Progress on PDF analysis by CTEQ-TEA group and its implications for the LHC

Hung-Liang Lai

Taipei Municipal University of Education
& Michigan State University

in collaboration with
J. Huston, M. Guzzi, Z. Li, P. Nadolsky, J. Pumplin,
D. Stump, and C.-P. Yuan
May 10, 2010

CTEQ-Tung Et Al.: recent activities

- Uncertainty induced by α_s in the CTEQ-TEA PDF analysis *(arXiv:1004.4624)*
- NLO general-purpose PDF fits
  - CTEQ6.6 set (published in 2008) $\longrightarrow$ CT09 $\longrightarrow$ CT10 (to be released)
  - new experimental data, statistical methods, and parametrization forms
- Constraints on new physics *(next talk by Marco Guzzi)*
- PDFs for Event Generators *(arXiv:0910.4183)*
- Exploration of statistical aspects (data set diagonalization) and PDF parametrization dependence *(Pumplin, arXiv:0909.0268 and 0909.5176)*

Uncertainty induced by α_s in the PDF analyses

- *Questions addressed:*
  - Two leading theoretical uncertainties in LHC processes are due to α_s and the PDFs; how can one quantify their correlation?
  - Which central $\alpha_s(M_Z)$ and which error on $\alpha_s(M_Z)$ are to be used with the existing PDFs?
  - What are the consequences for key LHC processes ($gg \to H^0$, etc.)?
- recent activities on this issue:
  - **MSTW** *(arXiv:0905.3531)*
  - **NNPDF** *(in 2009 Les Houches Proceedings, arXiv:1004.0962)*
  - **H1+ZEUS** *(arXiv:0911.0884)*

Our findings (arXiv:1004.4624)

Theorem

In the quadratic approximation, the total α_s+PDF uncertainty ΔX, with all correlation, reduces to

$$\Delta X = \sqrt{\Delta X_{PDF}^2 + \Delta X_{\alpha_s}^2},$$

where

- ΔX_{PDF} *is the PDF uncertainty with fixed* α_s*, e.g. uncertainty from 44 CTEQ6.6 PDFs with the same* $\alpha_s(M_Z) = 0.118$
- $\Delta X_{\alpha_s} = (X_{high} - X_{low})/2$ *is the* α_s *uncertainty computed with upper/lower* α_s *PDFs, e.g. CTEQ6.6AS PDFs for* $\alpha_s(M_Z) = 0.120$ *and* 0.116

Back-up slides: The main idea illustrated; key cross sections tabulated
The full proof is given in the paper

CT10 analysis (in progress)

Experimental data

- Combined HERA-1 neutral-current and charged-current DIS data with 114 correlated systematic effects *(see Guzzi's talk)*
  - replaces 11 separate HERA-1 sets used in the CTEQ6.6 fit
- CDF Run-2 and D0 Run-2 inclusive jet production
- Tevatron Run-2 Z rapidity distributions from both CDF and D0
- W electron asymmetry from CDF II and D0 II; W muon asymmetry from D0 II (CT10W set)
- Other data sets inherited from CTEQ6.6

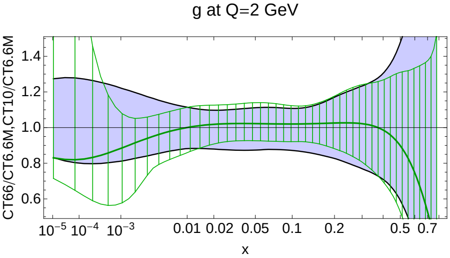
CT10 analysis (in progress)

Developments in techniques

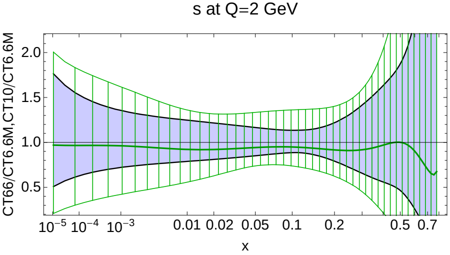
- Experimental normalizations N_i are treated on the same footing as other correlated systematic errors
- Set all data weights of 1, unless otherwise specified
- Require 90% CL for each experiment dynamically
- More flexible (i.e. less biased) parametrizations for $g(x, Q_0)$, $d(x, Q_0)$, and $s(x, Q_0)$
- Apply soft constraint on $R_s = \lim_{x \to 0} (s(x) + \bar{s}(x)) / (\bar{u}(x) + \bar{d}(x))$ which has little information from current data

More flexible parametrizations

CT10(green) vs. CTEQ6.6(blue) ; PRELIMINARY



$g(x, Q)$: large uncertainty at $x < 10^{-3}$, despite tighter constraints by the combined HERA data



$s(x, Q)$: wider uncertainty, covers both CTEQ6.6 and MSTW'08

Agreement between data sets

- Good overall agreement: $\chi^2/d.o.f. = 1.1$ (out of ~2800 data points)

- Noticable observations on the quality of the fit:

  - **Tevatron single-inclusive jet production:** Run-1 and Run-2 sets are moderately compatible *(arXiv:0904.2424)*

  - **Tevatron Run-2 Z rapidity:** D0 well described; CDF acceptable (higher stat.)

  - **Tevatron Run-2 W lepton asymmetry**
    - is precise; constrains $d(x)/u(x)$ at $x \to 1$
    - apparently disagrees with existing constraints on d/u, mainly provided by the NMC F_2^d/F_2^p and Run-1 W lepton asymmetry data; minor tension against BCDMS F_2^d data

Agreement between data sets

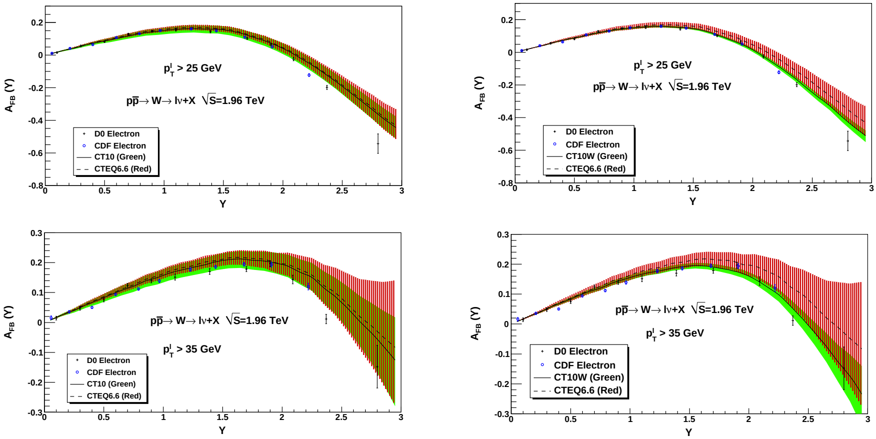
- Reaonable fits to electron (e) asymmetry data are possible without NMC and BCDMS; and vice versa
- No acceptable fit to D0 II e asymmetry and NMC/BCDMS data can be achieved, if they are included on the same footing
- Tension between Run-2 e asymmetry and μ asymmetry
- Good agreement between Run-2 e W asymmetry data and Z y data
- With special emphasis on D0 II e asymmetry data (weight>1), it is possible to obtain a reasonable agreement for W asymmetry ($\chi^2/d.o.f. = 1 - 2$) , with some remaining tension with NMC & BCDMS data, especially at $x > 0.4$

CT10 family

- Two series of PDFs are produced:
  - **CT10:** no D0 Run-2 W asymmetry data are included
  - **CT10W:** include D0 Run-2 W asymmetry, with an extra weight

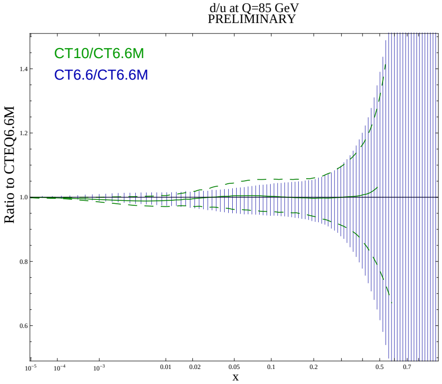
CT10 and CT10W fits with Tevatron Run-2 data

PRELIMINARY



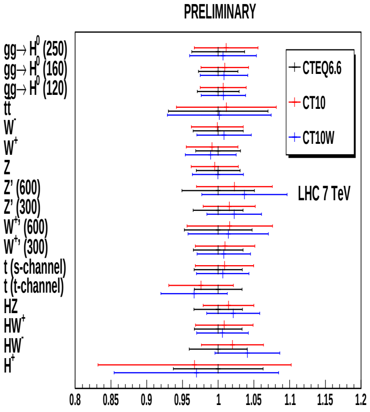
CT10W agrees better with W asy data; has smaller uncertainty than CTEQ6.6 or CT10

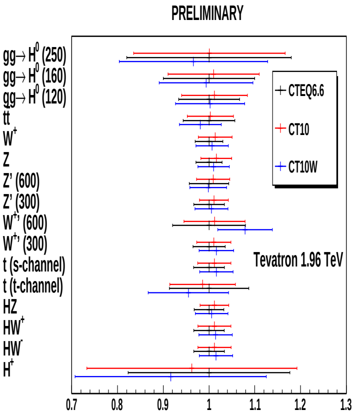
$d(x, Q)/u(x, Q)$ at $Q = 85$ GeV



CT10W prefers larger d/u, has smaller uncertainty than CTEQ6.6 or CT10

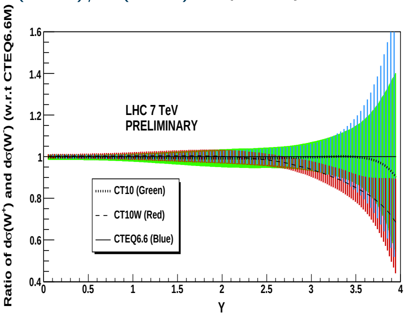
CT10 & CT10W predictions for the LHC & Tevatron





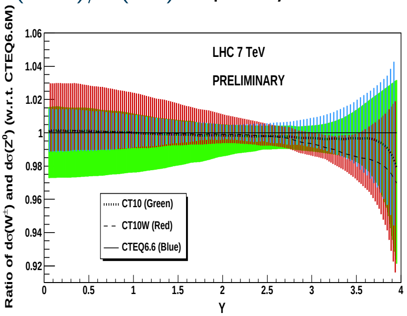
CT10 & CT10W predictions for the LHC

$\sigma(W^+)/\sigma(W^-)$ rapidity dist.



CT10W Uncertainty (red) is clearly smaller than that of CT10 & CTEQ6.6.

$\sigma(W^\pm)/\sigma(Z^0)$ rapidity dist.



CT10 (green) & CT10W (red) uncertainties in central y region are larger than that of CTEQ6.6 (blue), mainly due to larger uncertainty on s distribution.

Summary I

CTEQ6.6AS PDF sets (available in the LHAPDF library):

- from 4 alternative CTEQ6.6 fits for

$$\alpha_s(M_Z) = 0.116, .117, .119, .120$$

- sufficient to compute uncertainty in $\alpha_s(M_Z)$ at ≈68% and 90% C. L., including **the world-average** $\alpha_s(M_Z) = 0.118 \pm 0.002$ as an **input data point**
- **The CTEQ6.6AS** α_s uncertainty should be combined with the CTEQ6.6 PDF uncertainty as

$$\Delta X = \sqrt{\Delta X^2_{CTEQ6.6} + \Delta X^2_{CTEQ6.6AS}}$$

- The total uncertainty ΔX reproduces the full correlation between $\alpha_s(M_Z)$ and PDFs, also applicable to CT10 family and future PDFs.

Summary II

Tevatron Run-2 W asymmetry data...

...become increasingly complete and precise (measurements by both CDF and D0; electron and muon channels)

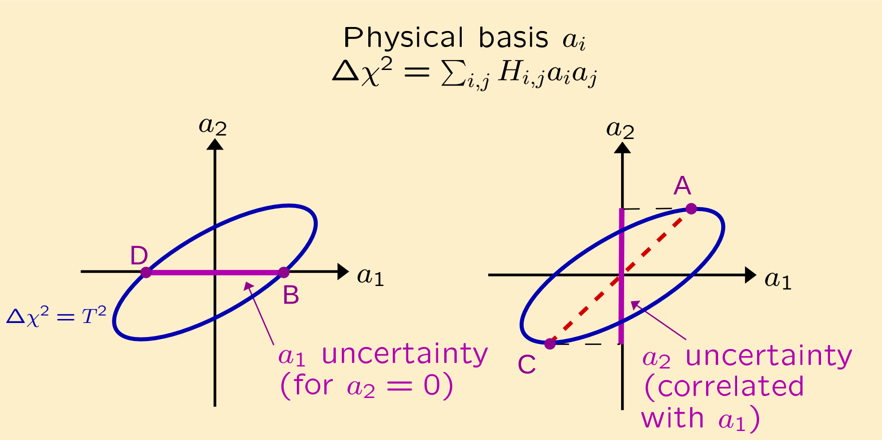
...cannot be explained based on the d/u ratio provided by the previously existing data

- Several cross checks of the theoretical calculation for W asymmetry; no problems were found
- Higher-twist and nuclear corrections in the large-x BCDMS/NMC deuterium data are the usual suspects

  (Virchaux and Milsztajn; Alekhin; Accardi et al.)
- CT10 and CT10W sets of PDFs for practical applications, without and with constraints from the D0 Run-2 W asymmetry

Backup slides

Illustration of the theorem for 2 parameters

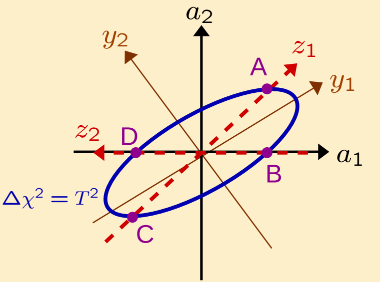


$\Delta X_1^2 = \frac{1}{4}\left(X(B) - X(D)\right)^2$ $\Delta X_2^2 = \frac{1}{4}\left(X(A) - X(C)\right)^2$

Illustration of the theorem for 2 parameters, cont.

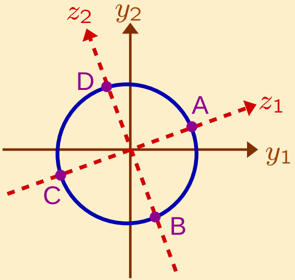
Physical basis a_i

$$\Delta\chi^2 = \sum_{i,j} H_{i,j} a_i a_j$$



Eigenvector bases y_i, z_i

$$\Delta\chi^2 = \sum_i y_i^2 = \sum_i z_i^2$$



$$\Delta X^2 = \frac{1}{4}\left[(X(A) - X(C))^2 + (X(B) - X(D))^2\right]$$
$$= \Delta X_1^2 + \Delta X_2^2$$

Full and reduced fits with variable α_s: cross sections

Process	CTEQ6.6+CTEQ6.6AS				CTEQ6.6FAS
$t\bar{t}$ (171 GeV)	σ_0	$\Delta\sigma_{PDF}$	$\Delta\sigma_{\alpha_s}$	$\Delta\sigma$	$\sigma_0 \pm \Delta\sigma$
LHC 7 TeV	157.41	10.97	7.54	13.31	160.10 ± 13.93
LHC 10 TeV	396.50	18.75	16.10	24.71	400.48 ± 25.74
LHC 14 TeV	877.19	28.79	30.78	42.15	881.62 ± 44.27
$gg \to H$ (120 GeV)	σ_0	$\Delta\sigma_{PDF}$	$\Delta\sigma_{\alpha_s}$	$\Delta\sigma$	$\sigma_0 \pm \Delta\sigma$
Tevatron 1.96 TeV	0.63	0.042	0.032	0.053	0.64 ± 0.055
LHC 7 TeV	10.70	0.31	0.32	0.45	10.70 ± 0.48
LHC 10 TeV	20.33	0.66	0.56	0.87	20.28 ± 0.93
LHC 14 TeV	35.75	1.31	0.94	1.61	35.63 ± 1.70
$gg \to H$ (160 GeV)	σ_0	$\Delta\sigma_{PDF}$	$\Delta\sigma_{\alpha_s}$	$\Delta\sigma$	$\sigma_0 \pm \Delta\sigma$
Tevatron 1.96 TeV	0.26	0.026	0.015	0.030	0.26 ± 0.031
LHC 7 TeV	5.86	0.16	0.18	0.24	5.88 ± 0.26
LHC 10 TeV	11.73	0.33	0.33	0.47	11.72 ± 0.50
LHC 14 TeV	21.48	0.68	0.56	0.88	21.43 ± 0.94
$gg \to H$ (250 GeV)	σ_0	$\Delta\sigma_{PDF}$	$\Delta\sigma_{\alpha_s}$	$\Delta\sigma$	$\sigma_0 \pm \Delta\sigma$
Tevatron 1.96 TeV	0.055	0.0099	0.0044	0.011	0.058 ± 0.012
LHC 7 TeV	2.30	0.085	0.081	0.12	2.32 ± 0.12
LHC 10 TeV	5.08	0.14	0.15	0.21	5.10 ± 0.22
LHC 14 TeV	10.03	0.26	0.27	0.37	10.04 ± 0.41

The full (CTEQ6.6FAS) and reduced (CTEQ6.6+CTEQ6.6AS) methods perfectly agree