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# Recent Results from BaBar on the CKM Angles

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Lehrstuhl experimentelle Physik 5



1. BaBar and PEP-II
2. CKM angles
3. recent results
  - on  $\beta$
  - on  $\alpha$
  - on  $\gamma$
4. summary

# BaBar and PEP-II



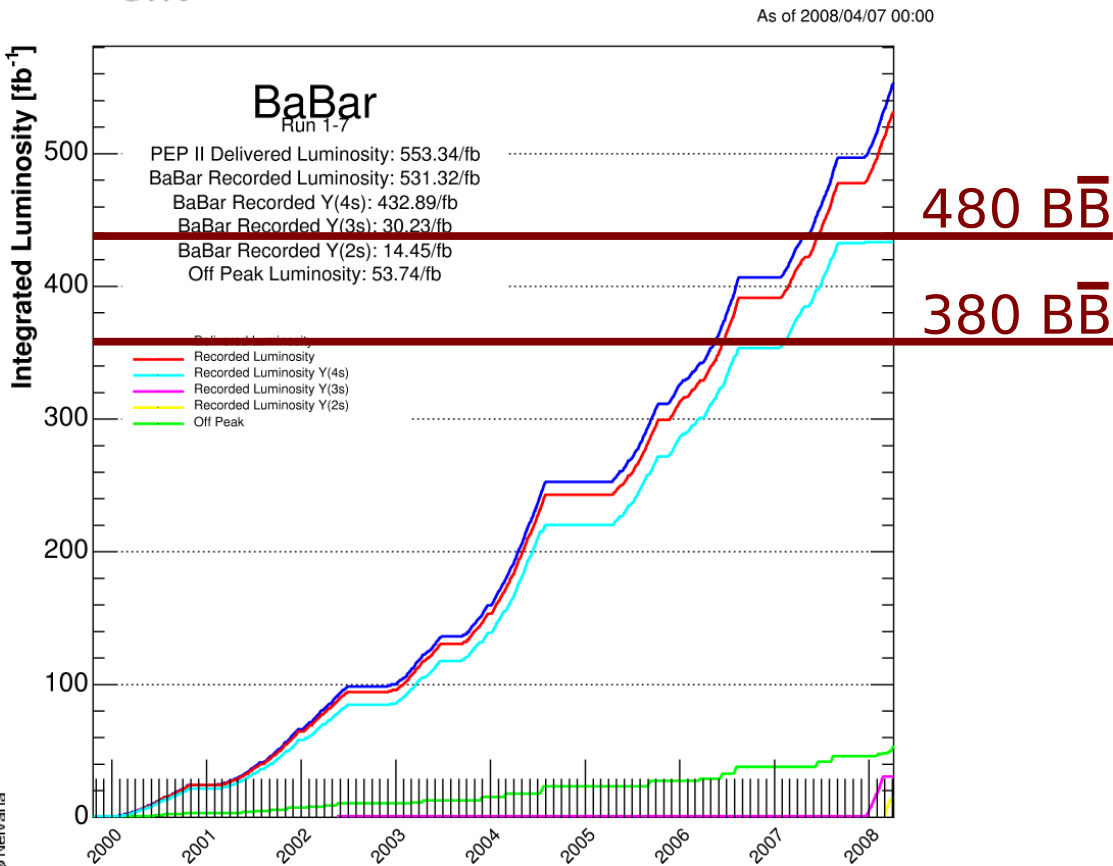
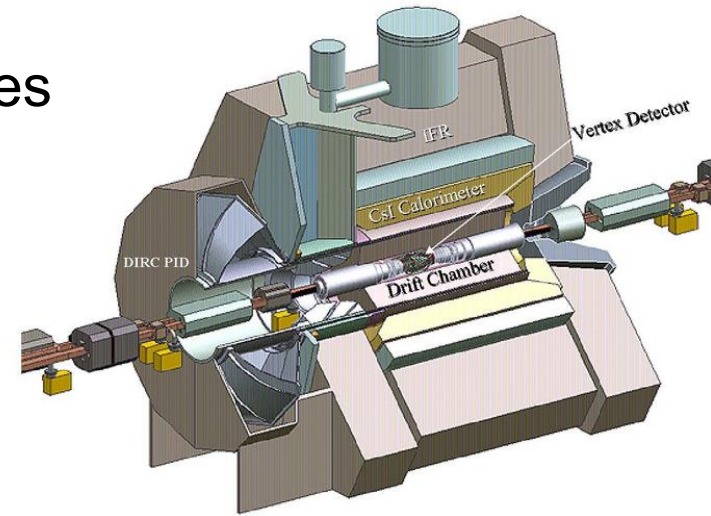
- B-Factory took data till April 7th, 2008.

**480 · 10<sup>6</sup> BB pairs** final  $\Upsilon(4S)$  dataset

**380 · 10<sup>6</sup> BB pairs** used by most analyses

$$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B^0\bar{B}^0, B^+B^-$$

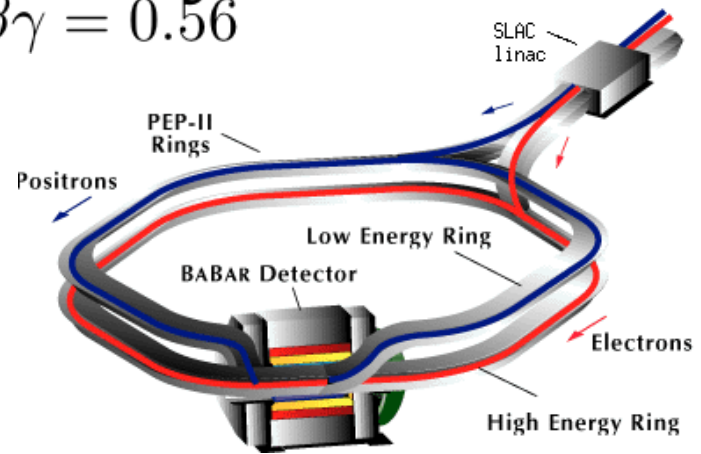
$$E_{cm} = 10.58 \text{ GeV}$$



$$E(e^+) = 3.1 \text{ GeV}$$

$$E(e^-) = 9.0 \text{ GeV}$$

$$\beta\gamma = 0.56$$



CKM angles

# CKM quark mixing mechanism



$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \approx \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

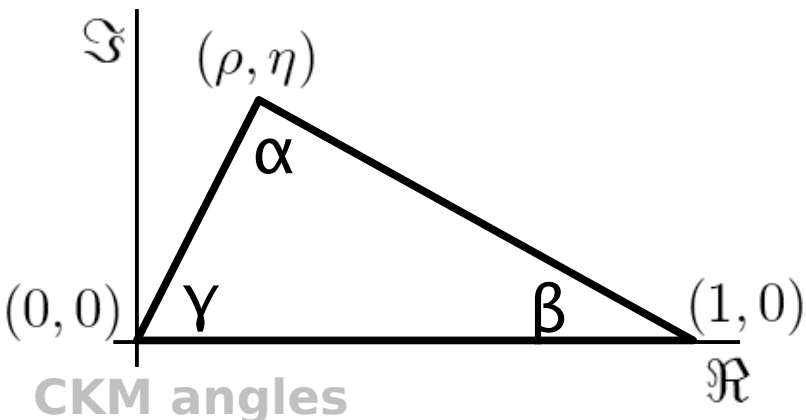
- flavor eigenstates are not mass eigenstates → relate them through a unitary matrix
- irreducible phase is the only source of CP violation in the Standard Model
- test the SM by over-constraining the unitarity triangle

**Cabibbo  
Kobayashi  
Maskawa**

$\lambda \approx 0.23$   
 $A \approx 0.8$   
 $\rho \approx 0.2$   
 $\eta \approx 0.4$

$$V^\dagger V = 1$$

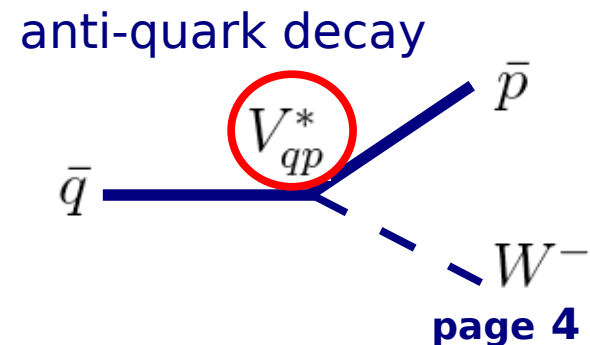
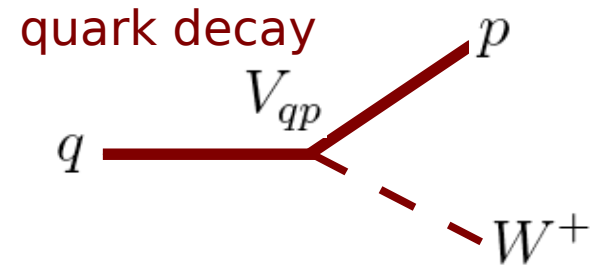
$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$



$$\alpha = \arg \left( -\frac{V_{td}V_{tb}^*}{V_{ud}V_{ub}^*} \right)$$

$$\gamma = \arg \left( -\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right)$$

$$\beta = \arg \left( -\frac{V_{cd}V_{cb}^*}{V_{td}V_{tb}^*} \right)$$



# $\beta$ from $B^0 \rightarrow J/\psi \pi^0$

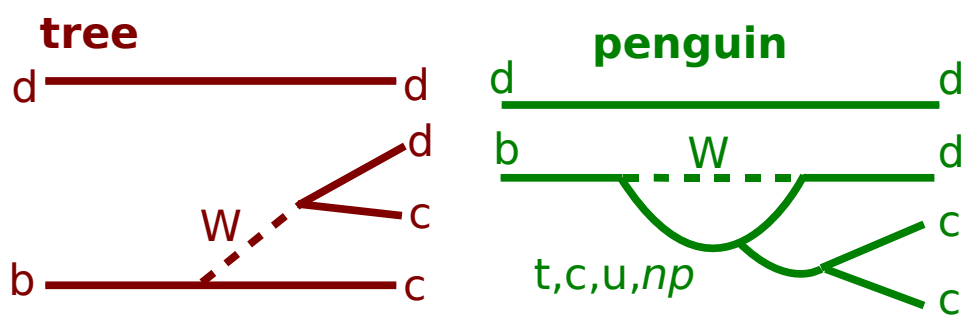
**466 · 10<sup>6</sup> BB**  
 April 2008 **new!**  
 arxiv:0804.0896

- Cabibbo suppressed  $b \rightarrow c\bar{c}d$  transition to CP even final state.  $B^0 - \bar{B}^0$  mixing amplitude contains  $\beta$ .

- time dependent measurement to extract S and C

$$f_{\pm}(\Delta t) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} [1 \pm S \sin(\Delta m_d \Delta t) \mp C \cos(\Delta m_d \Delta t)]$$

- Tree level expectation is  $S = -\sin 2\beta$  and  $C = 0$ . If there is a significant penguin amplitude this mode could be sensitive to new physics.



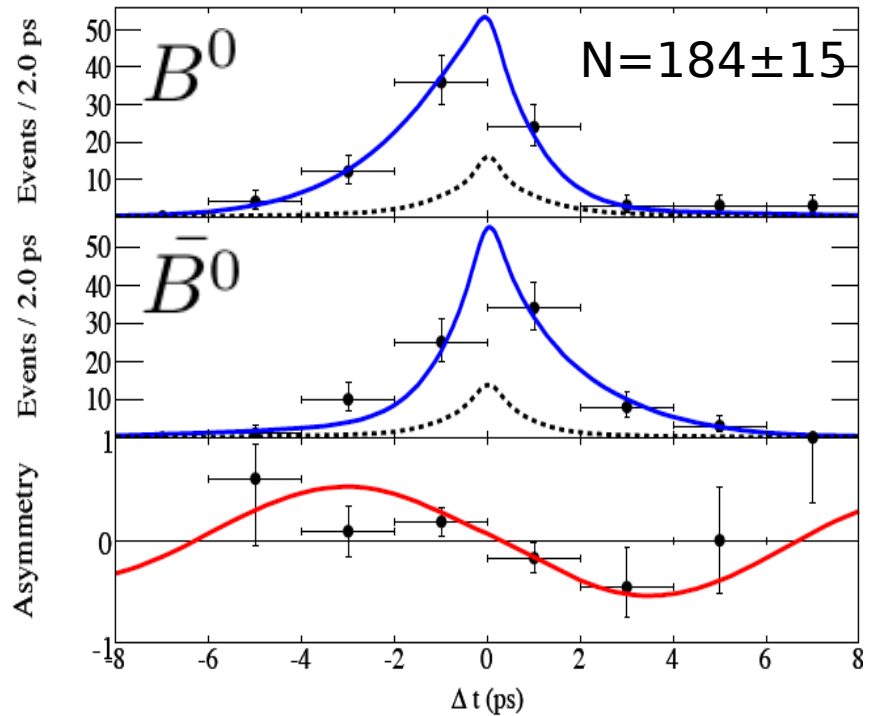
$$B = (1.69 \pm 0.14(\text{stat}) \pm 0.07(\text{syst})) \times 10^{-5},$$

$$S = -1.23 \pm 0.21(\text{stat}) \pm 0.04(\text{syst}),$$

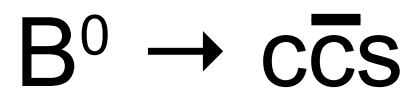
$$C = -0.20 \pm 0.19(\text{stat}) \pm 0.03(\text{syst}),$$

**non-zero at 4.0 $\sigma$  !**

Consistent with tree dominated SM.



# $\beta$ – more results



- precision measurement

$J/\psi K_S^0, J/\psi K_L^0, \psi(2S)K_S^0,$   
 $\chi_{c1}K_S^0, \eta_c K_S^0,$  and  $J/\psi K^{*0}$

$\sin 2\beta = 0.714 \pm 0.032(\text{stat}) \pm 0.018(\text{syst})$

**383 · 10<sup>6</sup> BB**  
October 2007  
PRL99, 171803

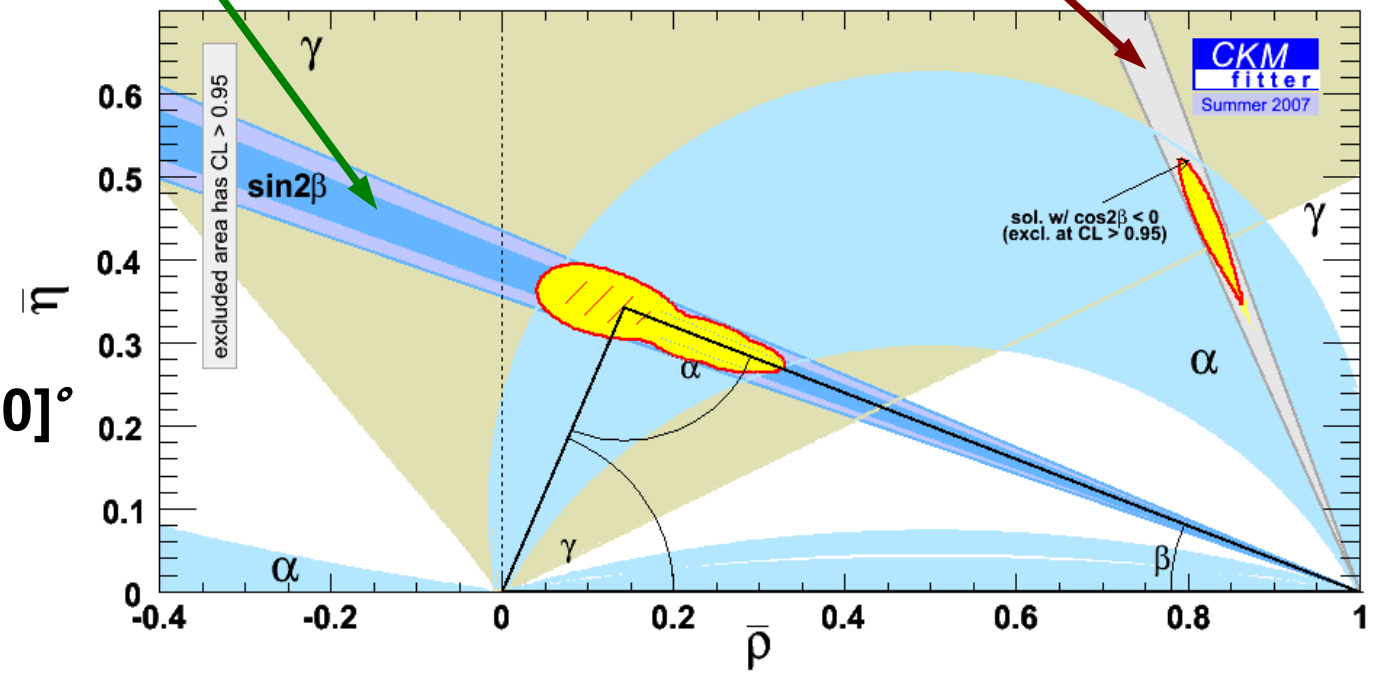
**383 · 10<sup>6</sup> BB**  
August 2007  
PRL99, 231802

$\cos 2\beta > 0$   
@86% C.L.

from  
 $B^0 \rightarrow D^{(*)}h^0$

excludes region

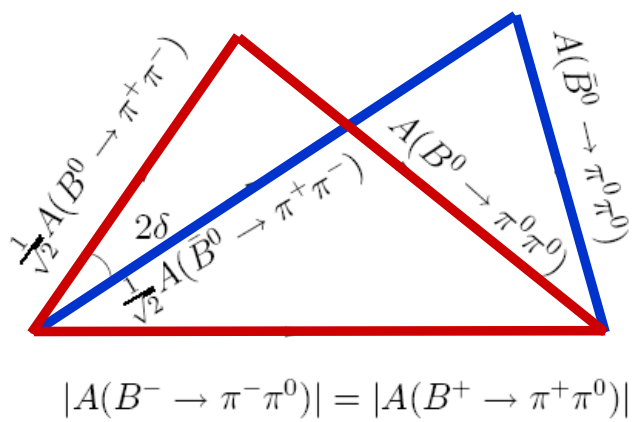
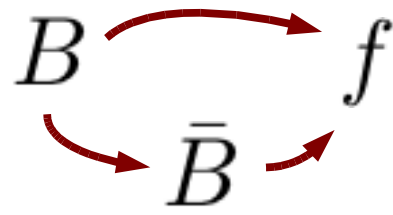
$\beta = 21.5^\circ [+1.0 -1.0]^\circ$   
CKMfitter



# $\alpha$ from $B^0 \rightarrow \pi^0 \pi^0$ , $B^+ \rightarrow \pi^+ \pi^0$ , $B^+ \rightarrow K^+ \pi^0$

**383 · 10<sup>6</sup> BB**  
 November 2007  
 PRD76, 091102

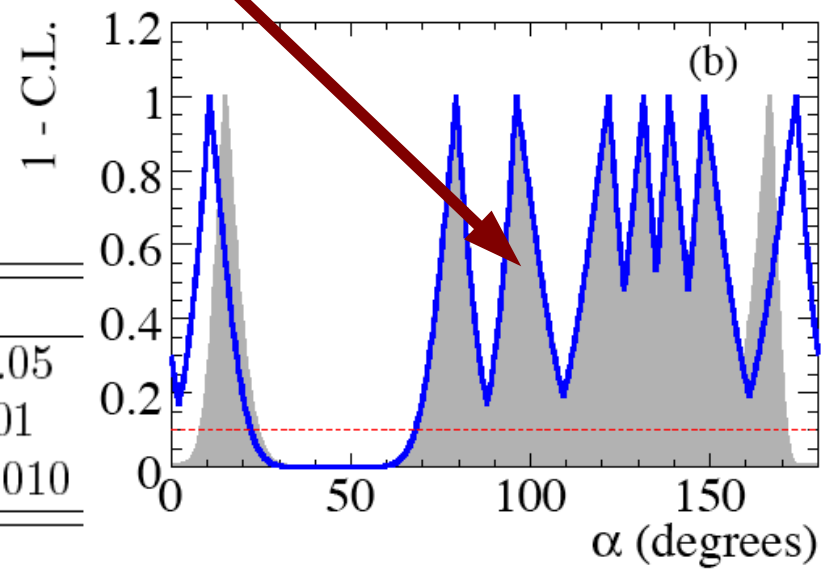
- Measure  $\alpha$  through interference of  $b \rightarrow u$  decays with and w/o  $B^0$  mixing.
- But BR measurements of  $B \rightarrow \pi\pi$  indicate penguins are large, so only sensitive to  $\alpha_{\text{eff}} = \alpha + \delta$
- use isospin relations to decouple penguin contribution



8-fold ambiguity

$\delta < 39^\circ$  @90% C.L.

$\alpha = (96_{-6}^{+10})^\circ$  most compatible with SM



Mode	$\mathcal{B}(10^{-6})$	Asymmetry
$B^0 \rightarrow \pi^0 \pi^0$	$1.47 \pm 0.25 \pm 0.12$	$-0.49 \pm 0.35 \pm 0.05$
$B^\pm \rightarrow \pi^\pm \pi^0$	$5.02 \pm 0.46 \pm 0.29$	$0.03 \pm 0.08 \pm 0.01$
$B^\pm \rightarrow K^\pm \pi^0$	$13.6 \pm 0.6 \pm 0.7$	$0.030 \pm 0.039 \pm 0.010$

**$B \rightarrow (\rho\pi)^0$**

**375 · 10<sup>6</sup> BB**  
July 2007  
PRD76, 012004

$\alpha = (87^{+45}_{-13})^\circ$

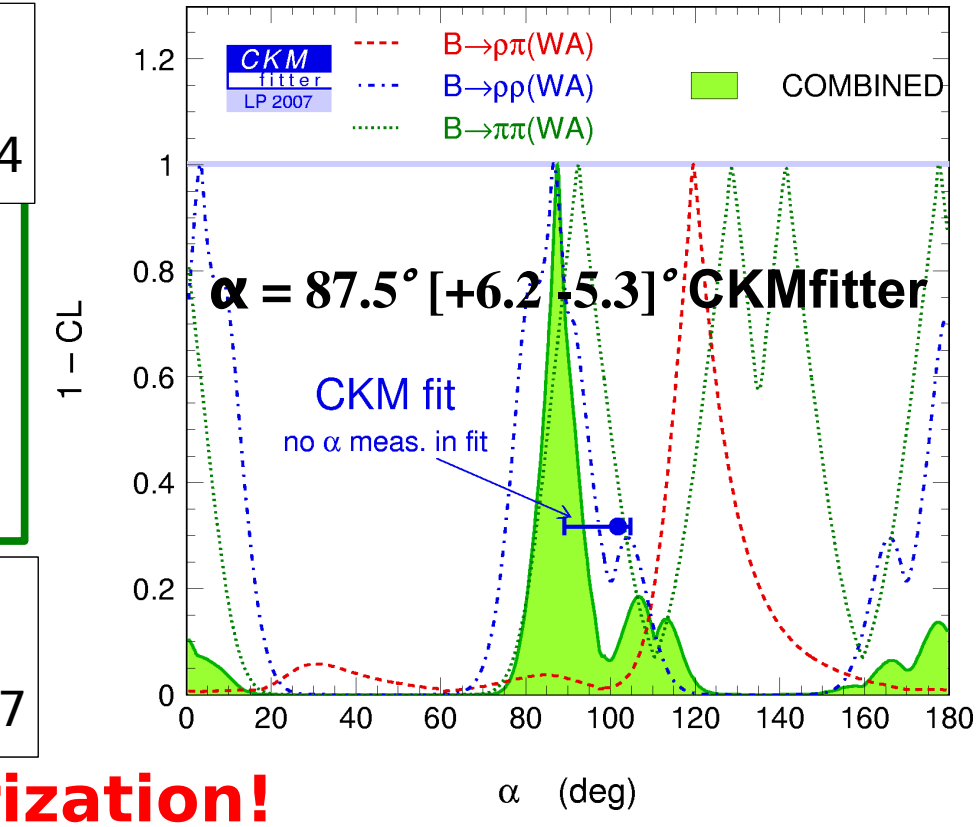
- Measure coefficients of time-dependent decay rate over Dalitz plot → no isospin analysis

**$B^0 \rightarrow \rho^+ \rho^-$**

**384 · 10<sup>6</sup> BB**  
July 2007  
PRD76, 052007

- Vector-Vector final state is a mixture of CP even & odd states → angular analysis required ( $f_L, S_L, C_L$ )
- Flavor SU(3) analysis

$\alpha = [83.3, 105.8]^\circ @68\% \text{ C.L.}$



**polarization!**

**$B^0 \rightarrow \rho^0 \rho^0$**

**427 · 10<sup>6</sup> BB**  
August 2007  
arxiv:0708.1630

- isospin analysis more effective

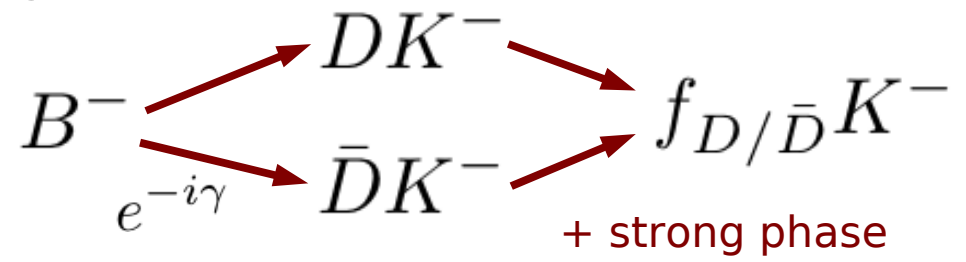
$\text{BR}(B \rightarrow \rho^0 \rho^0) < \text{BR}(B \rightarrow \pi^0 \pi^0) :$

$|\alpha - \alpha_{\text{eff}}| < 16.5^\circ$



# $\gamma$ from $B \rightarrow DK$

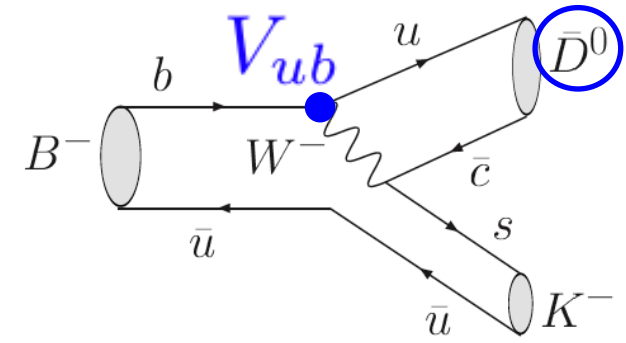
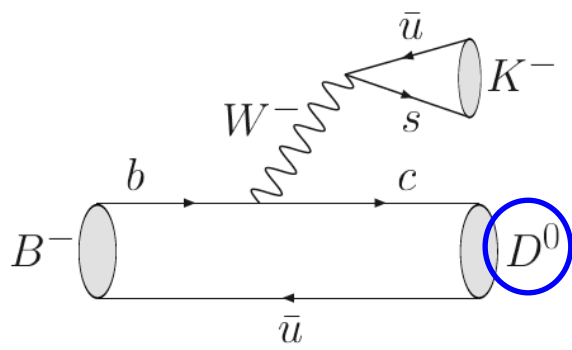
- $\gamma$  is the least well known CKM angle.
- Methods use final states accessible for both  $D^0$  and  $\bar{D}^0$ . Tree dominated, no new physics.



- Sensitivity on  $\gamma$  depends on amplitude ratio  $r$ . The uncertainty scales roughly like  $1/r$ .

$$r = \frac{|A(B \rightarrow \bar{D}^{(*)0}K)|}{|A(B \rightarrow D^{(*)0}K)|}$$

$$r \approx 0.1$$



- Several D final states can be used:
  - CP eigenstates (**GLW**)
  - Flavor eigenstates (**ADS**)
  - 3-body states (**GGSZ Dalitz**)

Gronau & London, PLB 253, 483 (1991)  
 Gronau & Wyler, PLB 265, 172 (1991)  
 Atwood, Dunietz, & Soni, PRL 78, 3257 (1997),  
 Atwood, Dunietz, & Soni, PRD 63, 036005 (2001)  
 Giri, Grossman, Soffer, & Zupan, PRD 68, 054018 (2003)  
 Bondar, PRD 70, 072003 (2004)

# $\gamma$ from $B^+ \rightarrow D^0 K^+$

**381 · 10<sup>6</sup> BB**  
 Feb 2008 *new!*  
 arxiv:0802.4052

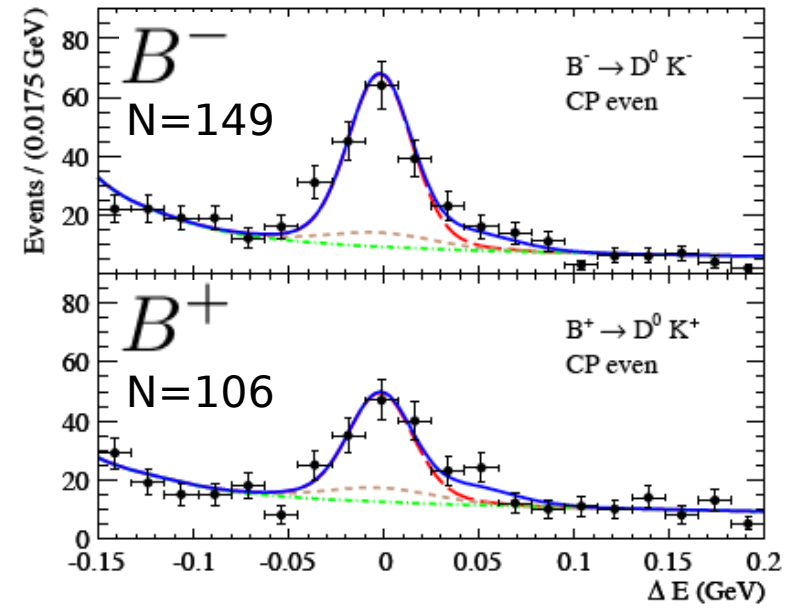
- **GLW** method uses CP final states accessible for both  $D^0$  and  $\bar{D}^0$ .
- based on triangle relations of amplitudes → inherent 8-fold ambiguity

$$R_{CP\pm} = 1 + r^2 \pm 2r \cos \delta \cos \gamma$$

$$A_{CP\pm} = \pm 2r \sin \delta \sin \gamma / R_{CP\pm}$$

$$R_{CP\pm} = \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{[\Gamma(B^- \rightarrow D^0 K^-) + \Gamma(B^+ \rightarrow \bar{D}^0 K^+)] / 2}$$

$$A_{CP\pm} = \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) - \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}$$



$D^0$ mode	$R_{CP}$	$A_{CP}$
$CP+$	$1.06 \pm 0.10 \pm 0.05$	$0.27 \pm 0.09 \pm 0.04$
$CP-$	$1.03 \pm 0.10 \pm 0.05$	$-0.09 \pm 0.09 \pm 0.02$

compatible with no CP violation @ **2.8 $\sigma$ !**

At current statistics the sensitivity on  $\gamma$  is low. Combine results with GGSZ Dalitz!

# $\gamma : B^+ \rightarrow D^{(*)0} K^{(*)+}$ with $D^0 \rightarrow K^0 K^+ K^-$ , $K^0 \pi^+ \pi^-$

**383 · 10<sup>6</sup> BB**  
 April 2008 **new!**  
 arxiv:0804.2089

- The **GGSZ** (Dalitz) method is the most precise single measurement of  $\gamma$

- Dalitz plot shows dynamics of the matrix element.

$$m_-^2 = m(K_S^0 \pi^-)^2 \quad m_+^2 = m(K_S^0 \pi^+)^2$$

- Dalitz amplitude depends on amplitude ratios  $r$ , the weak phase and a strong phase

$$A_{\mp}^{(*)}(m_-^2, m_+^2) \propto A_{D\mp} + \lambda r_B^{(*)} e^{i(\delta_B^{(*)} \mp \gamma)} A_{D\pm}$$

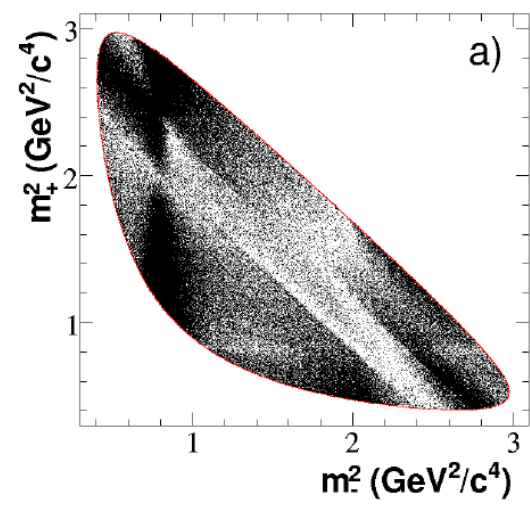
- obtain a Dalitz model  $A_{D\mp}$  from a high statistics control sample, fit it to the DK data

Cartesian coordinates:  
 (almost gaussian errors)

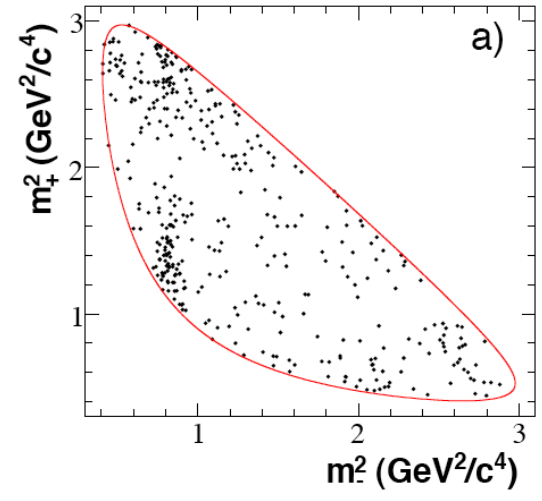
$$x_{\mp}^{(*)} = r_B^{(*)} \cos(\delta_B^{(*)} \mp \gamma)$$

$$y_{\mp}^{(*)} = r_B^{(*)} \sin(\delta_B^{(*)} \mp \gamma)$$

$D^* \rightarrow D\pi, D \rightarrow K_S \pi\pi$



$B^- \rightarrow DK^-, D \rightarrow K_S \pi\pi$



Parameters	$B^- \rightarrow \tilde{D}^0 K^-$	$B^- \rightarrow \tilde{D}^{*0} K^-$	$B^- \rightarrow \tilde{D}^0 K^{*-}$
$x_-, x_-^*, x_{s-}$	$0.090 \pm 0.043 \pm 0.015 \pm 0.011$	$-0.111 \pm 0.069 \pm 0.014 \pm 0.004$	$0.115 \pm 0.138 \pm 0.039 \pm 0.014$
$y_-, y_-^*, y_{s-}$	$0.053 \pm 0.056 \pm 0.007 \pm 0.015$	$-0.051 \pm 0.080 \pm 0.009 \pm 0.010$	$0.226 \pm 0.142 \pm 0.058 \pm 0.011$
$x_+, x_+^*, x_{s+}$	$-0.067 \pm 0.043 \pm 0.014 \pm 0.011$	$0.137 \pm 0.068 \pm 0.014 \pm 0.005$	$-0.113 \pm 0.107 \pm 0.028 \pm 0.018$
$y_+, y_+^*, y_{s+}$	$-0.015 \pm 0.055 \pm 0.006 \pm 0.008$	$0.080 \pm 0.102 \pm 0.010 \pm 0.012$	$0.125 \pm 0.139 \pm 0.051 \pm 0.010$

- Obtain ratios, strong phases and  $\gamma$  using a frequentist method.

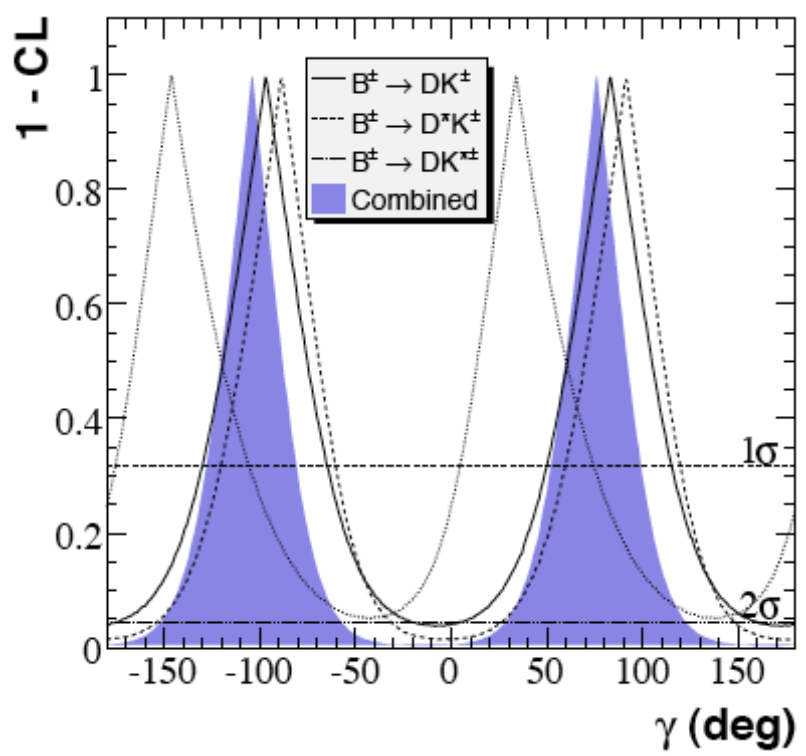
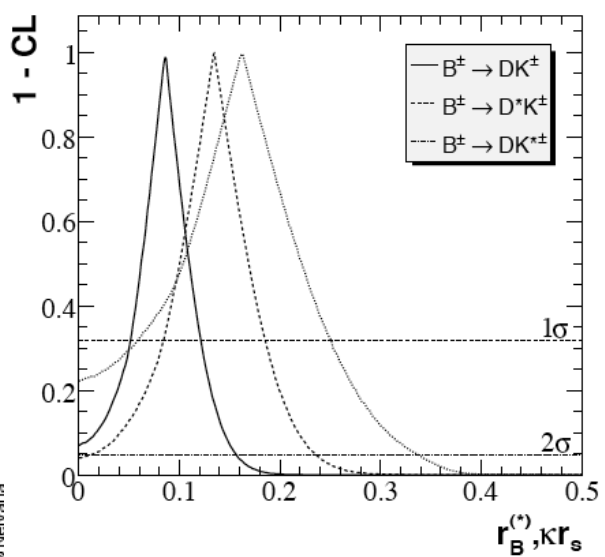
$$r_B = 0.086 \pm 0.035$$

$$r_B^* = 0.135 \pm 0.051$$

$$r_s = 0.181^{+0.100}_{-0.118}$$

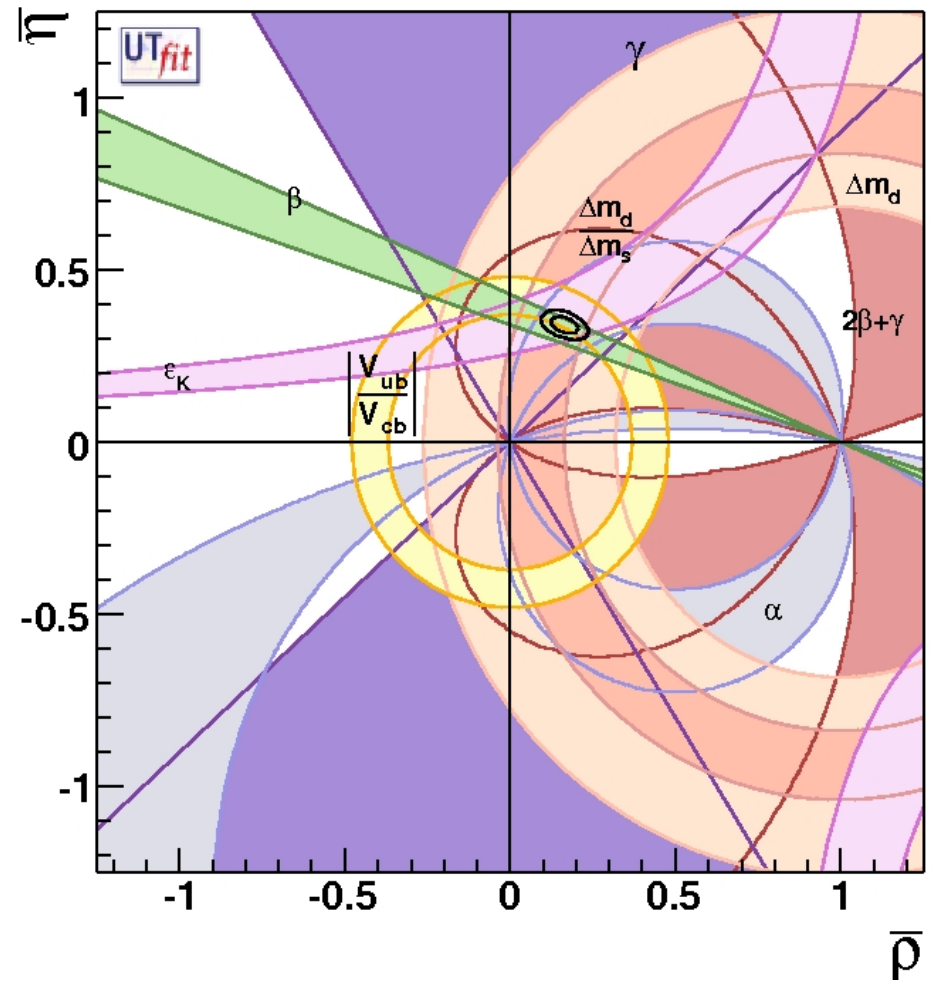
$$\gamma = (76 \pm 22 \pm 5 \pm 5)^\circ \pmod{180^\circ}$$

stat    syst    Dalitz



CPV significance:

$B \rightarrow DK$	$2.2\sigma$
$B \rightarrow D^*K$	$2.5\sigma$
$B \rightarrow DK^*$	$1.5\sigma$
combined	$3.0\sigma$

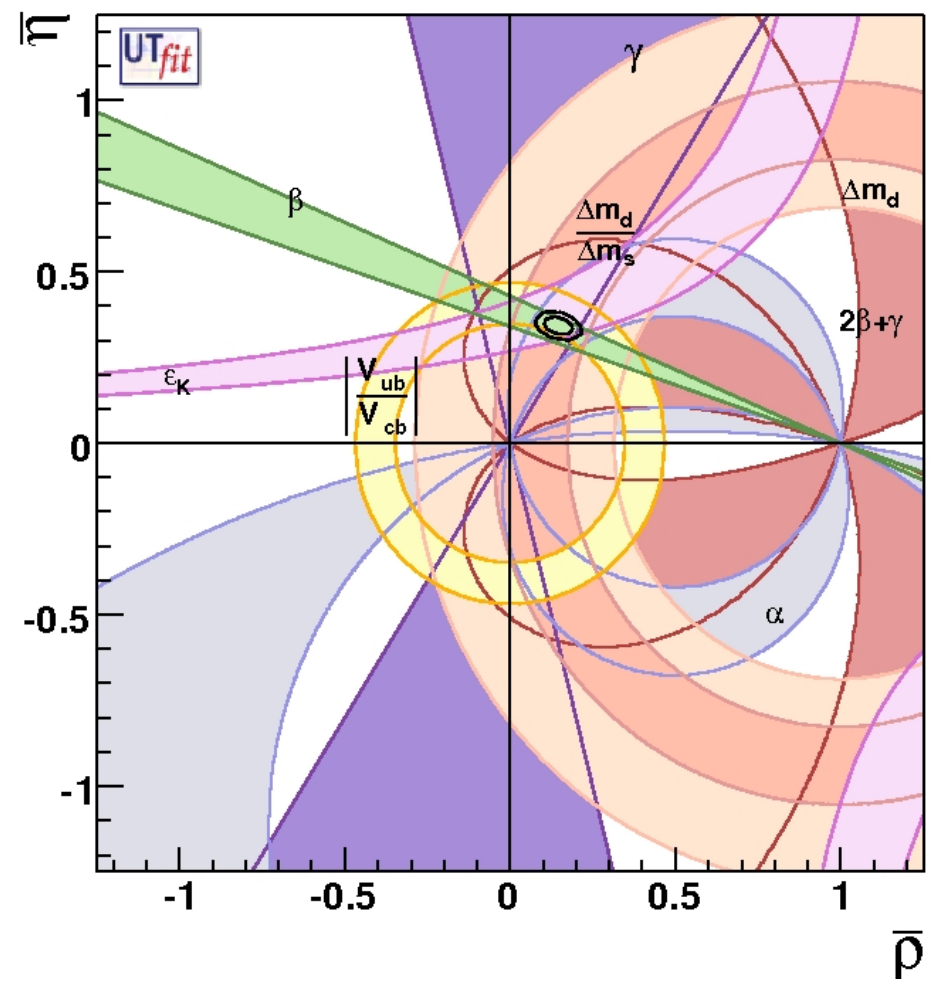


**UTfit**

before the 2008 Winter Conferences



## UTfit Moriond 08



combinations  
of direct measure-  
ments of the  
angles:

$\gamma = 80^\circ [+13 -13]^\circ$   
UTfit Moriond 08

$\alpha = 87.5^\circ [+6.2 -5.3]^\circ$   
CKMfitter  
LP/EPS 07

$\beta = 21.5^\circ [+1.0 -1.0]^\circ$   
CKMfitter  
LP/EPS 07

CKM angles

# summary

- BaBar has published many results on the CKM angles for the Winter conferences, some are covered in this presentation.
- **CKM  $\alpha$**  : Accessible in  **$B \rightarrow \pi\pi$**  (and higher resonances). But penguin contributions need to be controlled.  $\alpha = (96_{-6}^{+10})^\circ$
- **CKM  $\beta$**  : Precision measurements in the  **$B \rightarrow c\bar{c}s$**  system are available:  $\sin 2\beta = 0.714 \pm 0.032(\text{stat}) \pm 0.018(\text{syst})$
- **CKM  $\gamma$**  : Clean tree only environment in  **$B \rightarrow DK$** . GGSZ Dalitz method measures  $\gamma = (76 \pm 22 \pm 5 \pm 5)^\circ$

The datataking period of BaBar has ended by April 7th.

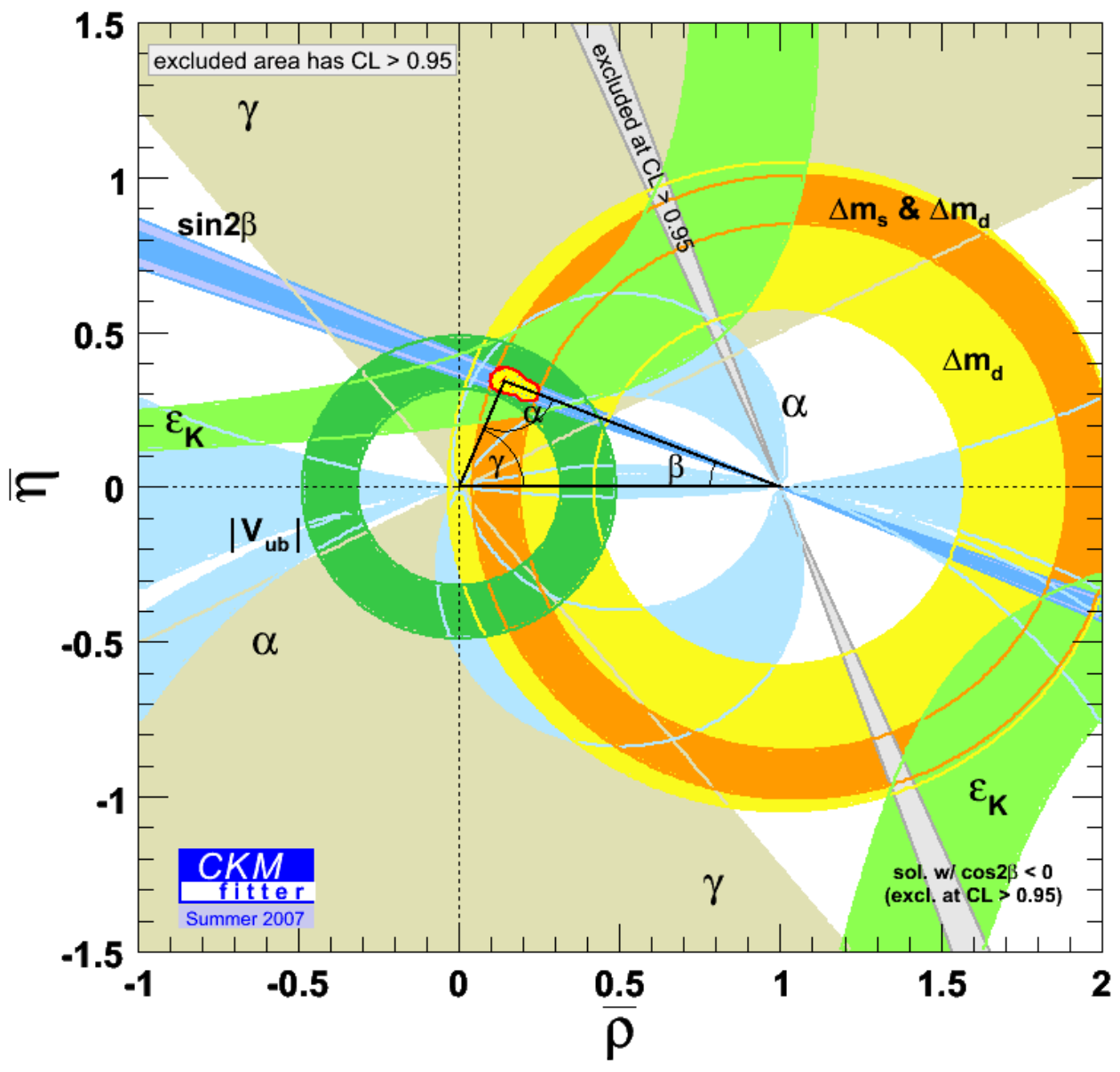
thanks to: Sören Prell, Viola Sordini,  
Cecilia Voena

[moritz.karbach@slac.stanford.edu](mailto:moritz.karbach@slac.stanford.edu)



backup







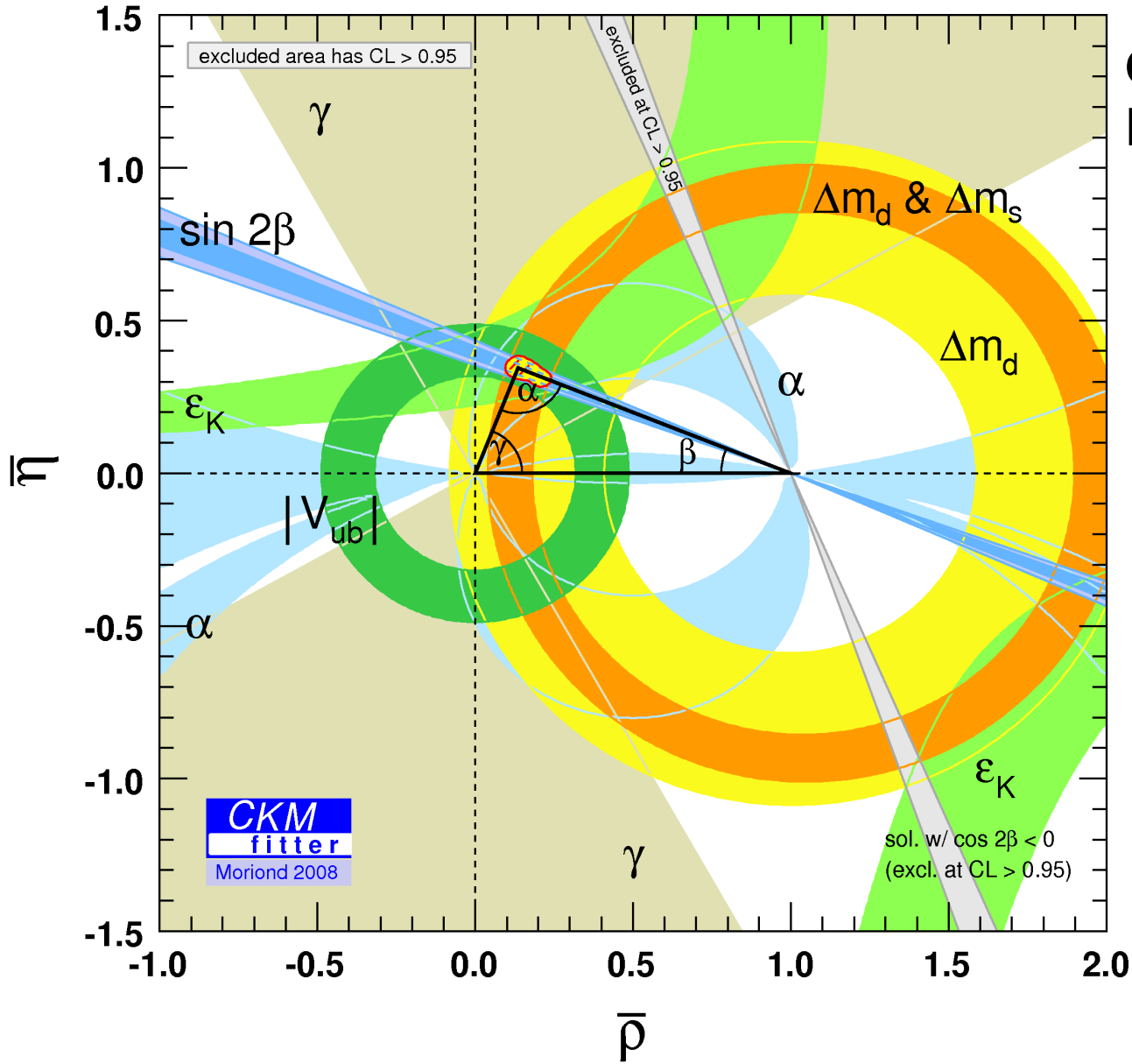
# CKMfitter

Moritz Karbach  
TU Dortmund

PHENO  
April 28<sup>th</sup> 2008



TM & © Nelvana



## CKMfitter Moriond 08

thanks to  
Stephane  
T'Jampens

CKM angles



CKMfitter Group (J. Charles et al.),  
Eur. Phys. J. C41, 1-131 (2005) [hep-ph/0406184],  
<http://ckmfitter.in2p3.fr>

# $\alpha$ from $B \rightarrow (\rho\pi)^0$

**375 · 10<sup>6</sup> BB**  
 July 2007  
 PRD76, 012004

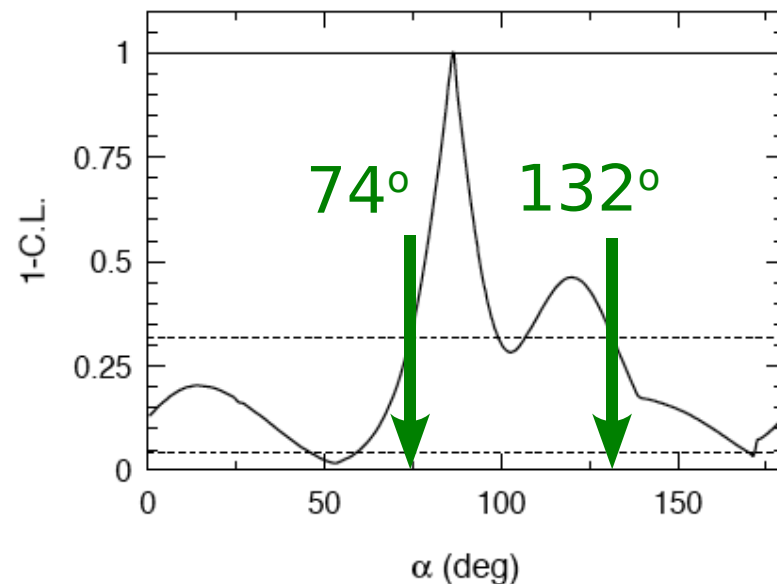
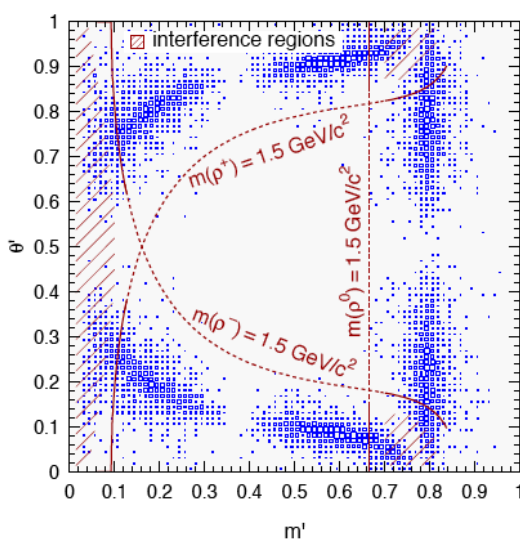
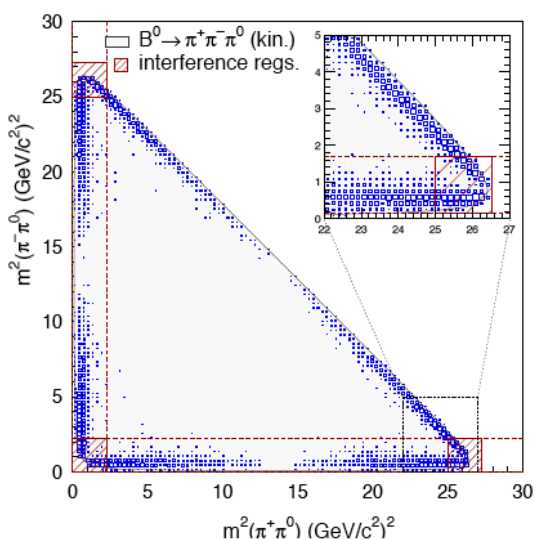
- full time-dependent Dalitz plot analysis of  $(\pi\pi\pi)^0$

$$f_{\pm}(\Delta t) \sim \frac{e^{-|\delta t|/\tau_B}}{4\tau_B} (1 \pm \eta_f S \sin(\Delta m_d \Delta t) - C \cos(\Delta m_d \Delta t))$$

- strong phases of the  $\rho$  vary over the dalitz plot – no isospin analysis needed to resolve ambiguities!
- fit for 26 form factor coefficients, combine them to  $S$ ,  $\Delta S$ ,  $C$ , ...

$$\delta_{+-} = (37 \pm 37)^\circ$$

$$\alpha = (87^{+45}_{-13})^\circ$$



# $\alpha$ from $B^0 \rightarrow \rho^+ \rho^-$ and $B^0 \rightarrow \rho^0 \rho^0$

**384 · 10<sup>6</sup> BB**  
July 2007  
PRD76, 052007

**427 · 10<sup>6</sup> BB**  
August 2007  
arxiv/0708.1630

- Vector-Vector final state is a mixture of CP even & odd states → angular analysis required ( $f_L, S_L, C_L$ )
- Flavor SU(3) analysis  
 $\alpha = [83.3, 105.8]^\circ$  @68% C.L.

- tracks in final state enable time-dependent analysis
- $BR(B \rightarrow \rho^0 \rho^0) < BR(B \rightarrow \pi^0 \pi^0)$  : isospin analysis more effective

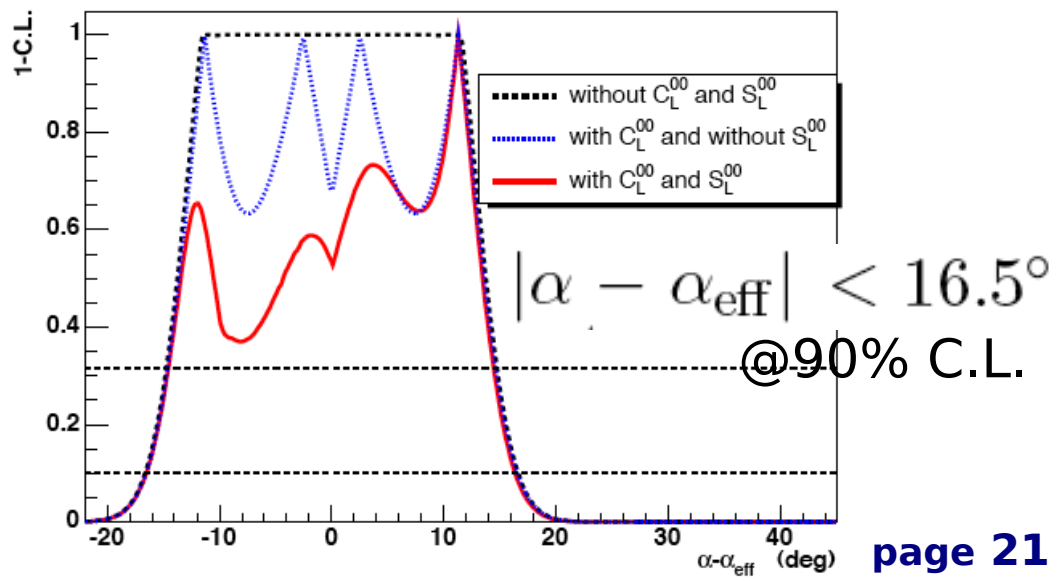
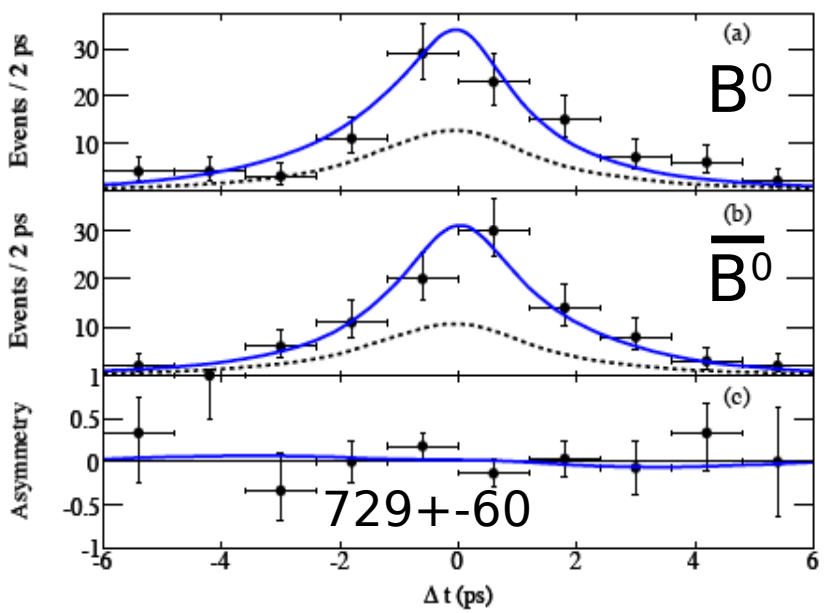
$$\mathcal{B}(B^0 \rightarrow \rho^+ \rho^-) = (25.5 \pm 2.1(\text{stat})_{-3.9}^{+3.6}(\text{syst})) \times 10^{-6}$$

$$S_L^{00} = 0.5 \pm 0.9 \pm 0.2$$

$$C_L^{00} = 0.4 \pm 0.9 \pm 0.2$$

$$f_L = 0.70 \pm 0.14 \pm 0.05$$

$$\mathcal{B} = (0.84 \pm 0.29 \pm 0.17) \times 10^{-6}$$



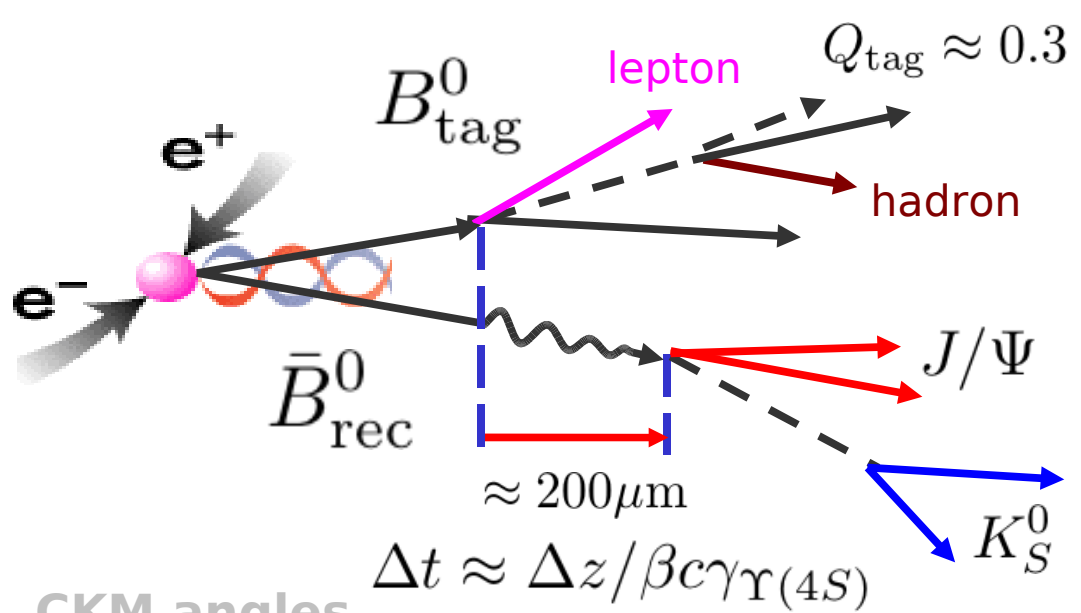
# $\beta$ from $B^0 \rightarrow c\bar{c}s$

**383 · 10<sup>6</sup> BB**  
 October 2007  
 PRL99, 171803



- this is a precision measurement  
 $J/\psi K_S^0, J/\psi K_L^0, \psi(2S)K_S^0, \chi_{c1}K_S^0, \eta_c K_S^0,$  and  $J/\psi K^{*0}$
- time dependent decay rate is governed by a sin (CPV in mixing) and cos (direct CPV) term
- in SM direct CPV and CPV in mixing are negligible in  $b \rightarrow c\bar{c}s$ . Easy access to  $\sin 2\beta$ :

$$A_{CP}(\Delta t) = -(1 - 2w)\eta_f \sin 2\beta \sin(\Delta m_d \Delta t)$$

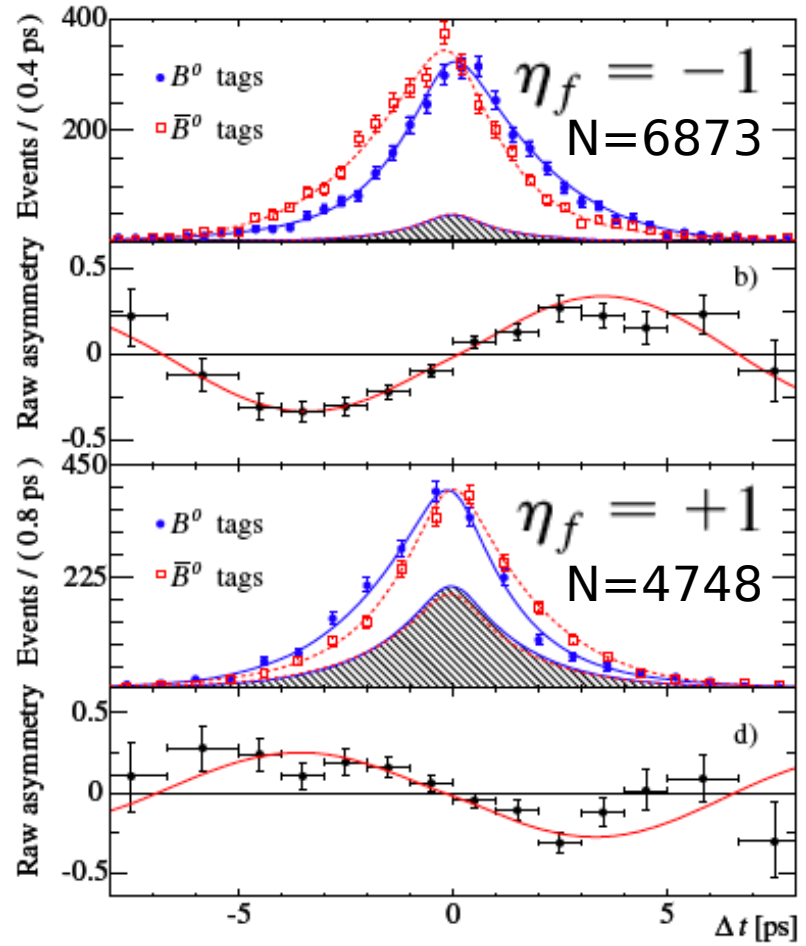


CKM angles

$$\lambda = (q/p)(\bar{A}/A)$$

$$\sin 2\beta = 0.714 \pm 0.032(\text{stat}) \pm 0.018(\text{syst})$$

$$|\lambda| = 0.952 \pm 0.022(\text{stat}) \pm 0.017(\text{syst})$$





# $\sin(2\beta+\gamma) : B^0 \rightarrow D_s^{(*)+} \pi^-, D_s^{(*)+} \rho^-, D_s^{(*)+} K^{*-}$

**381 · 10<sup>6</sup> BB**  
March 2008 **new!**  
arxiv:0803.4296

- There is theoretically clean sensitivity to  $\sin(2\beta+\gamma)$  from  $B^0 \rightarrow D^{(*)+} \pi^-$  and  $B^0 \rightarrow D^{(*)+} \rho^-$  decays.
- The method requires knowledge of  $r$ , ratio of interfering amplitudes. This is challenging because  $r$  is small in the  $D^{(*)+} \pi^-$  system:  $r \approx 0.02$
- Use flavor SU(3) to relate it to the

$D_s^{(*)+} \pi^-$  system:

$$r(D^{(*)} \pi) = \tan \theta_c \frac{f_{D^{(*)}}}{f_{D_s^{(*)}}} \sqrt{\frac{\mathcal{B}(B^0 \rightarrow D_s^{(*)+} \pi^-)}{\mathcal{B}(B^0 \rightarrow D^{(*)-} \pi^+)}}$$

$$r(D\pi) = [1.75 \pm 0.14 \text{ (stat)} \pm 0.09 \text{ (syst)} \pm 0.10 \text{ (th)}]\%$$

$$r(D^* \pi) = [1.81_{-0.14}^{+0.17} \text{ (stat)} \pm 0.12 \text{ (syst)} \pm 0.10 \text{ (th)}]\%$$

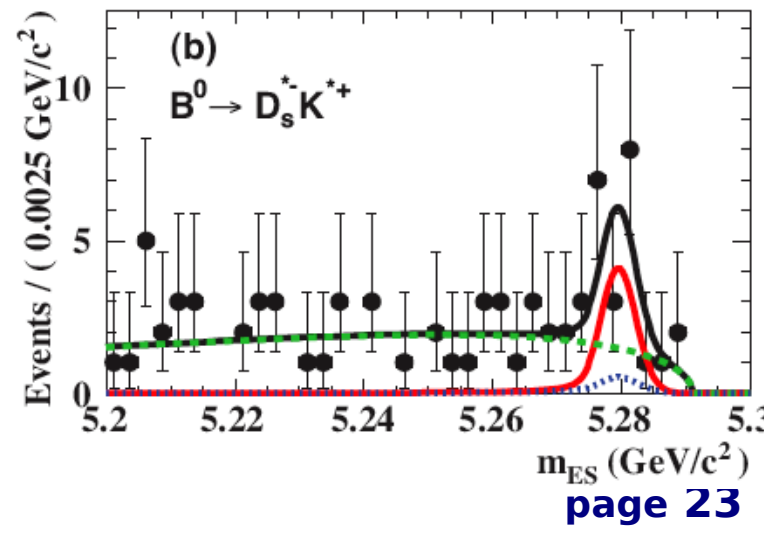
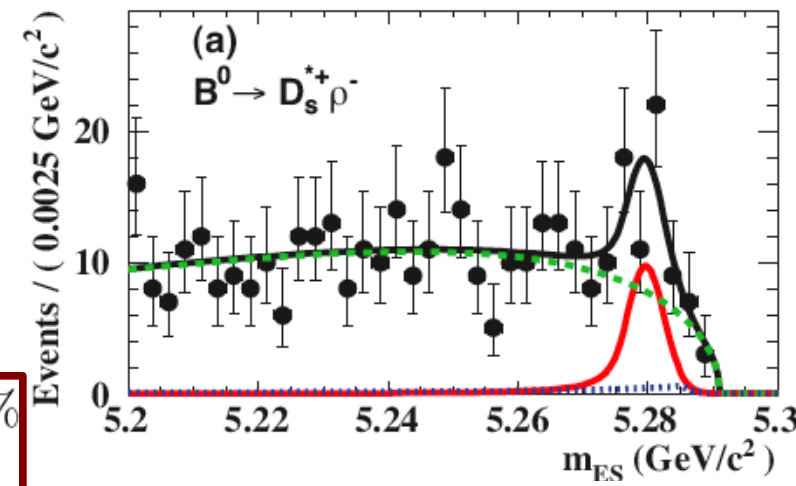
$$r(D\rho) = [0.71_{-0.26}^{+0.29} \text{ (stat)} \pm 0.11 \text{ (syst)} \pm 0.04 \text{ (th)}]\%$$

$$r(D^* \rho) = [1.50_{-0.21}^{+0.22} \text{ (stat)} \pm 0.16 \text{ (syst)} \pm 0.08 \text{ (th)}]\%$$

$$\mathcal{B}(B^0 \rightarrow D_s^{*+} \rho^-) = [4.4_{-1.2}^{+1.3} \pm 0.8] \times 10^{-5} \quad \mathbf{3.9\sigma}$$

$$\mathcal{B}(B^0 \rightarrow D_s^{*-} K^{*+}) = [3.0_{-1.2}^{+1.4} \pm 0.3] \times 10^{-5} \quad \mathbf{3.1\sigma}$$

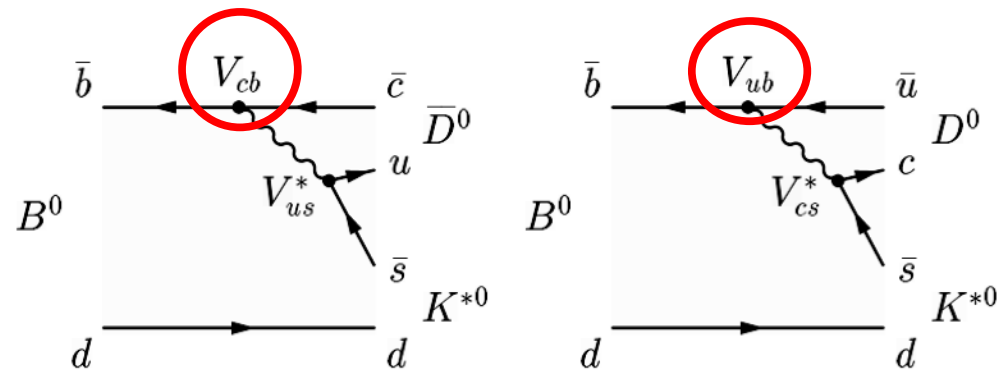
CKM angles



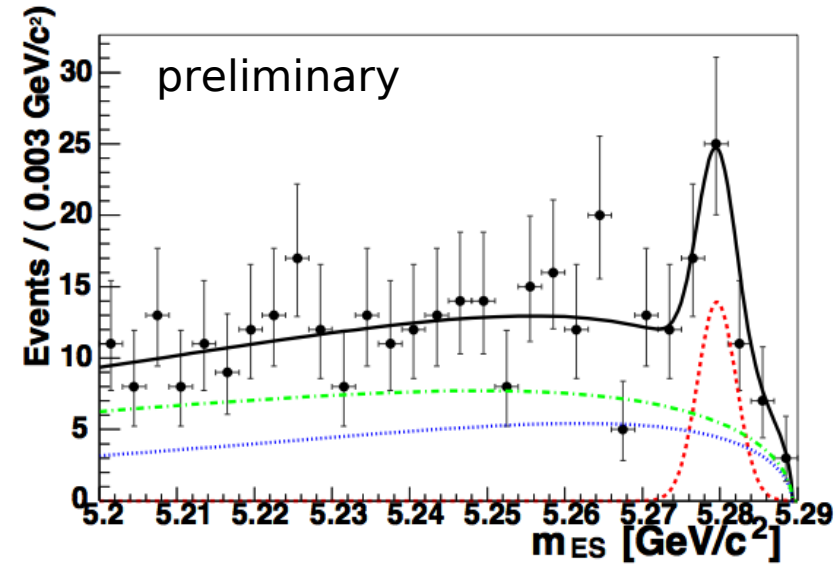
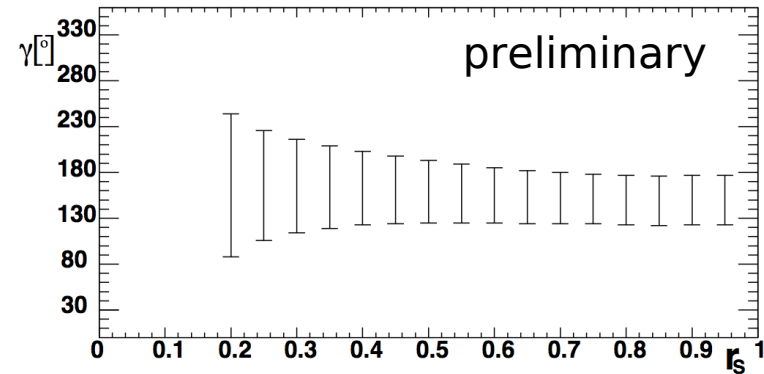
# $\gamma$ from $B^0 \rightarrow D^0 K^{*0}$ with $D^0 \rightarrow K^0 \pi^+ \pi^-$

**371 · 10<sup>6</sup> BB**  
 April 2008  
**preliminary**

- Novel technique! Works similar to the GGSZ Dalitz method. Same CKM elements are involved.
- The charge of the K from the  $K^{*0}$  decay tags the B flavor – no time dependent analysis needed.
- At current statistics,  $r_S = [0.3, 0.5]$  needs to be plugged in from external studies to obtain limits on  $\gamma$



preliminary  
 $\gamma = (162 \pm 56)^\circ$  or  $(342 \pm 56)^\circ$ ;  
 $\delta_S = (62 \pm 57)^\circ$  or  $(242 \pm 57)^\circ$ ;  
 $r_S < 0.55$  at 95% probability.





# $\sin(2\beta) : b \rightarrow s$ penguins

- Most theorists expect  $S(b \rightarrow sss) - S(b \rightarrow ccs) > 0$
- Most experiments measure  $\Delta S < 0$
- HFAG averages need to be taken with great care. For instance,  $S(f^0 K_S)$  from  $K_S \pi^- \pi^+$  Dalitz analysis has highly non-gaussian errors
- $K_S \pi^- \pi^+$  is in the process of publication. arxiv:0708.2097
- most BaBar measurements use 380M BB pairs – updates are expected.

$$\sin(2\beta^{\text{eff}}) \equiv \sin(2\phi_1^{\text{eff}})$$

