

Latest Advancements in TMD Phenomenology & Update From the MAP Collaboration



Chiara Bissolotti

Maria Goeppert Mayer Fellow

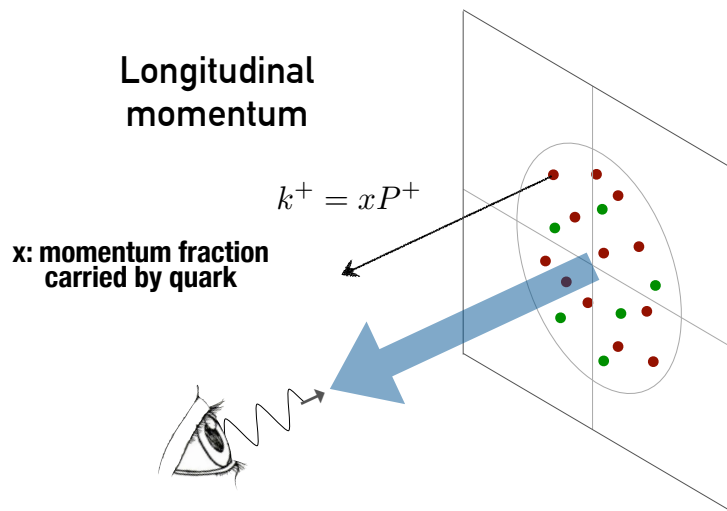
Argonne National Laboratory

PHY Division

June 12, 2025

Madison, WI

Parton distributions



momentum

position

$$\rho(x, \mathbf{k}_T, \mathbf{b}_T)$$



$$\int d^2\mathbf{b}_T$$

Transverse Momentum Distributions

TMDs

$$\int d^2\mathbf{k}_T$$

Parton Distribution Functions

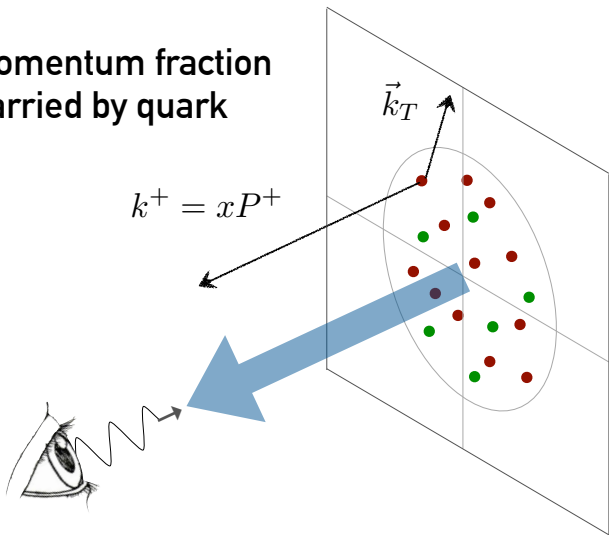
PDFs

TMDs: 3D maps

in momentum space

x : momentum fraction
carried by quark

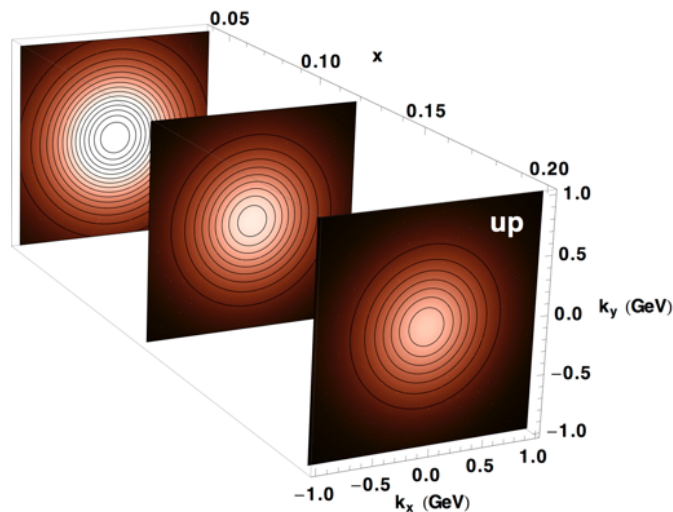
$$k^+ = xP^+$$



Transverse Momentum
Distributions

TMDs

$$f^q(x, \mathbf{k}_T)$$



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Leading quark TMDs

the distribution of quarks sharply depends on the orientation of their spins

Leading Quark TMDPDFs  Nucleon Spin  Quark Spin

		Quark Polarization		
		Un-Polarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	$f_1 = \text{Unpolarized}$		$h_1^\perp = \text{Boer-Mulders}$
	L		$g_1 = \text{Helicity}$	$h_{1L}^\perp = \text{Worm-gear}$
	T	$f_{1T}^\perp = \text{Sivers}$	$g_{1T}^\perp = \text{Worm-gear}$	$h_1 = \text{Transversity}$ $h_{1T}^\perp = \text{Pretzelosity}$

Leading Quark TMDFFs  Hadron Spin  Quark Spin

		Quark Polarization		
		Un-Polarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Unpolarized (or Spin 0) Hadrons		$D_1 = \text{Unpolarized}$		$H_1^\perp = \text{Collins}$
	L		$G_1 = \text{Helicity}$	$H_{1L}^\perp$
Polarized Hadrons	T	$D_{1T}^\perp = \text{Polarizing FF}$	$G_{1T}^\perp$	$H_1 = \text{Transversity}$ $H_{1T}^\perp$

from the TMD handbook,
[arXiv:2304.03302](https://arxiv.org/abs/2304.03302)

Transverse Momentum Distributions

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Leading Quark TMDPDFs  Nucleon Spin  Quark Spin

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from the TMD handbook,
[arXiv:2304.03302](https://arxiv.org/abs/2304.03302)

What's new

some recent works about TMDs

very active field!

Unpolarized TMDs

ART25 ● Determination of unpolarized TMD distributions from the fit of Drell-Yan and SIDIS data at N⁴LL
Valentin Moos, Ignazio Scimemi, Alexey Vladimirov, Pia Zurita – arXiv:2503.11201v1

MAP24 ● Flavor dependence of unpolarized quark Transverse Momentum Distributions from a global fit
MAP Collaboration – DOI: [10.1007/JHEP08\(2024\)232](https://doi.org/10.1007/JHEP08(2024)232) – arXiv:2405.13833

ART23 ● Extraction of unpolarized transverse momentum distributions from fit of Drell-Yan data at N⁴LL
Valentin Moos, Ignazio Scimemi, Alexey Vladimirov, Pia Zurita – DOI: [10.1007/JHEP05\(2024\)036](https://doi.org/10.1007/JHEP05(2024)036) – arXiv:2305.07473

MAPNN25 ● A Neural-Network Extraction of Unpolarized Transverse-Momentum-Dependent Distributions
MAP Collaboration – [arXiv:2502.04166](https://arxiv.org/abs/2502.04166)

HSO ● Phenomenology of TMD parton distributions in Drell-Yan and Z0 boson production in a hadron structure oriented approach
F. Aslan, M. Boglione, J. O. Gonzalez-Hernandez, T. Rainaldi, T. Rogers and A. Simonelli
arXiv: 2401.14266 – DOI: [10.1103/PhysRevD.110.074016](https://doi.org/10.1103/PhysRevD.110.074016)

What's new

some recent works about TMDs

*... about the
polarized TMDs*

Helicity & Transversity

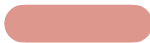
- First simultaneous global QCD analysis of dihadron fragmentation functions and transversity parton distribution functions
JAM Collaboration - DOI: [10.1103/PhysRevD.109.034024](https://doi.org/10.1103/PhysRevD.109.034024) - arXiv: 2308.14857
- Exploring the three-dimensional momentum distribution of longitudinally polarized quarks in the proton
MAP Collaboration
A. Bacchetta, A. Bongallino, M. Cerutti, M. Radici and L. Rossi - [arXiv:2409.18078](https://arxiv.org/abs/2409.18078).

Sivers

- Extraction of the Sivers function with deep neural networks
I. P. Fernando, D. Keller – DOI: [10.1103/PhysRevD.108.054007](https://doi.org/10.1103/PhysRevD.108.054007) - arXiv:2304.14328
- Global analysis of Sivers and Collins asymmetries within the TMD factorization
Chunhua Zeng, Hongxin Dong, Tianbo Liu, Peng Sun, Yuxiang Zhao – [arXiv:2412.18324](https://arxiv.org/abs/2412.18324)

TMD PDFs

every TMD has the same general structure

 perturbative terms

matching to the
collinear region

collinear PDFs

non-perturbative but used
as input here, not fitted

$$f_1^q(x, b; \mu, \zeta) = \sum_j (C_j \otimes f^j)(x, b_*; \mu_b) e^{R(b_*; \mu_b, \mu)} f_{\text{NP}}(x, b)$$

double scale dependence

perturbative
evolution

non perturbative
transverse content

many subtleties involved in TMD analyses

b^* prescription,
 ζ -prescription, hadron structure oriented

parametrized
and fitted to data



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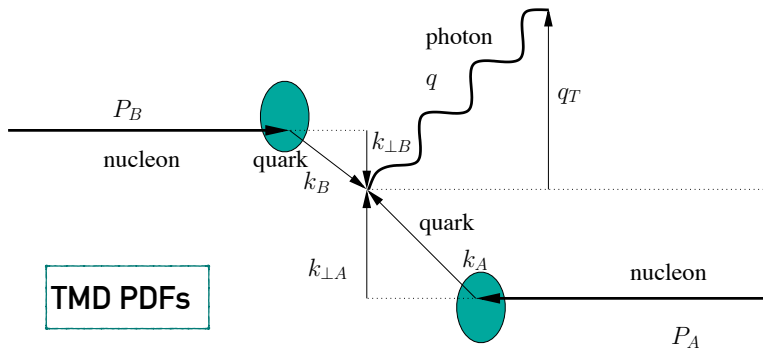
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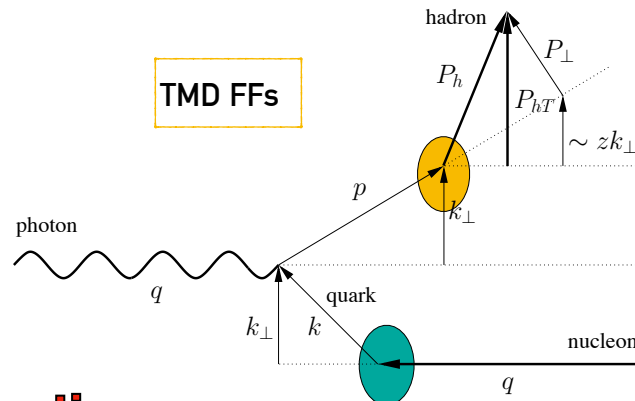


Drell-Yan and SIDIS

$$N(P_A) + N(P_B) \rightarrow \gamma^*/Z \rightarrow l^+ l^-$$



$$\ell(l) + N(p) \rightarrow \ell(l') + h(P_h) + X$$



TMD factorization

$$q_T \ll Q$$

$$M^2 \ll Q^2$$

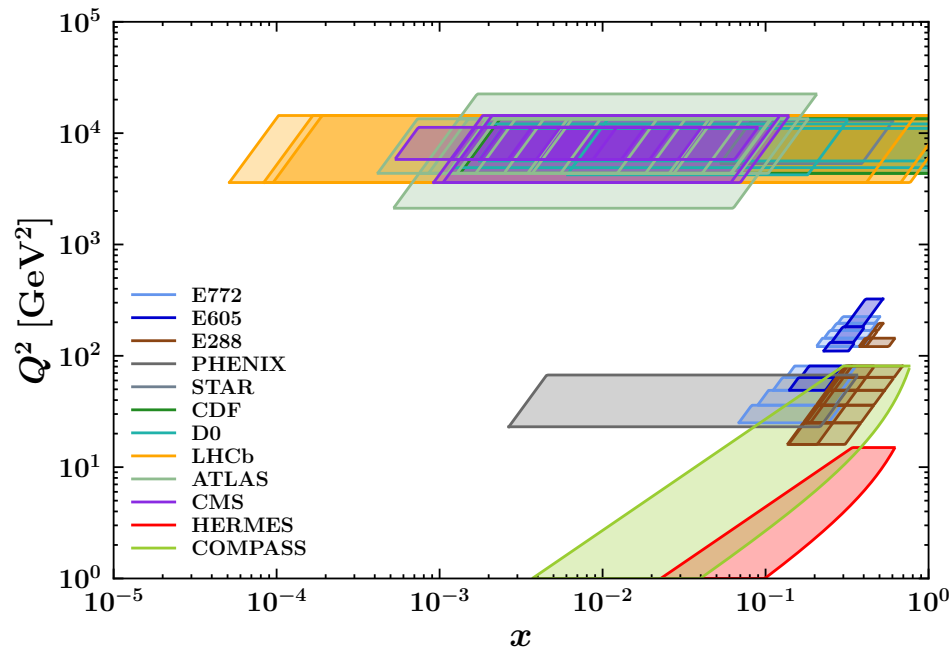
$$P_{hT}^2 \ll Q^2$$

$$\left(\frac{d\sigma}{dq_T} \right) \propto \int \frac{d^2 \mathbf{b}}{4\pi} e^{i\mathbf{b} \cdot \mathbf{q}_T} x_1 f_1^q(x_1, \mathbf{b}) x_2 f_1^{\bar{q}}(x_2, \mathbf{b})$$

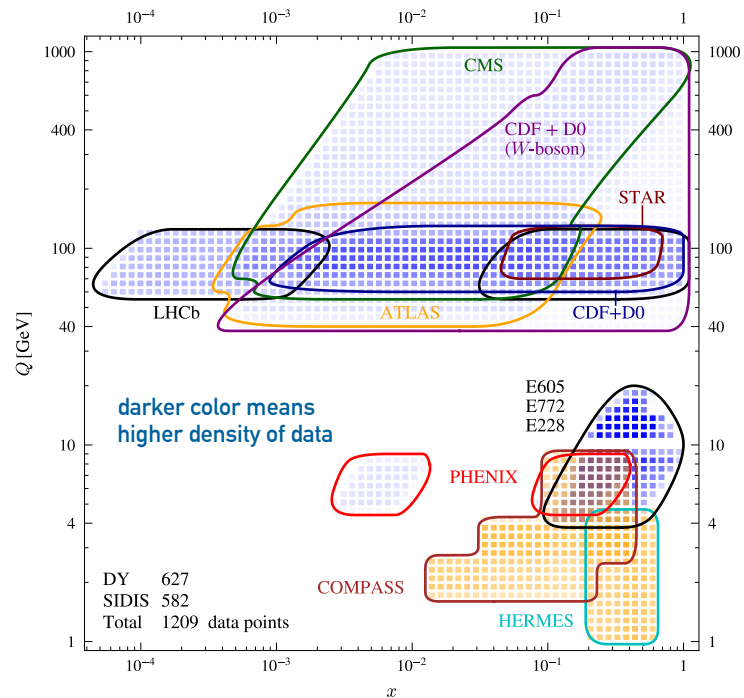
$$\left(\frac{d\sigma}{dq_T} \right) \propto \int \frac{d^2 \mathbf{b}}{4\pi} e^{i\mathbf{b} \cdot \mathbf{q}_T} f_1^q(x, \mathbf{b}) D_1^{q \rightarrow h}(z, \mathbf{b})$$

Data kinematical coverage

SIDIS & Drell-Yan



MAP Collaboration



ART25 - arXiv:2503.11201v1



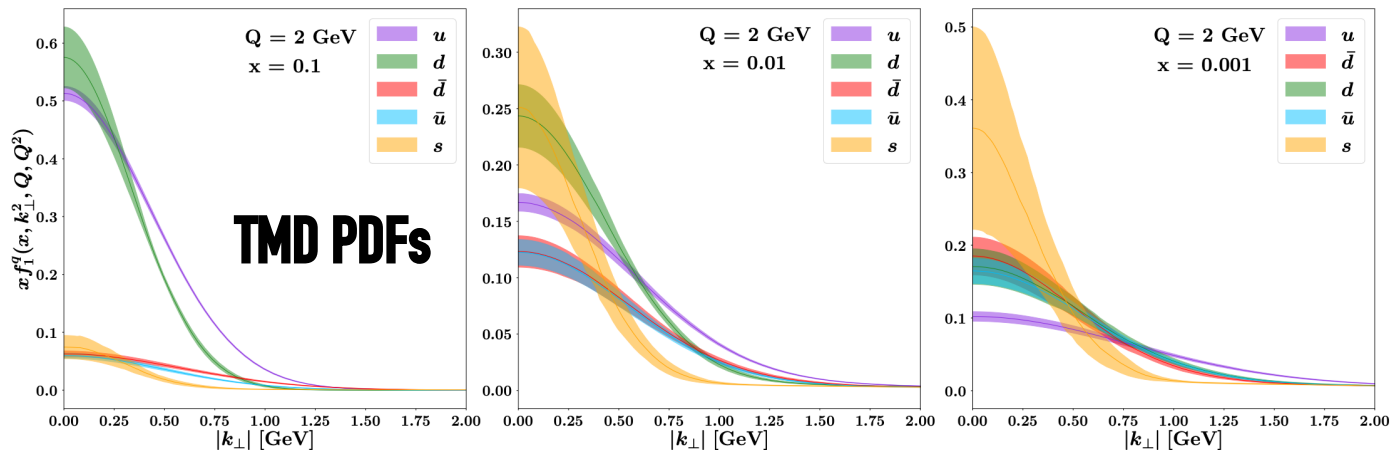
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Extractions of unpolarized TMDs

Reference	Accuracy	HERMES	COMPASS	DY	n. of points	χ^2/n
PV 2017 [arXiv:1703.10157]	NLL	✓	✓	✓	8059	1.5
SV19 [arXiv:1912.06532]	N ³ LL(-)	✓	✓	✓	1039	1.06
PV19 [arXiv:1912.07550]	N ³ LL	✗	✗	✓	353	1.07
SV19 + flavor dep. [arXiv:2201.07114]	N ³ LL	✗	✗	✓	309	<1.08>
MAP22 [arXiv:2206.07598]	N ³ LL(-)	✓	✓	✓	2031	1.06
ART23 [arXiv:2305.07473]	N ⁴ LL	✗	✗	✓	627	0.96
MAP24 [arXiv:2405.13833]	N ³ LL	✓	✓	✓	2031	1.08
ART25 [arXiv:2503.11201v1]	N ⁴ LL	✓	✓	✓	1209	1.05

global fit: DY & SIDIS



MAP Collaboration

NP EvOL : $g_K(b_T^2) = -g_2^2 \frac{b_T^2}{4}$

TMD PDFs : $f_{1\text{NP}}(x, b_T^2) \propto \text{F.T. of } \left(e^{-\frac{k_\perp^2}{g_{1A}}} + \lambda_B k_\perp^2 e^{-\frac{k_\perp^2}{g_{1B}}} + \lambda_C e^{-\frac{k_\perp^2}{g_{1C}}} \right)$

TMD FFs : $D_{1\text{NP}}(z, b_T^2) \propto \text{F.T. of } \left(e^{-\frac{P_\perp^2}{g_{3A}}} + \lambda_{FB} k_\perp^2 e^{-\frac{P_\perp^2}{g_{3B}}} \right)$

f_{NP} same as in MAP22

96 parameters

1 + (5 flavors $\times$ 10 parameters) for TMD PDFs, and
45 (5 channels $\times$ 9 parameters) for TMD FFs.

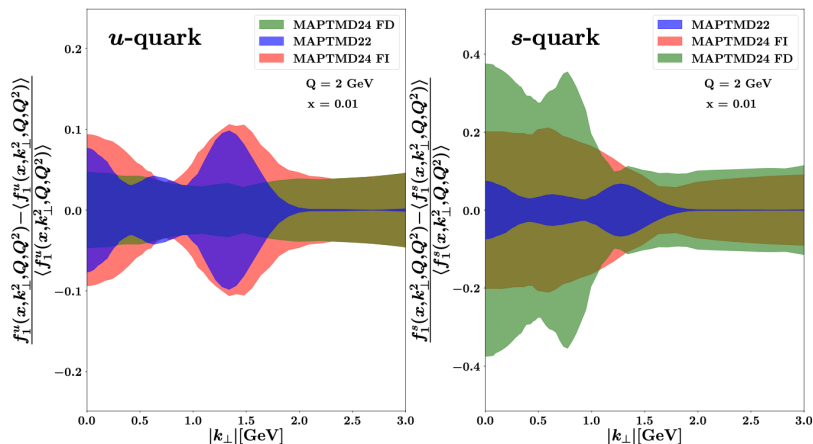
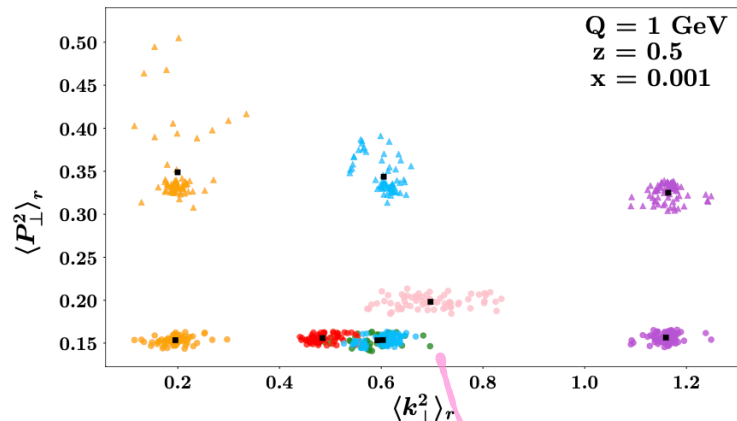
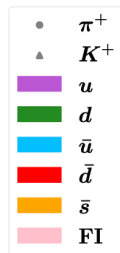
$$g_1(x) = N_1 \frac{(1-x)^\alpha x^\sigma}{(1-\hat{x})^\alpha \hat{x}^\sigma} \quad g_3(z) = N_3 \frac{(z^\beta + \delta)(1-z)^\gamma}{(\hat{z}^\beta + \delta)(1-\hat{z})^\gamma}$$

MAP24

flavor dependent global fit

MAP Collaboration

Evidence of different behaviors for
different flavors
and for different measured hadrons



uncertainties
are larger

each TMD replica is matched onto a
different replica of the collinear PDFs

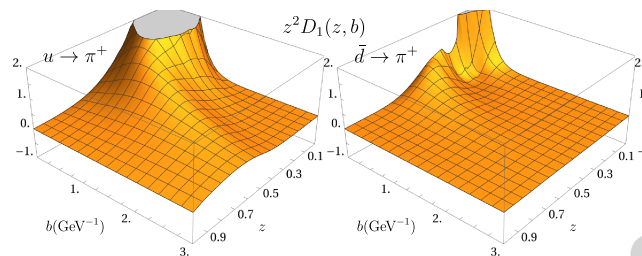
VS

MAP22

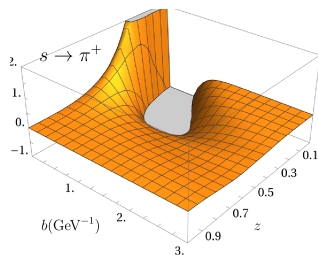
only central replica
of collinear PDFs

nice check:
flavor independent fit
is ~ average of all flavors

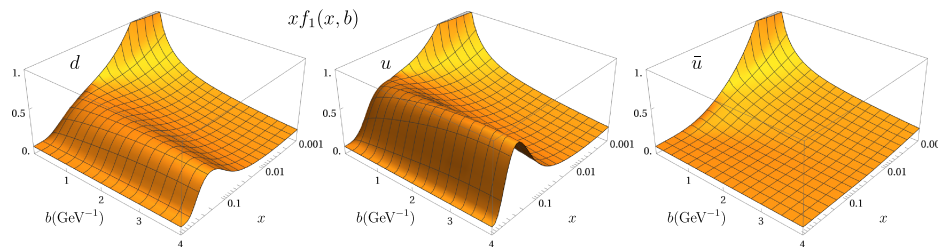
explicit flavor and hadron dependence



TMD FFs



TMD PDFs



TMD PDFs:
$$F_{\text{NP}}^f(x, b) = \frac{1}{\cosh[(\lambda_1^f(1-x)^{\lambda_3^f} + \lambda_2^f x) b]}$$

distinguish {u, d, ubar, dbar}
and sea = {s, sbar, c, cbar, bbar, b}

10 + 10 + 2 = 22
parameters

TMD FFs:
$$D_{\text{NP}}^{f/h}(z, b) = \frac{1 + \eta_1^{h,f} \frac{b^2}{z^2}}{\cosh\left(\eta_0^h \frac{b}{z}\right)}$$

NP Evol.:
$$\mathcal{D}_{\text{NP}}(b) = b b^* \left[c_0 + c_1 \ln\left(\frac{b^*}{B_{\text{NP}}}\right) \right]$$

NN TMDs

MAP Collaboration

Neural Network

extraction of $f_1(x, k_T)$ from DY data

MAP Collaboration
[arXiv:2502.04166](https://arxiv.org/abs/2502.04166)

chosen parametrization
of the non-perturbative part of $f_1(x, k_T)$

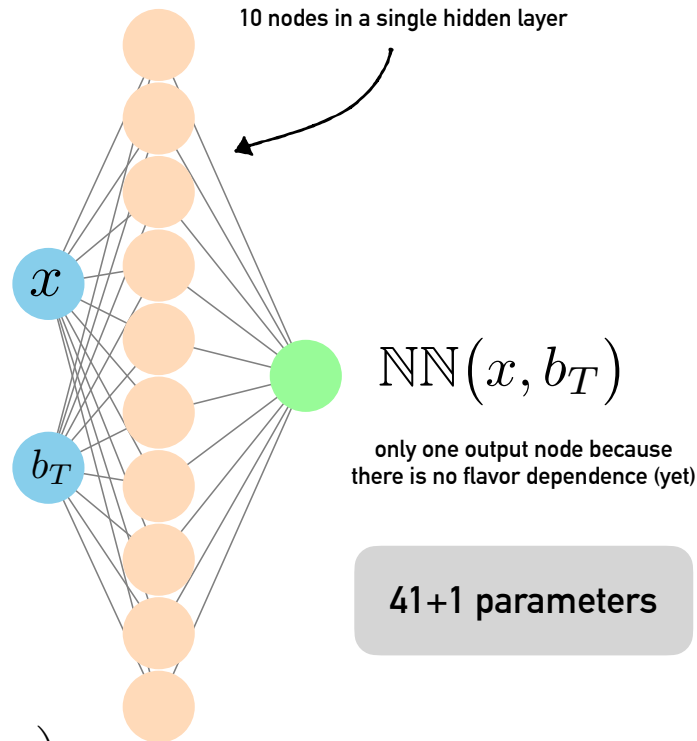
$$f_{\text{NP}}(x, b_T; \zeta) = \frac{\text{NN}(x, b_T, \{p_i\})}{\text{NN}(x, 0, \{p_i\})} \exp\left[-g_2^2 b_T^2 \ln\left(\frac{\zeta}{Q_0^2}\right)\right]$$

● physically required constraints

$$f_{\text{NP}} \rightarrow 1 \quad \text{for} \quad b_T \rightarrow 0$$

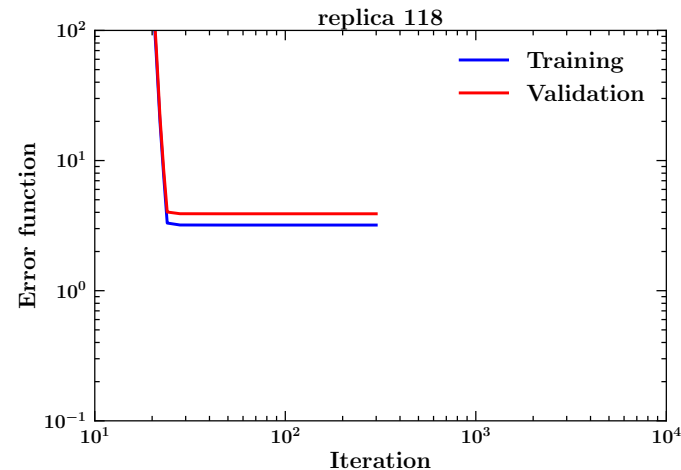
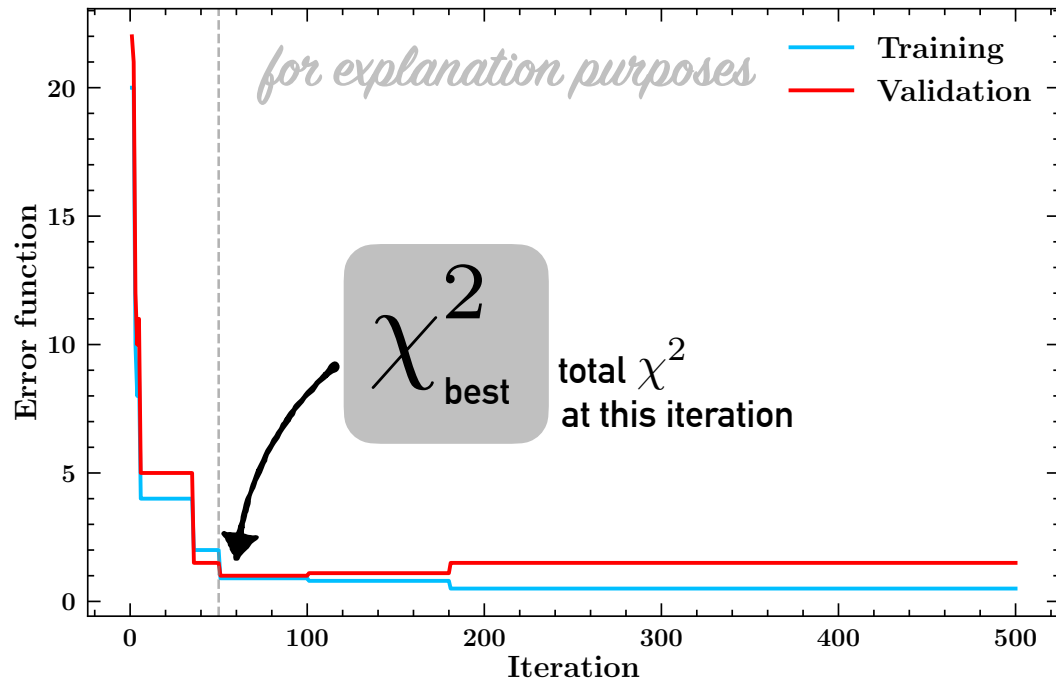
with activation function

$$\sigma(z) = \frac{1}{2} \left(1 + \frac{z}{1 + |z|} \right)$$



avoid overfitting

split data into training and validation set



random splitting

50% - 50%

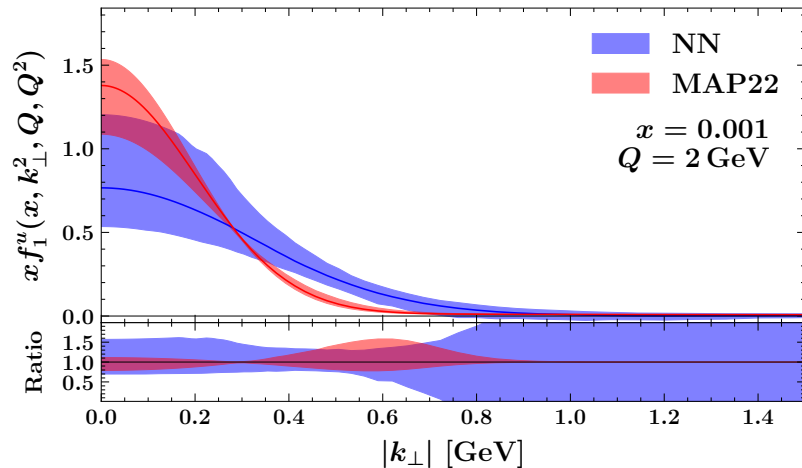
dataset by dataset

NN TMDs

MAP Collaboration

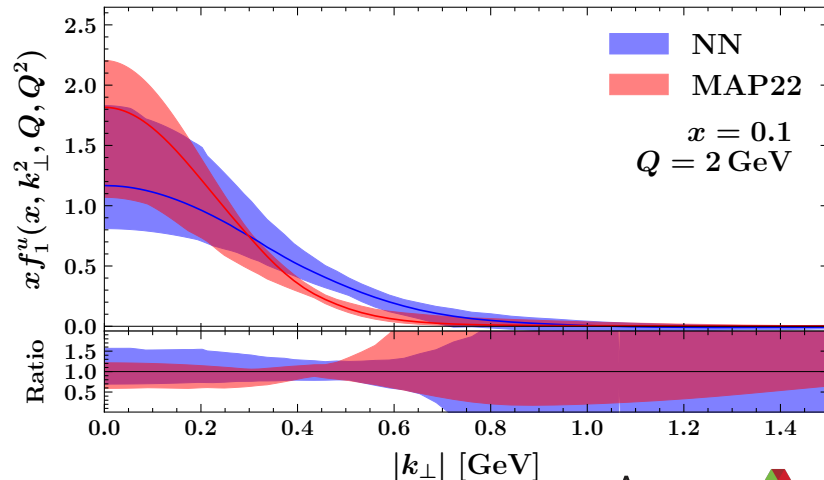
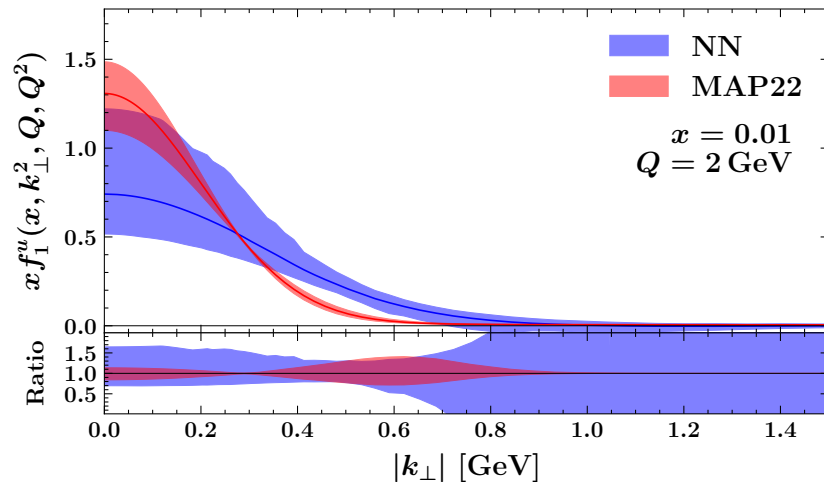
extraction of $f_1(x, k_T)$ from DY data

MAP Collaboration
arXiv:2502.04166



NN fit has larger bands

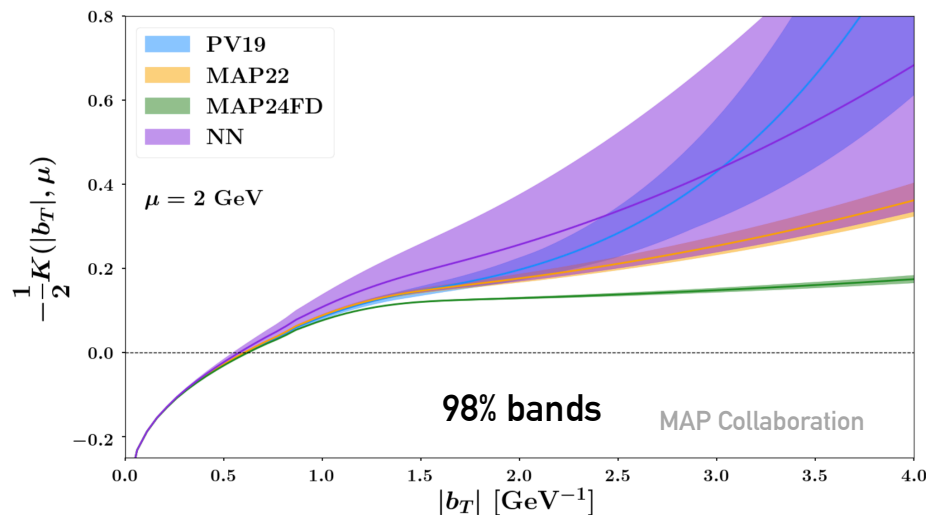
more reliable estimation uncertainties



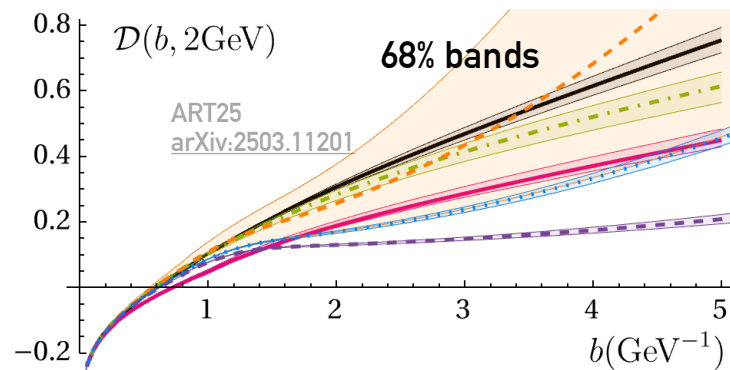
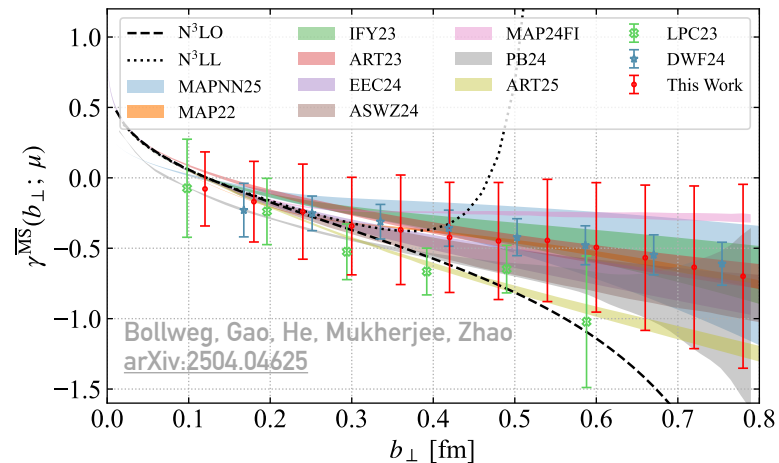
Collins-Soper kernel

“strong” universality

process independent,
insensitive to the types of external hadrons involved,
not dependent on polarization, on the flavors of the quarks, and on the scale Q



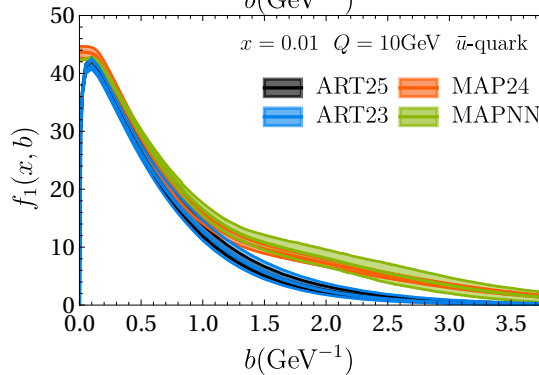
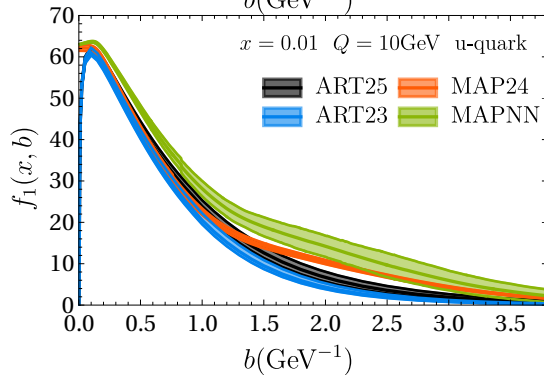
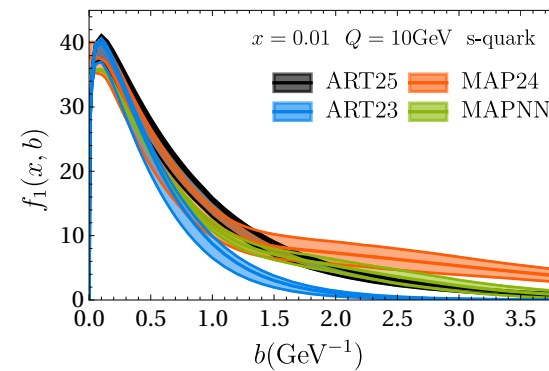
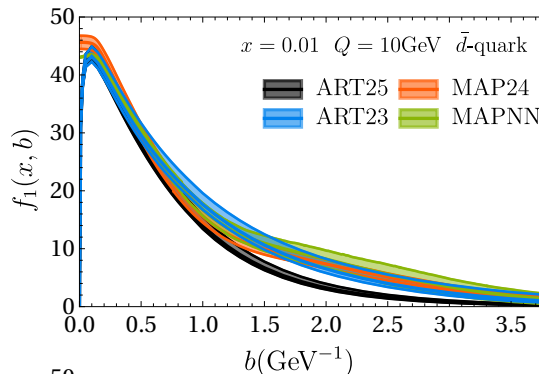
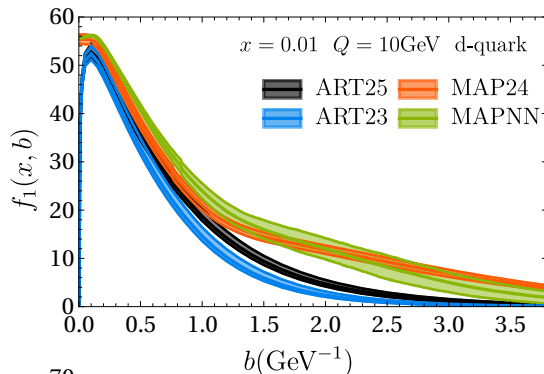
good agreement between the extractions



TMD PDFs comparison

from ART25

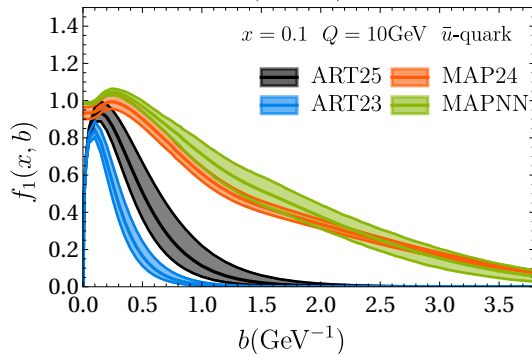
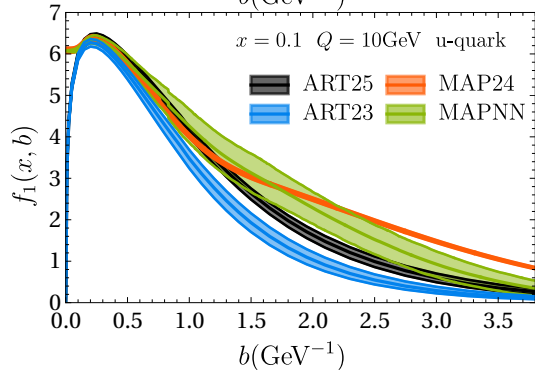
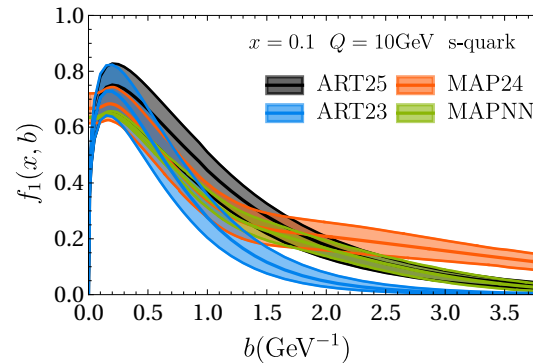
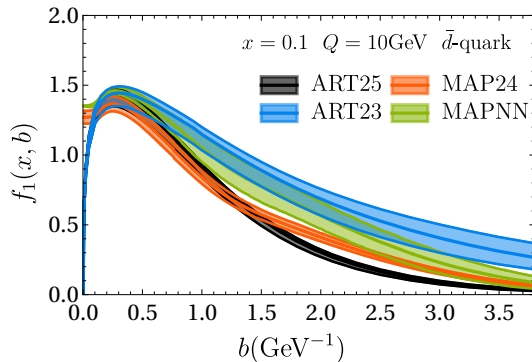
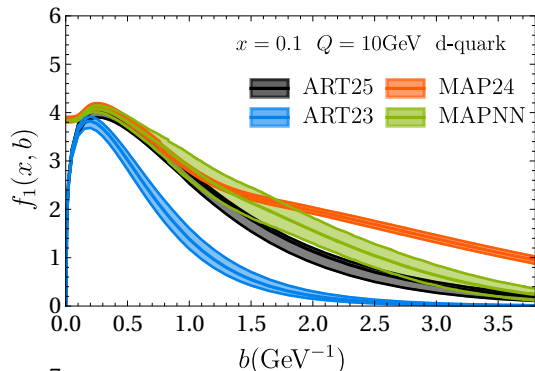
two latest extraction of
unpolarized quark TMD PDF
from the ART and the MAP Collaborations



TMD PDFs comparison

from ART25

two latest extraction of
unpolarized quark TMD PDF
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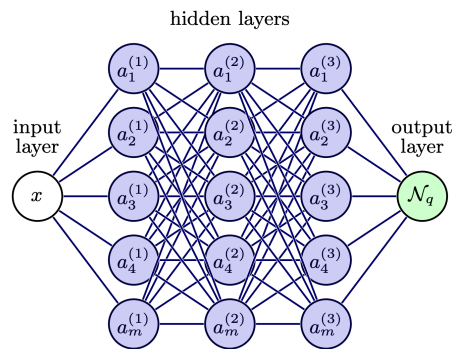
Sivers function

with Deep Neural Networks

I. P. Fernando, D. Keller
DOI: 10.1103/PhysRevD.108.054007
arXiv:2304.14328

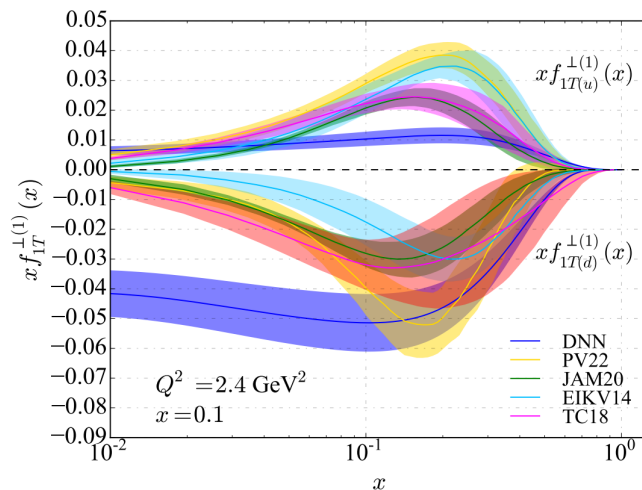
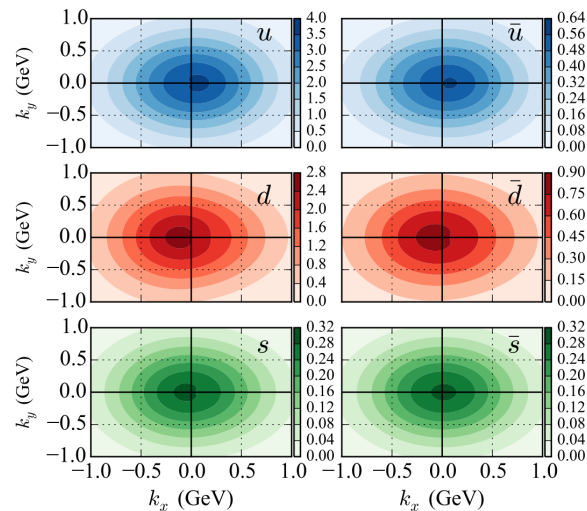
$$\rho_N^q(x, k_x, k_y; Q^2) = f_1^q(x, k_T^2, Q^2) - \frac{k_x}{M} f_{1T}^{\perp q}(x, k_T^2, Q^2)$$

in a nucleon polarized in the +y direction,
the distribution of quarks can be distorted in the x direction



exploratory analysis

using HERMES and COMPASS data



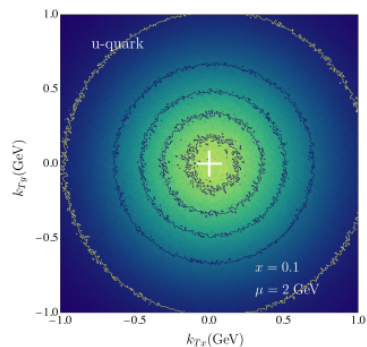
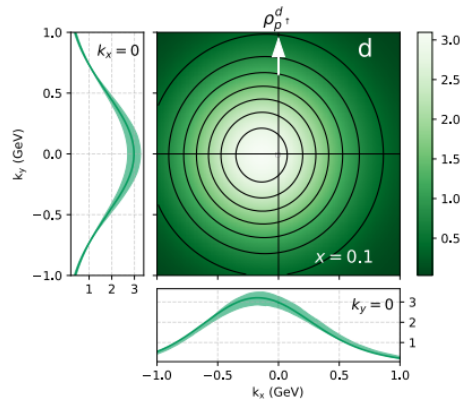
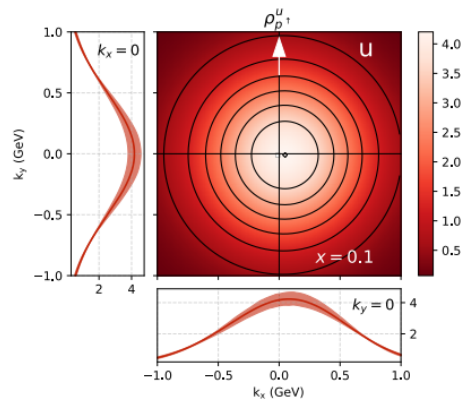
good agreement between
the extractions

Sivers function

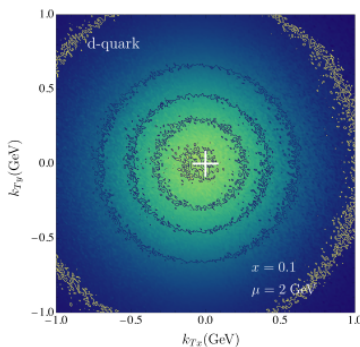
$Q = 2 \text{ GeV}$

$$\rho_N^q(x, k_x, k_y; Q^2) = f_1^q(x, k_T^2, Q^2) - \frac{k_x}{M} f_{1T}^{\perp q}(x, k_T^2, Q^2)$$

in a nucleon polarized in the +y direction,
the distribution of quarks can be distorted in the x direction



(a)



(b)

MAP Collaboration

A. Bacchetta, F. Delcarro, C. Pisano, M. Radici
arXiv: 2004.14278

M. Bury, A. Prokudin, A. Vladimirov
arXiv: 2103.03270



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Helicity

longitudinally polarized quarks

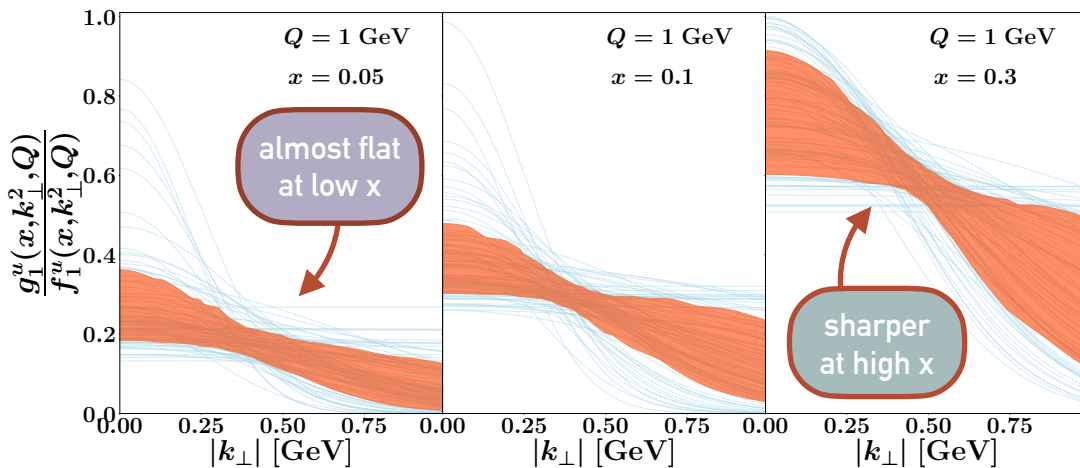
A. Bacchetta, A. Bongallino, M. Cerutti, M. Radici and L. Rossi
MAP Collaboration - [arXiv:2409.18078](https://arxiv.org/abs/2409.18078)

SIDIS data ~300

MAP Collaboration

$$A_1(x, z, Q, |P_{hT}|) = \frac{\sum_{a=q,\bar{q}} e_a^2 \int_0^{+\infty} d|b_T|^2 J_0\left(\frac{|b_T||P_{hT}|}{z}\right) \hat{g}_1^a(x, |b_T|^2, Q) \hat{D}_1^{a \rightarrow h}(z, |b_T|^2, Q)}{\sum_{a=q,\bar{q}} e_a^2 \int_0^{+\infty} d|b_T|^2 J_0\left(\frac{|b_T||P_{hT}|}{z}\right) \hat{f}_1^a(x, |b_T|^2, Q) \hat{D}_1^{a \rightarrow h}(z, |b_T|^2, Q)}$$

double spin asymmetry



3 parameters

but poorly constrained due
to lack of data

Parameters	N_{1g}	α_{1g}	σ_{1g}
NLL	0.70 ± 0.54	27.81 ± 27.70	0.42 ± 0.86
NNLL	0.87 ± 0.72	6.73 ± 6.58	3.04 ± 3.09

TMD phenomenology

Status and Future Directions

Unpolarized Quark TMDs

- we are entering the

precision era

TMDs extracted from fits of large datasets with high perturbative accuracy.

- flavor dependence, reduction of PDF bias

Polarized Quark TMDs

- great progress in extracting polarized TMDs

exploration of

- Sivers function
- Helicity,
- Transversity...

New techniques

- Neural Networks fits

more reliable estimation uncertainties



unpolarized quark TMD

$$\begin{aligned}
 F_{f/P}(x, \mathbf{b}_T; \mu, \zeta) &= \sum_j C_{f/j}(x, b_*; \mu_b, \zeta_F) \otimes f_{j/P}(x, \mu_b) \\
 &\times \exp \left\{ K(b_*; \mu_b) \ln \frac{\sqrt{\zeta_F}}{\mu_b} + \int_{\mu_b}^{\mu} \frac{d\mu'}{\mu'} \left[\gamma_F - \gamma_K \ln \frac{\sqrt{\zeta_F}}{\mu'} \right] \right\} \\
 &\times \exp \left\{ g_{j/P}(x, b_T) + g_K(b_T) \ln \frac{\sqrt{\zeta_F}}{\sqrt{\zeta_{F,0}}} \right\}
 \end{aligned}$$

matching to the collinear region

factorizes as **hard** and longitudinal non-perturbative

$b_T \ll 1/\Lambda_{\text{QCD}}$

CS and RGE evolution

non perturbative transverse content

parametrized and **fitted to data**

Logarithmic accuracy

$$\left(\frac{d\sigma}{dq_T}\right) \propto H(Q, \mu) \int \frac{d^2\mathbf{b}}{4\pi} e^{i\mathbf{b}\cdot\mathbf{q}_T} x_1 f_1^q(x_1, \mathbf{b}; \mu, \zeta_1) x_2 f_1^{\bar{q}}(x_2, \mathbf{b}; \mu, \zeta_2)$$

perturbative expansion
in $\alpha_s(\mu)$

$$f_1^q(x, b; \mu, \zeta) = \sum_j (C_{q/j} \otimes f^j)(x, b_*; \mu_b)$$

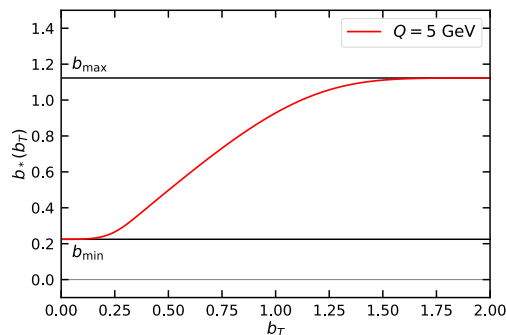
$$\times \exp \left\{ K(\mu_0) \ln \frac{\sqrt{\zeta}}{\sqrt{\zeta_0}} + \int_{\mu_0}^{\mu} \frac{d\mu'}{\mu'} \left[\gamma_F(\alpha_s(\mu')) - \gamma_K(\alpha_s(\mu')) \ln \frac{\sqrt{\zeta}}{\mu'} \right] \right\}$$

$$\times f_{\text{NP}}(x, b; \zeta)$$

Accuracy	H and $C_{q/j}$	K and γ_F	γ_K	PDF and α_s evol.
LL	0	-	1	-
NLL	0	1	2	LO
NLL'	1	1	2	NLO
NNLL	1	2	3	NLO
NNLL'	2	2	3	NNLO
N ³ LL	2	3	4	NNLO
N ³ LL'	3	3	4	N ³ LO

b^* prescription

$$b_T \rightarrow \infty \quad \alpha_s(\mu_b) = \alpha \left(\frac{2e^{-\gamma_E}}{b} \right) \gg 1 \quad \longrightarrow \quad \text{invalidates perturbative calculations} \Rightarrow b_{\max}$$



$$F(x, b; \mu, \zeta) = \left[\frac{F(x, b; \mu, \zeta)}{F(x, b_*(b); \mu, \zeta)} \right] F(x, b_*(b); \mu, \zeta)$$



$$f_{NP}(x, b, \zeta)$$

fit to data



perturbative

important

f_{NP} not directly comparable between fits,
it depends on the choice of b^* prescription

Hadron Structure Oriented approach

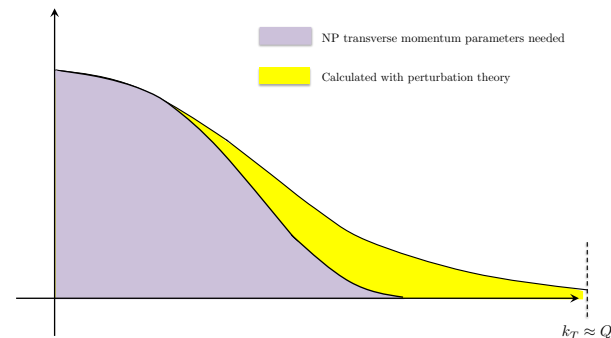
TMD PDF HSO parametrization at input scale

F. Aslan, M. Boglione, J. O. Gonzalez-Hernandez, T. Rainaldi, T. Rogers and A. Simonelli
DOI: 10.1103/PhysRevD.110.074016

$$f_{\text{inpt},i/p}(x, \mathbf{k}_T; \mu_{Q_0}, Q_0^2) = \text{pQCD and collinear factorization}$$

$$+ C_{i/p}^f \text{ NP model}$$

coefficient such that the
integral relations/OPE expansion is satisfied



the relative contributions
cannot be adjusted independently from one another

$$f_{j/h}(x, \mu) = \pi \int_0^{\mu^2} dk_T^2 f_{j/h}(x, k_T; \mu, \mu^2) + \Delta(f(x), \alpha_s(\mu))$$

+ power suppressed.

no need to divide space
into two parts with b_{max}

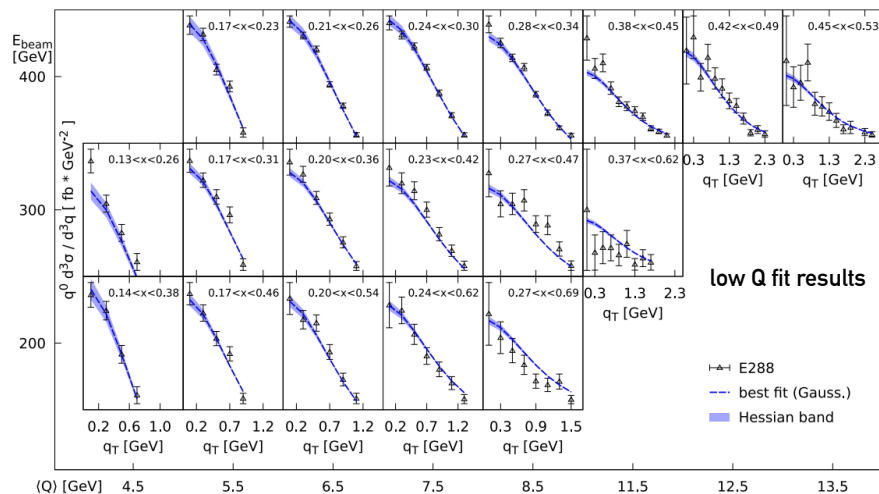
preserve the integral normalizations that
connect TMD and collinear PDFs

Hadron Structure Oriented (HSO)

proposed new approach to TMD phenomenology

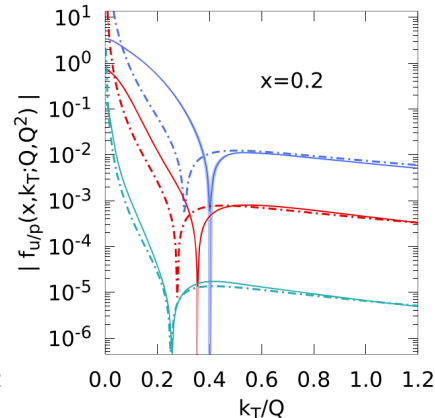
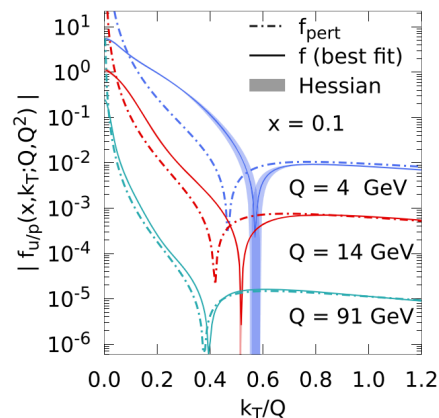
within 'the usual' TMD factorization

proof of principle



	E288 (130 pts)	E605 (52 pts)
$\chi^2_{d.o.f.}$	1.04	1.68

4 parameters



HSO approach guarantees that the TMD pdf asymptotes to the perturbative tail

PDF bias

ζ -prescription

M. Bury, F. Hautmann, S. Leal-Gomez, I. Scimemi,
A. Vladimirov, P. Zurita - arXiv: 2201.0714 - DOI: 10.1007/JHEP10(2022)118

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PDF bias and flavor dependence in TMD distributions

Marcin Bury,^a Francesco Hautmann,^{b,c,d} Sergio Leal-Gomez,^e Ignazio Scimemi,^f
Alexey Vladimirov^{g,h} and Pia Zuritaⁱ

N3LL

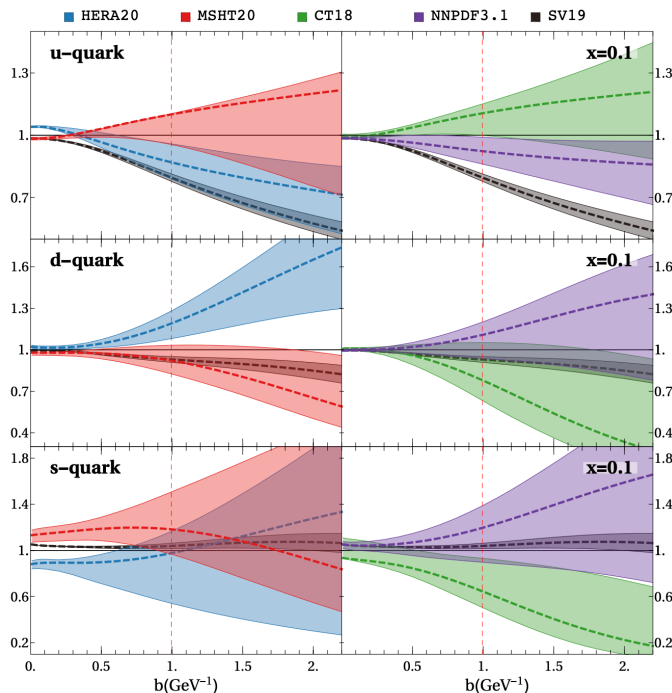
H	$C_{f \leftarrow f'}$	Γ_{cusp}	γ_V	$\mathcal{D}_{\text{resum}}$	α_s running & PDF evolution
α_s^2	α_s^2	α_s^3	α_s^2	α_s^2	NNLO

$$f_{\text{NP}}^f(x, b) = \exp \left[- \frac{[(1-x) \lambda_1^f + x \lambda_2^f] b^2}{\sqrt{1 + \lambda_0^f x^2 b^2}} \right]$$

distinguish {u, d, ubar, dbar}
and sea = {s, sbar, c, cbar, bbar, b}

comparison of uncertainty band for unpolarized
TMDPDFs extracted with different PDFs.

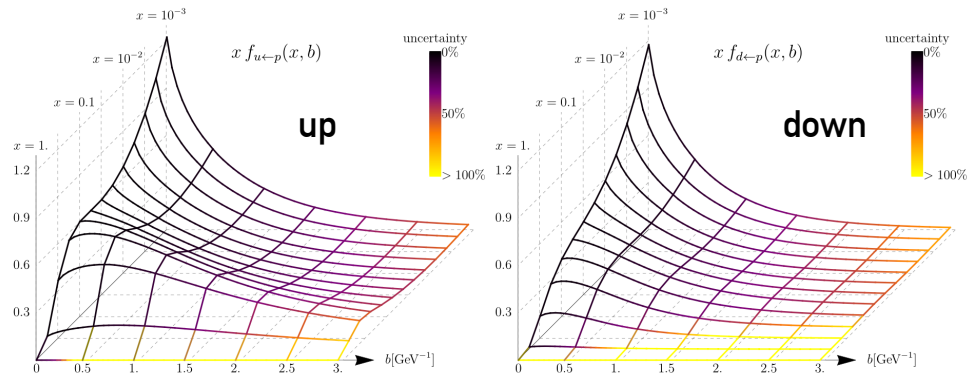
11 parameters



ART23

V. Moos, I. Scimemi, A. Vladimirov, P. Zurita
DOI: 10.1007/JHEP05(2024)036 - arXiv: 2305.07473

explicit flavor dependence



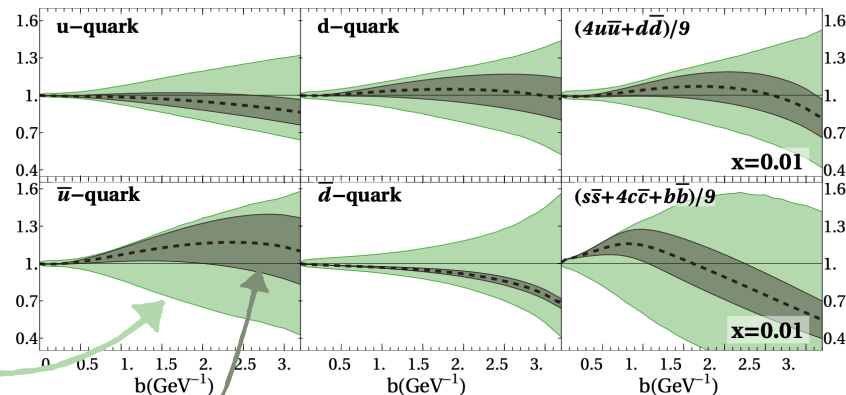
$$f_{\text{NP}}^f(x, b) = \frac{1}{\cosh\left(\left[\lambda_1^f (1-x) + \lambda_2^f x\right] b\right)}$$

10 + 3 parameters

extraction minimizes the PDF bias

N4LL

Γ_{cusp}	γ_V	$\mathcal{D}_{\text{small-b}}$	$C_{f \leftarrow f'}$	C_V	PDF
$a_s^5 (\Gamma_4)$	$a_s^4 (\gamma_4)$	$a_s^4 (d^{(4,0)})$	$a_s^3 (C_{f \leftarrow f'}^{[3]})$	a_s^4	NNLO



full uncertainty bands
in comparison to
the extraction at the central PDF replica

Extraction of unpolarized transverse momentum distributions from the fit of Drell-Yan data at N⁴LL

Valentin Moos,^a Ignazio Scimemi,^b Alexey Vladimirov,^b Pia Zurita^{a,b}

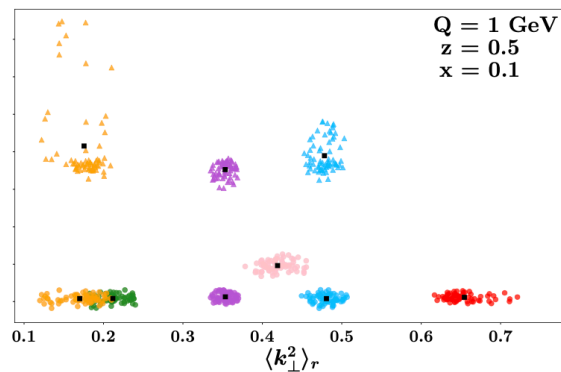
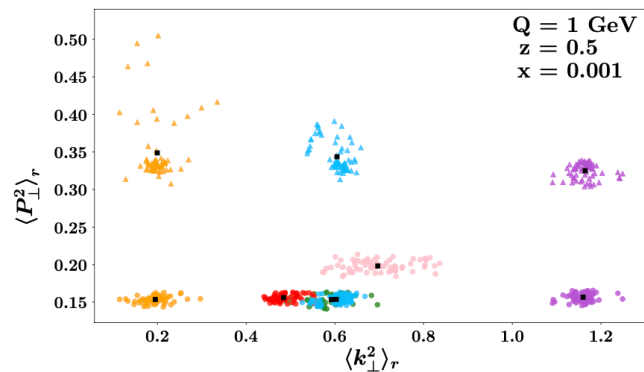
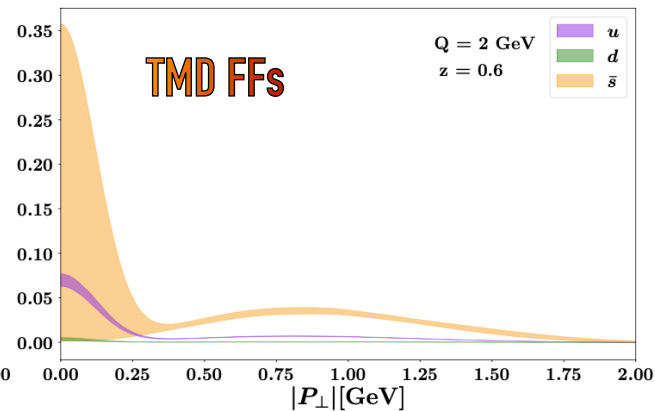
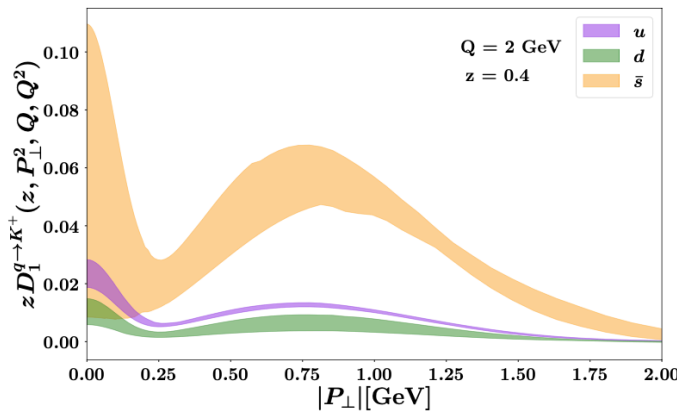
^aInstitut für Theoretische Physik, Universität Regensburg, Universitätsstraße 31, D-93040 Regensburg, Germany

^bDepartamento de Física Teórica & IPARCOS, Universidad Complutense de Madrid, Plaza de las Ciencias 1, E-28040 Madrid, Spain

E-mail: valentin.moos@physik.uni-regensburg.de, ignazio@ucm.es, alexeyvl@ucm.es, marzurit@ucm.es

MAP24

**b^* -prescription
with $b_{\min}$**



global fit: DY & SIDIS

f_{NP} same as in MAP22

96 parameters

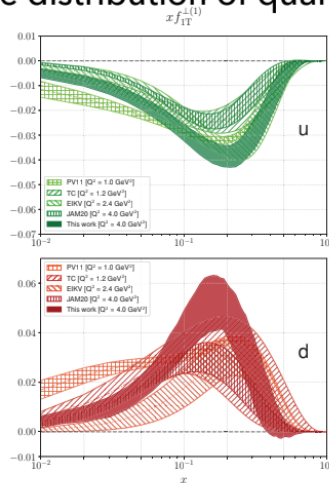
1 + (5 flavors $\times$ 10 parameters) for TMD PDFs, and
45 (5 channels $\times$ 9 parameters) for TMD FFs.

Sivers Function

comparison between extractions

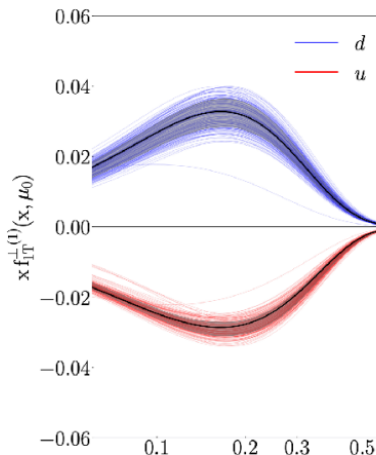
$$\rho_{N\uparrow}^q(x, k_x, k_y; Q^2) = f_1^q(x, k_T^2; Q^2) - \frac{k_x}{M} f_{1T}^{\perp q}(x, k_T^2; Q^2)$$

In a nucleon polarized in the +y direction,
the distribution of quarks can be distorted in the x direction



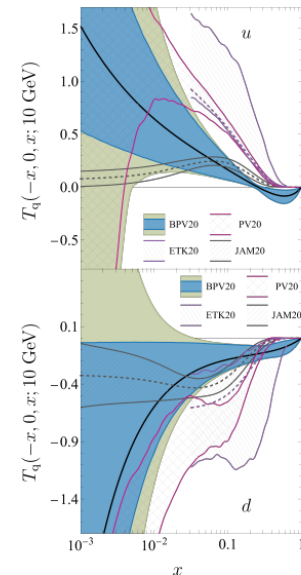
[Bacchetta, Delcarro,](#)

[Pisano, Radici, arXiv:2004.14278](#)



[Echevarria, Kang, Terry,](#)

[arXiv:2009.10710](#)

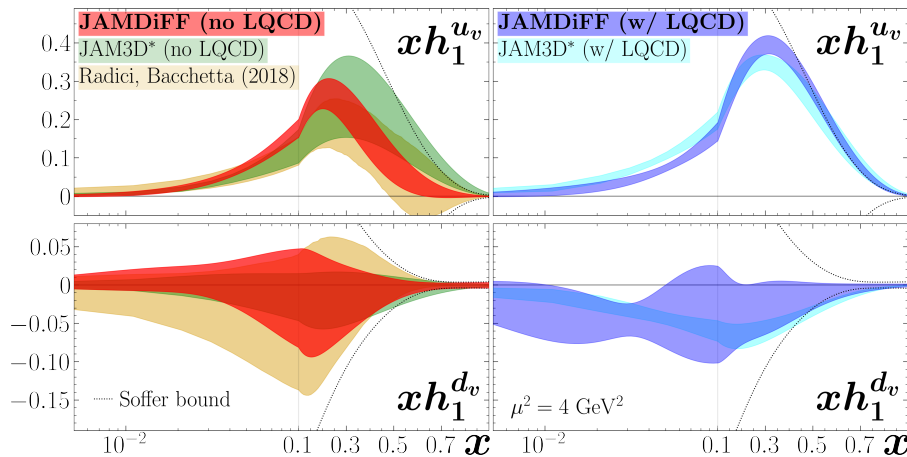


[Bury, Prokudin, Vladimirov,](#)

[arXiv:2103.03270](#)

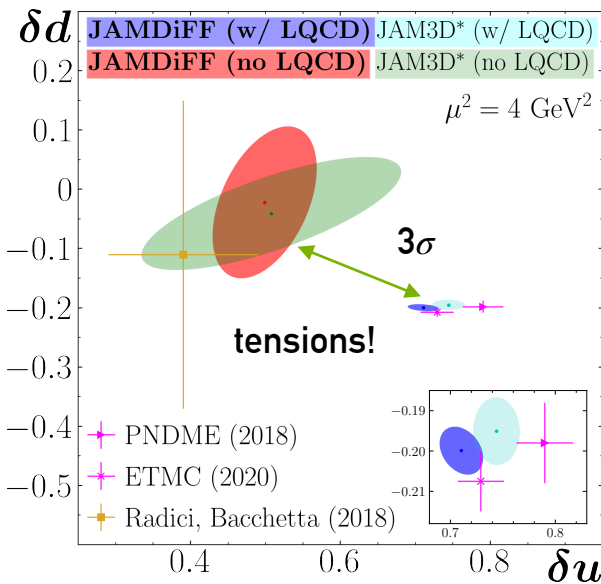
first simultaneous global analysis of the $\pi^+\pi^-$ DiFFs and transversity PDFs

h_1 quantifies the degree of transverse polarization of quarks within a transversely polarized nucleon.



e^+e^- , SIDIS, and pp data

LQCD data reduces uncertainties in the large- x region



inclusion of LQCD data on tensor charges in the fit

$$\delta u = \int_0^1 dx h_1^{u_v}(x; \mu), \quad \delta d = \int_0^1 dx h_1^{d_v}(x; \mu)$$

tensor charges

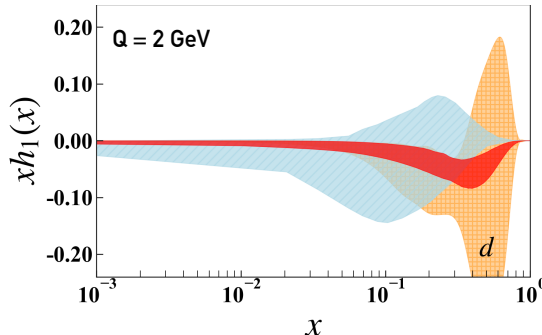
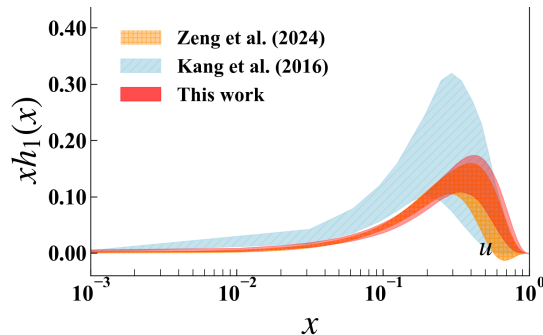
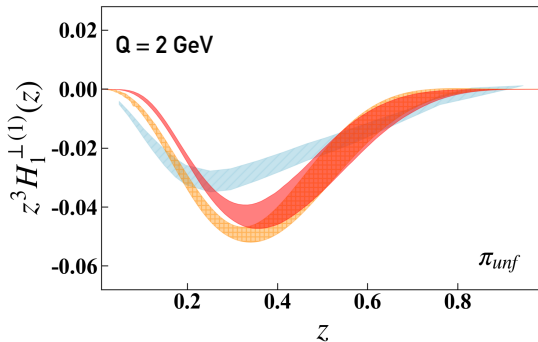
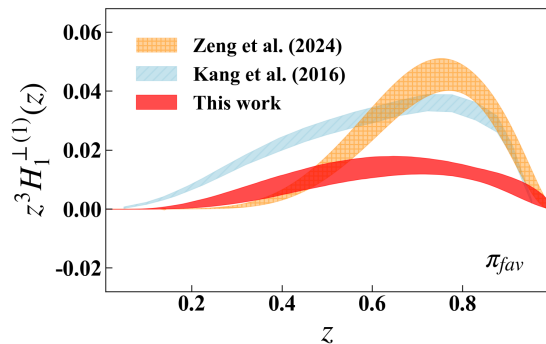
Phys. Rev. Lett. 132, 091901 (2024)
arXiv: 2306.12998

Global analysis of Sivers and Collins asymmetries

Chunhua Zeng, Hongxin Dong, Tianbo Liu, Peng Sun, Yuxiang Zhao

(Transverse Nucleon Tomography Collaboration)

arXiv:2412.18324



$$H_1^{\perp(1)}(z) = \int_0^{p_T^{\text{cut}}} d^2 p_T \frac{p_T^2}{2z^2 M_h^2} H_1^{\perp}(z, p_T),$$

cuts because of TMD formalism

$$h_1(x) = \int_0^{k_T^{\text{cut}}} d^2 k_T h_1(x, k_T).$$



studies slightly different



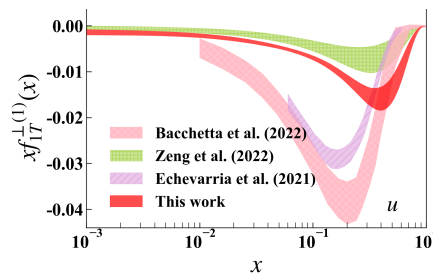
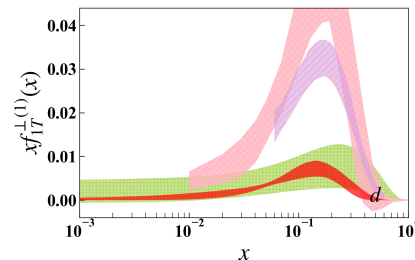
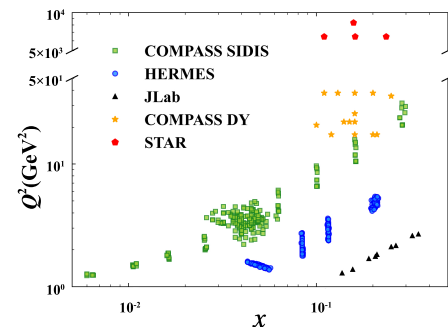
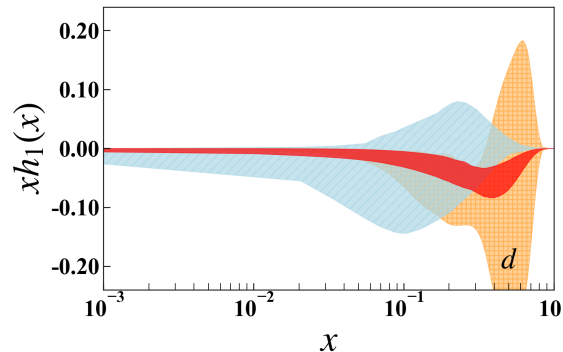
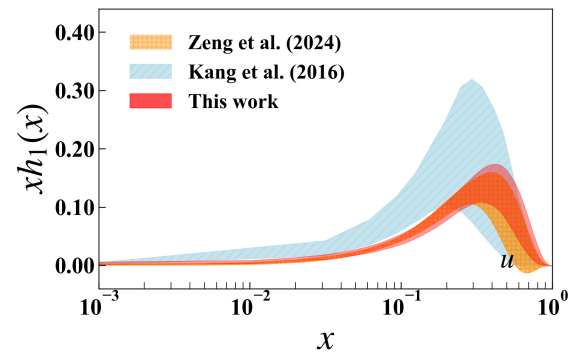
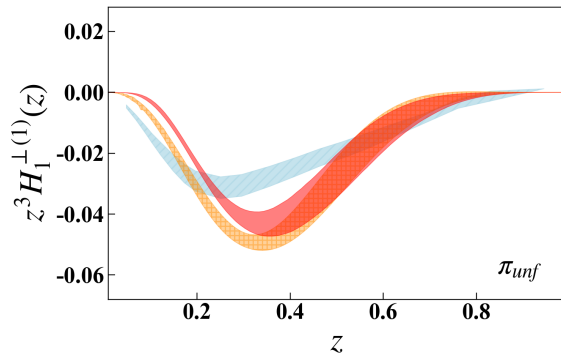
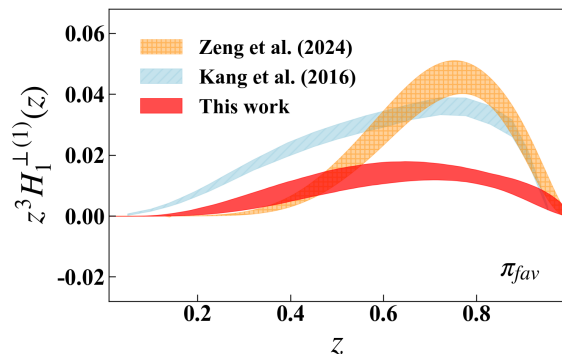
directly extracted as
collinear functions

Global analysis of Sivers and Collins asymmetries

Chunhua Zeng, Hongxin Dong, Tianbo Liu, Peng Sun, Yuxiang Zhao

(Transverse Nucleon Tomography Collaboration)

arXiv:2412.18324

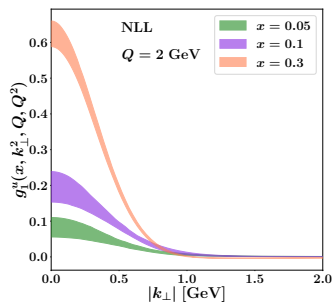
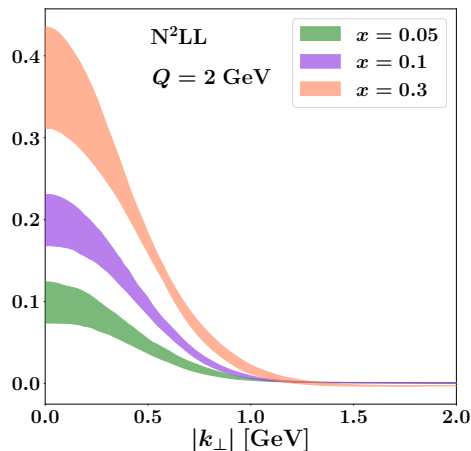


Helicity

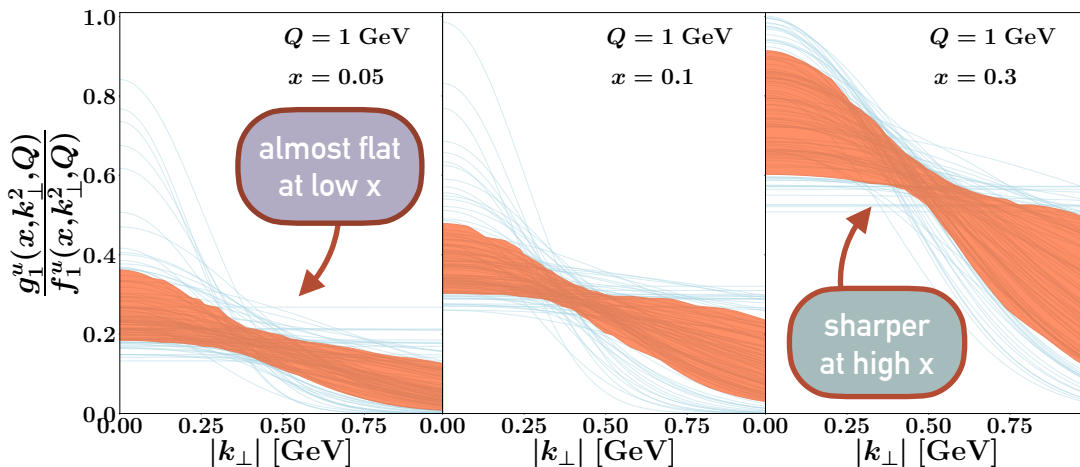
longitudinally polarized quarks

A. Bacchetta, A. Bongallino, M. Cerutti, M. Radici and L. Rossi
MAP Collaboration - [arXiv:2409.18078](https://arxiv.org/abs/2409.18078)

SIDIS data



$$A_1(x, z, Q, |P_{hT}|) = \frac{\sum_{a=q,\bar{q}} e_a^2 \int_0^{+\infty} d|b_T|^2 J_0\left(\frac{|b_T||P_{hT}|}{z}\right) \hat{g}_1^a(x, |b_T|^2, Q) \hat{D}_1^{a \rightarrow h}(z, |b_T|^2, Q)}{\sum_{a=q,\bar{q}} e_a^2 \int_0^{+\infty} d|b_T|^2 J_0\left(\frac{|b_T||P_{hT}|}{z}\right) \hat{f}_1^a(x, |b_T|^2, Q) \hat{D}_1^{a \rightarrow h}(z, |b_T|^2, Q)}$$



3 parameters

but poorly constrained due
to lack of data

MAP Collaboration

...a selection of some more works

on 3D hadron structure

- **Extraction of the Sivers function from SIDIS, Drell-Yan, and W / Z boson production data with TMD evolution**
M. Bury, A. Prokudin, A. Vladimirov –
DOI: 10.1007/JHEP05(2021)151, arXiv:2103.03270
- **Global analysis of polarized DIS and SIDIS data with improved small-x helicity evolution**
D. Adamiak, N. Baldonado, Y. V. Kovchegov, W. Melnitchouk, D. Pitonyak, N. Sato, M. D. Sievert, A. Tarasov, Y. Tawabutr (JAM Collaboration)
Phys. Rev. D 108, 114007 (2023) - arXiv: 2308.07461
- **Tomography of pions and protons via TMD distributions**
P. C. Barry, L. Gamberg, W. Melnitchouk, E. Moffat, D. Pitonyak, A. Prokudin, N. Sato (JAM Collaboration) - Phys. Rev. D 108, L091504 (2023) - arXiv: 2302.01192
- **Transversity distributions and tensor charges of the nucleon: extraction from dihadron production and their universal nature**
C. Cocuzza, A. Metz, D. Pitonyak, A. Prokudin, N. Sato, R. Seidl
Phys. Rev. Lett. 132, 091901 (2024), arXiv:2306.12998
- **Transverse momentum distributions at large x**
O. del Rio, A. Prokudin, I. Scimemi, A. Vladimirov - arXiv: 2501.17274
- **Transverse Momentum Moments**
C. Cocuzza, A. Metz, D. Pitonyak, A. Prokudin, N. Sato, R. Seidl
Phys.Rev.D 110 (2024), arXiv: 2402.01836



TMD phenomenology

Status and Future Directions

Unpolarized Quark TMDs

- Precision era: extracted from fits of large datasets with high perturbative accuracy. Flavor dependence.

Polarized Quark TMDs

- great progress in extracting polarized
- TMDs (Sivers, Helicity, Transversity)

NN fits

Gluon TMDs

- Complete leading twist classification with process dependence and evolution properties
- Few phenomenological studies exist due to scarce experimental information.
- Progress expected with more experimental data (EIC)



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