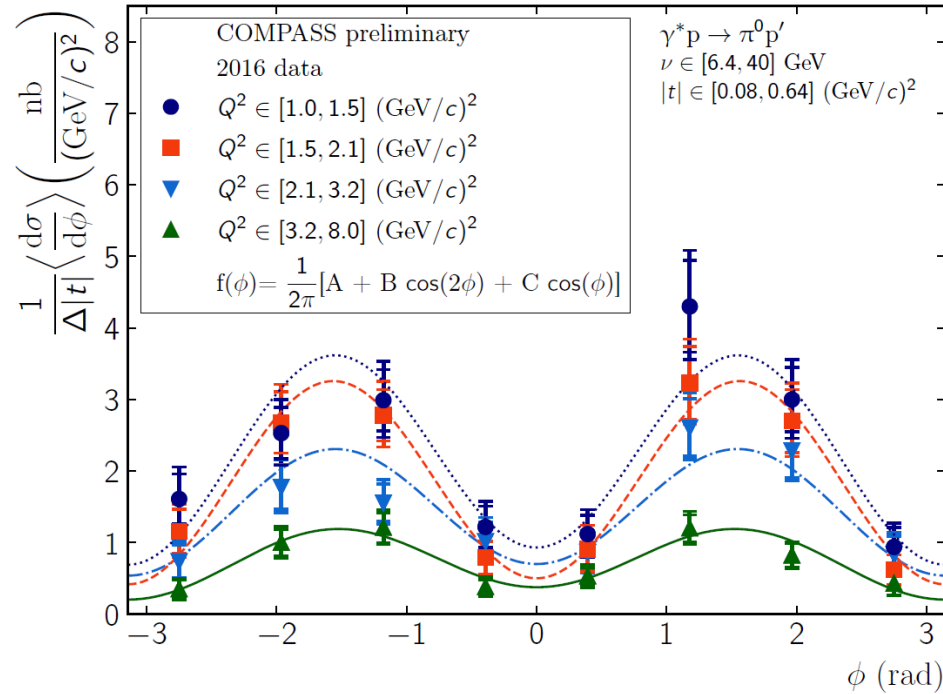
➤ Cross section decreases with increasing ν



	$\langle \nu \rangle$ [GeV]	$\langle Q^2 \rangle$ [GeV ² /c ²]	$\langle x_B \rangle$	$\langle \epsilon \rangle$
$\nu \in [6.4, 8.5]$	7.35	2.15	0.156	0.999
$\nu \in [8.5, 13.9]$	10.32	2.50	0.131	0.998
$\nu \in [13.9, 40.0]$	21.08	2.09	0.057	0.989

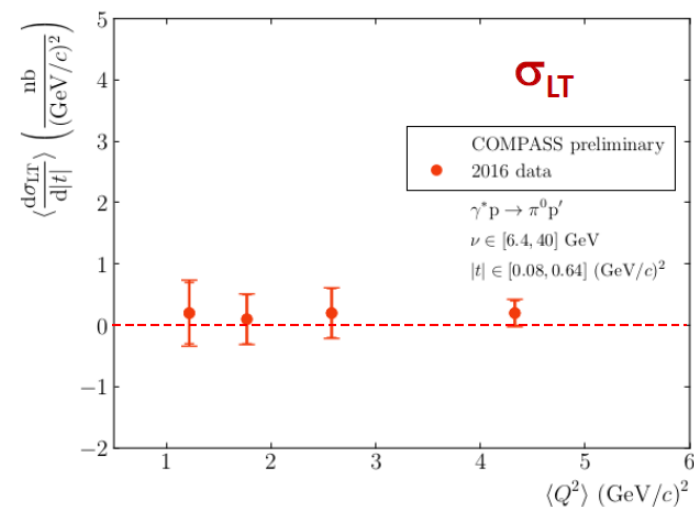
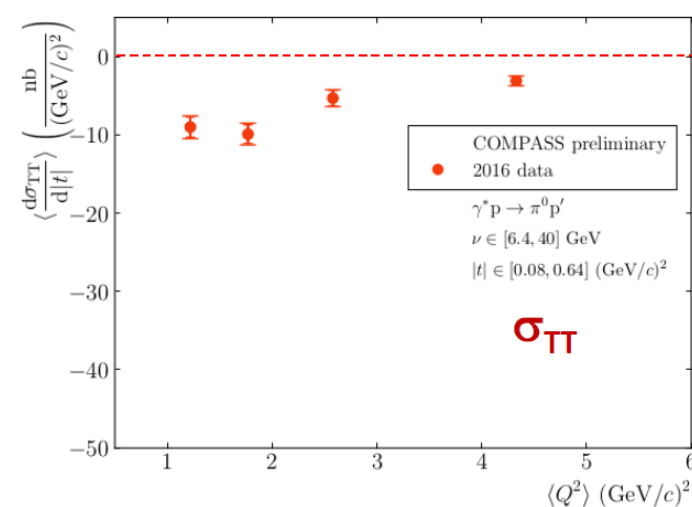
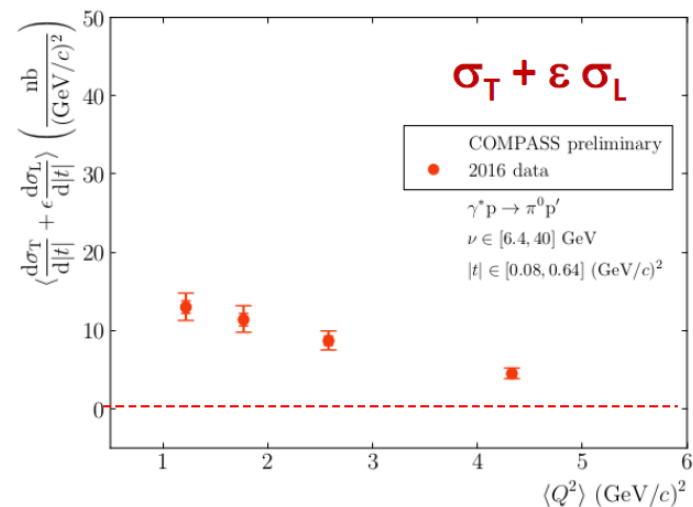
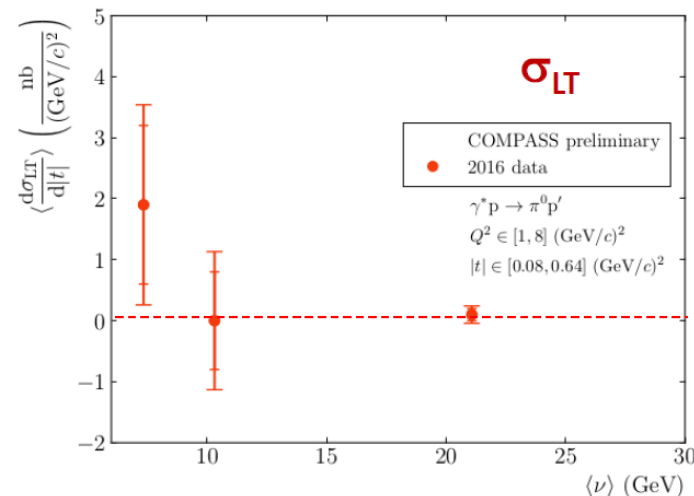
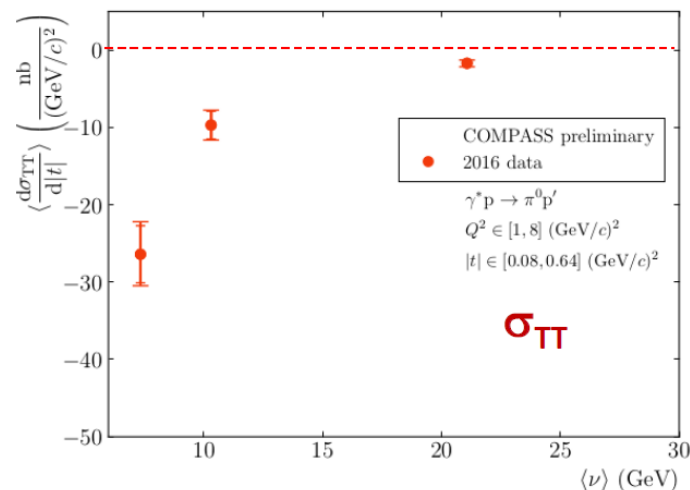
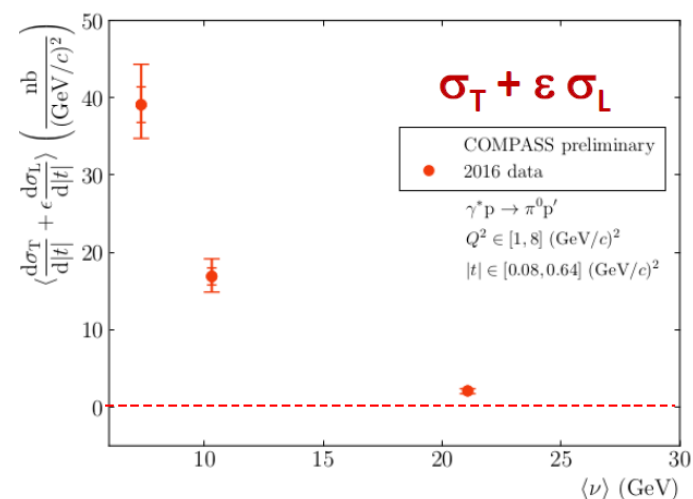
New 2016 Exclusive π^0 Cross-section Evolution with Q^2

➤ Cross section decreases with increasing Q^2



	$\langle Q^2 \rangle \text{ [GeV}^2/\text{c}^2]$	$\langle \nu \rangle \text{ [GeV]}$	$\langle x_B \rangle$	$\langle \epsilon \rangle$
$Q^2 \in [1.0, 1.5]$	1.22	10.54	0.072	0.997
$Q^2 \in [1.5, 2.1]$	1.77	9.81	0.109	0.997
$Q^2 \in [2.1, 3.2]$	2.58	9.82	0.157	0.997
$Q^2 \in [3.2, 8.0]$	4.33	10.39	0.247	0.997

New 2016 Evolution of the Structure Functions

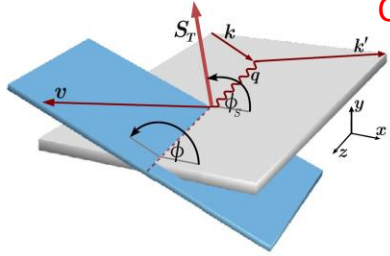


For both $\sigma_T + \epsilon \sigma_L$ and σ_{TT}
 \rightarrow Relatively larger evolution in ν , smaller in Q^2

σ_{LT} consistent with 0

2007 & 2010 HEMP with Transversely Polarized Target

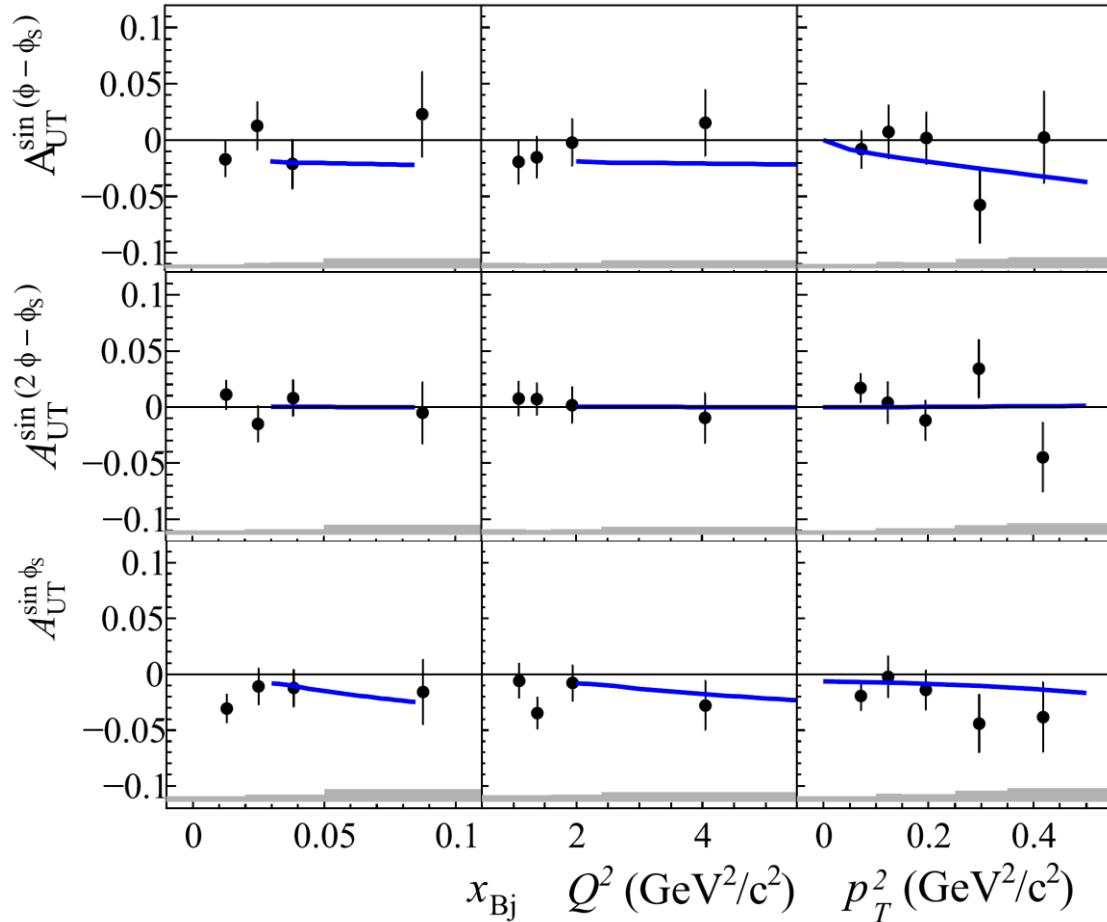
COMPASS, **NPB** 865 (2012) 1-20, **PLB** 731 (2014) 19



$$\rho^0 \rightarrow \pi^+ \pi^-$$

$$E_{\rho^0} = \frac{1}{\sqrt{2}} \left(\frac{2}{3} E^u + \frac{1}{3} E^d + \frac{3}{4} E^g / x \right)$$

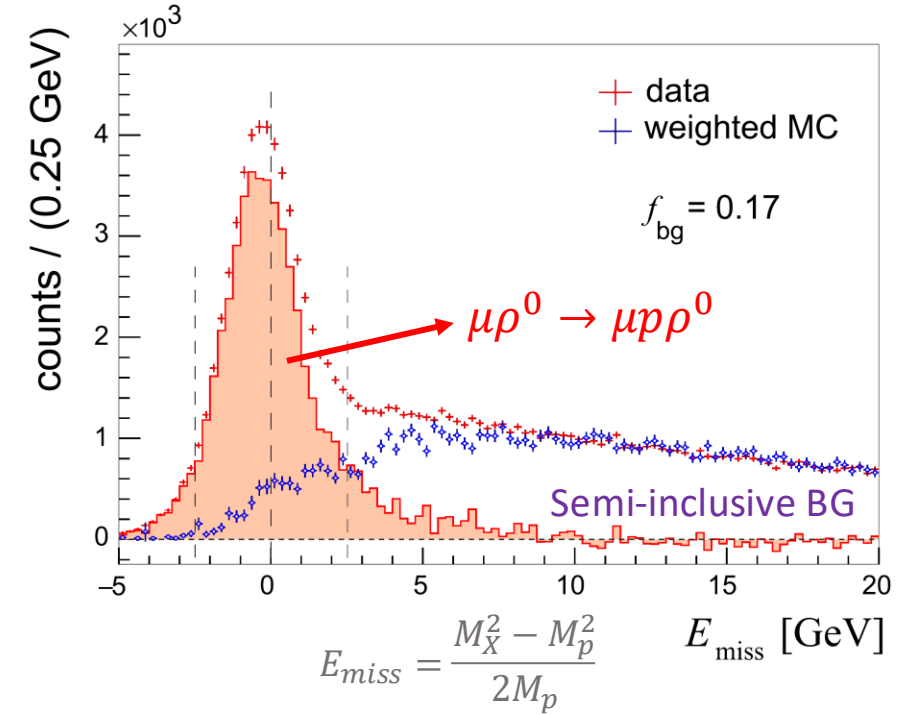
➤ Exclusivity ensured by “missing mass technique”



$$\propto \text{Im}(E^* H)$$

$$\propto \text{Im}(E^* \bar{E}_T)$$

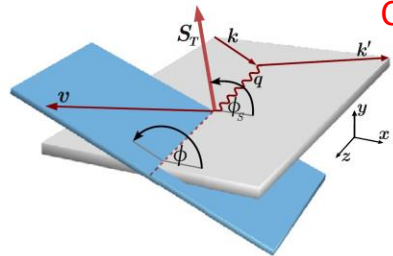
$$\propto \text{Im}(E^* \bar{E}_T - H^* H_T)$$



➤ Sensibility to E and H_T

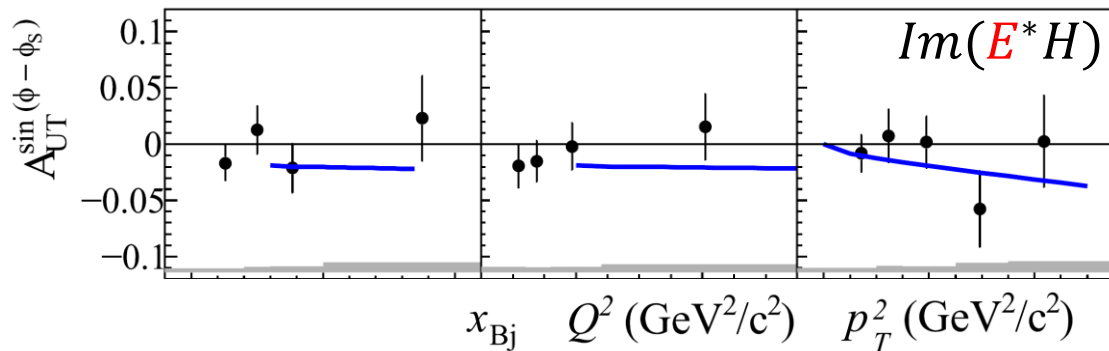
2007 & 2010 HEMP with Transversely Polarized Target

COMPASS, NPB 865 (2012) 1-20, PLB 731 (2014) 19



$$\rho^0 \rightarrow \pi^+ \pi^-$$

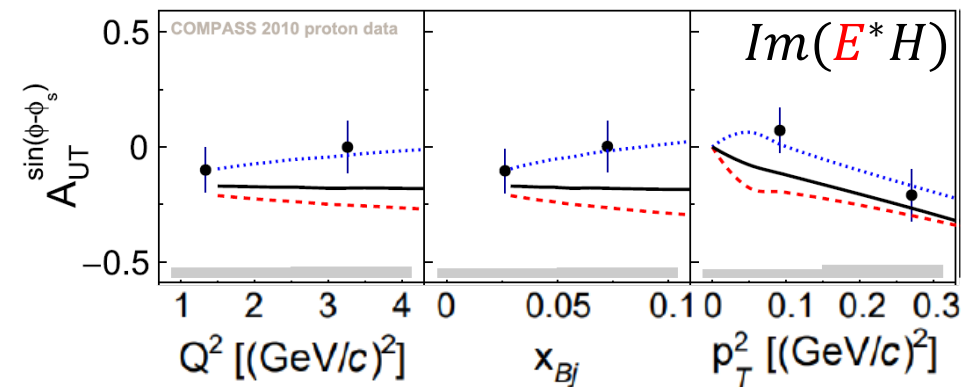
$$E_{\rho^0} = \frac{1}{\sqrt{2}} \left(\frac{2}{3} E^u + \frac{1}{3} E^d + \frac{3}{4} E^g / x \right)$$



COMPASS, NPB 865 (2012) 1-20, PLB 731 (2014) 19

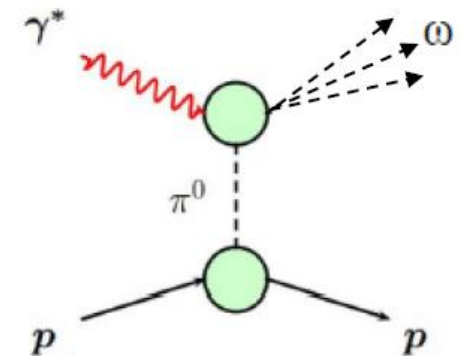
$$\omega \rightarrow \pi^+ \pi^- \pi^0$$

$$E_{\omega} = \frac{1}{\sqrt{2}} \left(\frac{2}{3} E^u - \frac{1}{3} E^d + \frac{1}{4} E^g / x \right)$$

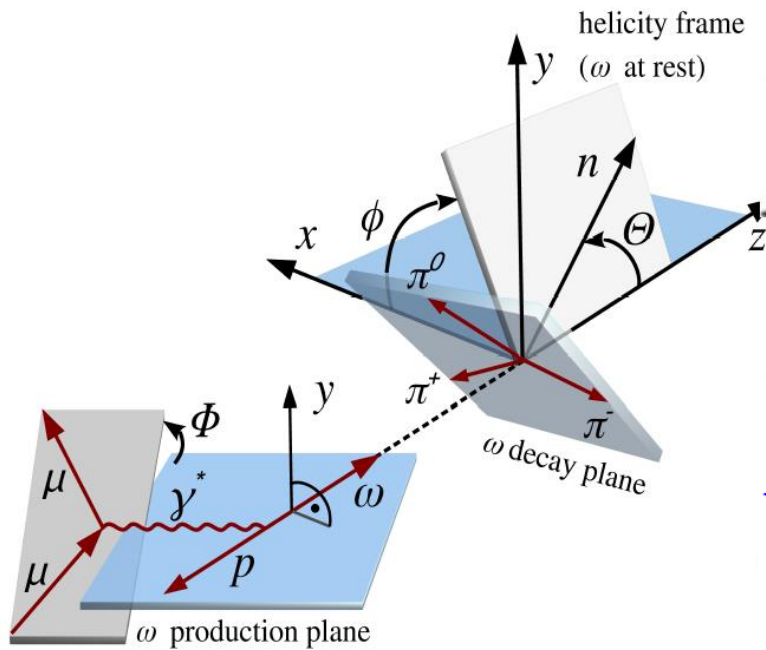


— No pion pole Negative $\pi\omega$ form factor
 - - - Positive $\pi\omega$ form factor

- E^u and E^d are of opposite sign $\rightarrow \omega$ is more promising for GPD study
- Nevertheless, obscured by the inherent pion pole contribution



Exclusive ω Production on Unpolarized Proton



Experimental angular distributions

$$\mathcal{W}^{U+L}(\Phi, \phi, \cos \Theta) = \mathcal{W}^U(\Phi, \phi, \cos \Theta) + P_b \mathcal{W}^L(\Phi, \phi, \cos \Theta)$$

15 unpolarized SDMEs in \mathcal{W}^U and 8 polarized in \mathcal{W}^L

$$\begin{aligned} \mathcal{W}^U(\Phi, \phi, \cos \Theta) = & \frac{3}{8\pi^2} \left[\frac{1}{2}(1 - r_{00}^{04}) + \frac{1}{2}(3r_{00}^{04} - 1) \cos^2 \Theta - \sqrt{2} \text{Re}\{r_{10}^{04}\} \sin 2\Theta \cos \phi - r_{1-1}^{04} \sin^2 \Theta \cos 2\phi \right. \\ & - \epsilon \cos 2\Phi \left(r_{11}^1 \sin^2 \Theta + r_{00}^1 \cos^2 \Theta - \sqrt{2} \text{Re}\{r_{10}^1\} \sin 2\Theta \cos \phi - r_{1-1}^1 \sin^2 \Theta \cos 2\phi \right) \\ & - \epsilon \sin 2\Phi \left(\sqrt{2} \text{Im}\{r_{10}^2\} \sin 2\Theta \sin \phi + \text{Im}\{r_{1-1}^2\} \sin^2 \Theta \sin 2\phi \right) \\ & + \sqrt{2\epsilon(1+\epsilon)} \cos \Phi \left(r_{11}^5 \sin^2 \Theta + r_{00}^5 \cos^2 \Theta - \sqrt{2} \text{Re}\{r_{10}^5\} \sin 2\Theta \cos \phi - r_{1-1}^5 \sin^2 \Theta \cos 2\phi \right) \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \sin \Phi \left(\sqrt{2} \text{Im}\{r_{10}^6\} \sin 2\Theta \sin \phi + \text{Im}\{r_{1-1}^6\} \sin^2 \Theta \sin 2\phi \right) \right], \end{aligned}$$

$$\begin{aligned} \mathcal{W}^L(\Phi, \phi, \cos \Theta) = & \frac{3}{8\pi^2} \left[\sqrt{1-\epsilon^2} \left(\sqrt{2} \text{Im}\{r_{10}^3\} \sin 2\Theta \sin \phi + \text{Im}\{r_{1-1}^3\} \sin^2 \Theta \sin 2\phi \right) \right. \\ & + \sqrt{2\epsilon(1-\epsilon)} \cos \Phi \left(\sqrt{2} \text{Im}\{r_{10}^7\} \sin 2\Theta \sin \phi + \text{Im}\{r_{1-1}^7\} \sin^2 \Theta \sin 2\phi \right) \\ & \left. + \sqrt{2\epsilon(1-\epsilon)} \sin \Phi \left(r_{11}^8 \sin^2 \Theta + r_{00}^8 \cos^2 \Theta - \sqrt{2} \text{Re}\{r_{10}^8\} \sin 2\Theta \cos \phi - r_{1-1}^8 \sin^2 \Theta \cos 2\phi \right) \right] \end{aligned}$$

➤ $\epsilon \rightarrow 1$, small \mathcal{W}^L

2012 Exclusive ω Prod. on Unpolarized Proton



SCHC ($\lambda_\gamma = \lambda_V$)

(S-Channel Helicity Conservation)

SCHC implies:

- $r_{1-1}^1 + \text{Im} r_{1-1}^2 = 0$

$= -0.010 \pm 0.032 \pm 0.047$ OK

- $\text{Re} r_{10}^5 + \text{Im} r_{10}^6 = 0$

$= 0.014 \pm 0.011 \pm 0.013$ OK

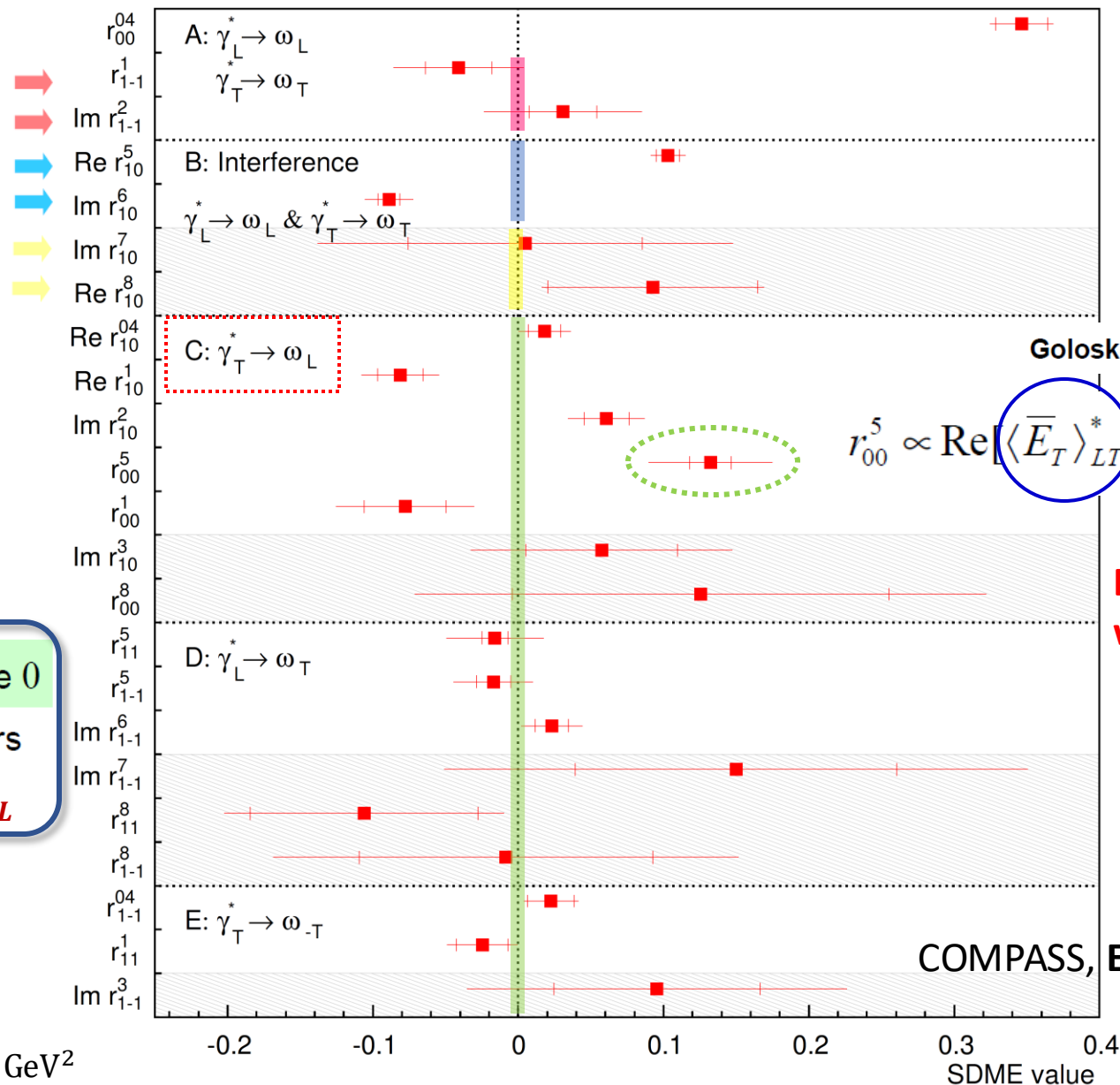
- $\text{Im} r_{10}^7 - \text{Re} r_{10}^8 = 0$

$= -0.088 \pm 0.110 \pm 0.196$ OK

- all elements of classes C, D, E should be 0

for $\gamma_L^* \rightarrow \omega_T$ and $\gamma_T^* \rightarrow \omega_{-T}$ OK within errors

NOT OBSERVED for transitions $\gamma_T^* \rightarrow \omega_L$



Goloskokov and Kroll, EPJC 74 (2014) 2725

$$r_{00}^5 \propto \text{Re}[\langle \bar{E}_T \rangle_{LT}^* \langle H \rangle_{LL} + \frac{1}{2} \langle H_T \rangle_{LT}^* \langle E \rangle_{LL}]$$

Exclusive ρ^0, ω production with trans. pol. target

COMPASS, NPB865 (2012) 1-20

COMPASS, PLB731 (2014) 19

COMPASS, NPB915 (2017) 454-475

COMPASS, Eur.Phys.J.C 81 (2021) 126

$\langle Q^2 \rangle = 2.1 \text{ GeV}^2, \langle W \rangle = 7.6 \text{ GeV}, \langle P_T^2 \rangle = 0.16 \text{ GeV}^2$

2012 Exclusive ρ^0 Prod. on Unpolarized Proton



SCHC ($\lambda_\gamma = \lambda_V$)

(S-Channel Helicity Conservation)

SCHC implies:

- $r_{1-1}^1 + \text{Im} r_{1-1}^2 = 0$

$= -0.000 \pm 0.006$

OK

- $\text{Re} r_{10}^5 + \text{Im} r_{10}^6 = 0$

$= -0.011 \pm 0.003$

Violation

- $\text{Im} r_{10}^7 - \text{Re} r_{10}^8 = 0$

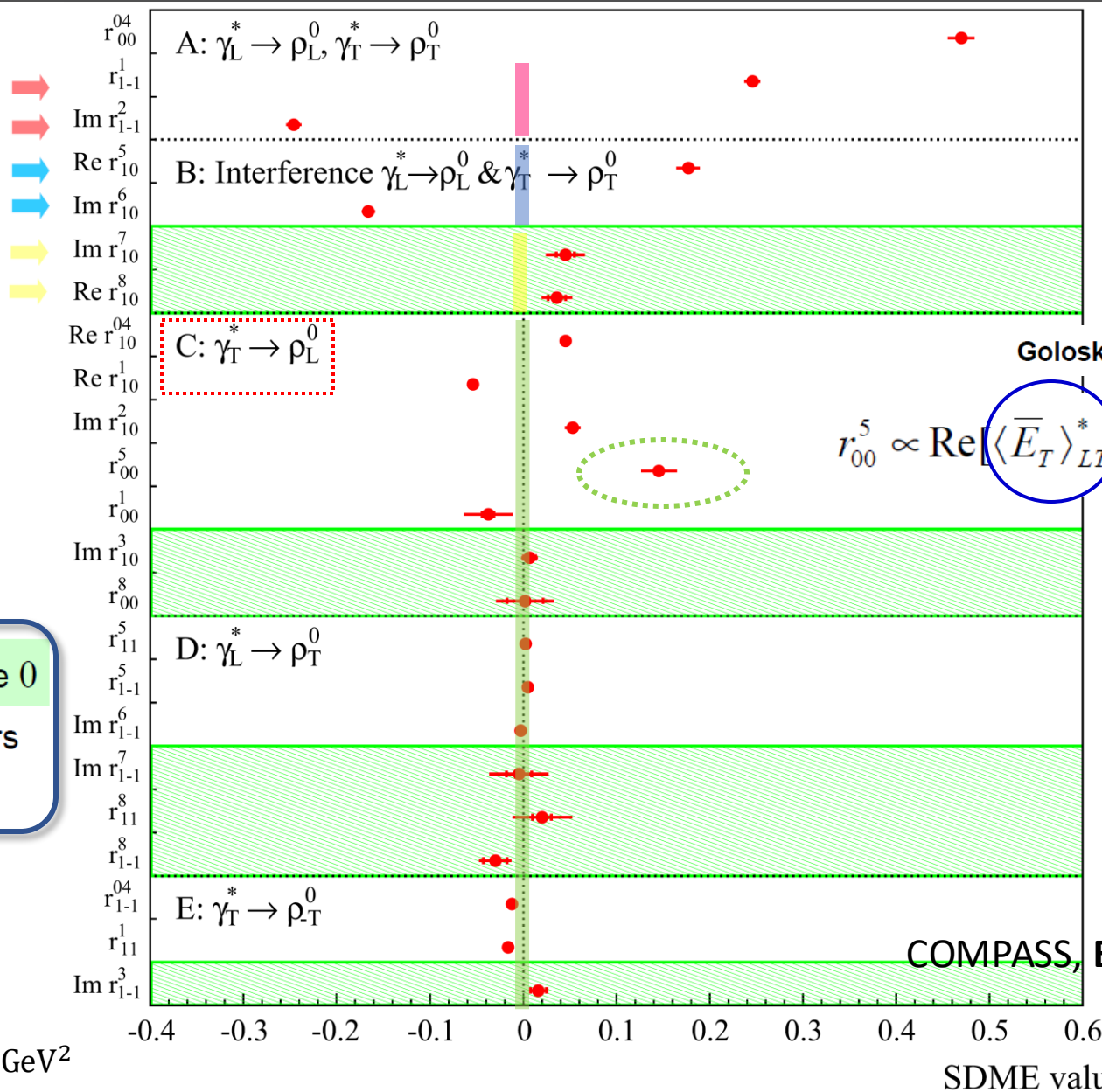
$= -0.009 \pm 0.031$

OK

- all elements of classes C, D, E should be 0

for $\gamma_L^* \rightarrow \omega_T$ and $\gamma_T^* \rightarrow \omega_{-T}$ OK within errors

NOT OBSERVED for transitions $\gamma_T^* \rightarrow \rho_L^0$



SDMEs COMPASS

Goloskokov and Kroll, EPJC 74 (2014) 2725

$$r_{00}^5 \propto \text{Re}[\langle \bar{E}_T \rangle_{LT}^* \langle H \rangle_{LL} + \frac{1}{2} \langle H_T \rangle_{LT}^* \langle E \rangle_{LL}]$$

First term dominates
→ Probes \bar{E}_T

COMPASS, Eur.Phys.J.C 83 (2023) 924

$\langle Q^2 \rangle = 2.4 \text{ GeV}^2, \langle W \rangle = 9.9 \text{ GeV}, \langle P_T^2 \rangle = 0.18 \text{ GeV}^2$

DVCS cross sections with polarized μ^+ and μ^-

- Beam charge-spin sum $\rightarrow \text{Im}\mathcal{H}(\xi,t) \rightarrow$ Transverse extension of partons as a function of x_{Bj}
- Beam charge-spin difference $\rightarrow \text{Re}\mathcal{H}(\xi,t) \rightarrow$ D-term, pressure distribution

HEMP of π^0 , ρ , ω , ϕ , J/ψ

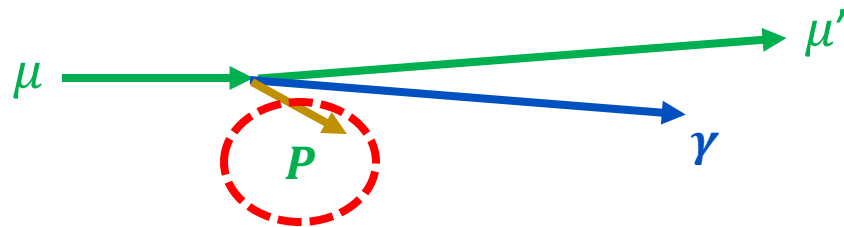
- Cross section of $\pi^0 \rightarrow$ Submitted to Physics Letters B
- SDME of ρ & $\omega \rightarrow$ Transversity GPDs & Flavor Decomposition
- ϕ , $J/\psi \rightarrow$ underway

➤ More results are coming!



Backup Slides

COMPASS 2016 Preliminary Results



$$\Delta\phi = \phi^{\text{cam.}} - \phi^{\text{spec.}}$$

Proton azimuthal angle

$$\Delta p_T = |p_T^{\text{cam.}}| - |p_T^{\text{spec.}}|$$

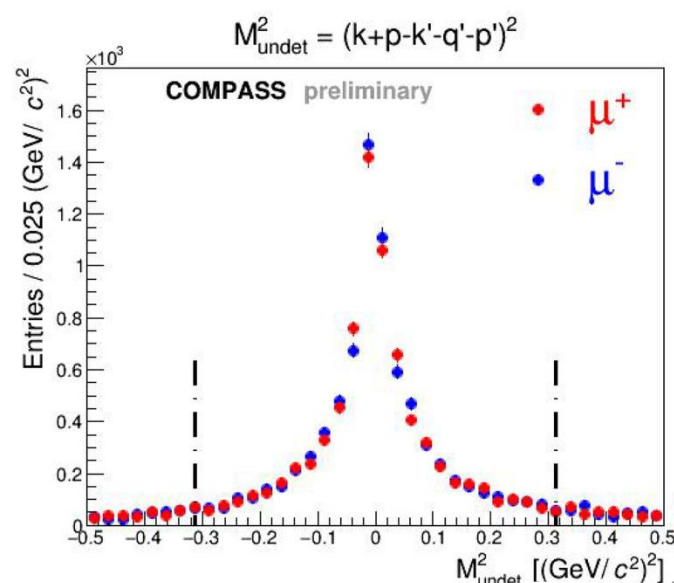
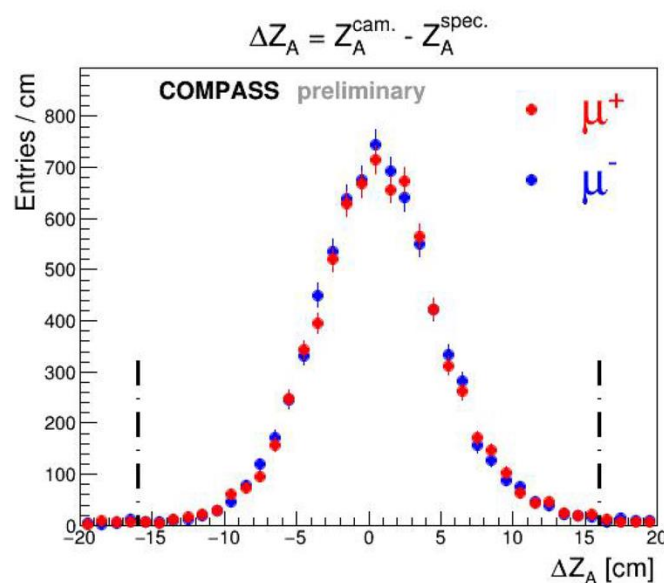
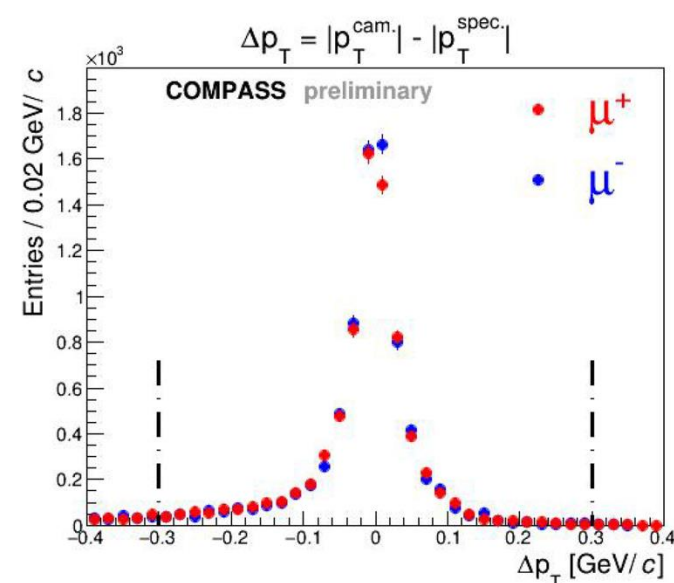
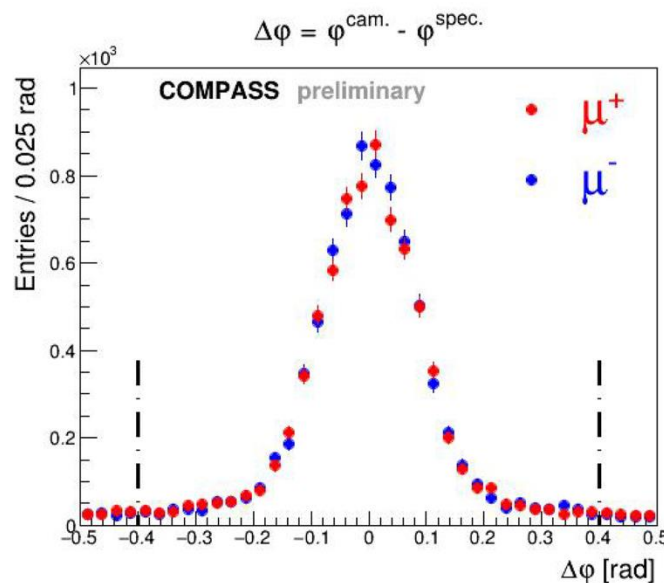
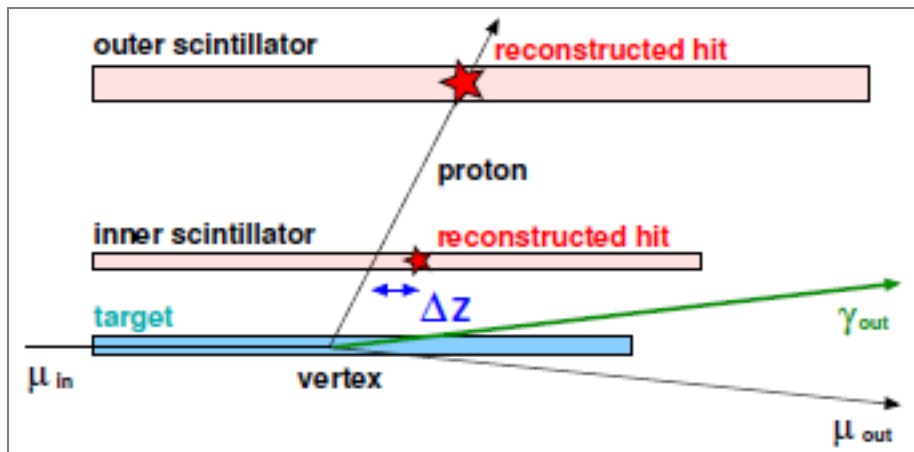
Proton momentum

$$\Delta z_A = z_A^{\text{cam.}} - z_A^{\text{spec.}}$$

Proton track position

$$M_{\text{undet}}^2 = (k + p - k' - q' - p')^2$$

Energy momentum balance



➤ Main background of exclusive single photon events: π^0 decay

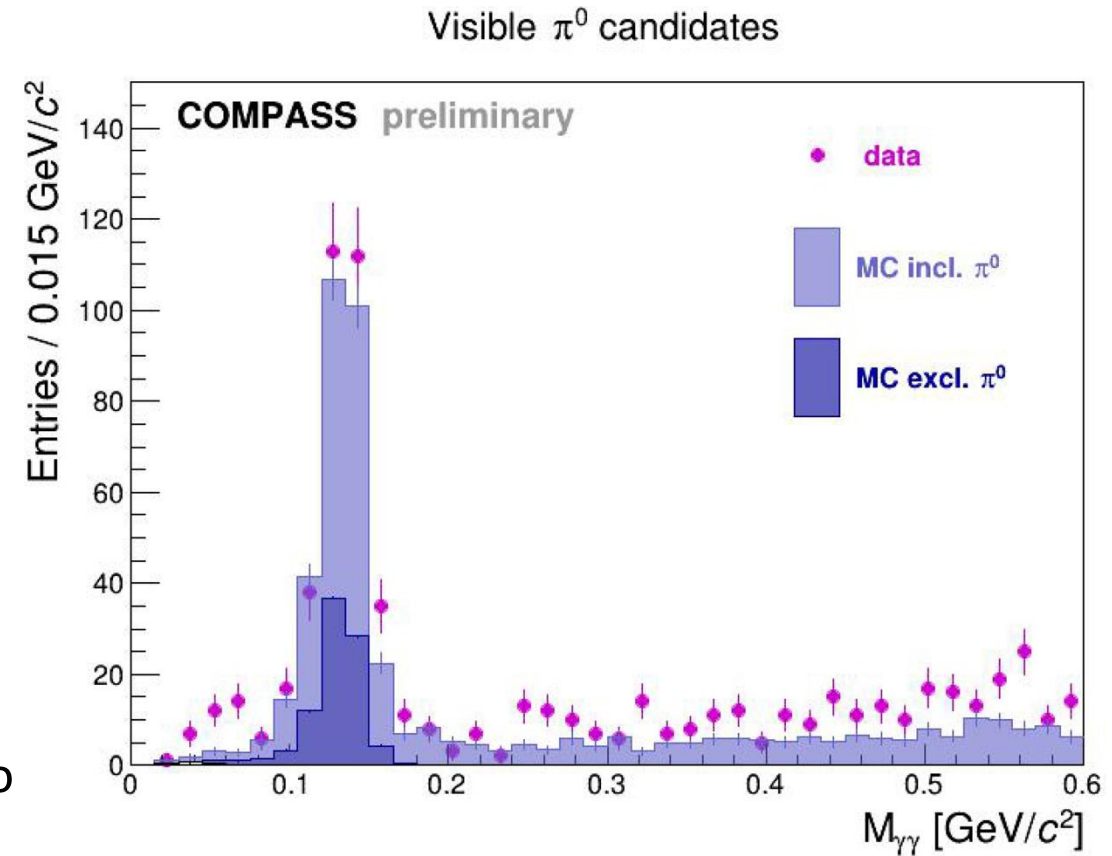
➤ Visible (both γ detected) – subtracted

A high-energy DVCS photon candidate is combined with all detected photons with energies lower than the DVCS threshold: (4,5) GeV in Ecal (0,1) respectively

➤ Invisible (one γ lost) – estimated by MC

- Semi-inclusive LEPTO 6.1
- Exclusive HEPGEN π^0 (GK model)

The sum of LEPTO and HEPGEN contributions is normalized to the π^0 peak in $M_{\gamma\gamma}$ of the real data



Beam Charge-spin Difference

$$\mathcal{D}_{CS,U}(\phi) \equiv d\sigma(\mu^{+\leftarrow}) - d\sigma(\mu^{-\rightarrow}) \rightarrow c_0^I + c_1^I \cos \phi$$

$$BCSA = \mathcal{D}_{CS,U}/S_{CS,U} = A_0 + A_{CS,U}^{\cos\phi} \cos\phi + A_2 \cos 2\phi$$

$$c_1^I \rightarrow \text{Re } F_1 \mathcal{H}$$

VGG

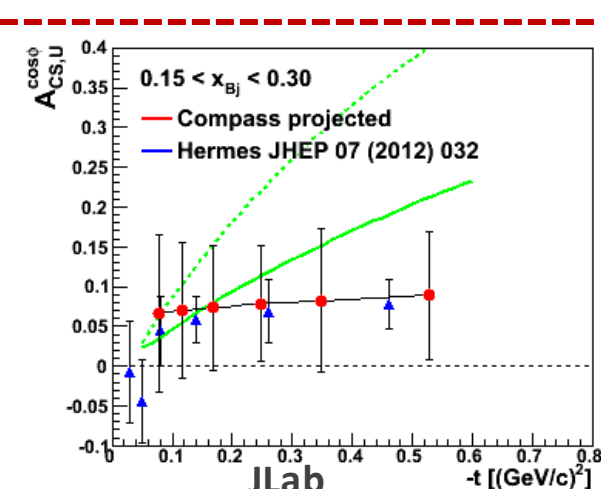
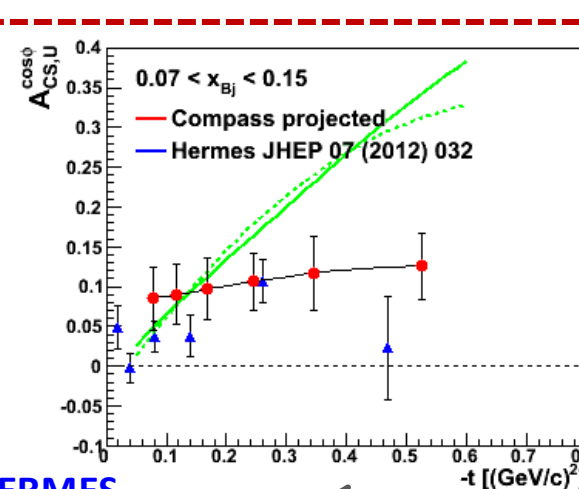
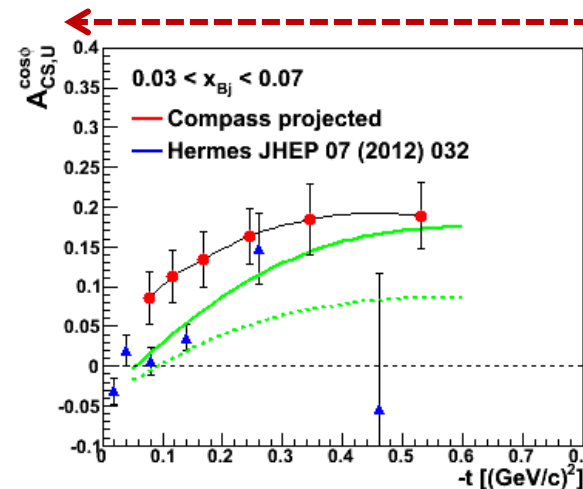
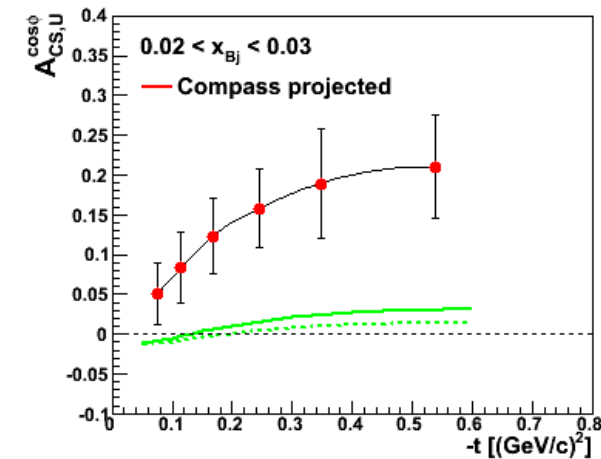
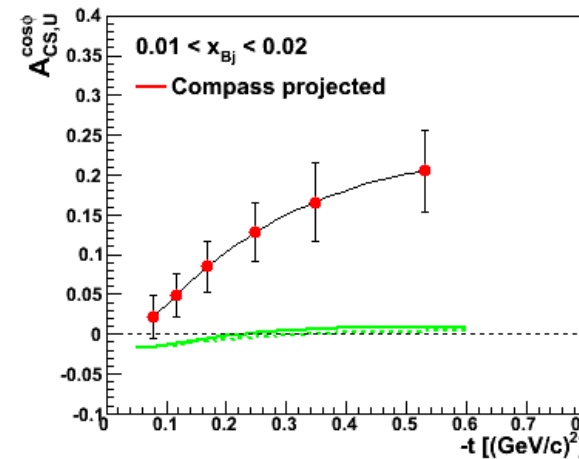
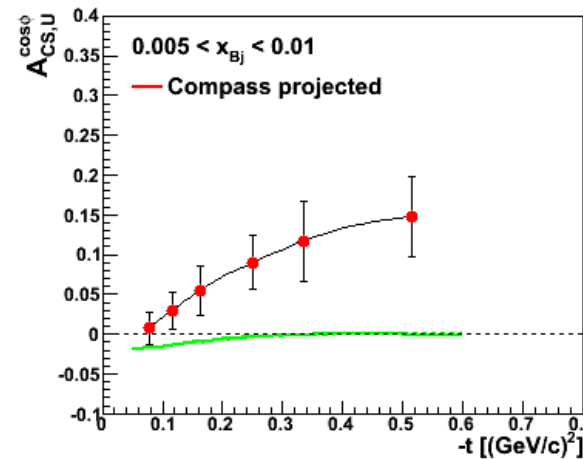
KM10 – fit to data

- With $\text{Re } F_1 \mathcal{H}$ and $\text{Im } F_1 \mathcal{H}$
→ Extraction of **D-term**

$\text{Re } \mathcal{H} > 0$ at H1

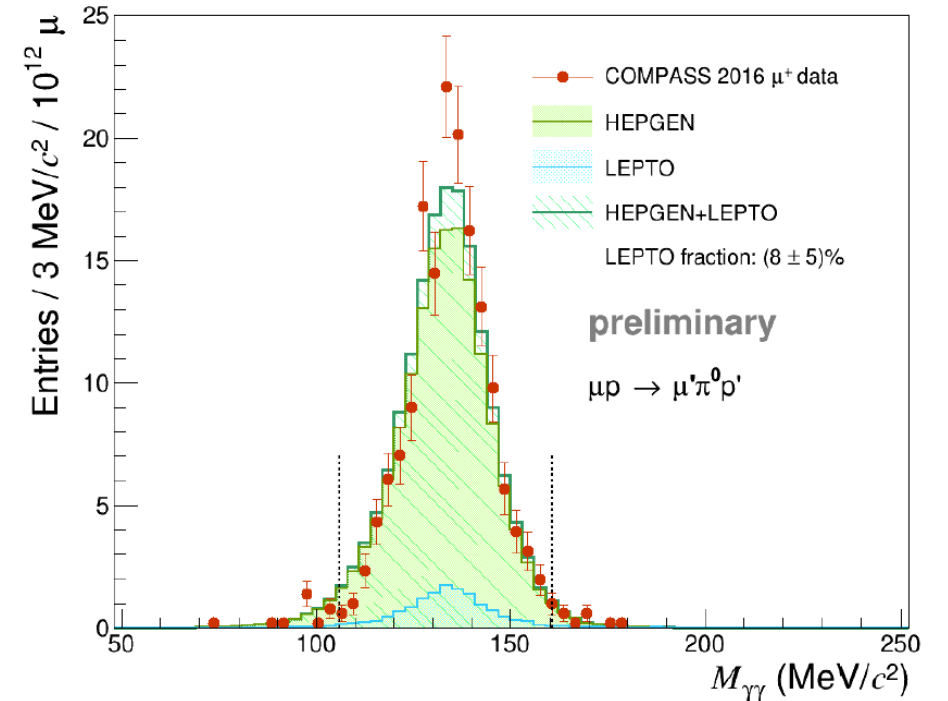
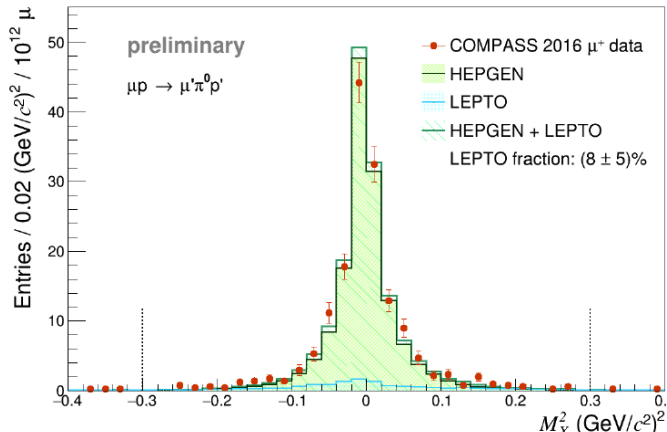
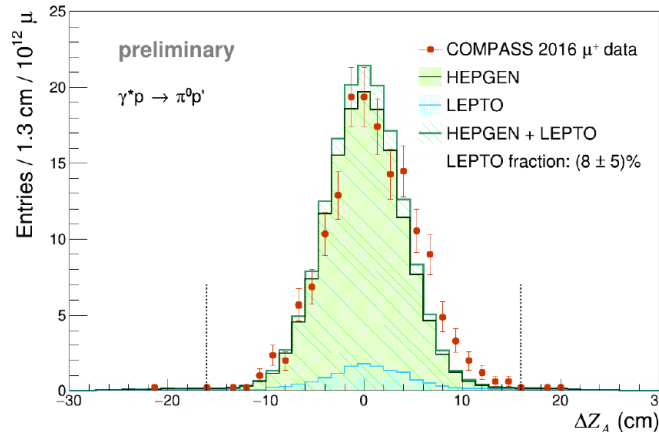
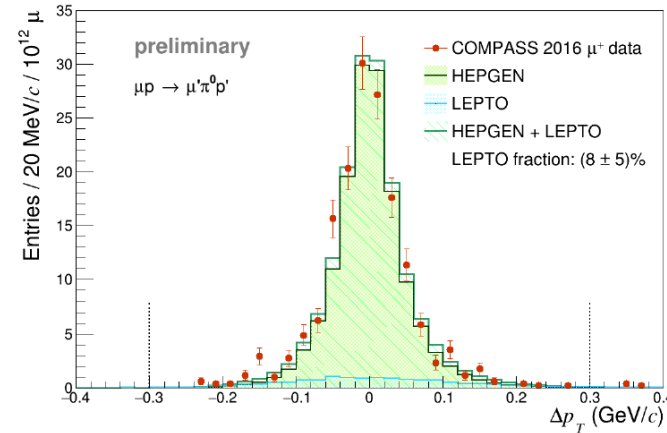
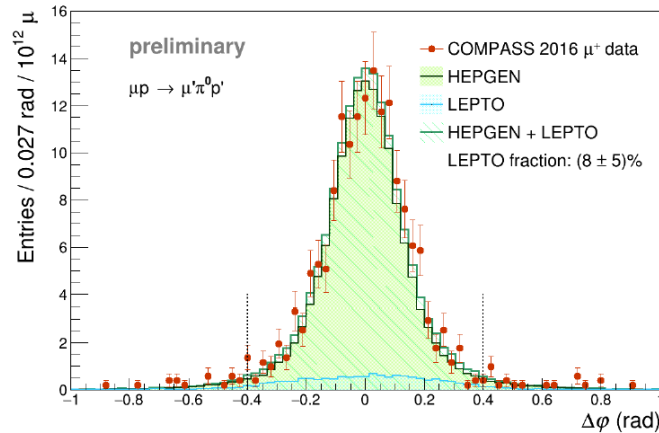
< 0 at HERMES

Value of x_{Bj} for the node?



Exclusive π^0 Selection and Background Estimation

- Exclusivity ensured by cuts on *exclusivity variables*, similar to DVCS.
- Background fraction determined by fitting the exclusivity variables with Monte Carlo simulations.
 - *LEPTO* for non-exclusive background
 - *HEPGEN* of exclusive π^0 for signal



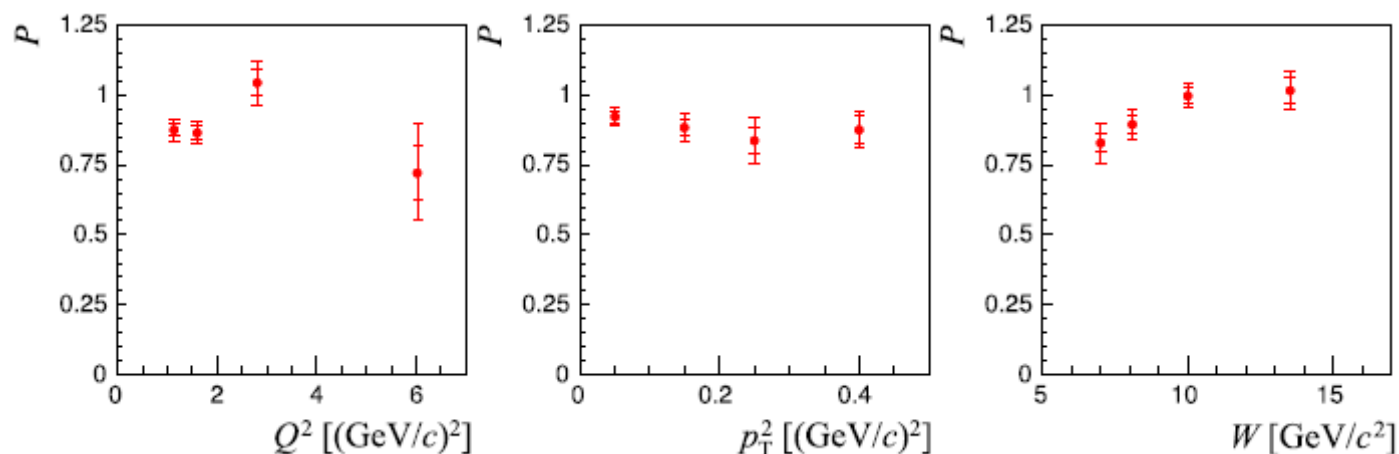
- In 2016 data, non-exclusive background fraction in data $\rightarrow 8 \pm 5 \%$

2012 NPE-to-UPE Asymmetry

$$P = \frac{2r_{1-1}^1}{1 - r_{00}^{04} - 2r_{1-1}^{04}} \approx \frac{d\sigma_T^N(\gamma_T^* \rightarrow V_T) - d\sigma_T^U(\gamma_T^* \rightarrow V_T)}{d\sigma_T^N(\gamma_T^* \rightarrow V_T) + d\sigma_T^U(\gamma_T^* \rightarrow V_T)}$$

NPE-to-UPE asymmetry of cross sections for transitions $\gamma_T^* \rightarrow V_T$

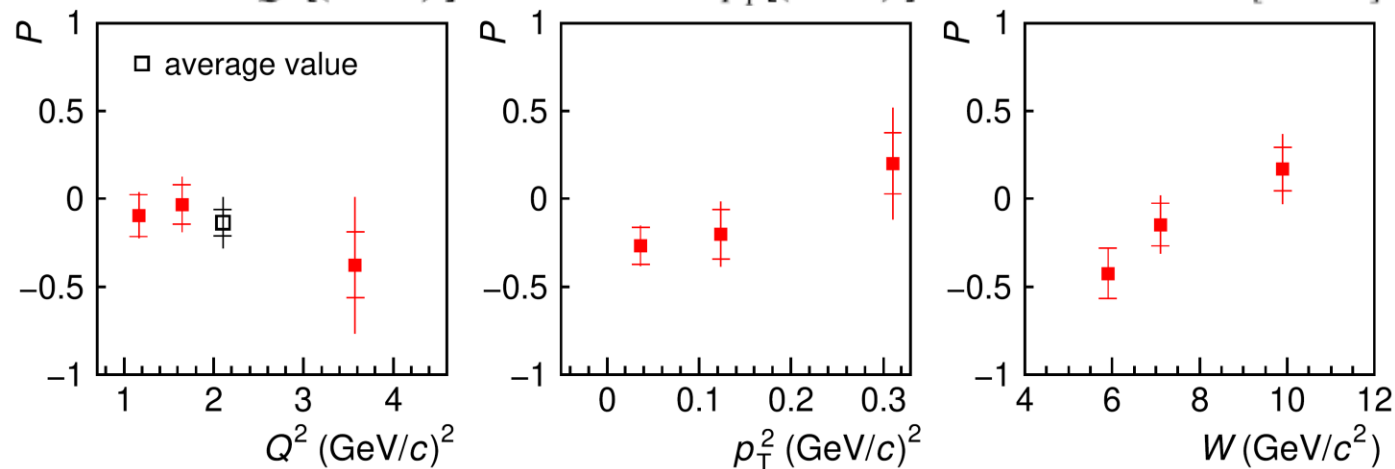
- NPE: Natural Parity Exchange
- UPE: Unnatural Parity Exchange



ρ^0

COMPASS, Eur.Phys.J.C 83 (2023) 924

- NPE Dominance
- NPE \rightarrow GPDs E, H



ω

COMPASS, Eur.Phys.J.C 81 (2021) 126

- NPE \approx UPE on average
- UPE Dominance at small W and p_T^2
- UPE \rightarrow GPDs \tilde{E}, \tilde{H}
+ Pion pole (dominant)

2012 $R = \sigma_L/\sigma_T$ for Exclusive ρ^0 Production

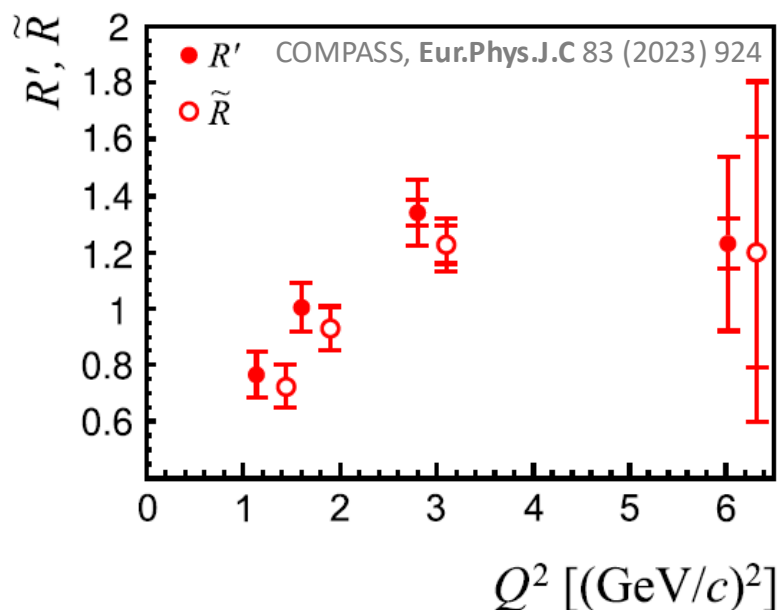
➤ Longitudinal-to-transverse γ^* cross section ratio:

$$R = \frac{\sigma_L(\gamma_L^* \rightarrow V)}{\sigma_T(\gamma_T^* \rightarrow V)}$$

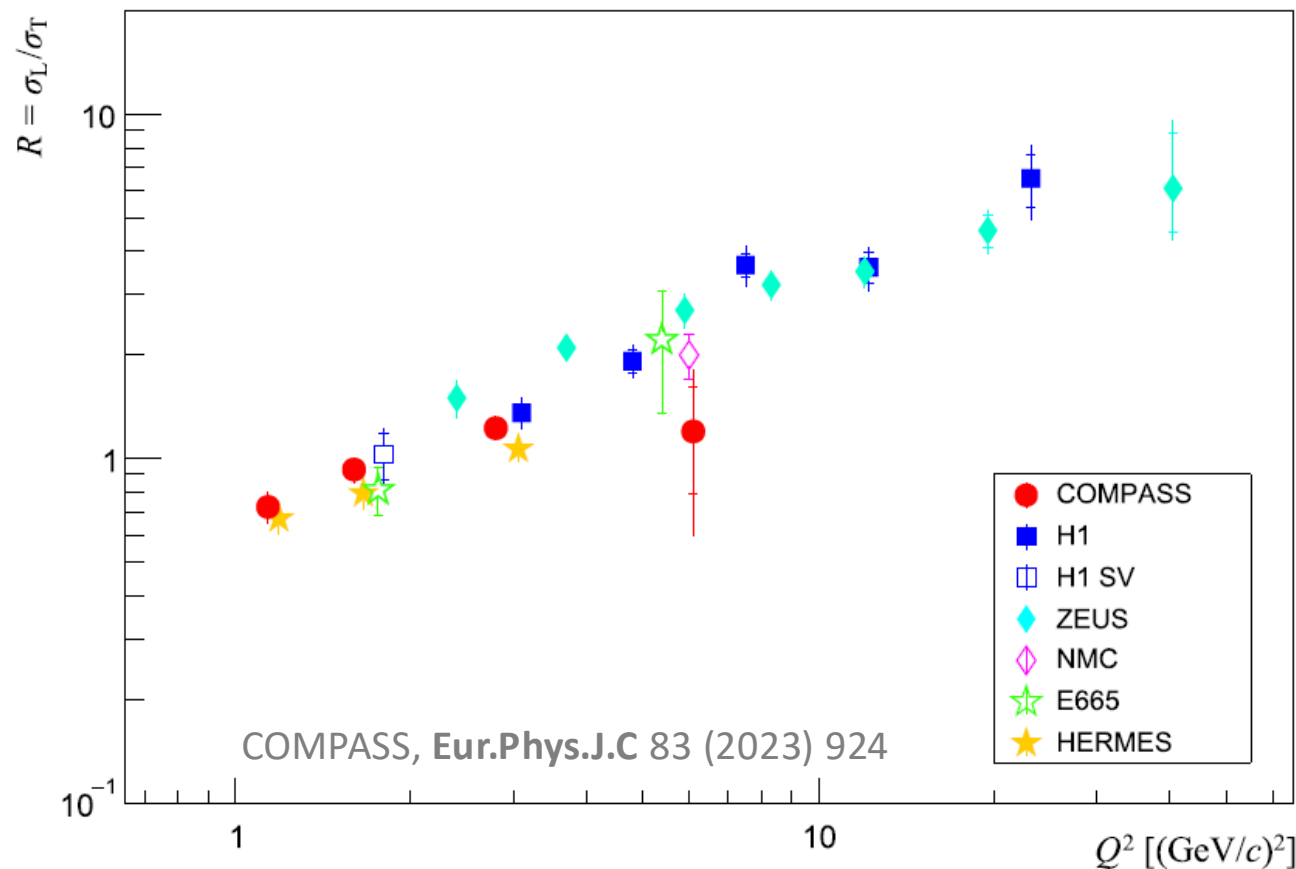
• Commonly used “effective” ratio ($R' = R$ only if SCHC):

$$R' = \frac{1}{\epsilon} \frac{r_{00}^{04}}{1 - r_{00}^{04}}$$

• Use of \tilde{R} , which takes SCHC violation into consideration, is preferred.



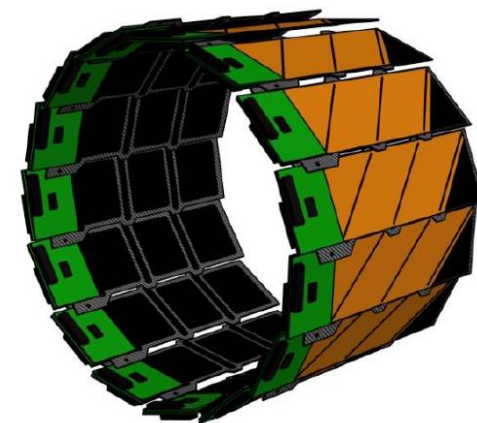
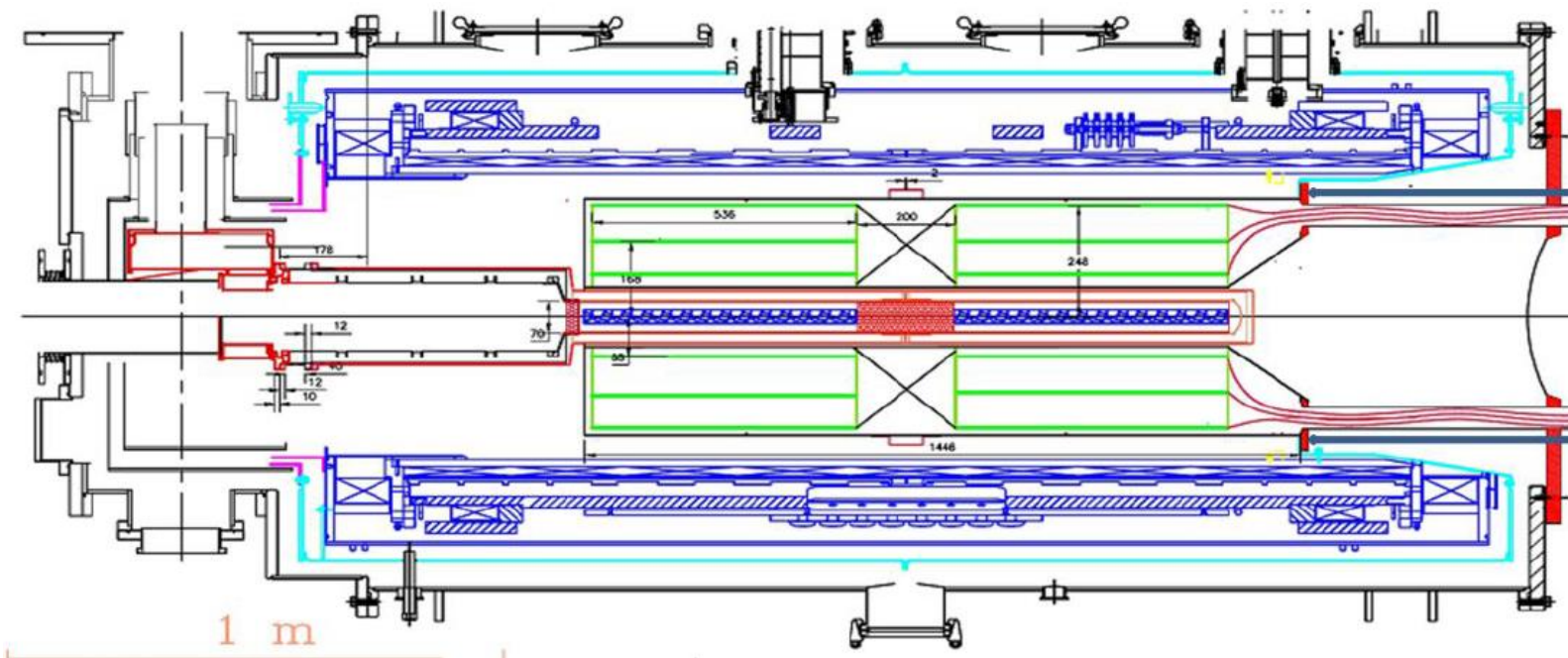
Results of all experiments with $Q^2 > 1$ (GeV/c)²



➤ Leading-order pQCD prediction: $Q^2/M_\rho^2 \rightarrow$ deviation due to effect of QCD evolution and q_T

Possible RPD for COMPASS⁺⁺/AMBER

A recoil proton detector (RPD) is mandatory to ensure the exclusivity. A Silicon detector is included *between* the target surrounded by the modified MW cavity *and* the polarizing magnet



A technology developed at JINR for NICA for the BM@N experiment

No possibility for ToF → PID of p/π with dE/dx
Momentum and trajectory measurements
 $|t|_{\min} \sim 0.1 \text{ GeV}$