Flavor Physics and Dark Matter in SUSY GUT Models

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Based on works with Bhaskar Dutta & Yukihiro Mimura PRD80:095005,2009

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Supersymmetry

Why SUSY?

- It provides solution to hierarchy problem,
- improves gauge coupling unification,
- provides dark matter particle.

Unsolved problem:

How do we understand flavor structure within SUSY? (How SUSY is broken?)

Flavor & SUSY

- Flavor puzzle of SUSY: (without restriction by hand) soft breaking terms allow large flavor changing processes.
- FCNC can be suppressed by flavor universal SUSY breaking:
 - Universal squarks and sleptons masses $m_{\tilde{U}}, m_{\tilde{D}}, m_{\tilde{Q}}, m_{\tilde{L}}, m_{\tilde{E}} = Im_0.$
 - Universal trilinear coupling coefficients $A = YA_0$ (Y = Yukawa).
- Nevertheless, nonuniversality still arises through RGE, \Rightarrow FCNC through radiative correction.
- Within SUSY GUT How the quark sector is related to the lepton sector?

$B_s - \bar{B}_s$ mixing

- Large phase is measured: CDF: $\phi_s \in [0.28, 1.29]$ (PRL100 (2008) 161802) D0: $\phi_s = 0.57^{+0.30}_{-0.24}(\text{stat})^{+0.02}_{-0.07}(\text{syst})$ (PRL101 (2008) 241801)
- Standard Model:

$$\phi_s = 2\beta_s \equiv 2\arg\left(-V_{ts}V_{tb}^*/V_{cs}V_{cb}^*\right) \simeq 0.04$$



$B_s - \bar{B}_s$ mixing - SUSY

- Chargino box diagrams.
- Double penguin diagrams through heavy Higgs. This is $\propto \tan^4 \beta$ and $\propto 1/m_A^4$ (Recall also that BR $(B_s \to \mu\mu) \propto \tan^6 \beta$)

Define

$$C_{B_s} e^{2i\phi_{B_s}} = \frac{M_{12}^{\rm SM} + M_{12}^{\rm NP}}{M_{12}^{\rm SM}}$$

then

$$\phi_s = 2(\beta_s - \phi_{B_s})$$

Neutrino in the GUT-shell

Observation: θ₁₂ (solar) - large, θ₂₃ (atmospheric) - large, θ₁₃ (reactor) - small, and small neutrino masses.

Light neutrinos through seesaw:

$$\mathcal{M}_{\nu}^{\text{light}} = f \langle \Delta_L \rangle - Y_{\nu} M_R^{-1} Y_{\nu}^{\text{T}} \langle H_u^0 \rangle^2$$

Seesaw type II I

 Δ_L is an SU(2)_L triplet, and f is a Majorana coupling $\frac{1}{2}LL\Delta_L$.

 Large mixing through Majorana coupling (type II) or Dirac coupling (type I).

GUT boundary condition

Squark and slepton mass matrices:

$$M_{\tilde{F}}^2 = m_0^2 [\mathbf{1} - \kappa_F U_F \operatorname{diag}(k_1, k_2, 1) U_F^{\dagger}]$$

Minimal type SU(5) :

$$\kappa_L = \kappa_{D^c}, \quad U_L = U_{D^c}, \quad \kappa_Q = \kappa_{U^c} = \kappa_{E^c} = 0$$

Minimal type SO(10) :

$$\kappa_Q = \kappa_{U^c} = \kappa_{D^c}, \quad U_Q = U_{U^c} = U_{D^c}, \quad \kappa_L = \kappa_{E^c}$$

(To obey proton decay constraint. Dutta, Mimura and Mohapatra, PRL94 (2005) 091804, PRD72 (2005) 075009)

Neutralino Dark Matter

Direct detection cross section

$$\sigma_{\tilde{\chi}_{1}^{0}-p} \simeq \frac{4}{\pi} m_{p}^{4} |(A^{u} f_{u}/m_{u} + A^{c} f_{c}/m_{c} + A^{t} f_{t}/m_{t}) + (A^{d} f_{d}/m_{d} + A^{s} f_{s}/m_{s} + A^{b} f_{b}/m_{b})|^{2}$$

where, $f_q \equiv \langle p | m_q \bar{q}q | p \rangle / m_p$, and $f_u \simeq 0.027$; $f_d \simeq 0.039$; $f_s \simeq 0.36$; $f_c = f_b = f_t \simeq 0.043$

$$A^{d,s,b} = \frac{g_2^2 m_{d,s,b}}{4M_W} \left(-\frac{\sin\alpha}{\cos\beta} \frac{F_h}{m_h^2} + \frac{\cos\alpha}{\cos\beta} \frac{F_H}{m_H^2} \right)$$
$$A^{u,c,t} = \frac{g_2^2 m_{u,c,t}}{4M_W} \left(\frac{\cos\alpha}{\sin\beta} \frac{F_h}{m_h^2} + \frac{\sin\alpha}{\sin\beta} \frac{F_H}{m_H^2} \right)$$

SU(5) $m_A - \mu$ plane



 $|2\phi_{B_s}| = 0.5$ rad.

SO(10) $m_A - \mu$ plane



 $|2\phi_{B_s}| = 0.5$ rad.



 $\tan \beta = 40$, $A_0 = 0$, $m_0 = 500 \text{ GeV}$, $m_{1/2} = 500 \text{ GeV}$



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Conclusion

- Solution We have looked at models of SUSY GUT in which $B_s \overline{B}_s$ mixing phase can be large and with large neutrino mixing.
- Combined with other flavor changing constraints and dark matter constraints we found that the funnel region is still allowed by both SU(5) and SO(10), and favored by SU(5).
- Stronger constraints from upcoming experimental results can provide further hints on the SUSY GUT model.