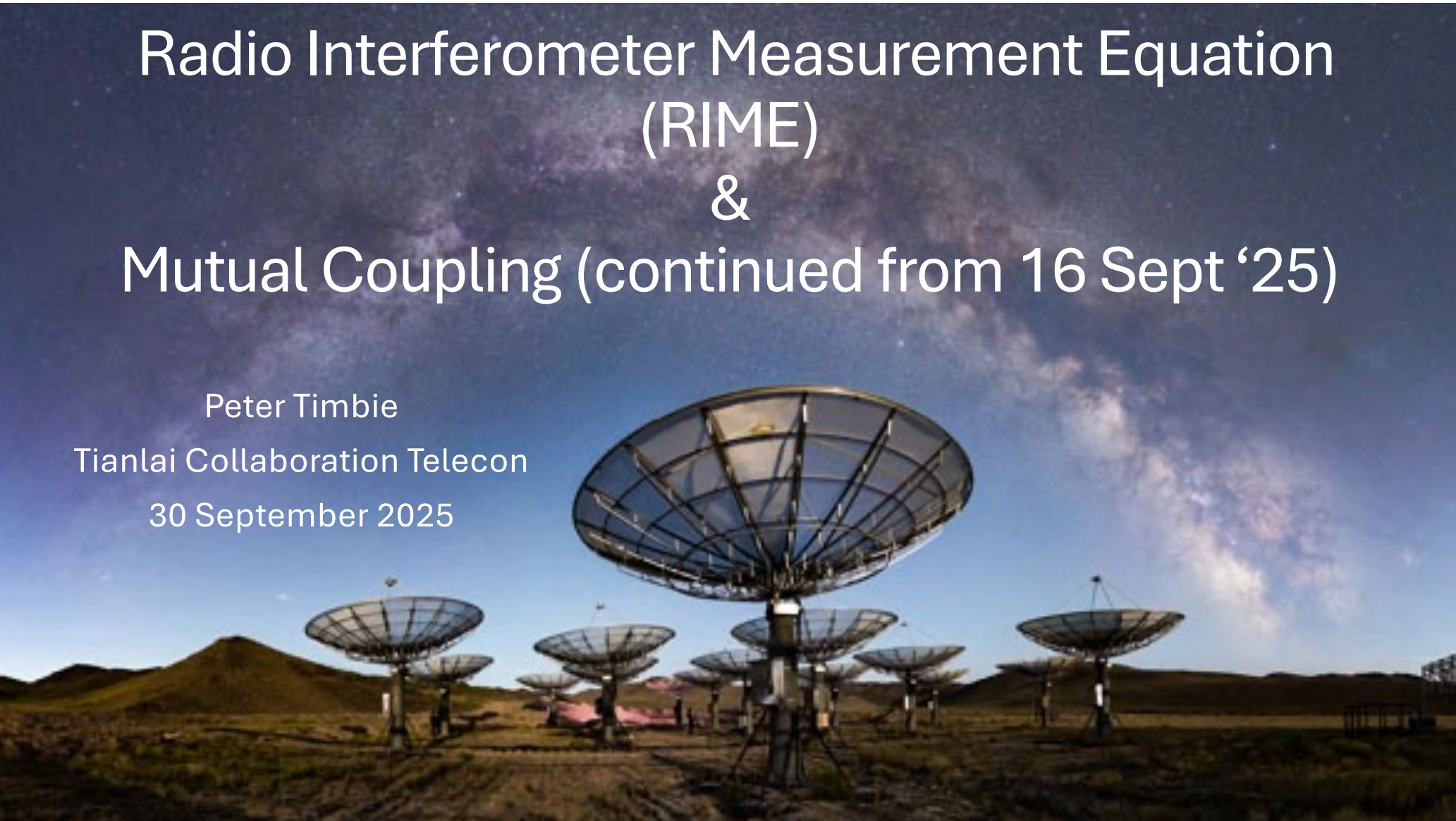


# Radio Interferometer Measurement Equation (RIME) & Mutual Coupling (continued from 16 Sept '25)

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**Voltage** at an antenna ' $p$ ' from a point source is a product of 2 x 2 **Jones matrices**:

Polarizations ' $a$ ' and ' $b$ '

$$\begin{pmatrix} v_{pa} \\ v_{pb} \end{pmatrix} = \mathbf{v}_p = \mathbf{J} \mathbf{e} = \mathbf{J}_n \mathbf{J}_{n-1} \dots \mathbf{J}_1 \mathbf{e}$$

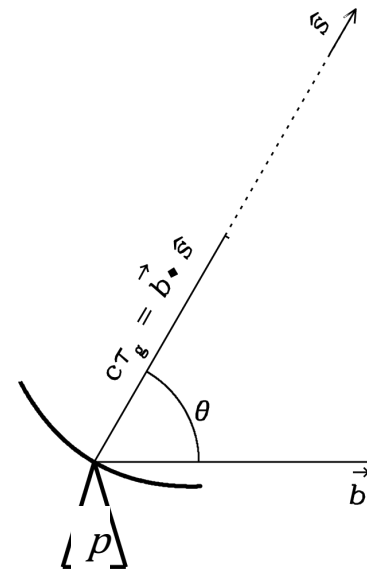
$$= \mathbf{G}_p \mathbf{E}_p \mathbf{K}_p \mathbf{e}$$

Direction  
Independent  
Gain

Direction  
Dependent  
Gain

'Phase delay'

$$e^{i2\pi \vec{b} \cdot \hat{s}} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$



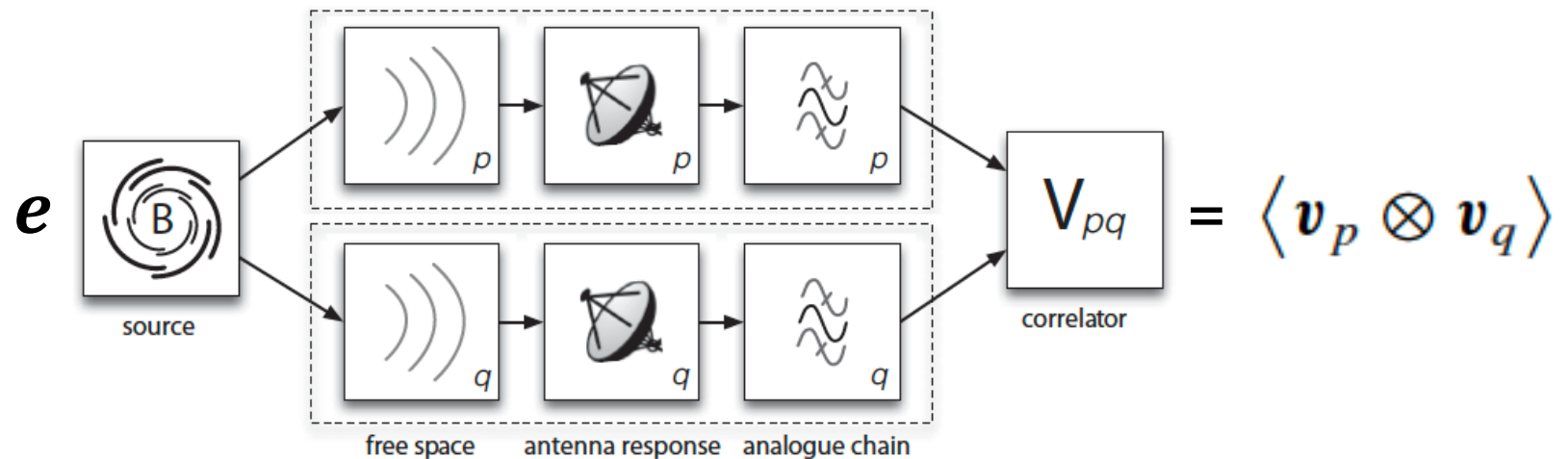
$$\mathbf{e} = \begin{pmatrix} e_x \\ e_y \end{pmatrix}$$

R. Clark Jones





# **Visibility:** Radio Interferometer Measurement Equation 'RIME'



$$V_{pq} = \langle \mathbf{v}_p \otimes \mathbf{v}_q \rangle$$

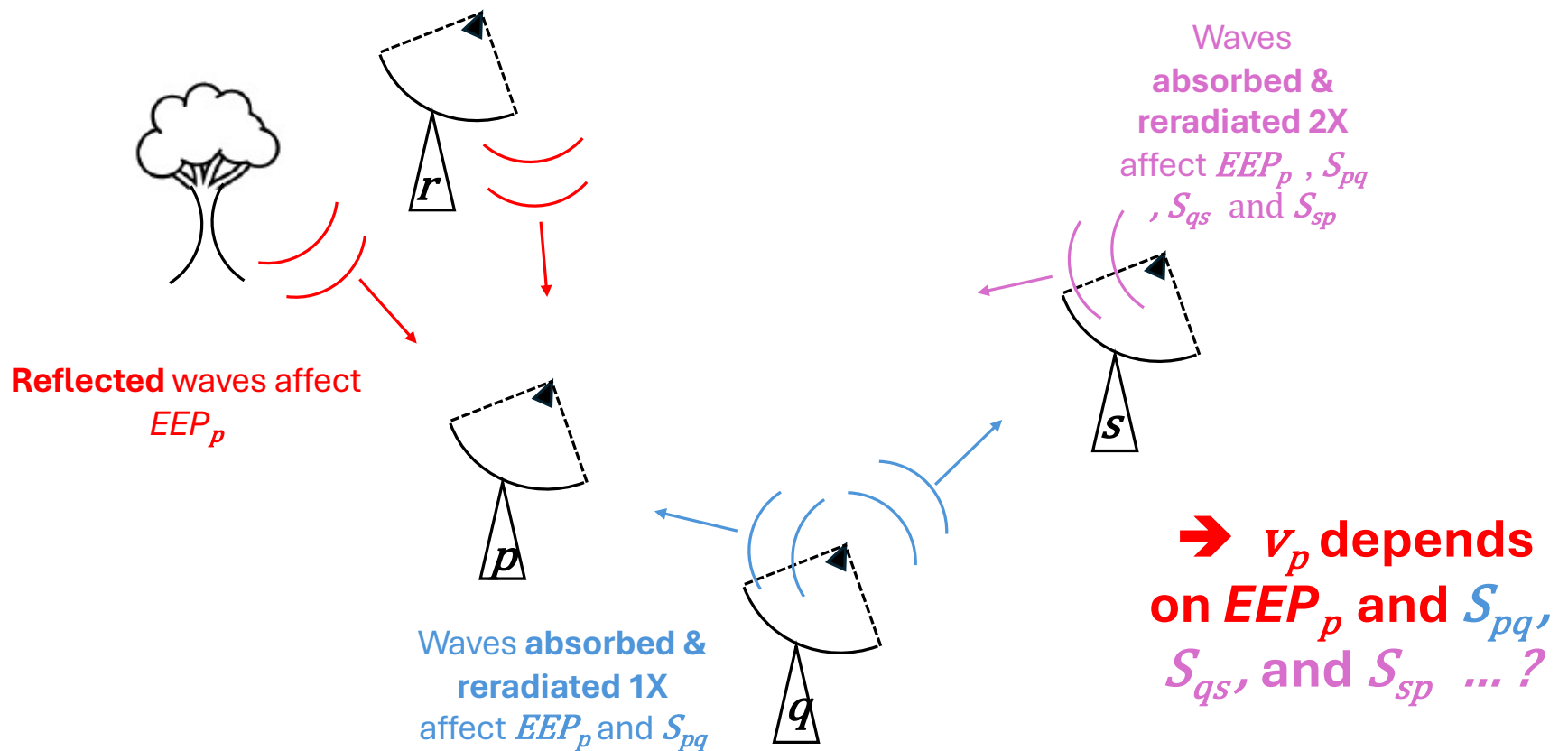
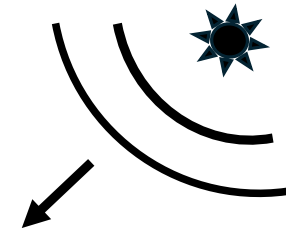
$$\mathbf{G}_q \mathbf{E}_q \mathbf{K}_q \mathbf{e} = \mathbf{v}_q$$

product of Jones matrices

(Hamaker 1996, Smirnov 2011)



# ***Mutual Coupling*** changes 'Embedded Element Patterns' (***EEPs***) & scattering (***S***) parameters





**If we knew all the S parameters (and beam patterns, EEPs) for an array, how would we account for them in a self-consistent way?**

$$\begin{pmatrix} v_1^- \\ v_2^- \\ \vdots \\ v_n^- \end{pmatrix} = \begin{pmatrix} S_{11} & S_{12} & \cdots & S_{1n} \\ S_{21} & & & \vdots \\ \vdots & & \ddots & \vdots \\ S_{n1} & \cdots & \cdots & S_{nn} \end{pmatrix} \begin{pmatrix} v_1^+ \\ v_2^+ \\ \vdots \\ v_n^+ \end{pmatrix}$$

Voltage wave incident on port n

Voltage wave reflected from port n