

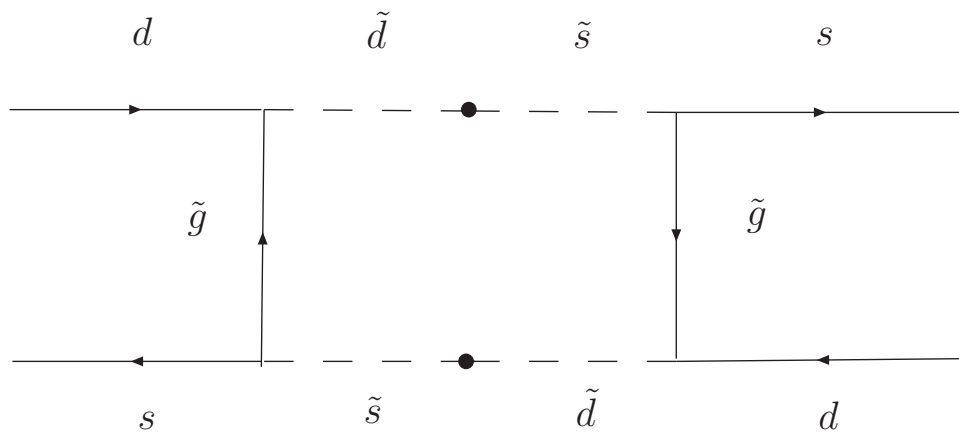
Outline

- SUSY Flavor Problem
- Motivation
- Model
- Predictions
- Summary and Conclusions

SUSY Flavor Problem

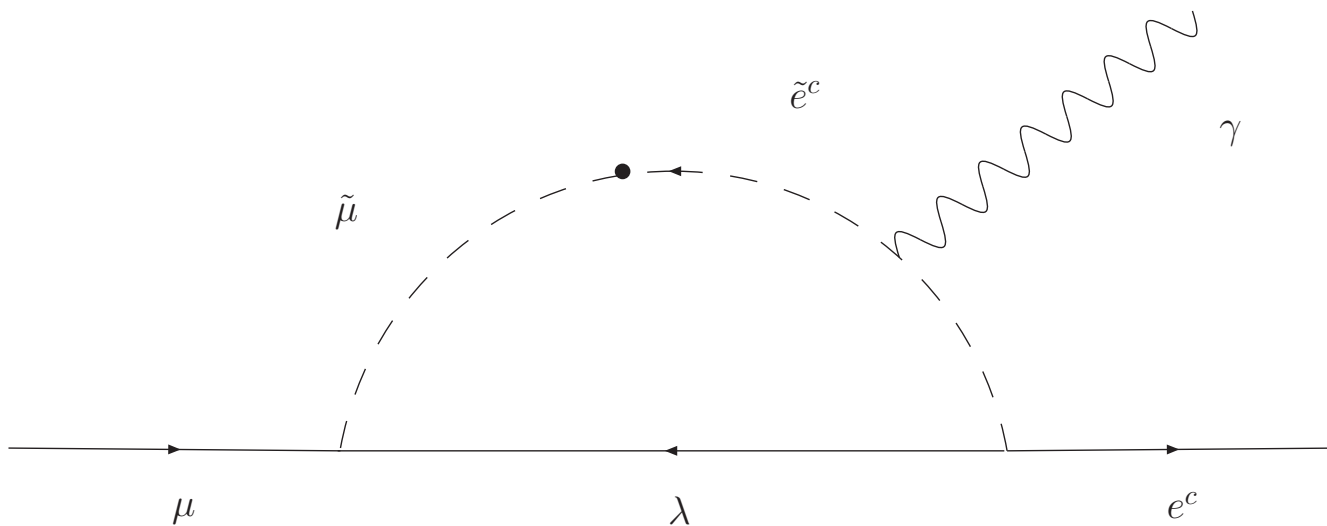
- Strongest constraint from $K^0 - \overline{K^0}$ mixing: $\Delta_{\tilde{d}\tilde{s}}/m_{sq}^2 < 10^{-4}$
- Solved by assuming universality:

$$m_{\tilde{d}\tilde{s}}^2 = \begin{pmatrix} m_1^2 & 0 \\ 0 & m_1^2 \end{pmatrix}$$



- Constraint from $\mu \rightarrow e\gamma$: $\Delta_{\tilde{e}\tilde{\mu}}/m_{sl}^2 < 10^{-3}$
- It's similarly assumed:

$$m_{\tilde{e}\tilde{\mu}}^2 = \begin{pmatrix} m_2^2 & 0 \\ 0 & m_2^2 \end{pmatrix}$$



Motivation

- It has been pointed out that the form

$$\begin{pmatrix} 0 & A & 0 \\ -A & 0 & B' \\ 0 & B & C \end{pmatrix}$$

for fermion mass matrices is consistent with phenomenology (Weinberg; Wilczek and Zee; Fritzsch)

- Factorizable Form (phases of A, B, B', C can be absorbed into fermion fields)

⇒ We wish to obtain this with some symmetry

- Consider symmetry with 3 families belonging to $2 + 1$

- $(\tilde{d}, \tilde{s}), (\tilde{e}, \tilde{\mu})$ in same multiplets \implies Explains mass degeneracy
- To generate fermion masses use $2 + 1$ pairs of Higgs doublets: $(H_1^{u,d}, H_2^{u,d}) + H_3^{u,d}$
- For $2 + 1$ of $SU(2)$, fermion mass matrices have form

$$\begin{pmatrix} 0 & y_1 H_3 & y_2' H_2 \\ -y_1 H_3 & 0 & -y_2' H_1 \\ y_2 H_2 & -y_2 H_1 & y_3 H_3 \end{pmatrix}$$

- If $\langle H_1^u \rangle / \langle H_2^u \rangle = \langle H_1^d \rangle / \langle H_2^d \rangle$, 13 and 31 entries can be rotated away

- If full (local) $SU(2)$, D -terms cause FCNC problems \implies Discrete subgroups of $SU(2)$
- The Higgs mass matrix ($W = H_i^u M_{ij} H_j^d$)

$$M = \begin{pmatrix} 0 & a & cb_1 \\ -a & 0 & cb_2 \\ b_1 & b_2 & 0 \end{pmatrix}$$

can give large masses to all but one pair of doublets ("doublet-doublet splitting") \implies MSSM at low energy

$$H^u = \frac{b_2^* H_1^u - b_1^* H_2^u - a^* H_3^u}{\sqrt{|b_1|^2 + |b_2|^2 + |a|^2}}, \quad H^d = \frac{c^* b_2^* H_1^d - c^* b_1^* H_2^d + a^* H_3^d}{\sqrt{|c|^2 |b_1|^2 + |c|^2 |b_2|^2 + |a|^2}}$$

Fermion Mass Matrices:

$$\frac{H^u}{\sqrt{|b_1|^2 + |b_2|^2 + |a|^2}} \begin{pmatrix} 0 & A_u a & B'_u b_1 \\ -A_u a & 0 & B'_u b_2 \\ B_u b_1 & B_u b_2 & C_u a \end{pmatrix},$$

$$\frac{H^d}{\sqrt{|c|^2|b_1|^2 + |c|^2|b_2|^2 + |a|^2}} \begin{pmatrix} 0 & A_d a & B'_d c b_1 \\ -A_d a & 0 & B'_d c b_2 \\ B_d c b_1 & B_d c b_2 & C_d a \end{pmatrix}$$

- 13,31 entries can be rotated away
- For real Yukawas, only complex c gives CP violation

The Group T'

- T' is the double covering of A_4
- Only subgroup of $SU(2)$ with doublets that are not self-conjugate
- Smallest subgroup of $SU(2)$ under which 3 does not break up

Representations of T' :

- true singlet, 1
- conjugate pair of singlets, $1', 1''$
- real triplet, 3
- pseudoreal doublet, 2
- conjugate pair of doublets, $2', 2''$

$T' \times Z_6$ Model

$SU(2)_L$ Doublets:

$$H^u, H^d : (2', \omega); H_3^u, H_3^d : (1', \omega); H'^u, H'^d : (2, \omega^2);$$
$$H_3'^u, H_3'^d : (1', -\omega^2); H_3''^u : (1'', -\omega); H_3''^d : (1'', -\omega^2);$$
$$Q : (2', \omega); Q_3 : (1', \omega)$$

$SU(2)_L$ Singlets:

$$T : (3, 1); D : (2', -1); D' : (2'', -1); S_1 : (1, \omega^2);$$
$$S_2 : (1, \omega); S_3 : (1, -\omega); S_4 : (1, -\omega^2); S_5 : (1, -1);$$
$$Q^c : (2', \omega); Q_3^c : (1', \omega)$$

- $\omega = e^{i\frac{2\pi}{3}}$
- Assignment commutes with $SO(10)$ Grand Unification

Superpotential for SM Singlet Higgs:

$$\begin{aligned} W = & a_1 D D' + a_2 T^2 + b_1 T^3 + b_2 D^2 T + b_3 D'^2 T + b_4 D D' T \\ & + a_3 S_1 S_2 + a_4 S_3 S_4 + a_5 S_5^2 + b_5 S_1^3 + b_6 S_2^3 + b_7 S_2 S_3^2 \\ & + b_8 S_1 S_4^2 + b_9 S_1 S_3 S_5 + b_{10} S_2 S_4 S_5 \end{aligned}$$

- Can generate VEV's for all fields
- No flat directions or accidental symmetries

Higgs Doublet Mass Matrix:

$$\begin{pmatrix}
 0 & 0 & 0 & \beta(T_1 - i\omega^2 T_2) & -\beta\omega T_3 & \delta D_2 & 0 \\
 0 & 0 & 0 & -\beta\omega T_3 & -\beta(T_1 + i\omega^2 T_2) & -\delta D_1 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & \zeta S_3 \\
 \alpha(T_1 - i\omega^2 T_2) & -\alpha\omega T_3 & 0 & 0 & \lambda S_1 & 0 & 0 \\
 -\alpha\omega T_3 & -\alpha(T_1 + i\omega^2 T_2) & 0 & -\lambda S_1 & 0 & 0 & 0 \\
 \gamma D_2 & -\gamma D_1 & 0 & 0 & 0 & 0 & \xi S_2 \\
 0 & 0 & \epsilon S_2 & 0 & 0 & m & 0
 \end{pmatrix}$$

Integrating out $H'^{u,d}$, $H_3'^{u,d}$, $H_3''^{u,d}$:

$$\begin{pmatrix} 0 & a & cb_1 \\ -a & 0 & cb_2 \\ b_1 & b_2 & 0 \end{pmatrix}$$

$$a = \frac{\alpha\beta}{\lambda} \frac{\langle T^2 \rangle}{\langle S_1 \rangle}, \quad b_1 = \frac{\gamma\zeta}{\xi} \frac{\langle S_3 D_2 \rangle}{\langle S_2 \rangle}, \quad b_2 = -\frac{\gamma\zeta}{\xi} \frac{\langle S_3 D_1 \rangle}{\langle S_2 \rangle}, \quad c = \frac{\delta\epsilon\xi}{\gamma\zeta} \frac{\langle S_2^2 \rangle}{\langle S_3 \rangle}$$

- Light modes couple to SM singlet Higgs, $H^u H^d \Phi$, with $\langle \Phi \rangle = 0$ in SUSY limit
- After SUSY breaking $\langle \Phi \rangle \sim M_{SUSY}$

- c complex \implies spontaneous CP violation
- Complex B_μ -parameter generated \implies SUSY CP problem not fully solved
- Discrete symmetries should come from broken local symmetries so that they are respected by gravity
- When $SU(2)$ reps. break up under T' , $1'$, $1''$ and $2'$, $2''$ always occur in pairs \implies This model can be difficult to obtain from a local symmetry (e.g. $4 \rightarrow 2' + 2''$, $5 \rightarrow 3 + 1' + 1''$, $6 \rightarrow 2 + 2' + 2''$)
- By extending the Abelian part of the symmetry, the model can be altered to use only complete multiplets of $SU(2)$

$T' \times Z_3 \times Z_6$ Model

$SU(2)_L$ Doublets:

$$\begin{aligned} H^u, H^d &: (2, \omega, \omega); & H_3^u, H_3^d &: (1, \omega, \omega); & H'^u, H'^d &: (2, 1, \omega^2); \\ H_3'^u, H_3'^d &: (1, \omega, -\omega^2); & H_3''^u &: (1, \omega^2, -\omega); & H_3''^d &: (1, \omega^2, -\omega^2); \\ Q &: (2, \omega, \omega); & Q_3 &: (1, \omega, \omega) \end{aligned}$$

$SU(2)_L$ Singlets:

$$\begin{aligned} T &: (3, \omega, 1); & T' &: (3, \omega^2, 1); & D &: (2, \omega, -1); & D' &: (2, \omega^2, -1); \\ S_1 &: (1, 1, \omega^2); & S_2 &: (1, 1, \omega); & S_3 &: (1, 1, -\omega); & S_4 &: (1, 1, -\omega^2); \\ S_5 &: (1, 1, -1); & Q^c &: (2, \omega, \omega); & Q_3^c &: (1, \omega, \omega) \end{aligned}$$

- $SU(2)$ can be broken to T' with a 7

Predictions

- Mass matrix forms with spontaneous CP violation:

$$M_d = \begin{pmatrix} 0 & A_d & 0 \\ -A_d & 0 & B'_d \\ 0 & B_d & C_d \end{pmatrix}, M_u = \begin{pmatrix} 0 & A_u & 0 \\ -A_u & 0 & B'_u e^{i\phi} \\ 0 & B_u e^{i\phi} & C_u \end{pmatrix}$$

Small Mixing ($C_u, C_d \gg B_u, B_d, B'_u, B'_d \gg A_u, A_d$):

- $|V_{ub}/V_{cb}| = \sqrt{m_u/m_c}$
- Assuming known quark masses: $0.15 < \theta_C < 0.29$

Large Mixing ($C_u, C_d \sim B_u, B_d \gg B'_u, B'_d \gg A_u, A_d$):

- $\theta_C \simeq^{m_d/m_s} \left[1 - \frac{1}{4} \left(\frac{m_s/m_b}{|V_{cb}|} \right)^2 \right]$

Summary

A Model with the following properties:

- MSSM at low energy
- Solves SUSY flavor problem
- Ameliorates SUSY CP problem
- Solves μ problem
- Consistent with Grand Unification