

In Search of Extra Dimensions

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Extra dimensions: 96-year old idea!

- G. Nordström, 1914:

Unify pre-GR gravity and EM in 5D.



- Th. Kaluza, 1921:

Unify GR and EM in 5D.



- O. Klein, 1926:

Unify GR and EM with one *compact* extra dimension.



Extra dimensions in Recent Times

- String theory, since the 1980's.
 - Quantum gravity.
 - Consistency requires 10 or 11 dimension.
 - Extra dimensions compactified near fundamental scale M_F ($M_P \sim 10^{19}$ GeV).
- Particle Physics, since the 1990's.
 - Motivation: the hierarchy, $m_W/M_P \sim 10^{-17}$.
 - Antoniadis, 1990: TeV^{-1} extra dimensions and SUSY breaking.
 - Weak scale superstrings, Lykken, 1996.
 - Large Extra Dimensions; Arkani-Hamed, Dimopoulos, Dvali, 1998: $m_W \lesssim M_F$.
 - A Warped Extra Dimension; Randall, Sundrum, 1999: $m_W \sim e^{-k\pi r_c} M_P$; $k\pi r_c \sim 35$.
 - TeV^{-1} Universal Extra Dimensions; Appelquist, Cheng, Dobrescu, 2000.
 - ...

Large Extra Dimensions (LED)

Arkani-Hamed, Dimopoulos, Dvali, 1998

- n compact extra dimensions, $M_F \sim \text{TeV}$: $M_P^2 \sim R^n M_F^{n+2}$

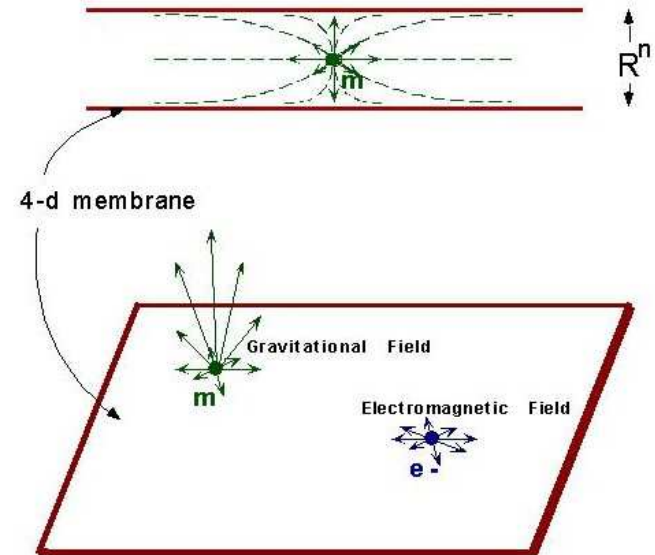
- $R \lesssim \text{mm}$ (gravity tests) $\Rightarrow n \geq 2$.

- SM localized on a 3-brane (4D).
 - Gravity propagates in all dimensions.
- Gravity “diluted” in extra dimensions.
- Graviton Kaluza-Klein (KK) modes.

- Quantized momenta in extra dimensions:

$$m_{KK} = j/R; \quad j = 0, 1, 2, \dots$$

$$\mathcal{L} = \frac{-1}{M_P} T^{\mu\nu} \sum_{\{\vec{j}\}} h_{\mu\nu}^{(\vec{j})}; \quad \text{fm} \lesssim R \lesssim \text{mm}; \quad 2 \leq n \leq 6.$$



Key Signals for LED

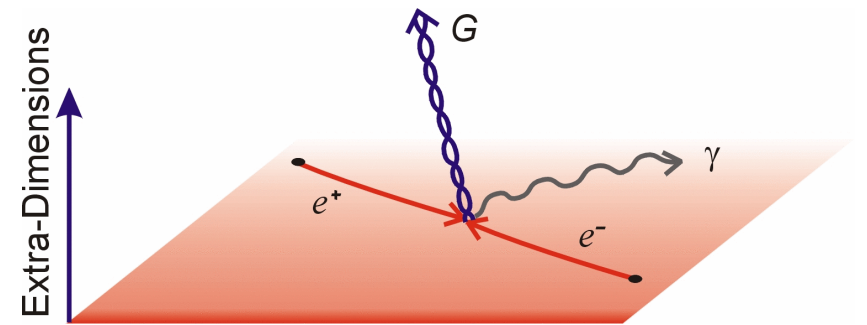
- Missing energy: KK gravitons escape into the “bulk.”

$$q\bar{q} \rightarrow j G_{KK} (\cancel{E}) \quad ; \quad e^+e^- \rightarrow \gamma G_{KK} \dots$$

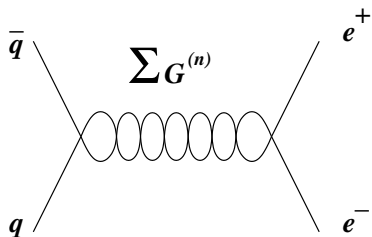
Missing E signature.

Giudice, Rattazzi, Wells 1998

Mirabelli, Perelstein, Peskin, 1998



- Virtual exchange of spin-2 tower.



Spin-2 mediated angular distributions.

Han, Lykken, Zhang, 1998

Hewett, 1998

- Black hole production for $\sqrt{s} \gg M_F$.

Giddings, Thomas, 2001

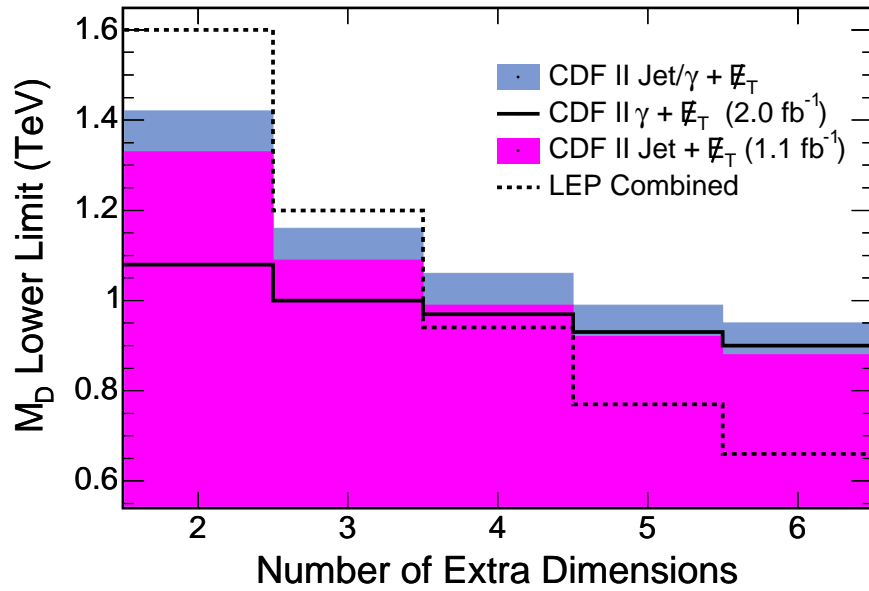
Dimopoulos, Landsberg, 2001

- Potentially spectacular signals: energetic multi-jets, leptons,
- Under debate.

e.g. Meade, Randall, 2007: $2 \rightarrow 2$ quantum gravity effects more likely at the LHC.

LED: Current Bounds and Future Prospects

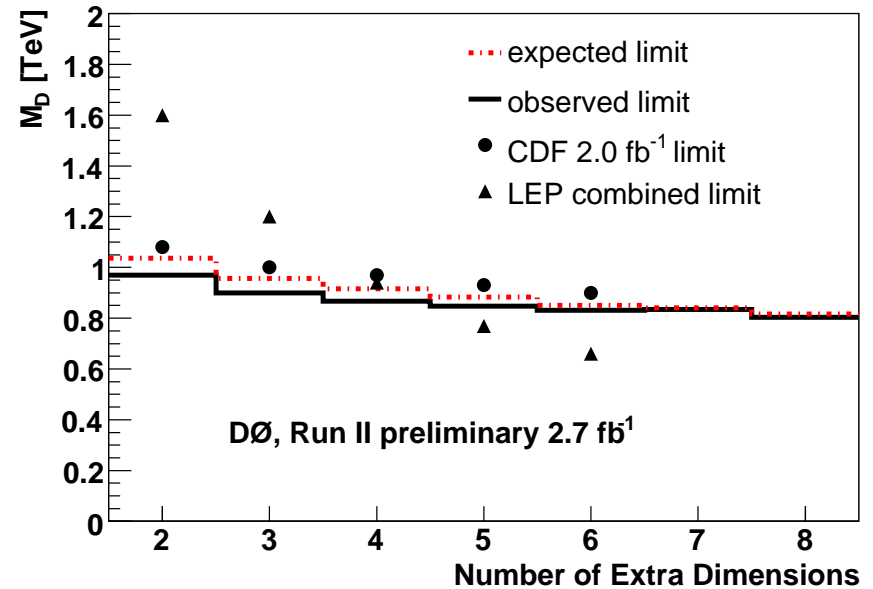
- Collider limits:



Jets/ γ + \cancel{E}_T
 CDF Collaboration (T. Aaltonen et al.),
 Phys.Rev.Lett.101:181602,2008

DØ Collaboration; γ + \cancel{E}_T

DØ Note 5729-CONF, 2008



● Cosmology and Astrophysics: [Arkani-Hamed, Dimopoulos, Dvali, 1998](#)

- Cosmology: Typically $T_{reheat} \lesssim 1$ GeV for $M_F \sim 1$ TeV.

- SN 1987A, energy loss: $M_F \gtrsim 50$ TeV for $n = 2$.

[Cullen, Perelstein, 1998](#)

- Neutron star, excess heat from KK-could: $M_F \gtrsim 700(30)$ TeV, $n = 2(3)$.

[Hannestad, Raffelt, 2001 & 2003](#)

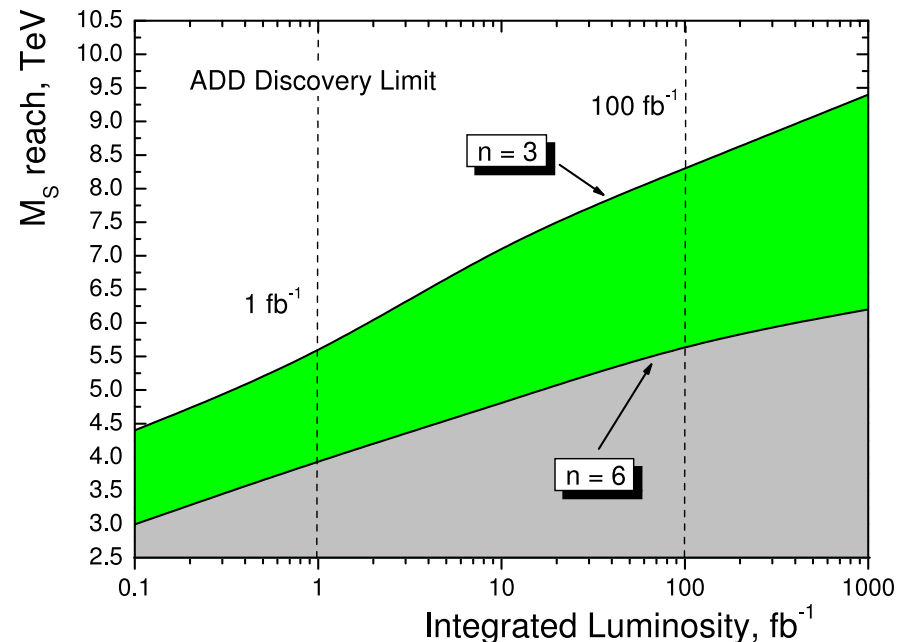
● 5σ LHC reach:

[Kabachenko, Miagkov, Zenin, ATL-PHYS-2001-012](#)

channel	n		2	3	4	5
$\gamma\gamma$	luminosiy	M_S^{max} (TeV)	6.3	5.6	5.1	4.9
	10 fb ⁻¹	S/B	36/18	36/18	39/25	34/13
	100 fb ⁻¹	M_S^{max} (TeV)	7.9	7.3	6.7	6.3
		S/B	50/53	62/96	55/72	51/53
l^+l^-	10 fb ⁻¹	M_S^{max} (TeV)	6.6	5.9	5.4	5.1
		S/B	33/11	31/8	30/6	30/6
	100 fb ⁻¹	M_S^{max} (TeV)	7.9	7.5	7.0	6.6
		S/B	49/48	38/21	36/16	29/6
$\gamma\gamma + l^+l^-$	10 fb ⁻¹	M_S^{max} (TeV)	7.0	6.3	5.7	5.4
	100 fb ⁻¹	M_S^{max} (TeV)	8.1	7.9	7.4	7.0

Dimuon channel

[I. Belotelov et al., CMS Note 2006/076](#)



Universal Extra Dimensions (UED)

Appelquist, Cheng, Dobrescu, 2000

- All SM in TeV^{-1} extra dimensions.
- Bulk momentum conservation: 4D KK number preserved.
 - KK particles not singly produced.
 - Only loop contributions to EW precision data.
 - Less stringent bounds on $1/R$.
- Chiral fermions via \mathbb{Z}_2 orbifolds: KK number \rightarrow KK-parity.
- Compactification: Lorentz violation along extra dimensions.
 - Loops around compact directions: δm_{KK} .

Cheng, Matchev, Schmaltz, 2002
 - Lightest KK particle (LKP) stable, dark matter candidate.
 - Can mimic supersymmetry at the LHC!

Cheng, Matchev, Schmaltz, 2002

UED: Current Status and LHC Prospects

- EW precision:

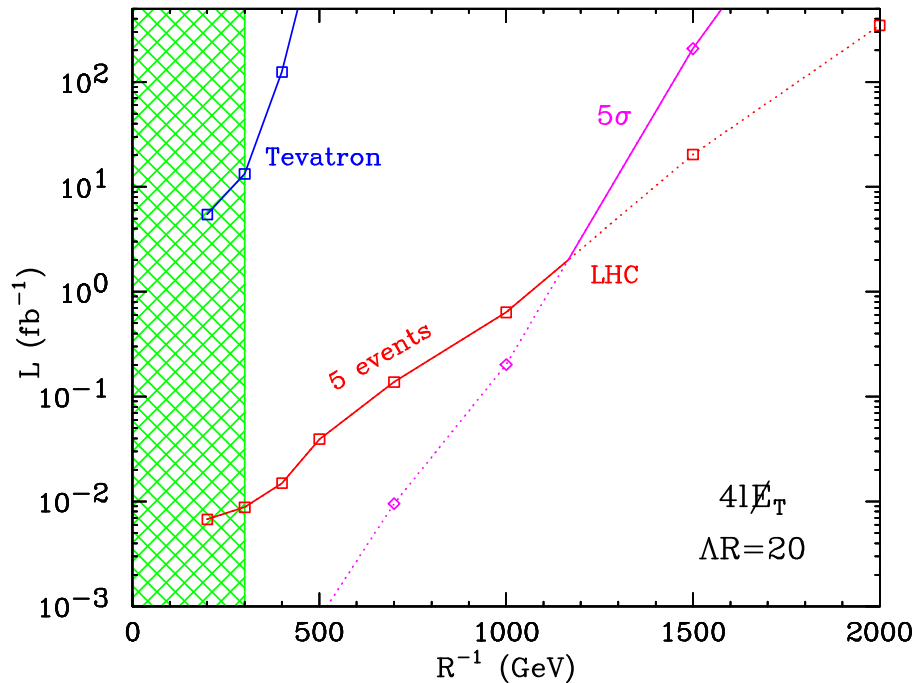
Hooper and Profumo, Phys.Rept.453:29-115,2007

- Tevatron: CDF, Run IB

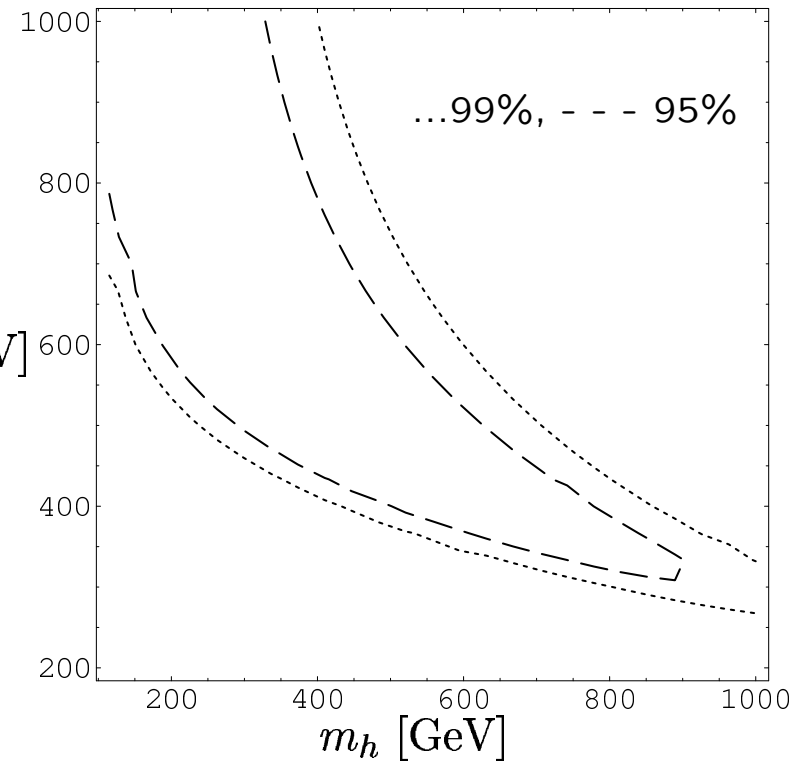
$$m_{KK} \gtrsim 280 \text{ GeV}$$

Lin, 2005

- LHC Prospects:



Flacke, Hooper, March-Russell, 2006



Cheng, Matchev, Schmaltz,
Phys.Rev.D66:056006,2002

Warped Models

- The Randall-Sundrum (RS) Model

Randall, Sundrum, 1999

- 5D warped model of hierarchy, $M_5 \sim M_P$.

- A slice of AdS_5 spacetime.

- Negative constant curvature.

- Flat boundaries: Planck (UV) and TeV (IR) branes.

- Gravity UV-localized, SM on TeV-brane.

- AdS/CFT: Dual geometric picture of strong dynamics.

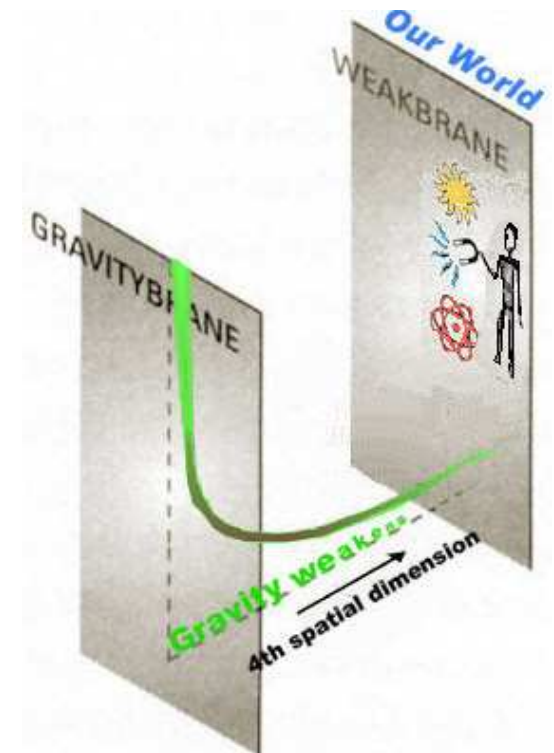
Maldacena, 1997

- Metric: $ds^2 = \underbrace{e^{-2ky}}_{\text{warp factor}} \eta_{\mu\nu} dx^\mu dx^\nu - dy^2$.

- $k \lesssim M_5$ and $y \in [0, \pi r_c]$.

- Redshift: $e^{-kr_c\pi} \langle H_5 \rangle \sim m_W$; IR-localized Higgs, $\langle H_5 \rangle \sim k$.

- $k\pi r_c \approx 35$; hierarchy via exponentiation.



RS Signatures with SM on the Wall

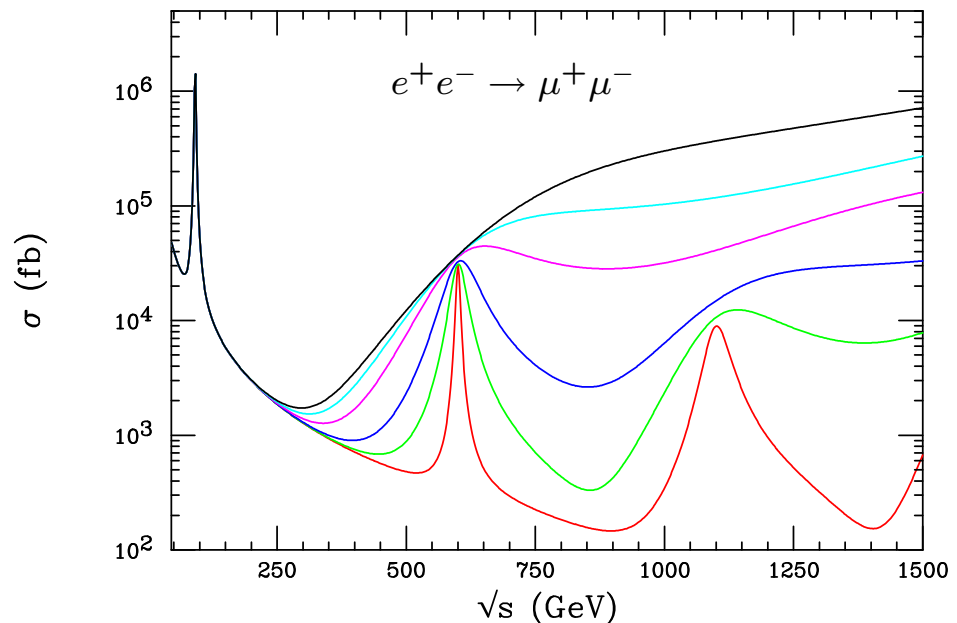
- TeV-scale tower of KK gravitons.

- KK masses $m_n = x_n k e^{-k\pi r_c}$

H.D., Hewett, Rizzo, 1999

$x_n = 3.83, 7.02, \dots$

- Coupling to SM-brane: $\sim \text{TeV}^{-1}$.
- KK graviton spin-2 resonances.
- Decay into e^+e^- , $\gamma\gamma$, \dots
- Distinct signature.



- Stabilized geometry \rightarrow Radion scalar

Goldberger, Wise, 1999

- Typically lighter than KK modes.
- Couplings similar to Higgs.
- Can mix with Higgs through curvature-scalar coupling.

Csáki, Graesser, Kribs, 1999

Tevatron Bounds and LHC Prospects

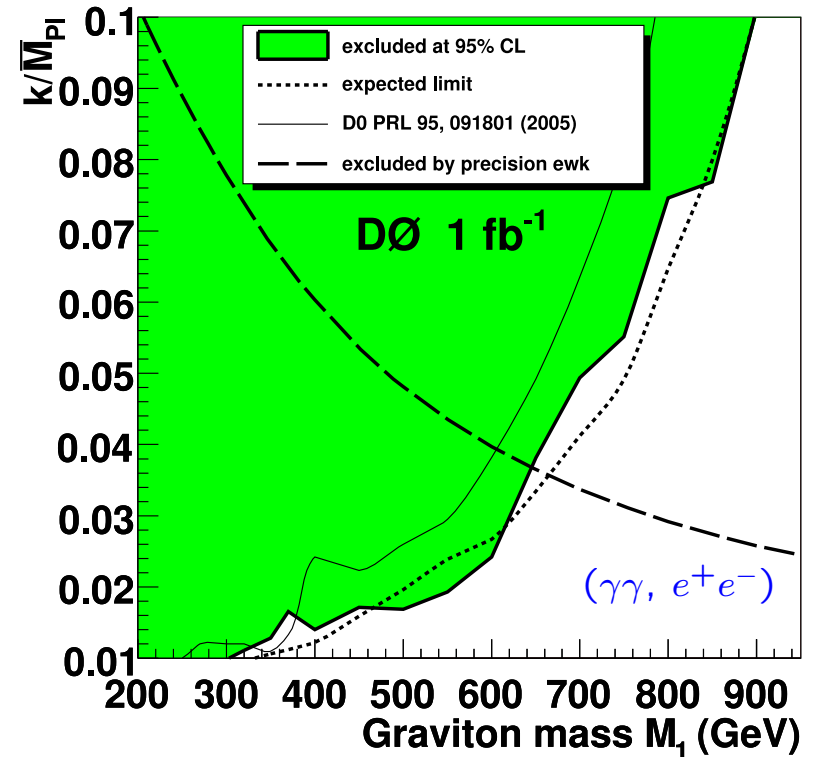
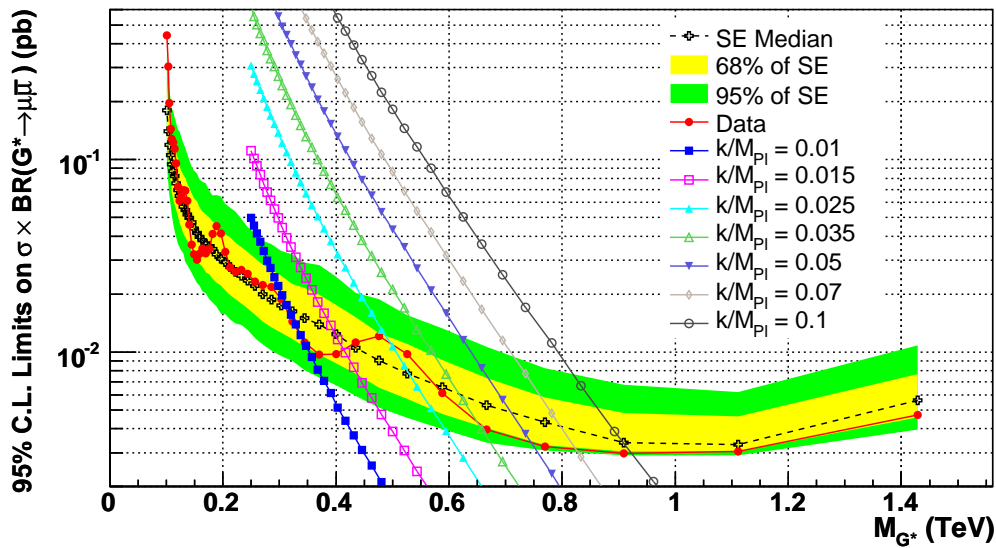
CDF Collaboration (Aaltonen *et al.*); di-muon channel

Phys.Rev.Lett.102:091805,2009

$m_G > 921$ GeV for $k/M_{Pl} = 0.1$; 2.3 fb^{-1}

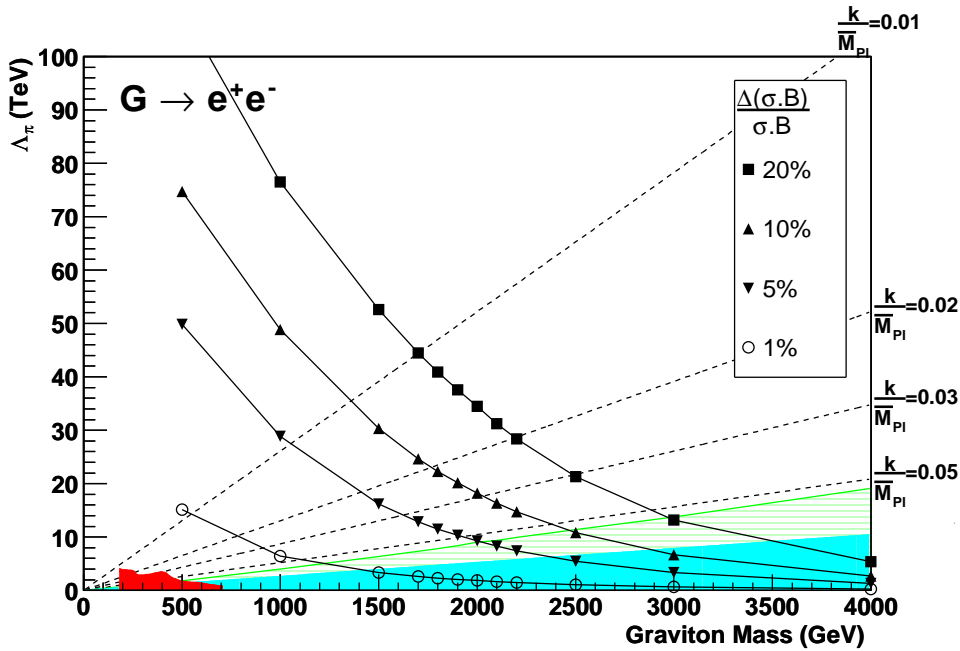
D0 Collaboration (Abazov *et al.*)

Phys.Rev.Lett.100:091802,2008



- ATLAS: 100 fb^{-1} , 3.5 TeV for $k/M_P \simeq 0.1$.

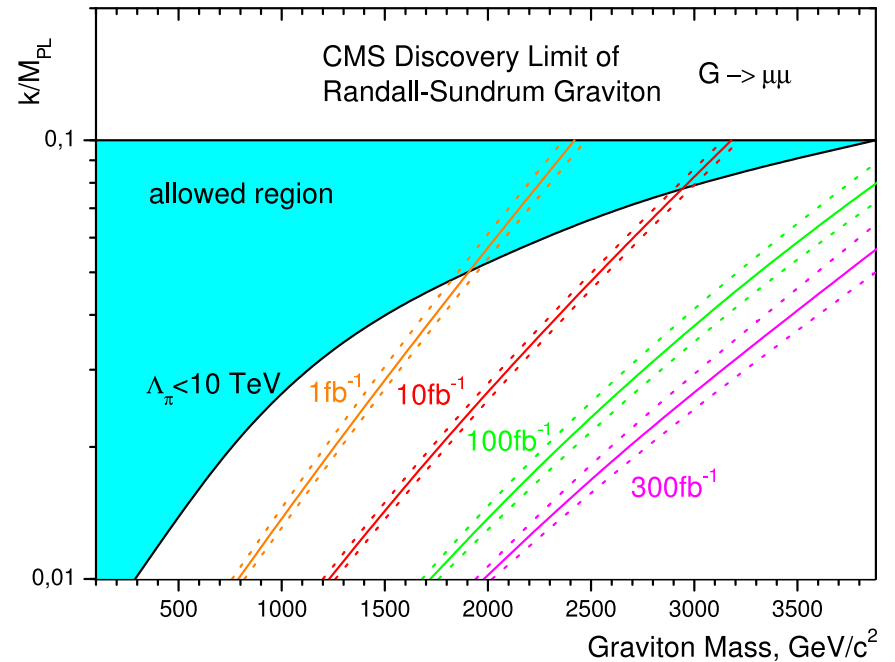
Allanach *et al.*, JHEP 0212:039,2002



- CMS:

100 fb^{-1} , 4 TeV for $k/M_P \simeq 0.1$.

Belotelov *et al.*, CMS Note 2006/104



The RS Model with 4D SM (1999)

Pros:

- Natural Planck-weak hierarchy.
- Striking signals.

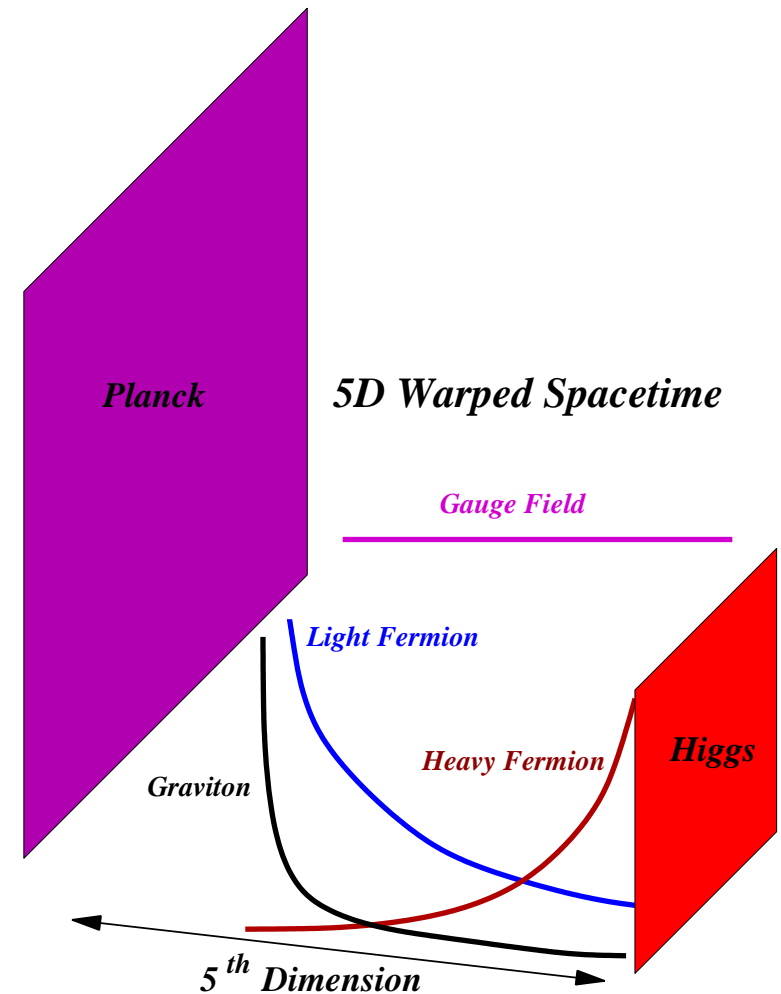
Cons:

- Dangerous operators: Large IR cutoff-scales \rightarrow little hierarchy.
- Flavor still a mystery.

SM Flavor from a Warped Bulk

- 5D fermion masses, $m/k \sim 1 \rightarrow$ localization. Grossman, Neubert, 1999
 - UV(IR)-localization (overlap with Higgs) \rightarrow Light (heavy) fermion.
 - UV-localization: Large effective cutoff scales. Gherghetta, Pomarol, 2000
- \therefore Unwanted light flavor operators suppressed.

- Modified KK couplings.
 - Gauge KK couplings: $(k\pi r_c \approx 35)$
 - UV-brane (e.g. e, u): $\sim g/\sqrt{k\pi r_c}$
 - IR-brane (e.g. H, t_R): $\sim g\sqrt{k\pi r_c}$
 - Graviton KK couplings in $\sim \text{TeV}^{-1}$:
 - Light fermions: \sim Yukawa.
 - IR-brane (e.g. H, t_R): ~ 1 .
 - Gauge fields (g, γ): $\sim 1/(k\pi r_c)$.



- Collider Signals: more challenging.
 - Important production and decay channels suppressed.

Constraints on Warped Hierarchy/Flavor Models

- Control δT : 5D custodial $G_c = SU(2)_L \times SU(2)_R \times U(1)_X$.

Agashe, Delgado, May, Sundrum, 2003

- $Zb\bar{b}$: $G_c \times \mathbb{Z}_2$ Agashe, Contino, Da Rold, Pomarol, 2006

- Gauge KK mass $m_{KK} \gtrsim 2 - 3$ TeV. Carena, Pontón, Santiago, Wagner, 2007

- KK gluon exchange contribution to ϵ_K : Agashe, Perez, Soni, 2004

Csaki, Falkowski, Weiler, 2008

- $m_{KK} \gtrsim 20$ TeV; $\mathcal{O}(30\%)$ uncertainty

Further 5D flavor structure for $m_{KK} \sim$ TeV. *E.g.* Fitzpatrick, Perez, Randall, 2007

Collider Signals and Realistic Bulk Flavor

- The basic RS signals need to be revisited.

- KK gluons:

Agashe, Belyaev, Krupovnickas, Perez, Virzi, 2006

Lillie, Randall, Wang, 2007

- Production from light quark initial states, suppressed.
- Decay mostly to $t\bar{t}$, $\Gamma_{KK} \sim m_{KK}/6$.
- Top-polarization (different t_L and t_R KK gluon couplings) a handle.
- LHC reach 3-4 TeV with 100 fb^{-1} .

- Limits on narrow $t\bar{t}$ resonances:

CDF Collaboration (T. Aaltonen *et al.*)
 Phys.Rev.D77:051102,2008 (995 pb^{-1})

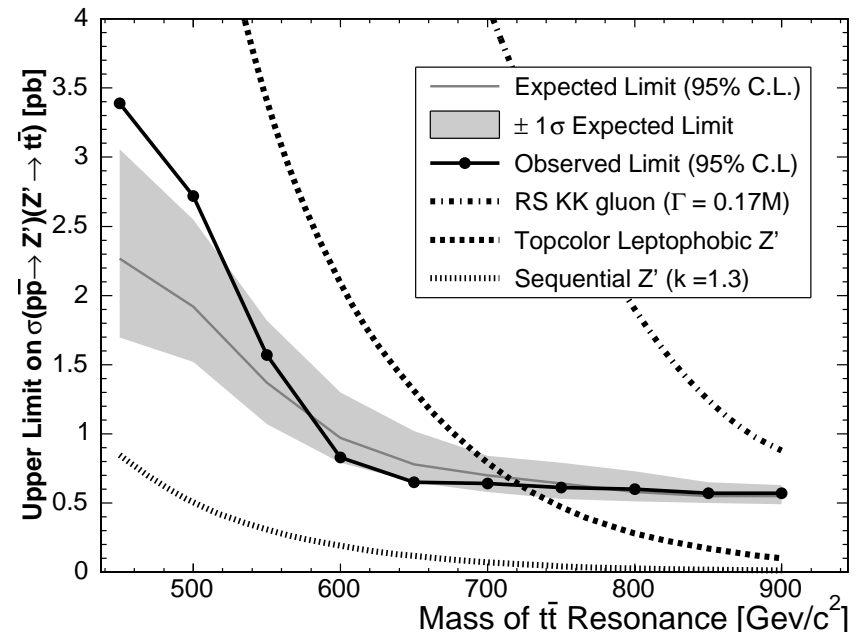
- ★ Light t^1 ($SU(2)_L \times SU(2)_R \times \mathbb{Z}_2$ models):

- Favored by EW data.

Carena, Pontón, Santiago, Wagner, 2006

- Larger Γ_{KK} , reduced $\text{BR}(g^1 \rightarrow t\bar{t})$.

Carena, Medina, Panes, Shah, Wagner, 2008



Fitzpatrick, Kaplan, Randall, Wang, 2007

Agashe, H.D., Perez, Soni, 2007

- KK gravitons:

- Distinct RS signal.
- Production through gg initial state, volume suppressed.
- Golden (dilepton, diphoton) modes negligible.
- Decay through the Higgs (including Z_L/W_L) and top sectors.
- $gg \rightarrow G^1 \rightarrow Z_L Z_L \rightarrow 4\ell \Rightarrow$ LHC reach $\lesssim 2$ TeV with 300 fb^{-1} . ADPS, 2007
- $Z \rightarrow jj$ highly boosted ($E \sim 1$ TeV), dominated by $Z + j$ background.

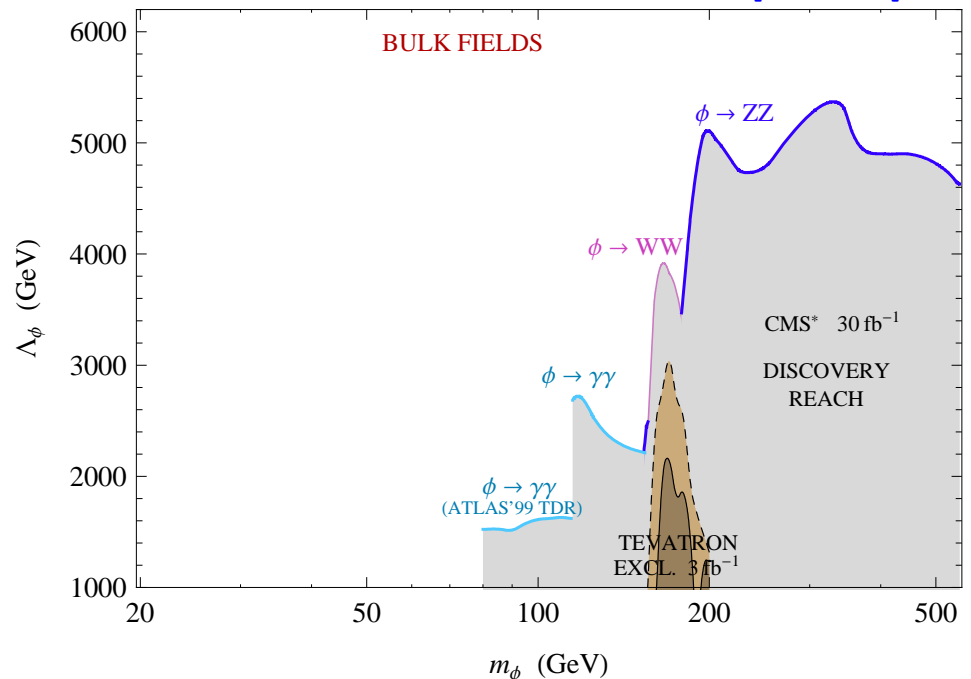
- The Radion:

- Associated with fluctuations of r_c .
- Typically the lightest new 5D state.
- 5D SM: new tree-level couplings.

Csáki, Hubisz, Lee, 2007

LHC reach from Higgs projections \rightarrow

M. Toharia, arXiv:1001.2693 [hep-ph]



- The electroweak sector:

- 5D $SU(2)_L \times SU(2)_R \times U(1)_X$ to accommodate EW precision data.

- Z' : [Agashe, et al., 2007](#)

- At the TeV scale, 3 neutral states, collectively denoted by Z' .

- Production dominated by light quark initial states.

- Main decay channels IR-brane fields: $H, W_L/Z_L, t$.

- $Z' \rightarrow W_L^+ W_L^- \rightarrow \ell^+ \ell^- E_{\cancel{H}}$: LCH reach 2 TeV with 100 fb^{-1} .

- $W \rightarrow jj$ boosted dijet challenge, requires more detailed analysis.

(Use of EM calorimeter to find 2 EM cores a possibility.)

- $t\bar{t}$ dominated by KK gluon “background.”

- W' : [Agashe, Gopalakrishna, Han, Huang, Soni, 2008](#)

- 4 Charged states.

- No KK gluon pollution.

- LHC reach similar to Z' .

- Reach may be improved by better control over reducible backgrounds.

Little Randall-Sundrum (LRS) Models

H.D., Perez, Soni, 2008

- RS as a model of flavor: $M_5 \ll M_P$ viable option.
- $M_5 \gg \text{TeV}$ needed to suppress unwanted (FCNC,...) operators.
- Volume-truncated RS models: $1 \ll kr_c\pi \ll 35$.
- Truncation: some unwanted contributions suppressed.

Example: tree-level oblique parameter $T_{\text{tree}} \propto kr_c\pi$ in RS models.

(5D custodial symmetry to suppress δT from UV-sensitive loops.)

- Explain $\langle H \rangle / M_5 \ll 1$ hierarchy \Rightarrow warped TeV-scale KK modes.
- LRS: significant improvement in *clean* collider signals.

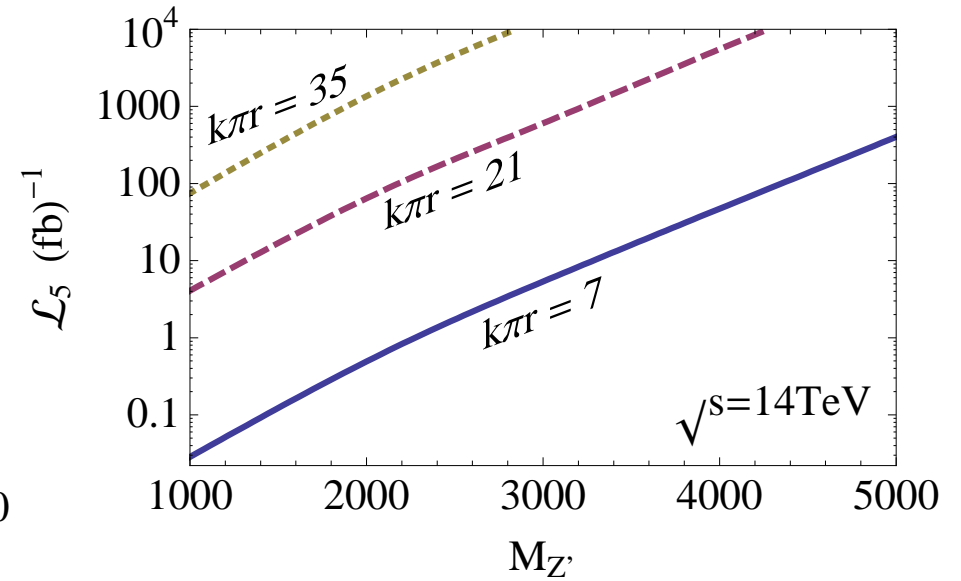
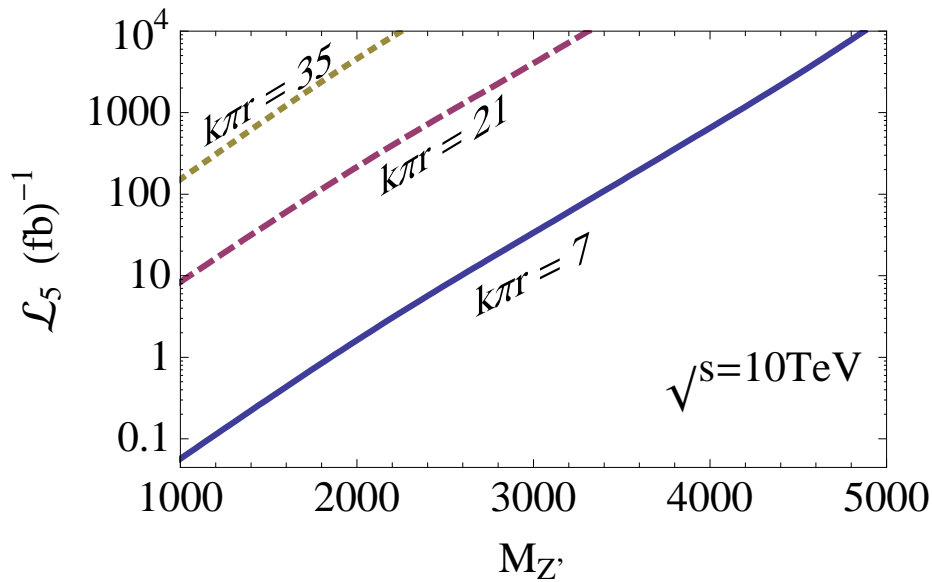
Example: $S \sim \sigma(q\bar{q} \rightarrow Z' \rightarrow l^+l^-) \propto 1/(kr_c\pi)^3$.

- Flavor constraints on LRS from ϵ_K : $k\pi r_c \gtrsim 7$ ($M_5 \gtrsim 10^4 \text{ TeV}$).

Bauer, Casagrande, Grunder, Haisch, Neubert, 2008

Dilepton Channel LHC Reach for the Little Z'

H.D., Gopalakrishna, Soni, Phys.Lett.B686:239-243,2010



- Cuts: $|\eta_\ell| < 3.0$, $p_{T_\ell} > 100$ GeV, $M_{\ell^+\ell^-}$ within $M_{Z'} \pm 100$ GeV.
- Background: irreducible SM only, due to low leptonic jet-fake rate (10^{-3}).
- \mathcal{L}_5 : $\int L dt$ for 5σ signal (≥ 3 events) in $pp \rightarrow \ell^+\ell^-$ ($\ell = e$ or μ).
- For $kr_c\pi \approx 7$: $M_{Z'} \approx 2(3)$ TeV at $\sqrt{s} = 10(14)$ TeV with 1 (4) fb^{-1} .
- Original RS ($kr_c\pi \approx 35$): $M_{Z'} \approx 3$ TeV, $\sqrt{s} = 14$ TeV, 300 fb^{-1} (any channel).
- Sensitivity to $\underline{kr_c\pi}$ can give clues about the UV scale M_5 .

Conclusions

- Extra dimensions: possibilities for hierarchy and more.
- New phenomena at the TeV scale.
- Discovery a fundamental revolution in science.
- Various extra dimensional scenarios can be tested at the LHC.
- Signals could be more subtle or elusive than the first estimates.

Examples:

- LED: Black hole signals could be less obvious/likely.
- Warped models of hierarchy and flavor:
 - * Signals likely more challenging than in original models, mass scales larger.
 - * Larger m_{KK} : boosted dijets from decays ($E \gtrsim 1$ TeV), mono-jet backgrounds.
- Truncated warped bulk (conformal depth) \leftrightarrow Enhanced clean signals.
- Observing TeV-scale KK modes: is Planck-weak hierarchy addressed?
- Little RS models: possible clues may be accessible at the LHC.