

# Exploring Higgs Triplet Models via Vector Boson Scattering at the LHC



[Phys. Rev. D \*\*81\*\*, 075026 \(2010\)](#)

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# Outline



- Introduction
- Higgs Triplet Models
  - The Littlest Higgs Model
  - The Left-Right Symmetric Model
  - The Georgi-Machacek Model
- Vector Boson Scattering
- Results
  - $W^\pm W^\pm$ ,  $W^\pm Z$ ,  $W^+ W^-$ ,  $ZZ$
  - Discovery Potential
- Conclusions

# Introduction

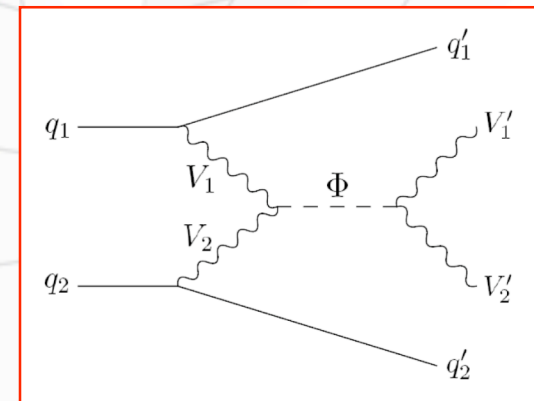


- Need Physics beyond the SM (hierarchy, fine-tuning problems)  
⇒ Extended Higgs sectors

- TeV scale Higgs bosons can be produced at the LHC via vector boson scattering:

$$pp \rightarrow \Phi jj \rightarrow VV jj \quad (V = W^\pm, Z)$$

- $\Phi^{\pm\pm}$  production via  $W^\pm W^\pm$  scattering has been studied in Higgs Triplet Models [G. Azuelos et al., hep-ph/0402037v1 & hep-ph/0503096v1](#)
- Also need to study  $\Phi^\pm$  production ( $W^\pm Z$ ) and  $\Phi^0$  production ( $W^+ W^-$  &  $ZZ$ )
- $W^+ Z \Phi^-$  interaction not present in 2HDM (i.e. SUSY)  
∴ WZ scattering may provide evidence for Higgs triplets



# The Littlest Higgs Model

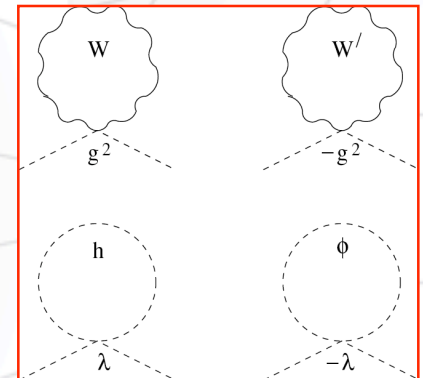
N. Arkani-Hamed et al. (2002) hep-ph/0206021



- Introduce new interactions at scale  $\Lambda = 4\pi f \sim 10$  TeV with new particles at  $f \sim 1$  TeV: heavy gauge bosons, heavy scalars, new heavy quarks.

- Quadratic divergences in  $M_H^2$  are cancelled by the contributions of these new particles.

$$\delta M_H^2 = \frac{G_F \Lambda^2}{4\sqrt{2}\pi^2} (6M_W^2 + 3M_Z^2 + M_H^2 - 12M_t^2) + \dots$$



- Scalar Sector:

$$h = \begin{pmatrix} h^+ \\ h^0 \end{pmatrix}$$

Doublet

$$\phi = \begin{pmatrix} \phi^{++} & \phi^+/\sqrt{2} \\ \phi^+/\sqrt{2} & \phi^0 \end{pmatrix}$$

Triplet



# The Littlest Higgs Model

N. Arkani-Hamed et al. (2002) hep-ph/0206021



- Higgs fields acquire vevs, triggering EWSB

$$\langle h^0 \rangle = v/\sqrt{2}$$

$$\langle i\phi^0 \rangle = v'$$

$$\begin{aligned} W_\mu^+ W_\nu^- \Phi^0 & -\frac{i}{2} g^2 (s_0 v - 2\sqrt{2}v') g_{\mu\nu} \simeq 0 \\ Z_\mu Z_\nu \Phi^0 & -\frac{i}{2} \frac{g^2}{c_W^2} (s_0 v - 4\sqrt{2}v') g_{\mu\nu} \simeq \sqrt{2} i \frac{g^2}{c_W^2} v' g_{\mu\nu} \\ W_\mu^+ Z_\nu \Phi^- & -i \frac{g^2}{c_W} v' g_{\mu\nu} \\ W_\mu^+ h \Phi^- & -i \frac{g}{2} (\sqrt{2}s_0 - s_+) (p_1 - p_2)_\mu \simeq -i g \frac{v'}{v} (p_1 - p_2)_\mu \\ W_\mu^+ W_\nu^+ \Phi^{--} & 2ig^2 v' g_{\mu\nu} \end{aligned}$$

- Couplings to vector bosons  $\sim v'$
- EW data indicate:  $1 \text{ GeV} \lesssim v' \lesssim 4 \text{ GeV}$  for  $f = 2 \text{ TeV}$

M.-C. Chen and S. Dawson (2004) hep-ph/0311032v3

# The Left-Right Symmetric Model

R.N. Mohapatra and J.C. Pati, Phys. Rev. D **11**, 566 (1975)



$$\Delta_L = \begin{pmatrix} \delta_L^+/\sqrt{2} & \delta_L^{++} \\ \delta_L^0 & -\delta_L^+/\sqrt{2} \end{pmatrix}$$
$$\Delta_R = \begin{pmatrix} \delta_R^+/\sqrt{2} & \delta_R^{++} \\ \delta_R^0 & -\delta_R^+/\sqrt{2} \end{pmatrix}$$

$$\langle \Delta_{L,R} \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & 0 \\ v_{L,R} & 0 \end{pmatrix}$$

- Triplet vevs break  $SU(2)_L \times SU(2)_R \times U(1)_{B-L} \rightarrow SU(2)_L \times U(1)_Y$
- $\Delta_R$  couples to  $W_R, Z_R$  (heavy gauge bosons) with couplings  $\sim v_R$
- $\Delta_L$  couples to  $W_L, Z_L$  (SM gauge bosons) with couplings  $\sim v_L$

$$\rho = 1.0004_{-0.0007}^{+0.0027} \text{ at } 2\sigma$$

C. Amsler et al. (PDG), Phys. Lett. B **667**, 1 (2008)

- Constraints on  $\rho$  parameter  $\Rightarrow$

$$v' \equiv v_L/\sqrt{2} \lesssim 2 \text{ GeV}$$

# The Georgi-Machacek Model

H. Georgi and M. Machacek, Nucl. Phys. B **262**, 463 (1985)



- Introduce scalar triplets:

$$\chi = \begin{pmatrix} \chi^0 & \xi^+ & \chi^{++} \\ \chi^- & \xi^0 & \chi^+ \\ \chi^{--} & \xi^- & \chi^{0*} \end{pmatrix}$$

$$\langle \chi^0 \rangle = \langle \xi^0 \rangle = v'$$

- Triplet mass eigenstates:

–  $(H_3^+, H_3^0, H_3^-)$  couples to fermions

–  $(H_5^{\pm\pm}, H_5^\pm, H_5^0)$  couples to vector bosons with couplings  $\sim s_H \sim v'$

$$s_H^2 \equiv \frac{8v'^2}{v^2}$$

- $\tan\theta_H \equiv s_H/c_H \lesssim 0.5, 1, 1.7$  for  $M_{H_3} = 0.1, 0.5, 1$  TeV (95% C.L. from  $Zb\bar{b}$ )

H. Haber and H. Logan, Phys. Rev. D **62**, 015011 (2000)

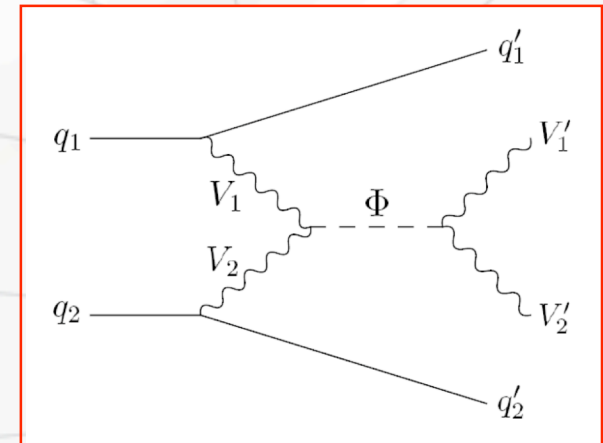
- In our calculations, we use  $\tan\theta_H = 0.5 \Rightarrow v' = 39$  GeV

# Vector Boson Scattering



$$pp \rightarrow V V jj \quad (V = W^\pm, Z)$$

Consider “gold-plated” leptonic decay modes  
(smaller branching ratio, but lower QCD backgrounds  
than hadronic or semileptonic decays)



Decay mode ( $l = e, \mu$ )	B.R.
$W^\pm W^\pm \rightarrow l^\pm \nu l^\pm \nu$	0.047
$W^\pm Z \rightarrow l^\pm \nu l^+ l^-$	0.015
$W^+ W^- \rightarrow l^+ \nu l^- \nu$	0.047
$Z Z \rightarrow l^+ l^- l^+ l^-$	0.0045
$Z Z \rightarrow l^+ l^- \nu \bar{\nu}$	0.019

## Signal Characteristics:

- 2 energetic forward jets
- Low jet activity in central region
- Leptons at low rapidity
- $\sigma_{\text{sig}} \sim v'^2$



# Vector Boson Scattering



Backgrounds      V. Barger et al. (1990) & J. Bagger et al. (1994, 1995)

- Irreducible EW background:  $q_1 q_2 \rightarrow q'_1 q'_2 V V$  at  $O(\alpha^4)$

$$\sigma_{signal}(pp \rightarrow V_L V_L jj) \equiv \sigma_{total}(pp \rightarrow V V jj) - \sigma_{SM}(pp \rightarrow V V jj)$$

- QCD background:  $q_1 q_2 \rightarrow V V + QCD \text{ jets}$  up to  $O(\alpha^2 \alpha_s^2)$

- Top quark backgrounds ( $t \rightarrow Wb$ ):

$W^\pm t\bar{t}$       for  $W^\pm W^\pm$  final state

$Z t\bar{t} + jet$       for  $W^\pm Z$  final state

$t\bar{t} + jet$       for  $W^+ W^-$  final state

- Include  $q_1 q_2 \rightarrow q'_1 q'_2 W^\pm Z \rightarrow \ell^\pm \ell^\pm + X$  as background to  $W^\pm W^\pm$  channel

- MADGRAPH was used to simulate the signals and backgrounds ( $\sqrt{s} = 14 \text{ TeV}$ )

# $\Phi^{\pm\pm}$ Production: $W^\pm W^\pm \rightarrow \ell^\pm \nu \ell^\pm \nu$



## SM Backgrounds:

- EW Background:

$$pp \rightarrow W^\pm W^\pm jj, \mathcal{O}(\alpha^4)$$

- QCD Background:

$$pp \rightarrow W^\pm W^\pm jj, \mathcal{O}(\alpha^2 \alpha_s^2)$$

- Top Quark Background:

$$pp \rightarrow W^\pm t\bar{t},$$
$$pp \rightarrow W^\pm t\bar{t}j,$$

with  $t \rightarrow Wb$ .

- $W^\pm Z$  Background:

$$pp \rightarrow W^\pm Z + nj$$

## Cuts:

$$3.0 < |y(j_{tag})| < 5.0$$

$$p_T(j_{tag}) > 40 \text{ GeV}$$

$$E(j_{tag}) > 500 \text{ GeV}$$

$$|y(j_{veto})| < 3.0$$

$$p_T(j_{veto}) > 100 \text{ GeV}$$

$$|y(l)| < 2.5$$

$$p_T(l_1) > 200 \text{ GeV}$$

$$p_T(l_2) > 50 \text{ GeV}$$

$$\Delta p_T(ll) = |p_T(l_1) - p_T(l_2)| > 300 \text{ GeV}$$

$$\Delta y(ll) = |y(l_1) - y(l_2)| < 3$$

$$M_T(WW) > 550 \text{ (800) GeV}$$

$$\text{for } M_\Phi = 1.0 \text{ (1.5) TeV}$$

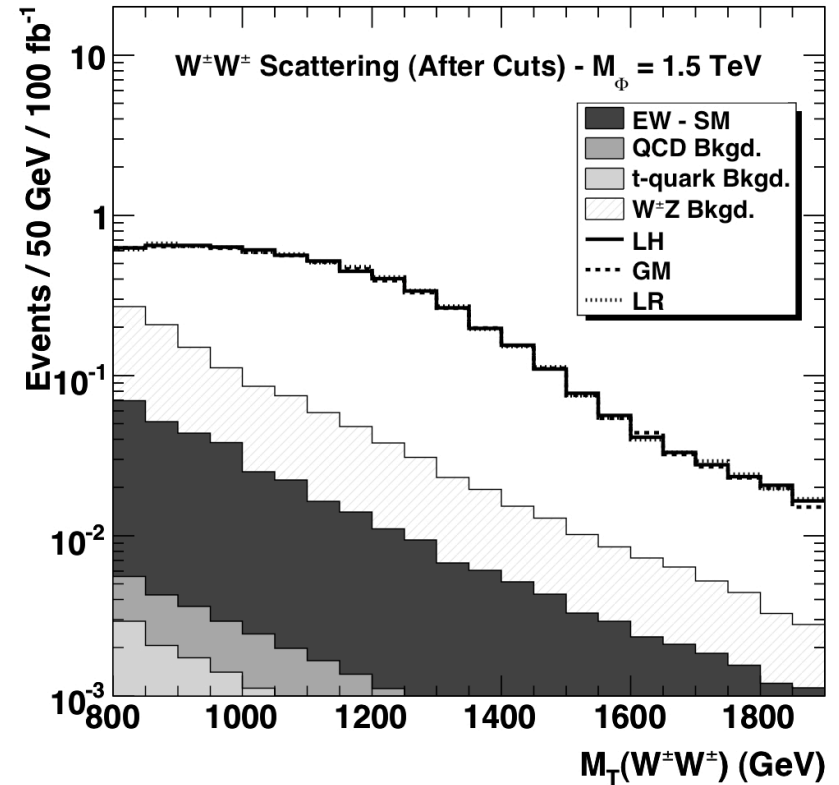
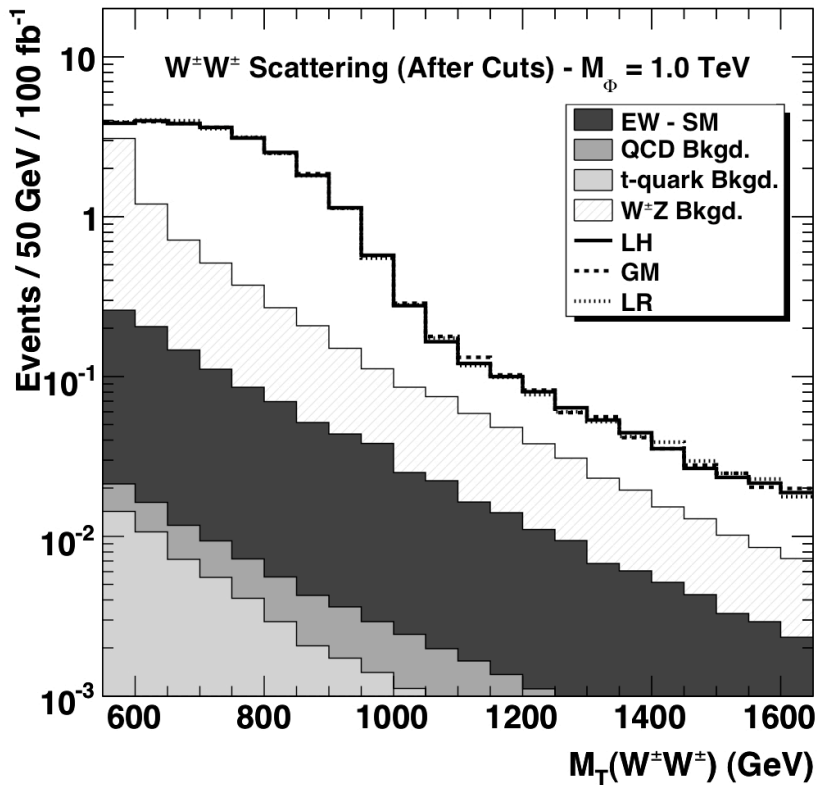
## WW Cluster Transverse Mass:

$$M_T^2(WW) = \left[ \sqrt{M^2(ll) + p_T^2(ll)} + |\mathbf{p}_T| \right]^2 - [\mathbf{p}_T(ll) + \mathbf{p}_T]^2$$

# $\Phi^{\pm\pm}$ Production: $W^{\pm} W^{\pm} \rightarrow l^{\pm} \nu l^{\pm} \nu$



$v' = 39 \text{ GeV}$



- Identical signals in all 3 models (same  $W^+W^+\Phi^-$  vertices)
- $\sigma_{\text{sig}} = 0.245$  (0.0848) fb &  $\sigma_{\text{back}} = 0.0798$  (0.0204) fb for  $M_{\Phi} = 1.0$  (1.5) TeV

# $\Phi^\pm$ Production: $W^\pm Z \rightarrow \ell^\pm \nu \ell^+ \ell^-$



## SM Backgrounds:

- EW Background:

$$pp \rightarrow W^\pm Z jj, \mathcal{O}(\alpha^4)$$

- QCD Background:

$$pp \rightarrow W^\pm Z j, \mathcal{O}(\alpha^2 \alpha_s)$$

$$pp \rightarrow W^\pm Z jj, \mathcal{O}(\alpha^2 \alpha_s^2)$$

- Top Quark Background:

$$pp \rightarrow Z t \bar{t},$$

$$pp \rightarrow Z t \bar{t} j,$$

with  $t \rightarrow W b$ .

## Cuts:

$$|y(l)| < 2.5$$

$$p_T(l_1) > 150 \text{ GeV}$$

$$p_T(l_2) > 50 \text{ GeV}$$

$$p_T(l_3) > 50 \text{ GeV}$$

$$\cancel{p}_T > 50 \text{ GeV}$$

$$M_T(WZ) > 900 \text{ (1250) GeV}$$

$$\text{for } M_\Phi = 1.0 \text{ (1.5) TeV}$$

$$3.0 < |y(j_{tag})| < 5.0$$

$$p_T(j_{tag}) > 40 \text{ GeV}$$

$$E(j_{tag}) > 500 \text{ GeV}$$

$$|y(j_{veto})| < 3.0$$

$$p_T(j_{veto}) > 100 \text{ GeV}$$

## WZ Cluster Transverse Mass:

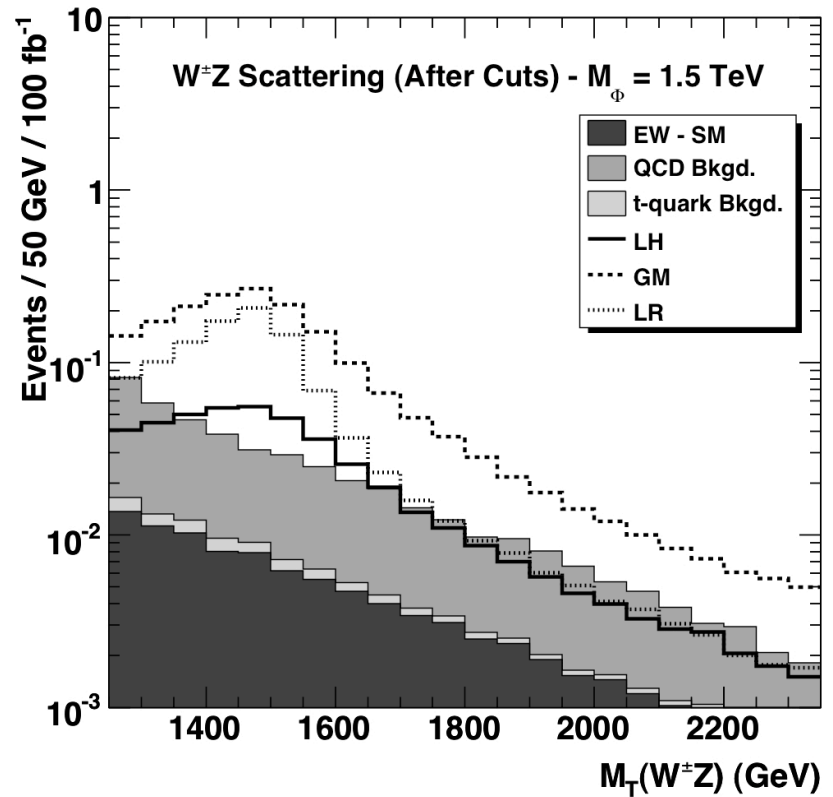
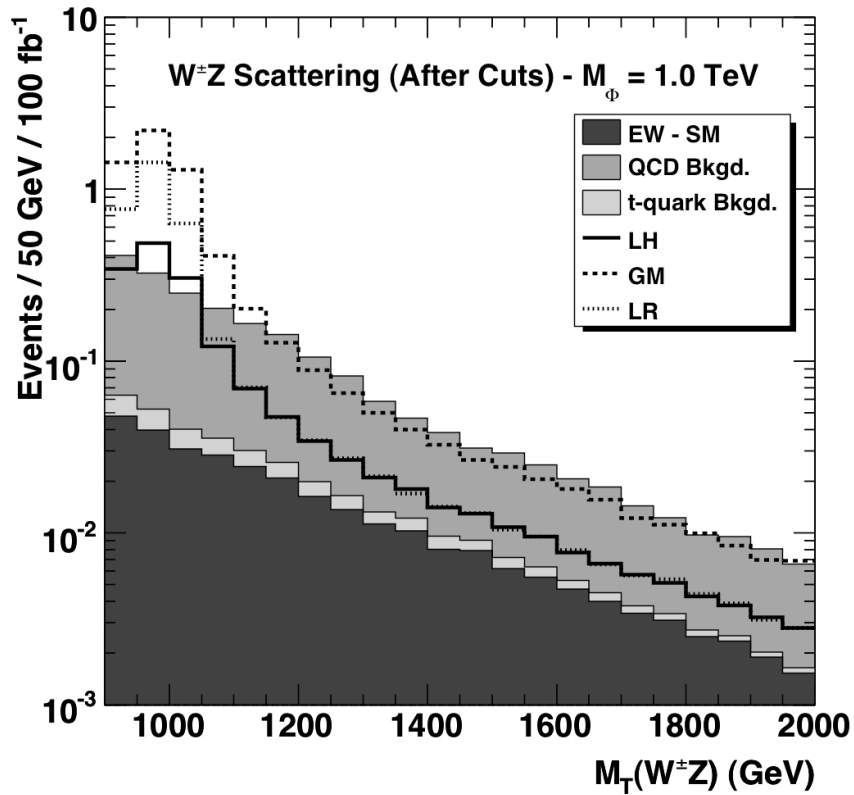
$$M_T^2(WZ) = \left[ \sqrt{M^2(lll) + p_T^2(lll)} + |\cancel{\mathbf{p}}_T| \right]^2 - [\mathbf{p}_T(lll) + \cancel{\mathbf{p}}_T]^2$$



# $\Phi^\pm$ Production: $W^\pm Z \rightarrow l^\pm \nu l^+ l^-$



$$v' = 39 \text{ GeV}$$



# $\Phi^0$ Production: $W^+ W^- \rightarrow \ell^+ \nu \ell^- \bar{\nu}$



## SM Backgrounds:

- EW Background:

$$pp \rightarrow W^+ W^- jj, \mathcal{O}(\alpha^4)$$

- QCD Background:

$$pp \rightarrow W^+ W^- j, \mathcal{O}(\alpha^2 \alpha_s)$$

$$pp \rightarrow W^+ W^- jj, \mathcal{O}(\alpha^2 \alpha_s^2)$$

- Top Quark Background:

$$pp \rightarrow t\bar{t},$$

$$pp \rightarrow t\bar{t}j,$$

with  $t \rightarrow Wb$ .

## Cuts:

$$3.0 < |y(j_{tag})| < 5.0$$

$$p_T(j_{tag}) > 40 \text{ GeV}$$

$$E(j_{tag}) > 800 \text{ GeV}$$

$$|y(j_{veto})| < 3.0$$

$$p_T(j_{veto}) > 60 \text{ GeV}$$

$$|y(l)| < 2.5$$

$$p_T(l_1) > 300 \text{ GeV}$$

$$p_T(l_2) > 150 \text{ GeV}$$

$$\Delta p_T(ll) = |p_T(l_1) - p_T(l_2)| > 500 \text{ GeV}$$

$$\Delta y(ll) = |y(l_1) - y(l_2)| < 3$$

$$M_T(WW) > 700 \text{ (1000) GeV}$$

for  $M_\Phi = 1.0 \text{ (1.5) TeV}$

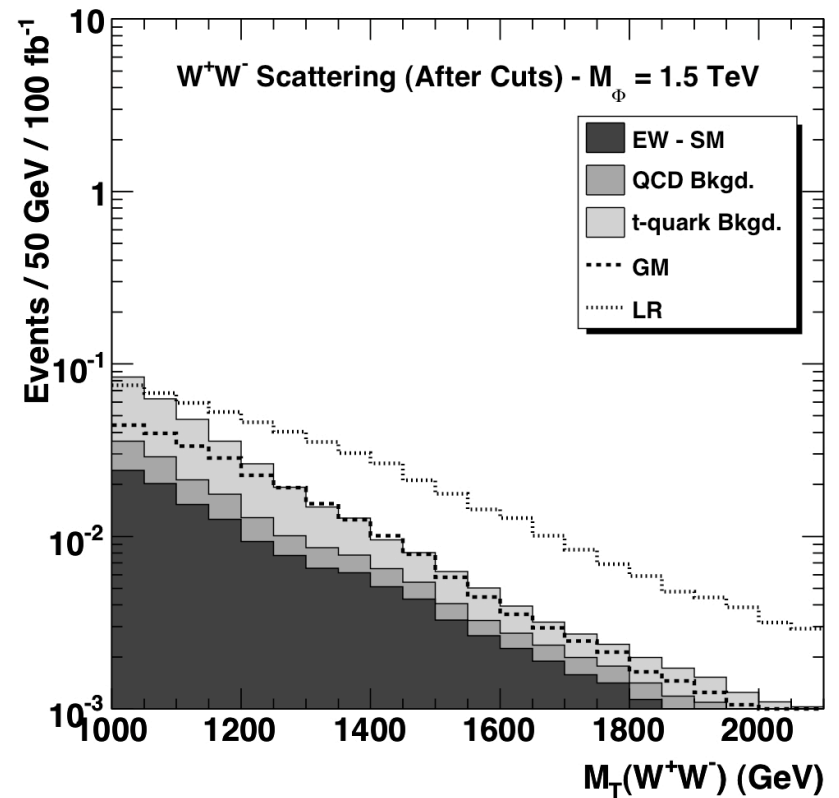
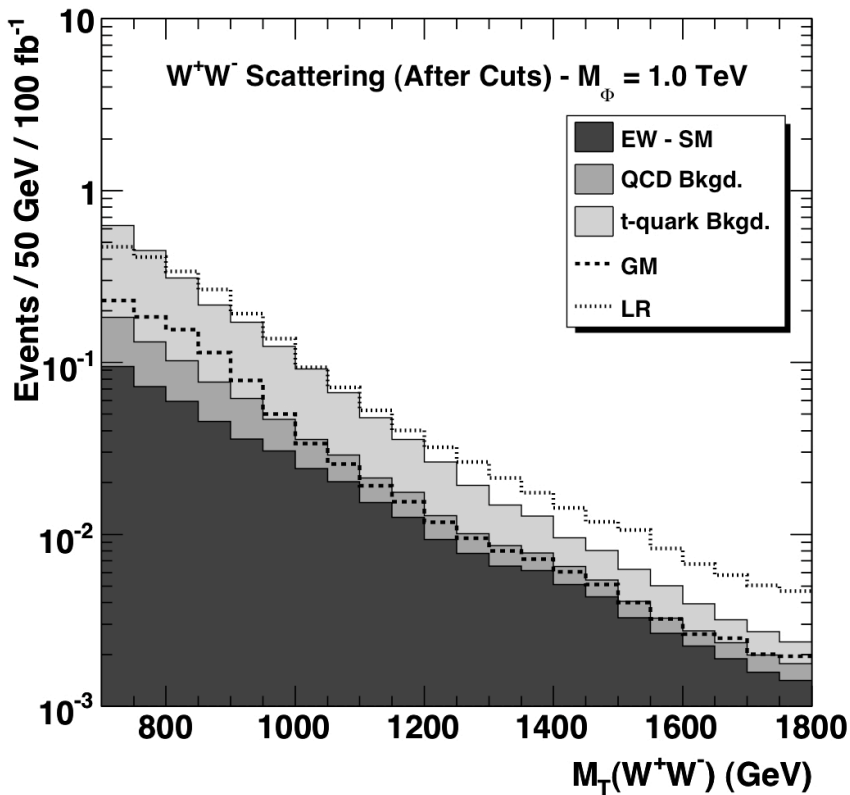
## WW Cluster Transverse Mass:

$$M_T^2(WW) = \left[ \sqrt{M^2(ll) + p_T^2(ll)} + |\not{\mathbf{p}}_T| \right]^2 - [\mathbf{p}_T(ll) + \not{\mathbf{p}}_T]^2$$

# $\Phi^0$ Production: $W^+ W^- \rightarrow \ell^+ \nu \ell^- \bar{\nu}$



$$v' = 39 \text{ GeV}$$



Note:  $W^+W^-\Phi^0 \approx 0$  in Littlest Higgs Model

$W^+W^-$  final state suffers from large QCD & t-quark backgrounds

# $\Phi^0$ Production: $ZZ \rightarrow \ell^+ \ell^- \ell^+ \ell^-$



SM Backgrounds:

- EW Background:

$$pp \rightarrow ZZjj, \mathcal{O}(\alpha^4)$$

- QCD Background:

$$pp \rightarrow ZZj, \mathcal{O}(\alpha^2 \alpha_s)$$

$$pp \rightarrow ZZjj, \mathcal{O}(\alpha^2 \alpha_s^2)$$

Cuts:

$$3.0 < |y(j_{tag})| < 5.0$$

$$p_T(j_{tag}) > 40 \text{ GeV}$$

$$E(j_{tag}) > 500 \text{ GeV}$$

no jet veto

$$|y(l)| < 2.5$$

$$p_T(l) > 70 \text{ GeV}$$

$$M(ZZ) > 900 (1250) \text{ GeV}$$

$$\text{for } M_\Phi = 1.0 (1.5) \text{ TeV}$$

No t-quark backgrounds

Jet veto not used, as this further reduces the already small number of signal events

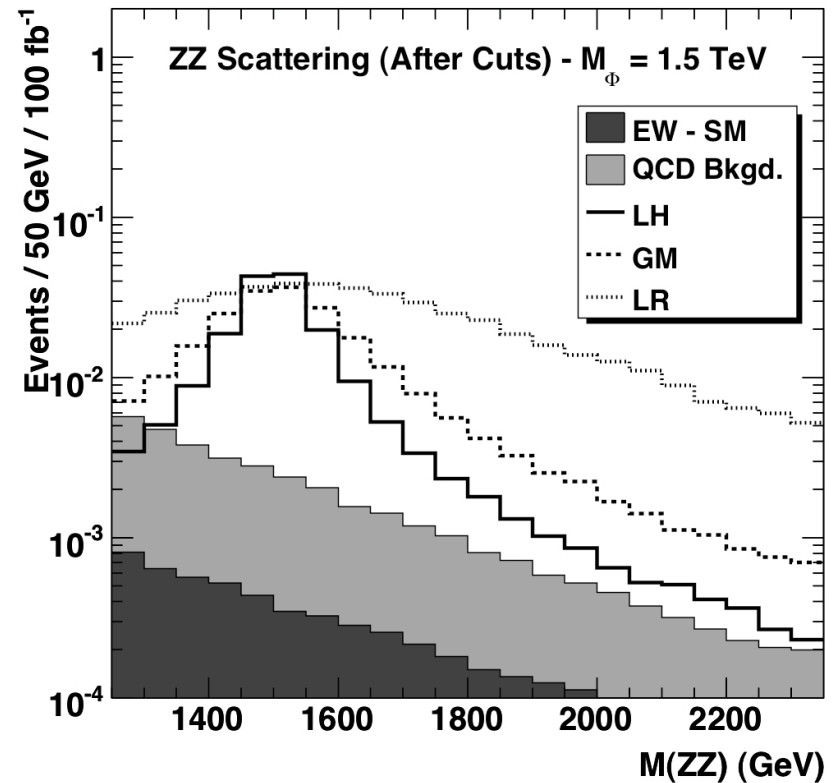
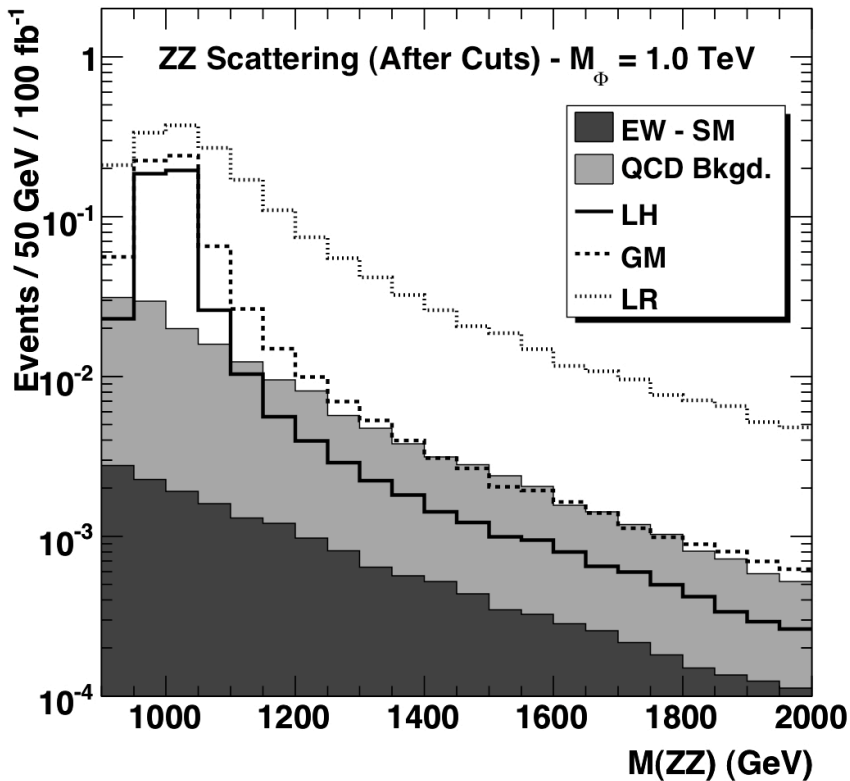
Can reconstruct ZZ invariant mass



# $\Phi^0$ Production: $ZZ \rightarrow l^+ l^- l^+ l^-$



$$v' = 39 \text{ GeV}$$



- Low event rate in  $ZZ \rightarrow 4 \text{ lepton}$  channel
- $ZZ \rightarrow l^+ l^- \nu \bar{\nu}$  mode may improve  $\Phi^0$  discovery potential

# Discovery Potential



Integrated luminosity required for at least 10 signal events and  $S / \sqrt{B} \geq 5$

Channel	Littlest Higgs		Georgi-Machacek		Left-right symmetric	
	$M_\Phi = 1.0$ TeV (fb <sup>-1</sup> )	$M_\Phi = 1.5$ TeV (fb <sup>-1</sup> )	$M_\Phi = 1.0$ TeV (fb <sup>-1</sup> )	$M_\Phi = 1.5$ TeV (fb <sup>-1</sup> )	$M_\Phi = 1.0$ TeV (fb <sup>-1</sup> )	$M_\Phi = 1.5$ TeV (fb <sup>-1</sup> )
$W^\pm W^\pm$	41	118	41	119	41	117
$W^\pm Z$	3300	4350	171	474	591	877
$W^+ W^-$	...	...	22 300	25 200	1840	2980
ZZ	2230	5780	1520	4290	543	1720

- Unlikely to observe triplet during early years of LHC running ( $\sim 10$  fb<sup>-1</sup> / year)
- Doubly charged (and possibly singly charged) Higgs in GM model may be observed once design luminosity ( $\sim 100$  fb<sup>-1</sup> / year) is achieved
- Note: These results assume  $v' = 39$  GeV, and  $\sigma_{\text{sig}} \sim v'^2$
- Discovery in LH model (assuming  $v' = 4$  GeV) and in L-R model (assuming  $v' = 2$  GeV) would require several ab<sup>-1</sup>

# Conclusions



- Cross sections for Higgs triplet production depend quadratically on  $v'$
- Discovery in the Georgi-Machacek model is more promising than in the Littlest Higgs or L-R Symmetric models (due to larger upper bound on  $v'$ )
- $W^\pm W^\pm$  channel is most promising for discovery at the LHC
- $W^\pm Z$  scattering signal may be discovered for certain regions of parameter space  
⇒ smoking gun for Higgs triplet
- Ratio of rates in  $W^\pm W^\pm$  &  $W^\pm Z$  channel allows to distinguish models
- Discovery not very promising for  $W^+ W^-$  final state (large QCD & t-quark backgrounds) or for  $ZZ \rightarrow 4$  leptons (small signal cross section)
- $ZZ \rightarrow \ell^+ \ell^- \nu \bar{\nu}$  mode may improve  $\Phi^0$  discovery potential
- Semi-leptonic decay modes may improve discovery potential
- High luminosity is required for some channels/models. Need to wait for SLHC.