



# Measurement of the CKM angle $\beta$ at *BaBar*

Roberto Covarelli

(University-INFN Perugia, Italy)

on behalf of the *BaBar* collaboration

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# CP violation and the $\beta$ angle

- CP violation in the Standard Model (SM)

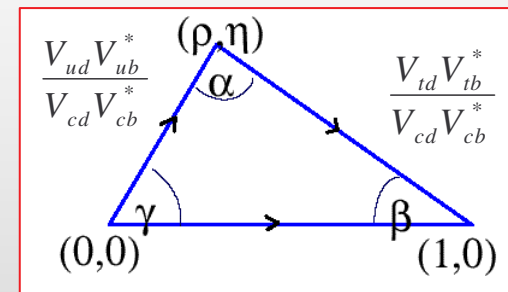
$\Leftrightarrow$

CP-odd phase in the CKM matrix

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

$\Leftrightarrow$

Non-null apex of the **unitarity triangle** ( $\eta \neq 0$ )



- How to measure it?**  $\rightarrow$  in  $B^0$  meson system CP violation effect in the interference between mixing and decay:

$$\Gamma(B^0(t) \rightarrow f_{CP}) \neq \Gamma(\bar{B}^0(t) \rightarrow f_{CP})$$

- Time-dependent asymmetry:

$$A_{CP}(t) = \frac{\Gamma(\bar{B}^0(t) \rightarrow f_{CP}) - \Gamma(B^0(t) \rightarrow f_{CP})}{\Gamma(\bar{B}^0(t) \rightarrow f_{CP}) + \Gamma(B^0(t) \rightarrow f_{CP})} = S_f \sin(\Delta m t) - C_f \cos(\Delta m t)$$

$$S_f = -\frac{2 \text{Im } \lambda}{1 + |\lambda|^2}$$

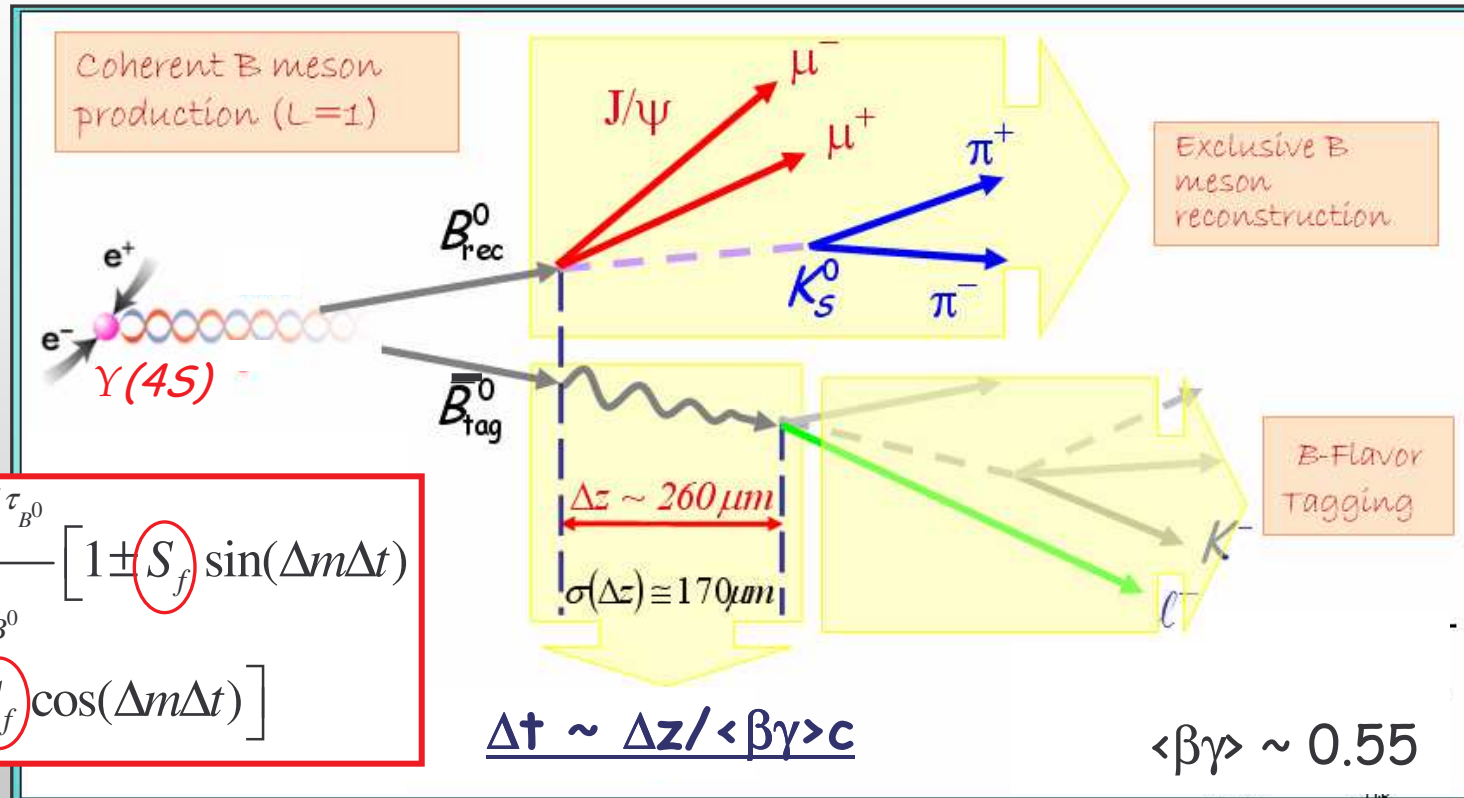
$$C_f = \frac{1 - |\lambda|^2}{1 + |\lambda|^2}$$

$$\lambda = \frac{q}{p} \cdot \frac{\bar{A}_f}{A_f}$$

Difference of mass eigenstates



# CP violation at the $\Upsilon(4S)$



$$f_{\pm}(\Delta t) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \left[ 1 \pm S_f \sin(\Delta m \Delta t) \mp C_f \cos(\Delta m \Delta t) \right]$$

In all modes considered in this talk the SM expectations are:

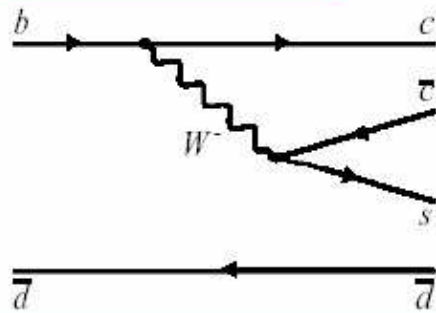
$$C_f = 0$$

$$S_f = \pm \sin 2\beta$$

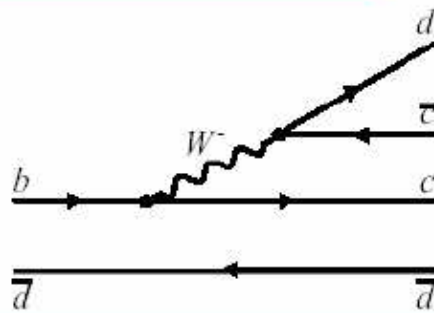


# Many ways of measuring $\beta$ ...

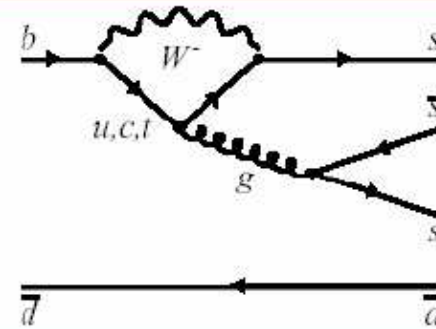
a)  $b \rightarrow c\bar{c}s$   
(charmonium)



b)  $b \rightarrow c\bar{c}d$  charm  
(and charmonium)



c) Penguin-dominated  
 $b \rightarrow d\bar{d}s, b \rightarrow s\bar{s}s$



$J/\psi K_S^0, \psi(2S)K_S^0, \chi_{c1}K_S^0,$   
 $\eta_c K_S^0, J/\psi K_L^0,$   
 $J/\psi K^{*0} (K^{*0} \rightarrow K_S^0 \pi^0)$

$D^{*+}D^-, D^+D^-$   
 $J/\psi \pi^0, D^{*+}D^{*-}$

$\phi K^0, K^+K^-K_S^0,$   
 $K_S^0 K_S^0 K_S^0, \eta' K^0, K_S^0 \pi^0,$   
 $\omega K_S^0, f_0(980)K_S^0$

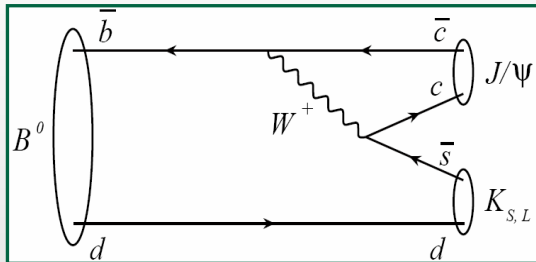
Large tree amplitude  
Low penguin pollution

Both tree and penguin  
amplitudes Cabibbo-  
suppressed: small BF's

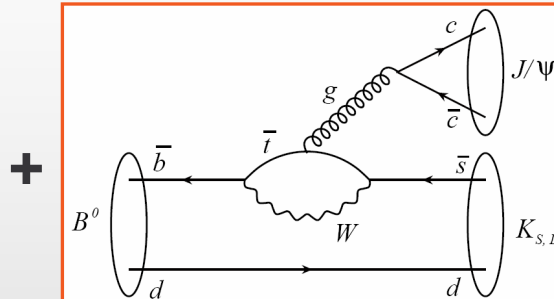
No tree: sensitivity to  
New Physics particles  
in the loop



# 1) $b \rightarrow c\bar{c}s$ (charmonium)



Color-suppressed tree



Gluonic penguin  
(same weak phase)

- Experimentally clean
- $\text{BF} = \text{O}(10^{-3}) \div \text{O}(10^{-4})$
- Still “golden-plated” channels
- In the SM:

$$\mathcal{A}_{\text{penguin}} \ll \mathcal{A}_{\text{tree}}$$

- Theoretical uncertainties on  $\Delta S_f = S_f - \sin 2\beta$ :

– Factorization + non-perturbative QCD:

- $\Delta S_{J/\psi K_s} = (-2.2 \pm 2.2) \cdot 10^{-4}$  [Boos et al., PRD 70, 036006 (2004)]
- $\Delta S_{J/\psi K_s} = (9.3^{+3.6}_{-4.6}) \cdot 10^{-4}$  [Li and Mishima, hep-ph/0610120]

– Model-independent data-driven calculation:  $\Delta S$  is constrained using measurements of the SU(3)-related process  $B^0 \rightarrow J/\psi\pi^0$ :

$$\Delta S_{J/\psi K_s} = (0.000 \pm 0.012) \quad [\text{Ciuchini et al., PRL 95, 221804 (2005)}]$$

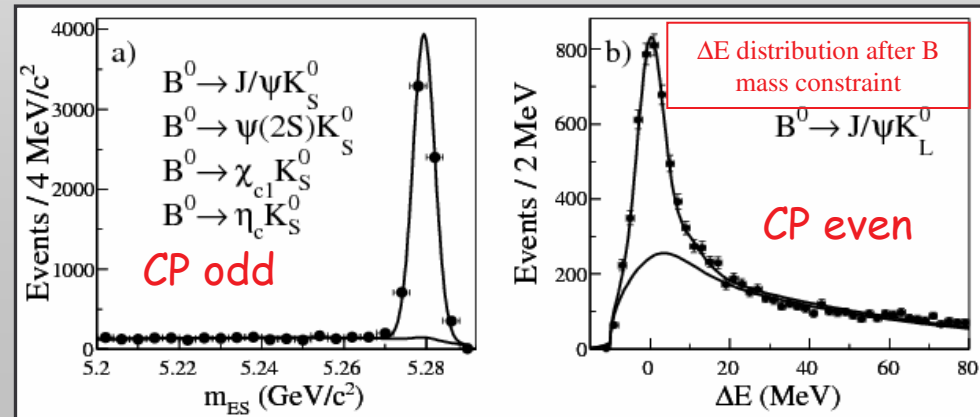
[Ciuchini at CKM 2006]



# $\sin 2\beta$ from $B^0 \rightarrow (c\bar{c})K^{(*)0}$ (I)

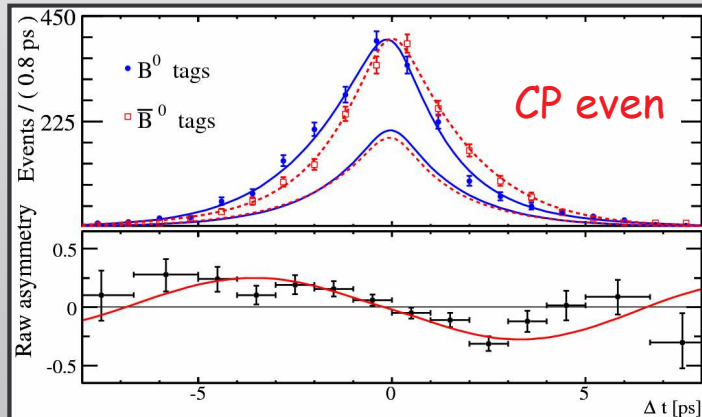
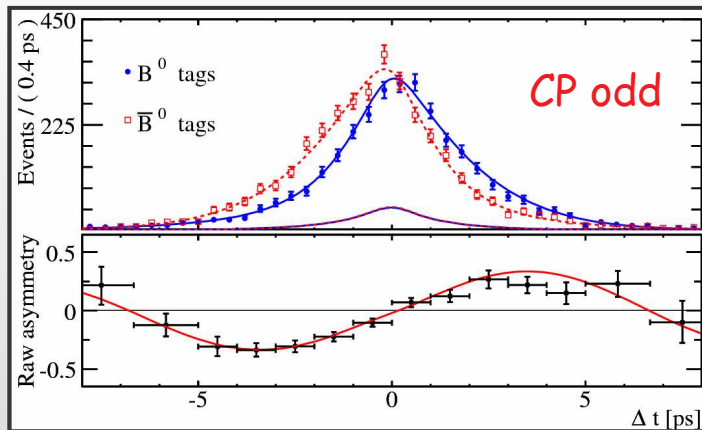
- “Reference”  $\sin 2\beta$  measurement (  $O(\%)$  uncertainty )
- Improvements with respect to previous BaBar measurements:
  - Using **full BaBar statistics**:  $383 \cdot 10^6 \text{ } B\bar{B}$  pairs
  - **Alternative  $\Delta t$  fit configurations** added to the nominal one (all even/odd modes together):
    - Fit of  $\sin 2\beta$  and  $|\lambda|$  for each mode separately
    - Fit of  $\sin 2\beta$  and  $|\lambda|$  for  $J/\psi K^0$  ( $K_S + K_L$ ) and  $J/\psi K_S$  only
  - Now including  $J/\psi K^{*0}$  ( $K_S \pi^0$ ) and  $J/\psi K_L$  in the  $|\lambda|$  measurement
  - Reduction of **systematic error** related to **backgrounds**

Sample	$N_{\text{events}}$	Purity (%)
CP-odd	6873	92
CP-even	4730	55
$J/\psi K^{*0}$	1056	66





# $\sin 2\beta$ from $B^0 \rightarrow (c\bar{c})K^{(*)0}$ (II)



hep-ex/0703021, submitted to PRL

$$\sin 2\beta = 0.714 \pm 0.032(\text{stat}) \pm 0.018(\text{syst})$$

$$|\lambda| = 0.952 \pm 0.022(\text{stat}) \pm 0.017(\text{syst})$$

- ~5% total uncertainty on  $\sin 2\beta$
- $|\lambda|$  result compatible with 1 at  $1.7\sigma$

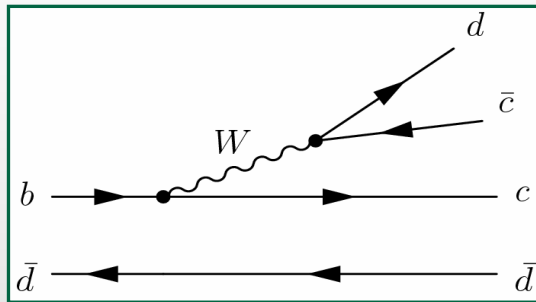
$\sin 2\beta$  result split in sub-modes:

$J/\psi K_S (\pi^+\pi^-)$	■	$0.702 \pm 0.042 \pm 0.020$
$J/\psi K_S (\pi^0\pi^0)$	■	$0.617 \pm 0.103 \pm 0.036$
$\psi(2S)K_S$	■	$0.947 \pm 0.112 \pm 0.062$
$\chi_{c1}K_S$	■	$0.759 \pm 0.170 \pm 0.037$
$\eta_c K_S$	■	$0.778 \pm 0.195 \pm 0.093$
$J/\psi K^{*+}$	■	$0.477 \pm 0.271 \pm 0.155$
$J/\psi K_S$	■	$0.686 \pm 0.039 \pm 0.015$
$J/\psi K_L$	■	$0.735 \pm 0.074 \pm 0.067$
$J/\psi K^0$	■	$0.697 \pm 0.035 \pm 0.016$
<b>All</b>	■	<b><math>0.714 \pm 0.032 \pm 0.018</math></b>



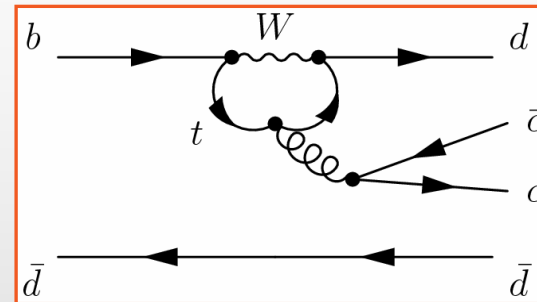


## 2) $b \rightarrow c\bar{c}d$ transitions



Cabibbo-suppressed tree

+



Gluonic penguin  
(different weak phase)

- $\text{BF}(B^0 \rightarrow D^{(*)}D^{(*)}) = \mathcal{O}(10^{-4})$
- Expected penguin contribution negligible: 2-10%  
[Z.-Z. Xing, Phys. Rev. D 61, 014010 (2000)]
- $\beta_{\text{eff}}$  (i.e.  $\beta$  angle as effectively measured in such processes)  
sensitive to New Physics in loops:  $\beta_{\text{eff}} - \beta$  up to 0.6 in  
supersymmetric models

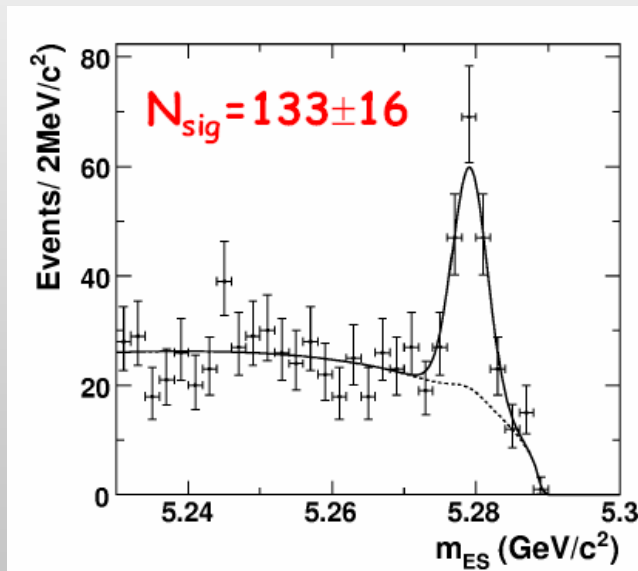
[Y. Grossman and M. Worah, Phys. Lett. B 395, 241 (1997)]





# Recent results: $B^0 \rightarrow D^+D^-$

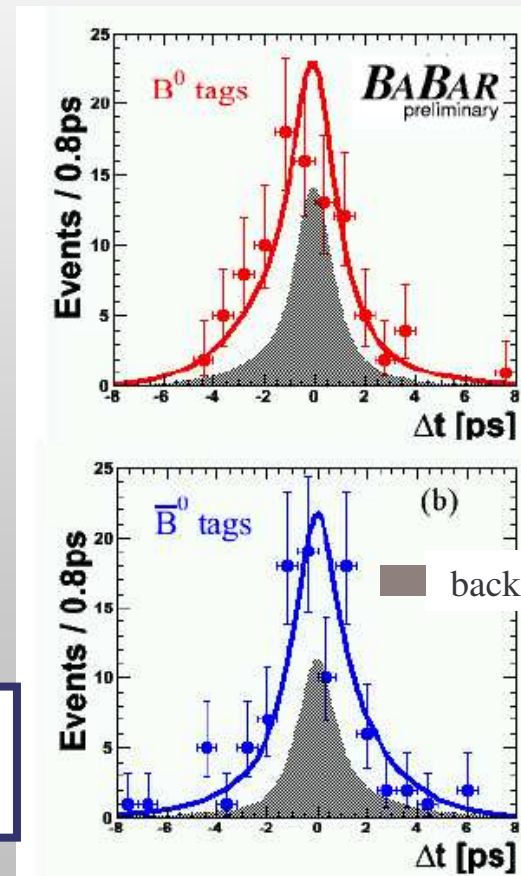
- Claim of a large CP violation measurement by Belle in  $B^0 \rightarrow D^+D^-$ :  
( $C_{DD}, S_{DD}$ )  $\neq$  (0, 0) at  $4.1\sigma$  [hep-ex/0702031, submitted to PRL]
- BaBar **does not** confirm observation:



$364 \cdot 10^6 \text{ } B\bar{B}$  pairs

D. Lange at  
Moriond 2007,  
PRELIMINARY

$$\sin 2\beta_{\text{eff}} = 0.54 \pm 0.34(\text{stat}) \pm 0.06(\text{syst})$$
$$C = 0.11 \pm 0.22(\text{stat}) \pm 0.07(\text{syst})$$





# $B^0 \rightarrow D^{*+}D^-$ and $B^0 \rightarrow D^+D^{*-}$

- Not a CP eigenstate: need to define  $C_{+}/C_{-}$  and  $S_{+}/S_{-}$  that depend on the **strong phase difference** between the two processes.

- General relation:  $S_{\pm\mp} = -\sqrt{1 - C_{\pm\mp}^2} \sin(2\beta_{eff} \pm \delta)$

$364 \cdot 10^6 \bar{B}B$  pairs

- If penguin contribution is negligible:  $\beta_{eff} = \beta$ ,  $C_{+-} = -C_{-+}$

- Signal of **CP violation**:

$$\sin 2\beta \neq 0 \iff S_{+-} \neq -S_{-+}$$

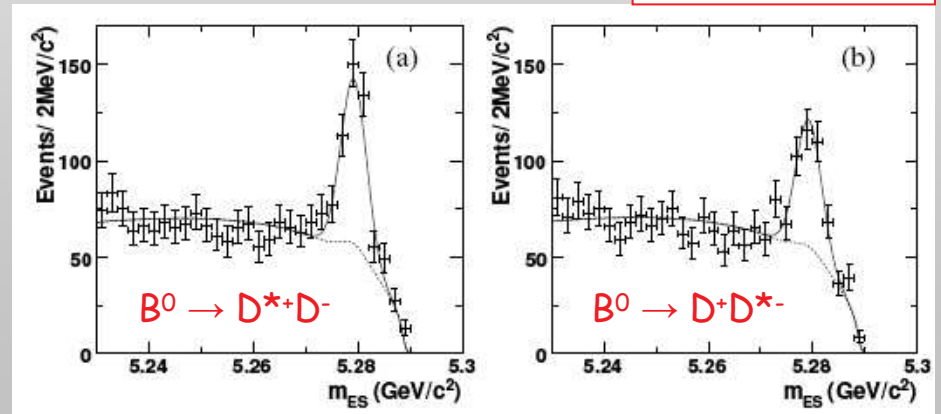
D. Lange at  
Moriond 2007,  
PRELIMINARY

$$C_{+-} = 0.18 \pm 0.15(\text{stat}) \pm 0.04(\text{syst})$$

$$C_{-+} = 0.23 \pm 0.15(\text{stat}) \pm 0.04(\text{syst})$$

$$S_{+-} = -0.79 \pm 0.21(\text{stat}) \pm 0.06(\text{syst})$$

$$S_{-+} = -0.44 \pm 0.22(\text{stat}) \pm 0.06(\text{syst})$$



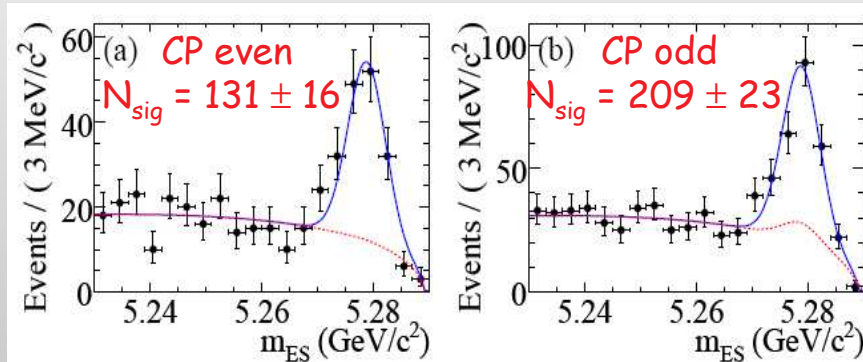


# Recent results: $B^0 \rightarrow D^{(*)0} h^0$

- Used modes:  $h^0 = \pi^0, \eta, \omega$      $D^0 = D^0_{CP} \rightarrow K^+K^-, K_S\pi^0, K_S\omega$
- $b \rightarrow \bar{c}u\bar{d}$  transition:
  - No penguin contribution  $\rightarrow$  theoretically clean
  - Very small contribution from DCS decays ( $b \rightarrow u\bar{c}d$ )

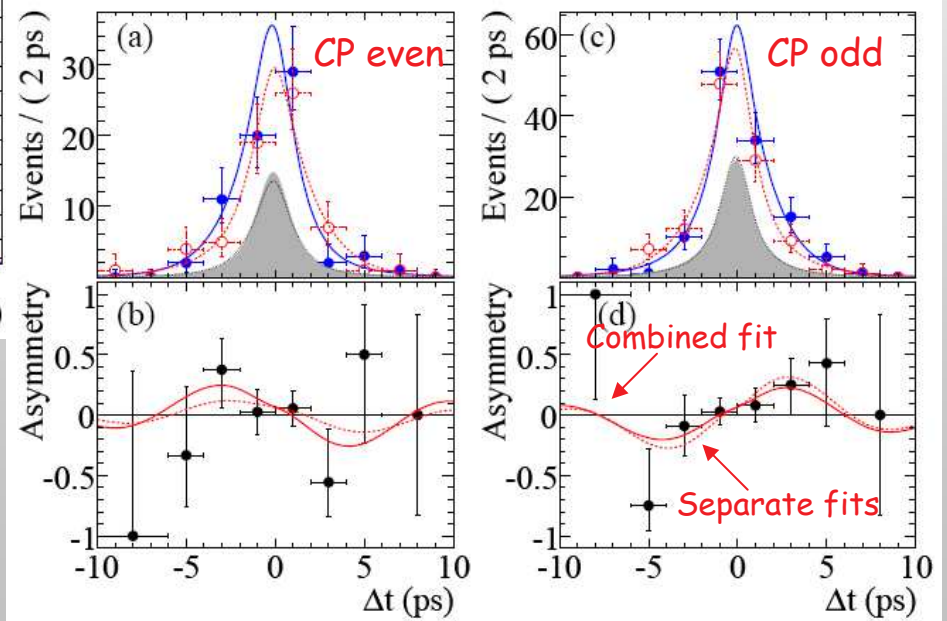
hep-ex/0703019, submitted to PRL

$383 \cdot 10^6 \bar{B}B$  pairs



$$\sin 2\beta_{eff} = 0.56 \pm 0.23(\text{stat}) \pm 0.05(\text{syst})$$

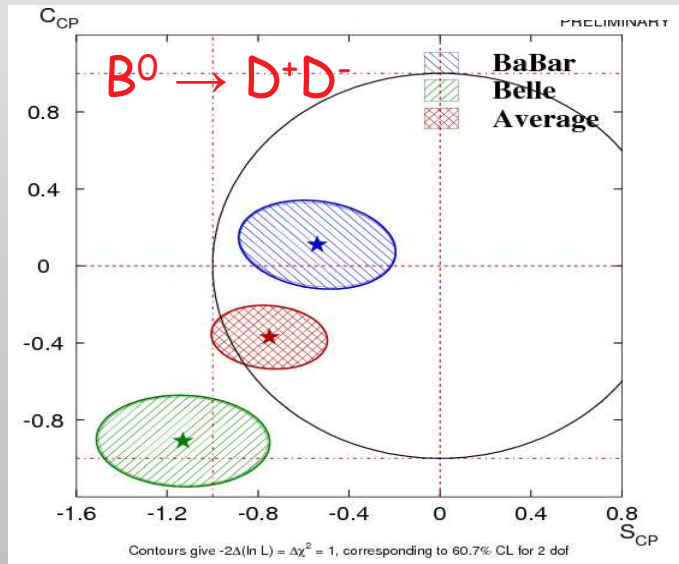
$$C = -0.23 \pm 0.16(\text{stat}) \pm 0.04(\text{syst})$$





# Summary of $b \rightarrow c\bar{c}d$ ( $c\bar{u}d$ )

- $B^0 \rightarrow D^+D^-$ 
  - No evidence of CP violation measured
  - $\sim 3\sigma$  disagreement between BaBar and Belle results



- $B^0 \rightarrow D^{*+}D^-, D^+D^{*-}$

$S(D^{*+}D^-)$ BABAR	$-0.79 \pm 0.21 \pm 0.06$
$S(D^{*+}D^-)$ Belle	$-0.55 \pm 0.39 \pm 0.12$
$S(D^{*+}D^-)$ Ave.	$-0.74 \pm 0.19$
<hr/>	
$S(D^+D^{*-})$ BABAR	$-0.44 \pm 0.22 \pm 0.04$
$S(D^+D^{*-})$ Belle	$-0.96 \pm 0.43 \pm 0.06$
$S(D^+D^{*-})$ Ave.	$-0.55 \pm 0.20$

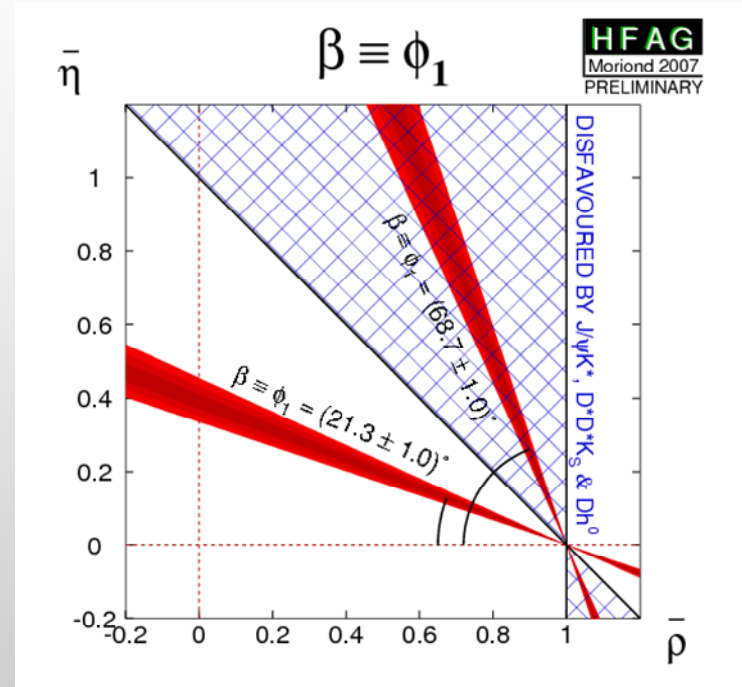
- Hints of CPV when combining Babar and Belle results:  $S_{+-} \neq -S_{-+}$  at  $\sim 4\sigma$

- $B^0 \rightarrow D^{(*)0}h^0$  (first measurement)
  - Both  $\sin 2\beta_{eff}$  and  $C$  consistent with SM expectations



# Resolving the $\beta$ ambiguity

- When extracting  $\beta$  from  $\sin 2\beta$ , two-fold ambiguity left in the  $\rho$ - $\eta$  positive quadrant
- $\cos 2\beta$  is measured from time-dependent analyses of  $J/\psi K^*$ ,  $D^0 h^0$ ,  $D^{*+} D^{*-} K_S$
- Recent BaBar results:
  - Time-dependent Dalitz analysis of  $B^0 \rightarrow D^{(*)0} h^0$  ( $D^0 \rightarrow K_S \pi^+ \pi^-$ )



Integrals over Dalitz phase space: positive under certain theoretical assumptions

$\cos 2\beta > 0$  at 87% CL

hep-ex/0607105, PRELIMINARY

- Time-dependent Dalitz analysis of  $B^0 \rightarrow D^{*+} D^{*-} K_S$ :

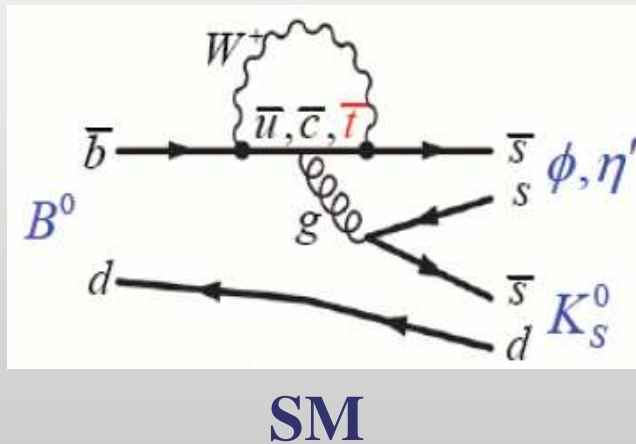
$(J_{s2}/J_0) \cos 2\beta > 0$  at 94% CL

Phys. Rev. D 74, 091101 (2006)

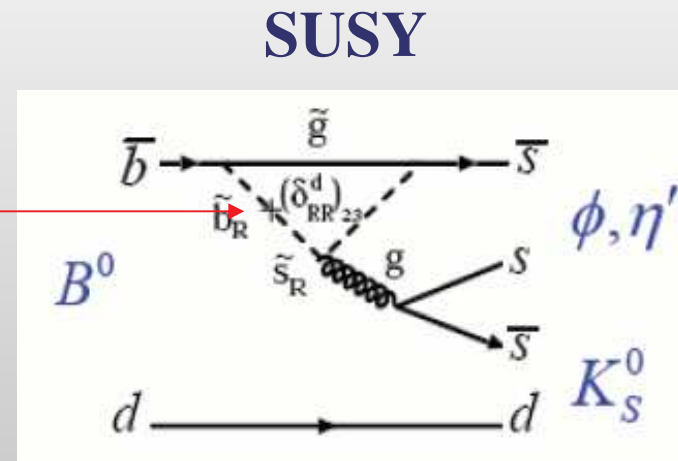


# 3) $\beta$ in penguins: motivations

- Pure  $b \rightarrow s\bar{s}$  transitions include a Flavor Changing Neutral Current: in the SM they must proceed through a **penguin diagram**
- $b \rightarrow d\bar{d}s$  (and similar): theoretical calculation predict penguin-dominated



SUSY coupling:  
 - mass-suppressed ( $\sim 1/M^2$ )  
 - coupling-enhanced ( $\sim \alpha_s/\alpha_w$ )



- Quark-squark coupling adds unknown SUSY phases to the mixing phase  $2\beta \rightarrow A_{CP}(\Delta t)$  sensitive to presence of new particles in the loop
- **Caveat:** interpretation of  $\beta_{eff} - \beta$  not completely clean in all cases due to **hadronic uncertainties**

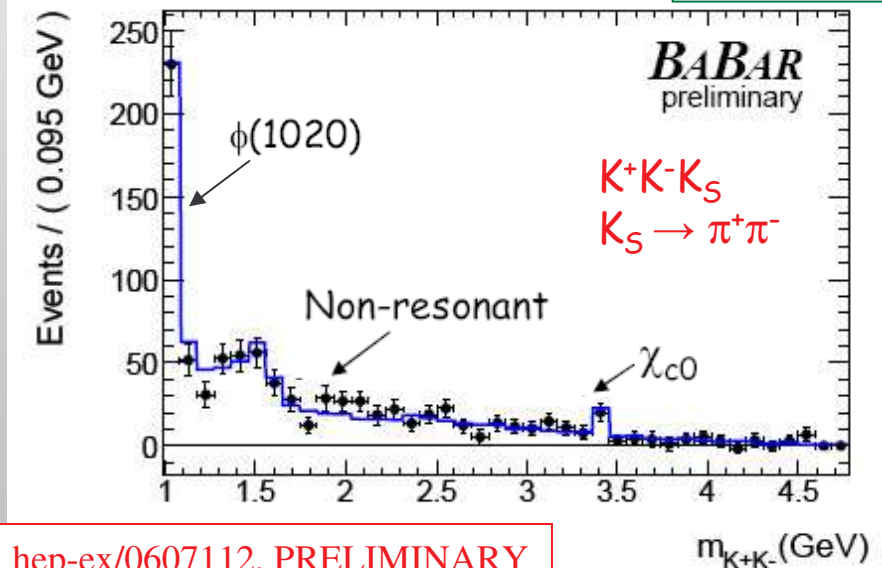




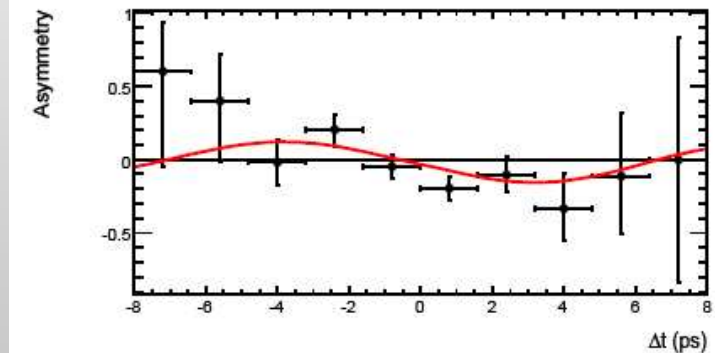
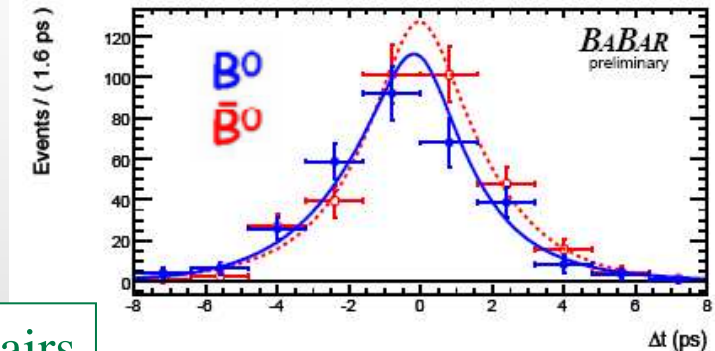
# Dalitz analysis of $B^0 \rightarrow K^+K^-K^0$

- Time-dependent Dalitz analysis:
  - Taking for the first time into account interference between high and low KK mass (close to  $\phi$  resonance) regions

$347 \cdot 10^6 B\bar{B}$  pairs



hep-ex/0607112, PRELIMINARY



Combined (whole Dalitz plot):

$\beta_{eff} = 0.361 \pm 0.079(\text{stat}) \pm 0.037(\text{syst})$

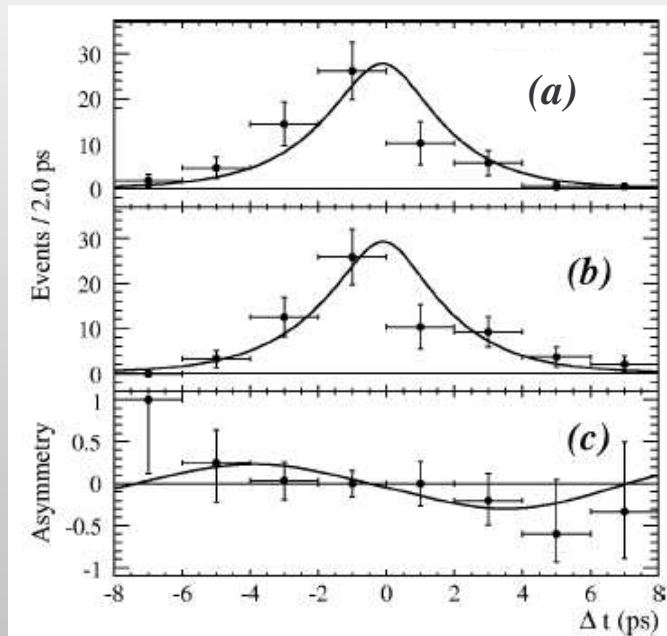
$C = 0.034 \pm 0.079(\text{stat}) \pm 0.025(\text{syst})$





# $B^0 \rightarrow K_S K_S K_S$ and $B^0 \rightarrow \eta' K^0$

- $B^0 \rightarrow K_S K_S K_S$ : hep-ex/0702046,  
Submitted to PRL
  - Challenging vertex reconstruction (beam-spot constraint used)



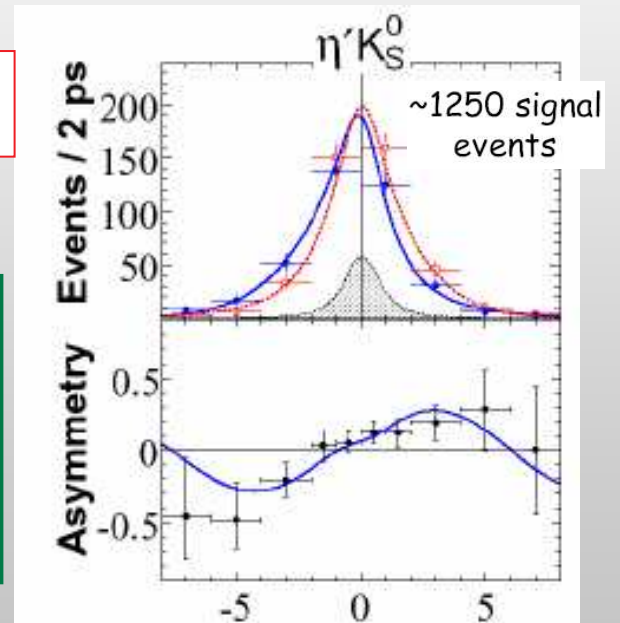
$$\sin 2\beta_{eff} = 0.71 \pm 0.24(\text{stat}) \pm 0.04(\text{syst})$$

$$C = 0.02 \pm 0.21(\text{stat}) \pm 0.05(\text{syst})$$

- $B^0 \rightarrow \eta' K^0$ :
  - Large BF ( $\sim 6 \cdot 10^{-5}$ )
  - Many  $\eta'$  reconstruction modes

Phys.Rev.Lett. 98,  
031801 (2007)

**Evidence of CPV with  $> 5\sigma$  significance**



$$\sin 2\beta_{eff} = 0.58 \pm 0.10(\text{stat}) \pm 0.03(\text{syst})$$

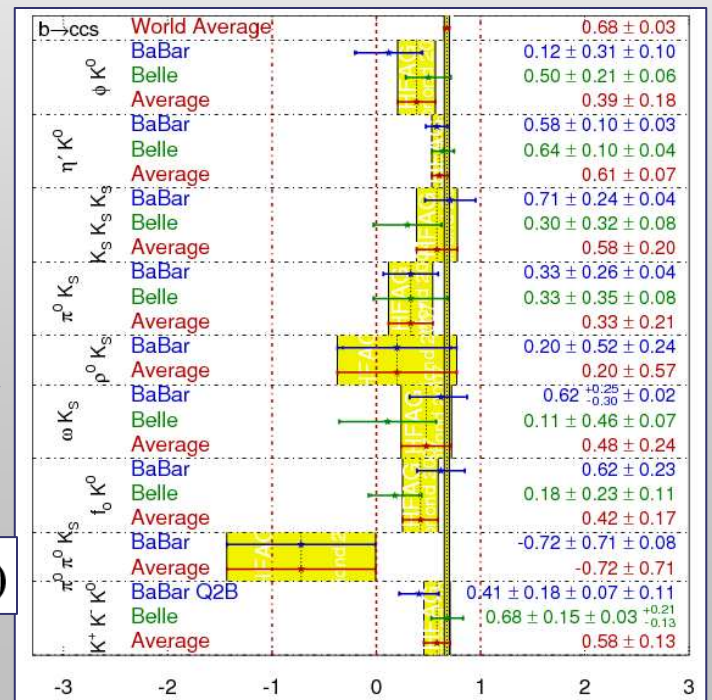
$$C = -0.16 \pm 0.07(\text{stat}) \pm 0.03(\text{syst})$$



# Conclusions

- Measurements of the CKM angle  $\beta$  have reached the O(%) precision:
  - CP violation well established in  $B^0$ -meson system
  - Main input in unitarity triangle fits
- **New results from BaBar:**
  - $\sin 2\beta$  update on  $B^0 \rightarrow (cc\bar{c})K^{(*)0}$  with 383 million B pairs
  - $\beta$  ambiguity broken by  $\cos 2\beta$  measurements
  - New results on  $B \rightarrow D^{(*)}D^{(*)}$  and  $B \rightarrow D^{(*)}0h^0$ 
    - Evidence for CPV in  $B^0 \rightarrow D^{*+}D^-$
    - $3\sigma$  puzzle in  $B^0 \rightarrow D^+D^-$  (BaBar-Belle)
  - Hints of difference between  $\sin 2\beta$  in trees and penguins persist ( $\Delta S = \sin 2\beta_{eff} - \sin 2\beta < 0$ ) but handle averages with care ...

$\beta = (21.3 \pm 1.0)^\circ$   
(World Average)



$\sin(2\beta^{eff})$



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# Backup slides



## Penguin averaging ...

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- Averaging over all s-penguin modes assumes that contributions with non-zero weak phases to the decay amplitudes can be neglected. This assumption may be significantly violated due to doubly CKM-suppressed  $V_{ub}$  penguin amplitudes, and, in some cases, doubly CKM-suppressed and color-suppressed  $V_{ub}$  tree amplitudes that contribute to the decay amplitude.
- Recent theoretical analyses indicate that it is reasonable to expect that, while the modes  $\phi K^0$ ,  $\eta' K^0$  and  $K_S K_S K_S$  have theoretical uncertainties of the order of 0.05 or smaller, these can be significantly larger for the other modes (in particular for non-ss-resonance modes:  $\pi^0 K_S$ ,  $\rho^0 K_S$ ,  $\omega K_S$  and  $K^+ K^- K^0$ ).

[Heavy Flavor Averaging Group webpage]