

VBFNLO

Robin Roth | 25.08.2016

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INSTITUTE FOR THEORETICAL PHYSICS



Goal

- test the Standard Model (SM) at the LHC with the highest possible precision
- look for deviations from the SM in a model independent way
- focus on processes with electroweak bosons

Methods

- more precise SM prediction, reduced theory error \Rightarrow NLO, \tilde{n} NLO, NLO+PS
- parametrize beyond-SM effects \Rightarrow Anomalous Couplings (AC) / EFT
- improve analyses \Rightarrow better cuts and observables, dynamical jet veto

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\Rightarrow VBFNLO

- 1 Overview and Features
- 2 BLHA Interface, Herwig 7
- 3 Anomalous Couplings
- 4 Loopsim / AC at \bar{n} NLO QCD
- 5 WZ production with a dynamical jet veto

Vector-Boson-Fusion at Next-to-Leading Order

Scattering, Diboson, Triboson, additional Jets
Vector-Boson-Fusion at Next-to-Leading Order

F
Physics
Vector-Boson-Fusion at Next-to-Leading Order

F Physics

Vector-Boson-Fusion at Next-to-Leading Order

[0811.4559, 1107.4038, 1404.3940]

- Fully flexible parton-level Monte Carlo for processes with electroweak bosons
 - accurate predictions for LHC physics
(both signal and background)
 - efficient for large number of final-state particles
(decays/off-shell effects of electroweak bosons included)
- anomalous couplings for many processes
- general cuts and distributions of final-state particles
- various choices for (dynamical) renormalization and factorization scales
- pdf set via LHAPDF
(or CTEQ6L1, CT10, MRST2004qed, MSTW2008 shipped with release)
- event files in Les Houches Accord (LHA) or HepMC format (**LO only**)
- [BLHA interface](#) to Monte-Carlo event generators
→ **NLO** event output

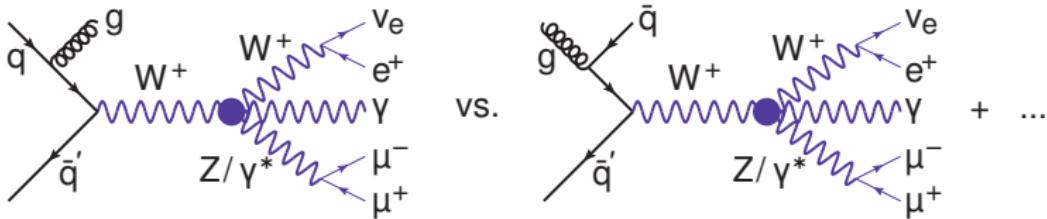
Overview of implemented processes

(New in VBFNLO 2.7.1/3.0.0 β 2)

- vector-boson fusion production at NLO QCD of
 - Higgs (+NLO EW, NLO SUSY)
 - Higgs plus third hard jet
 - Higgs plus photon
 - Higgs pair
- vector boson (W, Z, γ)
- two vector bosons (W^+W^- , $W^\pm W^\pm$, WZ , ZZ , $W\gamma$, $Z\gamma$)
- diboson production
 - diboson (WW , WZ , ZZ , $W\gamma$, $Z\gamma$, $\gamma\gamma$) (NLO QCD)
 - diboson via gluon fusion (WW , ZZ , $Z\gamma$, $\gamma\gamma$) (part of NNLO QCD contribution to diboson)
 - diboson (WW , WZ , ZZ , $W\gamma$) plus hard jet (NLO QCD)
 - diboson ($W^\pm W^\pm$, WZ , $W\gamma$, ZZ , $Z\gamma$) plus two hard jets (NLO QCD)
- triboson production (NLO QCD)
 - triboson (all combinations of W, Z, γ)
 - triboson ($W\gamma\gamma$) plus hard jet
- Higgs plus vector boson (NLO QCD) (including Higgs decays)
 - Higgs plus vector boson (WH)
 - Higgs plus vector boson plus hard jet (WH)
- Higgs plus two jets via gluon fusion (one-loop LO) (including Higgs decays)
- new physics models
 - anomalous Higgs, triple and quartic gauge couplings
 - K-matrix unitarization for selected couplings
 - Higgsless and spin-2 models
 - Two-Higgs model
- BLHA interface for VBF processes

Implementation Details

- Helicity amplitude method [Hagiwara, Zeppenfeld]
- Same building blocks for different Feynman graphs
 - Compute only once per phase-space point and reuse ("leptonic tensors")
 - Significantly faster than generated code (up to factor 10)
 - Easy extension for anomalous couplings



- Catani-Seymour dipole subtraction scheme

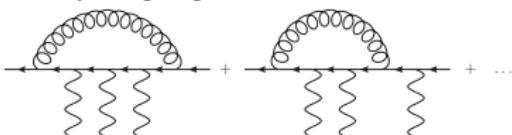
$$\sigma_{\text{NLO}} = \underbrace{\int_{m+1} [d\sigma^R|_{\epsilon=0} - d\sigma^A|_{\epsilon=0}]}_{\text{real emission}} + \underbrace{\int_m [d\sigma^V + \int_1 d\sigma^A]_{\epsilon=0}}_{\text{virtual contributions}} + \underbrace{\int_m d\sigma^C}_{\text{finite collinear term}}$$

Gauge Test

Tensor reduction of loop integrals using (-4: [Passarino, Veltman]; 5+: [Denner, Dittmaier])

→ numerical precision **limited** due to possibly small Gram determinants

- Identify → gauge test



replace one vector boson by corresponding momentum
(cache system for loop integrals
→ no reevaluation needed)

$$p_i^\mu \mathcal{M}_\mu^n(\{p\}; p_{i-1}, p_i, p_{i+1}) = \mathcal{M}^{n-1}(\{p\}; p_{i-1}, p_i + p_{i+1}) - \mathcal{M}^{n-1}(\{p\}; p_{i-1} + p_i, p_{i+1})$$

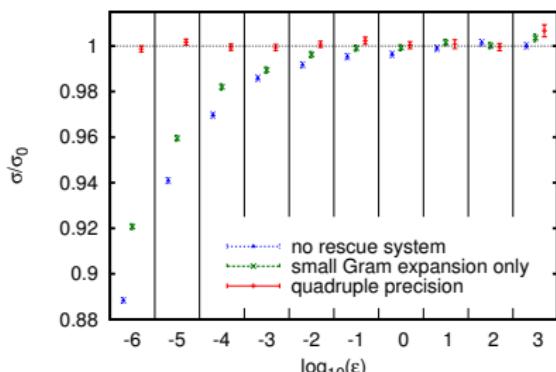
- Repair

→ rescue system (small Gram det. expansion) → quad precision → discard

[Impl: Campanario]

Example: $gg \rightarrow ZZg$

[Campanario, Li, Rauch, Spira]



ϵ : go to next step if $\frac{\Delta(p_i^\mu \mathcal{M}_\mu^n)}{\varepsilon_i^\mu \mathcal{M}_\mu^n} > \epsilon$

strong and efficient test of accuracy of building blocks

number of unstable points reduced to 10^{-6} level
additional CPU cost $\sim 10\%$

Standardized interface between Monte Carlo tools and one-loop programs
→ [Binoth Les Houches Accord \(BLHA\)](#)

[1001.1307, 1308.3462]

NLO calculation

- normalization correct to NLO
- additional jet at high- p_T accurately described
- theoretical uncertainty reduced

Parton Shower

- Sudakov suppression at small p_T
- events at hadron level possible

⇒ Combine advantages of NLO calculations and parton shower

- tree-level evaluation of matrix elements well under control
- modular structure of NLO calculations
- algorithms for treatment of infrared singularities (Catani-Seymour, FKS, ...)
- → incorporate one-loop matrix element information into MC tools

⇒ Matchbox module in Herwig7

[work led by S. Plätzer with substantial contributions by J. Bellm, A. Wilcock, M. Rauch, C. Reuschle]

One-loop provider (OLP)

- one-loop matrix elements
 $2\Re(\mathcal{M}_{\text{LO}}^\dagger \mathcal{M}_{\text{virt}})$ (coefficients of $\epsilon^{-2}, \epsilon^{-1}, \epsilon^0; |\mathcal{M}_{\text{LO}}|^2$)
- Born, colour- and spin-correlated Born (only BLHA2)

Monte Carlo Tool

- cuts, histograms, parameters
- Monte Carlo integration
- phase space (\rightarrow VBFNLO)
- IR subtraction
- Born, colour- and spin-correlated Born (only BLHA1)

VBFNLO

- VBF/VBS processes at NLO QCD [see also Jäger et al. (POWHEG-BOX VBF)]
 \rightarrow other processes in preparation
 - Anomalous Couplings
-
- Setup stage via “contract” file (needed for tools which generate code on the fly)
 - Run-time stage via binary interface (function calls) \rightarrow fast

Herwig7

- **Two parton showers:**
angular-ordered
Catani-Seymour dipoles
- **Two matching methods:**
MC@NLO and POWHEG

- events at NLO

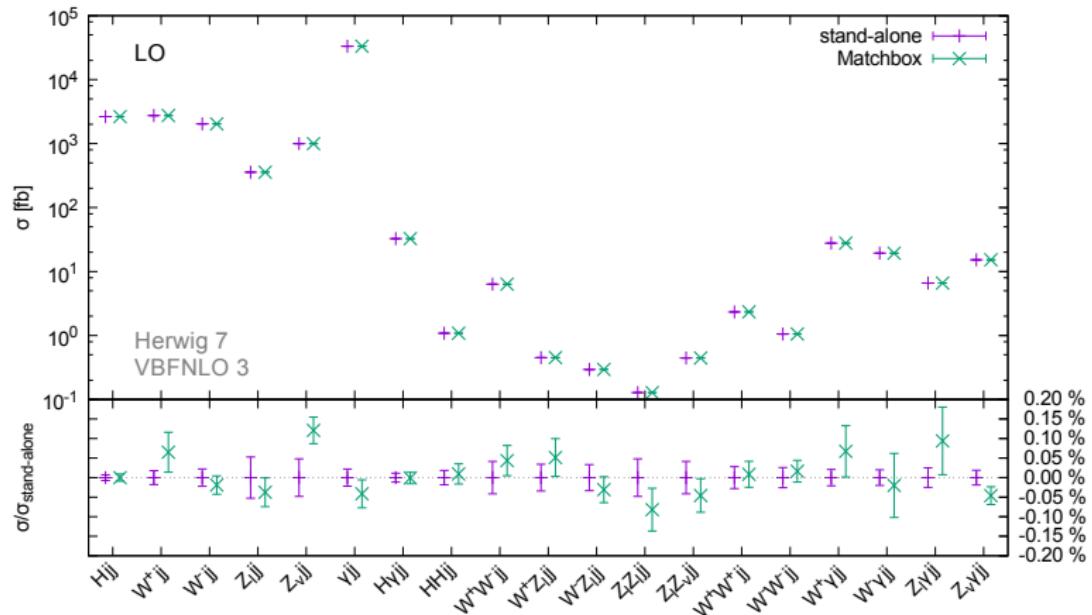
```
HepMC::Version 2.06.08
HepMC::IO_GenEvent--START_EVENT_LISTING
E 1 -1 1.000000000000000e+02 1.1426144356896106e-01 8.0545791941901580e-03 0 -1 5 10003 10006 0
1 9.6574119350375395e-05
N 1 "0"
U GEV MM
C 1.2003526218804084e+00 1.2429340593057579e+04
F 2 -2 1.9944966561722052e-01 5.475280981600089e-03 1.000000000000000e+02 4.8837107666330770e
-01 7.0773553098927189e-01 0 0
V -1 0 0 0 0 0 2 0
P 10001 24 -4.5106124574613865e+01 2.1914561871288999e+01 4.8707785224913533e+02
4.8305712963914090e+02 -8.0096530215583300e+01 11 0 0 -5 0
[...]
```

- anomalous couplings including available unitarization schemes
- BLHA interface completely following Les Houches standard
 - also working with other MC generators (e.g. Sherpa)
 - ↔ when using BLHA v1 with VBF processes, care needs to be taken to use the VBF approximation
 - also in the MC generator
- other process classes will follow (e.g. QCD-VV + 0,1,2 jets)

Validation

Compare LO results between VBFNLO stand-alone run and interfaced to Herwig 7 via Matchbox

(inclusive cuts, with leptonic gauge boson decays into single different-flavour combination, Higgs non-decaying)

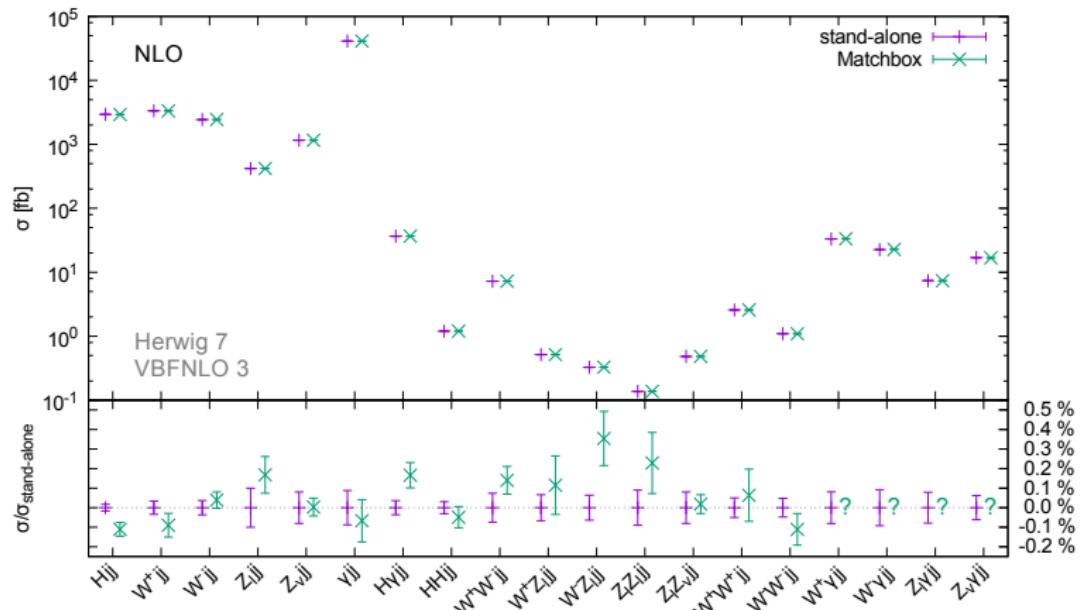


→ good agreement at or below permill level

Validation

Compare NLO results between VBFNLO stand-alone run and
interfaced to Herwig 7 via Matchbox

(inclusive cuts, with leptonic gauge boson decays into single different-flavour combination, Higgs non-decaying)



→ good agreement

discrepancy in $V\gamma$ processes: $\pm 0.7\%$ deviation → under investigation

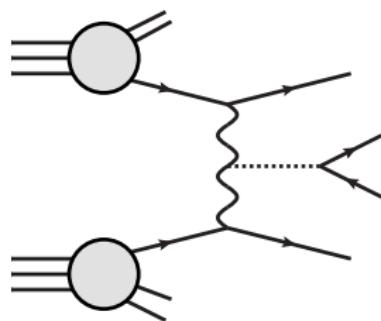
VBF event topology

VBF (vector-boson fusion) topology shows distinct signature

- two tagging jets in forward region
 - reduced jet activity in central region
 - leptonic decay products typically between tagging jets
- two-sided DIS

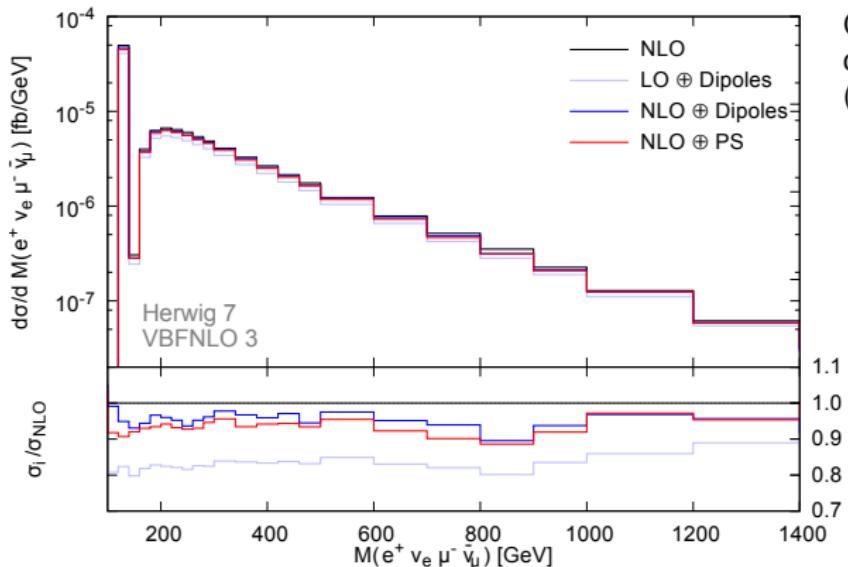
First studied in context of Higgs searches [Han, Valencia, Willenbrock; Figy, Oleari, Zeppenfeld; ...]

- $\sim 10\%$ compared to main production mode gluon fusion
- NLO QCD corrections moderate ($\mathcal{O}(\lesssim 10\%)$)
- NLO EW same size, opposite sign as QCD for $M_H \sim 126$ GeV
[Ciccolini *et al.*, Figy *et al.*]
- NNLO QCD known for subsets:
no significant contributions for integrated c.s.
[Harlander *et al.*, Bolzoni *et al.*]
corrections up to 10% in distributions
[Cacciari *et al.*]
- incl. NNNLO QCD: tiny effects [Dreyer, Karlberg]
- advantageous scale choice:
momentum transfer q^2 of intermediate vector bosons



VBF-H NLO+PS Distributions

$pp \rightarrow ((Hjj \rightarrow) W^+ W^- jj \rightarrow) e^+ \nu_e \mu^- \bar{\nu}_\mu jj$ via VBF
comparing Dipole shower and angular ordered matched to NLO parton shower



Cuts inspired from ATLAS VBF category in $H \rightarrow WW$
(CMS similar)

$$p_{T,j} > 30 \text{ GeV},$$

$$|y_j| < 4.5,$$

$$\text{anti-}k_T R = 0.4, b \text{ veto}$$

$$p_{T,\ell} > 20 \text{ GeV},$$

$$|y_\ell| < 2.5,$$

$$m_{e^+, \mu^-} > 15 \text{ GeV}$$

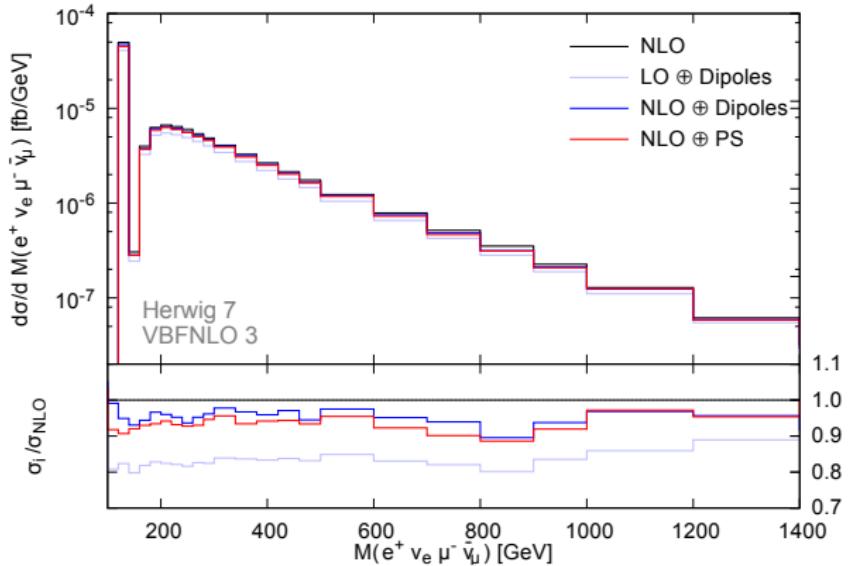
$$m_{j_1, j_2} > 600 \text{ GeV},$$

$$|y_{j1} - y_{j2}| > 3.6$$

PDF: MMHT2014 $\mu_0 = p_{T,j1}$

VBF-H NLO+PS Distributions

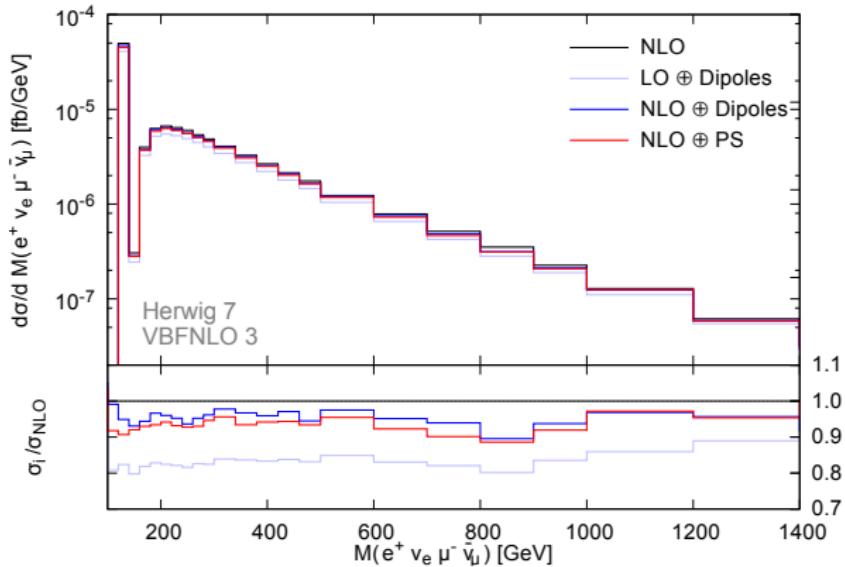
$pp \rightarrow ((Hjj \rightarrow) W^+ W^- jj \rightarrow) e^+ \nu_e \mu^- \bar{\nu}_\mu jj$ via VBF
comparing Dipole shower and angular ordered matched to NLO parton shower



- Higgs peak at 125 GeV
 - WW continuum production above 180 GeV
 - significant cancellation between diagrams at high invariant masses
 - $\mathcal{M}_{4\text{-vertex only}} \propto M_{4\ell}^4$
 - $\mathcal{M}_{\text{Higgs}} \propto M_{4\ell}^2$
 - $\mathcal{M}_{\text{tot}} \propto \text{const.}$
- ⇒ ideal test for anomalous couplings

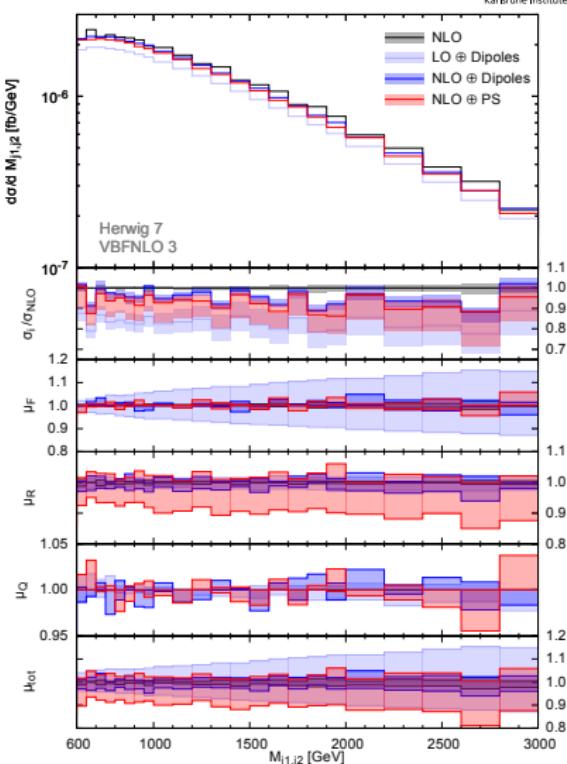
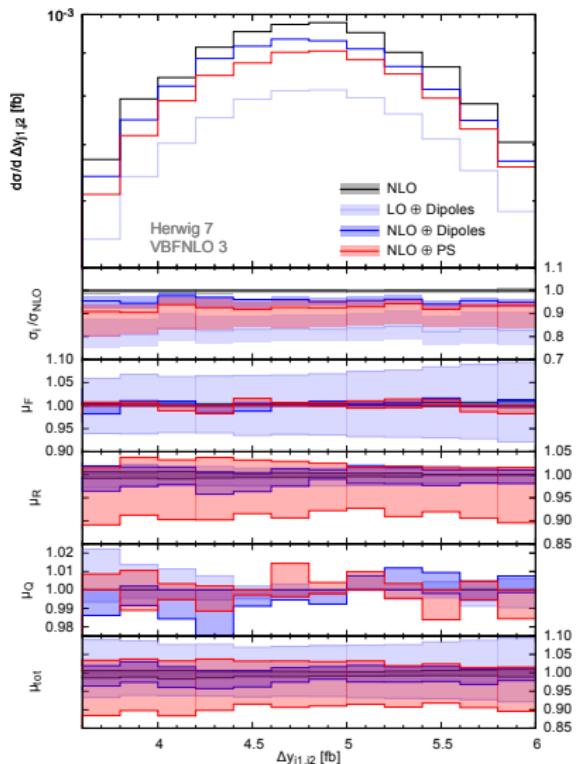
VBF-H NLO+PS Distributions

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comparing Dipole shower and angular ordered matched to NLO parton shower



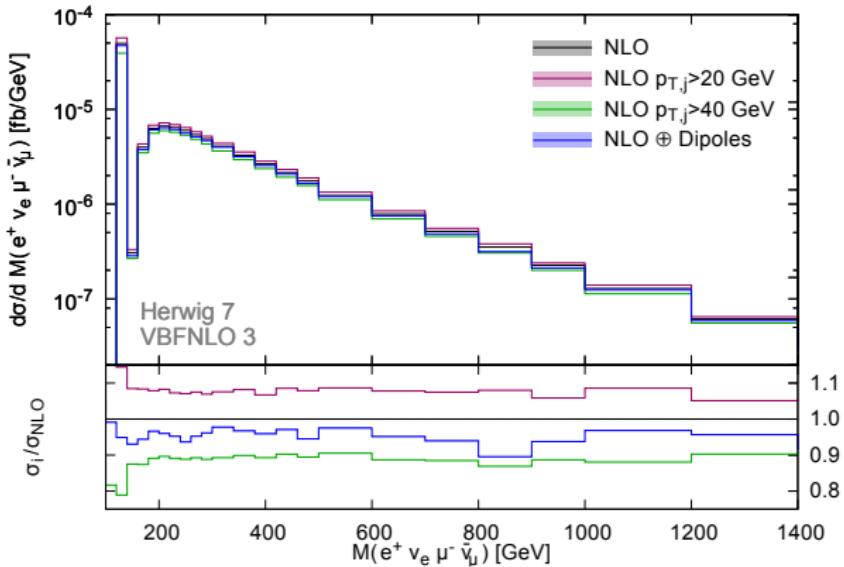
- all parton-shower results smaller than NLO cross section
- additional K -factor effect for LO \oplus Dipoles result ($K = 1.077$)
- no relevant shape changes (as expected: insensitive to QCD effects)

VBF Distributions



Migration Effects

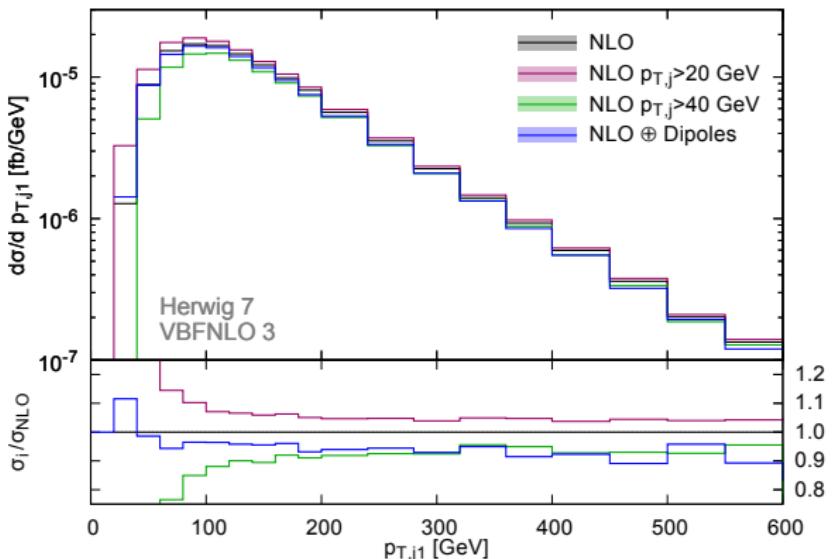
Vary transverse momentum cut of jets (default: $p_{T,j} > 30 \text{ GeV}$)



- same effect when slightly raising $p_{T,j}$ cut
- additional parton splittings: if hard & wide-angle emission → separate jet
- → reduces energy and transverse momentum of emitting parton
- ↔ $p_{T,j}$ cut, VBF cut $m_{jj} > 600 \text{ GeV}$

Migration Effects

Vary transverse momentum cut of jets (default: $p_{T,j} > 30 \text{ GeV}$)



- less pronounced for small $p_{T,j1}$
→ VBF cut main source
- → **migration of events** across cut boundary
- ↔ generation-level vs. analysis-level cuts
- ⇒ **no tuning** of acceptance criteria **required**
- generation-level cuts nevertheless chosen slightly weaker

Anomalous couplings

Effective Lagrangian $\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{SM}} + \sum_{d>4} \sum_i \frac{t_i^{(d)}}{\Lambda^{d-4}} \mathcal{O}_i^{(d)}$

- operators \mathcal{O} contain SM fields only
- respect SM gauge symmetries
- suppressed by $1/\Lambda^{d-4}$ (Λ : scale of new physics)

Building Blocks

- Higgs field Φ
- (covariant) derivative ∂^μ, D^μ
- fermion fields ψ
- field strength tensors $G^{\mu\nu}, W^{\mu\nu}, B^{\mu\nu}$

Redefine field strength tensors

$$\widehat{W}_{\mu\nu} = igT^a W_{\mu\nu}^a, \quad \widehat{B}_{\mu\nu} = ig' Y B_{\mu\nu} \quad \text{such that} \quad [D_\mu, D_\nu] = \widehat{W}_{\mu\nu} + \widehat{B}_{\mu\nu}$$

- includes coupling factors appearing naturally from New Physics Loops
- commonly adapted for dimension-6 operators

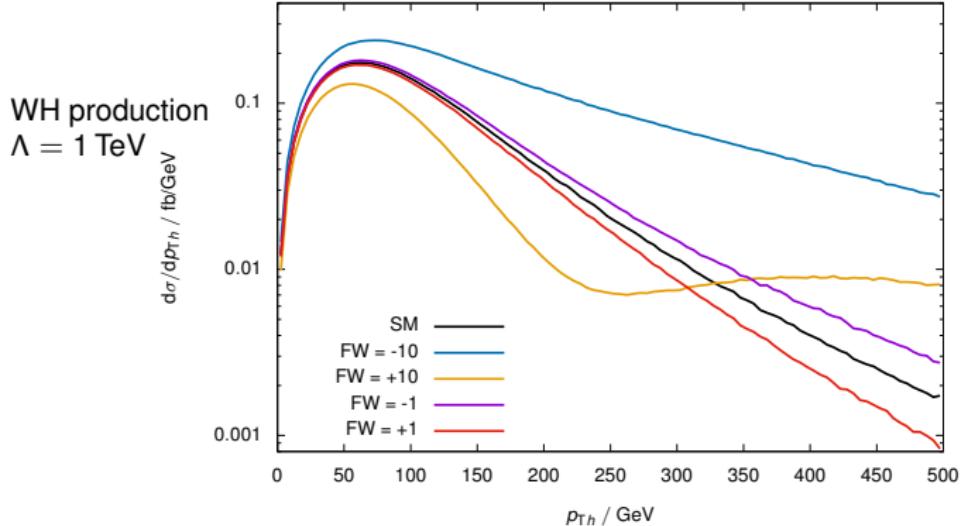
Operator dimensions

- $d = 6$: triple gauge couplings, higgs couplings
- $d = 8$: quartic gauge couplings, neutral triple gauge couplings

Anomalous Couplings – Example

Example operator: $\mathcal{O}_W = (D_\mu \Phi)^\dagger \hat{W}^{\mu\nu} (D_\nu \Phi)$, $\mathcal{L} = \mathcal{L}_{SM} + \frac{f_W}{\Lambda^2} \mathcal{O}_W + \dots$

WWH vertex: $\underbrace{igm_W g^{\mu\nu}}_{SM} - \underbrace{\frac{1}{2} i \frac{f_W}{\Lambda^2} gm_W \left(-g^{\mu\nu} (p_h \cdot p_- + p_h \cdot p_+) + p_h^\nu p_-^\mu + p_h^\mu p_+^\nu \right)}_{\mathcal{O}_W}$

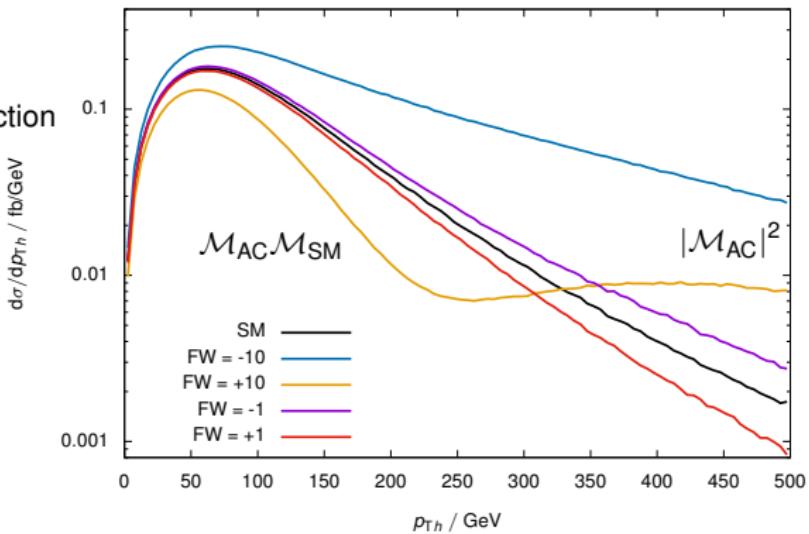


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WH production
 $\Lambda = 1 \text{ TeV}$



EFT assumptions

- all NP scales well above observables, no resonances at measurable scales
- f/Λ^2 “small”, depends on coupling: $\mathcal{O}(1)$ or $\mathcal{O}(\alpha_{\text{QED}})$

Power counting in Λ

$$\mathcal{M} = \mathcal{M}_{\text{SM}} + \underbrace{\mathcal{M}_{\text{AC}}^{d=6}}_{1/\Lambda^2} + \underbrace{\mathcal{M}_{\text{AC}}^{d=8}}_{1/\Lambda^4}$$

$$|\mathcal{M}|^2 = \underbrace{|\mathcal{M}_{\text{SM}}|^2}_{1/\Lambda^0} + \underbrace{2\text{Re}\mathcal{M}_{\text{SM}}^*\mathcal{M}_{\text{AC}}^{d=6}}_{1/\Lambda^2} + \underbrace{\left|\mathcal{M}_{\text{AC}}^{d=6}\right|^2}_{1/\Lambda^4} + \underbrace{2\text{Re}\mathcal{M}_{\text{SM}}^*\mathcal{M}_{\text{AC}}^{d=8}}_{1/\Lambda^4} + \underbrace{\left|\mathcal{M}_{\text{AC}}^{d=8}\right|^2}_{1/\Lambda^8}$$

- power-counting Λ^{-4} : $|\mathcal{M}_{\text{AC}}^{d=6}|^2$, $\mathcal{M}_{\text{SM}}^*\mathcal{M}_{\text{AC}}^{d=8}$?
- conservative: experimental fit only in range where $|\mathcal{M}_{\text{AC}}|^2 \ll \mathcal{M}_{\text{SM}}^*\mathcal{M}_{\text{SM}}$
- but: \mathcal{M}_{SM} accidentally small (weak coupling compared to \mathcal{M}_{AC} , radiation zero)
 $\Rightarrow \mathcal{M}_{\text{SM}}^*\mathcal{M}_{\text{AC}}$ suppressed, $|\mathcal{M}_{\text{AC}}^{d=6}|^2$ leading $1/\Lambda^4$ term

Anomalous Quartic Gauge Couplings

Vector-boson scattering ideal process to test anomalous quartic gauge couplings

[Feigl, Schlimpert; Löschner, Perez]

Dimension-8 operators in Lagrangian

[Eboli, Gonzalez-Garcia, Mizukoshi]

$$\mathcal{L}_{S,0} \propto [(D_\mu \Phi)^\dagger (D_\nu \Phi)] \times [(D^\mu \Phi)^\dagger (D^\nu \Phi)]$$

$$\mathcal{L}_{M,2} \propto [\widehat{B}^{\mu\nu} \widehat{B}_{\mu\nu}] \times [(\widehat{D}^\beta \Phi)^\dagger (\widehat{D}_\beta \Phi)]$$

$$\mathcal{L}_{T,1} \propto [\widehat{W}^{\alpha\nu} \widehat{W}_{\mu\beta}] \times [\widehat{W}^{\mu\beta} \widehat{W}_{\alpha\nu}]$$

...

(at least) four gauge fields in each term → modify quartic gauge couplings

paper defines $\widehat{W}^{\mu\nu}$, $\widehat{B}^{\mu\nu}$ without coupling constants ig , $ig' Y$

→ UFO file by Eboli, Gonzalez-Garcia follows this convention → MadGraph

→ VBFNLO implementation follows dim-6 convention

⇒ simple constant relations between the two, e.g. $f_{M,2}^{\text{VBFNLO}} = -\frac{4}{g'^2} \cdot f_{M,2}^{\text{Eboli}}$

Form factor tool

Contribution of higher-dimensional operators can violate unitarity above certain energy scale → unphysical

- Determine energy scale of unitarity violation → Partial-wave analysis
 - Consider amplitudes for on-shell $VV \rightarrow VV$ scattering ($V \in W, Z, \gamma$)
 - Decompose into series of partial waves with coefficients a_i , $i = 0, 1, 2, \dots$
 - → Condition for unitarity conservation: $|\text{Re}(a_i)| < \frac{1}{2}$
 - Strongest bound typically from $i = 0 \rightarrow$ check only this contribution

⇒ maximal energy scale Λ_{\max}

- Ensure unitarity at higher energies by applying form factor
 - Unitarity preserved by new-physics contributions entering at or before Λ_{\max}
→ acts as cut-off
 - effective implementation in low-energy theory ⇒ form factor
 - explicit form model-dependent → choice arbitrary
 - VBFNLO: dipole form factor

$$\mathcal{F}(s) = \frac{1}{\left(1 + \frac{s}{\Lambda_{\text{FF}}^2}\right)^n} \quad \Lambda_{\text{FF}}^2, \quad n: \text{free parameters}$$

- Determine maximal Λ_{FF} from given anomalous couplings, n and maximum energy considered

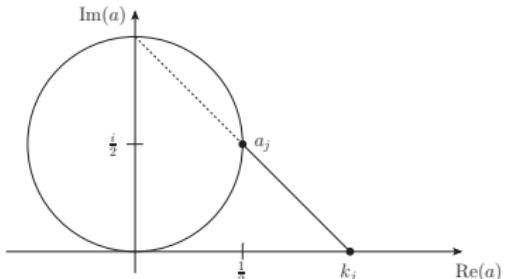
→ implemented in form factor tool available from VBFNLO web site

<http://www.itp.kit.edu/~vbfnloweb/wiki/doku.php?id=download:formfactor>

Example output

```
[...]
Reading in anomalous couplings parameter:
  SQRT_S          = 14000.
  FFEXP           = 2.0000
  FS0             = 0.10000E-09
  FS1             = 0.10000E-09
[...]
Checking tree-level unitarity violation with on-shell W+W- -> W+W- scattering
using the largest helicity combination of the zeroth partial wave...
[...]
Checking tree-level unitarity violation with on-shell VV->VV scattering
including all Q=0 channels involving W and Z bosons using the largest
helicity combination of the zeroth partial wave...
[...]
Results for each channel, taking only the helicity combination with the largest
contribution to the zeroth partial wave into account:
FFscale_WWWW =      688. GeV   ( without FF: |Re(pwave_0)| > 0.5 at    0.8 TeV )
[...]
No tree-level unitarity violation in W+W- -> AA scattering found.
[...]
Results for each channel, taking contributions from all helicity combinations to
the zeroth partial wave into account by diagonalizing the T-matrix:
FFscale_WWWW_diag =      688. GeV   ( without FF: |Re(pwave_0)| > 0.5 at    0.8 TeV )
[...]
FFscale_VVVV_Q_0 =      622. GeV   ( without FF: |Re(pwave_0)| > 0.5 at    0.7 TeV )
[...]
```

K matrix unitarization



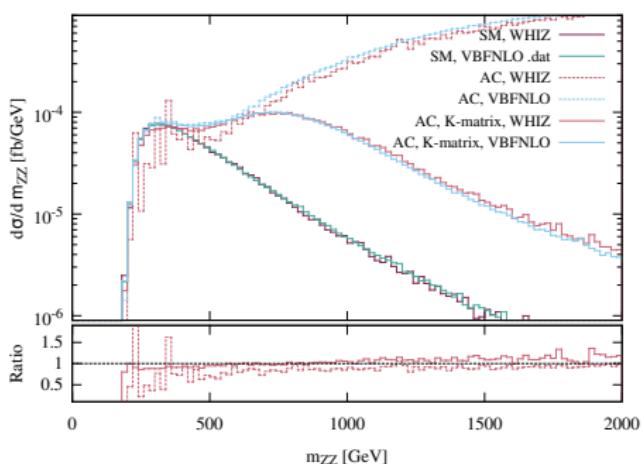
Project amplitude k_j ,
which exceeds (tree-level) unitarity,
back onto Argand circle
→ K matrix unitarization
→ a_j

[→ Marco's talk]

[VBFNLO implementation: Löschner, Perez; following: Alboteanu, Kilian, Reuter]

Comparison with Whizard, which has this method already implemented:

[Kilian, Ohl, Reuter, Sekulla, et al.]



Example: VBF-ZZ ($e^+e^- \mu^+\mu^-$)

good agreement between both codes for longitudinal ops. at LO
→ can now generate distributions also at NLO via VBFNLO

Extension to mixed and transverse operators not straight-forward
→ work ongoing

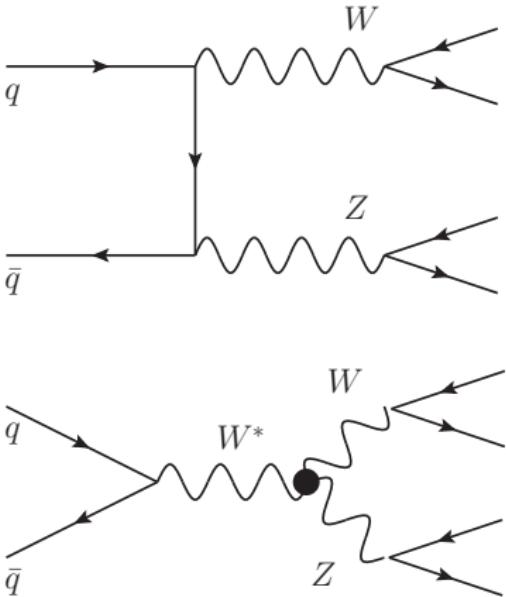
Diboson production at the LHC

Why Diboson

- leptonic decays: "easy" to tag, precise knowledge of final state
- access to triple gauge couplings, deviations in EW sector

Observables

- new resonances
- enhanced production at high energy
 \Rightarrow AC
- m_T, p_{TV}, p_{TI}
- decay angles, spin information



Idea

- “Giant QCD K-factors beyond NLO”
[\[Rubin, Salam, Sapeta, 1006.2144\]](#)
- merge different multiplicity final states
 $X@\text{NLO} + X_j@\text{NLO} = X@\bar{n}\text{NLO}$
- parton level (\rightarrow fast)
- use NLO events, interface to existing Monte Carlos programs

2	$\sigma_0^{(2)}$	$\sigma_1^{(2)}$	\dots
1	$\sigma_0^{(1)}$	$\sigma_1^{(1)}$	$\sigma_2^{(1)}$
0	$\sigma_0^{(0)}$	$\sigma_1^{(0)}$	$\sigma_2^{(0)}$
	0	1	2

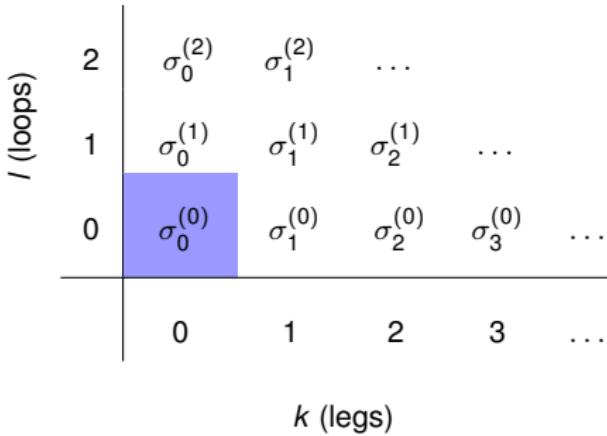
k (legs)

Properties

- preserve NLO total cross section
- exact tree-level and one-loop
- only singular two-loop contributions
- include dominant contributions from extra emissions, $\mathcal{O}(\alpha_s \ln^2 p_{T\text{jet}}/m_Z)$
- nearly NNLO in high- p_T tails

Idea

- “Giant QCD K-factors beyond NLO”
[\[Rubin, Salam, Sapeta, 1006.2144\]](#)
- merge different multiplicity final states
 $X@\text{NLO} + X_j@\text{NLO} = X@\bar{n}\text{NLO}$
- parton level (\rightarrow fast)
- use NLO events, interface to existing Monte Carlos programs



Properties

- preserve NLO total cross section
- exact tree-level and one-loop
- only singular two-loop contributions
- include dominant contributions from extra emissions, $\mathcal{O}(\alpha_s \ln^2 p_{T\text{jet}}/m_Z)$
- nearly NNLO in high- p_T tails

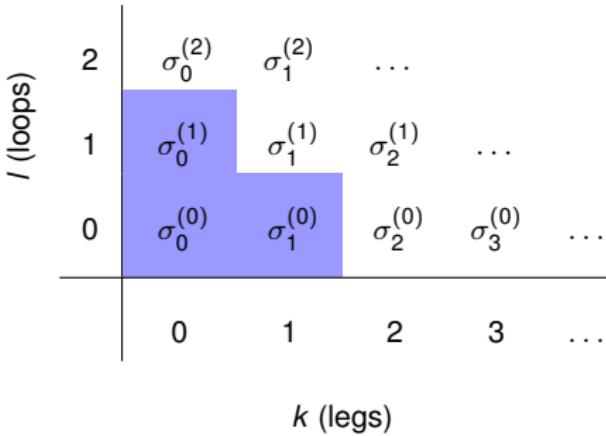
X@LO

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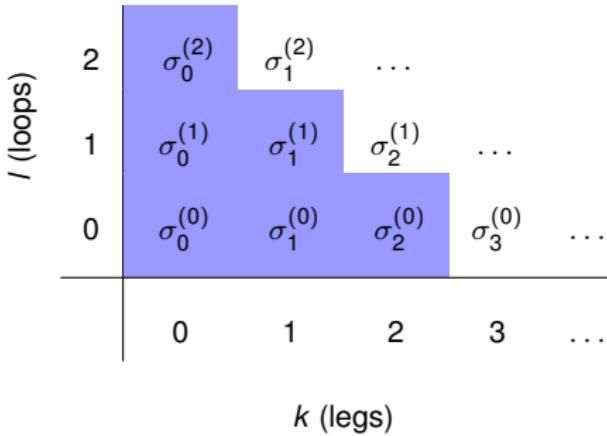
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X@NLO

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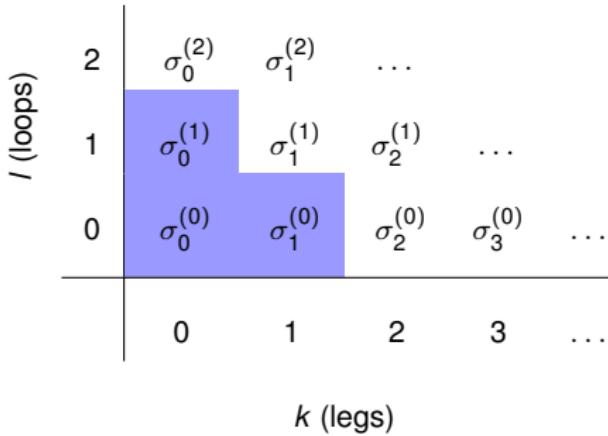
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X@NNLO

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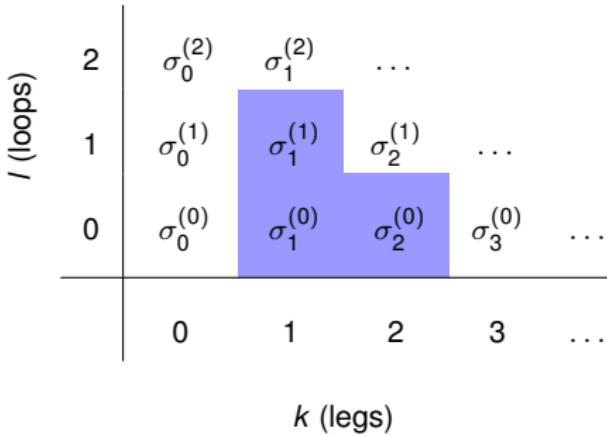
Properties

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X@NLO

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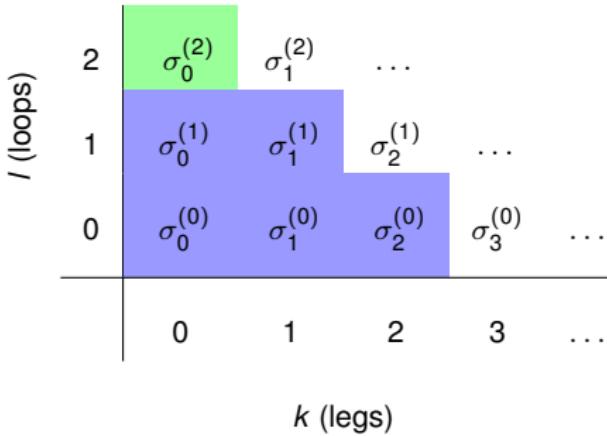
Properties

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- only singular two-loop contributions
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- nearly NNLO in high- p_T tails

X+jet@NLO

Idea

- “Giant QCD K-factors beyond NLO”
[\[Rubin, Salam, Sapeta, 1006.2144\]](#)
- merge different multiplicity final states
 $X@\text{NLO} + X_j@\text{NLO} = X@\bar{n}\text{NLO}$
- parton level (\rightarrow fast)
- use NLO events, interface to existing Monte Carlos programs



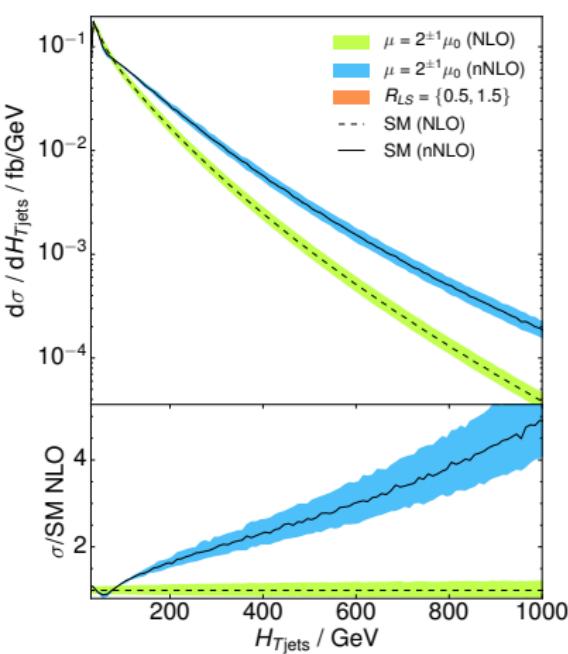
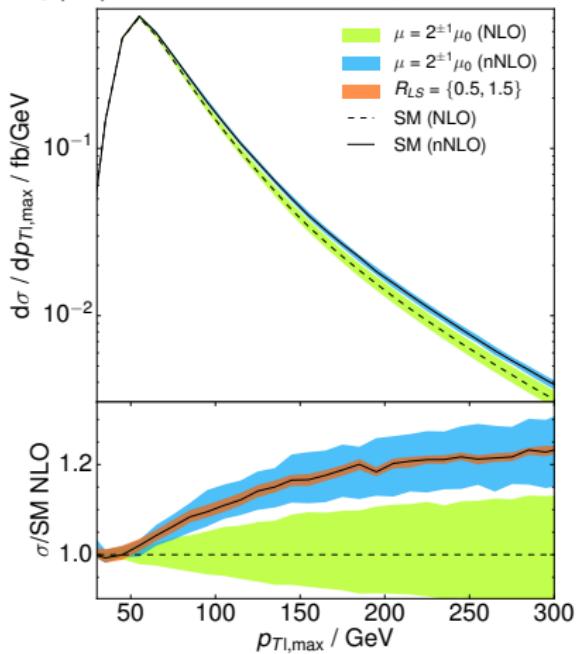
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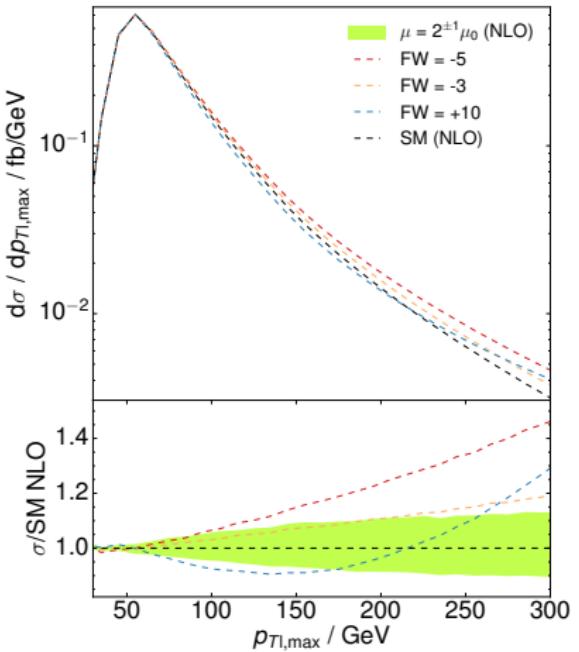
$X@\bar{n}\text{NLO}$

\bar{n} NLO for WZ production

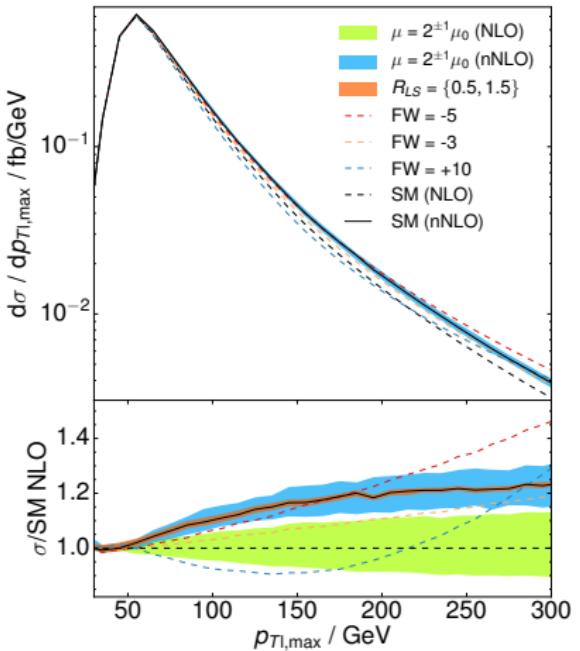
$e^+ \nu_e \mu^+ \mu^- + X$, LHC@13 TeV, inclusive cuts



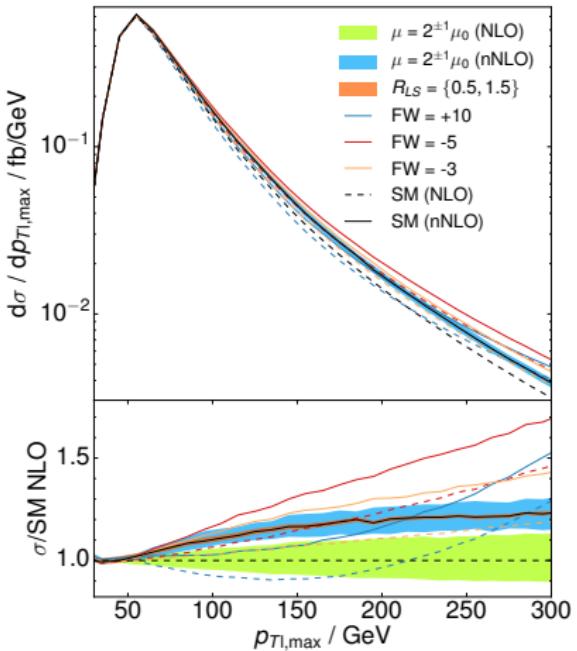
AC for diboson production



AC for diboson production

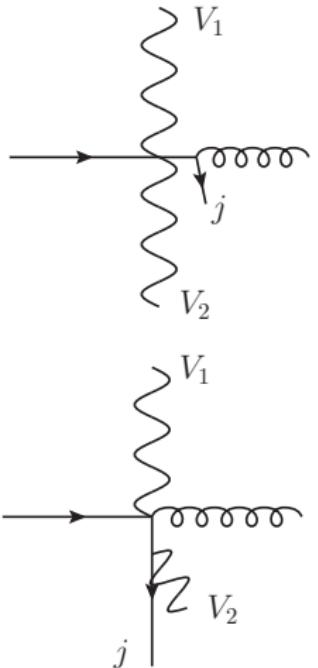


AC for diboson production



Jet vetos

want $VV + \text{jets}$, not $Vj + V$



Traditional (fixed) jet veto

- don't allow any jets above a fixed p_T threshold
- introduces large logs $\log p_{T\text{veto}}/m_{VV}$
- cuts away relevant phase space:
 $m_{VV} \approx 1 \text{ TeV} \leftrightarrow p_{T\text{jet}} = 50/300 \text{ GeV}$

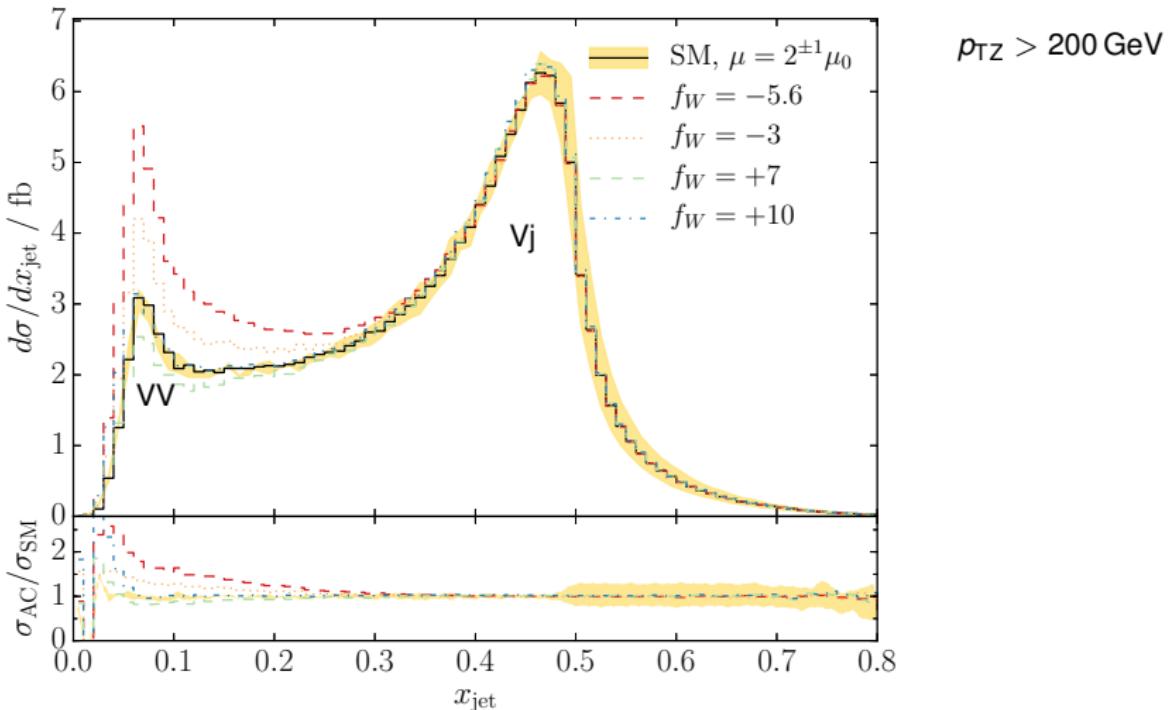
Dynamical veto

[Campanario, RR, Zeppenfeld, 1410.4840]

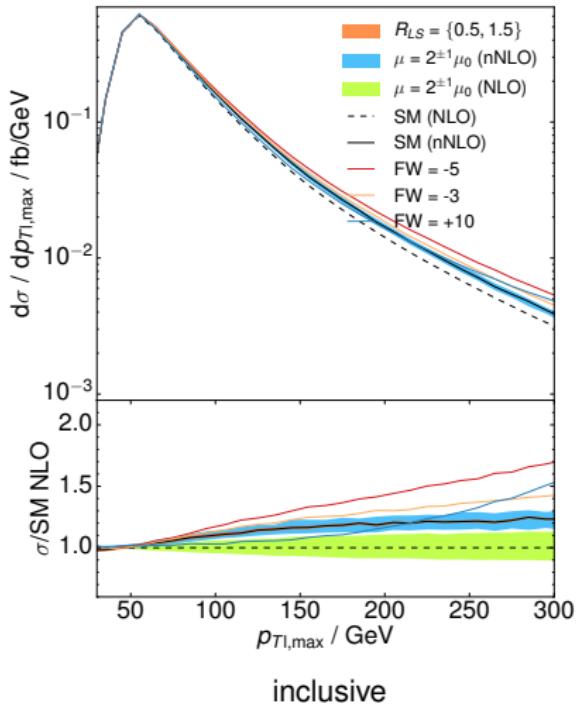
- veto scaled depending on overall scale \Rightarrow smaller logs
- allow more QCD radiation in tails of EW distributions

$$x_{\text{jet}} = \frac{\sum_{\text{jets}} E_{T,i}}{\sum_{\text{jets}} E_{T,i} + E_{T,W} + E_{T,Z}}$$
$$E_T = E \frac{|\vec{p}_T|}{|\vec{p}|}$$

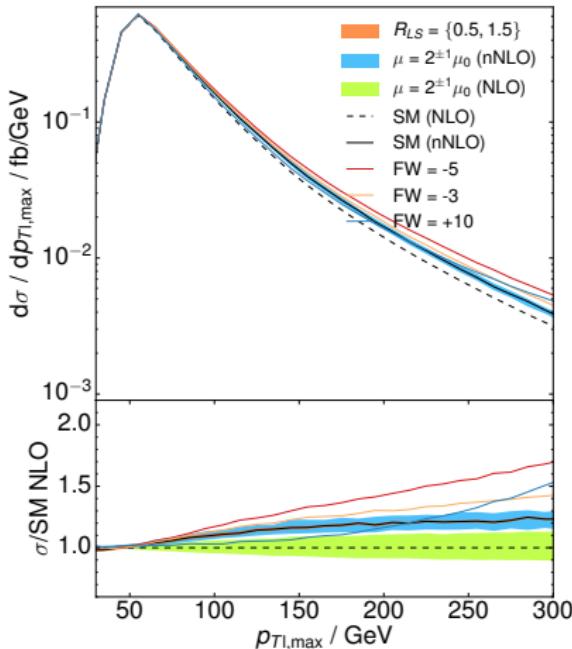
Observable $x_{\text{jet}} = \frac{\sum_{\text{jets}} E_{\text{T},i}}{\sum_{\text{jets}} E_{\text{T},i} + E_{\text{T},W} + E_{\text{T},Z}}$



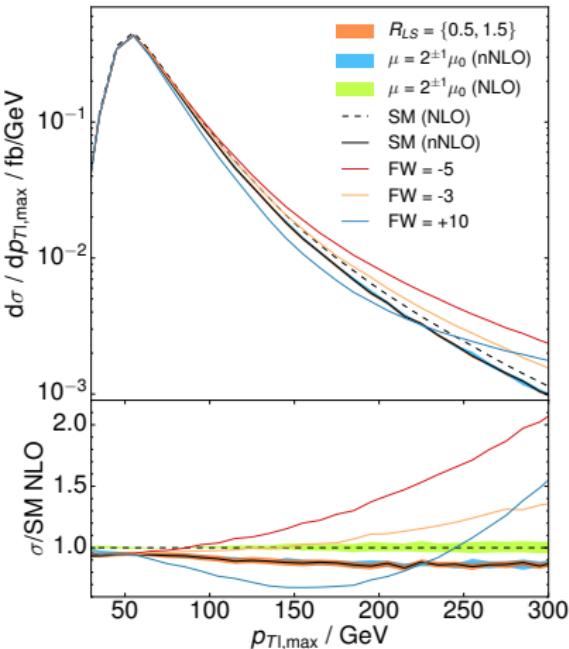
Dynamical veto to improve AC sensitivity



Dynamical veto to improve AC sensitivity



inclusive



$x_{\text{jet}} < 0.2$

Beyond NLO: Loopsim

- method to combine multiplicities consistently at parton level
 $X@\text{NLO} + Xj@\text{NLO} = X@\bar{n}\text{NLO}$
- captures log enhanced terms of real emission
- nearly NNLO in high- p_T region

Anomalous couplings

- diboson production interesting channel to study triple gauge couplings
- validity depends on coupling and phase space region
- increase sensitive \Rightarrow dynamical jet veto

$$x_{\text{jet}} = \frac{\sum_{\text{jets}} E_{\text{T},i}}{\sum_{\text{jets}} E_{\text{T},i} + E_{\text{T},W} + E_{\text{T},Z}}$$

Conclusions II

VBFNLO is a flexible parton-level Monte Carlo for processes with electro-weak bosons

- particular focus on speed and stability
- New features in latest VBFNLO release:
 - BLHA interface to MC generators
→ parton-shower (and hadronization) effects
 - K-matrix unitarization for selected couplings
- study merged NLO samples with LoopSim

VBFNLO is collaborative effort:

[0811.4559, 1107.4038, 1404.3940]

K. Arnold, J. Baglio, J. Bellm, G. Bozzi, M. Brieg, F. Campanario, C. Englert, B. Feigl,
J. Frank, T. Figy, F. Geyer, N. Greiner, C. Hackstein, V. Hankele, B. Jäger, N. Kaiser,
M. Kerner, G. Klämke, M. Kubocz, M. Löschner, L.D. Ninh, C. Oleari, S. Palmer,
S. Plätzer, S. Prestel, M. Rauch, R. Roth, H. Rzeħak, F. Schissler, O. Schlimpert,
M. Spannowsky, M. Worek, D. Zeppenfeld

Code available at <https://www.itp.kit.edu/vbfnlo>

Contact: vbfnlo@itp.kit.edu

Reweighting events (REPOLO)

[F. Schissler, available on request]

Generating events at detector-level time-consuming (shower, detector simulation, ...)

→ Reuse SM Higgs events and reweight for different BSM scenarios

→ REPOLO (REweighting POwheg events at Leading Order)

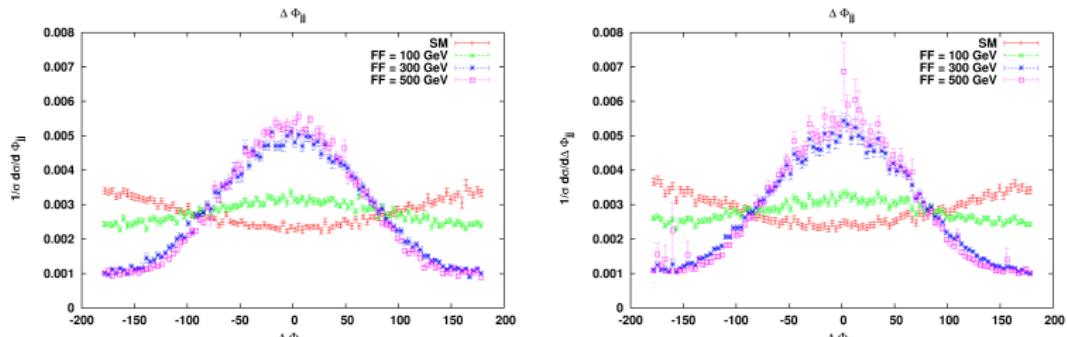
uses VBFNLO framework to multiply each event by a factor $\frac{|\mathcal{M}_{\text{BSM}}|^2}{|\mathcal{M}_{\text{SM}}|^2}$

Limitation:

event with high reweighting factor ($|\mathcal{M}_{\text{SM}}|^2 \ll |\mathcal{M}_{\text{BSM}}|^2$) can destroy distributions

→ only SM-like distributions can be safely reweighted

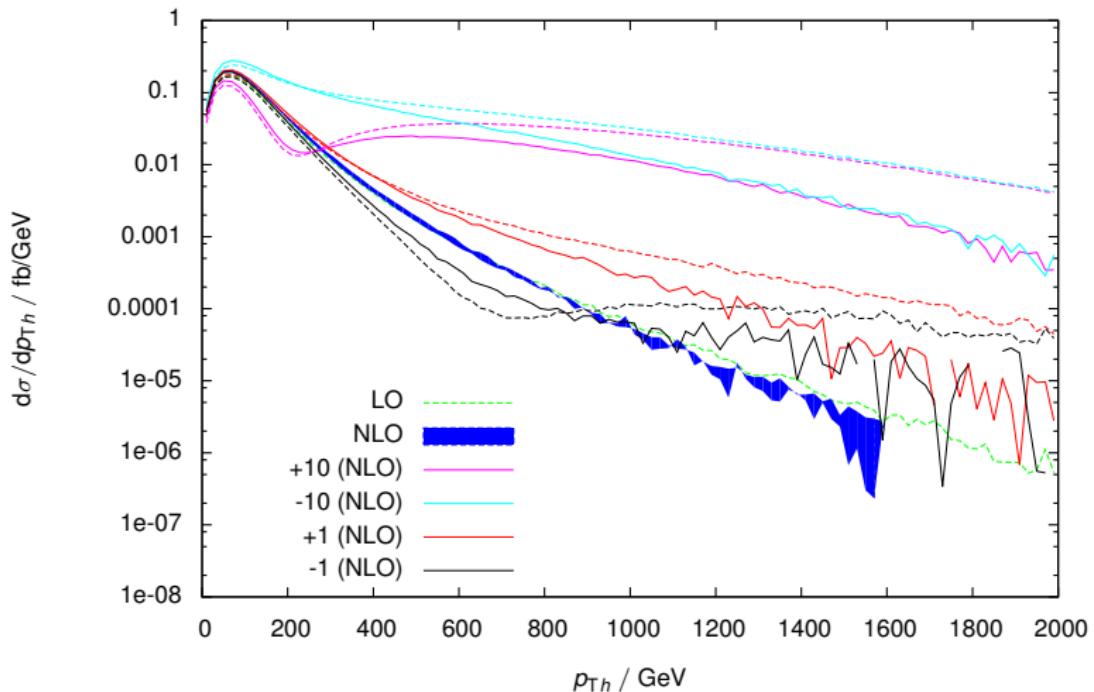
Example: VBF- $H \rightarrow \gamma\gamma$, SM → anomalous Higgs couplings (+ $HW_+^{\mu\nu}W_{\mu\nu}^-$, $HZ^{\mu\nu}Z_{\mu\nu}$)
left: direct generation; right: reweighting



⇒ distributions correctly reproduced, larger errors in SM-suppressed regions

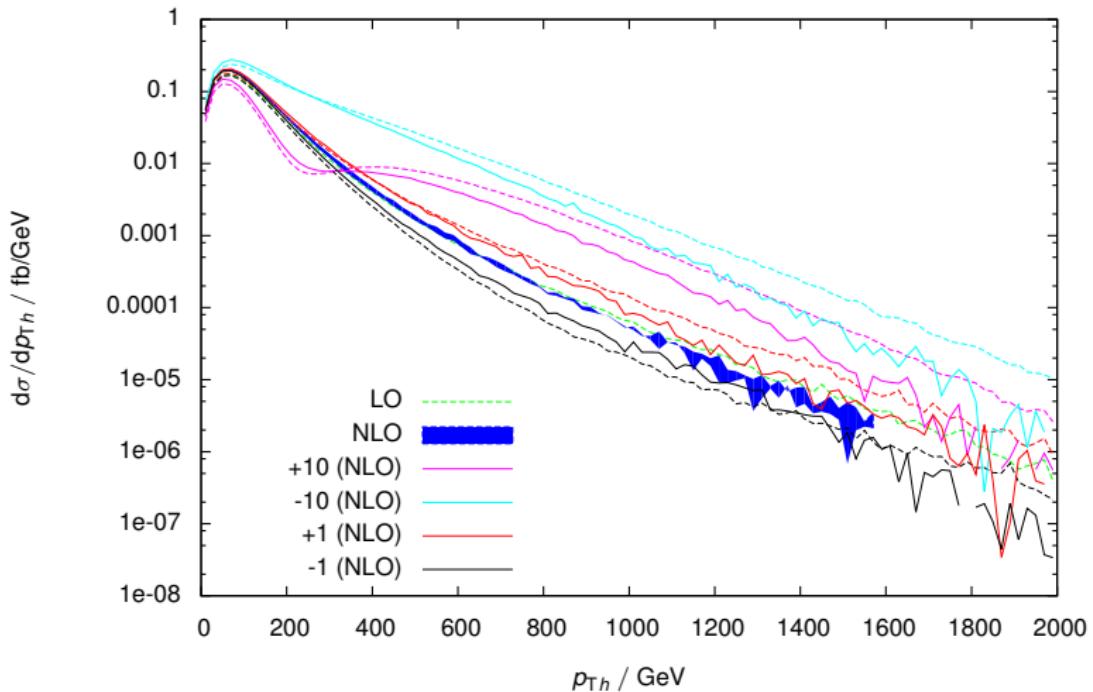
Anomalous Couplings – Formfactor effects

$W\bar{h}j$ with inclusive cuts and several values of f_W/Λ^2 in TeV^{-2} and no form factor



Anomalous Couplings – Formfactor effects

with form factor $\left(\frac{\Lambda^2}{\Lambda^2 + m_{WH}^2}\right)^2$, $\Lambda = 2 \text{ TeV}$



K-matrix + Parton Shower

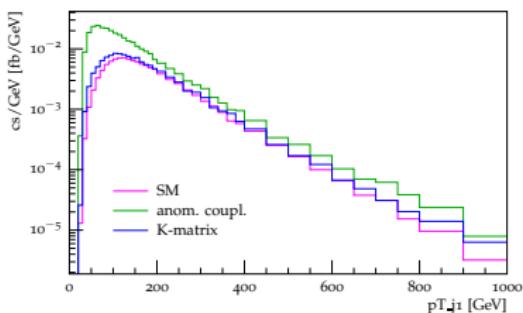
Combine K-matrix setup with parton shower

[VBFNLO3&Herwig7]

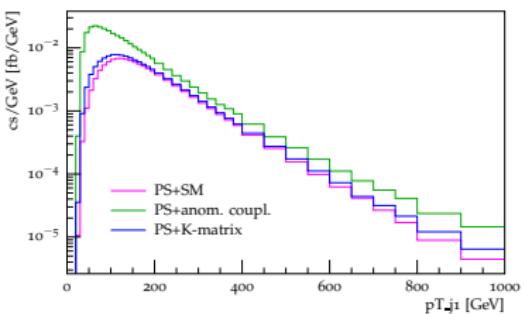
Example: VBF- $W^+ W^+$ ($pp \rightarrow e^+ \nu_e \mu^+ \nu_\mu jj$)

anom. coupl.: $f_{S,1} = 100 \text{ TeV}^{-4}$

fixed-order NLO



NLO+PS (MC@NLO + dipole shower)



Strong enhancement of leading jet at low transverse momenta without unitarization
small dependence on parton-shower effects

Combination with Parton Shower

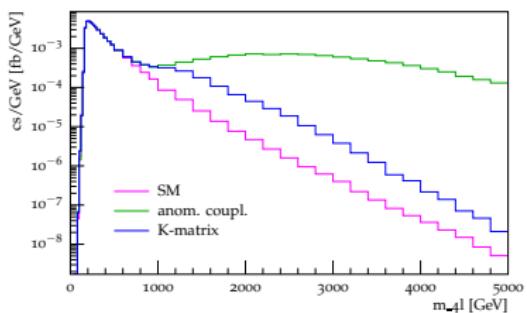
Can also combine K-matrix in setup with parton shower

[VBFNLO3&Herwig7]

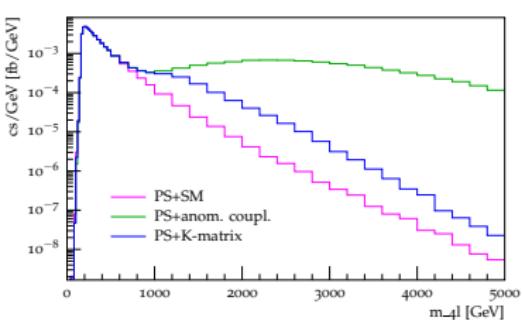
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fixed-order NLO



NLO+PS (MC@NLO + dipole shower)



No significant shape changes in m_{4l} when switching on PS

(integrated c.s. PS/NLO: -3.0% (SM) / -3.8% (K-matrix))

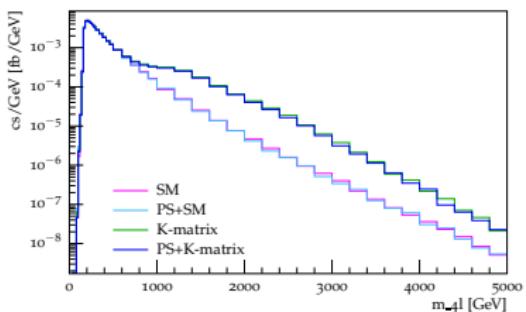
Combination with Parton Shower

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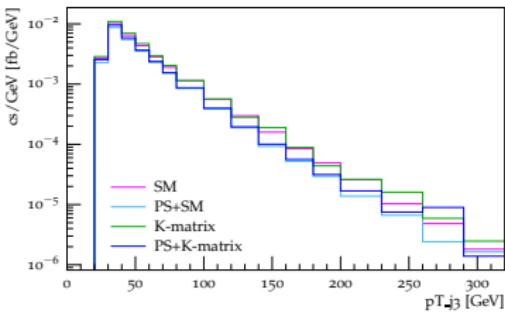
[VBFNLO3&Herwig7]

Example: VBF- $W^+ W^+$ ($pp \rightarrow e^+ \nu_e \mu^+ \nu_\mu jj$)
anom. coupl.: $f_{S,1} = 100 \text{ TeV}^{-4}$

$m_{4\ell}$ – Comparison



$p_{j,3}^T$ – Comparison

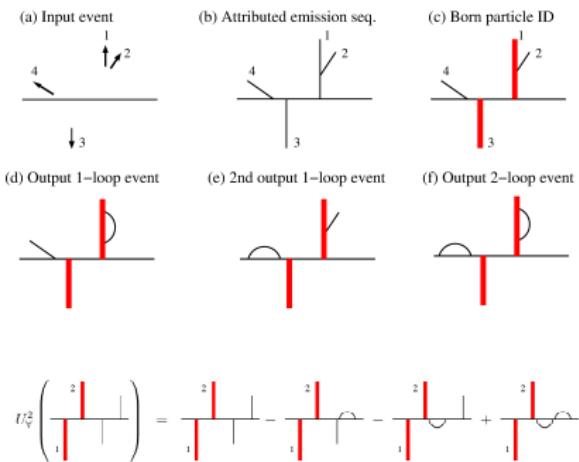


No significant shape changes in $m_{4\ell}$ when switching on PS
(integrated c.s. PS/NLO: -3.0% (SM) / -3.8% (K-matrix))

$\leftrightarrow p_{j,3}^T$ mostly sensitive to parton-shower effects

The Loopsim Method – “Looping”

- based on unitarity
- per-event: assign angular-ordered branching structure
(C/A algorithm with radius R_{LS})
- hard structure of event determined
→ remaining particles: “Born”
- construct virtual “loop” events:
recombine non-“Born” particles
⇒ subtraction events
- Clustering radius R_{LS} gives estimate
of dependence on merging
- Scale dependence preserved for
additional emissions, overestimates
the NNLO scale dependence



Interfacing with LoopSim

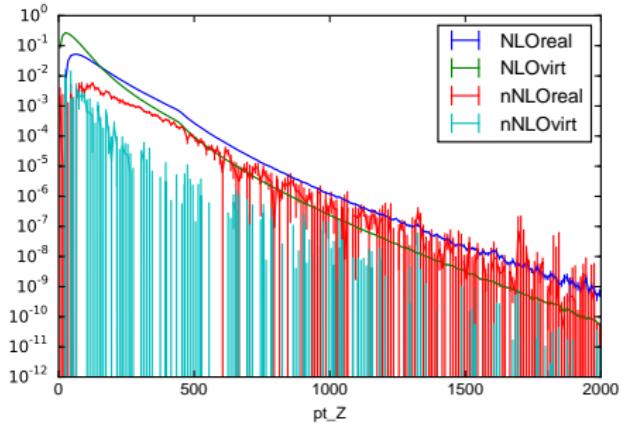
- VBFNLO produces event sample
- LoopSim generates looped events from sample
- run analysis on those final events

Issues

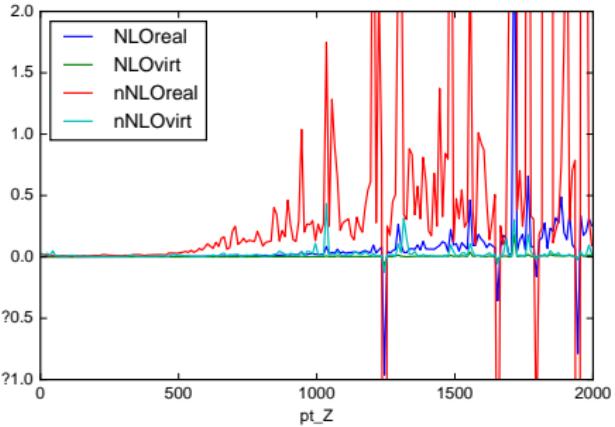
- no flavour information from VBFNLO (summed over)
- need very inclusive sample (no jet cut) to fill all of phase space
- Consistent scale choice over all samples needed

practical LoopSim

Ingredients for \bar{n} NLO

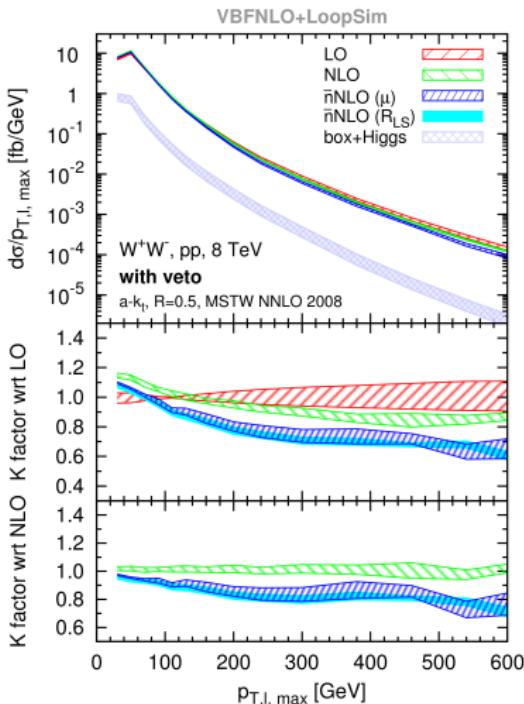
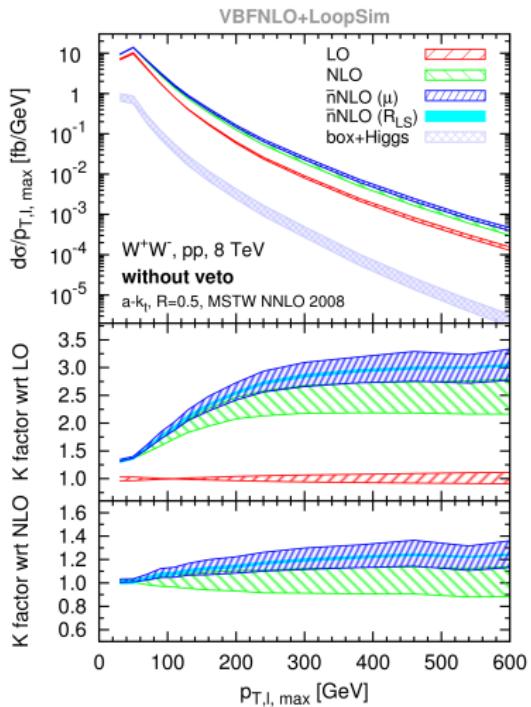


Relative error



- LoopSim slower than bare VBFNLO run by a factor 8
- interest not in phase space region with highest cross section but tails

Previous LoopSim results

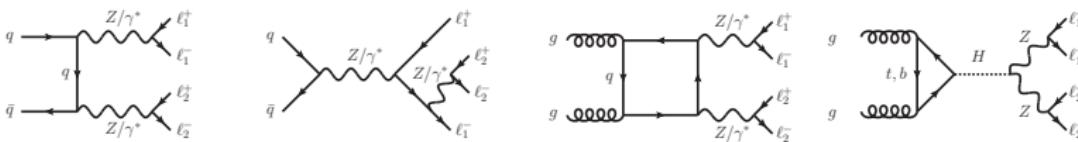


[Campanario, Rauch, Sapeta, 1309.7293]

ZZ production

$$pp \rightarrow \ell_1^+ \ell_1^- \ell_2^+ \ell_2^-, 8 \text{ TeV}$$

[Campanario, Rauch, Sapeta]



Integrated cross sections and scale variation (setup as in [1], inclusive on-shell ZZ):

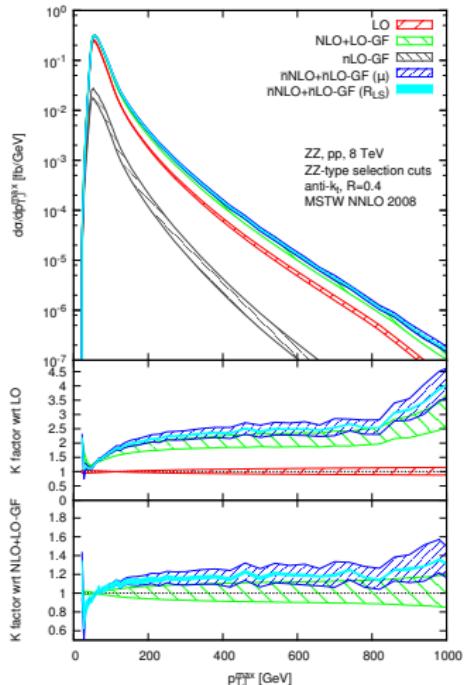
$\sigma_{\text{LO}} [\text{pb}]$	$5.0673(4)$	$^{+1.6\%}_{-2.7\%}$	(Ref. [1]: 5.060)	$^{+1.6\%}_{-2.7\%}$
$\sigma_{\text{NLO}} [\text{pb}]$	$7.3788(10)$	$^{+2.8\%}_{-2.3\%}$	(Ref. [1]: 7.369)	$^{+2.8\%}_{-2.3\%}$
$\sigma_{\text{NLO+LO-GF}} [\text{pb}]$	$7.946(3)$	$^{+4.2\%}_{-3.2\%}$		
$\sigma_{\text{NNLO}} [\text{pb}]$			(Ref. [1]: 8.284)	$^{+3.0\%}_{-2.3\%}$
$\sigma_{\bar{n}\text{NLO}} [\text{pb}]$	$8.103(5)$	$^{+4.7\%}_{-2.6\%}$ (μ)	$^{+0.8\%}_{-0.6\%}$ (R_{LS})	
$\sigma_{\bar{n}\text{NLO+LO-GF}} [\text{pb}]$	$8.118(5)$	$^{+4.7\%}_{-2.6\%}$ (μ)	$^{+0.8\%}_{-0.6\%}$ (R_{LS})	

good agreement between $\bar{n}\text{NLO}$ and NNLO \rightarrow 2% difference only
uncertainty due to LoopSim parameter R_{LS} small

[1]: Cascioli, Rathlev et al.

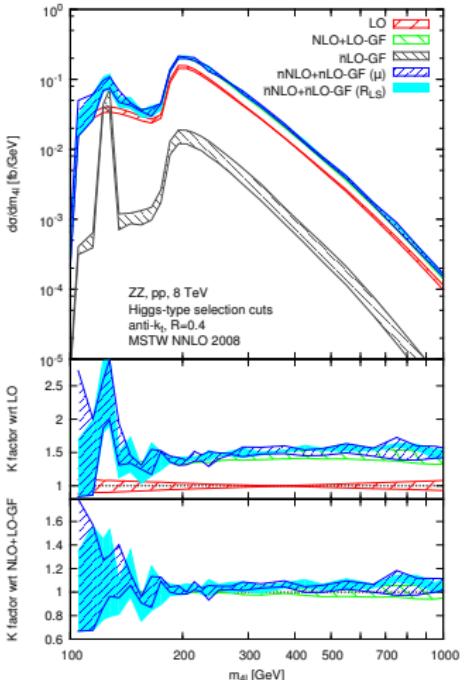
ZZ production

$p_{T,\ell}^{\max}$, inclusive cuts



significant $\bar{n}\text{NLO}$ corrections at high p_T

$m_{4\ell}$, Higgs cuts



distribution stable when adding $\bar{n}\text{NLO}$

Cuts

$$p_{\mathrm{T}j} > 30 \text{ GeV}$$

$$p_{\mathrm{T}I} > 15 \text{ GeV}$$

$$\not{p}_{\mathrm{T}} > 30 \text{ GeV}$$

$$|\eta_j| < 4.5$$

$$|\eta_I| < 2.5$$

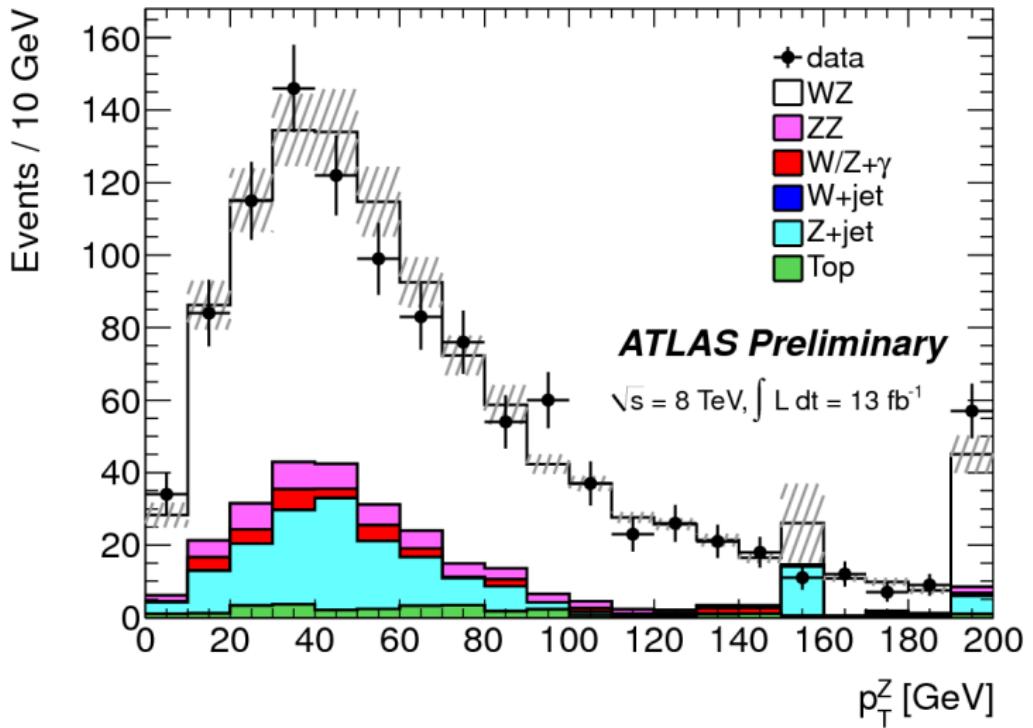
$$R_{I,j} > 0.4$$

$$60 \text{ GeV} < m_{\parallel} < 120 \text{ GeV}$$

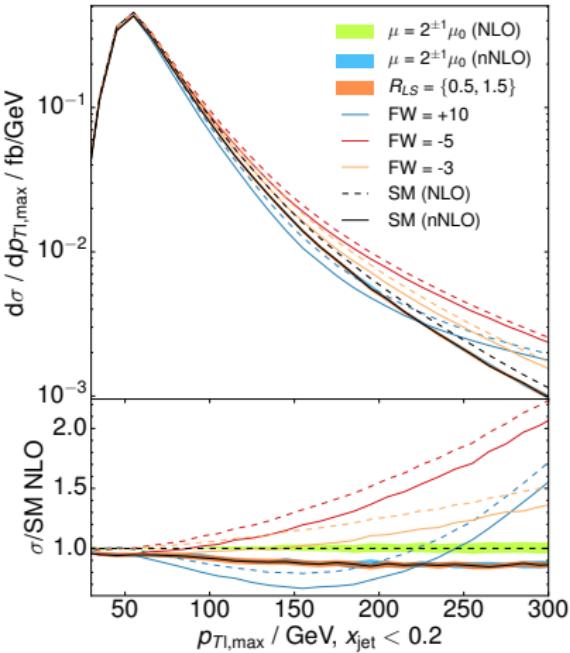
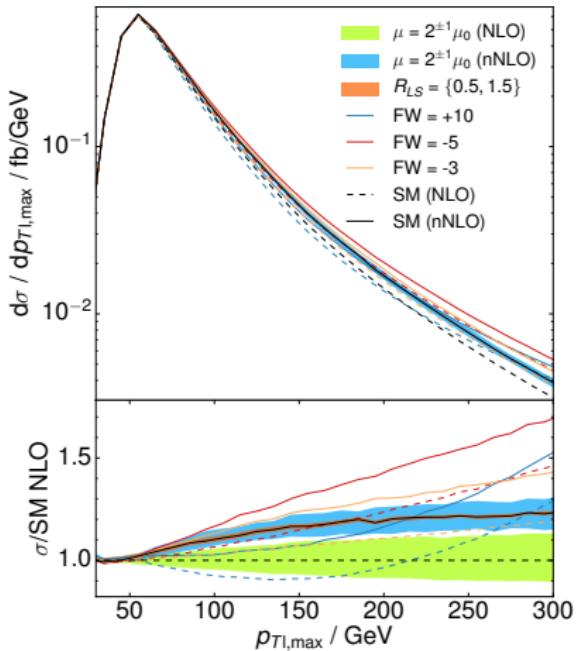
boosted: $p_{\mathrm{T}Z} > 200 \text{ GeV}$

Input values

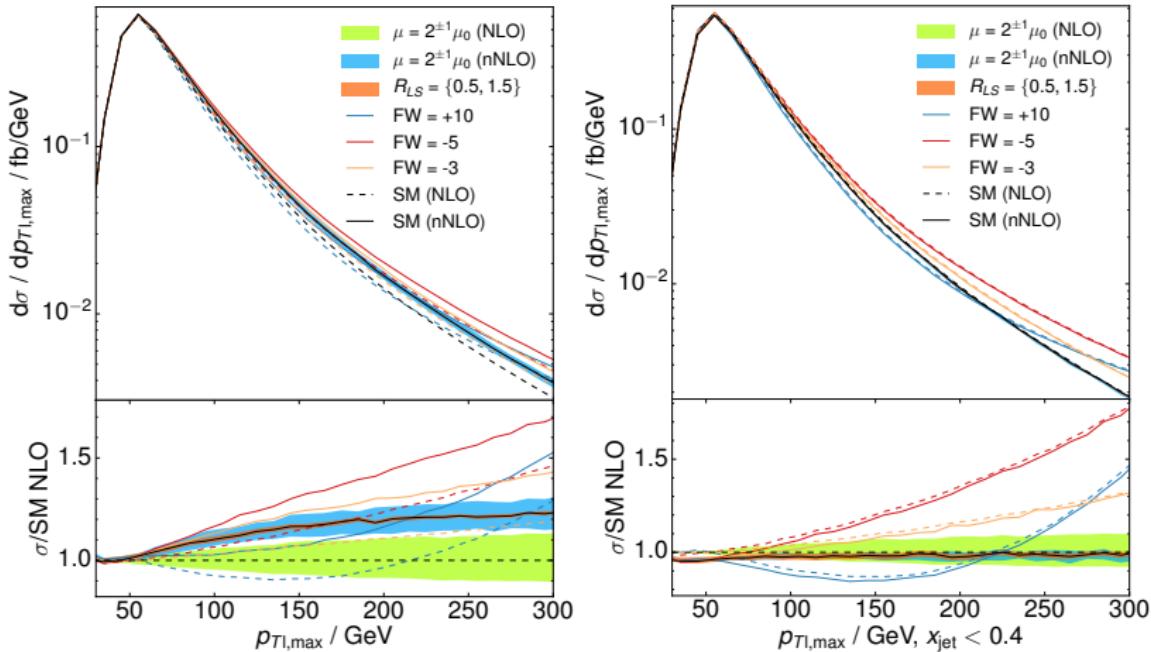
- EW constants: VBFNLO default
- PDF: NNPDF23



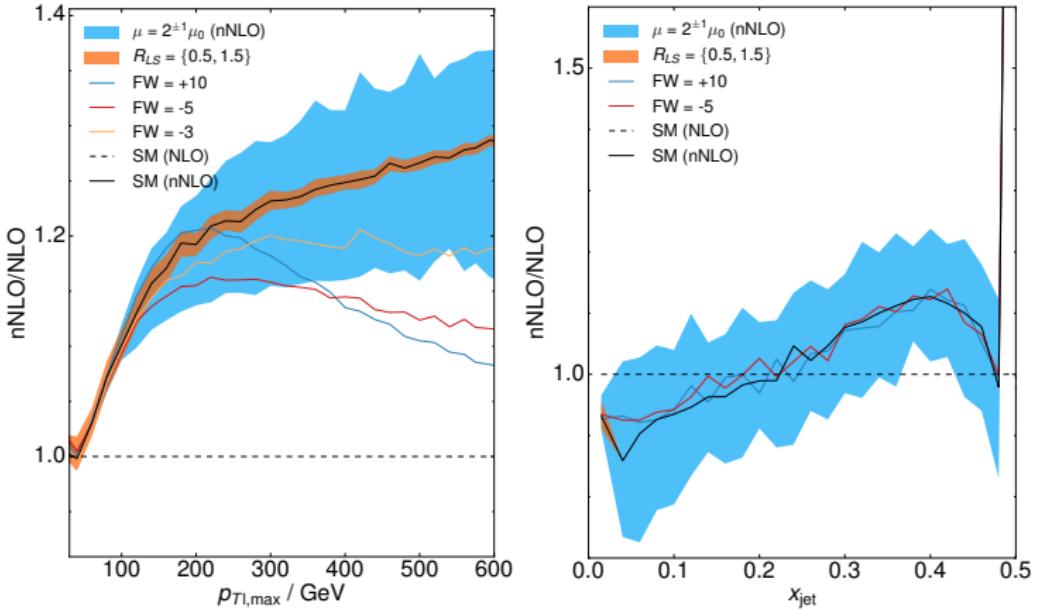
Different x_{jet} cuts



Different x_{jet} cuts



x_{jet} \bar{n} NLO corrections



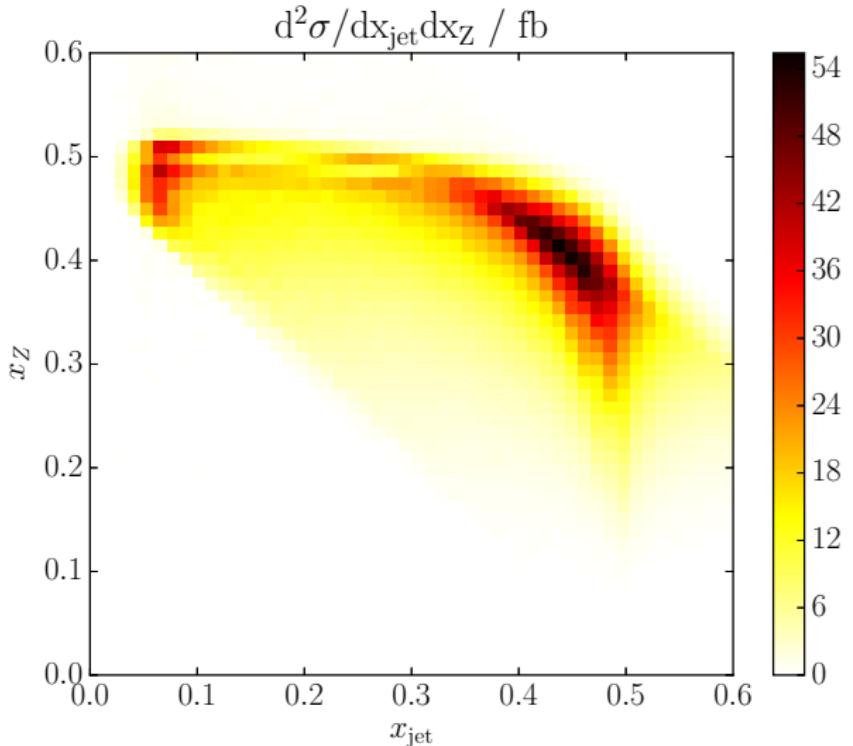
Motivation

- 3 particle final state (WZ)
- the transverse momenta can be parametrized using only two variables
6 d.o.f. ($p_{T,W}$, $p_{T,Z}$, $p_{T,\text{jet}}$) - 2 (total $p_T = 0$) - 1 (no ϕ dependence) - 1 (rescaling at high p_T)
- dalitz-like construction

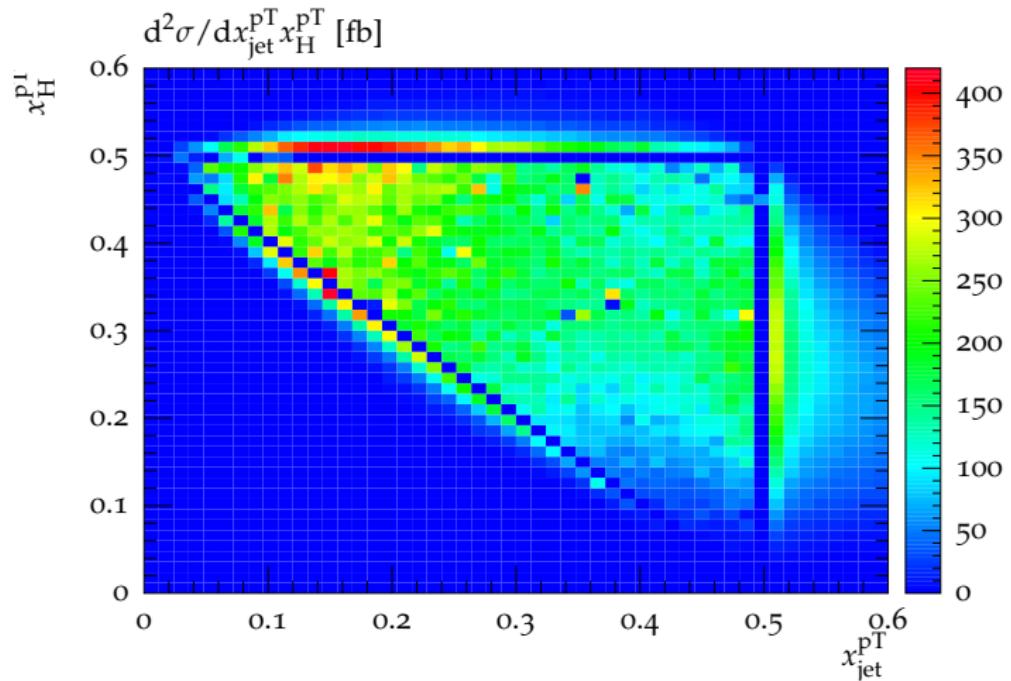
$$x_{\text{jet}} = \frac{\sum_{\text{jets}} E_{T,i}}{\sum_{\text{jets}} E_{T,i} + E_{T,W} + E_{T,Z}}, \quad x_V = \frac{E_{TV}}{\sum_{\text{jets}} E_{T,i} + E_{T,W} + E_{T,Z}}$$
$$x_{\text{jet}} + x_W + x_Z = 1$$
$$x_i \leq 0.5 \quad (\text{at LO only})$$

other choices: p_T instead of E_T , partons instead of jets, ...
Careful not to be (too) infrared-sensitive

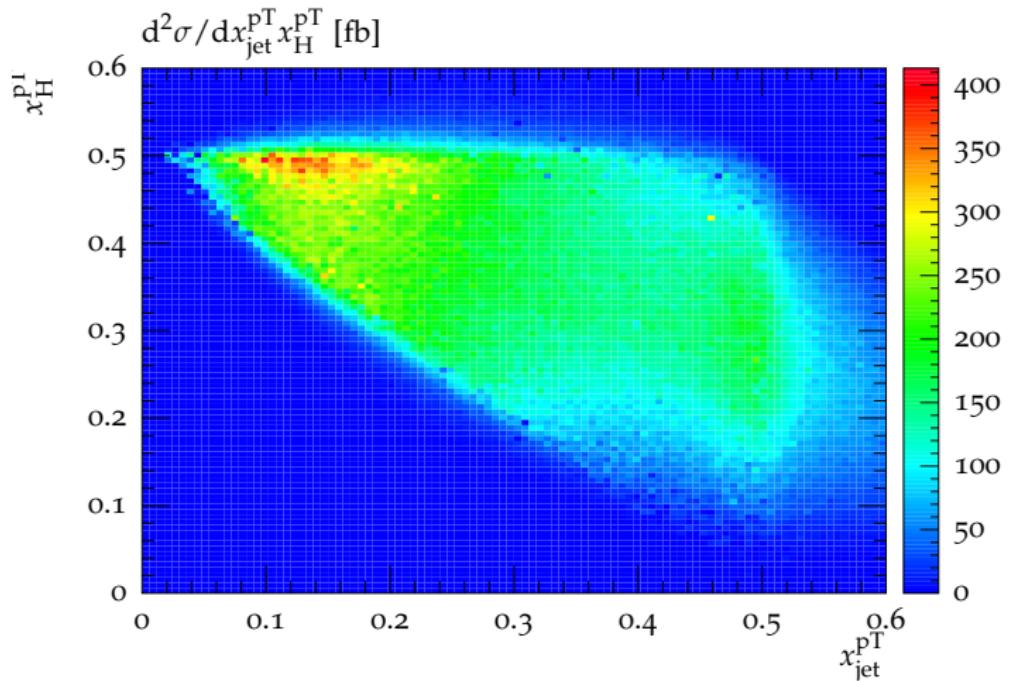
Observable: x_{jet}, x_Z



PS effects on x_{jet}

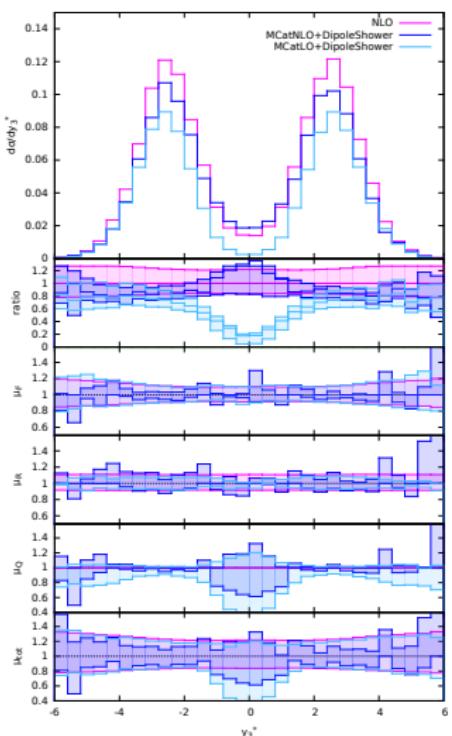


PS effects on x_{jet}



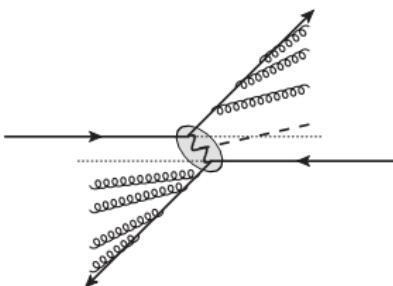
VBF- $W^+ W^-$ + parton shower

Example: VBF- $W^+ W^-$, VBF cuts, central scale: $\mu_0 = p_{j,1}^T$



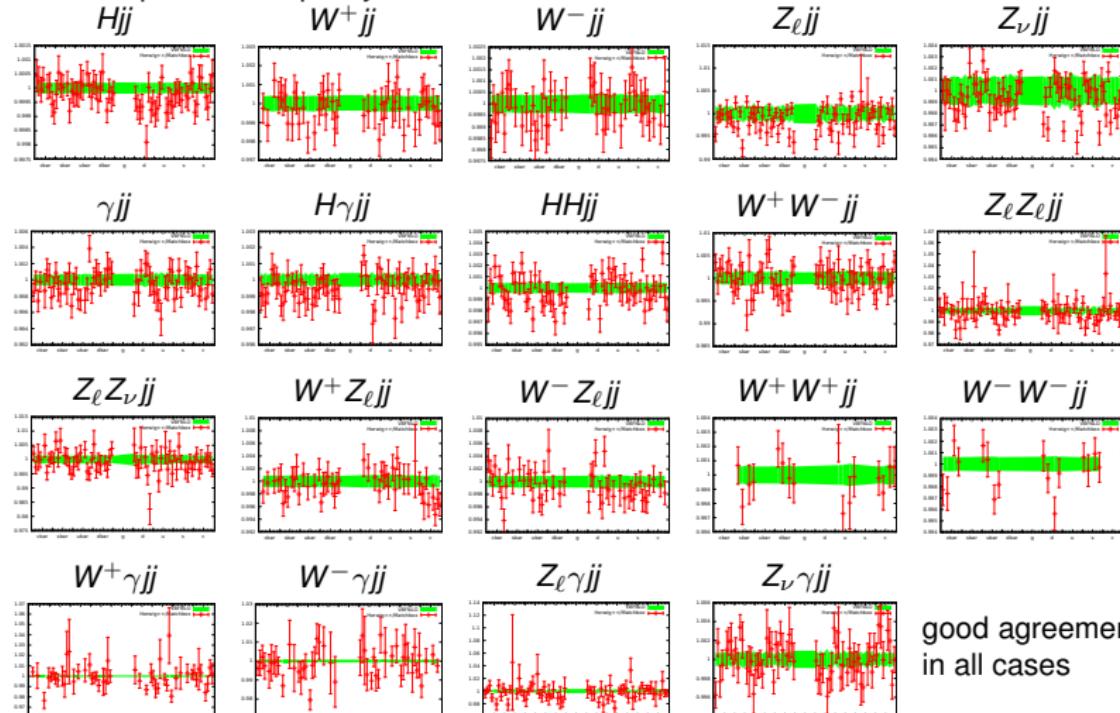
$$y_3^* = y_3 - \frac{y_1 + y_2}{2}$$

- almost no radiation generated in central region by LO+PS
- additional radiation by shower created mainly between jets and beam axis (color connections)
- → central region corrected at NLO by $W^+ W^- jj$ ME
- dipole shower “interpolates” between NLO behavior in central region and shower behavior at small angles



Cross checks

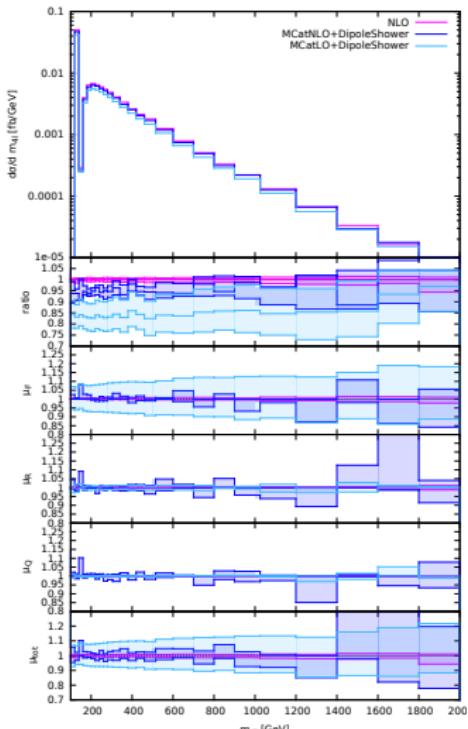
Compare standalone VBFNLO and Herwig7/Matchbox+VBFNLO
VBF/VBS processes split by initial state flavours:



good agreement
in all cases

VBF- $W^+ W^-$ + parton shower

Example: VBF- $W^+ W^-$, VBF cuts, central scale: $\mu_0 = p_{j,1}^T$



Comparison of:

- pure NLO
- NLO+PS (MC@NLO+dipole shower)
- LO+PS (dipole shower)

Panels:

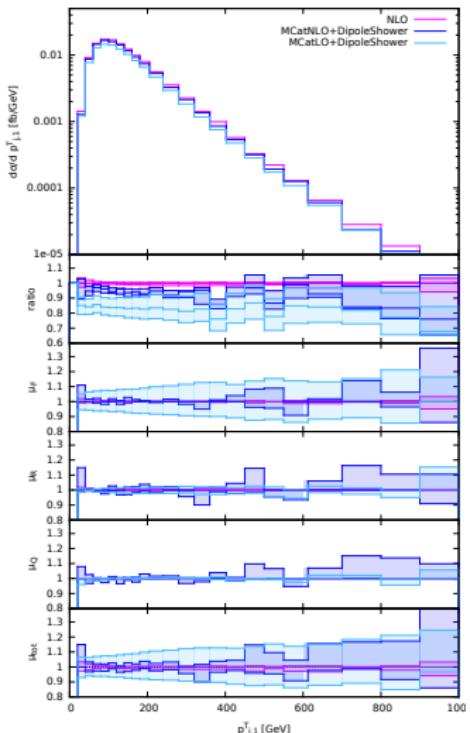
- differential c.s.
- ratio of c.s. and total scale variation
- individual variation of μ_F , μ_R , μ_Q (shower scale)
- total variation $\mu_i/\mu_0 \in [\frac{1}{2}; 2]$ with $\mu_i/\mu_j \in [\frac{1}{2}; 2]$

Inclusion of parton shower:

- smaller c.s. (additional splittings)
- larger uncertainties (additional shower scale unc.)

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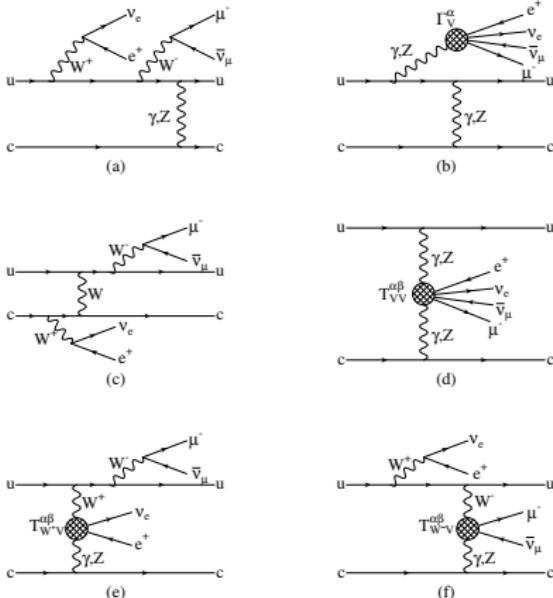
Diboson-VBF production

[Bozzi, Jäger, Oleari, Zeppenfeld (VV); Campanario, Kaiser, Zeppenfeld ($W^\pm \gamma$)
[Denner, Hosekova, Kallweit ($W^+ W^+$)]

- Important process for LHC run-II
- Part of the NLO wish list

[Les Houches 2005]

- background to Higgs searches
 - access to anomalous triple and quartic gauge couplings
 - NLO QCD implementation of
 - all boson combinations
 - leptonic and semi-leptonic decays
 - including off-shell and non-resonant contributions
 - VBF approximation
- **VBFNLO** [Rauch, Zeppenfeld et al.]



NLO plus Parton Shower

Combine advantages of NLO calculations and parton shower

NLO calculation

- normalization correct to NLO
- additional jet at high- p_T accurately described
- theoretical uncertainty reduced

Parton shower

- Sudakov suppression at small p_T
- events at hadron level possible

State of the Art

Implementations for specific VBF processeses

- POWHEG-BOX [Alioli, Hamilton, Nason, Oleari, Re]

currently available VBF implementations:

Z [Jäger, Schneider, Zanderighi]

W^\pm, Z [Schissler, Zeppenfeld]

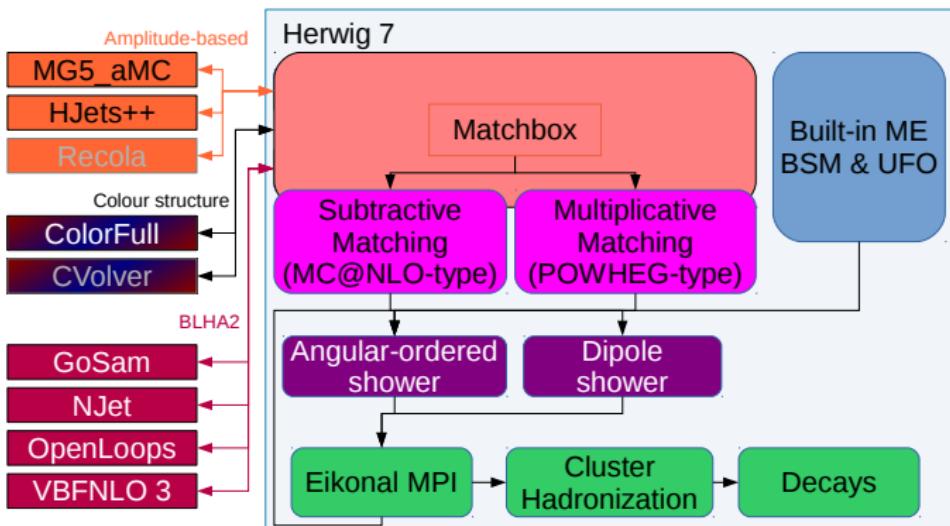
$W^\pm W^\pm, W^\pm W^\mp$ [Jäger, Zanderighi]

ZZ [Jäger, Karlberg, Zanderighi]

- VBF- H with POWHEG method [D'Errico, Richardson]

- HJets++ [Campanario, Figy, Plätzer, Sjödahl]

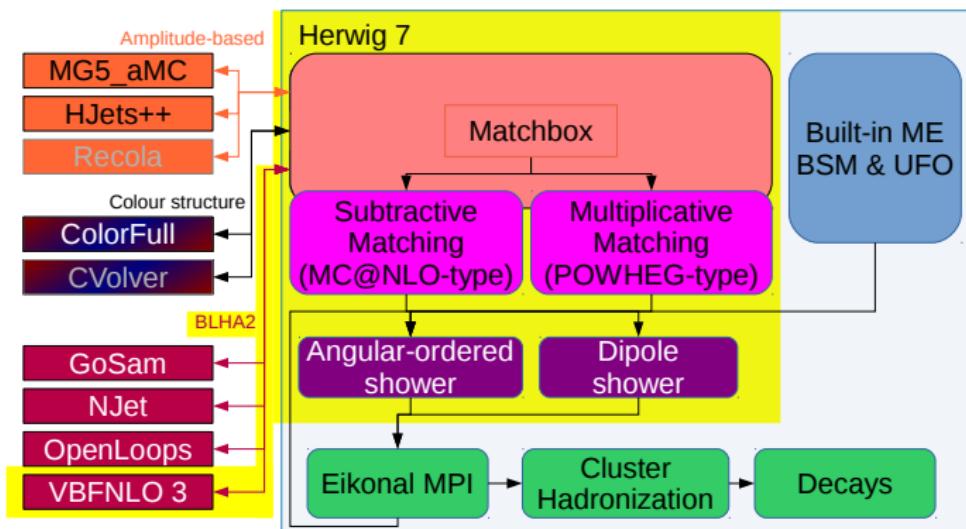
- fully automated matching of NLO to parton showers through Matchbox module
[work led by S. Plätzer with substantial contributions by J. Bellm, A. Wilcock, M. Rauch, C. Reuschle]
- subtractive (MC@NLO-type, \oplus) and multiplicative (POWHEG-type, \otimes) matching
- angular-ordered (QTilde, PS) and dipole (Dipoles) shower
- matrix elements through binary interface, no event files



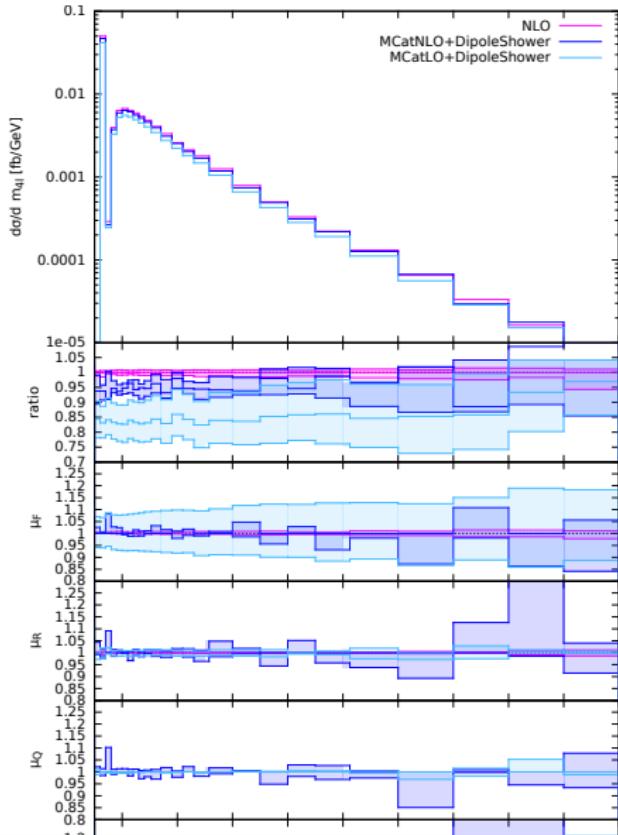
VBFNLO 3 & Herwig 7

- matrix elements from VBFNLO via **BLHA2** interface
- extensions to make accessible
 - phase-space sampling
 - (electroweak) random helicity summation
 - anomalous couplings

[Binoth et al., Alioli et al.]

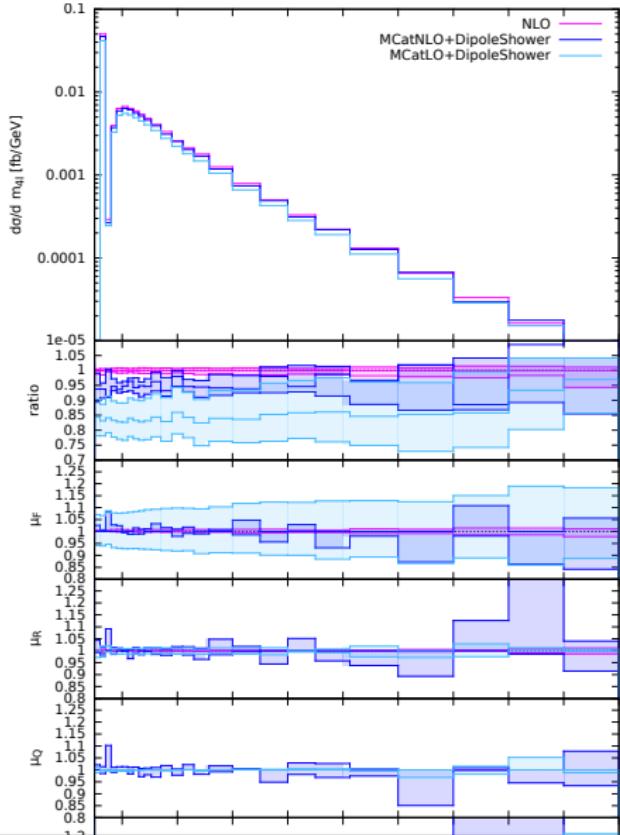


Four-lepton Invariant Mass



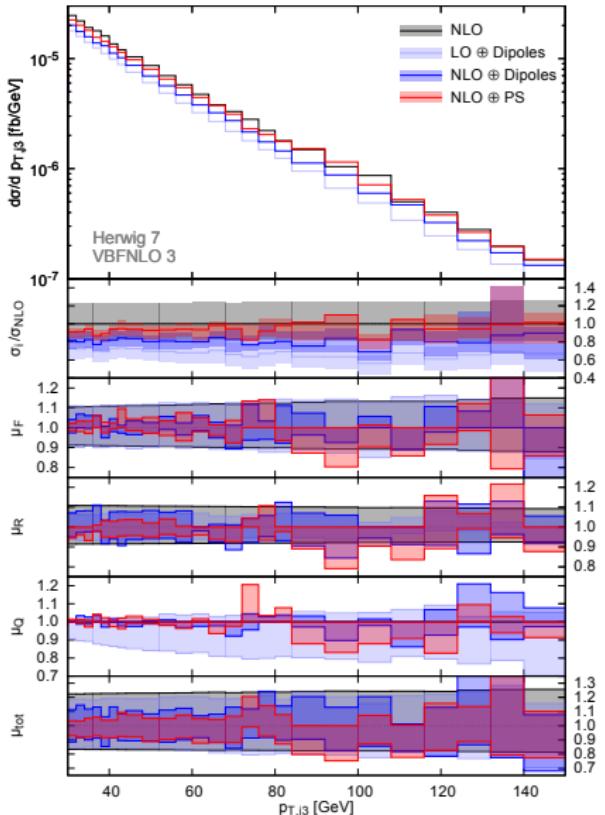
- ← ■ central scale $\mu_0 = p_{T,j1}$
transverse momentum of
leading jet
- ← ■ band: scale variation
 $\{\mu_F, \mu_R, \mu_Q\} / \mu_0 \in [\frac{1}{2}; 2]$
 $\mu_i / \mu_j \in [\frac{1}{2}; 2]$
- ← ■ factorization scale
 $\mu_F \in [\frac{1}{2}; 2]$
- ← ■ renormalization scale
 $\mu_R \in [\frac{1}{2}; 2]$
- ← ■ shower scale
 $\mu_Q \in [\frac{1}{2}; 2]$
- ← ■ all three scales

Four-lepton Invariant Mass



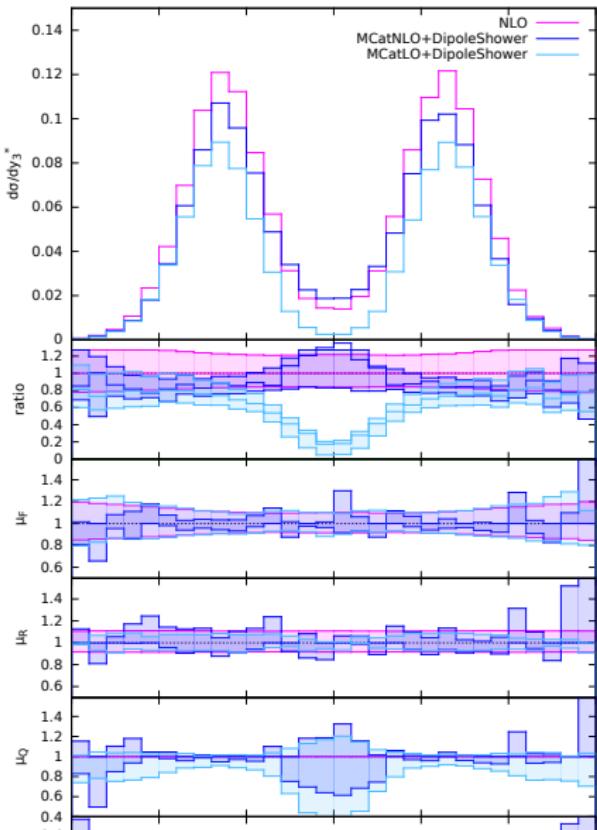
- consistent variation of scales between hard process and parton shower
- large factorization scale dependence for LO result
- larger dependence for down variation of renormalization scale in angular-ordered shower:
 $\text{larger } \alpha_s \rightarrow \text{more splittings} \rightarrow \text{bigger migration effects}$
- small variations from shower-scale changes
- modest remaining overall uncertainty

Transverse Momentum Third Jet



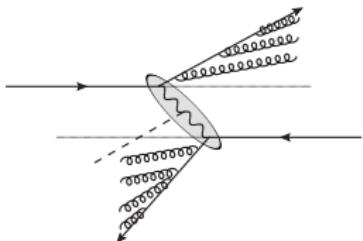
- large scale variation bands for
 - shower scale in LO \oplus Dipoles
→ pure parton-shower effect
 - fact./ren. scale in “NLO”
→ LO accuracy of observable
- reduced for both NLO + parton-shower curves
- still significant remaining uncertainty $\mathcal{O}(10 - 20\%)$
- call for multi-jet merging

Rapidity of third jet



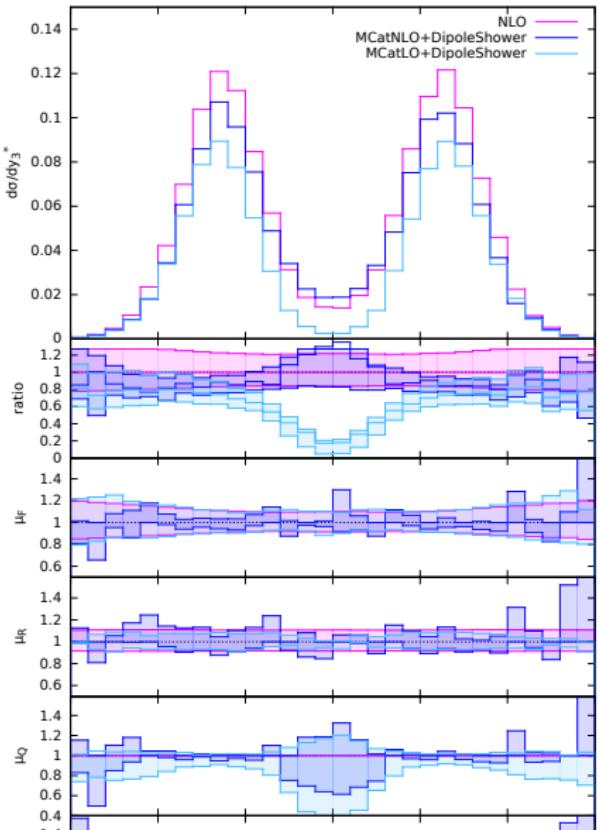
Rapidity of third jet
relative to two tagging jets

$$y_3^* = y_3 - \frac{y_1 + y_2}{2}$$



- VBF colour structure suppresses additional central jet radiation
- colour connection between tagging jet and remnant
- ↔ distinction from QCD-induced production

Rapidity of third jet

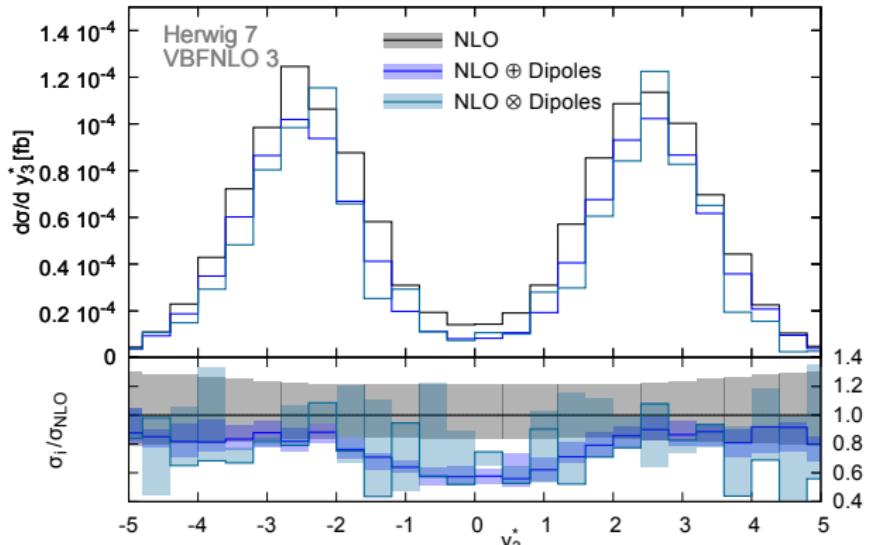


Rapidity of third jet
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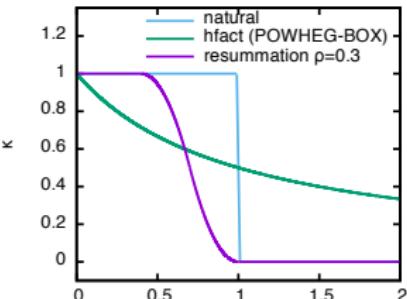
- impact of parton showers (+LO) long unclear
- Herwig predicts very low radiation in central region
- large shower-scale unc.
- stabilised when combining with NLO
- still reduction present
- scale variation bands not overlapping
- only small effects in forward region (mostly global normalization)

Rapidity of third jet – POWHEG

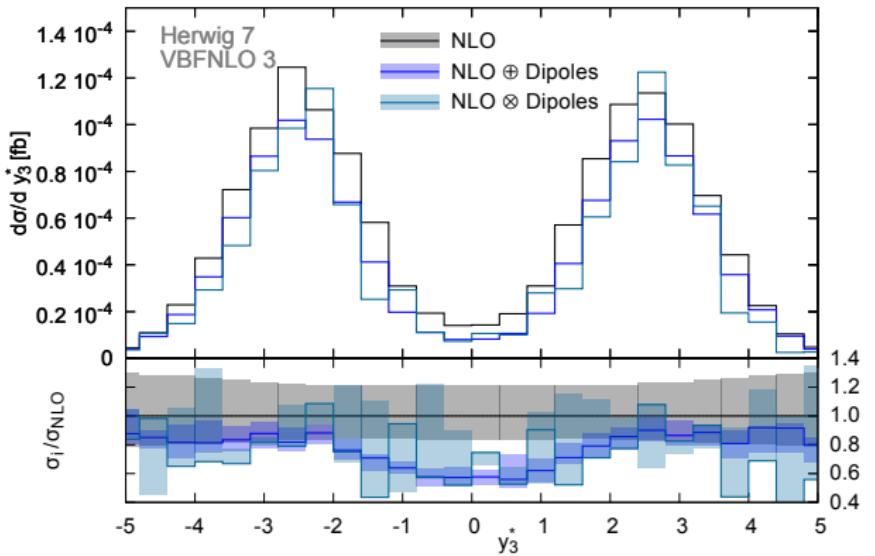


- POWHEG-like (\otimes) using resummation scheme [Plätzer]:

$$\kappa(Q, q; \rho) = \begin{cases} 1 & \text{for } q < (1 - 2\rho)Q \\ 1 - \frac{(1-2\rho-\frac{q}{Q})^2}{2\rho^2} & \text{for } (1 - 2\rho)Q < q < (1 - \rho)Q \\ \frac{(1-\frac{q}{Q})^2}{2\rho^2} & \text{for } (1 - \rho)Q < q < Q \\ 0 & \text{for } q > Q \end{cases}$$



Rapidity of third jet – POWHEG



- band: joint variation $\mu_F = \mu_R = \mu_Q \in [\frac{1}{2}, 2] \mu_0$
- similar predictions from MC@NLO-like (\oplus) and POWHEG-like (\otimes) matching
- also holds for other distributions

Conclusions

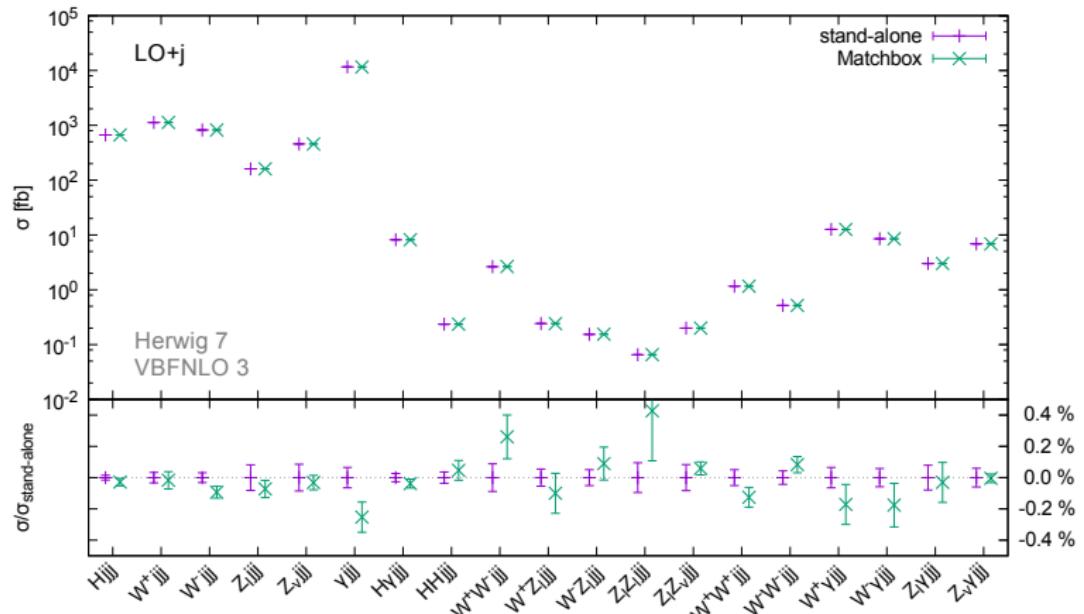
Parton-shower and scale variation effects in
 $W^+ W^- jj$ production via vector-boson-fusion

- important process for the LHC
 - Higgs properties – unitarity in WW scattering
 - testing anomalous (triple and) quartic gauge couplings
- study performed with Herwig 7 & VBFNLO 3
- compatible behavior of both parton showers and matching schemes
- small parton-shower effects for distributions of variables already present at LO
 - mostly reduction of inclusive cross section due to additional jet radiation
- presence of central rapidity gap stabilised
- → multi-jet merging to further reduce uncertainties

Validation

Compare LO+j results between VBFNLO stand-alone run and interfaced to Herwig 7 via Matchbox

(inclusive cuts, with leptonic gauge boson decays into single different-flavour combination, Higgs non-decaying)



→ good agreement

Setup

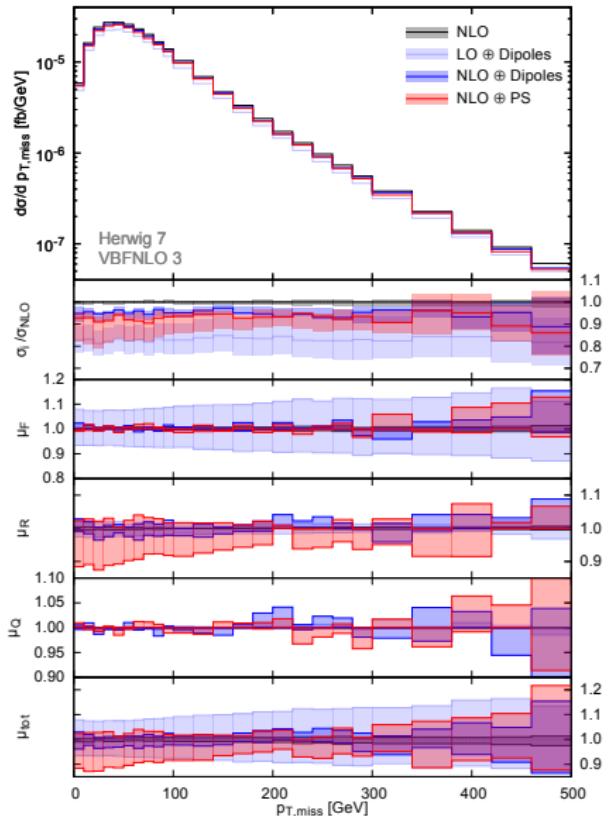
Generation-level cuts:

$p_{T,j} > 20 \text{ GeV},$ anti- k_T jets with $R = 0.4$,	$ y_j < 5.0,$ <i>b</i> -quark veto
$p_{T,\ell} > 15 \text{ GeV},$ $m_{e^+, \mu^-} > 15 \text{ GeV},$	$ y_\ell < 3.0,$
$m_{j1, j2} > 400 \text{ GeV},$	$ y_{j1} - y_{j2} > 3.0$

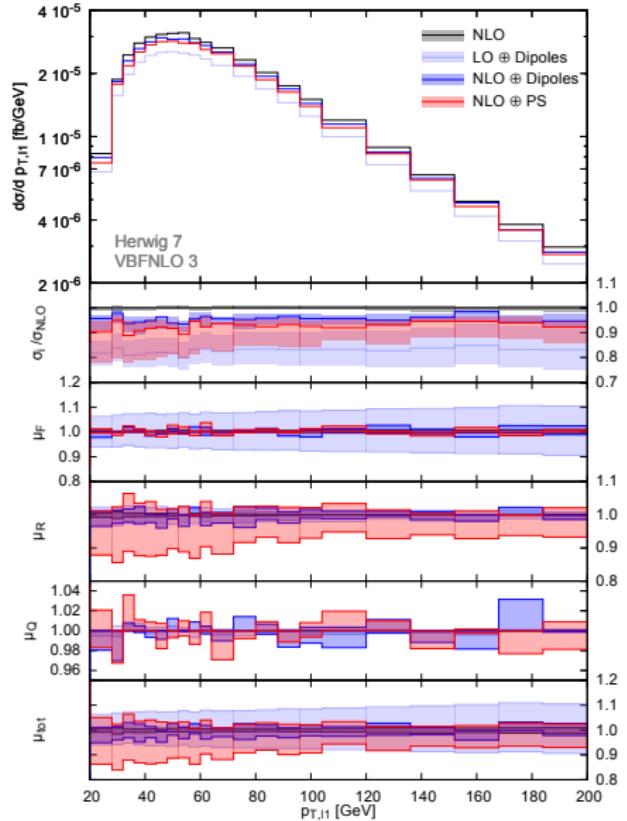
Analysis-level cuts:

$p_{T,j} > 30 \text{ GeV},$ anti- k_T jets with $R = 0.4$,	$ y_j < 4.5,$ <i>b</i> -quark veto
$p_{T,\ell} > 20 \text{ GeV},$ $m_{e^+, \mu^-} > 15 \text{ GeV},$	$ y_\ell < 2.5,$
$m_{j1, j2} > 600 \text{ GeV},$	$ y_{j1} - y_{j2} > 3.6$

Missing Transverse Momentum



Transverse Momentum of Leading Lepton



R Separation of Leading Jet and Leading Lepton

